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ACOUSTIC PROCESSING FOR ESTIMATING SIZE OF SMALL TARGETS

TO ALL WHOM IT MAY CONCERN:

BE IT KNOWN THAT ANTHONY A. RUFFA, citizen of the United States of America, employee of the United States Government and resident of Hope Valley, County of Washington, State of Rhode Island has invented certain new and useful improvements entitled as set forth above of which the following is a specification:

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DATE OF SIGNATURE
ACOUSTIC PROCESSING FOR ESTIMATING SIZE OF SMALL TARGETS

STATEMENT OF GOVERNMENT INTEREST

The invention described herein may be manufactured and used by or for the Government of the United States of America for Governmental purposes without the payment of any royalties thereon or therefor.

CROSS REFERENCE TO OTHER PATENT APPLICATIONS

Not applicable.

BACKGROUND OF THE INVENTION

(1) Field of the Invention

The present invention relates generally to acoustic processing, and more particularly to an acoustic processing method that can be used to estimate the size of small objects in a fluid medium.

(2) Description of the Prior Art

It is difficult to generate an image of an object using acoustic echoes when the object size is on the order of the wavelength of the acoustic radiation used to generate the echoes. At lower frequencies, or smaller sizes, scattering
becomes less "specular" and more "diffracting" in nature. While there have been some successful efforts involving the imaging of small objects in the near field, the technique cannot be extended to the imaging of small objects in the far field. If such far field imaging could be achieved, it could be used in medical acoustic, sonar, and particle detection on semiconductor wafer evaluation applications. In each of these applications, it may also be desirable to know the size of the small object, e.g., a tumor or other physical abnormality in medical acoustic applications, a mine-like object in sonar applications, and an imperfection in a semiconductor in wafer evaluation applications.

SUMMARY OF THE INVENTION

Accordingly, it is an object of the present invention to provide a method of acoustic processing that can be used to estimate the size of a small object.

Another object of the present invention is to provide a method of acoustic processing that can be used to estimate the size of an object that is smaller than one to two wavelengths of the acoustic radiation directed towards the object for the purpose of generating reflections or echoes therefrom.
Still another object of the present invention is to provide a method that uses only a single orientation of a sensor array to estimate the size of a small object.

Other objects and advantages of the present invention will become more obvious hereinafter in the specification and drawings.

In accordance with the present invention, a method for estimating the size of an object begins with monitoring acoustic radiation originating from a region of a fluid medium using a line array of $N$ acoustic receivers such that $N$ signals indicative of the acoustic radiation are generated. It is assumed that the acoustic radiation has a known wavelength $\lambda$. $M$ time series summations are formed using the $N$ signals. Each of the $M$ time series summations is formed using a unique time delay predicated on a corresponding unique estimated speed of propagation of the acoustic radiation where $M$ estimated speeds of propagation are defined. A temporal Fourier transform is performed on each of the $M$ time series summations to generate $M$ values. For an object in the region having a diameter $D<2\lambda$, the $M$ values will vary as a function of the $M$ estimated speeds of propagation. The resulting distribution of the $M$ values are indicative of diameter $D$. 
BRIEF DESCRIPTION OF THE DRAWINGS

Other objects, features and advantages of the present invention will become apparent upon reference to the following description of the preferred embodiments and to the drawings, wherein corresponding reference characters indicate corresponding parts throughout the several views of the drawings and wherein:

FIG. 1 is a diagrammatic view of an acoustically opaque screen having a two dimensional aperture formed therethrough where the screen is subjected to a planar acoustic wave on one side thereof to illustrate the propagation of the acoustic radiation passing through the aperture on the other side of the screen;

FIG. 2 is a schematic view of a line array of acoustic receivers used to detect acoustic radiation originating from targets located in both the end fire beam of the array and in beams away from end fire;

FIG. 3 is a flowchart of the method of the present invention;

FIG. 4A is a schematic view of a first embodiment of a system for processing the acoustic radiation received by the receivers in FIG. 2 in accordance with the present invention; and
FIG. 4B is a schematic of a second embodiment of a system
for processing the acoustic radiation received by the receivers
in FIG. 2 in accordance with the present invention.

DESCRIPTION OF THE PREFERRED EMBODIMENT(S)

Before describing the method of the present invention, it
will be beneficial to describe some background concepts on which
the present invention is predicated. Referring now to the
drawings, and more particularly to FIG. 1, an infinite,
acoustically opaque screen is referenced by numeral 10. Screen
10 has an aperture 12 formed therethrough. On one side of
screen 10, an acoustic source 14 propagates a planar acoustic
wave 16 towards screen 10. If the diameter of aperture 12 is
small (e.g., on the order of the wavelength of acoustic wave
10), acoustic wave 16 diverges as it passes through aperture 12
to form diverging waves 18-1, 18-2, ... traveling at a range of
velocities. The slowest velocities are found in the diverging
waves moving approximately parallel to screen 10 (e.g., wave 18-
1) and the fastest velocities are found in the diverging waves
moving approximately perpendicular to screen 10 (e.g., wave 18-
4).

The method of the present invention takes note of the fact
that an exact solution for (acoustic wave) diffraction of a two-
dimensional aperture in an infinite screen is given as
See G.C. Gaunaurd et al., J. Acoust. Soc. Am., Vol. 63, p. 5, 1978. In equation (1), \( p \) is the acoustic pressure, \( F(k_x, k_y) \) is the two-dimensional spatial Fourier transform in the screen that is in the X-Y plane, and \( k \) is the propagation wavenumber in the \( z \) direction. This equation solves the governing equation exactly and meets all boundary conditions.

The above diffraction integral can be evaluated using the generalized method of exhaustion to more clearly see the behavior of each component using the following

\[
\int_0^b f(x) \, dx = b \sum_{n=1}^{\infty} \sum_{m=-\infty}^{\infty} (-1)^m 2^{-n} f(mb/2^n) \tag{2}
\]

This method of exhaustion is disclosed by A.A. Ruffa, International Journal of Mathematics and Mathematical Sciences 31(6), 8 August 2002, p. 345. Note that propagating waves will only occur when the transverse wavenumber \((k_x^2 + k_y^2)^{1/2}\) is lower than the cutoff wavenumber, so the integral can be evaluated to \( \pm k \) with good accuracy (assuming that \( F(k_x, k_y) \) is an even function with respect to both \( k_x \) and \( k_y \)) as follows

\[
p(x, y, z, t) = \frac{e^{-i\omega t}}{4\pi^2} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} F(k_x, k_y) e^{-ik_x x} e^{-ik_y y} e^{i\sqrt{k_x^2 + k_y^2} z} \, dk_x dk_y \tag{1}
\]
From this expression, it can be shown that the resulting field is due to a summation of an infinite number of contributions (e.g., waves 18-1, 18-2, ...), each propagating at a different phase speed (and hence a different group speed) based on its value of $k_x$ and $k_y$.

The acoustic field radiating from such an aperture will have a continuous range of velocities, the amplitude distribution of which will depend on the Fourier transform of the field at the aperture $F(k_x, k_y)$. For example, if the field scattered from acoustic source 14 is replaced by plane wave of infinite extent, $F(k_x, k_y)$ becomes a Dirac delta function and the velocity distribution reduces to that of a single velocity. If, on the other hand, the aperture is very small compared to a wavelength, then $F(k_x, k_y)$ will be nearly constant up to the cutoff wavenumber and the propagation velocity distribution will be much larger.

In equation (3), the aperture will radiate propagating waves 18-1, 18-2, ... as long as $k^2 \geq k_x^2 + k_y^2$ (the cutoff wavenumber). For spanwise wavenumbers $k_x$ and $k_y$ that do not meet this condition, the resulting field will not propagate, but rather will be a decaying evanescent field. The phase speed will increase from $c$ at the zero spanwise wavenumber to infinity at the cutoff wavenumber. The group speed, however, will decrease from $c$ to zero at the cutoff.
wavenumber. The group speed is independent of range and is
given as

\[ c_g = c \sqrt{1 - (k_x^2 + k_y^2)/k^2} \]  \hspace{1cm} (4)

Large decreases in group speed will lead to increased Doppler
shifts. This can be potentially useful for low-Doppler targets.

Also, if the velocity distribution of the acoustic field
(associated with waves 18-1, 18-2, ...) can be measured, it will
be directly related to \( F(k_x, k_y) \), and therefore provide
information on the effective size of aperture 12.

The present invention provides a method for estimating the
size of a small object in a fluid medium using the principles
described above. To explain the present method, reference will
be made to FIG. 2 where two small objects 20 and 22 are assumed
to reside in a fluid (e.g., water) medium. A linear (or line)
array 30 of acoustic receivers are placed in the fluid medium.
As illustrated, object 20 lies in the end fire region of array
30 and object 22 lies in region away from the end fire of array
30.

The number of receivers used is not a limitation of the
present invention. In general, \( N \) acoustic receivers will be
discussed herein. Each of receivers 32-1 to 32-N is capable of
passively detecting acoustic radiation (waves) 21 and 23
originating from each of objects 20 and 22, respectively. Typically, acoustic radiation 21 and 23 is representative of acoustic reflections caused when an acoustic source 24 transmits acoustic radiation 25 of a known wavelength into the region(s) in which objects 20 and 22 reside. However, it is to be understood that use of acoustic source 24 is not a requirement or limitation of the present invention.

The present invention will first be described for estimating the size of object 20 lying in the end fire region of array 30. The N signals detected by N-channel array 30 are indicative of acoustic radiation (reflections) 21. The continuously received signals are sampled at a time based on the relative location of each acoustic receiver in array 30 and the speed of propagation of acoustic radiation (reflections) 21. For the end fire situation, acoustic receiver 32-1 is sampled at a time t and each successive receiver is sampled at a time delayed from t where the time delay is a function the distance d from acoustic receiver 32-1 and the speed of propagation of acoustic radiation (reflections) 21.

Based on the concepts for an aperture in an infinite screen described above, the speed of propagation of radiation (reflections) 21 will be a distribution of speeds if the size of object 20 is on the order of the wavelength of acoustic radiation (reflections) 21. More specifically, if object 20 has
a diameter $D$ that is less than approximately twice the
wavelength of acoustic radiation (reflections) 21, there will be
a distribution of propagation speeds that is indicative of the
size of object 20. In its simplest form, the present invention
assumes or approximates a circular shape for object 20.

However, it is to be understood that the invention can be used
to approximate other shapes for object 20 at the expense of more
complicated processing.

Assuming the size of object 20 is on the order of the
wavelength of acoustic radiation (reflections) 21, the present
invention determines the distribution of the speed of
propagation associated therewith. To do this, $M$ different
speeds of propagation are estimated and used in the processing
of the sampled signals from array 30. The $M$ different speeds
define a range of distribution of speeds that acoustic radiation
(reflections) 21 are expected to exhibit for the size of an
object (e.g., object 20) of interest.

In FIG. 3, there is shown a flowchart providing the method
of using this invention. This flowchart is made for the
embodiment in which an acoustic signal (25 in FIG. 2) is
transmitted toward an object (20 or 22 in FIG. 2) in step 36 and
reflects (21 or 23 in FIG. 2) from the object. Step 36 can be
omitted when the object is radiating an acoustic signal at a
known wavelength. The acoustic signal is received 38 at an
array of sensors 30. The received signal at each sensor is
processed 40 in parallel. In one embodiment, the step of
processing 40 can be merely forming an amplitude sum of the
signals received at each sensor. This is further detailed in
the discussion of FIG. 4A below. In another embodiment, the
step of processing 40 can be forming an amplitude sum of the
signals and then performing a temporal Fourier transform of the
signals. This is further detailed in the discussion of FIG. 4B
below. In either case, processing 40 accounts for the
orientation of the array 30 and the spacing of sensors 32-1
through 32-N while calculating the amplitude sum. In step 44,
the invention determines if velocity spreading exists in the
amplitude sums. If velocity spreading does not exist, the
object must be larger than two wavelengths (2λ), and a different
method must be used to determine size. If velocity spreading
does exist, a database of known object data 48 can be compared
in step 50 with the amplitude sums and the Fourier transforms to
give information about the object. In the most basic case, the
known object database 48 contains data from disks having a range
of diameters below the two wavelengths limit. In a more
complicated case, the know object database 48 contains objects
having a variety of different shapes, sizes and orientations.
These objects can be disks, spheres or cylinders. The
comparison step 50 provides an output of the diameter of the
object, the object's shape, and/or the object's orientation.

Output is provided in step 52 to a user or to another system.

Processing of the N sampled signals $s_i$ for $i = 1$ to $N$ is carried out as illustrated in FIGs. 4A and 4B where parallel processing (e.g., by individual processors or one parallel processor) improves processing efficiency; however, sequential processing can be used. Each of M processors 40-1, ..., 40-M forms a sum $V(t)$ of the time sampled signals $s_i$ where the first term in each summation is the signal sampled at acoustic receiver 32-1 at time $t$ and each successive $i$-th term is delayed by $(2\pi d_i/c_m)$ where $d_i$ is the distance from the $i$-th receiver to receiver 32-1, $c_m$ is an estimated speed of propagation for the $m$-th processor, and $f$ is the frequency of acoustic radiation (reflections) 21. Each of the resulting M time series summations (e.g., voltage signals $V_m(t)$) for $m = 1$ to M can have (as illustrated by the FIG. 4B embodiment) a temporal Fourier transform applied thereto at 42-1, ..., 42-M as a measure of the Doppler shift $\Delta f$. Lower speeds of propagation lead to increased Doppler shifts. The Doppler shift measurements are an independent check on each propagation velocity.

An amplitude distribution as a function of speed of propagation $c_m$ for $m = 1$ to M indicates the presence of a "small" target. Conversely, little or no velocity spread is indicative of the fact that no "small" targets are present in the region of
interest. Assuming there is a velocity distribution, the actual amplitude (voltage) distribution as a function of $c_m$ is used to estimate the size of object 20 as follows. The measured distribution is compared to a plurality of two-dimensional spatial Fourier transform distributions determined for a corresponding plurality of known-dimension, circular apertures in infinite acoustically-opaque screens. The aperture size of the spatial Fourier transform distribution that most closely matches the measured/determined amplitude distribution (vs. $c_m$ approximates a (circular shape) size of object 20.

For object 22 that resides away from the end fire of array 30, processing in each beam of array 30 would proceed the same as described above so that the amplitude would again be estimated for each of the $M$ estimated speeds of propagation $c_m$. Away from end fire, the effect of a distribution of propagation speeds is exhibited as a "beam spreading" effect where slower acoustic velocities lead to signals in adjacent beams. Beam spreading also occurs due to multipaths, which would show up in adjacent beams closer to broadside. In active sonar (e.g., where acoustic source 24 provides acoustic radiation that generates reflections 21), the main path could be identified as the one arriving first. As is known in the art, this can be accomplished with replica correlator processing. Multipaths would appear in adjacent beams closer to broadside while any
velocity distribution would lead to adjacent beams further away from broadside and involving velocities slower than the speed of propagation in the main path. The resulting Doppler shifts would be increased in adjacent beams due to the slower acoustic velocity in the beam. Since this would not occur as a result of multipaths, it provides a method to distinguish between beam spreading due to a velocity distribution with that due to multipaths.

The advantages of the present invention are numerous. Small underwater targets can have their size estimated. Such size estimation is an important clue used in target classification.

It will be understood that many additional changes in the details, materials, steps and arrangement of parts, which have been herein described and illustrated in order to explain the nature of the invention, may be made by those skilled in the art within the principle and scope of the invention as expressed in the appended claims.
ACOUSTIC PROCESSING FOR ESTIMATING SIZE OF SMALL TARGETS

ABSTRACT OF THE DISCLOSURE

A method is provided for estimating the size of an object from a region of a fluid medium when that object is emitting acoustic radiation of known wavelength $\lambda$ on its own or as the result of being interrogated by acoustic pulses that reflect from the object. The acoustic radiation is monitored using a line array of $N$ acoustic receivers such that $N$ signals indicative of the acoustic radiation are generated. $M$ time series summations are formed using the $N$ signals. Each of the $M$ time series summations is formed using a unique time delay predicated on a corresponding unique estimated speed of propagation of the acoustic radiation where $M$ estimated speeds of propagation are defined. For an object in the region having a diameter $D$ on the order of $\lambda$, the $M$ values will vary as a function of the $M$ estimated speeds of propagation with the resulting distribution of the $M$ values being indicative of diameter $D$. 
FIG. 4A

N SIGNALS FROM ACOUSTIC RECEIVERS 32

\[ V_1(t) = \sum_{i=1}^{N} S_i(t) \frac{2 \pi C_1}{f} \rightarrow \Delta f_1 \]

\[ V_2(t) = \sum_{i=1}^{N} S_i(t) \frac{2 \pi C_2}{f} \rightarrow \Delta f_2 \]

\[ \vdots \]

\[ V_m(t) = \sum_{i=1}^{N} S_i(t) \frac{2 \pi C_m}{f} \rightarrow \Delta f_m \]

\[ \vdots \]

\[ V_N(t) = \sum_{i=1}^{N} S_i(t) \frac{2 \pi C_N}{f} \rightarrow \Delta f_N \]

FIG. 4B

N SIGNALS FROM ACOUSTIC RECEIVERS 32

\[ V_1(t) = \sum_{i=1}^{N} S_i(t) \frac{2 \pi C_1}{f} \rightarrow \text{TEMPORAL FOURIER TRANSFORM} \rightarrow \Delta f_1 \]

\[ V_2(t) = \sum_{i=1}^{N} S_i(t) \frac{2 \pi C_2}{f} \rightarrow \text{TEMPORAL FOURIER TRANSFORM} \rightarrow \Delta f_2 \]

\[ \vdots \]

\[ V_m(t) = \sum_{i=1}^{N} S_i(t) \frac{2 \pi C_m}{f} \rightarrow \text{TEMPORAL FOURIER TRANSFORM} \rightarrow \Delta f_m \]

\[ \vdots \]

\[ V_N(t) = \sum_{i=1}^{N} S_i(t) \frac{2 \pi C_N}{f} \rightarrow \text{TEMPORAL FOURIER TRANSFORM} \rightarrow \Delta f_N \]