

# **real time fire control solution for individual and crew-served direct firing infantry weapons - algorithm and implementation**

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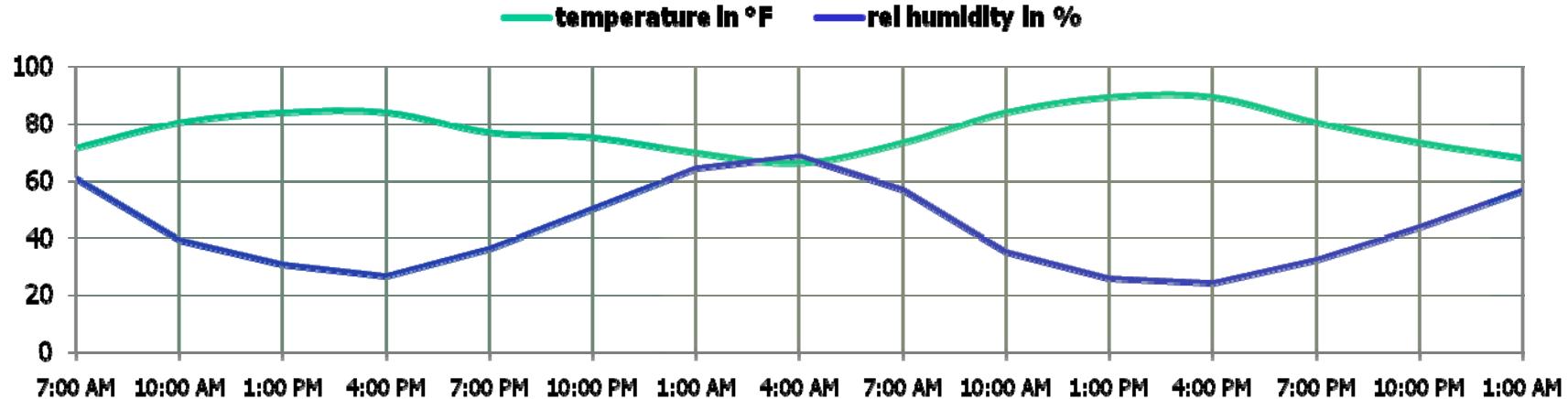
target range: 1500m

Mazár-e-Sharif

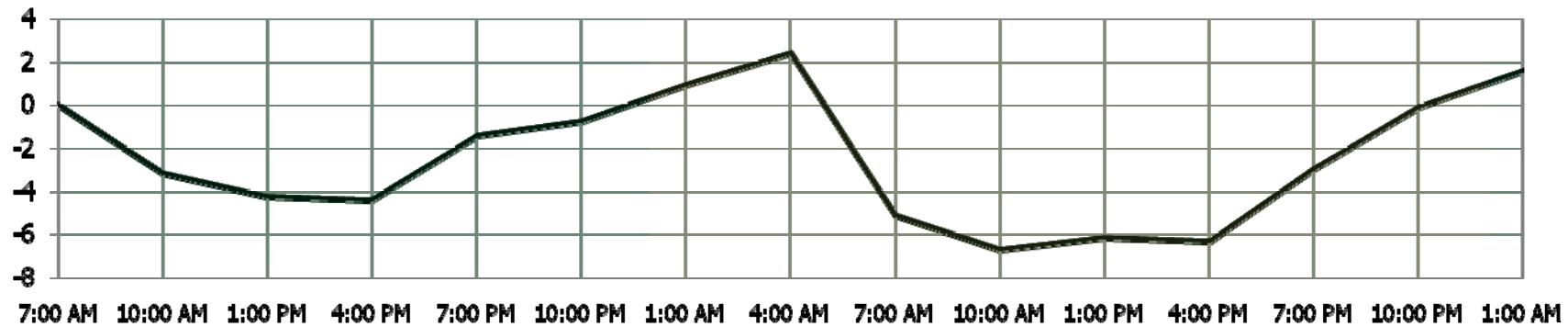
08 0730 D may 08

rH: 60% T: 71°F





### click adjustments due to weather conditions

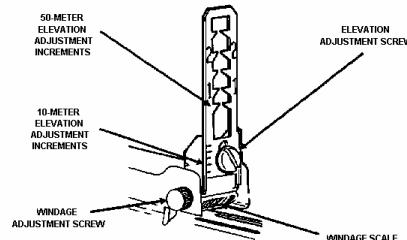
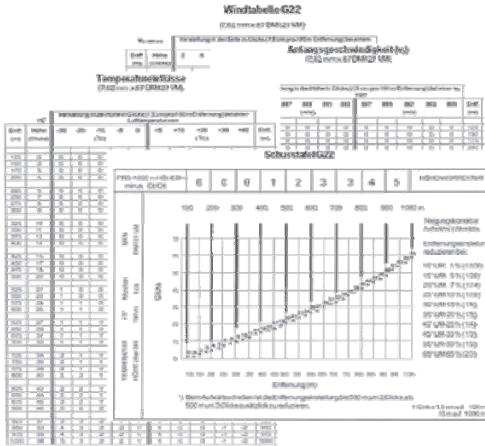


target range: 1500m

Mazár-e-Sharif

- 1. Status quo**
- 2. Requirements**
- 3. Theoretical Approach**
- 4. Algorithm**
- 5. Testing and Accuracy**
- 6. Performance**
- 7. Implementation**
- 8. Conclusions**

# Status Quo



**LRF**



**DMC**



**GPS**



**thermal  
sight**



**video sight**

# Requirements

<i>requirement</i>	<i>fulfilled</i>
<i>range- and crosswind</i>	
<i>arbitrary angle of site</i>	
<i>muzzle velocity</i>	
<i>coriolis force</i>	
<i>magnus force</i>	
<i>multiple ammunitions</i>	
<i>height dependent air temperature</i>	
<i>height dependent air pressure</i>	
<i>user-defined targeting sights</i>	
<i>time fuze capability</i>	

# Approach

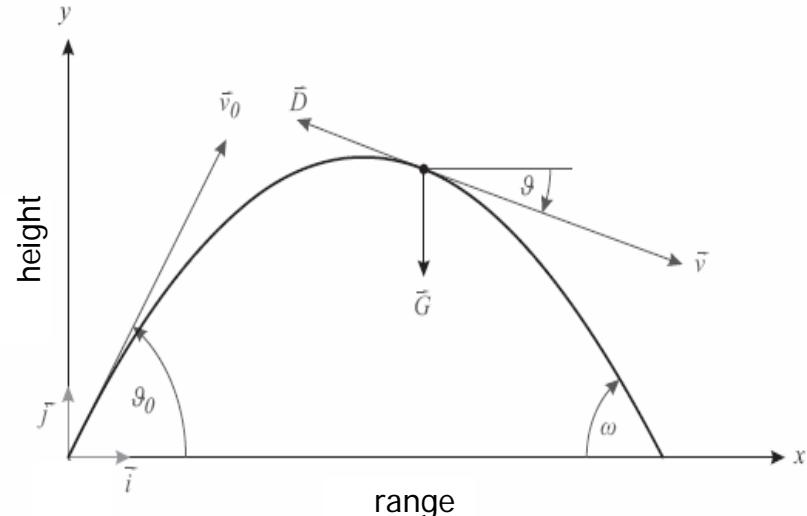
*Point Mass Trajectory Model*

*only drag and gravity acting on projectile*

*adding flat fire assumptions*

*Adding generalized power drag law*

*analytically solvable set of differential equations of motion*



$$\begin{aligned}
 \dot{x} &= v \cos(\vartheta), & x(t_0) &= 0; \\
 \dot{y} &= v \sin(\vartheta), & y(t_0) &= 0; \\
 \dot{v} &= -\frac{D}{m} - g \sin(\vartheta), & v(t_0) &= v_0; \\
 \dot{\vartheta} &= -\frac{g}{v} \cos(\vartheta), & \vartheta(t_0) &= \vartheta_0.
 \end{aligned}$$

# Approach

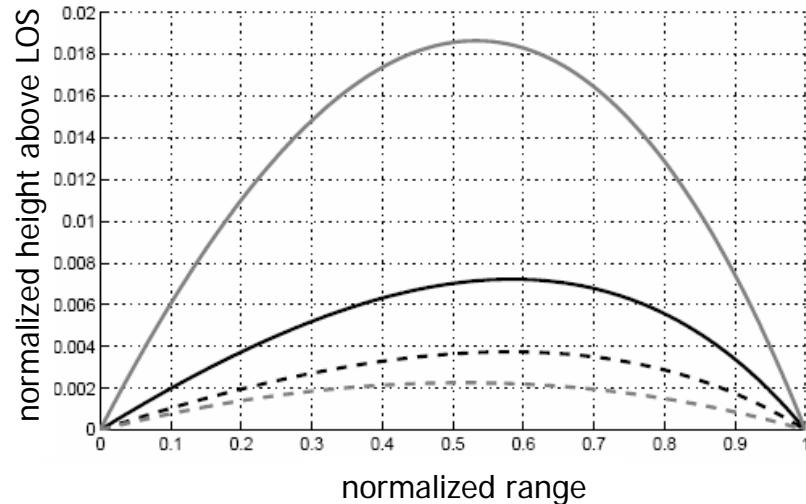
*Point Mass Trajectory Model*

*only drag and gravity acting on projectile*

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*analytically solvable set of differential equations of motion*



$$R := \frac{x_{max}}{y_{max}}$$

$$\vartheta_0 < 5^\circ$$

# Approach

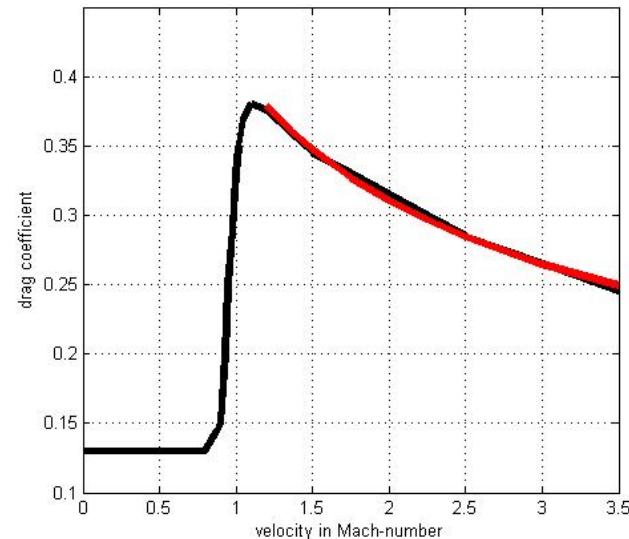
*Point Mass Trajectory Model*

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*Adding generalized power drag law*

*analytically solvable set of differential equations of motion*

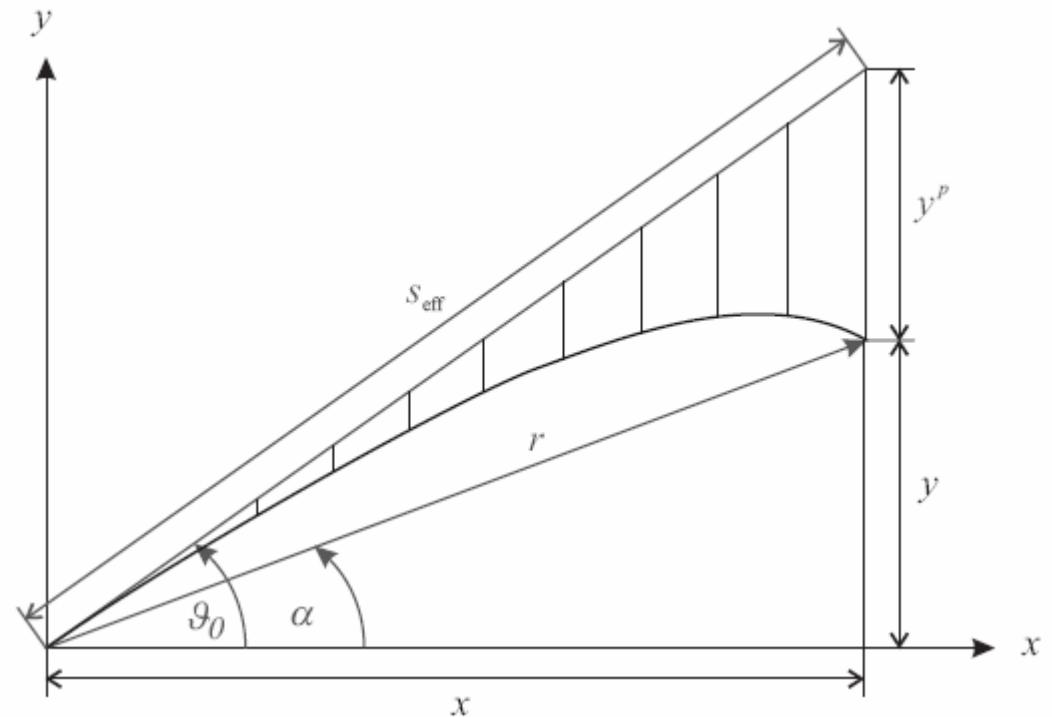


$$C_D := C_0 \text{Ma}^{-n}$$

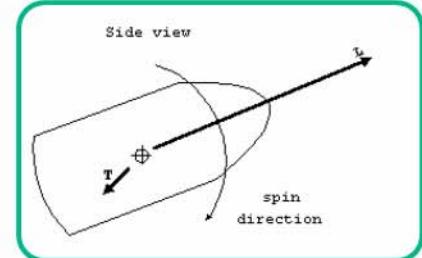
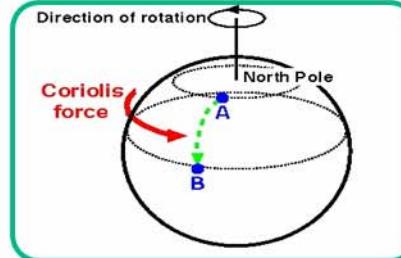
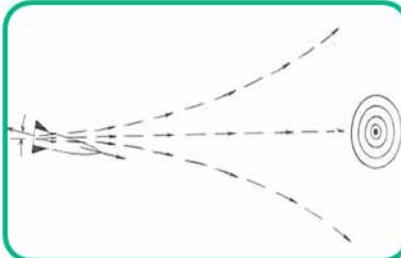
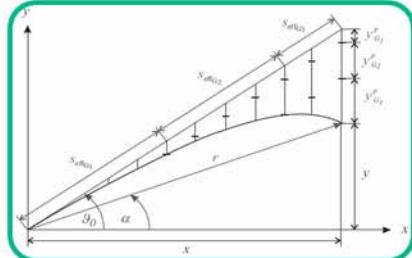
- ✓ *super elevation*
- ✓ *striking velocity*
- ✓ *time of flight*
- ✓ *striking energy*

*calculated using*

- *Mach dependent analytical solutions*
- *splitted solutions for slant range and gravity drop*
- *gravity corrected projectile velocity*



# Algorithm



## Multi Region Drag Fitting

- Extends range of validity

## Range- and Crosswind

- Using perturbation mathematics

## Coriolis Force

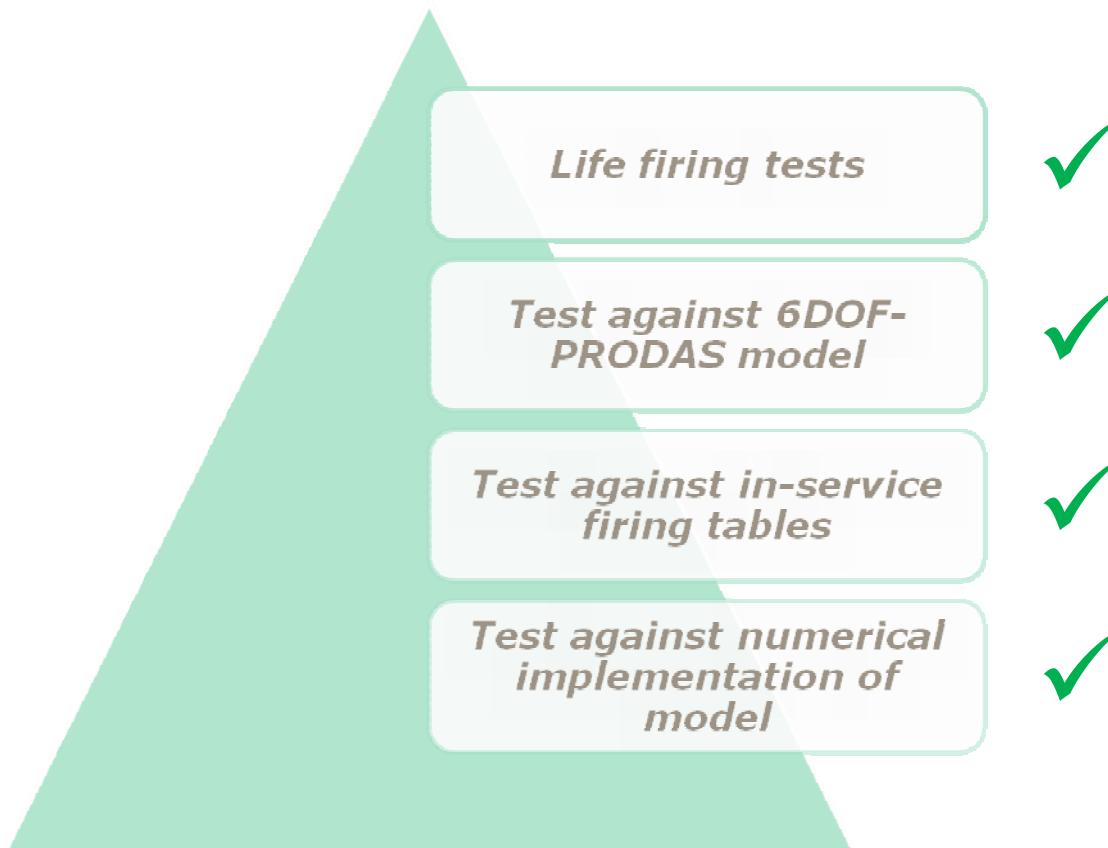
- Using McCoy's approximation

## Spin Deflection

- Using NATO STANAG 4355 Appendix F approximation

# Algorithm

<i>requirement</i>	<i>fulfilled</i>
<i>range- and crosswind</i>	✓
<i>arbitrary angle of site</i>	✓
<i>muzzle velocity</i>	✓
<i>coriolis force</i>	✓
<i>magnus force</i>	✓
<i>multiple ammunitions</i>	✓
<i>height dependent air temperature</i>	✓
<i>height dependent air pressure</i>	✓
<i>user-defined targeting sights</i>	✓
<i>time fuze capability</i>	✓

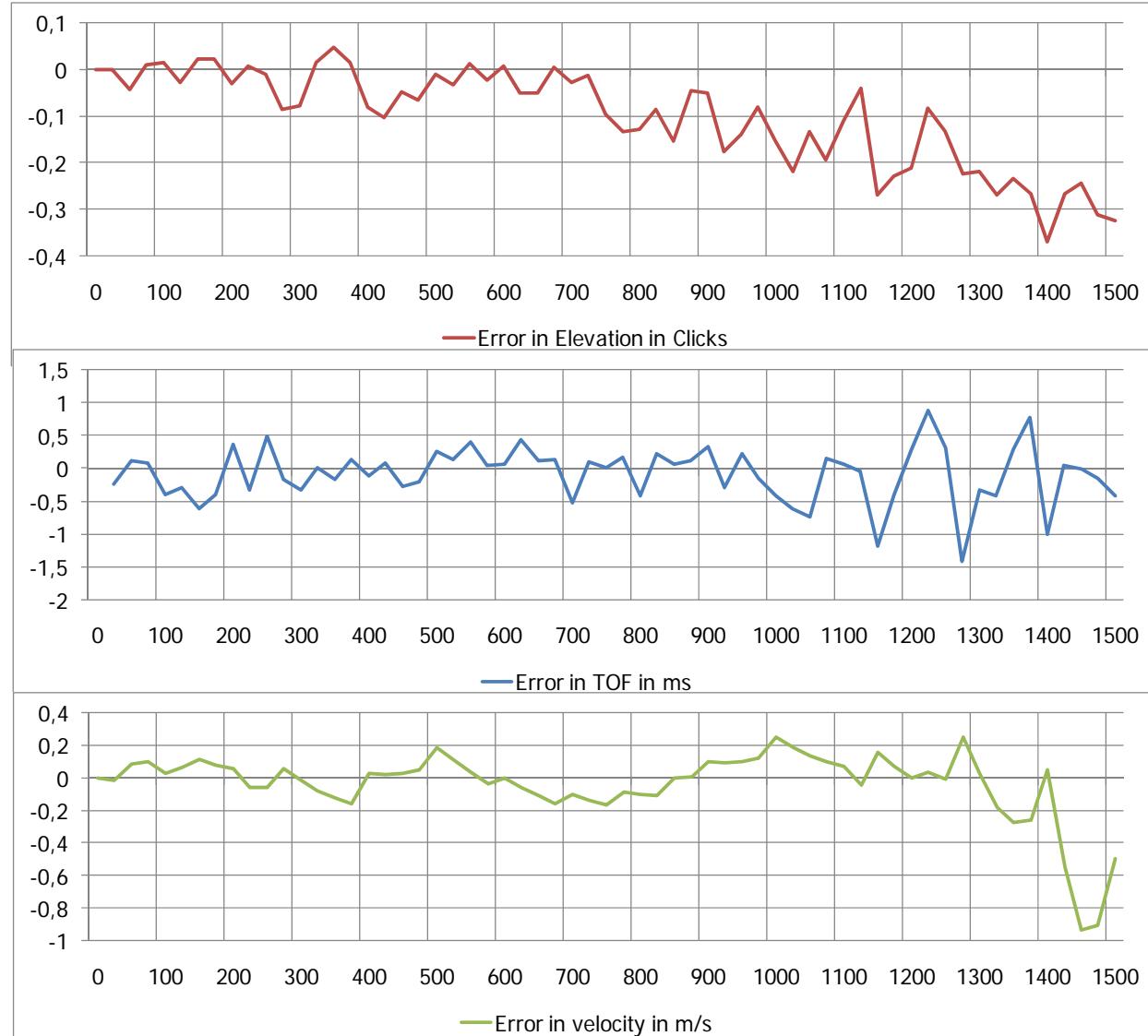


# Accuracy

weapon:  
*M82A1*

ammunition:  
*M8 .50BMG*

range:  
*0 – 1500 m*

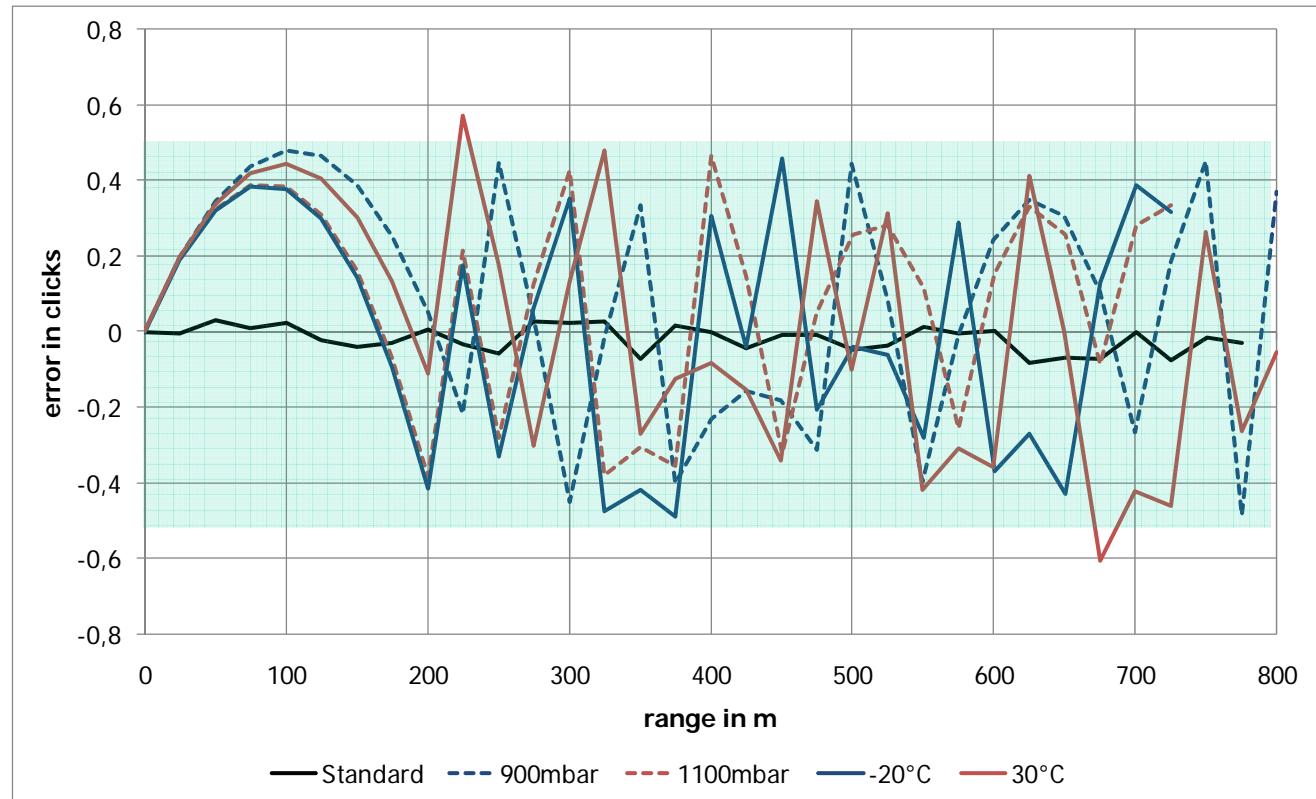


# *Met Variations*

weapon:  
*HK G3*

ammunition:  
*M80 .308*

range:  
*0 – 800 m*

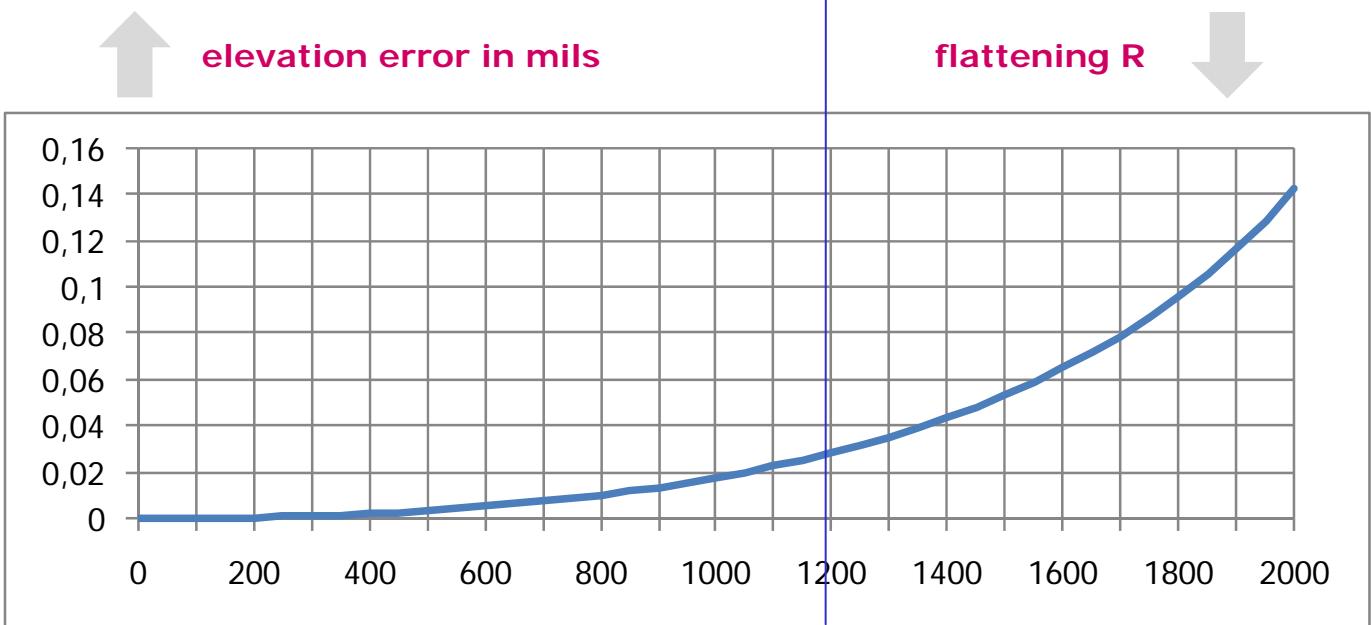
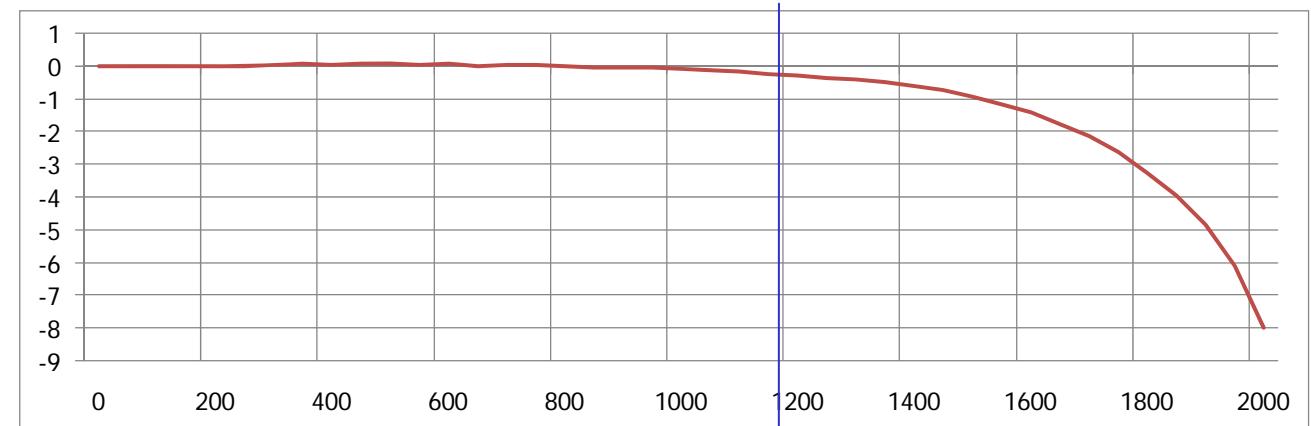


# Model Limitations

weapon:  
*HK GMG*

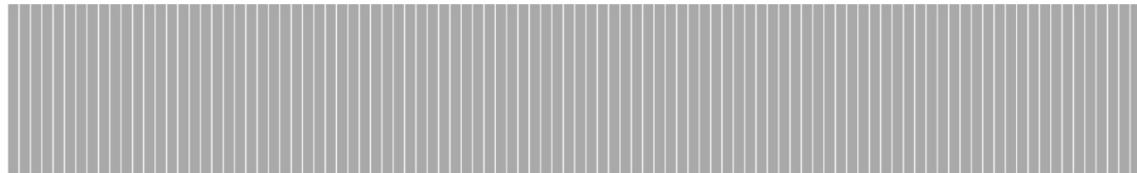
ammunition:  
*40mm*

range:  
*0 – 2000 m*



## *algorithm usage in an automated fire control system*

1 ms



*compute fire control solution*

*typically 0.1 to 1.2 ms  
depending on options used*

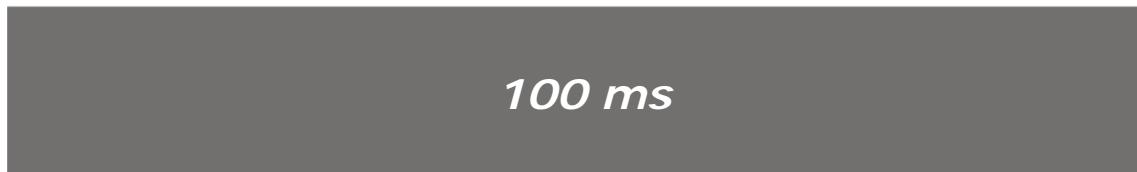
20 ms



*sensor readout*

*typically every 20 ms*

100 ms

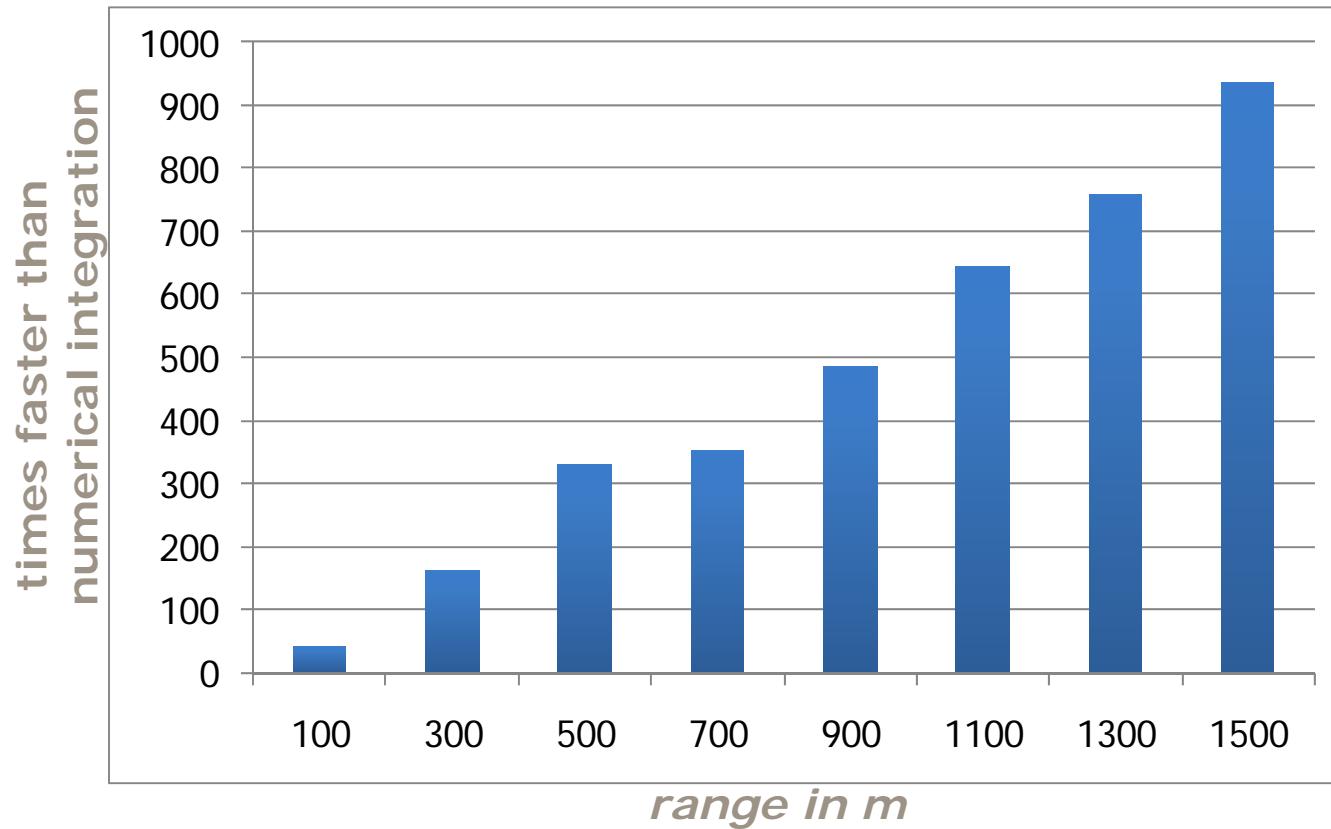


*re-align weapon*

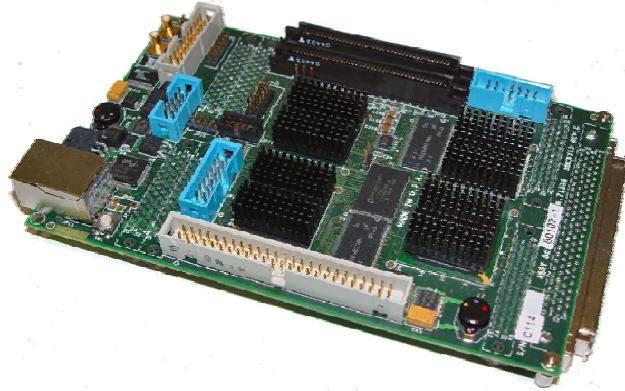
*typically 100 to 1000 ms*

# Performance

*Comparing analytical solution with numerical RK4 integration for a .50BMG rifle:*



# Implementations

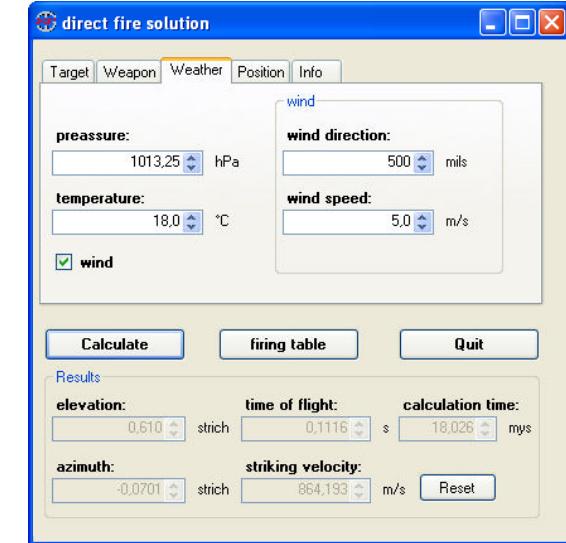
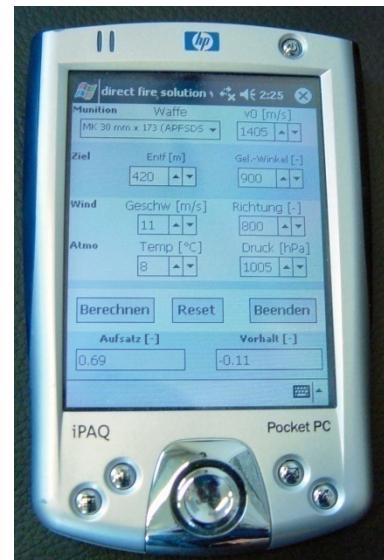


*DSP based stand alone  
fire control computer*

*Optimized MISRA-C source code compiled  
for TI DSP system*

*Pocket PC  
implementation*

*C# source code compiled for MS Pocket PC  
2003*



*Windows demonstrator  
front end*

*C# source code compiled for MS  
Windows*

# Implementations



using spare  
computational power



using spare  
computational power



# Conclusions

***An analytical solution for the differential equations of motion was found***

- thermodynamic state of the atmosphere was considered
- Multi region drag fitting
- uphill/downhill shooting
- wind / coriolis / spin deflection

***An optimized algorithm was developed***

- Optimized to minimized computation time
- Multi weapon / ammunition capabilities
- compact code size
- approved accuracy under nearly all conditions

***Sample implementations were introduced***

- handheld fire control for sniper teams
- in-sight automatic fire control for crew weapons

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