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**RDECOM**



# Numerical Computations of Dynamic Pitch-Damping Derivatives using Time-Accurate CFD Techniques



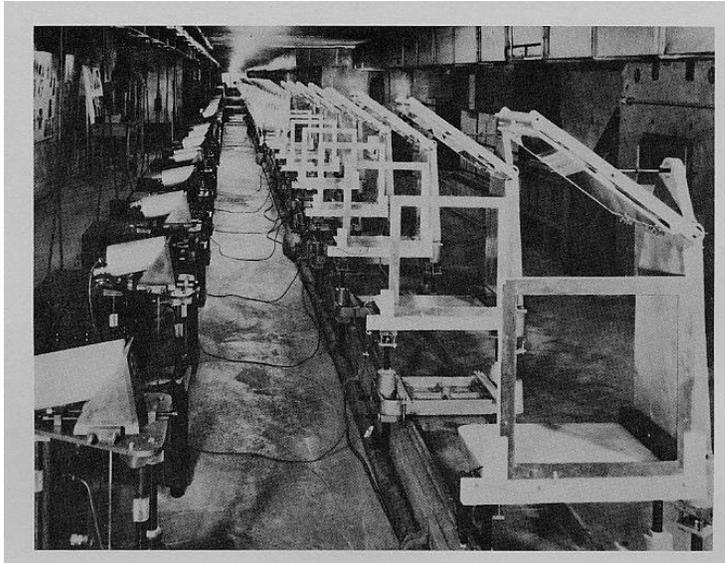
***TECHNOLOGY DRIVEN. WARFIGHTER FOCUSED.***

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Aerodynamics Branch  
U.S. Army Research Laboratory

24th International Symposium on Ballistics  
New Orleans, Louisiana  
22 . 26 September, 2008

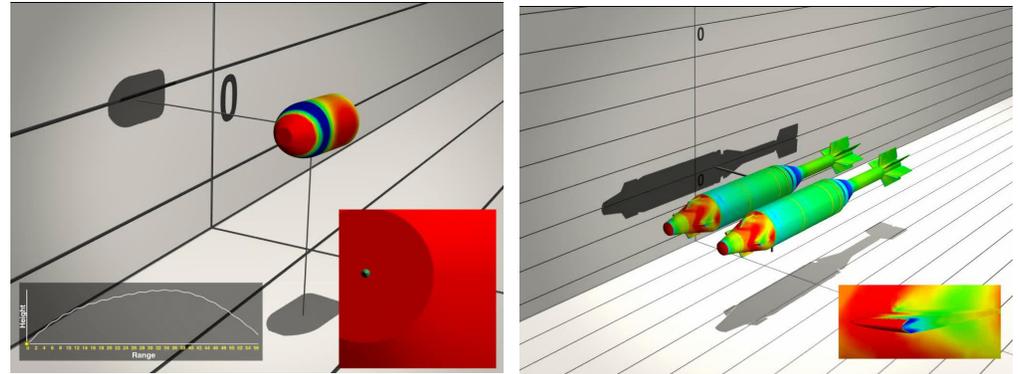
- **Wind Tunnel testing**
- **Actual flight testing**
  - ◆ **Experimental facilities (Aero Range, Transonic Range)**
  - ◆ **Measure the positions and orientations; get Aero from 6-DOF fits**
- **Empirical codes (AP, DATCOM, PRODAS etc.)**
- **Computational Fluid Dynamics (CFD)**
  - ◆ **Steady-State Aerodynamics**
  - ◆ **Unsteady Aerodynamics for Magnus, Roll Damping, Pitch Damping using unsteady rolling and imposed pitching motions (Virtual Wind-Tunnel Method)**
- **CFD and 6-DOF Rigid Body Dynamics Coupling for “Virtual Fly-Outs”**
  - ◆ **Simulate actual free flight (integrated unsteady aero/flight dynamics)**
  - ◆ **Extraction of aerodynamic coefficients (both static and dynamic) from virtual fly-outs**
  - ◆ **Easily extended for computation of dynamic pitch damping moment coefficient using imposed pitching motion– a special case of the virtual fly-out procedure**
  - ◆ **Roll damping and Magnus moment coefficients also are obtained from time-accurate computations of rolling motion, inherently an integral part of the virtual fly-out method**

## Aerodynamics Experimental Facility



- Measures projectile orientation and position only
  - Pitch, Roll, Yaw
  - X, Y, Z
  - 6DOF fit of range data
  - Limited visualization at a few stations
  - Aerodynamic coefficients determined
  - Characterize observed flight dynamics

## Digital Virtual Aerodynamic Range



- Computes entire projectile state
  - Pitch, Roll, Yaw
  - X, Y, Z
  - **Linear velocities**
  - **Pitch, Roll, and Yaw Rates**
  - Unlimited flow visualization
  - Integrated Aerodynamics and Flight Dynamics
  - Predictive capability for new geometries
  - Outputs wake and pressure contours

# Interdisciplinary Computational Technique



## CFD Computational Technique

- 3-D Unsteady Navier-Stokes equations
- Higher order turbulence modeling including hybrid RANS/LES
- Dual Time-Stepping for transient flow computations
  - Two time-steps
  - First (outer) global or physical step – usually set to 1/100<sup>th</sup> of the period of oscillation
  - Second (inner) step – 5 to 10 inner iterations
- Grid Motion and BC:
  - Grid moves and rotates as the projectile moves and rotates
  - Free stream is preserved for arbitrary mesh and arbitrary mesh velocity

## CFD/RBD COUPLING PROCEDURE

- 6-DOF equations solved at every CFD time-step
- CFD provides aerodynamic forces and moments
- 6-DOF provides the response of the body to the forces and moments
- The response is converted to translational and rotational accelerations
- Integrate the accelerations to obtain translational and rotational velocities
- Integrate once more to obtain linear position and angular orientations
- 6-DOF uses quaternions to define angular orientations
- From the dynamic response, grid point locations and velocities are set

## Complete Virtual Fly-Out Procedure

- **STEP 1:**
  - “Steady-state” mode
  - Grid velocities account only for translational motion
  - Initial conditions also include the angular orientations
- **STEP 2:**
  - “Uncoupled” mode (Kinematics)
  - Add rotational component in X (spin, p)
  - Compute for a few spin cycles until solution converges
- **STEP 3:**
  - “Coupled mode”
  - Add the other rotational components (q and r)
  - Full dynamic calculations

## Time-Accurate CFD Procedure for Dynamic Derivatives

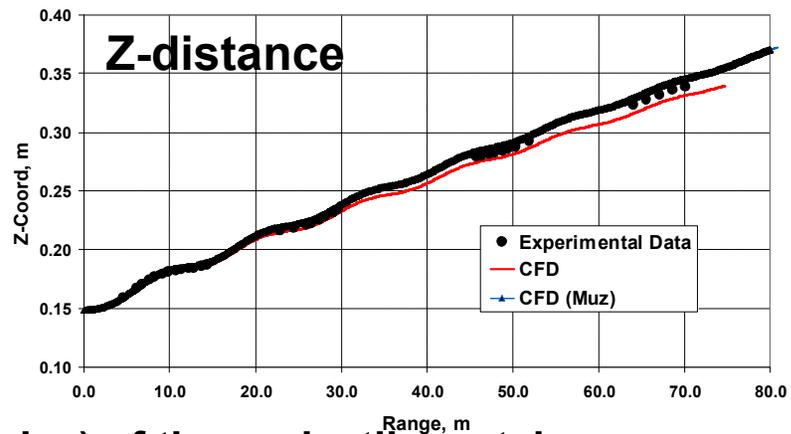
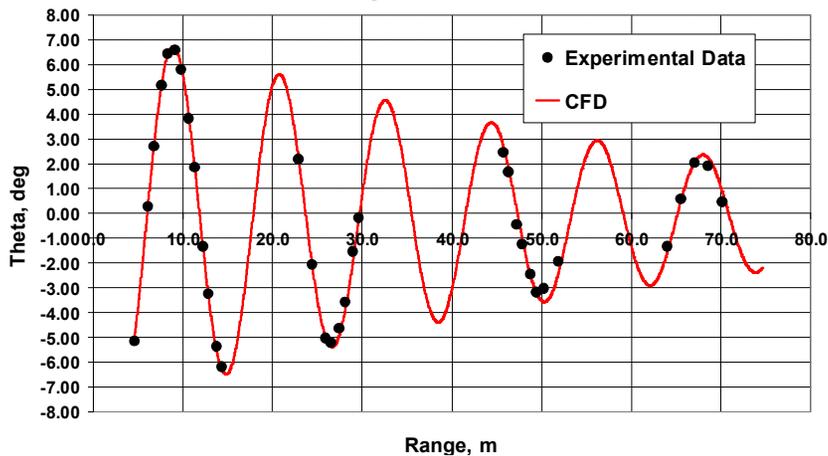
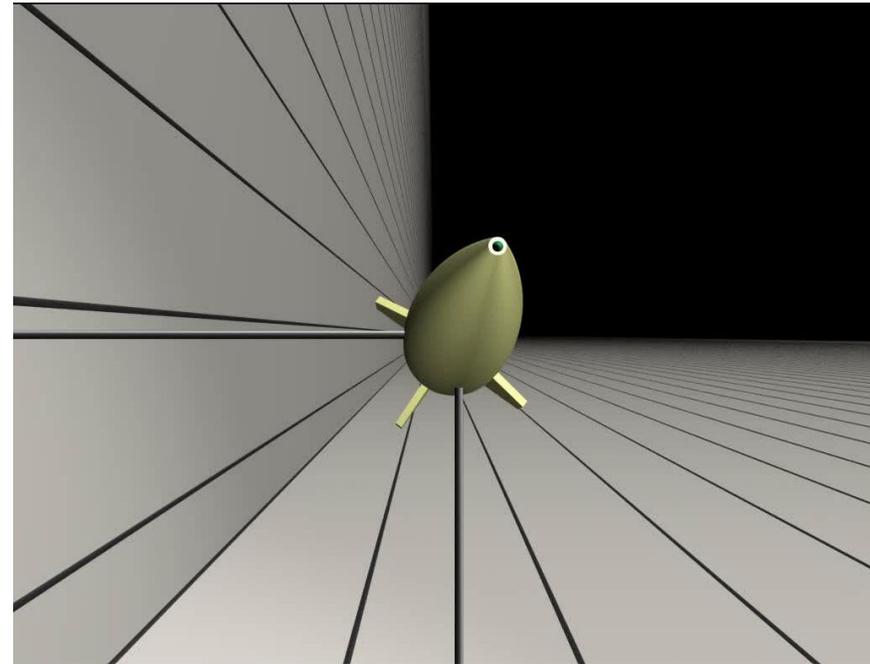
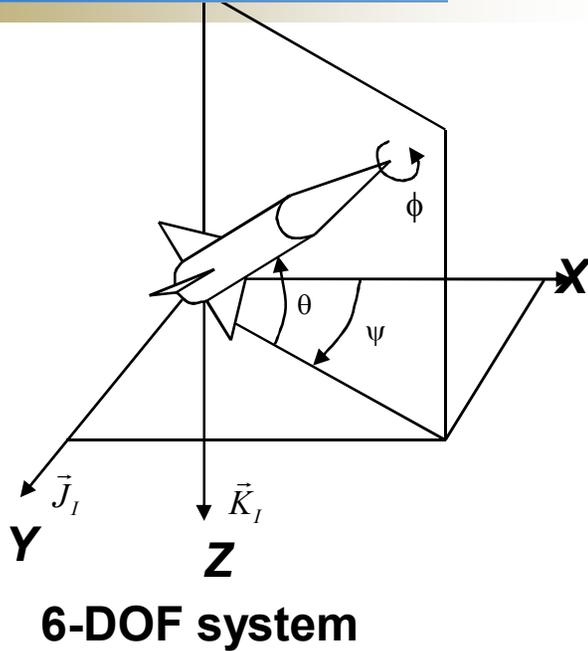
- **STEP 1:**
  - “Steady-state” mode
  - No translation motion
- **STEP 2:**
  - “Uncoupled” mode (Rolling Motion)
  - Add rotational component (spin, p)
  - Compute for a few spin cycles until solution converges
- **STEP 2:**
  - “Uncoupled” mode (Pitching Motion)
  - Add the other rotational component (q)  
i.e. impose pitching motion
  - Pitching motion can be sinusoidal

# Ballistic Fly-out of a Finned Projectile

## Initial Velocity, Mach = 3 (Supersonic)

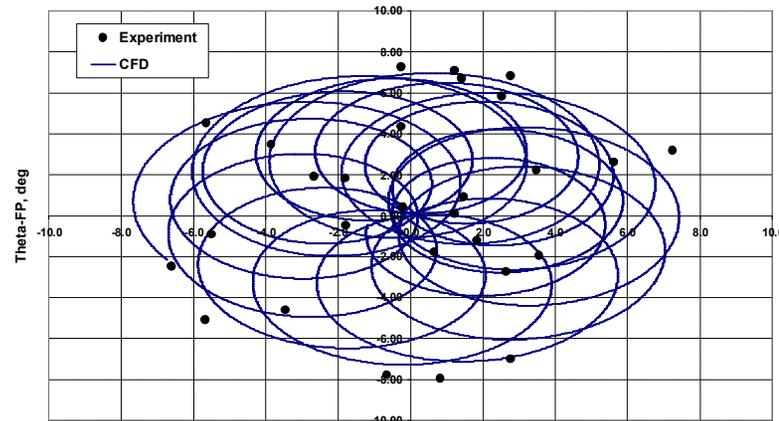
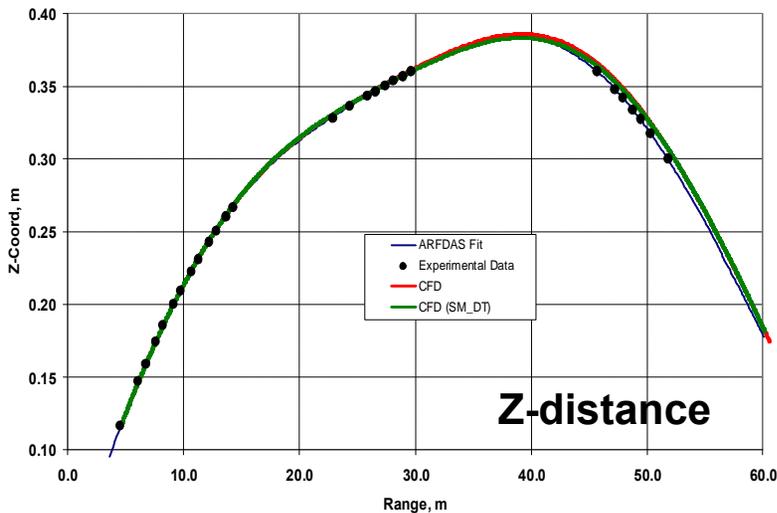
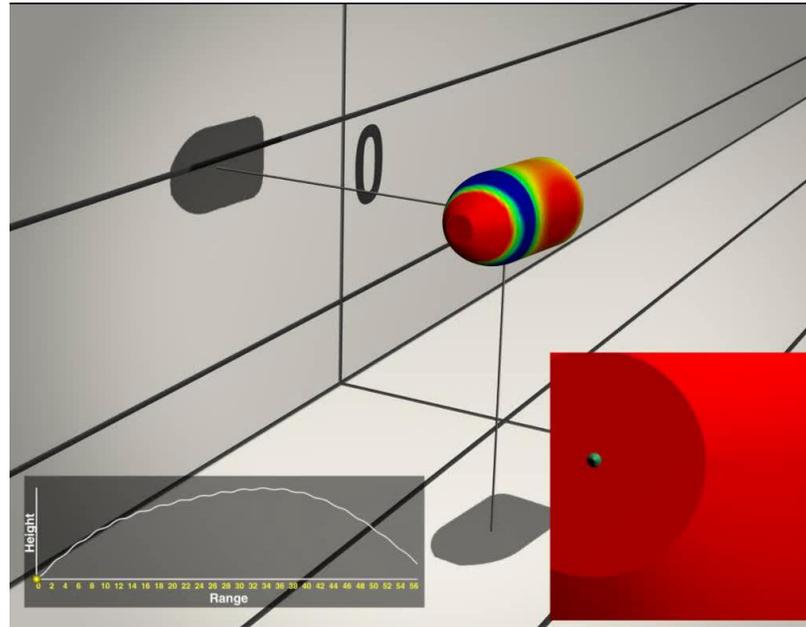
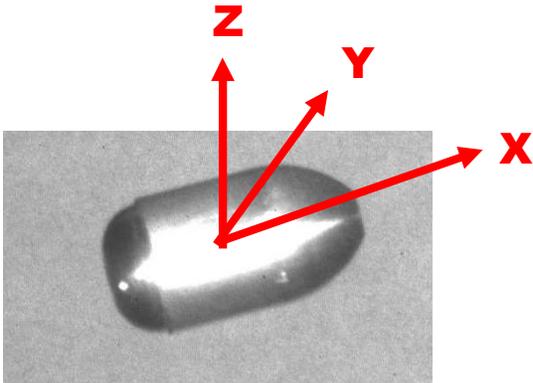


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Computed positions and orientations (Euler angles) of the projectile match very well with the data measured in actual free flight tests. **TECHNOLOGY DRIVEN. WARFIGHTER FOCUSED.**

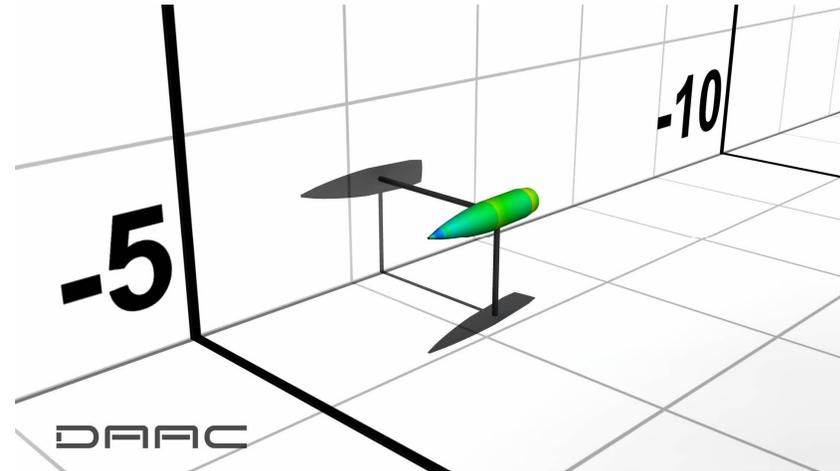
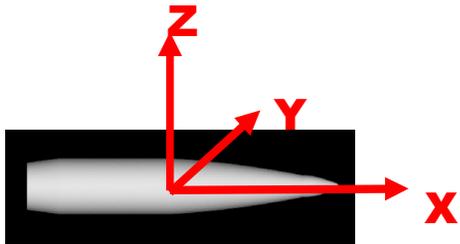
# Another Example: Spinning Projectile Initial Mach = 0.4 (Subsonic Flight)



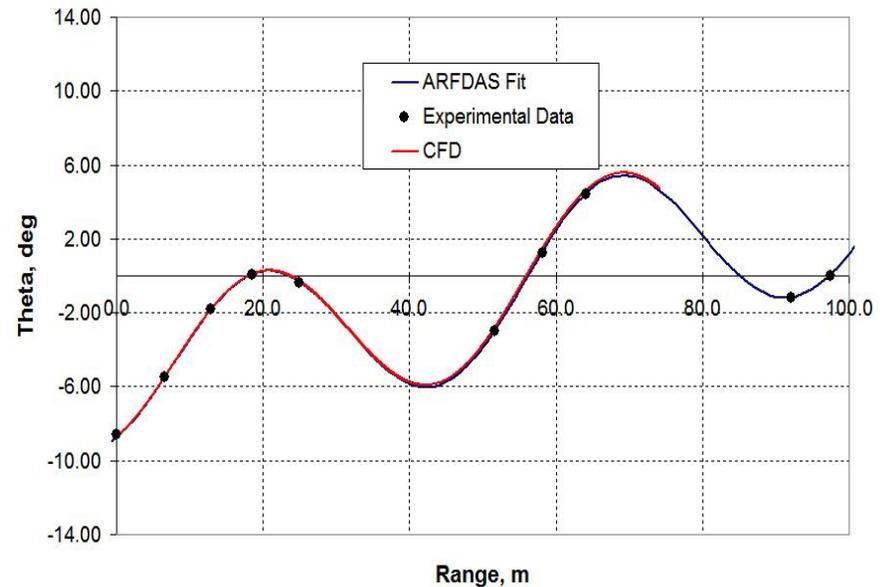
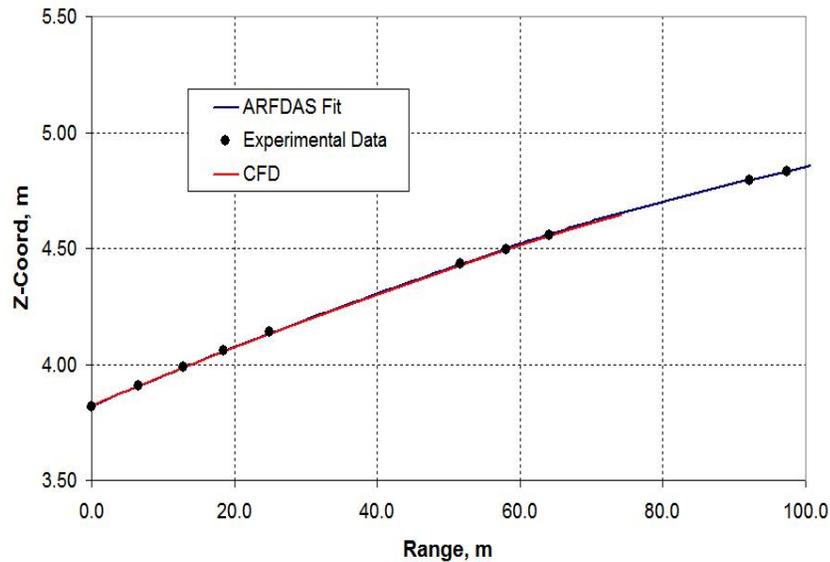
**Virtual fly-out technique computes the trajectory of an in-flight spinning projectile; computed results match well with the flight test data**

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# Virtual Fly-Out of a Spinning Projectile Initial Mach = 1.1 (Transonic Flight)



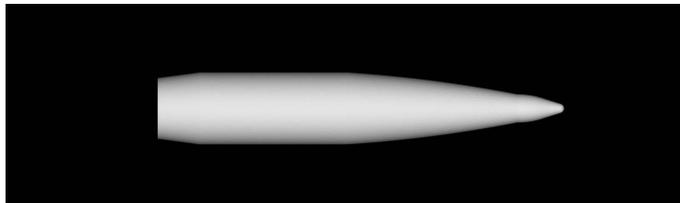
Z-distance



**Virtual fly-out technique computes the trajectory of an in-flight spinning projectile; computed results match well with the flight test data.**

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## **Extraction of Aerodynamic Coefficients from Virtual Fly-Out Simulations**



### **Spinning Projectile**

# raction of All Aerodynamic Coefficients



## Pitch-Damping Moment Coeff.

**Virtual fly-outs simulations require only the total aerodynamic forces and moments to fly the projectile.**

**How do we extract the aerodynamic force and moment coefficients from the virtual fly-out simulations? How good are they?**

### Different Approaches:

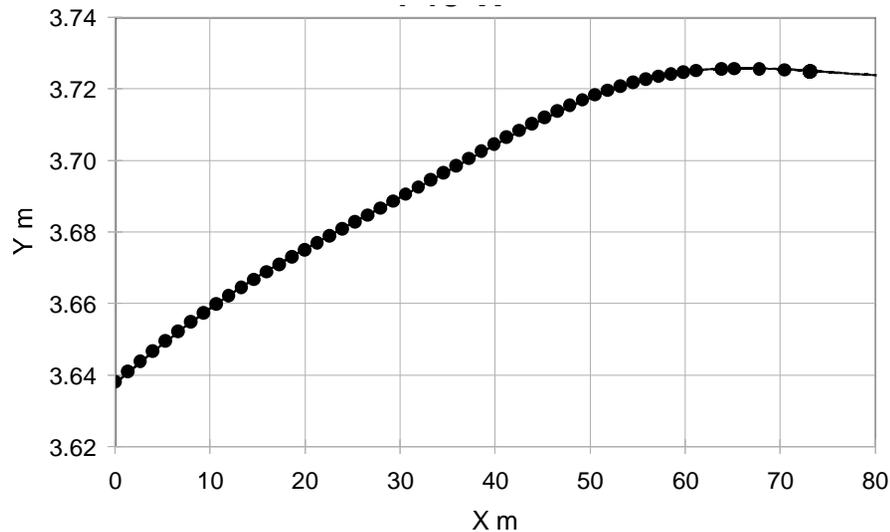
1. Aerodynamic coefficients extracted from CFD/RBD virtual fly-out solutions using range reduction software (ARFDAS, for example).
2. PACE - Simple fitting procedure that require a set of short time-histories (virtual fly-outs) at different Mach numbers.

# ARFDAS Fit of CFD Generated data Initial M = 1.1

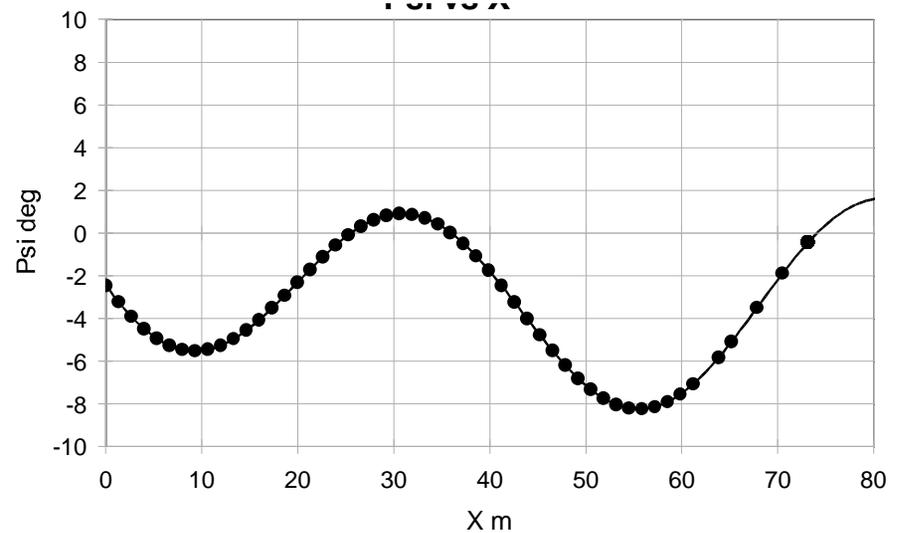


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1. Aerodynamic coefficients extracted from CFD using range reduction software, ARFDAS using the virtual fly-out solutions
2. Position (x,y,z) and the orientation (three Euler angles) of the projectile, obtained from the virtual fly-out simulations were provided as input to ARFDAS. **Same procedure is used for actual flight measured data.**



**Y-distance**



**Euler roll angle**

# Extracted force and moment coefficients (static and dynamic) from virtual fly-out simulation

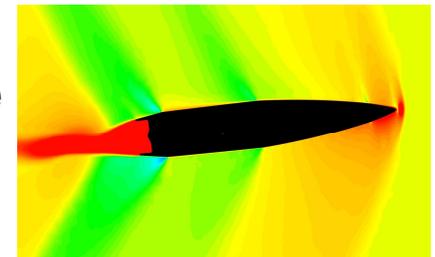


Data Source	Zero-Yaw Axial Force Coeff., $C_{D_0}$	Normal Force Coeff. Deriv., $C_{N_\alpha}$	Pitching Moment Coeff. Deriv., $C_{m_\alpha}$	Pitch Damping Moment Coeff., $C_{m_q}$	Magnus moment Coeff. Deriv., $C_{np_\alpha}$	Roll Damping Moment Coeff., $C_{lp}$
Spark Range	0.359	2.081	4.209	-25.3	1.05	-0.019
CFD	0.335	2.362	4.283	-22.9	0.93	-0.019

**Aerodynamic coefficients extracted from the virtual fly-out method matches very well with those obtained from free flight tests.**



**Validate using separate unsteady CFD (Virtual wind tunnel method)**



# Pitch Damping Moment



$$\text{Pitch Damping Moment} = \frac{1}{2} \rho V^2 S d \left( \frac{q d}{2V} \right) (C_{m_q} + C_{m_{\dot{\alpha}}})$$

Pitching motion imposed:

$$\alpha = \alpha_m + \alpha_0 \sin(\omega t)$$

Here,

$C_{m_q}$  = pitch damping moment coefficient due to  $q$

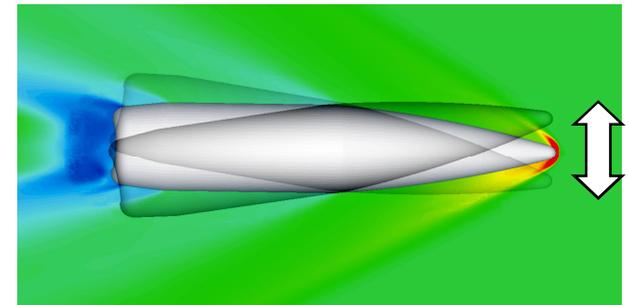
$C_{m_{\dot{\alpha}}}$  = pitch damping moment coefficient due to  $\dot{\alpha}$

$\alpha$  = instantaneous angle of attack

$\alpha_m$  = mean angle of attack

$\alpha_0$  = pitch amplitude

$\omega$  = pitch frequency, related to reduced frequency ( $k = qd/2V$ )

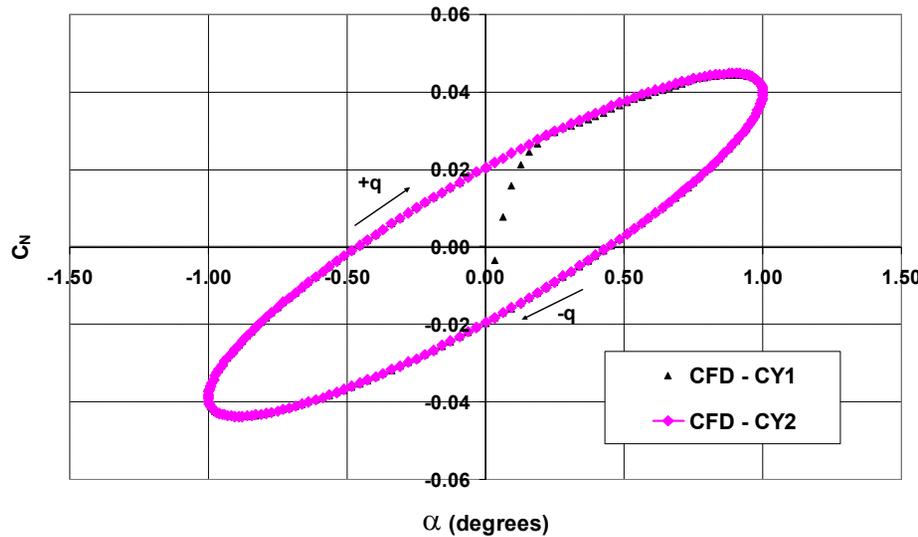


**Virtual wind tunnel method  
(Imposed pitching motion)**

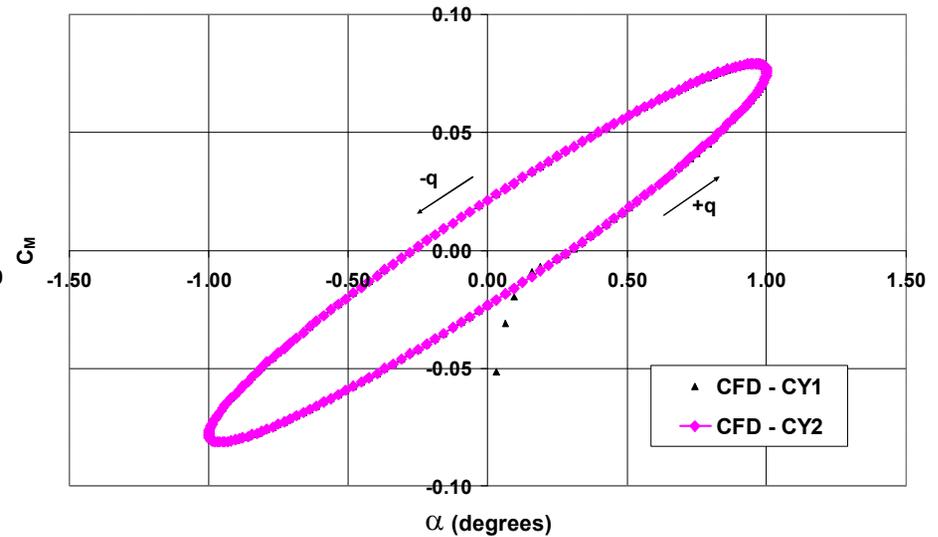
# Time-Histories of Normal Force and Pitching Moment coefficients



Mach = 1.1  
 $\alpha_0 = 1.0, k = 0.1$



Normal force



Pitching moment

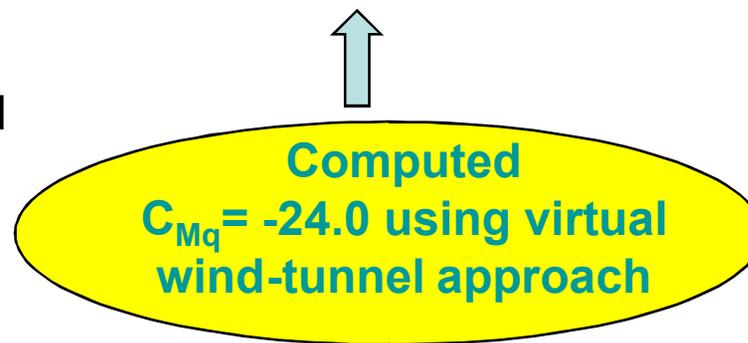
Pitch damping moment is obtained directly from the time-history plot of the pitching moment coefficient resulting from the imposed pitching motion.

# Extracted force and moment coefficients from virtual fly-out

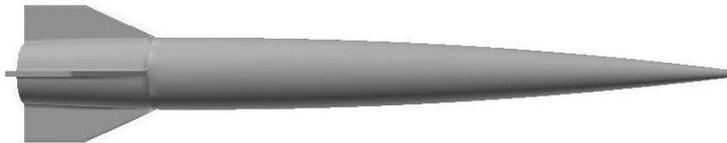


Data Source	Zero-Yaw Axial Force Coeff., $C_{D_0}$	Normal Force Coeff. Deriv., $C_{N_\alpha}$	Pitching Moment Coeff. Deriv., $C_{m_\alpha}$	Pitch Damping Moment Coeff., $C_{m_q}$	Magnus moment Coeff. Deriv., $C_{np_\alpha}$	Roll Damping Moment Coeff., $C_{lp}$
Spark Range	0.359	2.081	4.209	-25.3	1.05	-0.019
CFD	0.335	2.362	4.283	-22.9	0.93	-0.019

Pitch damping moment extracted from the virtual fly-out method matches very well with that obtained by a separate unsteady CFD approach with prescribed pitching motion.



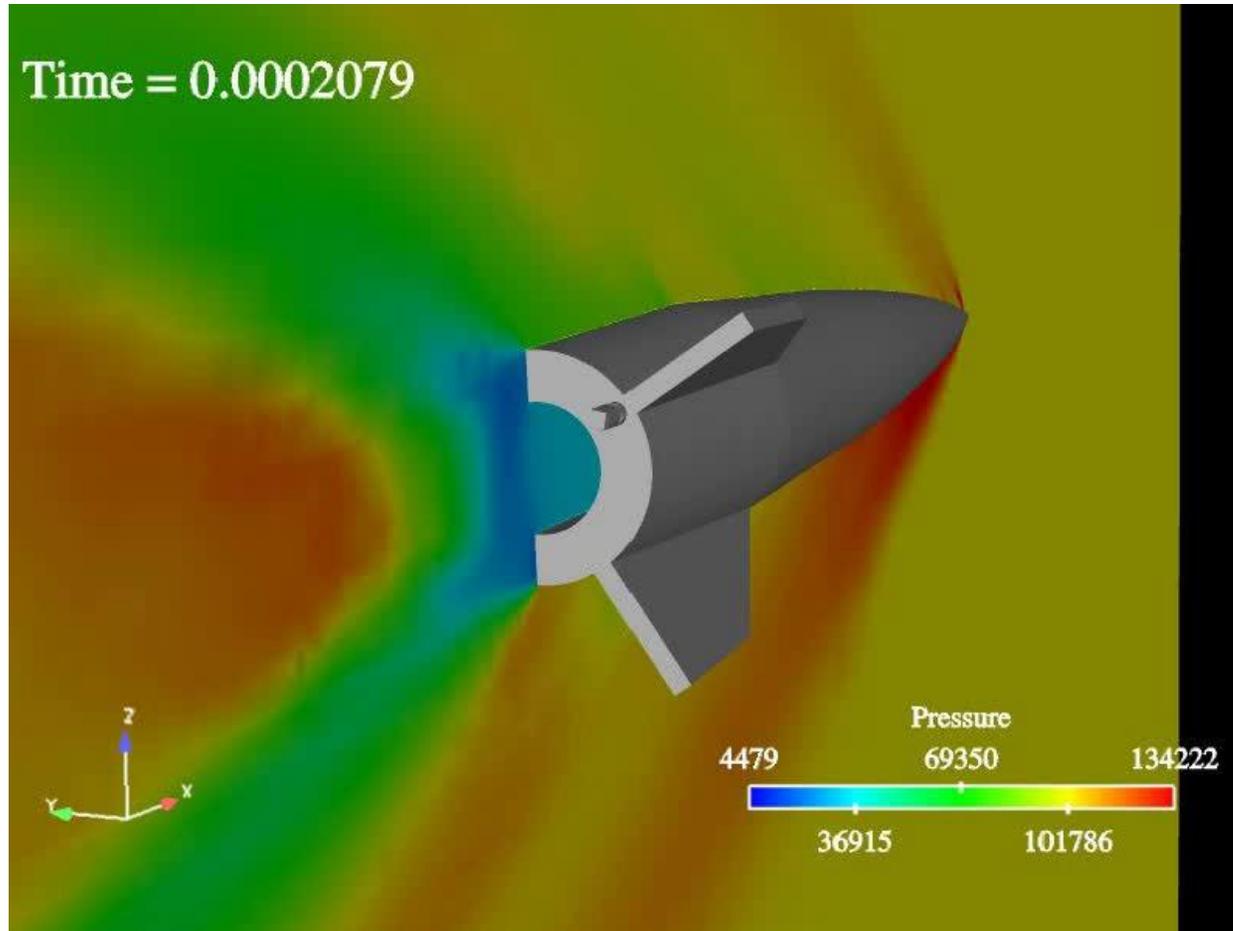
## **Extraction of Aerodynamic Coefficients from Virtual Fly-Out Simulations**



**Finned Projectile**

# Final Fly-out of a Finned Projectile

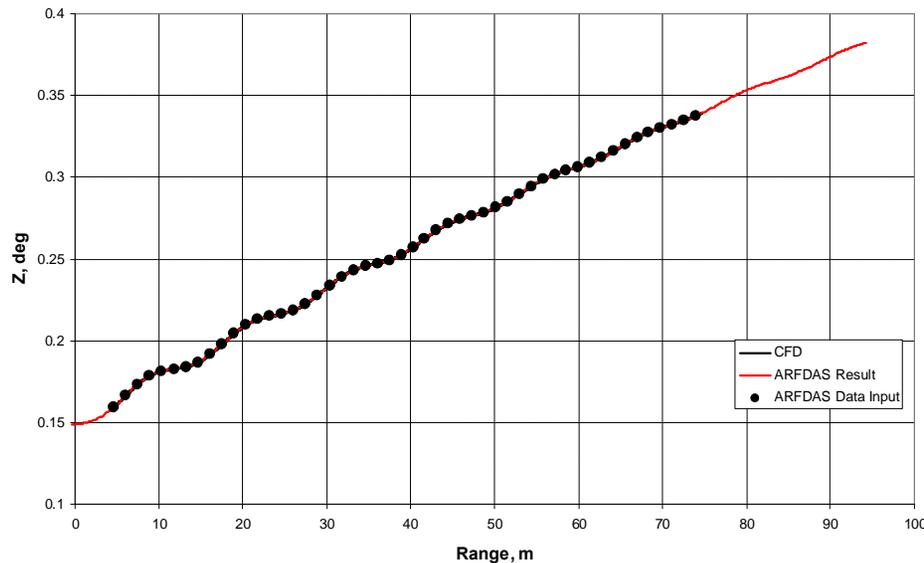
## Final Velocity, Mach = 3 (Supersonic)



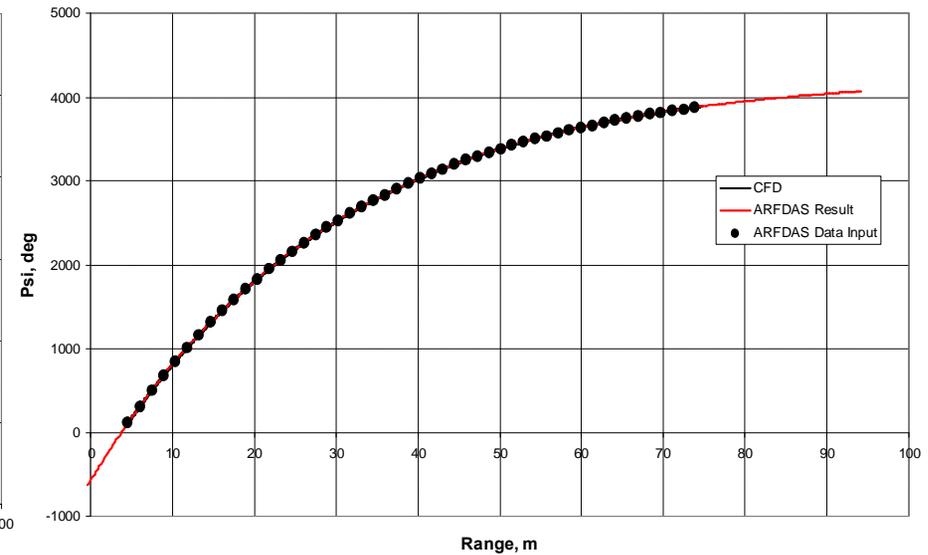
# ARFDAS Fit of CFD Generated data Initial M = 3.0



1. Aerodynamic coefficients extracted from CFD using range reduction software, ARFDAS using the virtual fly-out solutions
2. Position (x,y,z) and the orientation (three Euler angles) of the projectile, obtained from the virtual fly-out simulations, were provided as input to ARFDAS. **Same procedure is used for actual flight measured data.**



Z-distance



Euler roll angle

# Extracted Aerodynamic Coefficients from Virtual Fly-Out Simulation



Data Source	Mach No.	$C_{Xo}$	$C_{Na}$	$C_{ma}$	$C_{mq}$	$C_{lp}$
Spark Range	3.0	0.221	5.83	-12.60	-196	-2.71
CFD	3.0	0.253	5.88	-12.46	-172	-3.24



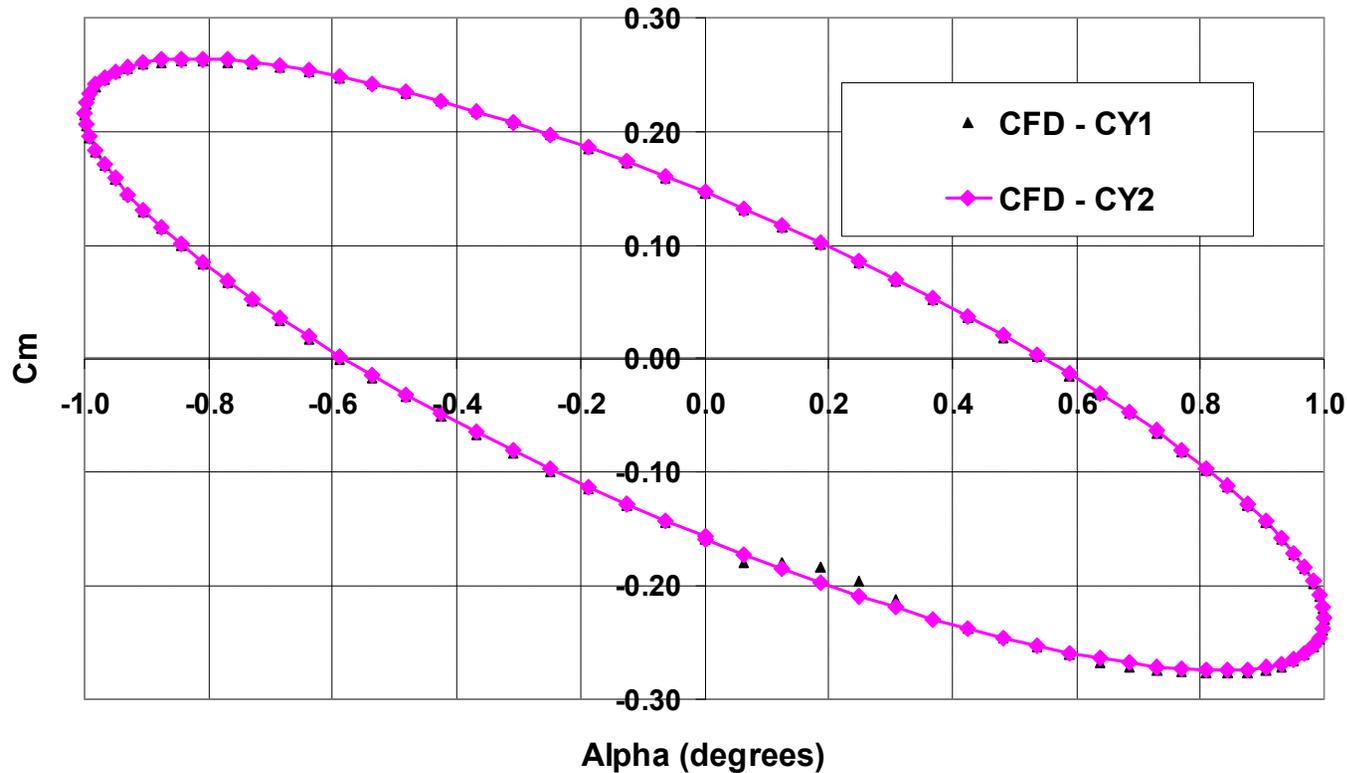
**Pitch-Damping Moment Coefficient**

# Time-history of the Pitching Moment with Angle of Attack



Mach = 3.0

Virtual Wind Tunnel Method

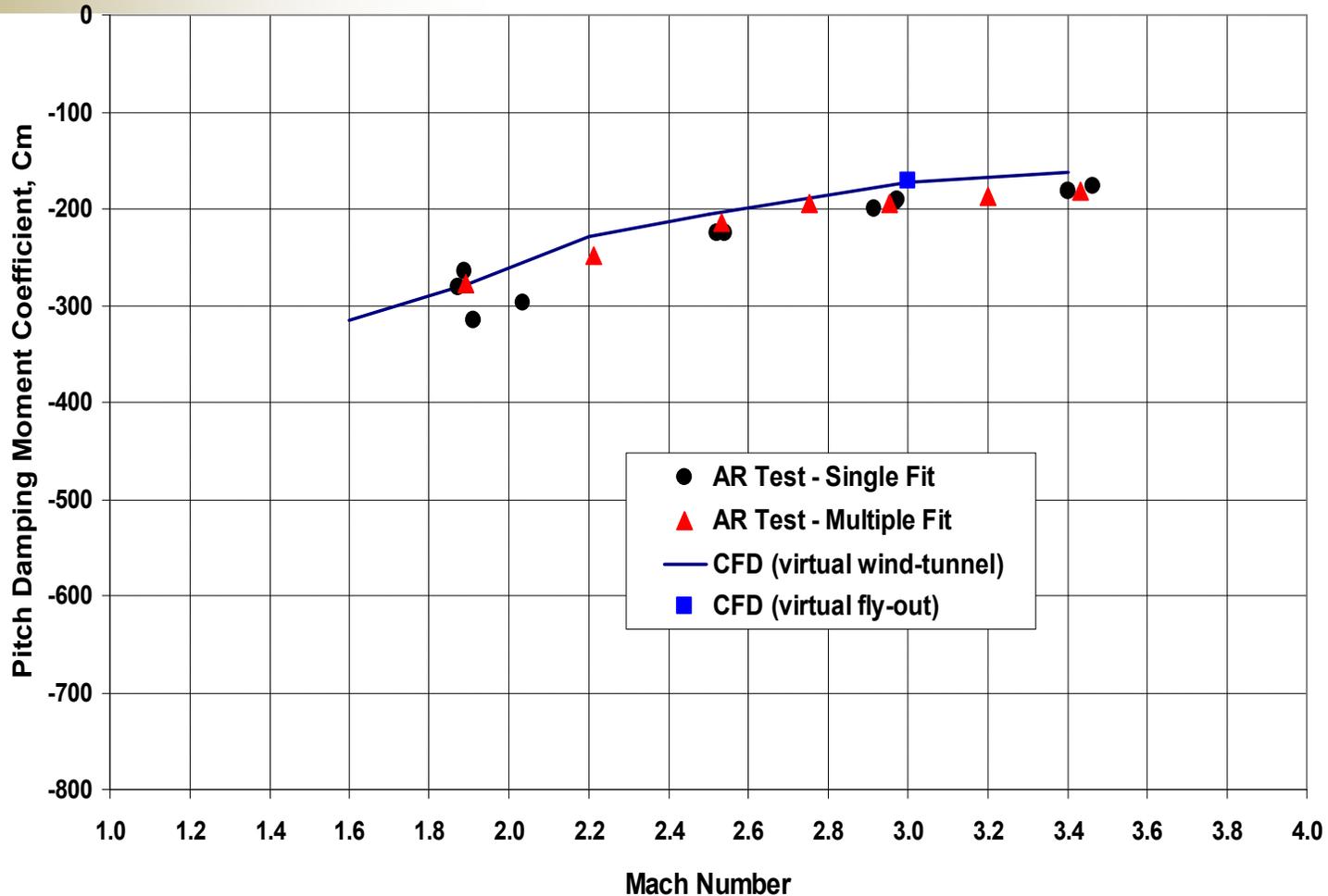


Pitch damping moment is obtained directly from the time-history plot of the pitching moment coefficient resulting from the imposed pitching motion.

# Computed Pitch-Damping Moment Coefficient as a function of Mach number



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- Computed pitch-damping moment coefficients match fairly well with the data obtained from free flight tests.
- Almost identical prediction by both virtual fly-out and virtual wind-tunnel techniques.

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## Concluding Remarks



- **Multidisciplinary CFD/Rigid Body Dynamics Coupling for Virtual Fly-Outs**
  - **Integrated unsteady aerodynamics and flight dynamics**
  - **All aerodynamic coefficients (static and dynamic) can be easily extracted from the same virtual fly-out solution**
  - **Technique easily reduces to the virtual wind tunnel approach for computation of dynamic pitch damping derivatives**
- **Aerodynamic coefficients extracted (both static and dynamic) match fairly well with the data obtained from free flight tests**
- **Both virtual fly-out and virtual wind-tunnel methods essentially predict the same dynamic pitch damping moment coefficients**