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COLUMBIA RADIATION LABORATORY
NEW YORK, NEW YORK 10027

March 31, 1980
COLUMBIA RADIATION LABORATORY

RESEARCH INVESTIGATION DIRECTED TOWARD EXTENDING THE USEFUL RANGE OF THE ELECTROMAGNETIC SPECTRUM

Progress Report No. 30
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Object of the research:

Basic research in the fields of quantum electronics; electromagnetic propagation, detection and sensing; and solid state electronics.

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March 31, 1980

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## Preliminary studies of spin relaxation of optically pumped sodium in xenon gas have shown that Van der Waals NaXe cause a substantial part of the relaxation. The electron-nuclear spin exchange–cross section between Na and Xe has been measured to be less than \(10^{-19} \text{ cm}^2\). Calculations and preliminary experiments have shown that radiofrequency spectroscopic studies of the anomalously long lived SD state of cesium are possible.
Further studies of dense alkali vapors have shown that all of the alkali vapors sodium, potassium, rubidium and cesium, have absorption bands in the spectral region between 1\mu and (2.5\mu). The possibility that some of these bands might be useful for the construction of infrared excimer lasers is being investigated.

A model system for studies of two photon optical pumping to produce ground-state spin polarization has been selected. We intend to work with the transition 5S_{1/2} → 5D_{3/2} in rubidium. A dye laser pumped by a krypton ion laser will be used to drive the transition.

Infrared emission bands of CsXe excimer states have been studied systematically as a function of temperature, and dissociation energies of the upper levels of several excimer transitions have been determined.

An apparatus to measure the Faraday rotation and circular dichroism of alkali noble gas excimers has been constructed. The results of this experiment will help to determine the quantum numbers of the upper states of the excimer transitions.

Particulate formation in mixtures of cesium vapor and deuterium or hydrogen gas has been investigated with a tunable dye laser. The stilbene dye is pumped with ultraviolet lines from an argon ion laser. Particulates, presumably CsD crystals, could be produced at very low cesium vapor density.

A new spin destruction mechanism for collisions between cesium atoms has been discovered. The new spin destruction rate is about 1% of the well known spin exchange rate. The spin destruction is probably due to the magnetic dipole-dipole interaction and it should exist for all alkali vapors.

We have determined the major energy transfer paths for COF\textsubscript{2} which exhibits a relaxation anomaly. The symmetric C-F stretch frequency (\nu_2) transfers energy to the antisymmetric C-F stretch mode \nu_4 more slowly than \nu_4 empties. We have also shown that the vibrational temperature of the coupled \nu_2, \nu_1 modes is very high compared to \nu_4. This suggests a metastable inverted population in COF\textsubscript{2}.

Intermolecule energy transfer between SO\textsubscript{2} and \textsuperscript{18}O\textsubscript{2} has been clearly demonstrated for the first time. Intermode energy transfer has been mapped in OCS and mixtures of OCS with rare gases. Both the SO\textsubscript{2}/\textsuperscript{18}O\textsubscript{2} and OCS systems are vibrationally metastable.

An extremely novel technique has been developed for producing supersonic beams of vibrationally excited molecules using relatively low power CW infrared lasers. Considerable advances have been made in the diagnostic studies of energy redistribution in supersonic expansions.

Preliminary studies of photofragmentation processes in SO\textsubscript{2} have been made using UV excimer laser radiation for photolysis. IR emission has been observed from vibrationally excited SO and SO\textsubscript{2} in the photolysis mixture.
Picosecond laser methods have been used to generate an important chemical intermediate, diphenyl carbene ($\text{C}^\cdot$) on photodissociation of the parent compound diphenyldiazomethane. We have discovered that excitation of the parent compound at 266 nm resulted in the generation of diphenylcarbene in an excited triplet state. This new and important channel for photodissociation was unknown prior to this work.

Picosecond laser coherent anti-Stokes Raman scattering (CARS) experiments have been carried out on gas phase benzene at room temperature. Both ground and excited state ($B_{2u}$) vibrational CARS signals have been observed. On photolyzing benzene with a pulse at 266 nm we have found, using CARS as a probe method, that multiphoton absorption by benzene generates fragments as small as C$_2$ extremely rapidly, i.e. within 25 ps. of excitation.

We report the direct measurement of electron solvation times in methanol and ethanol. A picosecond technique utilizing a laser triggered flash lamp and a streak camera is used to monitor the solvation process. The relationship of the solvation dynamics to dielectric relaxation, local heating, and pulse radiolysis results are presented.

We have discovered a new class of macroscopic reordering phenomena in gases, which is characterized by the periodic reformation of population "gratings" after standing-wave excitation. These gratings, detectable via their ability to scatter a probe laser, are useful in spectroscopic and collisional studies. We have completed the first phase of our investigation of the unusual properties of the three-pulse stimulated photon echo. We find that, in contrast to other echo effects, the stimulated echo is generated from information stored in one atomic state. Consequently, it may endure for unusually long times. We discuss our use of the stimulated echo to measure total elastic scattering cross sections. The Raman echo, excited in a vapor for the first time via a nonintermediate-state-resonant pathway, has been used to study collisional broadening of the forbidden 6P$_{1/2}$-6P$_{3/2}$ transition of atomic Ti. The tri-level echo technique, developed by us recently, has been employed to perform the most extensive study of the noble-gas-induced broadening of forbidden 3S-nS and 3S-nD transitions in Na. The two-pulse photon echo has been employed to study fundamental features of the collisional broadening of the 3S-3P$_{1/2}$ transitions in Na. Specifically, we have performed the first demonstration that the assumption of rectilinear collision trajectories is not in general correct even in the case of broadening of electronic transitions. An extensive theoretical treatment of rephasing processes in gases has been completed and published.

We have measured photon echo intensity as a function of pulse separation on the 3H$_4$-1D$_2$ transition in LaF$_3$:Pr$^{3+}$ (1.0% at. wt.). We have also performed preliminary photon-echo-nuclear-double-resonance (PENDOR) experiments to measure nuclear hyperfine splittings in the 3H$_4$ ground state.

A single-threshold detector is derived for a wide class of classical binary decision problems involving the likelihood-ratio detection of a signal embedded in noise. The class of problems considered encompasses the case of
multiple independent (but not necessarily identically distributed) observations of a nonnegative (or nonpositive) signal embedded in additive and independent noise, where the range of the signal and noise is continuous. It is shown that a comparison of the sum of the observations with a unique threshold comprises an optimum detector if a weak condition on the noise is satisfied independent of the signal. Examples of noise densities that satisfy and that violate this condition are presented. A sufficient condition on the likelihood ratio which implies that the sum of the observations is also a sufficient statistic is considered. This applies, in particular, to the case of heterodyne detection in the optical, infrared, and submillimeter where the signal, local oscillator, and noise can be treated as continuous random variables.

Statistical properties such as the cumulants, and the central, factorial, and ordinary moments are obtained for photocounting distributions when the incident radiation is intensity-modulated with arbitrary statistics. The results are applied in some detail to the cases of triangular, sinusoidal, and square-wave modulation of multimode superposed coherent and chaotic radiation. The coefficient of variation, skewness, and kurtosis are obtained as a function of modulation depth. Comparison is made with experimental data in the cases of triangular and sinusoidal modulation of a laser source. A computer simulation technique useful for generating superposed coherent and chaotic radiation of arbitrary spectral shape is described. Its advantages over other techniques include flexibility and ease of implementation, as well as the capability of incorporating spectral characteristics that cannot be generated by other methods. We discuss the implementation of the technique and present results to demonstrate its validity. The technique can be used to obtain numerical solutions to photon statistics problems through computer simulation. We argue that experiments involving photon statistics can be carried out using a wideband source in place of an amplitude-stabilized source whenever the spectral characteristics of the source are not important. Experimental results that corroborate the argument are presented.

We demonstrate the equivalence of detectors with and without nonparalyzable dead time in the presence of constant-intensity radiation and additive Poisson noise. We show that the performance of a detector with dead time will be the same as that of a similar detector without dead time used under exactly the same conditions, with the same threshold number of counts and sampling time, and the same radiation intensity, but with a reduced quantum efficiency. This result is valid in general whenever a detector with dead time is used in conjunction with a Poisson point process.

Experimental and theoretical studies of electronic carrier transport and optoelectronic processes at interfaces between semiconductors, insulators and metals are presented. The particular investigations reported here are internal photoemission mechanisms at metal-germanium interfaces, the dependence of capture cross sections of Si-SiO\(_2\) interface states on energy, and energy band discontinuities in semiconductor heterojunctions.
Block 19 continued - Key Words

Energy transfer
Vibrations
COF$_2$
OCS
SO$_2$
O$_2$
Nozzle
Vibrational temperature
Metastable
Photofragmentation
Picosecond
Laser
Raman
Photolysis
Benzene
Electron Solvation
Alcohols
Pulse radiolysis
Photodissociation
Diphenyl carbene
Fluorescence
Rydberg states
Collisional broadening
Grating echoes
Tri-level echoes
Raman echoes
Phase-matching
Photon echoes
Photon echo nuclear double resonance
Heterodyne detection
Single-threshold detection
Infrared detection
Likelihood-ratio detection
Submillimeter detection
Statistical properties
Photon counting
Wave noise
Optical detection
Dead time
Photon count antibunching
Optical communications
Optical radar
Metal-Germanium interfaces
Si-SiO$_2$ interfaces
Semiconductor heterojunctions
Interface states
Internal photoemission
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M. C. Teich and H. C. Card, "Photocounting Distributions for Exponentially Decaying Sources," Optics Lett. 4, 146 (1979). (JSEP-Work Unit 13)


H. C. Card and W. Hwang, "On the Transport Theory of Schottky Barriers"
to Polycrystalline Silicon Thin Films," IEEE Trans. on Electron Dev., Special Issue on Photovoltaic Devices (1980), accepted for publication. (DOE)


T. C. Poon and H. C. Card, "Admittance Measurements of Si-SiO₂ Interface States under Optical Illumination," J. Appl. Phys., to be published. (JSEP-Work Unit 15)

W. Hwang and H. C. Card, "Comments on Conduction Mechanisms of Metal-Nondegenerate Semiconductor Contacts" to be published. (JSEP-Work Unit 15)

C. M. Wu and E. S. Yang, "Current Suppression Induced by Conduction-Band Discontinuity in Al₀.₃₅Ga₀.₆₅As-GaAs N-p Heterojunction Diodes," J. Appl. Phys., in press. (JSEP-Work Unit 15)


Papers by CRL Staff Members Presented at Scientific Meetings


T. W. Mossberg, "Relaxation of Rydberg S and D States in Atomic Sodium Perturbed by He, Ne, Ar, Kr or Xe," International Conference on the Physics of Electronic and Atomic Collisions (ICPEAC), Kyoto, Japan, August 29 - September 4, 1979.


Lectures


K. Eisenthal, "Picosecond Laser Studies of Excited State Proton Transfer," Physical Chemistry Seminar, University of California, Berkeley, California, March 13, 1979; Seminar, Department of Chemistry, University of California at Los Angeles, Los Angeles, California, March 16, 1979.


Meetings are held periodically at Columbia University, New York, New York during the academic year and are open to all members of the New York Scientific community. Guest speakers are invited to discuss work in the general area of the research in the Columbia Radiation Laboratory.


Frank Fang, IBM Watson Research Center, "Effects of Uniaxial Pressure on Energy Bands at Si-SiO2 Interfaces", November 2, 1979.


I. ENERGY TRANSFER AND RELAXATION IN ALKALI METALS

A. NUCLEAR SPIN POLARIZATION OF Xe BY OPTICAL PUMPING∗

(B. Suleman, T. McClelland, W. Happer)

It is well known(1) that an alkali atom can exchange its electronic angular momentum with the nuclear spin of a noble gas atom in an alkali-noble gas collision. The polarization of optically pumped alkali vapor can be transferred to the noble gas nuclei by these spin exchange collisions. As much as 10% polarization of Xe^{129} has been reported(2) by using Rb vapor of about 10% polarization. We would like to polarize Xe by using optically pumped Na vapor. By using a laser instead of a conventional lamp to pump high density Na vapor, we expect to achieve considerable Xe polarization. In addition to measuring the spin exchange cross section, we also want to study the relaxation of polarized Xe.

The origin of the spin exchange process is the contact hyperfine interaction between the alkali valence electron and the noble gas nucleus.(3) The effective Hamiltonian governing this interaction can be written as

\[ V = \gamma \mathbf{I} \cdot \mathbf{S} \]  

(1)

where \( \mathbf{I} \) is nuclear spin of the noble gas, \( \mathbf{S} \) is the electronic angular momentum of the alkali atom and \( \gamma \) is the strength of spin exchange interaction. During a collision, the spins \( \mathbf{I} \) and \( \mathbf{S} \) of the colliding pair rotate rapidly around the resultant angular momentum \( \mathbf{I} + \mathbf{S} \). This tendency of the spin exchange collisions to rotate the spins can be represented by an effective magnetic field which produces a shift in the Zeeman resonance frequency of the alkali atoms. The frequency
shift can be written as

$$\Delta \omega_0 = 2Z \phi \langle I_z \rangle$$  \(2\)

where \(\langle I_z \rangle\) is the polarization of the noble gas and \(Z\) is the kinetic collision rate. \(\phi\) is the total phase angle produced during a collision and averaged over all impact parameters. A very rough estimate of frequency shift is

$$\Delta \omega_0 \approx 5.61 \times 10^3 P \langle I_z \rangle \text{ sec}^{-1} \text{torr}^{-1}$$  \(3\)

where \(P\) is the pressure of Xe in the cell. The nuclear polarization of \(\text{Xe}^{129}\) can be detected by measuring the frequency shift \(\Delta \omega_0\) of the Na Zeeman resonance transitions.

The apparatus we are using for producing and detecting the nuclear polarization of Xe is shown in Fig. 1. Sodium D\(_1\) resonance light from a Spectra Physics 370 dye laser is circularly polarized and pumps the Na vapor in a cell which contains about 2 torr of Xe, 500 torr of helium and a few torr of nitrogen. The strong pump beam is kept on for about 100 seconds. We estimate that during this time the Na-Xe spin exchange collisions will produce about 0.2% Xe\(^{129}\) polarization.

For detecting the Xe polarization, the Na ensemble is operated as a magnetometer by applying a radio frequency field from a frequency synthesizer. The incident photon flux and the RF field strength are attenuated such that they do not cause appreciable broadening of the Zeeman resonance lines and yet give us a good signal to noise ratio. The variation of light intensity with RF field is shown in Fig. 2. The driving radio frequency
Figure 1: Frequency synthesizer produces the Na resonance frequency $\omega_1$. The input of VCO is a triangular wave of frequency $\Omega$ produced by function generator. The frequency modulated output of VCO is fed to Xe coils.
Figure 2: Signal $\Delta I$ due to frequency shift $\Delta \omega_0$ produced by adiabatic reversal of Xe spins at a rate $\Omega$. 
ω is set at the side of the line (Fig. 2) where the response of the system is maximum to variations in frequency. The Xe spins are now flipped parallel and antiparallel to the external magnetic field $H_0$ by adiabatic fast passage. To do this an audio frequency oscillating field is applied perpendicular to $H_0$ by a second set of Helmholtz coils. The voltage controlled oscillator produces a frequency modulation and the audio frequency field is swept through the xenon resonance frequency ($\approx 1.17$ KHz/Gauss) at a fixed rate $\Omega$. The adiabatic reversal of Xe spins modulates the transmitted light intensity at the same frequency $\Omega$. The transmitted light is collected in a photodetector and is fed to a phase sensitive detector locked at frequency $\Omega$. If we tune the frequency of the RF field to $\omega_0$ (Fig. 2), the half maximum point, then the signal $\Delta I$ is given by

$$\Delta I = \frac{\Delta \omega}{\Gamma} [I(\text{max}) - I(\text{min})]$$  \hspace{1cm} (4)

where $\Gamma$ is the full width at half maximum. For minimum detectable frequency shift $\Delta \omega_{\text{min}}$, the signal $\Delta I$ has to be at least equal to noise $N$, so that

$$\Delta \omega_{\text{min}} \geq N \Gamma / [I(\text{max}) - I(\text{min})]$$ \hspace{1cm} (5)

Apart from laser noise $N$, the major source of noise is the fluctuation in the ambient magnetic field $H_0$. We are now planning to use mu-metal shields to get rid of magnetic noise. A preliminary Zeeman resonance curve is shown in Fig. 3. The noise $N$ is mainly due to laser intensity fluctuations.
Figure 3: A chart recorder trace of resolved Zeeman lines obtained by sweeping $H_0$. Frequency synthesizer was kept at 3.0 MHz. The sweeping rate is about 10.6 KHz/division.

$\Gamma = 2.1$ kHz
*This research was also supported by the Air Force Office of Scientific Research under Grant AFOSR-79-0082.


B. SPECTROSCOPY OF THE 5D STATE OF CESIUM

(A. Sharma, W. Happer)

Most of the low lying states in cesium atoms have been studied with respect to their hyperfine structure. The 5D state is a conspicuous exception. Many of these states have, apart from the usual magnetic dipole and electric quadrupole interactions, additional splittings due to the polarization of the core of electrons by the single valence electron. It arises from the fact that two electrons with parallel spins have a different interaction than when they have antiparallel spins. This interaction is especially known to be very pronounced in the nD5/2 states; so much that the magnetic dipole constant which by simplistic arguments ought to be greater than zero, actually turns out to be negative. Of the D3/2 states we expect this effect to be most pronounced in the 5D3/2 state as it lies closest to the nucleus in the series of D3/2 states and therefore most effective in polarizing the inner core of electrons.

We have discussed earlier (1) the problems in studying this state and the reasons why it could not be studied earlier. Since then we have made a number of computer calculations that make the experiment apparently feasible. For example, using a dye laser (Coherent Model #CR-599) we can selectively excite a few Zeeman states in the 5D3/2 level by tuning the frequency to an appropriate position in the absorption profile of cesium atoms. Figure 1 shows the absorption cross section of cesium atoms from ground state to the 7P1/2 state as a function of the single mode detuning, at 400°K with σ+ light and with a magnetic field of 800 Gauss.

As mentioned in reference (1) we intend applying a radiofrequency signal to cause transitions between the various Zeeman levels of the 5D3/2
Figure 1
state and observe the change in the intensity of the fluorescent light. As an example, our calculations show that by tuning the dye laser to detuning position -5 Ghz in Figure 1, we can obtain a signal to background ratio of 3%. We are in the process of making preliminary measurements, like the amount of noise tolerable in the detection system (lead sulphide crystal cooled to 193°K) and also the temperature we can raise the cell to without destroying the polarization in the excited state by collisions.

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(1) CRL Progress Report #29, March 31, 1979, p. 49.
C. INFRARED ABSORPTION OF ALKALI MOLECULES*

(A. Vasilakis, N. D. Bhaskar, W. Happer)

Previous progress reports discussed the new infrared absorption we discovered in potassium\(^1\) and cesium\(^2\) saturated vapors out to at least 2.5µ. Here we report on a recently completed study of infrared absorption in saturated sodium vapor. This study shows many similarities with potassium and cesium. The absorption from .83 to 1.18µ in saturated sodium vapor may be the analog of the ultraviolet emission continuum of \(\text{H}_2\), possibly arising from the sodium dimer \(\text{Na}_2^+ \rightarrow \text{Na}_2^+\) transition, along with contributions from higher sodium polymers. At longer wavelengths out to 2.5µ the absorption is probably due to higher polymers of sodium (\(\text{Na}_3, \text{Na}_4, \ldots\)).

A diagram of the experimental apparatus is shown in Figure 1. The length of the heat pipe is 2 m with an outside diameter of 25 mm and 3 mm wall thickness. A capillary structure of several turns of stainless steel mesh is used to return the condensed sodium liquid to the central heating region of the pipe. Helium buffer gas is used to protect the windows of the heat pipe from the hot alkali vapor. Water cooling is also applied to the ends of the heat pipe to condense the vapor before it reaches the windows. To measure the effective length of the vapor column (40-65 cm) in the heat pipe,\(^3\) 45 thermocouples were used to measure the temperature profile along its length. Heating was provided by electrical heaters capable of supplying over 3 KW. Operating temperatures ranged from 630 to 870°C, pressure and temperature were found to agree within 10% with the empirical formula\(^4\)

\[
\log_{10} P_{\text{mm}} = 7.4103 - \frac{5232.1}{T}.
\]  

(1)
Figure 1: Apparatus used to measure the absorption coefficient of saturated sodium vapor.
The experimental procedure was as follows: the intensity $I(\lambda, T_0)$ of the light at wavelength $\lambda$ at a temperature $T_0$ transmitted through the heat pipe was measured where $T_0$ is a temperature slightly above the melting point of sodium (no appreciable sodium vapor pressure). Then the intensity $I(\lambda, T)$ transmitted through the vapor is measured for different temperatures and the length $Z$ of the vapor is determined by the temperature profile along the pipe. $I(\lambda, T_0)$ is then measured again; if it agrees with the first within a few percent, the data is used. We can then determine the attenuation coefficient $\alpha(\lambda, T)$ from

$$\alpha(\lambda, T) = Z^{-1} \ln \left[ \frac{I(\lambda, T_0)}{I(\lambda, T)} \right]$$  \hspace{1cm} (2)

In addition, it is empirically found that the data fits the formula

$$\alpha(\lambda, T) = \exp[A(\lambda) - E(\lambda)/RT] \quad .$$  \hspace{1cm} (3)

The data can be graphed for $\ln \alpha(\lambda, T)$ versus $1/T$ and straight lines fitted to the data very well. The various contributions to the total absorption coefficient for various clusters of $n$ sodium atoms are given by terms of the form

$$\alpha_n(\lambda, T) = b(\lambda) N_{Na}^n \exp\left[ -\frac{V(\lambda)}{RT} \right] ,$$  \hspace{1cm} (4)

where $V(\lambda)$ is the potential energy of association of $n$ sodium atoms into a configuration for which an electronic transition of wavelength $\lambda$ is possible. The number density of sodium atoms is $N_{Na}$ and the factor $b(\lambda)$ contains oscillator strengths and phase-space factors.
Using the ideal-gas law and (1) we can rewrite Eq. (4) as

\[ \alpha_n(\lambda, T) = C(\lambda) \exp[-(n\varepsilon + V)] , \]

where \( \varepsilon \) is the latent internal energy of vaporization and is related to the latent heat \( l \) by \( \varepsilon = l - RT_r = 21.8 \text{ kcal/mole} \). The value of \( l \) is obtained from the Clausius-Clapeyron equation (1) yielding \( l = 23.9 \) kcal/mole, and \( T_r = 1060.6^\circ\text{K} \) is a typical value for the temperature. Comparing (3) and (5) we conclude that the activation energy \( E(\lambda) \) is equal to the sum of the association energy \( V \) plus \( n \) factors of the vaporization energy \( \varepsilon \),

\[ E(\lambda) = n\varepsilon + V . \]

In Figure 2 a summary of our experimental data is shown, the attenuation coefficient \( \alpha(\lambda, T) \) and the activation energy \( E(\lambda) \) are plotted as a function of wavelength \( \lambda \) for \( T = 1060.6^\circ\text{K} \). The energies \( 2\varepsilon = 43.6 \) and \( 3\varepsilon = 65.4 \text{ kcal/mole} \) are shown for reference in Figure 2.

For the region .84 to 1.02\( \mu \) the activation energy is a little larger than we expected for absorption from the repulsive ground state, while that from 1.02 to 1.18\( \mu \) has activation energies of the size one might expect for the repulsive ground state. A possible explanation for this is that trimers or higher polymers along with the \( (3\Sigma_u^+ + 3\Sigma_u^+) \) transition of the dimer are responsible for absorption from .83 to 1.18\( \mu \). The activation energy after 1.18\( \mu \) in saturated sodium vapor undergoes a rapid increase, similar to the behavior of potassium after 1.6\( \mu \). The jump in activation energy does not reach the \( 3\varepsilon \) level however as in the case of potassium vapor (Figure 2). We believe that bound trimers, or higher
Figure 2: Activation energies (points) and attenuation coefficient (solid line) for saturated sodium vapor as a function of wavelength. The standard deviation of the activation energies were obtained by weighted least squares error analysis and are shown at representative wavelengths. The error estimates for the absorption coefficient are also shown. The absorption coefficient is shown for $T = 1060.6^\circ\text{K} (P = 300 \text{ Torr})$. 
polymers are responsible for the jump in activation energy after the 1.18\mu knee in the absorption coefficient of the sodium data.

At present we are examining absorption in saturated rubidium vapor for comparison to the other already studied alkalies. In addition, we are planning fluorescence experiments for these alkalies in the spectral regions we have studied in absorption.

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D. GROUND-STATE POLARIZATION BY TWO-PHOTON OPTICAL PUMPING OF ATOMIC VAPORS*

(N. Tran, W. Happer)

The idea of remotely sensing magnetic fields by optically pumping atmospheric Xe$^{129}$ was first proposed two years ago.\(^{(1)}\) Due to atmospheric absorption, direct one-photon optical pumping is ruled out, and alternative two-photon pumping schemes have been proposed.

Preliminary experiments at NADC\(^{(2)}\) failed to detect any nuclear polarization in Xe$^{129}$, but excellent two photon pumping rates were observed. Further feasibility studies in our laboratory\(^{(3)(4)}\) and recent advances in excimer laser technology\(^{(5)}\) have maintained the interest in the original idea.

As a first step towards an ultimate practical system, we have undertaken to observe and measure the ground-state polarization of Rubidium atomic vapors with a two-photon pumping scheme. Our goal is to demonstrate the feasibility of such a scheme, and also to learn more about possible pitfalls in such systems. Although excited-state polarization has been observed in numerous multi-photon experiments, both in atomic vapors\(^{(6)}\) and in solids,\(^{(7)}\) to our knowledge polarization in the ground-state has yet to be detected.

The proposed pumping scheme is depicted in Figure 1, and the experimental set-up is shown in Figure 2. A Krypton ion laser is used to pump Oxazine 750 dye. The circularly polarized light beam at 7781 Å is focussed into a cell containing Rb vapor, N$_2$ quenching gas and helium buffer gas. Two-photon excitation takes place between the ground-state and the 5D$_{5/2}$ excited state via a virtual state close to the 5P$_{3/2}$ state. The
Figure 1
CH: Chopper
QW: Quarter-Wave Plate (7781 Å)
C: Cell
L: Lenses
O: Oven
H: Helmholtz Coils
IF: Interference Filter (4202 Å)

Figure 2
fluorescence \(^{6P} _{3/2} \rightarrow ^{5S} _{1/2}\) at 4202 \(\AA\) is detected at 90° with a photomultiplier tube.

There are many reasons for picking these states in Rubidium for a preliminary study. By solving the steady-state pumping-diffusion problem in cylindrical symmetry (neglecting variation along the light beam), we find:

\[
\langle S_z \rangle(r) = \begin{cases} 
A I_o \left(\sqrt{\frac{R+r}{D}} r \right) + \frac{R/3}{R+\gamma} & (r \leq r_o) \\
B K_o \left(\sqrt{\frac{\gamma}{D}} r \right) & (r > r_o) 
\end{cases}
\]

Here \(\langle S_z \rangle\) is the Rubidium ground-state polarization,

- \(A\) and \(B\) are constants determined from boundary conditions,
- \(I_o\) and \(K_o\) are modified Bessel's functions,
- \(\gamma\) is the spin relaxation rate,
- \(D\) is the diffusion constant,
- \(r_o\) is the geometrical laser beam waist, and
- \(R\) is the two-photon pumping rate per atom, derived earlier in reference (3).

It happens that with these particular states in Rb, pumping rates \(R\) of the order of \(\sim 10^3\) sec\(^{-1}\) are possible with presently available laser power. Using values for \(\gamma\) inferred from recent experiments by Bhaskar et al., one can show from the above equation that percent polarizations \(2\langle S_z \rangle \sim 10\%\) should be obtainable. The apparatus of Figure 2 is now under construction and we hope to perform the first experimental studies of two-photon optical pumping by the fall of 1980.
*This research was also supported by the Naval Air Development Center, Warminster, Pennsylvania.


(2) E. Greeley and L. Bobb, private communication.


(8) W. Happer and N. Tran, to be published.

E. TEMPERATURE AND DENSITY VARIATION OF THE INFRARED BANDS OF CsXe; CESIUM POLYXENIDE BANDS*

(R. Novak, W. Happer, N. Bhaskar)

The previous Progress Report(1) described the first investigations of alkali-noble gas excimer molecules in the spectral range between 1.0 and 2.0 microns. These investigations found bands and satellites for the CsNe, CsAr, CsKr, CsXe, RbKr, RbXe, and KXe molecules. During the past year, the infrared bands of CsXe have been studied in detail. From this study, the dissociation energy of the 7SE_{1/2} state of CsXe has been experimentally determined and experimental evidence for the presence of CsXe_2 has been found.

Electronic states of an alkali-noble gas molecule are associated with the states of the free cesium atom. The nature of these states and methods of populating them have been discussed previously.(1)(2) Typical data for the molecular transitions of CsXe associated with the 7S \rightarrow 6P transitions of atomic cesium appear in Figure 1. The band and satellite of the molecular 7SE_{1/2} \rightarrow 6P_{3/2} transition are on the long wavelength side of the 7S_{1/2} \rightarrow 6P_{3/2} atomic transition; the bands and satellites of the 7SE_{1/2} \rightarrow 6P_{3/2} and 7SE_{1/2} \rightarrow 6P_{1/2} transitions fall on the red side of the 7S_{1/2} \rightarrow 6P_{3/2} transition. The intensity of the satellite peak normalized to the 7S_{1/2} \rightarrow 6P_{3/2} atomic peak [S(\lambda,[Xe],T)] was studied for cells with densities of 0.9, 2.4, 4.5, and 6.9 Amagats (1 Amagat = 2.69 \times 10^{19}/cm^3) in the temperature range between 150 and 400°C. This normalized satellite intensity varies as(3)

\[
S(\lambda,[Xe],T) = G(\lambda,[Xe]) T^{-1/6} \exp[(V_u(\infty) - V_u(R))/kT]
\]
Figure 1: Infrared spectra of CsXe between 1.35 and 1.70 μm.
where $G$ is a constant and $V_u(R)$ is the potential energy curve of the upper $(7S\frac{1}{2})$ state. According to the Franck-Condon principle during a transition, the interatomic distance, $R$, remains a constant; thus, $R$ is the interatomic distance associated with the satellite peak. A temperature profile of CsXe should yield a value for $V_u(\infty) - V_u(R)$.

The normalized intensities for the $7S\frac{1}{2} \rightarrow 6P\frac{1}{2}$ satellite at 1.44\(\mu\) and the $7S\frac{1}{2} \rightarrow 6P\frac{3}{2}$ satellite at 1.668\(\mu\) are presented on the semilog plot of Figure 2. The linearity of the data indicates that the $7S\frac{1}{2}$ molecular state of CsXe is in thermal equilibrium with the $7S\frac{1}{2}$ atomic state of cesium; the slope gives a value for $V(\infty) - V(R)$. The equality of the slopes for the two satellites indicates that each satellite originates in the same region of the upper state potential. A similar plot for wavelengths in the bands between the satellites and the atomic lines yields smaller values for the slope. This indicates that the satellites originate from the bottom of the $7S\frac{1}{2}$ potential well. The slope of the normalized intensities provides an experimental value of the dissociation energy of the $7S\frac{1}{2}$ state of CsXe; this value is taken to be $1015 \pm 30$ cm$^{-1}$.

Figure 3 compares the measured values of this experiment to the previous experiments of Sayer(4) and Hedges.(5) Sayer's value for the $7S\frac{1}{2}$ state is consistent with the present investigation; Hedges' values for the $6P\frac{3}{2}$ states are about 100 cm$^{-1}$ too high; the shape of the $6P\frac{3}{2}$ state of Hedges is not consistent with the present data.

Deviations from a straight line for high density and low temperature data (Figure 2) suggested the presence of cesium polyxenide molecules; polyxenide molecules have been previously reported for KXe.(6)
Figure 2: Semilog plot of normalized satellite intensity versus \(1/T\). The \(T^{1/6}\) factor is needed to analyze satellite intensities.
Figure 3: Comparison of energy levels found in the present experiment to previously found experimental energy levels.
were taken in both the visible (Figure 4) and infrared (Figure 5). Both spectra sets of spectra have properties similar to those of $KXe_n$. (7)

Data for the red wing normalized to the monoxenide peak appear in Figure 6. This data suggest the following variation for the wing intensity

$$I(\lambda, [Xe], T) / I(5723\text{Å}, [Xe], T) = [Xe] \exp \left[ \frac{E(\lambda)}{kT} \right].$$

The consistency of the experimental points among the data for the three different densities indicates that the wing intensity is primarily due to $CsXe_2$ molecules. The potential energy of this $CsXe_2$ state is lower than the potential energy of the $7\Sigma^+_1/2$ state of $CsXe$ by approximately $1100 \text{ cm}^{-1}$; this indicates that the first xenon atom attached to the cesium atom has little effect on the electric field around the alkali core.

In summary, an experimental value for the dissociation energy of the $7\Sigma^+_1/2$ state of $CsXe$ has been determined to be $1015 \pm 30 \text{ cm}^{-1}$ and the first experimental evidence for the existence of $CsXe_2$ has been found.

*This research was also supported by the Army Research Office (Durham) under Contract DAAG29-80-C-0043.

(1) CRL Progress Report #29, March 31, 1979, p. 4.
Figure 4: Visible spectra of the $7S_{1/2} \rightarrow 6S_{1/2}$ transition in CsXe illustrating the red wing dependence on xenon density.
Figure 5: Infrared spectra of the $7\Sigma_{1/2} \rightarrow 6\Pi_{3/2}$ satellite illustrating temperature and density dependence of the band shape.
Figure 6: Normalized red wing data of the $7S_{1/2} \rightarrow 6S_{1/2}$ transition. Linearity indicates the presence of CsXe$_2$. 

\[
\frac{I(\lambda_1[Xe]T)}{[Xe]} \frac{I(5723 \AA[Xe]T)}{I(6900 \AA[Xe]T)} \text{ vs. } \frac{1}{T}
\]
F. FARADAY ROTATION AND MAGNETIC CIRCULAR DICHROISM OF ALKALI-NOBLE GAS SYSTEMS*

(M. Islam, A. Kponou, W. Happer)

The primary objective of this experiment is to determine unambiguously the quantum numbers associated with the absorption bands of alkali-noble gas systems. (1) Initially, attention will be focussed on the cesium-xenon gas excimer. The plan is to search for both Faraday Rotation (FR) and Magnetic Circular Dichroism (MCD) of the alkali noble gas system.

In this reporting period, the apparatus described in the last year's report has been modified considerably, mainly as a result of our attempts, so far with some success, to observe FR in a solution of cobaltous nitrate$^{(2)}$ Co(NO$_3$)$_2$, which is of the same order of magnitude as estimated for Cs-Xe.

The present experimental arrangement for FR is shown in Figure 1. For MCD, a $\lambda/4$ plate is inserted between modulator and cell and the analyzer A removed. The source is a 100 W projection lamp which will be soon replaced by 150 W xenon arc lamp. This replacement has been found necessary because of the high degree of collimation and consequent loss of the light beam as it passes through the cell. Reflections of light from the walls of the absorption cell can alter its polarization and introduce error in the measurement. The iris diaphragm serves to collimate the light and to minimize reflections from the cell walls. The filter F removes second order diffraction from the light emerging through the exit slit of the monochromator.

The emergent light is polarized by the plane grating of the monochromator. The polarization depends on wavelength and therefore could lead to
S = Source of light
C = Chopper
F = Filter
L₁, L₂ = Lenses
P = Polarizer
ID = Iris diaphragm
RM = Rotating modulator
ASB = Layers of asbestos
H = Nichrome wire as heating element
CR = Ceramic paper
G = Pressure gauge
A = Analyzer
D = Detector

Figure 1
serious errors in measuring FR. Its effect was in fact observed while studying the Co(NO$_3$)$_2$ solution. To avoid systematic errors due to the polarizing properties of the monochromator, a linear polarizer is used at the exit slit of the monochromator to define a wavelength independent polarization of the light before it enters the modulator. Another approach would be to place a polarization scrambler at the monochromator exit. Errors introduced by the polarizing properties of the monochromator can also be eliminated by passing white modulated light through the cell and detecting the emergent light through the analyzer by the monochromator and the subsequent detecting stages.

The principle of modulation has been retained but the modulator has been modified by using twenty-two pieces of polaroid instead of just two. Thus, there are eleven cycles of polarization modulation for each complete rotation of the modulator, resulting in a modulation frequency of 11f where f is the rotation frequency of the motor. (Examination of polarization modulation in this modulator has revealed that the number of polaroid pieces has to be 4n + 2 where n = 0, 1, 2, 3, ... ) Enhancement of modulation frequency was necessary to get rid of low frequency noise which is easily generated in the system and to achieve better signal to noise ratio.

Faraday Rotation $\alpha$ is given by $V_\lambda \ell B_z$ where $\ell$ is the length of the interaction region, B$_z$ is the component of the magnetic field parallel to the direction of propagation of light and $V_\lambda$ is the Verdet Constant of the sample at the wavelength $\lambda$ involved. A long interaction region and a strong magnetic field are therefore desirable. This is especially so in this experiment because the system is in the gas phase and has a much
smaller number density than the liquid or solid phases. A solenoid magnet having a length of 34" and capable of producing an average field of about 3000 gauss over the length (B_{average} = 0.8 \cdot B_{center}) will be used. The magnet is water cooled.

Several unsuccessful attempts were made to prepare 33" long and 1" i.d. glass cells. Some cells cracked before Cs was distilled; in others Cs did not uniformly distribute itself over the length of the cell and it also attacked the windows of the cell. Besides, the high pressure of xenon anticipated in a loaded cell made it potentially hazardous. Among other choices of cell material, stainless steel, which is highly resistant to the attack by alkali vapors turned out to be a good alternative to glass. Such a cell has been assembled. It consists of a 304 s.s. tubing 50" long, 3/4" i.d. and 1/16" thick wall. The windows are 1/8" thick 1720 Corning glass with a useful aperture of 5/8". Inside the tube are two layers of size 100 stainless steel wire mesh 36" wide. The purpose of the mesh is to provide a uniform layer of cesium in the interaction region. By capillary action, any cesium which condenses outside the heated segment of the cell will flow toward the center. The cell at this time is ready to be loaded with Cs following the procedure described by E. Zouboulis. (3) The cell will be heated by nichrome wire wound tightly on a layer of ceramic paper wrapped around the tube. Thermal insulation between the heater and the magnet will be provided by several layers of asbestos material. The nichrome wire is wound noninductively to cancel out any magnetic field produced in the interaction region due to the alternating current passing through it.
The scheme for measuring Faraday Rotation is based on the following analysis: Let $P_1$ and $P_2$ represent the polarization of the modulated light at an angle $\theta$ and $A$ represent the transmission axis of the analyzer at an angle $\phi$ about some axis $OY$ (Figure 2). If $\alpha$ is the Faraday produced by the sample, the mean and difference in the transmitted intensities detected are respectively given by

$$I_m = I'_0 \left[ \cos^2(\phi-\alpha) \cos^2 \theta + \sin^2(\phi-\alpha) \sin^2 \theta \right]$$  \hspace{1cm} (1)

$$\Delta I = I'_0 \sin 2(\phi-\alpha) \sin 2\theta$$  \hspace{1cm} (2)

where $I'_0 = I_0 e^{-k\ell}$; $I_0$, $t$, $k$ and $\ell$ represent the intensity of light before the cell, transmittance of the analyzer, absorption coefficient and the length of the sample respectively. It can be shown that high detection sensitivity and signal to noise ratio can be achieved by setting $\phi = 0^\circ$ or $90^\circ$ and $\theta = 45^\circ$. Under this condition and for small rotation $\alpha$, it follows from equations (1) and (2) that the Faraday Rotation is

$$\alpha = \frac{1}{4} \frac{\Delta I}{I_m}.$$  \hspace{1cm} (3)

$I_m$ and $\Delta I$ are obtained at the lock in amplifiers #1 and #2 which are driven by reference signals generated by the chopper and the rotating modulator respectively (Figure 1). The output of the ratiometer is proportional to $\Delta I/I_m$. The constant of proportionality can be determined by producing a known rotation on the analyzer and noting the reading on the ratiometer. In the case of MCD, with magnetic field on, the difference in the transmitted intensity measures directly the difference in absorption
$P_1, P_2 = \text{Initial polarization of the modulated light before the cell.}$

$S_1, S_2 = \text{Final polarization of the modulated light after the cell.}$

$A = \text{Transmission axis of the analyzer.}$

$\alpha = \text{Rotation of the plane of polarization produced by the sample.}$

$\theta = \text{Angle made by each of the polarization axes in the rotating modulator.}$

$\phi = \text{Angle made by the transmission axis of the analyzer.}$

Figure 2
between left circularly polarized and right circularly polarized light. With the magnetic field off, a zero field absorption is obtained. It is then a simple matter to obtain MCD.

From measurements that have been recently made, the system is capable of measuring a rotation of about $4 \times 10^{-4}$ radians. Noise in the system is close to the shot noise limit.

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G. PARTICULATE FORMATION IN CESIUM-DEUTERIUM GAS CELLS*

(J. Camparo, J. Pietras, N. Bhaskar, W. Happer)

Several years ago in our laboratory Tam et al. discovered what has come to be known as "Laser Snow." (1) In mixtures of cesium vapor and helium gas they could excite the pressure broadened cesium second resonance lines with two fixed frequency blue lines of an Ar<sup>+</sup> laser (4545Å and 4579Å). The excited cesium atoms in the presence of hydrogen gas led to the formation of dense clouds of white particulates which fell under their own weight, hence the name laser snow. It was observed that these particulates were micron sized, and carried a positive charge (~ 10<sup>4</sup> e). They postulated that these particulates were actually CsH crystals, and from experimental evidence they proposed a mechanism for their formation:

\[
\text{Cs} + \text{hv} \rightarrow \text{Cs}^*(7\text{P})
\]

\[
\text{Cs}^*(7\text{P}) + \text{H}_2 \rightarrow \text{CsH} + \text{H}
\]

\[
\text{CsH} + \text{CsH} \rightarrow [\text{CsH}]_2
\]

The last step describing the molecular condensation into particulates.

Unfortunately, Tam’s work was limited by the imperfect overlap of the Ar<sup>+</sup> laser lines with the cesium second resonance lines (4555Å and 4593Å). In our present work we have been able to remove this limitation by exciting the cesium vapor on resonance with a tunable dye laser. An Ar<sup>+</sup> laser (Spectra-Physics 171-19) operating all lines in the ultraviolet (~ 2.5 W) pumps stilbene 3 dye in a Coherent 599-03E dye laser (200-300 mW). Stilbene 3 has a tuning range from 410 nm to 480 nm. This tunability has opened up a whole new range of possibilities for investigating these
particulates: we have observed them over a very wide range of cesium number densities by tuning the laser frequency to compensate for optical thickness; we have formed them in the absence of He; and we have investigated their behavior as a function of laser tuning.\(^{(2)}\)

As shown in Figure 1, our blue laser light is split into two parts: a strong pump beam, and a weak probe beam. With this arrangement we can pump the cesium atoms into CsH molecules and crystals, and then probe their return to Cs atoms when the pump light is shut off. This method is completely analogous to that used for studying spin relaxation in the dark, and in fact we have been able to attain measurable spin polarization in sample cells containing Cs, 20 torr deuterium, and an atmosphere of He at cesium number densities $\sim 10^{14}/\text{cm}^3$. (We have obtained 50% polarization at $[\text{Cs}] \sim 10^{13}/\text{cm}^3$.) We also have a red probe beam from a He/Ne laser travelling along the same path as the blue laser beam but in the opposite direction. Since this red light is only attenuated by scattering from the particulates, we can use a red filter to unambiguously monitor the Mie scattering.

The laser light is admitted to a cell constructed from alkali-resistant aluminosilicate glass (Corning 1720). Some of our cells contain internal electrode plates (Figure 1): molybdenium rods are sealed to the glass, and non-magnetic stainless steel plates are spot welded to the rods. We found that annealing these cells in a dry hydrogen atmosphere chemically reduced $\text{MoO}_3$, which getters both $\text{H}_2$ and $\text{D}_2$.

The cells contain cesium metal plus varying amounts of $\text{D}_2$ and He. We used $\text{D}_2$ instead of $\text{H}_2$ because the literature quoted an enormously high dissociation pressure for CsD,\(^{(3)}\) and we hoped to use this fact to study
Figure 1: Experimental set up. Typical power of the tunable dye laser beam ≈ 200 mW. The intensity of the weak probe beam is only (1/200)\(^{th}\) the intensity of the strong pump beam.
the atomic and molecular processes in the absence of particulate formation. However, on inspection of the original data of Hackspill and Borocco\(^{(4)}\) we found that their empirical fit to the data is some three orders of magnitude too high. Their data is fit more reasonably by the formula,

\[
\log_{10} P = 11.27 - \frac{5419}{T}
\]

(2)

where \(P\) is the dissociation pressure of CsD in torr, and \(T\) is the absolute temperature. This formula leads to dissociation pressures of CsD which are only about a factor of two greater than those of CsH, and so little is gained by using \(D_2\) instead of \(H_2\).

By measuring the terminal velocity of these particulates as they fall through the He vapor, we have been able to estimate their size by using Stokes law. To measure the velocity we displace the He/Ne beam a distance \(d\) below the strong pump beam so that its transmitted intensity is attenuated by Mie scattering from the particulates. A certain time \(\Delta t\) after the pump beam is blocked, the transmission of the He/Ne beam will increase (Figure 2). Thus, \(\Delta t\) is the time required for the particulates to fall from the pump beam through the He/Ne beam. In this manner we have determined that the CsD particulates are about one micron in diameter. As shown in Figure 2 \(\Delta t\) seems to decrease with decreasing laser power; this would imply that particulate size increases as the exciting photon flux decreases.

As in the original work of Tam et al.\(^{(1)}\) we find that these CsD particulates are charged. Since individual particulates are clearly visible through a microscope as they fall through the red He/Ne light, it is a simple matter to apply an electric field between the two plates which just
Figure 2: Transmitted intensity of He/Ne light as particulates fall through He/Ne beam which is a distance $d$ below blue pump light. Three data sets are shown, where different neutral density filters were placed in front of pump beam (N.D. = 0, 0.3, 0.5). $t_0$ is the time the pump light was blocked, and $\tau$ is the time when the transmitted He/Ne intensity increased. We can compute the terminal velocity of these particles: $v = d/\Delta t$, $\Delta t = \tau - t_0$. 
cancels the effect of gravity. In this way we can measure the charge on the particles, and at an optical depth of > 2 cm we find that these particles carry a positive charge \( \sim 10^2 \) e.

At this optical depth an electric field (\( \sim 100 \text{ V/cm} \)) which is pulsed on will quickly sweep all the particles out of the red He/Ne beam, and there will be no visible Mie scattering. If we tune the laser closer to resonance (optical depth \( \sim 2-3 \) mm) the electric field appears to have no effect on the red Mie scattering. We conclude that for the pump light tuned very near resonance these particulates are either minimally charged or completely neutral.

In addition we noticed that the particulates do not disappear uniformly throughout the entire length of the red beam as the electric field is pulsed on. We biased the electrode plates such that the particulates would be deflected upwards, and tuned the laser away from resonance (optical depth > 2 cm). When the field was pulsed on, those particulates nearest the pump laser entrance were deflected upwards first, and then those further away were deflected out of the He/Ne beam in turn. The effect can best be described as a red scattering wave retreating from the entrance face of the cell. We then tuned the laser closer to resonance, and observed that this red scattering wave changed direction: those particulates furthest away from the pump beam entrance were deflected upwards first, and then those closer to the entrance were deflected in turn.

It is easy to show that the acceleration of these charged particulates out of the red He/Ne beam is directly related to their charge to mass ratio. One possible explanation for this red scattering wave is that the charge to mass ratio of these particulates is not uniformly distributed.
throughout the length of the pump beam. Since the distribution of $q/M$ for these particulates would then appear to be dependent on laser tuning, we could conclude that the magnitude of $q/M$ for a particulate depends on the photon flux in the neighborhood of the particulate. Also, since this red scattering wave changes direction, it would seem likely that $q/M$ must have an extremum in its dependence on photon flux.

We have carried out some preliminary experiments to investigate the changes in transparency of the vapor cells when particulates are formed by the blue resonant light. We found that very substantial changes in the transparency did occur and that at least two mechanisms are operating. First, the incorporation of cesium atoms into the particulates depresses the atomic cesium number density and thereby increases the transparency of the vapor to the blue resonant light. Secondly, the particulate clouds which are formed by the blue laser light can become so dense that they cause significant attenuation of the laser beams. The attenuation due to particulates affects both the blue pump light and also the red, HeNe probe light. In all cases we have studied the transparency of the vapor for the blue pumping light increased with time after the pumping light was turned on.

As shown in Figure 1 the rotating chopper wheel admits the strong pump beam to the cell; the decrease in the number of absorbers in the pump beam’s path depends on the incident laser intensity ($\Delta N = \nu_0^{3/4}$). The pump beam is then blocked, and the transmission of the probe beam is monitored with a photodiode and recorded with a Nicolet 1170 multichannel averager. As the vapor returns to its unperturbed state the transmitted intensity of the probe decreases.
Our results show that at least two time domains are involved in this relaxation of the vapor. When the pump beam is first turned off, absorbers quickly appear in the volume of the probe beam at a rate $\sim 30 \text{ sec}^{-1}$. This is followed by a much slower decrease in the transparency of the vapor which takes $\sim 10 \text{ sec}$ to reach its steady-state value. The difference between the asymptotic transparency of the first transient and the final transparency of the vapor is $\sim 35\%$. If an electric field ($\sim 100 \text{ V/cm}$) is applied between the two electrode plates, the rate of the first transient is about four times greater ($\sim 120 \text{ sec}^{-1}$), and no slow transient is observed.

We have found that the transmitted intensity of the probe beam during the fast transient has the functional form:

$$\ln \left( \frac{I(t)}{I_0} \right) = A e^{-\gamma t}$$

where $I_0$ is the asymptotic value of the transmitted intensity; $\gamma$ is the characteristic rate of the fast transient; and $A$ is a constant. Some very preliminary results would indicate that the increased rate of the "field on" transient depends on the photon flux and duration of the strong pump beam.

Although our data shows that the bleaching of the vapor due to the removal of cesium atoms outweighs any increase in opacity due to Mie scattering of the particulates, the attenuation due to Mie scattering is certainly comparable to the attenuation due to the change in the atomic cesium number density. We have performed an experiment where the cell was illuminated with $300 \text{ mw}$ of blue dye laser light and particulate buildup
was allowed to come to equilibrium in the absence of an electric field. The electric field was suddenly pulsed on and a substantial change in the transparency of the vapor was observed. When the laser was tuned so that the optical depth exceeded the cell length (optical depth $\gtrsim 2$ cm) the application of the electric field caused a substantial ($\sim 20\%$) increase in the transmission of the vapor which was due to the removal of Mie scattering particles from the laser path by the electric field.

When the laser was tuned close to resonance so that the optical depth was about 1.5 cm or less (about 3/4 of the cell length) the application of an electric field caused the transmission of the vapor to decrease by about $30\%$. We do not understand this phenomenon, but it is completely reproducible. Somehow the presence of particulates makes it easier for the blue pumping light to remove free cesium atoms from the vapor. Perhaps the particulates serve as local sinks for newly created CsH diatomic molecules or small polymer clusters and without the particulates the many excited atoms and vibrationally excited $D_2$ molecules destroy the CsH polymers and form free cesium atoms. Further studies are underway to investigate the curious interplay of particulates with the bleaching efficiency for atomic cesium.

The particulates also cause a substantial decrease in the transparency of the vapor for red HeNe laser light. When an electric field is applied to the cell the particulates are swept out of the laser beam and the transmission of the HeNe laser beam increases. In contrast to the situation for the transmission of resonant light, the application of an electric field always leads to an increase in the transparency of the vapor to the HeNe light irrespective of the tuning of the blue laser.
Tam et al.(5) studied the emission spectra of CsH molecules by exciting a mixture of cesium vapor and 100 torr of He gas using the 4579 Å Ar⁺ laser line. The laser excited fluorescence spectra consists of a series of P and R doublets and emission bands from Cs₂ molecules. In a similar experiment using the rotating chopper wheel we studied the intensity of the spectrally dispersed fluorescence signal from CsH as a function of time after the light is turned on. We observe an increase in the fluorescence intensity of one of the CsH doublets as a function of time. The time constant of this transient is \( \approx 300 \text{ sec}^{-1} \). We observe no time dependence of the Cs₂ emission. Further study is underway to understand this transient.

In summary, we have shown that a tunable cw dye laser is a very powerful tool for investigating the properties of the photogenerated particulates in mixtures of cesium vapor and deuterium gas. We have shown that substantial changes of the vapor opacity are caused by the blue second resonance light from the cw dye laser and that the changes in opacity are due to both Mie scattering and to changes in the number density of free cesium atoms. Recovery of the opacity in the dark depends critically on whether an electric field is used to sweep the particulates out of the beam. These preliminary studies will be followed up by more detailed experiments to determine the main mechanisms involved in bleaching, particulate formation, particulate charge and recovery of the cells to normal conditions.

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(2) To be published.

(4) L. Hackspill and A. Borocco, Bull. de La Société Chimique de France, 6, 91 (1939).

H. SPIN DESTRUCTION IN COLLISIONS BETWEEN CESIUM ATOMS*

(J. Camparo, J. Pietras, N. Bhaskar, W. Happer)

The evolution of spin polarization due to collisions between ground-state atoms in $^2S_{1/2}$ states is known to be dominated by spin exchange, as was first pointed out by Purcell and Field$^1$ and by Wittke and Dicke.$^2$

An atom with a $^2S_{1/2}$ ground state and a nuclear spin I will have two Zeeman multiplets of total angular momentum $F = I + 1/2$ and $F = I - 1/2$. Spin exchange collisions are extremely effective in destroying the population imbalance $<I \cdot S>$ between these two multiplets. However, spin exchange collisions conserve the total spin angular momentum of the colliding pair of atoms. Thus, spin exchange collisions have no effect on the relaxation of $<F_z>$, the projection of the total spin, nuclear plus electronic, along the direction of the ambient magnetic field.$^3$

Of course rigorous conservation of spin cannot occur since various spin-spin and spin-orbit interactions come into play during a collision between $^2S_{1/2}$ atoms. These interactions can couple the spin to the translational angular momentum of the colliding pair of atoms. In the present work we have seen relaxation due to interactions of this type.

The apparatus used in this work consisted of an argon ion laser (Spectra-Physics 171-19) with $\geq 2.5$ W of power in the ultraviolet lines pumping a cw dye laser (Coherent Radiation 599-03(E)) operating with Stilbene-3 dye. Dye laser output powers of 200-300 mW could be obtained at the blue $D_1$ second resonance line of cesium (4593 Å). The dye laser frequency could be held constant to within 25 GHz.

The sample cells had linear dimensions of about 2 cm and were constructed from alkali-resistant aluminosilicate glass (Corning 1720). A
small amount of cesium metal was distilled into the cell and helium and nitrogen buffer gases were added before seal off. The buffer gas served three main purposes, spin confinement, pressure broadening of the optical absorption line, and fluorescence quenching. Quenching is essential in these high-density experiments to prevent multiply scattered unpolarized first resonance light from depolarizing the spins. A few hundred torr of nitrogen was sufficient to quench effectively. The pressure broadening of the optical absorption line exceeded the laser linewidth, and further frequency stabilization of the laser was not necessary.

The cell was situated in an oven with a slight upward temperature gradient which prevented condensation of the cesium vapor on the cell windows. A static magnetic field of a few gauss was produced by Helmholtz coils, and a radiofrequency magnetic field could be applied with a small orthogonal set of coils.

We measured spin relaxation in the dark by a variant of the techniques introduced by Franzen(4) and Bouchiat.5 The linearly polarized dye laser output beam was split into two parts as described in our report on Cs photochemistry.6 The weak probe beam was further attenuated by neutral density filters until its intensity was 200 times weaker than that of the pump beam. Both beams were circularly polarized by a λ/4 plate before entering the cell. A rotating chopper wheel allowed the strong pump beam to enter the cell for about 10 msec. Equilibrium polarizations of 10% to 60% were produced by the pump beam, which had a mean pumping rate of about 5000 sec⁻¹. The spin polarized atoms were confined to a cylindrical volume of about the same radius (a = 1 mm) as the pump beam by the high buffer gas pressure.
After the pump beam was blocked by the chopper, the probe beam continued to pass through the cell along the same optical path as the pump beam. The probe-beam radius (b = 2 mm) was about twice as big as the pump-beam radius. The pumping rate of the probe beam was negligible. The transmitted intensity $I$ of the probe beam was monitored with a silicon photodetector while the transmitted intensity decreased with time. The signal to noise ratio of the transient was improved by repetitively averaging the signal with a Nicolet 1170 multichannel averager for about one minute. After most of the spins had relaxed a pulse of rf was applied at the magnetic resonance frequency of the cesium atoms to destroy the remaining spin polarization and to define the transmitted intensity $I_u$ for unpolarized atoms. The probe beam was then blocked for a few milliseconds to determine the dark current of the detection system.

The variation in the transmitted intensity $I$ is due to the variation of the local spin polarization in the path of the probe beam. From theoretical arguments (7) we find that our data should be expressed in the form

$$\ln \ln \left( \frac{I}{I_u} \right) = \text{const.} - \gamma_0 t - \ln \left( a^2 + b^2 + 4Dt \right)$$

(1)

In this expression $D$ is the diffusion constant of polarized atoms through the buffer gas, and $\gamma_0$ is the bulk spin decay rate in the absence of any diffusion.

As shown in Figure 1 we plot this quantity as a function of time. Note that quite good straight lines of slope $-\gamma$ are obtained. From (1) we see that the slope can be interpreted as
Figure 1: Temperature dependence for spin relaxation in the dark for cell C.
\[- \frac{\text{dy}}{\text{dt}} = \gamma = \gamma_0 + \frac{4D}{a^2 + b^2 + 4Dt} \quad (2)\]

The first term \(\gamma_0\) is the bulk relaxation rate while the second term accounts for diffusion of spin polarized atoms out of the probe beam. In our experiments \(D \approx 0.5 \text{ cm}^2 \text{ sec}^{-1}\) and \(a^2 + b^2 = 5 \times 10^{-2} \text{ cm}^2\) so the diffusional contribution to the decay rate is

\[\gamma_D = \frac{4D}{a^2 + b^2 + 4Dt} \approx 40 \text{ sec}^{-1} \quad (3)\]

From Figure 1 we see that the measured slopes are much greater than the estimate (3) of the diffusion rate. Note that in our work it is not very useful to discuss the diffusion in terms of normal modes of the cell, since dozens of normal modes are excited. The formula (2) can be obtained by summing over many modes.

Data like that of Figure 1 were obtained from three different cells, and the measured decay rates \(\gamma\) are plotted versus the cesium number density \((8)\) in Figure 2. After accounting for the effects of the nuclear spin we find that the rate constant is

\[K = \frac{\text{dy}}{\text{d}[\text{Cs}]} = 7.88 \times 10^{-12} \text{ cm}^3 \text{ sec}^{-1} \quad (4)\]

We may define a mean cross section

\[\sigma = K(\bar{v})^{-1} = 2.03 \times 10^{-16} \text{ cm}^2 \quad (5)\]

where \(\bar{v} = (\frac{16kT}{\pi m})^{1/2} = 3.88 \times 10^4 \text{ cm sec}^{-1}\) is the mean relative velocity of
Figure 2: Dependence of relaxation rate $\gamma$ on cesium number density for three sample cells. The buffer gas pressures at 20°C were: cell A: 200 Torr $N_2$, 550 Torr He; cell B: 200 Torr $N_2$, 530 Torr He; cell C: 760 Torr $N_2$, 2090 Torr He.
a pair of cesium atoms at 200°C. Cell C, made by cooling at constant pressure the same gas mixture contained in cell A to liquid nitrogen temperature before seal off, contained 3.8 times as much buffer gas density as cell A. Since there is no significant difference between the rate constants for cell A and C we conclude that three-body effects\(^9\) are negligible and the temperature dependent relaxation is primarily due to cesium-cesium binary collisions.

In a cell with high buffer gas pressure we expect the diffusional relaxation rate to be less and the relaxation rate due to collisions between cesium atoms and buffer gas atoms to be greater than in a cell at low buffer gas pressure. These effects partially compensate; they are not expected to depend strongly on temperature, but they may account for the slight systematic differences between data from cells A, B and C in Figure 2.

The cross section \(\sigma = 2.03 \times 10^{-16} \text{ cm}^2\) measured here for electron spin destruction due to cesium-cesium collisions is much smaller than the cross section for spin exchange\(^10\) \(\sigma_x = 2.2 \times 10^{-14} \text{ cm}^2\), but much larger than the cross section for spin destruction in alkali-noble gas collisions\(^11\) \(\sigma \lesssim 10^{-19} \text{ cm}^2\). In alkali noble gas collisions the spin depolarization is known to be due to the spin-rotation interaction\(^12\)

\[
H_{SN} = \gamma \hat{S} \cdot \hat{N}
\] (11)

where the coupling constant \(\gamma\) is of the order \(10^{-4} \text{ cm}^{-1}\). A similar spin-rotation interaction must exist for a pair of cesium atoms on the \(^3\Sigma\) ground-state potential curve, but there is no obvious reason why it should be big enough to account for the relaxation rates observed in this...
experiment. However, a pair of cesium atoms on the \(^3\Sigma^+\) ground state potential curve is also subject to the spin-spin interaction

\[
H_{SS} = \frac{2}{3} \lambda [S_x S_x - S_z S_z]
\]

(12)

which does not exist for an alkali-noble gas pair. Furthermore, the interaction constant \(\lambda\) is known to be quite large, for example, \((13)(14)\) \(\lambda = 2.0\ \text{cm}^{-1}\) for \(O_2\), \(\lambda = 5.3\ \text{cm}^{-1}\) for \(SO\). It is reasonable to suppose that \(\lambda = 1\ \text{cm}^{-1}\) for a pair of cesium atoms on the \(^3\Sigma^+\) potential curve at the distance of closest approach during a collision. The spin-spin interaction is of the right order of magnitude to account for spin destruction rates reported here.

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I. SPIN EXCHANGE AND RELAXATION IN Na–NOBLE GAS MIXTURES
(B. Suleman, M. Hou, N. Bhaskar, T. McClelland, W. Happer)

We have studied the relaxation of optically pumped sodium vapors in
diamagnetic gases Helium and Xenon. The apparatus (Figure 1) used to
measure the relaxation rates was essentially the same as described in an
earlier report. (1) For better signal to noise ratio and higher time reso-
lution a Nicolet Model SD-71B multichannel analyzer was used instead of an
eductor for averaging the transmission of a weak probe beam. Circularly
polarized pump and probe beams were used to monitor the relaxation of the
observable \( \langle S_z \rangle \). During measurements of \( \langle S_z \rangle \) we tuned the laser to the
center of gravity of the two hyperfine levels to avoid any hyperfine pump-
ning and production or monitoring the observable \( \langle I \cdot S \rangle \). For measuring the
observable \( \langle I \cdot S \rangle \) a linearly polarized pump and probe was used and the laser
was tuned such that it overlapped more strongly with one of the two hyper-
fine levels. Reproducible results could be obtained only when the dye
laser was operated in a single mode, since the relative amounts of \( \langle S_z \rangle \)
and \( \langle I \cdot S \rangle \) produced depend critically on the laser frequency.

The observables \( \langle S_z \rangle \) and \( \langle I \cdot S \rangle \) relax to a Boltzmann distribution after
the pump beam is turned off. A typical trace of the signal, which shows
the change in transmission of probe with time, is shown in Figure 2. The
probe intensity \( I(t) \) at time \( t \) after passing through an optically thick
vapor can be written as

\[
\frac{T}{T_1} = \ln \frac{I(t)}{I(\infty)} + \ln \frac{I(o)}{I(\infty)} \quad (1)
\]

where \( I(\infty) \) is the intensity when the vapor has returned to Boltzmann
Figure 1
Figure 2
equilibrium and $T_1$ is the decay constant of the observable being measured. If we observe either $\langle S_z \rangle$ or $\langle I \cdot S \rangle$ for a sufficiently long time, we always find that the observables decay with a single exponential, i.e.

$$\frac{d}{dt} \langle S_z \rangle = -\frac{1}{T_1} \langle S_z \rangle \quad (2)$$

$$\frac{d}{dt} \langle I \cdot S \rangle = -\frac{1}{T_2} \langle I \cdot S \rangle \quad (3)$$

A typical plot of $\ln \ln \left[ \frac{I(t)}{I(\infty)} \right] \text{vs} \ t$ is shown in Figure 3. From the slope of these lines the decay rate $1/T_1$ or $1/T_2$ was measured.

Four major relaxation mechanisms contribute independently to the experimentally observed rates $1/T_1$ and $1/T_2$.

1) **Diffusion:** The optically pumped sodium vapor diffuses through the buffer gas (Helium) to the walls of the cell. Every collision with the cell walls completely destroys the polarization. The slowest decay rate $1/T_D$ of any observable in cylindrical cells of length $L$ and radius $r$ is

$$\frac{1}{T_D} = \left[ \frac{\pi^2}{L^2} + \frac{(2.405)^2}{r^2} \right] \times D_0 \left( \frac{760}{P} \right)$$

where $D_0$ is the diffusion constant at 760 Torr of buffer gas which has a pressure $P$ in the cell.

2) **Binary Collisions:** The spin orbit interaction in sudden binary alkali-noble gas collisions\(^{(2)}\) causes the observable $\langle I \cdot S \rangle$ to relax with a single time constant\(^{(3)}\) $1/T_H$ such that

$$\frac{1}{T_H} = [N] \bar{v} \sigma_B$$
8 FAST DECAY
\[ \gamma = 640 \text{sec}^{-1} \]

7 SLOW DECAY
\[ \gamma = 239 \text{sec}^{-1} \]

UNIT OF TIME: 268 \(\mu\text{sec}\)

Figure 3
where \([N]\) is the number density of the noble gas, \(\bar{v}\) is the average relative velocity of the colliding pair and \(\sigma_B\) is the electron randomization cross section, for binary alkali-noble gas collisions.

The slowest relaxation rate of the observable \(\langle S_z \rangle\) due to binary collisions is \(f/T_H\), where \(f\) is the slowing down factor due to the nuclear inertial effect.\(^{(4)}\) It varies between 1/6 and 1/8 for Na(I = 3/2) depending on whether the Na vapor is in spin temperature equilibrium or not.

3) Three Body Collisions: If the sodium and noble gas atoms collide in the presence of a third particle, alkali-noble gas molecules can be formed due to weak attractive Van der Waal's forces. The observable \(\langle S_z \rangle\) relaxes with a time constant \(1/T_S\). During the lifetime of the Van der Waals molecule the atomic populations are redistributed among the Zeeman sublevels in a particular hyperfine multiplet. Very few transitions take place between hyperfine levels, and as a consequence \(\langle \mathbf{I} \cdot \mathbf{S} \rangle\) does not relax.\(^{(5)}\) The decay rate \(1/T_S\) depends on the external magnetic field and on the pressure of the buffer gas which serves as a third body.

4) Spin Exchange Collisions: Two colliding alkali atoms can inter-change their spins during collision. This spin exchange can very effectively relax \(\langle \mathbf{I} \cdot \mathbf{S} \rangle\). If \(\langle S_z \rangle\) is maintained at zero then the relaxation rate of \(\langle \mathbf{I} \cdot \mathbf{S} \rangle\) due to spin exchange is \(^{(4)}\)

\[
\frac{1}{T_{\text{ex}}} = [\text{Na}] \bar{v} \sigma_{\text{ex}}
\]

where \([\text{Na}]\) is the sodium number density and \(\sigma_{\text{ex}}\) is spin exchange cross section.
From the above discussion it is clear that the relaxation rate $1/T_1$ of $\langle S_z \rangle$ is

$$\frac{1}{T_1} = \frac{1}{T_D} + \frac{f}{T_H} + \frac{1}{T_S}$$

(5)

The relaxation rate $1/T_2$ of $\langle I\cdot S \rangle$ is

$$\frac{1}{T_2} = \frac{1}{T_D} + \frac{1}{T_H} + \frac{1}{T_{ex}}$$

(6)

Discussion of Results: The depolarization cross section for Na-He collisions is very small ($\sim 10^{-26}$ cm$^2$) therefore Helium merely serves as a buffer gas or as a third body. To get the diffusion constant in Helium we measured the relaxation of $\langle S_z \rangle$ in cells with no xenon. A plot of $1/T_1$ vs $P^{-1}$ is shown in Figure 4. From the slope of the line we get

$$D_0(\text{Na-He}) = (0.35 \pm 0.19) \text{ cm}^2/\text{sec}$$

The relaxation rates of $\langle I\cdot S \rangle$ and $\langle S_z \rangle$ at different temperatures are shown in Figure 5. From equations 5 and 6 we have

$$\frac{1}{T_2} \text{ (no xenon)} = \frac{1}{T_D} + \frac{1}{T_{ex}}$$

(7)

$$\frac{1}{T_2} \text{ (2 torr xenon)} = \frac{1}{T_D} + \frac{1}{T_{ex}} + \frac{1}{T_H}$$

(8)

$1/T_{ex}$ is the only term which depends on sodium number density. From the slope of two parallel lines we get

$$\sigma_{ex} = 1.57 \times 10^{-14} \text{ cm}^2$$

64
He(46 Torr) + N₂(10 Torr) + Xe(2 Torr)

He(46 Torr) + N₂(10 Torr)

Figure 5
The difference between the relaxation rates of \(\langle I \cdot S \rangle\) with 2 torr of xenon and with no xenon at a fixed sodium number density gives us \(1/T_H\) (see equations 7 and 8), the relaxation rate due to Na-Xe binary collisions.

\[
\frac{1}{T_{xe}} = 232 \text{ Sec}^{-1} \text{ per torr of Xe.}
\]

So the binary sodium spin depolarization cross section is

\[
\sigma_B (\text{Na-Xe}) = 1.19 \times 10^{-19} \text{ cm}^2.
\]

**Three body effects:** The relaxation rate of \(\langle S_z \rangle\) at different helium pressures for 2 torr of xenon is shown in Figure 6. The absence of a straight line clearly indicates that \(\langle S_z \rangle\) does not relax due to binary collisions alone. At high helium pressures the Na-Xe molecules break up more rapidly due to collisions with He atoms and there is less time available for spin relaxation within the Van der Waals molecule. This decreases the relaxation rate \(1/T_S\). At lower helium pressure (\(< 46\) torr) the relaxation due to Van der Waals molecules is more dominant.

To further investigate the three-body effect, the external magnetic field \(H_o\) was varied. The relaxation rate of \(\langle S_z \rangle\) vs \(H_o\) is shown in Figure 7. At high fields the total angular momentum \(\vec{F} (= \vec{I} + \vec{S})\) precesses around \(H_o\) instead of coupling to the rotational angular momentum \(\vec{N}\) of the tumbling Na-Xe molecule. This decoupling slows down the relaxation \(1/T_S\), and hence the total relaxation rate decreases with increasing \(H_o\). From the half width of the curve the estimated life time of the Van der Waals molecules is of the order of \(10^{-8}\) sec. A systematic study of
Figure 7

RELAXATION RATE sec^{-1}

Na+46 Torr He + 10 Torr N₂ + 2 Torr Xe

EXTERNAL FIELD H₀ (gauss)
the three-body effects is necessary for a better understanding of the relaxation mechanism of the Na-Xe system. We plan to start these experiments in the near future.

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(1) CRL Progress Report #29, March 31, 1979, p. 13.
II. ENERGY TRANSFER AND RELAXATION IN SMALL POLYATOMIC MOLECULES

A. METASTABLE ENERGY DISTRIBUTIONS IN COF$_2^*$

(R. Bohn, G. W. Flynn)

The molecule COF$_2$ provides a system which exhibits a variety of interesting phenomena. Since it absorbs many CO$_2$ laser lines, COF$_2$ can be easily excited in the infrared. There have been reports of visible emission$^{(1)}$ and photofragmentation$^{(2)}$ following intense laser excitation of this molecule.

We have studied the intermode energy transfer of COF$_2$ following excitation of the $v_2$ symmetric C-F stretching frequency. Fluorescence emission has been observed from all fundamental levels on time scales ranging from microseconds to milliseconds after laser pumping.$^{(3)(4)}$ A major question which we have been able to answer in the past ye- is the mechanism for filling of the $v_4$ antisymmetric C-F stretch mode. This state is 282 cm$^{-1}$ higher in energy than the initially excited $v_2$ state. The fluorescence from $v_4$ exhibits extremely unusual behavior since it consists of both a fast exponential growth and a slow exponential growth followed by overall slow decay. Kinetically such a pattern of dynamic energy flow is remarkably rare, and we have determined that $v_4$ is a level that empties faster than it fills. The overall mechanism for energy transfer involving $v_4$ is

\[
\text{Laser Excitation} \quad \text{COF}_2(0) + h\nu_L \rightarrow \text{COF}_2(v_2) \]

(1)

\[
\text{Endothermic V-V Energy Transfer} \quad \text{COF}_2(v_2) + M \rightarrow \text{COF}_2(v_4) + M - 282 \text{ cm}^{-1} \]

(2)
Resonant V-V Energy Transfer
\[ \text{COF}_2(v_4) + M \rightleftharpoons \text{COF}_2(v_3 + v_5) + M \] (3)

Reverse Ladder Climbing V-V Energy Transfer
\[ \text{COF}_2(v_3 + v_5) + \text{COF}_2(0) \rightleftharpoons \text{COF}_2(v_3) + \text{COF}_2(v_5) \] (4)

The levels \(2v_3\) and \(2v_5\) may also be involved in steps (3) and (4). The crucial feature of this scheme is that step (2) occurs with about 1/5 the probability of step (3) thus leading to the unusual fluorescence behavior observed for the \(v_4\) state.

We are currently developing a consistent set of coupled differential equations which will allow us to describe fully the energy transfer pathway for all the modes of \(\text{COF}_2\). Currently we are faced with only one vexing question. Step (2) competes with the exothermic V-V event

Exothermic V-V Energy Transfer
\[ \text{COF}_2(v_2) + M \rightleftharpoons \text{COF}_2(v_6) + M + 199 \text{ cm}^{-1} \] (5)

The overall fluorescence pattern is a sensitive function of this competition and we have not yet been able to establish the degree of importance of the event (5). We expect to determine the cross section for this process in the next few months.

In addition to the visible emission(1) and photofragmentation(2) phenomena mentioned above, we have also shown that \(\text{COF}_2\) is an excellent candidate for a new class of laser system.(5) Gain calculations suggest the possibility of laser action on the \(v_1 + v_4\), \(v_1 + v_6\), \(v_1 + v_3\), and/or \(v_1 + v_5\) transitions.
*This research was also supported by the National Science Foundation under Grant NSF-CHE77-24343.


B. VIBRATIONAL TEMPERATURE MEASUREMENT IN STRONGLY PUMPED COF₂*

(M. I. Lester, G. W. Flynn)

Infrared laser-induced fluorescence studies in small polyatomic molecules have shown that most vibration to vibration (V-V) energy transfer processes occur on a relatively fast time scale compared to overall vibration to translation/rotation (V-T/R) relaxation.\(^1\) The V-V energy transfer processes fall into two basic categories: intramode processes which redistribute excess vibrational energy throughout the various levels of a particular vibrational mode and intermode processes which couple the distinct vibrational modes of the molecule. The intramode processes are controlled by near-resonant 'ladder-climbing' collisions of the form

\[
    M((v_j-1)v_j) + M(v_j) \rightleftharpoons M(v_jv_j) + M(0) \tag{1}
\]

which typically occur in 1-10 gas kinetic collisions. Intermode vibrational energy transfer usually requires several hundred gas kinetic collisions through nonresonant processes of the type

\[
    M(v_i) + M \rightarrow M(v_j) + M + \Delta E = E_i - E_j \tag{2}
\]

where \(v_j\) is the quantum number of the mode \(v_j\) having energy \(E_j\). Following state selective excitation of the molecule with a CO₂ laser, these collisional processes can establish a distinctly non-thermal steady state population distribution in the vibrational modes.\(^2\) Under the steady state condition, the population in each mode can be described in the harmonic oscillator limit by a characteristic vibrational temperature, \(T_1\).\(^2\) Further, the vibrational temperatures of individual modes are...
related strictly by the mechanism which couples the modes. Prior to overall vibrational relaxation, these vibrational temperatures are in general different from the instantaneous translational/rotational temperature, $T$. Under strong excitation conditions, collisions can also serve to enhance the absorption of the molecule. If the laser pulse duration is long compared to the mean time between molecular collisions, ladder climbing collisions (1) can remove population from the pumped state and allow the molecule to exceed the conventional 2-level saturation limit of 1/2 photon absorbed per molecule. Thus, collisional processes can lead to multiphoton absorption as well as highly non-equilibrium vibrational energy distributions.

We are currently investigating these vibrational energy distribution and excitation effects in carbonyl fluoride (COF$_2$). This system is a particularly interesting one to study under intense IR excitation conditions since there have been recent reports of photofragmentation,$^5$ COF$_2$ + nhv (10.6$\mu$m) $\rightarrow$ COF + F

and reverse internal conversion$^6$ with the resultant emission of vis-UV luminescence under similar conditions. In addition, the kinetic pathway information derived from these studies can compliment the results obtained from IR laser-induced fluorescence studies. We have begun measurements of the mode vibrational temperatures in COF$_2$ using the cold gas filter technique.$^7$$^8$

The cold gas filter technique provides a relative measurement of the total fluorescence intensity at a frequency $\nu_j$ from all states in the particular mode, $I_j$, to the total fluorescence intensity minus the...
v_j = 1→0 component, I_{v_j}^t - I_1^t. This is accomplished by observing the fluorescence emanating from a particular mode through a cell of length L' placed between the fluorescence window and the detector. The fluorescence intensity is measured with the cell empty and with the cell filled to some pressure P' of the gas under study which removes the v_j = 1→0 emission. From the ratio of these fluorescence intensities, the vibrational temperature can be determined from the expression

\[ \frac{I_{v_j}^t - I_1^t}{I_{v_j}^t} \sim 1 - \left(1 - e^{-\frac{h\nu_i}{kT_i}}\right)^2 \]  

(4)

where \( \nu_i \) is the frequency of mode i with vibrational temperature \( T_i \).

Note that equation (4) is strictly valid only for a diatomic molecule in the harmonic oscillator limit, yet it can be used for a polyatomic system to yield a reasonable estimate of the vibrational temperatures in the individual modes.

Although the cold gas filter is designed to eliminate all fluorescence emanating from the v=1 level, in practice it only removes 85-95% of this emission for heavy polyatomics. The remainder of the light leaks through the filter because it terminates on high J levels in the ground state (v=0) with very small population. In principle, this emission could be eliminated by significantly increasing the pressure (P') in the cold gas filter above the sample cell pressure, but this introduces additional complications due to pressure broadening. The initial work using the cold gas filter technique to measure vibrational temperatures attempted to correct for this leftover emission by an extrapolation procedure. In the present measurements, we have attempted to improve the accuracy of the
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technique by employing a calibration procedure for the cold gas. The calibration consists of using a weak laser source to excite only into the v=1 level of a given mode. By monitoring the light through the cold gas filter under low level excitation, we can determine the amount of this residual light emission.

We have measured the vibrational temperature of the carbonyl mode $v_1$ ($\nu 2000 \text{ cm}^{-1}$) as a function of COF$_2$ pressure for TEA laser excitation. The carbonyl stretch is populated from pumped C-F symmetric stretch $v_2$ via the processes (9):

$$\text{COF}_2(0) + h\nu (10.6 \mu) \rightarrow \text{COF}_2(v_2) \text{ laser pump}$$

$$2\text{COF}_2(v_2) \leftrightarrow \text{COF}_2(0) + \text{COF}_2(2v_3) \text{ V-V up pumping}$$

$$\text{COF}_2(2v_2) + M \rightarrow \text{COF}_2(v_1) + M \text{ intermode V-V}$$

Steps (6) and (7) occur in approximately 30 gas kinetic collisions. The intermode V-V step is atypically fast since it is aided by Fermi of the $2v_2$ and $v_1$ states. Because the V-V processes (6) and (7) are nearly resonant, the vibrational temperatures of the pumped mode carbonyl stretch $v_1$ should be essentially the same ($T_1 = T_2$).

The vibrational temperature of the $v_1$ mode is plotted as a function of COF$_2$ pressure in Figure 1. The observed pressure dependence is qualitatively explained in the following way. As the number of over the fixed laser pulse width (2-3 µsec) increases, V-V ladder (6) should become more important in enhancing the level of excitation of the coupled $v_1$ and $v_2$ modes. Further, increasing the pressure...
pressure broaden the absorption linewidth leading to increased overlap with the laser line profile. The maximum temperature reached to date, even at higher pressures is approximately 1500 K. This is surprisingly low considering that COF$_2$ both photofragments and emits vis-UV luminescence under similar excitation conditions. This suggests that the initial energy distribution produced by the laser and probably not the steady state energy distribution caused by collisions is responsible for these processes. Collisions probably play at most a minor role (e.g. reducing rotational bottlenecks).

We have also measured the vibrational temperature of the antisymmetric C-F stretch mode $v_4$ ($\nu = 1244$ cm$^{-1}$). The COF$_2$ pressure dependence of these results are also shown in Figure 1. At every pressure studied, the $v_4$ mode has a significantly lower temperature than $v_1$. Since $v_1$ and $v_2$ are expected to be at the same temperature, this suggests that the $v_4$ mode is endothermically coupled to $v_2$ via the intermode process

$$\text{COF}_2(v_2) + M \leftrightarrow \text{COF}_2(v_4) + M - 290 \text{ cm}^{-1} \tag{8}$$

IR fluorescence studies have indicated that this step occurs in $\sim$ 500 gas kinetic collisions.$^{(10)}$ The steady state condition for this process, on a time scale short compared to $V$-$T/R$ relaxation, leads to a relationship between the temperatures $T_2$ and $T_4$ of the modes $v_2$ and $v_4$ given by

$$\frac{v_2}{T_2} - \frac{v_4}{T_4} = \frac{(v_2 - v_4)}{T} \tag{9}$$

where $T$ is the instantaneous translational/rotational temperature. For $T = 300$ K and $v_2$ (964 cm$^{-1}$) < $v_4$ (1244 cm$^{-1}$), equation (9) yields the
result \( T_4 < T_2 \) as observed. For an initial excitation level of \( T_2 \sim 1200 \) K, equation (9) predicts a vibrational temperature of \( \sim 700 \) K for \( \nu_4 \). This simple 3 mode picture \((\nu_2, \nu_1, \nu_4)\) is in amazingly good agreement with the observed vibrational temperature for \( \nu_4 \) of \( \sim 550 \) K. Within the approximation of a 3 mode model for \( \text{CO}_2 \), the vibrational temperatures observed for \( \nu_1 \) and \( \nu_4 \) correspond to a mean excitation level of \( \sim 0.8 \) \( \text{CO}_2 \) quanta absorbed per molecule at 8 torr and \( \sim 1.3 \) photons absorbed per molecule at 20 torr. For both cases cited, these excitation levels are well in excess of the conventional 2-level saturation limit.

The results of the vibrational temperature measurements for \( \nu_1 \) and \( \nu_4 \) have interesting ramifications with regard to possible laser action in \( \text{CO}_2 \). Recently, it has been shown that population inversions can be achieved in laser pumped molecules which establish metastable steady state population distributions.\(^{(11)}\) The conditions which favor a population inversion are: (1) rapid endothermic coupling of the pumped mode fundamental to the fundamental of another mode; (2) rapid near-resonant coupling of the overtone of the pumped mode to a fundamental of another mode; and (3) low translational temperature. All three of these conditions are met in \( \text{CO}_2 \) allowing for a population inversion of the \( \nu_1 \) state (Fermi mixed to the pumped mode overtone \( 2\nu_2 \)) with respect to the \( \nu_4 \) state (endothermically coupled to \( \nu_2 \)). Once again assuming a 3 mode model for \( \text{CO}_2 \) \((\nu_2, \nu_1, \nu_4)\), a population inversion between these states \((\nu_4 \text{ and } \nu_1)\) can be achieved at the modest excitation level of \( \sim 1 \) photon absorbed per molecule. Our present results suggest that the conditions necessary for population inversion between the \( \nu_1 \) and \( \nu_4 \) states have already been realized at \( \text{CO}_2 \) pressures above 8 torr.

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Future work includes cold gas filter measurements of the vibrational temperatures in the low lying modes of \( \text{COF}_2 (v_3, v_5 \text{ and } v_6) \) to gain additional information on the mechanism for vibrational energy transfer in the molecule. The effects of laser energy, pulse width, and wavelength, as well as rare gas dependence will be investigated to determine the extent to which they influence the steady state population distribution.

*This research was also supported by the Department of Energy under Contract DE-AS02-78ER04940 and by the National Science Foundation under Grant NSF-CHE77-24343.


C. INTERMOLECULAR VIBRATIONAL ENERGY TRANSFER DYNAMICS IN IR LASER PUMPED SO$_2$/18O$_2$ MIXTURES*

(M. I. Lester, G. W. Flynn)

Vibrational energy transfer processes in SO$_2$/18O$_2$ mixtures have been observed by monitoring fluorescence emission from the SO$_2$ v$_3$ mode following pulsed CO$_2$ laser excitation of the v$_1$ mode. The kinetic mechanism determined from these fluorescence studies allows for intermode vibrational energy transfer in SO$_2$ due to collisions with both SO$_2$ and 18O$_2$ as well as an intermolecule vibrational energy exchange process between SO$_2$ and 18O$_2$. The energy crossover from SO$_2$ to 18O$_2$ occurs via the step

$$\text{SO}_2(v_3) + 18\text{O}_2 \xrightarrow{k_{30}} \text{SO}_2(0) + 18\text{O}_2(1) - 107 \text{ cm}^{-1}$$

The rate constant for this vibrational energy sharing process ($k_{30}$) was found to be 5.74 (± 0.91) msec$^{-1}$ (torr 18O$_2$)$^{-1}$ or approximately 1400 gas kinetic collisions.

Kinetic modeling of the vibrational energy transfer processes in SO$_2$/16O$_2$ mixtures has clarified an inconsistency in the SO$_2$/O$_2$ literature. An ultrasound investigation had reported an energy crossover process from the v$_3$ state of SO$_2$ to the v=1 level of 16O$_2$; yet, no energy sharing process has been observed by the infrared fluorescence technique. Kinetic modeling of the population deviation in the fluorescing SO$_2$ v$_3$ state has indicated that the amplitude of a crossover step which occurs on the time scale reported by the ultrasound study would be too small to be observed by present IR fluorescence experimental techniques.

The probability of a vibrational transition during a bimolecular collision as a result of short-range spherically symmetric repulsive forces
can be determined from the SSH breathing sphere model. Vibrational energy transfer probabilities have been calculated by this method for the intermolecule vibrational energy sharing process in $\text{SO}_2^{\text{18}}\text{O}_2$ and $\text{SO}_2^{\text{16}}\text{O}_2$ mixtures. The SSH model predicts probabilities of energy transfer per $\text{SO}_2-\text{O}_2$ collision in the range of $3.6 \times 10^{-4}$ to $1.3 \times 10^{-3}$ for energy crossover to $^{\text{18}}\text{O}_2$ and a corresponding range of $5.6 \times 10^{-5}$ to $3.7 \times 10^{-4}$ for crossover to $^{\text{16}}\text{O}_2$ (see Table I). The intermolecular repulsion parameter, $\alpha$, was varied from $4.5 \times 10^8$ cm$^{-1}$ to $6.5 \times 10^8$ cm$^{-1}$.

Another approach for calculating the probability of a vibrational energy transfer during a bimolecular collision is based on the roll of long-range multipolar forces in effecting the transition. The theory of energy transfer caused by dipole–dipole and dipole–quadrupole interactions has been developed by Sharma and Brau.\textsuperscript{(9)(10)} The probability of V–V energy transfer due to long-range interactions is strongly dependent on the energy mismatch of the collision pair. As a result of the range of the multipolar potential, the probability of energy transfer falls off rapidly as the energy discrepancy is increased. Only 'near-resonant' processes have been shown to contribute significantly to the energy transfer cross section.

In the present investigation of intermolecule energy transfer in $\text{SO}_2/\text{O}_2$ mixtures, long-range interactions might at first glance appear to have little consequence for the overall transition probability. The energy gaps for the crossover processes from $\text{SO}_2 (v_3)$ to $^{\text{18}}\text{O}_2 (1)$ and $^{\text{16}}\text{O}_2 (1)$, - 107 cm$^{-1}$ and - 195 cm$^{-1}$, respectively, are too large for the transitions to be considered as near-resonant. However, since the lowest order multipole interaction is between the instantaneous dipole moment of $\text{SO}_2$ and the
<table>
<thead>
<tr>
<th></th>
<th>$^{18}$O$_2$</th>
<th>16O$_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\Delta E$</td>
<td>-107 cm$^{-1}$</td>
<td>-195 cm$^{-1}$</td>
</tr>
<tr>
<td>$k_{30}$ a</td>
<td>5.74 (± 0.91)</td>
<td>0.26 b</td>
</tr>
<tr>
<td>$P_{\text{EXP}} = \frac{k_{30}}{k_{\text{gk}}}$ c</td>
<td>$7.0 \times 10^{-4}$</td>
<td>$3.1 \times 10^{-5}$</td>
</tr>
<tr>
<td>$P_{\text{SSH}}$ d</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\alpha = 4.5 \times 10^8$ cm$^{-1}$</td>
<td>3.6 $\times 10^{-4}$</td>
<td>5.6 $\times 10^{-5}$</td>
</tr>
<tr>
<td>$\alpha = 5.5 \times 10^8$ cm$^{-1}$</td>
<td>7.6 $\times 10^{-4}$</td>
<td>1.7 $\times 10^{-4}$</td>
</tr>
<tr>
<td>$\alpha = 6.5 \times 10^8$ cm$^{-1}$</td>
<td>1.3 $\times 10^{-3}$</td>
<td>3.7 $\times 10^{-4}$</td>
</tr>
<tr>
<td>$P_{\text{SB}}$ f</td>
<td>$6.5 \times 10^{-4}$</td>
<td>$1.2 \times 10^{-5}$</td>
</tr>
</tbody>
</table>

a. Rate constants are in units of msec$^{-1}$ (torr O$_2$)$^{-1}$.
b. Reference (5) in text.
c. $k_{\text{gk}}$ is the gas kinetic rate.
$$k_{\text{gk}} = 2.56 \times 10^{3}[\frac{\sigma_{\text{SO}_2} + \sigma_{O_2}}{2}]^{\frac{1}{2}} / \mu^{\frac{1}{2}} \text{ (msec}^{-1} \text{ torr}^{-1})$$
at T=300K. $\mu$ is the reduced mass of the collision partners in amu. All $\sigma$'s are taken from Reference (11).
d. Probabilities calculated from SSH breathing sphere model (References (6)-(8)).
e. $\alpha$ is the range parameter of the intermolecular potential.
d. Probabilities calculated from Sharma-Brau theory (Ref. (9)(10)).
quadrupole moment of O₂, rotational degrees of freedom turn out to cancel much of the relatively large vibrational band center mismatch. The Sharma-Brau long range theory predicts a probability of intermolecule energy transfer per SO₂-O₂ collision of $6.5 \times 10^{-4}$ for SO₂/¹⁸O₂ mixtures and a corresponding probability of $1.2 \times 10^{-5}$ for SO₂/¹⁸O₂ mixtures.

A comparison of experimental and theoretical results can be obtained by examination of Table I. The experimental probability for intermolecule energy sharing ($P_{\text{exp}} = k_{30}/k_{\text{gk}}$) in SO₂/¹⁸O₂ mixtures falls well within the range of probabilities predicted by the SSH breathing sphere model. The probability of energy exchange in SO₂/¹⁶O₂ mixtures as determined by the ultrasound measurements is somewhat lower than the predictions of the short-range model. The origin of this discrepancy could be in the simple theory used or in the experimental results for SO₂/¹⁶O₂ mixtures. Accurate determination of the energy sharing rate constant by ultrasound methods is difficult since oxygen contributes only a small amount to the total vibrational heat capacity in these experiments. However, the qualitative agreement between experiment and theory is sufficient in both cases to conclude that short-range repulsive forces may have some role in these energy transfer processes.

The probability of energy crossover from SO₂ to ¹⁸O₂ calculated from the long-range force model is in excellent agreement with the present experimental results. In contrast, the probability of energy sharing predicted by the long-range theory for SO₂/¹⁶O₂ mixtures is significantly smaller than the probability reported in the ultrasound study. The agreement between theory and experiment in the SO₂/¹⁸O₂ case suggests that long-range multipolar forces are a viable means for energy transfer in
this system. Long-range interactions appear to be much less important in
SO$_2$/16O$_2$ mixtures simply because the energy mismatch of the vibrational
band centers is much greater for this oxygen isotope.

Comparison of calculated and experimentally observed probabilities
indicates that both short-range and long-range forces contribute to the
intermolecular energy transfer process in SO$_2$/18O$_2$. A similar comparison
for the SO$_2$/16O$_2$ system suggests that long-range forces have little role
in the energy transfer process and that short-range forces probably
dominate the interaction.

A technique has been developed for calculating the propagating error
in the kinetic rate constants due to the experimental uncertainties of the
measured eigenvalues in polyatomic molecule energy transfer experiments.
The standard deviation for each rate constant, $\sigma_{K_i}$, can be expressed in
terms of the standard deviations of the eigenvalues, $\sigma_{\lambda_j}$, as

$$
\sigma_{K_i} = \left[ \sum_{j=1}^{n} \left( \frac{\partial K_i}{\partial \lambda_j} \right)^2 \sigma_{\lambda j}^2 \right]^{1/2}
$$

where $n$ is the number of independent eigenvalues associated with the
system. For convenience in evaluation, the partial derivations above can
be rewritten in terms of partial derivatives of the form $\frac{\partial \lambda_j}{\partial K_i}$ by
means of a Jacobian transformation.

A full manuscript describing this work has been accepted for publica-
tion and is scheduled to appear in the Journal of Chemical Physics during
June 1980.

*This research was also supported by the National Science Foundation under
Grant NSF-CHE-77-24343.
(1) CRL Progress Report #29, March 31, 1979, p. 55.


D. VIBRATIONAL ENERGY TRANSFER MAP FOR OCS*

M. L. Mandich and G. W. Flynn

Although vibrational energy transfer processes have been investigated in a large number of molecules,\(^{(1)}\) the impact of most of these studies has been limited by the variety of possible interpretations which fit the experimental results. Kinetic rate constants are by far the most useful quantities for describing vibrational energy transfer, but these constants can only be determined when their associated kinetic events can be identified. Usually, the available experimental rate data consists of time dependent population changes which just yield eigenvalues of a rate matrix corresponding to convolutions of several coupled kinetic events. Bridging the gap between measured eigenvalues and kinetic rate constants requires solving the rate matrix formed by all of the competing energy transfer processes. While this has never been completely achieved for any polyatomic molecule, the most advanced knowledge of this type exists for CH\(_3\)F\(^{(2)}\)(3) and SO\(_2\).\(^{(4)(5)}\) A partial mapping for OCS, well known as a chemical\(^{(6)}\) and infrared laser,\(^{(7)}\) has been attempted by several laboratories with conflicting results.\(^{(8)-(13)}\) In this work, these differences have been resolved and we report an energy transfer map for OCS which includes all of the major kinetic pathways plus their rates.\(^{(14)}\) The pathways and rates can be used to describe the flow of excess vibrational energy among the three OCS vibrational modes as well as overall relaxation into rotations and translations.

The essential ingredients required to construct a kinetic map are the measured eigenvalues and amplitudes describing the time dependent behavior of the perturbed vibrational state populations. In OCS, the
initial excess population is placed in the first overtone of the bending vibration, \(2v_2\), by way of a CO\(_2\) laser pump pulse. Improved detectors and signal averaging equipment have permitted accurate measurement of time dependent fluorescences emanating from all three fundamental vibrational states and two other combination states. (See Figure 1 and Table I.)

From the fluorescence data and subsequent kinetic analysis, the following sequence of events is deduced for the vibrational energy transfer map in OCS.\(^{(14)}\)

1) Initially, the \(2v_2\) level is pumped with the CO\(_2\) laser,
\[
9.6 \mu \text{COS}(0) \xrightarrow{P(22)} \text{CO}_2 \text{laser} \xrightarrow{} \text{COS}(2v_2).
\]

2) The bending modes rapidly equilibrate (in about 10-30 gas kinetic collisions) by near resonant up-the-ladder collisional processes such as:
\[
\begin{align*}
\text{OCS}(2v_2) + \text{OCS}(0) & \leftrightarrow \text{OCS}(v_2) + \text{OCS}(v_2) \\
\text{OCS}(2v_2) + \text{OCS}(v_2) & \leftrightarrow \text{OCS}(3v_2) + \text{OCS}(0) \\
\text{OCS}(3v_2) + \text{OCS}(v_2) & \leftrightarrow \text{OCS}(4v_2) + \text{OCS}(0).
\end{align*}
\]

3) The first intermode \(V-V\) energy transfer occurs on a much longer timescale as the asymmetric stretch, \(v_3\), is populated via
\[
\text{OCS}(4v_2) + \text{OCS} \leftrightarrow \text{OCS}(v_3) + \text{OCS} + 43 \text{ cm}^{-1}
\]
at a rate corresponding to 680 gas kinetic collisions. This unfavorable exchange of what is formally five vibrational quanta is the most rapid intermode \(V-V\) energy transfer process.
Figure 1: Experimentally observed OCS fluorescences are depicted on this OCS energy level diagram for energies up to 2400 cm\(^{-1}\). All of these fluorescences (marked with wavy lines) terminate on the ground state. The pulsed CO\(_2\) laser excitation is marked with a heavy arrow.
<table>
<thead>
<tr>
<th>$-\lambda_2 (&quot;\nu_1\ filling&quot;)$</th>
<th>$-\lambda_3 (&quot;\nu-T&quot;\ decay)$</th>
<th>$-\lambda_4 (&quot;\nu_3\ filling&quot;)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$5.6 \pm .6 \ (4.94\ \mu\ \text{decay})$</td>
<td>$1.8 \pm .15 \ (4.94\ \mu\ \text{decay})$</td>
<td>$47 \pm 4 \ (4.94\ \mu\ \text{rise})$</td>
</tr>
<tr>
<td>$5.5 \pm .4 \ (11.7\ \mu\ \text{rise})$</td>
<td>$1.7 \pm .2 \ (11.7\ \mu\ \text{decay})$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$1.8 \pm .2 \ (19.1\ \mu\ \text{decay})$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$1.7 \pm .2 \ (5.36\ \mu\ \text{decay})$</td>
<td></td>
</tr>
</tbody>
</table>

*a. errors reported are \( \pm \) two standard deviations.*
4) The symmetric stretch equilibrates more slowly via

$$\text{OCS}(2\nu_2) + \text{OCS} \not\leftrightarrow \text{OCS}(\nu_1) + \text{OCS} + 188 \text{ cm}^{-1}$$

at a rate corresponding to 2400 gas kinetic collisions. This vibrational mode may also be populated by a secondary path of

$$\text{OCS}(\nu_2) + \text{OCS} \not\leftrightarrow \text{OCS}(\nu_1) + \text{OCS} - 339 \text{ cm}^{-1}$$

at a much slower rate requiring more than 24,000 gas kinetic collisions.

5) Loss of total excited vibrational population through V-T/R relaxation,

$$\text{OCS}(\nu_2) + \text{OCS} \not\leftrightarrow \text{OCS}(0) + \text{OCS} + 520 \text{ cm}^{-1}$$

occurs at a rate corresponding to 3400 gas kinetic collisions.

Combining these kinetic steps with their accompanying rate constants, the population fluctuations of the vibrational levels can be calculated as a function of time which is shown in graphical form in Figure 2 for the pumped mode ($2\nu_2$) and the three fundamental modes ($\nu_1$, $\nu_2$ and $\nu_3$).

The probabilities measured for energy transfer in OCS-OCS collisions can be directly compared to calculated energy transfer probabilities using a model based on either short range repulsive forces (15-(17) or long range attractive forces. (18) The relative agreement and disagreement between various predicted and measured values highlight the nature of the interaction potential and the importance of mechanical and electrical anharmonicities in determining the kinetic paths. The short range force model calculation gives theoretical values for all intermode vibration-vibration probabilities which are grossly below the observed probabilities when the states are approximated by simple harmonic oscillators.
Figure 2: Time evolution of the perturbed populations in the three OCS fundamental levels ($v_1$, $v_2$ and $v_3$) plus the pumped level ($2v_2$).
However, when anharmonically mixed states\(^{(19)-(21)}\) are used in the calculation, the short range force model calculation adequately describes the qualitative features of \(V-V\) and \(V-T/R\) energy transfer probabilities in OCS but gives theoretical probabilities which are lower than the experimentally measured quantities. The probability for intermode \(V-V\) transfer from \(4v_2\) to \(v_3\) calculated using a long range force model is also close to the measured value but is too large by about a factor of three. (See Table II.) Almost certainly, anharmonic mixing of the vibrational states and the large electrical anharmonicity of the \(v_2\) mode are crucial factors in promoting intermode vibrational energy transfer in OCS.

A complete manuscript describing this work has been accepted for publication in the Journal of Chemical Physics.

*This research was also supported by the National Science Foundation under Grants NSF-MPS-75-04118 and NSF-CHE-77-24343.


### TABLE II

**Experimental and Theoretical Energy Transfer Probabilities for OCS**

<table>
<thead>
<tr>
<th>Transition (^{a})</th>
<th>Experimental (^{b})</th>
<th>SSH-Harmonic Oscillator States (^{c})</th>
<th>SSH-Anharmonic Mixed Stated (^{d})</th>
<th>Sharma-Brau (^{e})</th>
</tr>
</thead>
<tbody>
<tr>
<td>OCS(4(v_2)) + OCS (\leftrightarrow) OCS(3) + OCS +43 cm(^{-1})</td>
<td>1.5(\pm)0.3(\times)10(^{-3})</td>
<td>4.2(\times)10(^{-12})</td>
<td>5.1(\times)10(^{-4})</td>
<td>4.7(\times)10(^{-3})</td>
</tr>
<tr>
<td>OCS(2(v_2)) + OCS (\leftrightarrow) OCS(1) + OCS +188 cm(^{-1})</td>
<td>4.2(\pm)0.6(\times)10(^{-4})</td>
<td>8.0(\times)10(^{-7})</td>
<td>2.9(\times)10(^{-5})</td>
<td>-</td>
</tr>
<tr>
<td>OCS(1) + OCS (\leftrightarrow) OCS(2) + OCS +339 cm(^{-1})</td>
<td>&lt;4(\times)10(^{-5})</td>
<td>3.8(\times)10(^{-6})</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>OCS(2) + OCS (\leftrightarrow) OCS(0) + OCS +520 cm(^{-1})</td>
<td>2.9(\pm)0.7(\times)10(^{-4})</td>
<td>8.7(\times)10(^{-5})</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>

\(^{a}\) A positive \(\Delta E\) denotes an exothermic process, a negative \(\Delta E\) denotes an endothermic process.

\(^{b}\) Errors are reported to \(\pm 3\) standard deviations.

\(^{c}\) Energy transfer probability as calculated using the "SSH-Breathing Sphere" model (see Refs. 15-17) with all vibrational states derived from a purely harmonic oscillator model.

\(^{d}\) Same as c. above except anharmonically mixed vibrational states are used.

\(^{e}\) Energy transfer probability as calculated using the dipole-dipole long range attractive force model according to the method of Sharma and Brau.


(13) Progress Report, March 31, 1979, pp. 60-64.


(20) Y. Morino and T. Nakagawa, J. Mol. Spectrosc. 26, 496 (1968).

E. COLLISIONAL RELAXATION OF VIBRATIONALLY EXCITED OCS IN RARE GAS MIXTURES*

(M. L. Mandich, G. W. Flynn)

An energy transfer map describing the major vibrational relaxation processes for OCS has been presented in a previous study.\(^{(1)}\) The rates of these relaxation events due to collisions of OCS with other non-OCS partners can provide additional information about the nature of the intermolecular interaction potential for collisional vibrational energy transfer. Other investigations of the energy transfer kinetics for OCS have included measurements of vibrational energy relaxation rates in mixtures of OCS with the various rare gases, \(\text{O}_3\), Br, CO, HCl, and HBr.\(^{(2)-(7)}\) All of these studies predate a detailed understanding of the major kinetic pathways in OCS.

We have measured the rates for the collisional vibration-vibration (V-V) energy transfer between the \(v_1\) level of OCS and the \(v_2\) bending mode as well as the overall vibration to translation/rotation (V-T/R) relaxation of OCS in mixtures of OCS with \(^4\text{He}, \text{Ne}, \text{Ar}, \text{Kr}\) and \(\text{Xe}\) (see Table I). From these measured rates plus further kinetic analysis based on the vibrational energy transfer map known for pure OCS,\(^{(1)}\) the experimental probabilities for the bimolecular kinetic events,

\[
\text{OCS}(2v_2) + M \xrightarrow{k_A} \frac{k_A}{k_A} \text{OCS}(v_1) + M + 188 \text{ cm}^{-1} \tag{1}
\]

and

\[
\text{OCS}(v_2) + M \xrightarrow{k_T} \frac{k_T}{k_T} \text{OCS}(0) + M + 520 \text{ cm}^{-1} \tag{2}
\]
TABLE I
Eigenvalues Measured$^a$ (msec$^{-1}$ torr$^{-1}$) From $\nu_1$ Fluorescence

<table>
<thead>
<tr>
<th></th>
<th>&quot;$\nu_1$ Filling&quot;</th>
<th>&quot;V-T Decay&quot;</th>
</tr>
</thead>
<tbody>
<tr>
<td>OCS : $^4$He : Xe (3 : 1 : 10)$^c$</td>
<td>$-3.2 \pm .3$</td>
<td>$-1.0 \pm .1$</td>
</tr>
<tr>
<td>OCS : Ne (1 : 1)$^c$</td>
<td>$-3.3 \pm .4$</td>
<td>$-1.1 \pm .1$</td>
</tr>
<tr>
<td>OCS : Ar (1 : 3)$^c$</td>
<td>$-2.4 \pm .3$</td>
<td>$-.48 \pm .05$</td>
</tr>
<tr>
<td>OCS : Kr (1 : 6)$^c$</td>
<td>$-1.5 \pm .2$</td>
<td>$-.25 \pm .04$</td>
</tr>
<tr>
<td>OCS : Xe (1 : 6)$^c$</td>
<td>$-1.7 \pm .2$</td>
<td>$-.27 \pm .06$</td>
</tr>
</tbody>
</table>

a) Errors are reported to $\pm 3 \sigma$.

b) Eigenvalues are reported per torr of total pressure in OCS-M mixtures at constant mole fraction.

c) Relative mole ratio of constituents used in the mixtures which are prepared at constant mole fraction.
for the five possible rare gas collision partners (M = $^4$He, Ne, Ar, Kr, and Xe) have been determined (see Table II).

The corresponding theoretical probabilities have also been determined using the spherically symmetric, short range repulsive interaction potential model.\(^{(8)-(10)}\) The theoretical and measured probabilities are in reasonable qualitative agreement (although absolute numbers vary by as much as a factor of ten, depending on the steepness assumed for the repulsive potential wall) except for the rate of crossover $2v_2 \rightarrow v_1$ derived from the experimental data for the OCS-$^4$He mixture. Here, the experimental probability is at least five times larger than any reasonable value obtained from the model calculations (see Figures 1 and 2).

A cyclic kinetic path in OCS-$^4$He mixtures may account for the unexpectedly large experimental rate measured for the equilibration of $v_1$ with the bending manifold. This cyclic path is as follows,

$$
\begin{align*}
\text{OCS}(2v_2) + \text{OCS}(0) & \xrightarrow{k_{21}} \frac{k_{21}}{k_{12}} \text{2OCS}(v_2) + 7 \text{ cm}^{-1} \\
\text{OCS}(2v_2) + \text{He} & \xrightarrow{k_{A}} \frac{k_{A}}{k_{A}} \text{OCS}(v_1) + \text{He} + 188 \text{ cm}^{-1} \\
\text{OCS}(v_2) + \text{He} & \xrightarrow{k_{B}} \frac{k_{B}}{k_{B}} \text{OCS}(v_1) + \text{He} - 339 \text{ cm}^{-1} \\
\text{OCS}(v_2) + \text{He} & \xrightarrow{k_{T}} \frac{k_{T}}{k_{T}} \text{OCS}(0) + \text{He} + 520 \text{ cm}^{-1}
\end{align*}
$$

The model calculations suggest that this cyclic relaxation mechanism is
Table II
Experimental Energy Transfer Rate Constants and Probabilities for OCS with Rare Gas Collision Partners

<table>
<thead>
<tr>
<th>Collision Partner</th>
<th>$K_A$ (msec$^{-1}$)</th>
<th>$P_A = \frac{K_A}{Z_{OCS-M}}$ (x 10$^{-4}$)</th>
<th>$K_T$ (msec$^{-1}$)</th>
<th>$P_T = \frac{K_T}{Z_{OCS-M}}$ (x 10$^{-4}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>OCS $^a$</td>
<td>3.3 ± 0.5</td>
<td>4.2 ± 0.6</td>
<td>2.3 ± 0.5</td>
<td>2.9 ± 0.6</td>
</tr>
<tr>
<td>He $^f$</td>
<td>8 ± 0.3</td>
<td>5 ± 0.2</td>
<td>17 ± 2</td>
<td>12 ± 2</td>
</tr>
<tr>
<td>Ne</td>
<td>&lt; 1.3</td>
<td>&lt; 1.7</td>
<td>1.1 ± 0.6</td>
<td>1.4 ± 0.8</td>
</tr>
<tr>
<td>Ar</td>
<td>0.9 ± 0.3</td>
<td>1.2 ± 0.4</td>
<td>0.2 ± 0.2</td>
<td>0.3 ± 0.3</td>
</tr>
<tr>
<td>Kr</td>
<td>0.5 ± 0.1</td>
<td>0.8 ± 0.2</td>
<td>0.1 ± 0.1</td>
<td>0.2 ± 0.2</td>
</tr>
<tr>
<td>Xe</td>
<td>0.7 ± 0.1</td>
<td>1.0 ± 0.2</td>
<td>1.0 ± 0.1</td>
<td>1.0 ± 0.1</td>
</tr>
</tbody>
</table>

a) Errors are reported to ± 3σ; all K's are quoted at a pressure of one torr. Note that the value listed for $K_M$ is at one torr of M ($X_M = 1$).
b) $K_A^M$ refers to the energy transfer process in eqn. 1 of the text where $K_A = X_{OCS}K_{OCS} + X_{M}K_{M}^M$.
c) $Z_{OCS-M} = 2.56 \times 10^3 (R_{OCS}^OCS + R_{O}^OCS) / 4\mu^{1/2}$ at 1 torr (in a.u.).
d) $K_T^M$ refers to the energy transfer process in eqn. 2 of the text where $K_T = X_{OCS}K_{OCS} + X_{M}K_{M}^M$.
e) Values for pure OCS are obtained from reference 1.
f) These probabilities are calculated assuming that only $2v_2 + v_1$. There is evidence, as discussed in the text, that the path $v_2 + v_1$ may be comparably favorable in OCS-He collisions. The net result would be that the probability for $2v_2 + v_1 (p_{He})$ can range from 0 to $7 \times 10^{-4}$, that the probability for $v_2 + v_1 (p_{He})$ can range from 0 to $1 \times 10^{-4}$, and that the probability for V-T/R (pHe) can range from 7 to $13 \times 10^{-4}$, depending on the relative contribution of each path to the V-V coupling of $v_1$ with the bending manifold.
Figure 1: Experimental and calculated (SSH-breathing sphere) probabilities vs. square root of the reduced mass for the vibration-translation/rotation relaxation of OCS by $^4$He, Ne, Ar, Kr, and Xe. The calculated probabilities are indicated by circles and the experimentally derived probabilities are shown as solid squares with associated error bars. The error bars with a dashed line instead of a lower limit actually have a lower limit of zero which cannot be shown on the In scale. The model calculated values are shown for three reasonable values of $L$ (the steepness of the repulsive potential wall). The dashed line is the approximate relationship between the probability and $\mu^{1/2}$ for $L = 0.16 \AA$; similarly, the solid line corresponds to $L = 0.19 \AA$ and the dotted line corresponds to $L = 0.22 \AA$. 
Figure 2: Experimental and calculated (SSH-breathing sphere) probabilities vs. square root of the reduced mass for the vibration-vibration relaxation from $2v_2 \to v_1$ of OCS by $^4$He, Ne, Ar, Kr, and Xe. The calculated probabilities are indicated with circles and the experimentally derived probabilities are shown as solid squares with associated error bars. The error bar with a dashed line instead of a lower limit actually has a lower limit of zero which cannot be shown on the ln scale. The model calculated values are shown for three reasonable values of $L$ (the steepness of the repulsive potential wall). The dashed line is the approximate relationship between the probability and $\mu^{1/2}$ for $L = .16\text{Å}$; similarly, the solid line corresponds to $L = .19\text{Å}$ and the dotted line corresponds to $L = .22\text{Å}$. 

PROBABILITY $\times 10^4$

$\ln \sqrt{\mu}$ (amu$^{1/2}$)

$L = .16\text{Å}$

$L = .19\text{Å}$

$L = .22\text{Å}$
reasonable, but its presence cannot be definitely established from the experimental data obtained in these experiments.

Cyclic relaxation pathways, in general, may occur in the overall vibrational relaxation mechanism of many molecules.\(^{(1)}\)(11)-(15) A cyclic path can enhance overall V-V relaxation rates if it connects states which all have relatively sizable populations. Moreover, if the cyclic path is also "unstable" it will increase the rate of V-T/R relaxation.\(^{(1)}\)(11)-(12) Many cyclic paths can be expected to require population flow through a "bottle-neck" state which has a small ambient population; such cycles will not effect either rapid V-V or V-T/R relaxation. However, in complex or highly excited molecules, there may occur cyclic paths which can be termed "catastrophic"; these cycles can greatly speed up both V-V and V-T/R relaxation and thus quickly destroy any mode selective vibrational excitation placed in the molecule.

A complete manuscript describing the results of OCS-rare gas collision studies and model calculations for cyclic paths has been submitted for publication.

*This research was also supported by the National Science Foundation under Grants NSF-MPS-75-04118 and NSF-CHE-77-24343.


(13) F. Lepoutre, Ph.D. Thesis (Université de Paris-Sud, Centre D'Orsay, March 1979).
Molecular beam reactive scattering experiments involving diatomic reagents have shown clearly that vibrational energy can be utilized to overcome activation barriers in simple bimolecular reactions. It is of interest to extend these studies to include polyatomic molecules, e.g., SF₆, CH₃F, etc. To this end, we have carried out experiments in our laboratory aimed at producing internally excited beams of SF₆ by irradiating with a low power, continuous wave CO₂ laser. During the course of these experiments we have developed a technique which makes possible the determination of the average energy of the beam molecules and the distribution of this energy between the internal and translational degrees of freedom.

Gases expanding in the throat of a supersonic nozzle pass rapidly from a high pressure (collisional) region into an essentially collision free environment. The expanding gas is irradiated in the high pressure region near the nozzle exit where the number density is high, the absorption lines are collisionally broadened, rotational hole filling keeps saturation effects at a minimum and relatively large amounts of energy can be deposited through collisional up-pumping processes. Following excitation, the molecules move rapidly into the collision free region "freezing" a large fraction of the absorbed energy in the internal degrees of freedom.

Changes in total beam energy are monitored with a liquid He-cooled bolometer while a standard mass spectrometer-time-of-flight device is used to measure beam intensity and translational energy.

Initially, the SF₆ beam was irradiated immediately down stream of the nozzle exit with a loosely focussed CO₂ laser (5 watts at 10.6 μm [P(16)]).
Under typical conditions, there was a 7-8% laser-induced increase in total energy content of the transmitted beam molecules, corresponding to a net energy deposition of 0.11 IR photons per SF₆ molecule in the beam. Vibration-translation relaxation converted some of the absorbed infrared energy into translational kinetic energy as manifested by an increase in both transverse and axial velocity of the SF₆ molecules. A significant loss of forward beam flux due to the enhanced transverse velocity component was observed. Approximately 70-80% of the absorbed energy was found to be "frozen" in the internal degrees of freedom of the SF₆.

In more recent experiments, a nozzle was fabricated from ZnSe, an infrared transmitting material, to allow irradiation upstream of the nozzle exit. By irradiating at the proper point in the nozzle, it should be possible to maximize the energy deposition while still maintaining high levels of internal excitation. Preliminary studies reveal an order of magnitude increase in the amount of energy deposited per SF₆ molecule with the new nozzle. Work is continuing with the new configuration to find the optimum conditions for laser pumping.

In addition to providing fundamental information about energy transfer processes and chemical reactions of vibrationally excited species, the techniques developed here can be used as diagnostic tools to study the dynamics of supersonic expansions.

*This research was also supported by the National Science Foundation under Grants NSF-CHE-77-24343 and NSF-CHE-77-11384 and by the Department of Energy under Contract DE-AS02-78ER04940.


Considerable work has been done on the transfer of vibrational energy between polyatomic molecules, however, practically all these studies deal with stable species in a singlet ground state. We are currently studying the relaxation of the vibrationally excited triplet radical, $\text{SO}(^{3}I^{-})$ produced by the photodissociation of $\text{SO}_2$.

The ultraviolet photolysis of $\text{SO}_2$ at wavelengths below 2190Å is known to yield $\text{SO}(^{3}I^{-})$ as the primary product.\(^{(1)}\) Studies of the translational energy distribution of the fragments, when $\text{SO}_2$ is irradiated at 1930Å, show that less than half of the 6250 cm\(^{-1}\) of available excess energy is deposited in the translational degrees of freedom.\(^{(2)}\) Furthermore, it can be argued that the degree of rotational excitation is small. Thus, it is expected that the SO fragment vibrational distribution will be vibrationally inverted with most of the population in the $v = 3$ and 4 states. It should be noted that the $\text{SO}(^{1}A)$ state is not accessible for photolysis at 1930Å.

We are studying the relaxation of vibrational energy in UV photolyzed mixtures of $\text{SO}_2$ and Argon by observing the amplitude of the time dependent infrared emission of the $v_3$ mode of $\text{SO}_2$ excited by energy transfer from vibrationally excited SO. The $v_3$ mode should be sensitive to the population of $\text{SO}(v)$ and therefore to the decay processes of the excited SO. We have observed a minimum of three pressure dependent decay eigenvalues in the $v_3$ fluorescence. Further studies of the intensity dependence of these rates are in progress and will aid in the assignment of these eigenvalues to the microscopic rate constants in this system. We are also considering looking at the fluorescence in the 9μ region due to the overlap of the $v_1$ mode of
$\text{SO}_2$ and the excited $\text{SO}$. The problem here is to deconvolute the two emissions and it is hoped that the $\nu_3$ data will allow this.

We are also exploring another probe technique for the $\text{SO}/\text{SO}_2$ system. A narrow linewidth ($<.0001 \text{ cm}^{-1}$) diode laser, tunable from 1075 to 1125 cm$^{-1}$, will be used to probe the populations of the $\text{SO}(v = 0-5)$ and $\text{SO}_2(v_1)$ states. The diode laser will be used to monitor the time resolved absorptions of selected vibrational/rotational states, and will allow the determination of both the initial $V/J$ distribution of the $\text{SO}$ fragments and the rates of vibrational relaxation for each of the vibrational states of the $\text{SO}$. We are currently monitoring the behavior of the $\text{SO}_2(v_1)$ with encouraging results.

*This research was also supported by the National Science Foundation under Grant NSF-CHE-77-24343 and by the Department of Energy under Contract DE-AS02-78ER04940.


A. PICOSECOND LASER STUDIES OF PHOTO-INDUCED DISSOCIATION OF MOLECULES*

(G. Korenowski, C. Dupuy, W. Hetherington, M. McAuliffe, and K. B. Eisenthal)

We are using the methods of picosecond spectroscopy to determine the pathways and dynamics of molecular photodissociation. The molecular system we are investigating is dephenylidiazomethane \( \phi \rightarrow C = N_2 \)

\[
\begin{array}{c}
\text{Ph}
\end{array}
\]

\( = N_2 \)

in a 3-methylpentane solvent. This molecule was selected because it generates the diphenyl carbene \( \phi \rightarrow C : \) on photodissociation. This radical and the entire class of carbenes \( \phi \rightarrow C : \) play a key role as intermediates in many chemical reactions. The central "divalent" carbon is bonded to two groups, \( R_1 \) and \( R_2 \), and contains two nonbonding electrons which can be anti-parallel (singlet) or parallel (triplet). Due to their importance in chemistry there has been considerable experimental and theoretical research on the structure, spectroscopy and chemical properties of these molecules.

The sequence of elementary steps involved in fragmenting the parent compound, dephenylidiazomethane, and generating the carbene have been thought to be the following:

a) Excitation

\[
\phi \rightarrow C = N_2 + h\nu \rightarrow \phi \rightarrow C = N_2 \rightarrow ^* S_1
\]
We have used a frequency quadrupled Nd laser at 266 nm to excite the parent compound. We have set up an optical parametric amplifier, OPA, to generate tunable picosecond pulses to monitor the rate of formation of the triplet ground state of the carbene fragment. The idea is to excite the ground state triplet carbene, (its absorption spectrum is known at low temperature\(^{(1)}\)(\(^{(3)}\)) with the OPA and to measure the carbene fluorescence \((T^* \rightarrow T_0)\). The intensity of the carbene fluorescence as a function of the time separation between the photodissociating pulse (266 nm) and the OPA probe pulse would yield the formation dynamics of the triplet ground state carbene.

In the course of these experiments we discovered something unexpected and important. We found that the excitation pulse at 266 nm was generating some fraction of the diphenylcarbene molecules in an excited triplet state. Thus the sequence of steps must now be extended to include a new channel, unknown prior to this finding, in the decay process, namely the production of excited triplet carbenes. We identified that the triplet carbene was being produced by observing its fluorescence \((T^* \rightarrow T_0)\) (Figure 1). One key issue which we have resolved is whether the
Figure 1: Fluorescence (F* + F0) of diphenyl carbene in 3-methylpentane at room temperature.
excited triplet carbene is produced by a multiphoton process or by a one photon process. In the multiphoton process there are two possible pathways for generating the excited triplet carbene. One channel is a multiphoton absorption of diphenyldiazomethane which fragments from a higher state \( (2\nu h = 9.3\text{eV}) \) and utilizes the extra energy to produce the excited triplet. Another possibility is one photon absorption by diphenyldiazomethane which fragments to the carbene within the picosecond laser pulse width (\( \sim 25\ \text{psec} \) for the Nd:YAG and 5 psec for the Nd:glass) and a second photon is absorbed by the carbene thereby producing the excited triplet carbene. In the one photon process there would have to be sufficient energy in one photon (266 nm) to fragment the parent molecule and produce the excited triplet carbene. From Figure 2 we see that the carbene fluorescence \( (T^* \rightarrow T_0) \) is linear with the exciting laser power. The lower curve is the background signal obtained from the 3-methylpentane solvent with no diphenyldiazomethane present. To further confirm that there were no spectral features in the fluorescence which were intensity dependent we measured the fluorescence spectrum at two different laser intensities. On dividing one spectrum by the other we note from Figure 3 that we obtain a horizontal line which indicates that the spectral features are not intensity dependent.

We are presently investigating the rate of formation of the triplet and the pathway by which it is produced.

*This work was also supported by the National Science Foundation under Grant NSF-CHE79-23291 and by the National Institute of Health under Grant HL19488-04.

Figure 2: Fluorescence intensity versus exciting laser power. The upper curve (circles) is the carbene fluorescence ($T^* \rightarrow T_0$) versus exciting laser power. The lower curve (triangles) is the 3MP solvent fluorescence background power dependence.
Figure 3: Division of a weak fluorescence spectrum (weak incident laser pulse) by a strong fluorescence spectrum (strong incident laser pulse) shows spectral features are not intensity dependent.
(2) Carbenes, R. A. Moss and M. Jones, Jr. (Eds.), John Wiley & Sons, New York, 1975), Vol. II.


B. COHERENT ANTI-STOKES EXPERIMENTS ON GAS PHASE BENZENE*

(W. Hetherington, G. Korenowski, K. B. Eisenthal)

In studying ultrafast molecular processes we and other investigators seek to identify the states, structures, and intermediate chemical species through which a system of interest evolves.\(^{(1)-(7)}\) A principal tool in these studies is transient electronic absorption and emission. Although it remains as an important method, electronic spectroscopy is often complicated by overlapping broad and featureless electronic transitions. In such cases vibrational or electronic Raman scattering can often provide more unambiguous information than electronic absorption spectroscopy. Two different chemical structures can possess electronic spectra so similar that discrimination between the two is not feasible whereas the Raman spectra of the two species can be resolved. It is therefore advantageous in such cases to use Raman scattering to monitor the evolution of a molecular system through its various chemical species and changing structures.

Besides spontaneous Raman scattering, the coherent anti-Stokes Raman scattering (CARS) is of great utility.\(^{(8)-(18)}\) In this technique, beams at frequencies \(\omega_1\) and \(\omega_2\) are mixed in the system of interest to produce

\[
\omega_3 = 2\omega_1 - \omega_2 = \omega_1 + (\omega_1 - \omega_2) = \omega_1 + \Delta.
\]

A large signal at \(\omega_3\) is obtained when the frequency mismatch corresponds to a Raman active transition of the system. We have successfully carried out picosecond CARS experiments on gas phase benzene at room temperature (\(P \sim 80\) torr) in a 20 cm. cell. In our initial experiments we used a 532 nm pulse as \(\omega_1\) and generated \(\omega_2\) by a stimulated Raman scattering method in neat benzene. However, what is generally required to carry out a wide range of experiments is tunability so that \(\omega_1 - \omega_2\) can be brought into resonance with a Raman active
vibration of interest. To achieve this we have set up an optical parametric amplifier which enables us to tune $\omega_2$ from 400 nm to 700 nm.

Using picosecond light pulses in a collinear geometry at the wavelengths $\lambda_1 = 532$ nm and $\lambda_2 = 635.4$ nm a resonance was observed which is due to the ground state symmetric C-H stretch at $\Delta = 3060$ cm$^{-1}$ (Figure 1). We then introduced into the benzene gas cell, at the same time as $\lambda_1$ and $\lambda_2$, a picosecond pulse at the fourth harmonic of Nd:YAG, 266 nm. The 266 nm light excites the benzene although it is about 490 cm$^{-1}$ on the low energy side of the $B_{2u}$ origin. Generating a $\lambda_2 = 638.3$ nm with the OPA and mixing it with $\lambda_1 = 532$ nm we observed a CARS resonance at $\Delta = 3130$ cm$^{-1}$ which we ascribe to the C-H stretch in the excited singlet $B_{2u}$. The literature value$^{(19)}$ for the C-H stretch in the $B_{2u}$ state is 3134 cm$^{-1}$.

In addition to our interest in excited state CARS we were motivated to use CARS to study the fragments generated by photolysis of benzene with 266 nm light pulses. This interest was prompted by the successful work of others$^{(20)}$ in the use of CARS to study the products produced by photolysis of benzene. Our interest was to determine the sequence of fragments generated in the initial steps, namely how does photoexcited benzene break apart on the subnanosecond time scale. On varying $\omega_2$ from 625 nm to 637 nm we could examine resonances, e.g. Figure 2, of $\Delta = 2800$ cm$^{-1}$ to $\Delta = 3200$ cm$^{-1}$ using $\omega_1 = 532$ nm. The strongest fragment signals were observed in the 2900-2935 cm$^{-1}$ region, tailing off on the low energy side. The CARS signal in this region has been attributed$^{(20)}$ to the $C_2$ fragment. Since the excitation and CARS pulses at $\omega_1$ and $\omega_2$ were not delayed with respect to each other, i.e. coincident in time.
Figure 1: Ground state benzene CARS intensity vs. wavelength. Signal at Channel 239 is 457.5 nm and signal at Channel 400 is a wavelength marker.
\[ \lambda_1 = 532 \text{ nm}; \quad \lambda_2 = 635.4 \text{ nm}; \quad \Delta = 3060 \text{ cm}^{-1}. \]
Figure 2: CARS intensity vs. wavelength of the C₂ fragment. Signal at Channel 215 is 460.9 nm and signal at Channel 400 is a wavelength marker. Photolysis at 266 nm.

\[ \lambda_1 = 532 \text{ nm}; \quad \lambda_2 = 629.1 \text{ nm}; \quad \Delta = 2901 \text{ cm}^{-1} \]
(as well as overlapping spatially), our observation of the CARS signals indicate that (1) benzene undergoes a multiphoton fragmentation to produce, among other products, C₂, and (2) that a fragment as small as C₂ is produced within 25 ps. after photoexcitation of benzene.

We are presently carrying out experiments to identify the different fragments and determine their sequence of formation.

*This work was also supported by the National Science Foundation under Grant NSF-CHE79-23291 and by the National Institute of Health under Grant HL19488-04.


C. PICOSECOND LASER STUDIES OF ELECTRON SOLVATION IN LIQUIDS*  
(Y. Wang, M. Crawford, M. McAuliffe, K. B. Eisenthal)

When low energy excess electrons are injected into a polar fluid they become rapidly thermalized. These thermalized electrons are initially localized in shallow potential wells formed by the surrounding solvent molecules. In the absence of a reactive chemical channel, the surrounding solvent dipoles restructure themselves about the electron, deepening the potential well and leading to the formation of the solvated electron.

There has been great activity and progress extending over many years in studies of the effects of ionizing radiation on materials with electron solvation in liquids as one of the areas of intense interest. In addition to the scientific interest there is marked technological interest due to the importance of lithography, e.g. using electrons, to achieve high density storage of information. In pulse radiolysis experiments the energy transferred to the medium generates local regions of ionization, and molecular electronic, vibrational and rotational excitations. These ionization and excitation events are important in the description of molecular motions, energy relaxation, and the generation of reactive species of materials. To this date the fundamental processes involved in electron solvation in liquids are poorly understood.

We have approached the problem of electron solvation in polar liquids by picosecond laser transient absorption spectroscopy. Although picosecond laser methods have been used in a prior study to measure electron solvation in water it was found that the solvation process was completed within the laser pulse width and thus time resolved dynamics was not obtained. In the experiments reported here we have obtained time resolved...
information for the first time using picosecond laser methods. The electrons are generated in the liquids methanol and ethanol by picosecond laser two photon ionization\(^{(8)}\) of the pyrene solute molecules present.

\[
\text{Pyrene} + 2\text{hv} \rightarrow \text{Pyrene} + e^- \tag{1}
\]

The electrons are very rapidly trapped\(^{(6)}\) \((<10^{-12} \text{ sec.})\) and ultimately become solvated electrons. We obtain the kinetics of solvation by measuring the growth of the absorption characteristic of the solvated electron in the alcohols used.\(^{(4)-(9)}\)

A laser triggered flash lamp and picosecond streak camera are used to obtain the time dependence of the solvation dynamics (Figure 1). This technique is quite different from the variable delay and transmission echelon techniques\(^{(7)}\) which utilize one or more laser probe pulses. These latter techniques require many laser shots in order to yield the time dependent absorption profile, whereas in our method the continuous time absorption is obtained in one laser shot. It is also worthwhile to note the potential use of our system for experiments in which both time and wavelength dependences of the transient absorption signal can be obtained in one laser firing.

Solvation times measured in this work are listed in Table I together with those determined by pulse radiolysis. The values obtained by photoionization are larger than those obtained by pulse radiolysis. We ascribe these differences to the local heating effect resulting from pulse radiolysis. In pulse radiolysis experiments the secondary electrons generated by the incident ionizing radiation dissipate their energy very rapidly through ionizations and excitations (electronic, vibrational and
Figure 1: Schematic of experimental set-up. PC: Pockels cell.
SHG: second harmonic generating crystal. THG: third harmonic generating crystal.
### TABLE I

**Picosecond Formation Times of Solvated Electrons in Alcohols at 293°K**

<table>
<thead>
<tr>
<th></th>
<th>Solvation Times psec</th>
<th>Dielectric relaxation times d psec</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>picosecond laser</td>
<td>pulse radiolysis</td>
</tr>
<tr>
<td>methanol</td>
<td>17 ± 3(^a)</td>
<td>10.7 ± 1(^b)</td>
</tr>
<tr>
<td>ethanol</td>
<td>26 ± 5(^a)</td>
<td>23 ± 2(^b)</td>
</tr>
</tbody>
</table>

\(^a\) This work.

\(^b\) Reference 4.

\(^c\) Reference 5.

\(^d\) \( \tau_1, \tau_2 \) and \( \tau_3 \) are the dielectric relaxation times under constant external field. \( \tau'_1 \) and \( \tau'_2 \) are the corrected values of \( \tau_1 \) and \( \tau_2 \) according to \( \tau' = \tau \varepsilon_\infty / \varepsilon_0 \).

2. Values of \( \varepsilon_\infty \) and \( \varepsilon_0 \) are either obtained or extrapolated from reference 17.
rotational). This thermalization process typically occurs within 1 psec after the initial ionization. The sudden transfer of electron kinetic energy to vibrational and rotational energy of the surrounding molecules in a small region (spur) causes a jump in local temperature and accelerates the solvation of the electron.

By comparing the pulse radiolysis data with the picosecond laser data we can make an estimate of the spur temperature. It is found that the pulse radiolysis data at 261°K in methanol and 277°K in ethanol have the same solvation rates as the corresponding rates measured in our study at 293°K. Assuming that these differences arise from the local heating phenomena in pulse radiolysis, this implies an "effective" temperature jump of 32°K for methanol and 16°K for ethanol in the pulse radiolysis experiments. These estimates are consistent with a theoretical model of small spurs (\(\sim 20\phi\)) and an average energy deposition of 30 eV in a spur. The existence of a significant temperature jump in the spur is thus for the first time directly supported by experiment.

Next we turn our attention to the relationship between the solvation and dielectric relaxation times. In Table I we list the various dielectric relaxation times associated with these liquids. \(\tau_1\) is interpreted as the time required for the breaking of intermolecular hydrogen bonds followed by reorientation of the molecule, \(\tau_2\) is the time required to reorient a free monomer, and \(\tau_3\) is the reorientation time of OH dipoles. All of these \(\tau\) values were obtained under the experimental condition of a constant weak external electric field applied to the system, which is clearly not the case with electron solvation in fluids. When an electron is injected into a medium, the charge of the electron can speed
Figure 2: The formation of solvated electron in methanol. Solid curve represents experimental points and broken curve represents theoretical points. The pre-pulse (fwhm is 7 channels) is ahead of the excitation pulse (not shown in the plot) by 52 channels. The data shown here is the average of 10 shots.
up the dielectric relaxation rate. The corrected dielectric relaxation time, $\tau'$, under constant charge approximation is given by

$$\tau' = \tau \cdot \varepsilon_\infty / \varepsilon_0$$

where $\tau$ is the normal dielectric relaxation time under constant field, $\varepsilon_\infty$ is the limiting high frequency dielectric constant, and $\varepsilon_0$ is the limiting low frequency dielectric constant. In Table I, $\tau'_1$ and $\tau'_2$ are the corrected values of $\tau_1$ and $\tau_2$ respectively according to equation (2).

The fair correlation between the solvation times measured by pulse radiolysis and the reorientation time of a free monomer ($\tau_2$), rather than the $\tau_1$ which is determined by the relaxation of hydrogen bonding structures, has led to the suggestion that in the process of electron solvation the intermolecular hydrogen bonding is not a limiting factor. However, since the relaxation is occurring in the presence of a fixed charge rather than under a constant electric field (as mentioned above), the solvation rate should actually be correlated with the corrected dielectric relaxation rate. It can be seen that our picosecond laser data does not yield good agreement with the calculated values of $\tau'_2$ and $\tau'_1$ for methanol and ethanol. We must conclude therefore that for these cases at least the solvation dynamics cannot be described solely in terms of any simple molecular motions or dielectric relaxation process. Further measurements of the electron solvation rates as a function of temperature and the extension of measurements to the longer chain alcohols are needed to develop an adequate model of electron solvation in these polar liquids.
*This work was also supported by the National Science Foundation under Grant NSF-CHE79-23291 and by the National Institute of Health under Grant HL19488-04.

(1) For a survey of both experiments and theories, see


IV. GENERATION AND CONTROL OF RADIATION

A. SPONTANEOUS AND INDUCED COHERENT RADIATION GENERATION AND CONTROL IN ATOMIC VAPORS*

(K. P. Leung, R. Kachru, E. Whittaker, T. W. Mossberg, S. R. Hartmann)

The past year has been quite fruitful with regard to both of our research objectives, which are 1) to advance the basic understanding of the generation of coherent radiation in atomic vapors, and 2) to utilize coherently generated radiation to study atomic processes occurring within such vapors. We first discuss the results of programs which have continued from the previous report.

In the previous interval we reported the discovery that the stimulated photon echo can be generated from the phase information stored in a single atomic state. In light of this fact we pointed out that the collisional degradation of the stimulated echo can be used to determine absolute total elastic scattering cross sections and to study velocity-changing collisions. We have completed experiments on stimulated echoes generated in Na and reported\(^1\)(2) the collisional effects associated with Na(3S)-He, Na(3P\(_{1/2}\))-He and Na(3S)-CO collisions.

In our last report we also presented early results of tri-level echo\(^3\) studies of the collisional broadening of electric-dipole forbidden 3S-nS(nD) transitions in Na. We were able to measure the He-, Ne-, and Ar-induced broadening of transitions for which the upper state was well into the Rydberg regime. These results have been published\(^4\). In the current interval we have dramatically extended our early work. Broadening rates of the Na 3S-nS(nD) transitions up to \(n = 40\) have been measured for all five noble gases. Our broadening measurements, performed at low perturber-gas pressures, constitute by far the most extensive work to date on...
transitions involving Rydberg states. Since the tri-level echo is generated by coupling states of the same parity both Rydberg S and D states can be accessed from the ground 3S state of Na. Interestingly, the broadening of 3S-nS and 3S-nD transitions shows (see Figure 1) interesting differences and, while some work has already been done, this result should stimulate theoretical work. The broadening rates of transitions to Rydberg states are important in a practical sense, because of the potential use of these transitions for frequency calibration. Our current results will be published shortly. In the future we plan to extend our measurements to other alkalis and other perturbers. Perturbers such as CO should be particularly interesting since they have a permanent electric dipole moment and can be expected to give rise to a qualitatively different broadening behavior at high n.

We have continued our work on two-photon echoes and have completed an indepth study of noble-gas-induced collisional broadening of the $6^2P_{1/2} - 6^2P_{3/2}$ electric-dipole forbidden transition of atomic thallium. In contrast to our earlier work in Na, we have been able to produce the two-photon echo (or in this difference-frequency case the "Raman" echo) with the laser fields detuned as much as 600 GHz from the intermediate $7^2S_{1/2}$ state. This constitutes the first observation of a non-resonantly excited two-photon echo in an atomic vapor. The dependence of Raman echo intensity on Ti number density and on detuning of the laser field from intermediate-state resonance has been studied. Interestingly, it is found that loss of phase-matching resulting from population transfer during the excitation pulses appears to set the maximum echo signal obtainable. Working at temperatures between 750 and 840 degrees K,
Figure 3.

Figure 1
we have found the following noble-gas-induced broadening cross sections for the $^2P_{1/2} - ^2P_{3/2}$ transition:

<table>
<thead>
<tr>
<th>Perturber</th>
<th>Broadening Cross Section ($\AA^2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>He</td>
<td>59 (6)</td>
</tr>
<tr>
<td>Ne</td>
<td>67 (7)</td>
</tr>
<tr>
<td>Ar</td>
<td>126 (13)</td>
</tr>
<tr>
<td>Kr</td>
<td>166 (17)</td>
</tr>
<tr>
<td>Xe</td>
<td>202 (20)</td>
</tr>
</tbody>
</table>

These results are being prepared for publication.

In the current interval we have discovered an entirely new class of reordering phenomena in gases. If an atomic vapor is resonantly excited by a short standing-wave laser pulse, the population in both the ground and excited state exhibits a spatial variation whose spatial periodicity (wavevector) is determined by the wavevector of the excitation field $k_e$. Specifically, after the standing-wave pulse the ground-state population density $\rho_{gg}$ is given by

$$2\rho_{gg} = 1 + J_0(\theta^o_1) + \sum_{n=1}^{\infty} (-1)^n J_{2n}(\theta^o_1)\cos(2nk_ez),$$  \hspace{1cm} (1)

where $J_1$ is a Bessel function of order 1, $z$ is the position coordinate along the direction of the standing-wave field, and $\theta^o_1$ is the peak area of the standing-wave field. The spatially modulated population forms a grating and can be detected by scattering a probe beam from it. Note that gratings having as wavevectors all even multiples of $k_e$ are generated. The thermal motion of the atoms rapidly eliminates the spatial modulation.
We have found, however, that a second standing-wave pulse, similar to the first but delayed by a time $\tau$, causes spatial order to appear periodically thereafter. Gratings of spatial periodicity $\lambda/2\beta$, where $\lambda = 2\pi/k_0$ and $\beta = (1, 2, 3, \ldots )$, appear at the times $n\tau/2\beta$ ($n = 1, 2, 3, \ldots$) after the second pulse. The gratings of periodicity $\lambda/2$, which appear every $\tau/2$ after the second pulse, can be detected by their backscattering of laser radiation which has the same wavelength as the exciting standing-wave pulses. Certain "grating echoes," as we term them, never depend on coherence between the ground and excited state and as such should prove useful in collisional studies.

Recent work\(^{(10)}\) has shown that the use of standing-wave excitation pulses in a regular photon echo experiment leads to the emission of multiple echoes. We have performed the first "standing-wave" photon echo experiment in an atomic vapor\(^{(11)}\) and have provided experimental checks on theoretical analysis\(^{(10)}\) of the effect.

Both "grating" and "standing-wave" echoes are important in terms of their possible applications in spectroscopy. In certain cases both types of echo display oscillations in amplitude as a function of laser frequency when the laser is tuned within the natural width of the transition. The oscillation which under proper conditions is independent of laser spectral width may provide sub-natural width spectroscopic resolution. The origin of the oscillation is found to be similar to that observed in Ramsey fringe experiments.

We have applied the two-pulse photon echo to perform a detailed study of the He-induced collisional broadening of the $3S-3P_{1/2}$ transition in Na.\(^{(12)}\) By monitoring the simple exponential decay $I_e(P) \sim \exp(-\delta P)$ of echo intensity
versus He pressure P we determine $\beta$ which can be used to determine the collisional broadening rate. We found that $\beta$ so determined exhibited a non-linear dependence on the excitation pulse separation $\tau$ (see Figure 2). The only plausible explanation for this behavior is to assume that collisional velocity changes contribute to echo decay. This is very surprising since it has been predicted\(^{(13)}\) the velocity changes should play no role in the broadening of electronic transitions. Our results\(^{(12)}\) will undoubtedly provoke a reexamination of certain aspects of the analysis of collisions. It should be noted that broadening measurements performed with echo effects are unhindered by the Doppler-width and the laser spectral width. In certain cases even the natural width is irrelevant. These factors made it possible for us to make our observations of the subtle role of collision velocity changes in the broadening of electronic transitions.

We have completed a theoretical analysis of optical echoes in gaseous media.\(^{(14)}\) This treatment provides a general framework for the analysis of the conditions under which traveling-wave excitation pulses will generate echoes in a gas. Our treatment concentrates on echoes which arise from the excitation of more than two distinct energy levels by use of laser excitation pulses of widely different frequencies. We are currently working on a simple intuitive description of generalized echoes which should be very useful in understanding the mechanisms of echo production.

*This research was also supported by the Office of Naval Research under Contract N00014-78-C-0517

Figure 2

PULSE SEPARATION $\tau$ (nsec) vs. $\beta$ (Torr$^{-1}$)


(13) P. R. Berman, Phys. Rev. A 5, 927 (1972); and 6, 2157 (1972), and references therein.

B. RELAXATION AND EXCITATION TRANSFER OF OPTICALLY EXCITED STATES IN SOLIDS

(K. Chiang, E. Whittaker, S. R. Hartmann)

We recently reported\(^1\) the results of photon echo modulation experiments on the \(3\text{H}_4 - 3\text{P}_0\) transition in \(\text{Pr}^{3+}\) doped crystals of \(\text{LaF}_3\). We demonstrated the feasibility of obtaining information about the hyperfine structure in the terminal levels of the echo transition with a resolution that was not limited by the large inhomogeneous linewidth of the transition or the multi-GHz linewidth of nitrogen-laser-pumped dye lasers. In addition, by carefully analyzing the detailed form of the echo modulation pattern we were able to determine the relative principal axes orientations of the ground and excited state interaction hamiltonians.

With the aim of investigating the hyperfine structure of the \(1\text{D}_2\) state in \(\text{LaF}_3: \text{Pr}^{3+}\), using the techniques that were used in the study of the \(3\text{P}_0\) state, we have performed photon echo experiments on the \(3\text{H}_4 - 1\text{D}_2\) transition in the same crystal. This transition involves the lowest crystal field split components of the \(3\text{H}_4\) and \(1\text{D}_2\) states; these components are electronic singlets that are each split into three doubly degenerate nuclear levels by the combined influence of the Pr nuclear quadrupolar and second order dipolar interactions. The energy splittings, which are of the order of several Mhz, are small compared to the linewidth of our two lasers; hence, we are able to coherently excite the system into a superposition involving all the sublevels. This leads to photon echo modulation effects that are observable on a time scale of several tens of nanoseconds.

The details of the experimental set up are similar to those used for measurements of the echo signal on the \(3\text{H}_4 - 3\text{P}_0\) transition. We employed
two thyatron triggered nitrogen-laser-pumped dye lasers to provide the
two laser pulses necessary for photon echo excitation. The two nitrogen
lasers were interfaced, via a multi-pulse generator unit, to a PDP8/e
minicomputer, that allowed us to conveniently vary, under program control,
the delay in the firing of one laser with respect to the other. The laser
pulses were combined and focused to a 200 \(\mu\) diameter spot in the LaF\(_3\):
Pr\(^{3+}\) crystal, which was of concentration 1.0 % at. wt. and had a thickness
of 4 mm. The c-axis was in the plane of the optically buffed crystal face,
and was oriented at right angles to the E-field vectors of the laser pulses.

The oscillator strength of the \(^3\)H\(_4\) - \(^1\)D\(_2\) transition is small and
accounts for the relatively poor signal-to-noise ratio in our preliminary
modulation data. In fact, the experiments of Brewer\(^{(2)}\) enable us to place
an upper limit of roughly 4.5 \(\times\) 10\(^{-5}\) debye for the magnitude of the dipole
matrix element between the \(^3\)H\(_4\) and \(^1\)D\(_2\) states. Assuming a laser power
input of 1 kw into the sample, it would be necessary to focus the laser
beams to a spot size of roughly 5 \(\mu\) diameter in order to obtain a 90 degree
pulse. For such a small spot size, the distance over which the laser beam
cross-section remains roughly constant is only 100 \(\mu\), so that we not only
have problems with beam overlap in a direction transverse to the direction
of the laser beam, but also in a direction along the direction of propaga-
tion of the beam. Under the conditions mentioned above, the number of
photons in the echo signal for the \(^3\)H\(_4\) - \(^1\)D\(_2\) transition for a 1.0 % at. wt.
sample, was estimated to be of the order of 10\(^7\). We may contrast this
with the number of photons in the echo signal for the \(^3\)H\(_4\) - \(^3\)P\(_0\) transition,
which for the same laser power of 1 kw, is estimated to be of the order
of 10\(^{11}\).
We performed some preliminary experiments to measure the echo signal as a function of laser spot size at the sample, and found that for a 200 \( \mu \) diameter the echo intensity at a particular fixed pulse separation was a maximum. That the echo signal should experimentally turn out to be larger for the 200 \( \mu \) spot size is due to the greater ease with which it was possible to obtain spatial overlap of the two laser pulses. In the limit when the "area" of the pulses are small, the echo signal is independent of the spot size at the sample, as long as the distance \( L \), over which the beam diameter remains smaller than twice the narrowest beam waist, does not exceed the thickness of the crystal. Since the thickness of our crystal was 4 mm, the echo signal should have (neglecting spatial overlap factors) gotten smaller for beam spot sizes greater than 50 \( \mu \).

In Fig. 1. we present the experimentally observed photon echo intensity versus pulse separation for the \( ^3H_4 - ^1D_2 \) transition. The fluorescence background from the excitation pulses has not been subtracted. Some care has to be exercised in analyzing the modulation curve because, at the temperatures that we performed these experiments, the measured signal contains contributions from two effects; there is an ordinary two-pulse photon echo component as well as a long-lived stimulated photon echo component. The formation of the latter can be explained as follows. Consider two resonant laser pulses, separated by time \( \tau_{12} \), incident upon the sample. The Fourier transform of the two excitation pulses exhibits interference fringes, with a frequency splitting of \( 1/\tau_{12} \), within the single pulse spectrum profile of 10 Ghz. Therefore, after the passage of the two excitation pulses, the ground state population will also exhibit a frequency dependent sinusoidal variation, the depth of this modulation
LaF$_3$:Pr$_{3+}$ 1.0 % at. wt.

$^3\text{H}_4 \rightarrow ^1\text{D}_2$ transition (592.5 nm)

Photon echo modulation of the $^3\text{H}_4 \rightarrow ^1\text{D}_2$ transition in LaF$_3$:Pr$_{3+}$

Figure 1.
pattern depending on the "area" of the excitation pulses. A third laser pulse incident on the sample at a time $\tau_{23}$ after the second pulse will then give rise to a stimulated echo, the intensity of which will depend on the depth of the modulation pattern mentioned above. This pattern of modulation in the ground state will persist for very long times if the process of thermalization of populations in the nuclear hyperfine levels of the ground state is slow, and hence stimulated echoes should be observable for pulse separations $\tau_{23}$ long compared to the excited state lifetime, which for the $^1D_2$ state is 500 usec. In our case, the third pulse was, unfortunately, the same as the second pulse in a subsequent two pulse photon echo sequence. Recent photon-echo-nuclear-double-resonance experiments showed that the long-lived stimulated echo component could be effectively eliminated by irradiating the sample with oscillating RF fields of frequency 16.7 Mhz and 8.47 Mhz, which correspond to the energy splittings in the ground $^3H_4$ state. Clearly, the RF fields, by inducing transitions between the nuclear hyperfine levels, accelerate the process of thermalization and completely degrade the long-lived stimulated echo.

By means of an optical-RF double resonance experiment, Erickson\(^{(3)}\) has shown that the splittings in the state are 3.7 Mhz and 4.7 Mhz resp. From these splittings we can determine the parameters in the interaction hamiltonian for the $^1D_2$ state, and we have calculated the echo modulation pattern for various relative axes orientations of the $^1D_2$ and $^3H_4$ interaction hamiltonians. A cursory comparison shows little agreement between either one of the calculated and experimental curves, which leads us to surmise that the parameters we used in the hamiltonian are wrong, or that the hamiltonian is incompletely known.
Another unexplained observation is the fast decay of the echo modulation envelope. It has been shown that for a 0.05 % LaF$_3$:Pr$^{3+}$ crystal, the homogeneous linewidth in the absence of any applied magnetic fields is of the order of 50 Khz. Our data seems to indicate that the linewidth is three times larger. As in the case of the $^3H_4 - ^3P_0$ transition, there appears to be a dependence of the homogeneous linewidth on Pr$^{3+}$ ion concentration.

Although our original aim was to measure nuclear hyperfine splittings in the $^1D_2$ state, so as to obtain the correct parameters in the Hamiltonian for our echo modulation calculation, we are currently engaged in performing photon-echo-nuclear-double-resonance (PENDOR) experiments on the $^3H_4 - ^3P_0$ transition. This would not only provide an independent check of the nuclear hyperfine splittings and linewidths measured using the modulated photon echo technique, but would also enable us to perfect our PENDOR technique on a transition where the photon echo signals are several orders of magnitude larger than those on the $^3H_4 - ^1D_2$ transition. Preliminary experiments have already shown a degradation of the stimulated echo signal for RF frequencies corresponding to nuclear hyperfine splittings in the $^3H_4$ ground state.

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V. QUANTUM DETECTION AND SENSING OF RADIATION

A. COHERENT DETECTION AND SENSING IN THE INFRARED

(R. A. Meyers, P. R. Prucnal, M. C. Teich)

The likelihood-ratio detection of a signal embedded in noise constitutes an important class of classical binary decision problems that has found widespread applicability in the synthesis and analysis of many types of systems. These applications range from optical communications to radar systems. For complex signal and noise statistics, it is sometimes difficult or impossible to express the likelihood ratio in closed form, however. Even for simple signal and noise statistics, direct implementation of the likelihood ratio as an optimum processor may be rather difficult. It may be possible to reduce the likelihood ratio to a simpler, but equivalent processor by using various ad hoc geometric arguments or lengthy algebraic manipulations.

We have made excellent progress in deriving a simple processor that is optimum for a broad range of classical binary decision problems involving the likelihood-ratio detection of a signal embedded in noise. The class of problems we have considered encompasses the case of N independent (but not necessarily identically distributed) observations of a nonnegative (or nonpositive) signal random variable embedded in an additive, independent, and noninterfering noise random variable, where the range of the signal and noise is continuous. This applies, in particular, to the case of heterodyne detection in the optical, infrared, and submillimeter, where the signal, local oscillator, and noise, can be treated as continuous random variables. We have shown that a comparison of the sum of the N observations with a unique threshold comprises
optimum processing, provided that the logarithm of the noise probability density does not contain a point of inflection. This condition on the noise probability density is not necessary, but is sufficient, to imply our single-threshold processor and does not depend on the signal probability density. The results are applicable to a spatial array of heterodyne detectors exposed to a temporal sequence of observations. We have shown by example that in many cases it is not difficult to test the log of the noise density for a point of inflection analytically. In more difficult cases, a graphical representation of the noise density with a logarithmic ordinate scale may be useful in revealing a point of inflection. We have applied the results to a generalized heterodyning optical communication system and shown that background noise, dark noise, modulation, avalanche multiplication, and channel distortions are easily included in our model.

We had previously\(^{(18)}\) derived a limited version of these results for a single observation \((N=1)\) of a nonnegative signal embedded in noise, when the logarithm of the noise density is concave downward. The proof was based on the existence of a nonunique continuous extension of the noise density, so that implementation of the result depended on a proper choice of this continuous extension. We have also previously\(^{(22)}\) derived an analogous result for the case of multiple \((N>1)\) independent observations of a nonnegative (or nonpositive) signal random variable embedded in an additive, independent, and non-interfering noise random variable, where the range of the signal and noise is discrete.

B. THE EFFECTS OF WAVE NOISE ON THE ABSORPTION AND DETECTION OF INFRARED AND OPTICAL RADIATION*

(P. R. Prucnal, M. C. Teich, G. Vannucci)

The great variety of photocounting distributions that can be generated with intensity-modulated radiation is by now well known.\(^{(1)}\)-\(^{(15)}\) It is evident that modulation broadens these distributions; this can be interpreted as an accentuation of photon bunching since both low- and high-count probabilities are increased at the expense of counts near the mean. Indeed the extent of the broadening appears to depend strongly on the intensity distribution of the underlying radiation.\(^{(6)}\) However, the counting distributions for intensity-modulated radiation can be characterized by a number of widely recognized and accepted statistical parameters, which have thus far received little attention.

Such modulation is sometimes deliberate, but more often is unavoidable. It may be imparted to the underlying radiation by mechanisms as diverse as transmission through a stochastic channel (e.g., the turbulent atmosphere\(^{(7)}\)(\(^{(9)}\)) and power-supply ripple.\(^{(6)}\) It is also important when the source is pulsed (e.g., exponentially decaying\(^{(14)}\)) rather than continuous. The analysis presented here applies also to nuclear counting\(^{(5)}\) and neural counting.\(^{(16)}\) It will generally not be applicable in the presence of dead time.\(^{(17)}\)

We have obtained detailed statistical properties such as the cumulants, and the central, factorial, and ordinary moments for counting distributions when the incident radiation is intensity modulated with arbitrary statistics.\(^{(18)}\) Our calculations are valid for the case where the integrated intensity is separable into a product of modulation-dependent and modulation-independent components. The results are applied
to the case of triangular, sinusoidal, and square-wave modulation of superposed coherent and chaotic radiation. The coefficient of variation, skewness, and kurtosis have been obtained as a function of modulation depth. Comparison has been made with experimental data in the cases of triangular and sinusoidal modulation of a laser source.

We also recognize that the photon statistics generated by thermal and chaotic light sources have evoked substantial interest ever since the well-known experiment by Hanbury-Brown and Twiss\(^{(19)}\)\(^{(20)}\) demonstrated the occurrence of photon correlation in light generated by natural sources. With most natural sources, however, the time scale over which photon correlation is observable is typically very short and is often virtually negligible; indeed very sensitive and carefully designed experiments are usually required in order to observe such correlation. Correspondingly, the coherence time of the associated electromagnetic field is very short for such sources, as the coherence time provides a measure of the time scale over which variations occur in the intensity of the field.\(^{(21)}\)

To circumvent this difficulty, a number of researchers have devised a variety of techniques to generate simulated chaotic light with an increased coherence time in the laboratory. Most of these techniques require a laser as the primary source of light, since they make use of the narrow bandwidth and high degree of coherence of laser radiation. They generate chaotic light by simulating, to different degrees, the physical characteristics of natural sources of chaotic light. One such method\(^{(22)}\)\(^{(23)}\) consists of scattering laser light from particles suspended in a fluid, each particle acting as an independent radiator whose frequency is the laser frequency, Doppler-shifted by the Brownian
motion of the particle. In this configuration, the spectral bandwidth and shape can be adjusted to some extent by manipulating the statistical distribution of the size of the particles. Another method consists of scattering laser light from a moving rough surface, such as a rotating ground-glass screen\(^{(24)(25)}\) or a rotating roughened wheel;\(^{(26)}\) here the different surface elements act as independent radiators, and the bandwidth of the light can be adjusted by varying the speed of motion of the surface. Reference \((27)\) provides a survey of the properties of scattered light in general.

If only the intensity variations of chaotic light are of interest (as is the case for the statistics of photon arrivals), it is possible to use the method suggested by Ruggieri et al.\(^{(28)}\) to simulate a superposition of coherent and chaotic radiation. This method uses two independent generators of Gaussian random noise to simulate the in-phase and quadrature components of the radiation field. The sum of the squares of these components yields the simulated light intensity, which is then used to modulate the output of a laser source. It should be noted that this method is less physical than the others cited above, since only the intensity (amplitude) variations of a chaotic radiation field are reproduced (the phase of the field depends solely on the characteristics of the primary laser source). Indeed, the narrow bandwidth and high degree of coherence of laser radiation are not necessary in this type of simulation, since the laser is used only to generate photons with the statistics of a Poisson point process whose rate can be controlled by modulating the intensity of the radiation. An arbitrary source yielding photons with the statistics of a Poisson point process with constant
rate can be used in place of the laser to obtain the same simulated photon statistics (doubly stochastic Poisson process\(^{(21)}\)). Furthermore, it should be noted that with independent generators, only a limited class of power spectra can be reproduced.

We have shown how a small laboratory computer can be used to generate the two random processes needed for this particular type of simulation.\(^{(29)}\) The computer can drive the modulator directly through a digital-to-analog converter. The advantages of using the computer include increased flexibility since an arbitrary spectral shape can be easily simulated. Increased accuracy and simplicity in the experimental setup are other benefits since critical adjustments, noise filtering, and matching of the two independent noise generators are not necessary.

The most useful application of this technique will likely be in conjunction with another program that simulates a Poisson point process with a given rate, to generate computer-simulated photocounting statistics under arbitrary conditions. This will be very useful for the study of systems that are not amenable to analytic solutions, such as photocounting with different types of dead time in conjunction with chaotic light of a given spectrum.

*Portions of the research were also supported by the National Science Foundation under Grant NSF-ENG78-26498.


(3) P. Pearl and G. J. Troup, Phys. Lett. **27A**, 560 (1968). Equation (3) in this paper is incorrect and should be replaced by Eq. (38) of Ref. 6.


C. PHOTON COUNT ANTIBUNCHING FOR OPTICAL COMMUNICATIONS, RADAR, IMAGING, AND SPECTROSCOPIC APPLICATIONS

(M. C. Teich, G. Vannucci)

In the absence of dead time, the probability \( p_0(n|W_s) \) of recording exactly \( n \) counts in a time interval \( T \) from a detector illuminated by a source of radiation with constant intensity is

\[
p_0(n|W_s) = \frac{W_s^n}{n!} \exp(-W_s) .
\]

Here \( W_s = (\lambda + \lambda_n)T \), where \( \lambda \) is the average number of counts per unit time due to the signal and \( \lambda_n \) is the average number of counts per unit time due to noise (with the assumption that noise presents itself as an independent Poisson point process with constant rate \( \lambda_n \)). This is the well-known Poisson distribution with mean \( W_s \). In the absence of radiation the probability of recording \( n \) noise counts is again given by Eq. (1) with \( W_s \) replaced by \( W_n = \lambda_n T \). If such a counter is used as a threshold detector, we seek the probability that the number of counts registered exceeds a certain threshold value \( n_t \) both in the presence and in the absence of radiation, and we denote that quantity by \( P_0(n_t, W) \) where \( W \) represents either \( W_s \) or \( W_n \). Since the events corresponding to \( p_0(n_1|W) \) and \( p_0(n_2|W) \) are mutually exclusive whenever \( n_1 \neq n_2 \), \( P_0(n_t, W) \) will be given by the expression

\[
P_0(n_t, W) = \sum_{n=n_t+1}^{\infty} p_0(n|W) = \sum_{n=n_t+1}^{\infty} \frac{W^n}{n!} \exp(-W) = 1 - \sum_{n=0}^{n_t} \frac{W^n}{n!} \exp(-W)
\]

In the presence of a fixed nonparalyzable dead time \( \tau \), we can make use of the results obtained by Ricciardi and Esposito\(^{(1)} \) and other
workers, (2)-(7) who have provided an expression for the probability of registering exactly \( n \) counts in a time interval \( t \), under the assumption that the counts occur as a Poisson point process with constant rate

\[
p(n|W, t/T) = \begin{cases} 
\sum_{k=0}^{n} p_{0}(k|W[1-nT/T]) - \sum_{k=0}^{n-1} p_{0}(k|W[1-(n-1)t/T]), & n < T/t \\
1 - \sum_{k=0}^{n-1} p_{0}(k|W[1-(n-1)t/T]), & T/t \leq n < T/t + 1 \\
0, & n \geq T/t + 1.
\end{cases}
\]

Again, the probability that the number of counts exceeds the threshold value \( n_t \) is

\[
P(n_t, W, t/T) = \sum_{n=n_t+1}^{\infty} p(n|W, t/T) = 1 - \sum_{n=0}^{n_t} p(n|W, t/T).
\]

Substituting Eq. (3) into Eq. (4) and exchanging the order of summation, we obtain

\[
P(n_t, W, t/T) = 1 - \sum_{k=0}^{n_t} \frac{[\lambda t(1-n_t t/T)]^k}{k!} \exp\left(-\lambda t(1-n_t t/T)\right),
\]

for \( n_t < T/t \).

We observe that this expression for \( P(n_t, W, t/T) \) is identical to the expression for \( P_0(n_t, W(1-n_t t/T)) \) provided in Eq. (2). Thus, for a counter with nonparalyzable dead time \( t \) and a sampling time interval \( T \),
the probability of exceeding a certain threshold number of counts \( n_t \) is the same as for a counter with no dead time that registers counts at the same rate, but during a sampling time \((T - n_t \tau)\).

This fact can be established directly, without making use of Eq. (3), through the following intuitive argument. Imagine that a Poisson point process generator is connected to the inputs of two counters in parallel, designated A and B. Counter A exhibits a nonparalyzable dead time \( \tau \) after the detection of each and every pulse (i.e., it is unable to detect additional incoming pulses during a time interval of duration \( \tau \) after the registration of a pulse). Counter B is constructed in such a way that it behaves precisely like counter A for the first \( n_t \) pulses, and thereafter behaves like a counter with no dead time.

It is clear that with such a system the probability of exceeding \( n_t \) counts is identical for both counters, since both reach \( n_t \) counts precisely at the same time. However, for \( k > n_t \) the probability that counter B records exactly \( k \) counts can be calculated by observing that it has been dead (unable to detect pulses) for an over-all length of time \( n_t \tau \), while during the remaining time interval \( T - n_t \tau \) it has detected \( k \) pulses. Since the pulses are Poisson distributed, each pulse is independent of the others, and it is irrelevant in what manner the time interval \( T - n_t \tau \) is chopped (as long as there is no correlation between where each dead-time interval \( \tau \) is placed and the pulses that are possibly killed by it). Therefore, if we denote the rate of the Poisson process as \( \lambda \), the probability of recording exactly \( k \) pulses in that length of time is given by Eq. (1) with \( W_s \) replaced by \( \lambda(T - n_t \tau) \); i.e.,
\[ P_B(k|\lambda T, \tau/T) = p_o(k|\lambda(T - n_T \tau)) \]  

\[ = \frac{[\lambda T(1 - n_T \tau/T)]^k}{k!} \exp\{-\lambda T(1 - n_T \tau/T)\} \text{ for } k > n_T. \]  

Note that this argument is valid only for \( k > n_T \) and not for \( k = n_T \); in fact, only in the former case are we certain that the counter is dead during a length of time precisely equal to \( n_T \tau \). When \( k \) is equal to \( n_T \), the dead-time interval following the last pulse might go beyond the end of the sampling time \( T \). In conclusion, the probability that counter \( B \) registers more than \( n_T \) counts is

\[ P_B(n_T, \lambda T, \tau/T) = \sum_{k=n_T+1}^{\infty} P_B(k|\lambda T, \tau/T) \]

\[ = \sum_{k=n_T+1}^{\infty} \frac{[\lambda T(1 - n_T \tau/T)]^k}{k!} \exp\{-\lambda T(1 - n_T \tau/T)\} \]

\[ = 1 - \sum_{k=0}^{n_T} \frac{[\lambda T(1 - n_T \tau/T)]^k}{k!} \exp\{-\lambda T(1 - n_T \tau/T)\} \]  

which is identical to Eq. (5). As we remarked previously, this is the same as the probability that counter \( A \) exceeds \( n_T \) counts. Equation (7) can now be used to obtain Eq. (3) by observing that

\[ p(n|W, \tau/T) = P(n-1, W, \tau/T) - P(n, W, \tau/T). \]
This argument therefore provides an alternate route to Eq. (3), for $n < T/r$.

Thus we have demonstrated the equivalence of detectors with and without nonparalyzable dead time in the presence of constant-intensity radiation and additive Poisson noise.

VI. PHYSICAL PROPERTIES AND EFFECTS IN ELECTRONIC MATERIALS

A. CARRIER TRANSPORT ACROSS SEMICONDUCTOR INTERFACES*

(H. C. Card, E. S. Yang, W. Hwang)

Since last year's report we have made substantial progress in the understanding of the interband optical transitions in metal-germanium (Schottky barrier) contacts. We have been able to interpret the wavelength dependence of the quantum efficiencies observed in terms of the fundamental optical parameters of the 50-500 Å thin metal films, and their dependence on metal thickness. We have further extended these experimental studies to the longer wavelength region in which the photoresponse is dominated by internal photoemission of electrons from the metal over the Schottky barrier, and into the conduction band(s) of the germanium.

A theoretical description of this mechanism has been developed in which we take into account the front and back optical absorptance, hot electron scattering, and multiple reflections of excited electrons from the surfaces of the thin electrode film. We have found it necessary to impose a modification of the Fowler theory of photoemission when applied to internal photoemission from thin metal films over a Schottky barrier. This modification relates to an enhanced photoexcitation within the metal films which is attributed in the present theory to a density of states which exhibits a peaked distribution in energy rather than the simple parabolic bands assumed by Fowler.

The results of this work are described in detail in publications 1-3 below.

With regard to our studies of the Si-SiO₂ interface, and of ultrathin SiO₂ layers, the potential barriers of the ultrathin SiO₂ layers in the
thickness range 20-40 Å (range limited by the experimental method) to electrons and holes tunneling between the semiconductor and the metal have been measured independently on the same MOS samples by a new experimental technique. The method combines dark measurements of current and capacitance vs. voltage with measurements of photocurrent suppression under optical illumination. The potential barriers to majority carriers are determined by the preexponential current factor after the barrier heights are obtained.

The potential barriers to minority carriers are determined from suppression of photocurrent due to the tunneling process. Analysis of the data shows that the tunneling barriers for holes are consistently much larger than those for electrons. Interpretation of these tunneling probabilities indicates that a Franz dispersion relation is not obeyed even assuming different carrier masses in the conduction band and valence band of the SiO$_2$. This work is described in publications 4 and 5.

We have recently developed an experimental method for the measurement of electron and hole capture cross sections of Si-SiO$_2$ interface states, and for their dependence on electric field. This is accomplished by frequency dependent admittance measurements of MOS structures, in a background of optical illumination, and is described in publications 6 and 7.

Our studies of electronic processes at semiconductor heterojunction interfaces is continuing, and the major studies during this year were concerned with experimental measurements of the carrier transport in AlGaAs-GaAs structures, and with the determination of the energy band discontinuity. This work is described in publications 8 and 9.

We have also discovered recently that minority carrier injection can contribute strongly to or in some cases dominate the transport current in
metal-semiconductor contacts. This work is being prepared for publication in the journal of Applied Physics (publication 10).

*This research was also supported by the Department of Energy under Contract DOE-ET-78R-031876.


(7) T. C. Poon and H. C. Card, "Admittance Measurements of Si-SiO₂ Inter-


(9) C. M. Wu and E. S. Yang, "Current Suppression Induced by Conduction-

(10) W. Hwang and H. C. Card, "Comments on Conduction Mechanisms of Metal-

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