Millimeter-Wave and Submillimeter-Wave/Terahertz Passive Imaging System Requirements: A Phenomenological Perspective

by Steven R. Murrill
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Millimeter-Wave and Submillimeter-Wave/Terahertz Passive Imaging System Requirements: A Phenomenological Perspective

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The phenomenology of imaging in the millimeter-wave (MMW) and submillimeter-wave (SMMW)/terahertz (THz) frequency regimes is investigated and described. The primary factors related to imaging in these frequency regimes are phenomenologically driven and involve trade-offs between spatial (angular) resolution; the impact of atmospheric and obscurator attenuations such as fog, dust, and concealing materials; and system sensitivity requirements. Minimum system sensitivity requirements for adequate imaging in three important military/security scenarios are identified and described in terms of minimum apparent temperature differences between targets and their backgrounds. Mathematical equations for calculating the minimum system sensitivity (noise equivalent power [NEP] per root hertz [Hz]) required to provide image frames with enough signal-to-noise ratio (SNR) to produce good imagery at video frame rates are derived.

Millimeter-Wave, Sub-Millimeter-Wave, Terahertz, Imaging System, Phenomenology, Apparent Brightness Temperature, Contrast Ratio, SNR, SCR
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1. Introduction

Renewed interest and investment in millimeter-wave (MMW) (millimeter wavelength ($\lambda$)—nominally 30 GHz [$\lambda = 10$ mm] to 300 GHz [$\lambda = 1$ mm]) and submillimeter-wave (SMMW)/terahertz (THz) (submillimeter wavelength—nominally 0.3 THz [$\lambda = 1$ mm] to 3 THz [$\lambda = 0.1$ mm]) imaging technology has increased in recent years. Demand for imaging in degraded visual environments (DVEs) and for imaging concealed weaponry carried by people in both the domestic and theater-of-operations realms is on the increase. Currently, MMW imaging technology has demonstrated the potential to image through such obscurants as atmospheric fog, smoke, blowing dust, and sand (brownout); and concealment materials such as clothing. SMMW/THz imaging technology also offers the potential to image through these obscurants, but with higher spatial resolution for a given imaging system aperture size, allowing the potential for target/weapon detection or identification at greater, more-useful (safer) standoff ranges.

Many MMW and SMMW/THz imaging system approaches are now being investigated including active-illumination-based systems, passive-illumination/emission-based systems, continuous-wave (CW) systems, and time-domain (active, pulsed) systems. Typical system architectures include focal-plane-array (FPA), scanning line-array, and single-pixel scanning receiver (and possibly transmitter) sub-systems. In general, active-illumination imaging systems are more complex than passive (CW) imaging systems, but offer the potential to produce imagery with better target-to-background contrast ratios (CRs) and better signal-to-noise ratios (SNRs). Concurrently, active-illumination-based systems typically produce imagery that is more specular in nature, which can also be degraded by clutter from illumination backscatter. Passive-illumination-based systems are dependent on both natural/environmental illumination and target/background emissions, but typically produce imagery that is less specular and more natural in appearance.

This report focuses on passive MMW and SMMW/THz imaging system requirements that are shaped and driven by the imaging phenomenology. The perspective is that the phenomenology then drives the critical imaging characteristics of apparent target-to-background CRs, system receiver target and background signal (power) levels, and signal (target)-to-clutter ratios (SCRs). As such, the system receiver characteristics combined with the phenomenology drive the system signal-to-noise plus clutter ratios (SNCRs). This report compares and contrasts the MMW and SMMW/THz imaging regimes, and explores three important imaging scenarios: in-flight obstacle avoidance, landing/takeoff obstacle avoidance, and concealed weapon detection/identification. While many passive MMW and SMMW/THz imaging systems have been constructed throughout the United States (and the world) that can produce high-quality, reasonable-contrast, and low-noise imagery given adequate frame times of seconds to minutes, few passive systems are capable of producing useful imagery at real-time video rates (nominally
30 Hz). This report draws conclusions about the critical receiver sensitivity levels required to provide useful, real-time (video rate) passive imagery in the scenarios explored.

2. Imaging Phenomenology

Several phenomenological effects shape and impact the ability to image objects/targets of interest in the MMW and SMMW/THz frequency regimes. Following is a brief synopsis of the primary factors involved.

2.1 Atmospheric Effects

The primary impact of the atmosphere on MMW and SMMW/THz imaging is attenuation, principally due to water vapor, and scattering from atmospheric particles (1, 2). Figures 1 and 2 (from Rosker et al. [1, 3]) plot atmospheric attenuation as a function of frequency over different ranges. Table 1 lists the atmospheric conditions plotted in figures 1 and 2. Both plots show that atmospheric attenuation increases significantly from approximately 100 GHz to 10 THz with windows of relatively low attenuation. From figure 1, it is interesting to note that in the region of approximately 100 GHz, the atmospheric attenuation is about the same as it is in the 8–12 µm window. Also, note that the primary atmospheric condition that is extremely detrimental to imaging in the visible region is fog, which has little impact in the MMW regime. Figure 2 shows the large variation in atmospheric attenuation for different, normally occurring environmental conditions (1).

![Figure 1. Attenuation (dB/km) across the electromagnetic spectrum at sea level based on currently accepted models. Rain = 4 mm/h, fog = 100 m visibility, STD (standard atmosphere) = 7.5 gm/m³ water vapor, and 2XSTD = 15 gm/m³ water vapor (excerpted from Rosker et al. [1, 3]).](image-url)
The primary impact of the atmosphere on an imaging system’s capability to provide imagery useful for detecting or identifying concealed weapons carried by people is the reduction in the SNCR in the sensor image. A lower SNCR can result from reducing the illumination function on the scene (active illumination or sky illumination), reducing the signal reflected or radiated by the scene, or having an intermediate scattering effect. The SNCR is affected by the transmitted power (or the temperature of the surrounding environment in the case of passive imaging); the receiver sensitivity; the reflectivity of the weapon (generally close to one) and skin; and finally the attenuation (or emissivity and reflectivity) of any intervening material, e.g., clothing (1).

Loss from the atmosphere tends to drive system designs to lower frequencies while accepting the loss in resolution or accepting a larger aperture/antenna.

### 2.2 Other Obscurant Effects

In addition to the atmosphere (primarily fog), other imaging obscurants exist, including dust, smoke, and for the case of imaging concealed weapons carried by people, clothing materials.
Several studies designed to measure the impact of dust on imaging in the MMW regime demonstrate that in heavy dust situations that completely obscure imaging in either the visible or infrared (IR) regimes, there is minimal impact on transmission through dust clouds at MMW lengths, and thus, minimal impact on MMW imaging. In one study, Wikner measured losses less than 0.02 and 0.08 dB for 94 and 217 GHz, respectively, across 1 m of dust with a density of 3000 mg/m$^3$ (4). In a second study, Schuetz et al. measured an average attenuation of 1.14 dB/km at 77 GHz through a dust cloud created from slow flyovers by a small military helicopter (5). In a third experiment, Mackrides et al. measured a peak attenuation of approximately 20% (0.97 dB) at 77 GHz through a dust cloud created from slow flyovers by a large, heavy military helicopter (6). Figure 3 illustrates the dust cloud attenuation measurement setup for this third experiment. Figure 4 shows a plot of W-band (77 GHz) attenuation during the rotary craft flyovers.

![Figure 3](image1.png)

**Figure 3.** Dynamic W-band dust cloud attenuation setup at Yuma Proving Ground (YPG) used to measure the attenuation due to dust clouds for small, medium, and large rotary aircraft (excerpted from Mackrides et al. [6]).

![Figure 4](image2.png)

**Figure 4.** Plot of attenuation within the W-band during the rotary craft flyovers (excerpted from Mackrides et al. [6]).
Attenuation from smoke in the MMW and most of the SMMW/THz imaging regimes will be minimal, as the particle size of smoke is significantly smaller than MMWs.

Studies on the impact of clothing material on the attenuation of MMW and SMMW/THz electromagnetic (EM) radiation show a strong dependence on frequency, material type, and material thickness. One study by Bjarnason et al. that performed transmission measurements on cloth samples from eight types of fabric common in garments and baggage found the following:

- Transmission measurements revealed that all clothing samples were adequately transparent at MMW frequencies up to approximately 300 GHz (based on a 3-dB criterion).
- At frequencies near 1 THz, the average transmission was down by approximately 8 dB with an approximately 9-dB spread.
- Attenuation in the IR region was very high (approximately 25 dB) for all sample types except rayon and nylon (~12 dB of attenuation). The significantly higher transmission through rayon and nylon is attributed to pores intrinsic to these materials.
- Surface backscattering was not measured; however, microphotographs reveal roughness on the scale comparable to a THz wavelength, particularly in the coarse filamentary pattern of nylon and the interlaced weave of rayon and silk. Because these three sample types were found to be the most transparent, it is surmised that any surface scattering must be fairly weak (7).

Figure 5 shows a plot of the results.
Another study on the impact of clothing material on the attenuation of MMW and SMMW/THz EM radiation by Petkie et al. measured similar results and found the following:

- Static transmission results through 13 different single-layer clothing items indicate transmission levels greater than 50% from approximately 100 to 600 GHz.

- Dynamic transmission results through an overcoat that was slowly “waved” to mimic the motion of clothing on a moving person show a variation on the order ±10%. It is speculated that this level of variation may also be present as a spatial modulation across a static target and that this “clutter” may present more of a limitation to imaging systems than the loss of signal intensity.

- Coherent effects in the clothing material were observed by varying the angle of incidence of the radiation beam. Variations in transmission on the order of approximately 12% were observed as a function of incident radiation angle.

- Active imaging at 640 GHz yielded high resolution and contrast, but also showed coherent effects that can lead to fringes in the images (8).

Figure 6 shows a plot of the results.
2.3 Sky Illumination

For passive MMW imaging systems, where the reflectivities of many objects are relatively high and the wavelengths of the propagating EM radiation are typically substantially longer than the surface roughness of many objects of interest, the apparent sky temperature is an important consideration for detecting objects with different reflectivities. The sky temperature can either enhance the apparent signature of highly reflective items, such as metal weapons (if the imaging geometry is correctly oriented), or it can create an apparent or confusing element in the scene, such as when reflective clothing or skin obscures the detection of weapons ([1]). Figure 7 (from Rosker et al.) plots the apparent sky temperature as a function of frequency.
Note that while passive MMW systems operating at, say, 94 GHz may be designed to exploit the sky as an illuminator, the available contrast rapidly diminishes as frequency increases in all but the driest environmental conditions. Above approximately 300 GHz, the apparent sky temperature is essentially the same as the background (~300 K) (1).

The apparent sky temperature is a strong function of angle from zenith, especially under high-attenuation and/or foggy environmental conditions. Generally, the apparent temperature of the sky is the coldest at zenith and can progressively warm to a maximum at the horizon sky. The horizon sky is typically the part of the sky that has the highest brightness temperature because the path attenuation (hence emission) through the atmosphere is the highest in that direction. In fog, the absorption of MMW energy along a path to the horizon is high enough to make its brightness temperature equal to the ambient air temperature (9).

2.4 Target/Background Reflectivities and Emissivities

For active imaging, the signature (target-to-background contrast) is determined by small differences in reflectivity across the band. For passive imaging, the contrast mechanism changes as frequency increases. At frequencies of 100 GHz and below, the optical properties of, for example, the body and explosives are dominated by their reflectivity and it is the geometry that gives rise to the signature. In passive imaging above 100 GHz, the signature is produced by the differences in emissivity and reflectivity between skin and explosives or metal. At frequencies of 500 GHz and above, the optical properties are dominated by emissivity and it is the physical temperatures, along with emissivities, which predominately determine the passive signature.

As frequency increases, emissivity increases while both transmission and reflectivity of non-metallic objects tend to decrease. Where emissivity dominates the optical properties, the passive signature becomes more a function of the physical temperatures of the object and background, as in the IR region of the EM spectrum. Table 2 (from Appleby et al.) lists the emissivity, reflectivity, and transmission of various materials relevant to the concealed weapons detection/identification imaging scenario. Note that while the difference in reflectivity at 100 GHz between human skin (r = 0.35) and an explosives pack on the skin (r = 0.24) will produce enough contrast for detection of the target (explosives pack), above 500 GHz this difference is substantially reduced with skin (r = 0.09) and the explosives pack on the skin (r = 0.05). The decrease is due primarily to the increase in emissivities (2).
Table 2. Optical properties of 5-mm-thick explosives, skin, metal, denim, and T-shirt (excerpted from Appleby et al. [2]).

<table>
<thead>
<tr>
<th></th>
<th>Emissivity (ε)</th>
<th>Reflectivity (ρ)</th>
<th>Transmission (τ)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>100 GHz</td>
<td>500 GHz</td>
<td>1 THz</td>
</tr>
<tr>
<td>Explosive on skin</td>
<td>0.76</td>
<td>0.95</td>
<td>0.94</td>
</tr>
<tr>
<td>Metal</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Skin</td>
<td>0.65</td>
<td>0.91</td>
<td>0.93</td>
</tr>
<tr>
<td>Denim</td>
<td>0.09</td>
<td>0.49</td>
<td>0.85</td>
</tr>
<tr>
<td>Tee-shirt</td>
<td>0.04</td>
<td>0.2</td>
<td>0.3</td>
</tr>
</tbody>
</table>

In another study, image-based reflectivity measurements that were then used to determine the reflectivity of human skin at a wavelength of 10.6 µm (IR regime) yielded emissivity values from the skin on the back side of the hand between 0.9918 and 0.9985 at a wavelength of 10.6 µm (10).

In a third study, airborne measurements of forest and agricultural land surface emissivity at millimeter wavelengths have been obtained over a range of frequencies (20–200 GHz) and viewing angles (approximately 0° to 50°). Emissivities were measured for open water; lake ice; bare soil; frozen soil; open and close stubble and grass; open and close summer and winter forest; and winter conifers. These results are summarized in table 3 (11).

Table 3. Mean nadir emissivities for video classifications (excerpted from Hewison [11]).

<table>
<thead>
<tr>
<th>Category</th>
<th>e(24)</th>
<th>e(50)</th>
<th>e(89)</th>
<th>e(157)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water 18°C</td>
<td>0.443</td>
<td>0.513</td>
<td>0.573</td>
<td>0.668</td>
</tr>
<tr>
<td>Water 0°C</td>
<td>0.491</td>
<td>0.588</td>
<td>0.657</td>
<td>0.733</td>
</tr>
<tr>
<td>Lake Ice</td>
<td>0.908</td>
<td>0.920</td>
<td>0.922</td>
<td>0.925</td>
</tr>
<tr>
<td>Bare Soil</td>
<td>0.955</td>
<td>0.967</td>
<td>0.962</td>
<td>0.966</td>
</tr>
<tr>
<td>Frozen Soil</td>
<td>0.962</td>
<td>0.982</td>
<td>0.979</td>
<td>0.980</td>
</tr>
<tr>
<td>Open Stubble</td>
<td>0.960</td>
<td>0.966</td>
<td>0.962</td>
<td>0.974</td>
</tr>
<tr>
<td>Close Stubble</td>
<td>0.953</td>
<td>0.963</td>
<td>0.962</td>
<td>0.974</td>
</tr>
<tr>
<td>Open Grass</td>
<td>0.959</td>
<td>0.968</td>
<td>0.961</td>
<td>0.973</td>
</tr>
<tr>
<td>Close Grass</td>
<td>0.964</td>
<td>0.967</td>
<td>0.963</td>
<td>0.972</td>
</tr>
<tr>
<td>Summer Open Forest</td>
<td>0.983</td>
<td>0.985</td>
<td>0.983</td>
<td>0.990</td>
</tr>
<tr>
<td>Summer Close Forest</td>
<td>0.984</td>
<td>0.987</td>
<td>0.985</td>
<td>0.994</td>
</tr>
<tr>
<td>Winter Open Forest</td>
<td>0.985</td>
<td>0.986</td>
<td>0.985</td>
<td>0.987</td>
</tr>
<tr>
<td>Winter Close Forest</td>
<td>0.987</td>
<td>0.990</td>
<td>0.991</td>
<td>0.993</td>
</tr>
<tr>
<td>Winter Open Conifer</td>
<td>0.987</td>
<td>0.989</td>
<td>0.991</td>
<td>0.994</td>
</tr>
<tr>
<td>Winter Close Conifer</td>
<td>0.989</td>
<td>0.990</td>
<td>0.992</td>
<td>0.995</td>
</tr>
</tbody>
</table>
Additional observations made by Hewison were as follow:

- Nadir emissivities for all categories were above 0.90 except for open water (~0.4 to 0.7 depending on frequency).
- Emissivity is a strong function of incident viewing angle for lake water and lake ice. Emissivity is a weak function of incident viewing angle for bare soil, close conifers, and all other forests/conditions.

2.5 Spatial Resolution

The limiting spatial angular resolution of an imaging system using a circular focusing element/aperture is given by

$$\theta = \frac{\lambda}{D}$$  \hspace{1cm} (1)

where $\theta$ is the limiting spatial angular resolution in radians, $\lambda$ is the wavelength of the propagating EM radiation in meters, and $D$ is the imaging system aperture diameter in meters ($12$).

Using the well-known relationship between wavelength and frequency,

$$\lambda = \frac{c}{f}$$  \hspace{1cm} (2)

where $\lambda$ is the wavelength in meters, $c$ is the speed of light in meters per second ($3.0 \times 10^8$ m/s), and $f$ is the frequency in hertz, and substituting equation 2 into equation 1 yields

$$\theta = \frac{c}{fD}$$  \hspace{1cm} (3)

where again $\theta$ is the limiting spatial angular resolution in radians, $c$ is the speed of light in meters per second ($3.0 \times 10^8$ m/s), $f$ is the frequency in hertz, and $D$ is the imaging system aperture diameter in meters.

Using equation 3, table 4 shows the amount of spatial resolution that can be achieved by imaging systems operating in different frequency regimes. The calculations are based on a fixed imaging system aperture size of 0.5 m.

<table>
<thead>
<tr>
<th>EM Radiation Frequency (GHz)</th>
<th>EM Radiation Wavelength (mm)</th>
<th>System Aperture Diameter (m)</th>
<th>Limiting Angular Resolution (milliradians)</th>
</tr>
</thead>
<tbody>
<tr>
<td>100</td>
<td>3.000</td>
<td>0.5</td>
<td>6.000</td>
</tr>
<tr>
<td>640</td>
<td>0.469</td>
<td>0.5</td>
<td>0.938</td>
</tr>
<tr>
<td>30,000</td>
<td>0.010</td>
<td>0.5</td>
<td>0.020</td>
</tr>
</tbody>
</table>
The number of spatial cycles of resolution across the critical dimension of a target in object space is given by

\[ N_{\text{cyc}} = \frac{d}{\theta R} \] (4)

where \( N_{\text{cyc}} \) is the number of spatial cycles of resolution, \( d \) is the critical dimension of a target in meters, \( \theta \) is the limiting spatial angular resolution in radians, and \( R \) is the range or distance in meters between the imaging system and the target of interest.

Rearranging equation 4 and substituting equation 3 into equation 4 yields

\[ R = \frac{d \cdot f \cdot D}{c \cdot N_{\text{cyc}}} \] (5)

where again \( R \) is the range or distance in meters, \( d \) is the critical dimension of a target in meters, \( f \) is the frequency in hertz, \( D \) is the imaging system aperture diameter in meters, \( c \) is the speed of light in meters per second \((3.0 \times 10^8 \text{ m/s})\), and \( N_{\text{cyc}} \) is the number of spatial cycles of resolution across the critical dimension of a target in object space.

Using equation 5, the maximum range that an imaging system can be used to perform the task of detecting a target within a background is calculated for a range of EM radiation frequencies under the following assumptions:

- the EM radiation frequencies \((f's)\) are 100, 640, and 30,000 GHz \((30 \text{ THz}, \text{ which corresponds to a 10-µm wavelength})\),
- the critical dimension \((d)\) of the target is 3 in or approximately 0.076 m,
- the imaging system aperture diameter \((D)\) is 0.5 m,
- the speed of light \((c)\) in meters per second is \(3.0 \times 10^8 \text{ m/s}\), and
- the number of cycles on target \((N_{\text{cyc}})\) required to perform the task of detection is 1.0.

Table 5 shows the results.

<table>
<thead>
<tr>
<th>EM Radiation Frequency (GHz)</th>
<th>EM Radiation Wavelength (millimeters)</th>
<th>System Aperture Diameter (meters)</th>
<th>Critical Target Dimension (meters)</th>
<th>Spatial Cycles on Target (unitless)</th>
<th>Maximum Standoff Range (meters)</th>
</tr>
</thead>
<tbody>
<tr>
<td>100</td>
<td>3.000</td>
<td>0.5</td>
<td>0.076</td>
<td>1.0</td>
<td>12.7</td>
</tr>
<tr>
<td>640</td>
<td>0.469</td>
<td>0.5</td>
<td>0.076</td>
<td>1.0</td>
<td>81.1</td>
</tr>
<tr>
<td>30,000</td>
<td>0.010</td>
<td>0.5</td>
<td>0.076</td>
<td>1.0</td>
<td>3800.0</td>
</tr>
</tbody>
</table>
The analysis above demonstrates and quantifies the impact that both the EM wave frequency and the imaging system aperture size have on system resolution, and the ability to resolve and detect a target within a background at standoff ranges. Higher EM wave frequencies result in higher spatial resolution that can be used to detect (or identify) targets at greater standoff ranges or reduce the size of the imaging system aperture, or some combination of both. Larger imaging system apertures also result in higher spatial resolution that can be used to detect (or identify) targets at greater standoff ranges, operate at lower EM wave frequencies, or some combination of both.

3. Imaging Regimes and Scenarios

From a phenomenological perspective, passive imaging in the MMW and SMMW/THz regions does in fact divide into two general regimes close to their wavelength-based definitions with a transition region in-between. At frequencies of 100 GHz and below, the optical properties (contrast mechanism) of, for example, the human body (skin) (background) and explosive packs (target) are dominated by their reflectivity and it is then the illumination/observation geometry that gives rise to the (target-to-background contrast) signature. Between approximately 100 and 500 GHz, there is a contrast mechanism transition region where the (contrast) is produced by the combination and/or differences in emissivity and reflectivity between the target and background material, e.g., explosives or metal (target) and human skin (background). At frequencies of 500 GHz and above, the contrast mechanism is dominated by emissivity and it is the physical temperatures that largely determine the passive (target-to-background contrast) signature.

As frequency increases, emissivity increases while both transmission and reflectivity of non-metallic objects tend to decrease. Again, where emissivity dominates the optical properties, the passive signature becomes more a function of the physical temperature of the objects, as in the IR region of the EM spectrum.

Additional attributes include relatively low atmospheric, dust, smoke, and clothing-obscurant attenuations in the MMW regime, with increasingly higher atmospheric and clothing-obscurant attenuations in the SMMW/THz regime.

The following sections describe the phenomenology and the respective imaging system requirements for three important passive imaging scenarios—two in the MMW regime and one in the SMMW/THz regime.

3.1 Scenario A: In-flight Obstacle Avoidance

In 2004, Wikner performed measurements to explore the use of image processing enhancement techniques to improve passive MMW (93 GHz) imagery for use in aircraft obstacle avoidance. The effort focused on enhancing detectability of two common obstacles, a concrete office
building and a tree line, from the perspective of low-flying aircraft for terrain-following/terrain-avoidance during very challenging, low-visibility, foggy conditions. Wikner made several important observations:

- The quantity that is important for aircraft obstacle avoidance is the difference in brightness temperature between the horizon sky and the obstacle.

- The horizon sky is typically the part of the sky that has the highest brightness temperature because the path attenuation (hence emission) through the atmosphere is the highest in that direction. In fog, the absorption of MMW energy along a path to the horizon is high enough to make its brightness temperature equal to the ambient air temperature.

- Building walls usually emit a brightness temperature close to the ambient temperature, unless they have been warmed by direct sunlight. What little energy is reflected toward the sensor does not come from the cold part of the sky, but rather the warm horizon behind the sensor.

- The brightness temperature difference between the horizon sky and a tree line is typically well below zero on cold days, and just above zero on warm, humid, or foggy days. The brightness contrast between the horizon sky and a tree line in fog is consistently just a few degrees positive (typically about 2 K), due to the fact that the foggy horizon sky has a high brightness temperature compared to the (cold) sky temperature reflected off of the leaves or branches of trees in the tree line. (Note that here the leaves and tree branches are the target; more typically, they represent a cluttered background.)

- Finally, the measured data suggest that a thermal sensitivity of about 0.2 K is required for a passive imaging system operating a 30 Hz if it is to be used to reliably detect and avoid collisions with tree lines in foggy conditions (13).

3.2 Scenario B: Landing/Takeoff Obstacle Avoidance

In 2006, Wikner performed measurements to quantify the available brightness temperature contrast between various obstacles that are relevant to helicopter takeoffs and landings in a sand environment. Passive radiometric images (at 93 GHz) of various obstacles situated in a sand background were taken at various depression angles and with vertical and horizontal polarizations. Obstacles included a fence post, a large boulder, a Hedgehog, cinder blocks, a J-log, a chain-link fence, a berm, and a ditch. Key findings from the study include the following:

- There is a strong polarimetric signature/effect present for both sand and cinder block between 10° and 30° of depression angle.

- Measurements of sand at a 30° depression angle led to estimates of effective emissivities for both vertical and horizontal polarizations of 0.86, and 0.78, respectively.
• Most obstacles yielded a brightness temperature contrast of approximately 6 K, with most objects being slightly less bright than the sand background. The wooden fence post, being a good emitter, was at a brighter temperature than the surrounding sand.

• Despite good sensor thermal resolution/sensitivity (<0.3 K), the ditch was barely visible as a dark line across the image. The berm was also very difficult to detect (14).

In 2009, Schuetz et al. (15) performed a series of studies to determine the impact of dust clouds generated by helicopter landings, takeoffs, and hovering. The data were acquired using a W-band (77 GHz), dual-polarization radiometric scanner using optical-upconversion detectors. Key findings from the studies include the following:

• Static, passive MMW images were collected for 23 different landing zone obstacles against a packed dirt background. Calibrated contrast measurements were calculated for six, simple landing zone objects from this set. The six objects were a 14-cm-wide wooden post, a 0.6-m-diameter hole in the soil, a 0.6-m basaltic rock, a cinder block, a stack of adobe bricks (front aspect), and a stack of adobe bricks (top aspect). Because radiometric contrast is a function of incidence angle due to the strong gradation of sky temperature, the imager was elevated to a height of 3 m above ground level to simulate an anticipated helicopter approach angle of ~25°. Horizontal polarization root-sum-squared (RSS) target-to-background contrasts ranged from 15–28 K, while vertical polarization RSS contrasts ranged from 3–10 K.

• An E-field polarized parallel to the horizon (H-polarization) presents far better temperature contrast than the orthogonal V-polarization. This effect is due primarily to the significantly higher reflection coefficient of packed dirt to the parallel polarization state, which provides lower background temperatures due to the effective cold sky temperatures (15).

3.3 Scenario C: Concealed Weapon Detection/Identification

Due to the general requirements to detect and/or identify concealed weapons carried by people at substantial (safe) standoff distances using imaging equipment with reasonably small aperture sizes, it is assumed that imaging systems designed for this scenario would most likely operate in the SMMW/THz regime, probably in one of the 320- or 640-GHz atmospheric transmission windows (see figure 2).

From table 2, the primary contrast mechanism for the listed targets against a human skin background near 500 GHz is emissivity. Assuming that the target and background are at the same temperature, the (target-to-background) contrast will occur due to the differences in emissivities:

• The estimated CR for a metal weapon against human skin is $\frac{0.91-0.00}{0.91+0.00} = 1$.

• The estimated CR for an explosive pack against human skin is $\frac{0.95-0.91}{0.95+0.91} = 0.02$. 
Applying the CR for the case of an explosive pack against human skin at a temperature of approximately 310 K yields an equivalent blackbody temperature difference of approximately $310 \times 0.02 = 6.2$ K.

4. Imaging System Requirements

An imaging system must meet resolution requirements to allow for enough spatial cycles on target at a desired standoff distance to enable an observer to adequately perform the task of either detecting or identifying a target against typical background materials. In addition, such a system must be capable of capturing image frames with enough SNR to produce good imagery at video frame rates.

The differential power received by the imaging system’s receiver from the target and background is primarily governed by phenomenology. It is also affected by some of the imaging system characteristics/parameters such as the spectral bandwidth, the aperture size, and the instantaneous field of view (IFOV) of the imaging system. As such, realizing an adequate system SNR depends on achieving adequate system sensitivity (low noise-equivalent power [NEP]). To determine the required system sensitivity for capturing useful imagery at video rates, a radiometric formulation of the target and background powers received by the system’s detector element(s) is first described.

Using the radiometric transfer process developed by Murrill et al. (16), the power emitted from the target and background surfaces within the detector area (in object space) and within the receiver spectral bandwidth is first calculated, and then these powers are propagated through any target concealment/obscurant material and through the atmosphere to the receiver aperture a distance $R$ (meters) away (figure 8). The emitted powers are assumed to radiate in a Lambertian fashion ($Gain$ equal to 4).

![Figure 8. Illustration of the radiometric model for passive target/background thermal emission.](image-url)
Calculation of the power emitted from the target/background surface begins with the calculation of thermal exitance by integrating the spectral exitance (Planck’s radiation law \[17\]) over the spectral bandwidth of the system receiver and then multiplying by the emissivity of the surface. The thermal exitance (M) of the target or background surface is given by

\[
M_{\text{thermal}} = \int_{\lambda_C - \Delta\lambda / 2}^{\lambda_C + \Delta\lambda / 2} \left( \frac{2\pi \times h \times c^2}{\lambda^5 \times \left( \exp\left\{ h \times c / (\lambda \times k \times T) \right\} - 1 \right) \Delta\lambda} \right) d\lambda \quad \text{in} \ W/m^2, \tag{6}
\]

where \(h\) is Planck’s constant (J·s), \(c\) is the speed of light (m/s), \(\lambda\) is wavelength (m), \(k\) is Boltzmann’s constant (J/K), \(T\) is the surface temperature (K), \(\lambda_C\) is the center wavelength of the system receiver (m), and \(\Delta\lambda\) is the spectral bandwidth of the system receiver (m).

The power emitted from the target/background surface into the detector’s IFOV is calculated from

\[
P_{\text{emitted}} = M_{\text{thermal}} \times A_{\text{do}}(R) \times \varepsilon_{\text{surface}} \quad \text{in} \ W, \tag{7}
\]

where \(A_{\text{do}}(R)\), the detector area in object space, is as calculated in equation 8 and \(\varepsilon_{\text{surface}}\) is the emissivity of the surface.

The detector area, \(A_{\text{do}}(R)\), is the detector area in object space and is given by

\[
A_{\text{do}}(R) = \pi \left( \frac{\text{IFOV}}{2} \times R \right)^2 \quad \text{in} \ m^2, \tag{8}
\]

where \(\text{IFOV}\) is the detector’s IFOV.

The emitted power from the target and background surfaces is then propagated to the imaging system through any target concealment/obscurant material and through the atmosphere to the receiver aperture located a distance \(R\) away, and the receiver aperture irradiance is calculated. The irradiance at the receiver aperture is given by

\[
E_{\text{aperture}} = \frac{P_{\text{emitted}} \times \tau_{\text{air}} \times \tau_{\text{obs}} \times \text{Gain}}{4\pi R^2} \quad \text{in} \ W/m^2, \tag{9}
\]

where \(\text{Gain}\) is the reflective (emissive) gain from the target or background surface given by

\[
\text{Gain} = \frac{4\pi}{\Omega_{\text{refl}}}, \tag{10}
\]

and \(\Omega_{\text{refl}}\) is the solid angle of the reflected (emitted) beam in steradians. For Lambertian emission, \(\Omega_{\text{refl}}\) is \(\pi\) steradians, yielding a \(\text{Gain}\) equal to 4.

Finally, the power incident on the detector is calculated to be

\[
P_{\text{det,IFOV}} = E_{\text{aperture}} \times A_{\text{aperture}} \times \tau_{\text{aperture}} \times \eta_{\text{antenna}} \quad \text{in} \ W, \tag{11}
\]
where $A_{\text{aperture}}$ is the area of the aperture in $m^2$, $\tau_{\text{aperture}}$ is the transmission of the aperture, and $\eta_{\text{antenna}}$ is the coupling efficiency of the detector’s antenna.

Combining equations 6–10 into equation 11 yields

$$P_{\text{detIFOV}} = M_{\text{thermal}}(\lambda_c, \Delta\lambda, T) \times \epsilon_{\text{surface}} \times \frac{IFOV^2}{2} \times A_{\text{aperture}} \times \tau_{\text{atm}} \times \tau_{\text{obs}} \times \tau_{\text{aperture}} \times \eta_{\text{antenna}} \text{ in W. (12)}$$

Note that the power received by the system detector(s) is independent of range ($R$) (for ranges where the target is fully resolved). This is due to the fact that the surface area of the target or background that the system’s IFOV subtends increases by $R^2$ as range increases, while the power density (irradiance) that the system aperture receives decreases by $R^2$ as range increases.

The power received by the system detector(s) is a strong function of the frequency or wavelength of the EM radiation along with the spectral bandwidth. Figure 9 shows the spectral exitance ($M$) of a blackbody at a temperature of 300 K as a function of wavelength. Note that radiant power peaks at a wavelength of approximately 10 µm (IR regime) and is approximately 7 orders of magnitude lower at a wavelength of 1 mm (MMW regime). Figure 10 displays this same curve on a log-log scale.

Figure 9. Spectral exitance of a blackbody at a temperature of 300 K.
Figure 10. Spectral exitance of a blackbody at a temperature of 300 K plotted on a log-log scale.

The incremental temperature above a background temperature that produces a system SNR of unity is the system’s noise equivalent difference temperature (NEDT) (18). For this analysis, the difference between the power received by the system detector(s) from the target surface and the power received from the background surface (from the minimum target-to-background apparent temperature difference) is equated to the system’s electrical NEP such that the system SNR is unity, i.e.,

\[
SNR_{System} = \frac{|P_{Tgt}(W) - P_{Bkgd}(W)|}{NEP_{System}},
\]

where \(P_{Tgt}(W)\) is the power (in watts) received by the system detector(s) from the target surface (from equation 12), \(P_{Bkgd}(W)\) is the power (in watts) received by the system detector(s) from the background surface (from equation 12), and \(NEP_{System}\) is the NEP of the system (in watts).

The system NEP is a function of the noise equivalent bandwidth (NEBW) and is given by

\[
NEP_{System} = NEP^* \left( \frac{W}{\sqrt{Hz}} \right) \times \sqrt{NEBW \ (Hz)},
\]

where \(NEP^* \left( \frac{W}{\sqrt{Hz}} \right)\) is the fundamental system sensitivity expressed as watts per root Hz, and NEBW (Hz) is inversely related to the detector temporal integration time \(t_{det \_int}\) available for each image pixel per image frame (18, 19) by,

\[
NEBW \ (Hz) = \frac{1}{2t_{det \_int \ (s)}}.
\]
Substituting equation 13 into equation 14 yields

\[
NEP^* \left( \frac{W}{\sqrt{Hz}} \right) = \frac{|P_{Tg}(W) - P_{Bkgd}(W)|}{(SNR_{System} \times \sqrt{NEBW\ (Hz)})} \cdot (W \cdot Hz^{-1/2})
\]

(16)

where again \( P_{Tg}(W) \) is the power (in watts) received by the system detector(s) from the target surface (from equation 12), \( P_{Bkgd}(W) \) is the power (in watts) received by the system detector(s) from the background surface (from equation 12), and NEBW (Hz) is the noise equivalent bandwidth of the system.

Alternatively, substituting equation 15 into equation 16 yields

\[
NEP^* \left( \frac{W}{\sqrt{Hz}} \right) = \frac{|P_{Tg}(W) - P_{Bkgd}(W)|}{SNR_{System}} \times \sqrt{2t_{det \cdot int}(s)} \cdot (W \cdot Hz^{-1/2})
\]

(17)

The previous section provided minimum contrast temperature differences that an imaging system must be capable of capturing, with adequate SNR, for three important MMW and/or SMMW/THz imaging scenarios. Within each scenario, the worst-case contrast temperature differences were 2 and 6 K at 77 GHz, and approximately 6 K at 320 or 640 GHz.

From a top level, imaging systems designed to effectively image in these scenarios must be able to capture images with 2–6 K contrast temperature differences in the respective EM radiation frequency bands with adequate SNR (assume at least an SNR = 6) under the very crucial constraint of operating at video rates (approximately 30 Hz).

As can be seen from the above formulations, many factors go into determining the differential power levels actually captured by the system receiver element(s), which then, of course, drive the system noise floor or sensitivity requirement. To summarize, the primary factors are the following:

- the effective exitance (power) levels of the target and background contained within the spectral bandwidth of the system (includes target and background temperatures and emissivities),
- the minimum contrast temperature difference that must be resolved,
- the IFOV of the system,
- the size of the receiver aperture,
- the atmospheric attenuation at standoff range,
- the coupling efficiency of the receiver/antenna, and
- any concealment material attenuation.

Again, on the system receiver side of the equation (system noise), a crucial parameter is the amount of integration time available for each image pixel per image frame. The NEP* sensitivity
requirement of the system scales with the square root of the available integration time ($t_{\text{det_int}}$) —

System noise (watts) = $\text{NEP}^*$ (watts per root Hz)/square root of $2t_{\text{det_int}}$ (s). The less integration time available to the system, the higher the imaging system sensitivity requirement (lower numerical value).

All of the above factors have been incorporated into and accounted for in the U.S. Army Research Laboratory’s (ARL) Enhanced Terahertz/MMW Imaging System Performance Analysis and Design Tool for Concealed Weapon Identification (20). Present plans call for evaluating select passive MMW and SMMW/THz imaging systems using this modeling tool.

5. Discussion and Conclusions

Phenomenologically, the advantages of passive imaging in the MMW regime include the following:

- Low atmospheric attenuation and scattering
- Low attenuation due to atmospheric fog, smoke, dust, sand, and typical person-borne concealment materials.

Relative to passive imaging in the SMMW/THz regime, the primary disadvantage of passive imaging in the MMW regime is lower spatial resolution for a given imaging system aperture size. A secondary disadvantage is the relative dependence on sky illumination for larger target-to-background CRs.

Advantages of passive imaging in the SMMW/THz regime include the following:

- Increased spatial resolution for a given imaging system aperture size
- Slightly better target-to-background CRs with indoor scenarios (no sky illumination) due to higher thermal emissivities and spectral exitances.

Relative to passive imaging in the MMW regime, the primary disadvantages of passive imaging in the SMMW/THz regime include the following:

- Higher atmospheric attenuation and scattering
- Higher attenuation due to atmospheric fog, smoke, dust, sand, and typical person-borne concealment materials
- Possible degradation of image quality (lower SNCRs) due to clutter from spatial variations in atmospheric attenuation and spatial/temporal variations in concealment material attenuation due to material motion relative to the target/background.
Some knowledge gaps remain in the understanding/quantification of a few phenomenological aspects of passive imaging in the MMW and SMMW/THz regimes. For the most part, these knowledge gaps fall into the category of clutter and include the following:

- A better understanding of the impact of variations in both sky and fog illumination on an observer’s ability to perform the task of detecting or identifying a slightly cluttered target within a slightly cluttered background.
- A better, more quantitative understanding of the impact of spatial variations of atmospheric attenuation on an observer’s ability to perform the task of detecting or identifying a slightly cluttered target within a slightly cluttered background.
- A better, more quantitative understanding of the impact of variations in concealment material attenuation due to material motion relative to the target/background on an observer’s ability to perform the task of detecting or identifying a slightly cluttered target within a slightly cluttered background.

Based on the MMW and SMMW/THz radiometric data cited in the imaging scenarios of section 3, along with an assumption that a reasonable SNR of 6 (approximately 8 dB) is required for good imagery, it is concluded that the following minimum imaging system receiver sensitivities are required for the successful discrimination of all targets of interest within their respective backgrounds:

- In-flight obstacle avoidance: \( 2 \text{ K/6} = \text{approximately} \ 0.3 \text{ K} \)
- Landing/takeoff obstacle avoidance: \( 6 \text{ K/6} = \text{approximately} \ 1.0 \text{ K} \)
- Concealed weapon detection/identification: \( 6.2 \text{ K/6} = \text{approximately} \ 1.0 \text{ K} \).

The extremely important constraint that goes along with these sensitivity levels is the requirement for the passive MMW and/or SMMW/THz system to meet these specifications using real-time, video frame rates.

If, for example, a passive MMW or SMMW/THz imaging system uses a scanning, line-array receiver architecture, then the receiver sensitivity requirement — \( \text{NEP}^* \) (watts per root Hz) — will nominally increase relative to a system using a FPA by the square-root of the number of rows or columns that are scanned to form a complete image. (This assumes a zero-time budget for the scanning process itself.) If a passive MMW or SMMW/THz imaging system uses a single-pixel, scanning receiver architecture, then the receiver sensitivity requirement — \( \text{NEP}^* \) (watts per root Hz) — will nominally increase relative to a system using a FPA by the square-root of the number of pixels that are scanned to form a complete image. (Again, this assumes a zero-time budget for the scanning process.)

Mathematical formulations of the required passive imaging system receiver sensitivity requirement — \( \text{NEP}^* \) (watts per root Hz) — to provide image frames with enough SNR to
produce good imagery at video frame rates have been derived (equations 16 and 17). The equations show that the required system sensitivity is a function of the following variables:

- the spectral bandwidth of the imaging system,
- the minimum temperature difference between the target and the background,
- the emissivities of the target and background,
- the IFOV of the system detector(s),
- the area of the system entrance aperture,
- atmospheric transmission (attenuation),
- aperture transmission,
- obscurant transmission (attenuation),
- antenna coupling efficiency,
- the desired system SNR, and
- the available detector integration time per pixel per frame.

Future work will include identifying and subsequent performance modeling of selected commercial-off-the-shelf (COTS) and/or Government off-the-shelf (GOTS) MMW and/or SMMW/THz passive imaging systems. These systems will be analyzed using ARL’s Enhanced Terahertz Imaging System Performance Analysis and Design Tool for Concealed Weapon Identification (20).
6. References


### List of Symbols, Abbreviations, and Acronyms

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<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tr>
<td>ARL</td>
<td>U.S. Army Research Laboratory</td>
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<td>CRs</td>
<td>contrast ratios</td>
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<td>CW</td>
<td>continuous-wave</td>
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<td>DVEs</td>
<td>degraded visual environments</td>
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<td>EM</td>
<td>electromagnetic</td>
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<tr>
<td>FPA</td>
<td>focal-plane-array</td>
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<tr>
<td>IFOV</td>
<td>instantaneous field-of-view</td>
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<td>IR</td>
<td>infrared</td>
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<tr>
<td>MMW</td>
<td>millimeter-wave</td>
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<tr>
<td>NEDT</td>
<td>noise equivalent difference temperature</td>
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<tr>
<td>NEP</td>
<td>noise-equivalent power</td>
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<td>RSS</td>
<td>root-sum-squared</td>
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<td>SCRs</td>
<td>signal (target)-to-clutter ratios</td>
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<tr>
<td>SMMW</td>
<td>submillimeter-wave</td>
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