Analogy just looks like high level perception:
Why a domain-general approach to analogical mapping is right

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Abstract

Hofstadter and his colleagues have criticized current accounts of analogy, claiming that such accounts do not accurately capture interactions between processes of representation construction and processes of mapping. They suggest instead that analogy should be viewed as a form of *high level perception* that encompasses both representation building and mapping as indivisible operations within a single model. They argue specifically against SME, our model of analogical matching, on the grounds that it is modular, and offer instead programs like Mitchell & Hofstader’s Copycat as examples of the high level perception approach. In this paper we argue against this position on two grounds. First, we demonstrate that most of their specific arguments involving SME and Copycat are incorrect. Second, we argue that the claim that analogy is high-level perception, while in some ways an attractive metaphor, is too vague to be useful as a technical proposal. We focus on five issues: (1) how perception relates to analogy, (2) how flexibility arises in analogical processing, (3) whether analogy is a domain-general process, (4) how should micro-worlds be used in the study of analogy, and (5) how best to assess the psychological plausibility of a model of analogy. We illustrate our discussion with examples taken from computer models embodying both views.

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1. Introduction

The field of analogy is widely viewed as a cognitive science success story. In few other research domains has the connection between computational and psychological work been as close and as fruitful as in this one. This collaboration, along with significant influences from philosophy, linguistics and history of science, has led to a substantial degree of theoretical and empirical convergence among researchers in the field (e.g., Falkenhainer, Forbus & Gentner, 1989; Halford, 1993; Holyoak & Thagard, 1989; Keane, Ledgeway & Duff, 1994). There has been progress both in accounting for the basic phenomena of analogy and in extending analogy theory to related areas, such as metaphor and mundane similarity, and to more distant areas such as categorization and decision making (See Gentner and Holyoak, in press; Gentner & Markman, in press; Holyoak & Thagard, 1995, in press). Though there are still many debated issues, there is a fair degree of consensus on certain fundamental theoretical assumptions. These include the usefulness of decomposing analogical processing into constituent subprocesses such as retrieving representations of the analogs, mapping (aligning the representations and projecting inferences from one to the other), abstracting the common system, and so on; and that the mapping process is a domain-general process that is the core defining phenomenon of analogy (Gentner, 1989).

Hofstadter and his colleagues express a dissenting view. They argue for an approach to analogy as “high-level perception” (Chalmers, French, & Hofstadter, 1992; French, 1995; Hofstadter, 1995a; Mitchell, 1993) and are sharply critical of the structure-mapping research program and related approaches. Indeed, Hofstadter (1995a, pp. 155-165) even castigates Waldrop (1987) and Boden (1991) for praising models such as SME and ACME. This paper is a response to these criticisms.

Hofstadter and his colleagues argue against most current approaches to modeling analogical reasoning. One of their major disagreements is with the assumption that mapping between two analogs can be separated from the process of initially perceiving both analogs. As Chalmers, French, & Hofstadter (1992) (henceforth, CFH) put it: “We argue that perceptual processes cannot be separated from other cognitive processes even in principle, and therefore that traditional artificial-intelligence models cannot be defended by supposing the existence of a 'representation module' that supplies representations ready-made.” (CFH, p. 185)

Hofstadter (1995a, p. 284-285) is even more critical: “SME is an algorithmic but psychologically implausible way of finding what the structure-mapping theory would consider to be the best mapping between two given representations, and of rating various mappings according to the structure-mapping theory, allowing such ratings then to be compared with those given by people.” Hofstadter (1995b, p. 78) further charges analogy researchers with “trying to develop a theory of analogy making while bypassing both gist extraction and the nature of concepts…” an approach “as utterly misguided as trying to develop a theory of musical esthetics while omitting all mention of both melody and harmony.” Writing of Holyoak and Thagard’s approach to analogy, he states that it is “to hand shrink each real-world situation into a tiny, frozen caricature of itself, containing precisely its core and little else.”

Hofstadter and colleagues are particularly critical of the assumption that analogical mapping can operate over pre-derived representations and of the associated practice of testing the simulations using
representations designed to capture what are believed to be human construals. “We believe that the use of hand-coded, rigid representations will in the long run prove to be a dead end, and that flexible, content-dependent, easily adaptable representations will be recognized as an essential part of any accurate model of cognition.” (CFH, p. 201) Rather, they propose the metaphor of “high level perception” in which perception is holistically integrated with higher forms of cognition. They cite Mitchell & Hofstader’s Copycat model (Mitchell, 1993) as a model of high-level perception. CFH claim that the flexibility of human cognition cannot be explained by any more modular account.

We disagree with many of the theoretical and empirical points made by Hofstadter and his colleagues. In this paper we present evidence that the structure-mapping algorithm embodied in SME approach can capture significant aspects of the psychological processing of analogy. We consider and reply to the criticisms made against SME and correct some of Hofstadter’s (1995a) and CFH’s claims that are simply untrue as matters of fact. We begin in Section 2 by summarizing CFH’s notion of high level perception and outlining general agreements and disagreements. Section 3 describes the simulations of analogical processing involved in the specific arguments: SME (and systems that use it) and Copycat. This section both clears up some of the specific claims CFH make regarding both systems, and provides the background needed for the discussion in Section 4. There we outline five key issues in analogical processing, and compare our approach with CFH with regard to them. Section 5 summarizes the discussion.

2. CFH’s notion of high level perception

CFH observe that human cognition is extraordinarily flexible, far more so than is allowed for in today’s cognitive simulations. They postulate that this flexibility arises because, contrary to most models of human cognition, there is no separation between the process of creating representations from perceptual information and the use of these representations. That is, for CFH there is no principled decomposition of cognitive processes into “perceptual processes” and “cognitive processes.” While conceding that it may be possible informally to identify aspects of our cognition as either perception or cognition, CFH claim that building a computational model that separates the two cannot succeed. Specifically, they identify analogy with “high-level perception”, and argue that this holistic notion cannot productively be decomposed.

One implication of this view is that cognitive simulations of analogical processing must always involve a “vertical” slice of cognition (see Morrison and Dietrich (1995) for a similar discussion). That is, a simulation must automatically construct its internal representations from some other kind of input, rather than being provided them directly by the experimenters. In Copycat, for instance, much of the information used to create a match in a specific problem is automatically generated by rules operating over a fairly sparse initial representation. CFH point out that Copycat’s eventual representation of a particular letter-string is a function of not just the structure of the letter string itself, but also on the other letter strings it is being matched against.

2.1 Overall points of agreement and disagreement.

CFH’s view of analogy as high-level perception has its attractive features. For instance, it aptly captures a common intuition that analogy is “seeing as”. For example, when Rutherford thought of modeling the
atom as if it were the solar system, he might be said to have been “perceiving” the atom as a solar system. It further highlights the fact that analogical processing often occurs outside of purely verbal situations. Yet while we find this view in some respects an attractive metaphor, we are less enthusiastic about its merits as a technical proposal, especially the claim of the inseparability of the processes.

We agree with CFH that understanding how analogical processing interacts with perception and other processes of building representations is important. We disagree that such interactions necessitate a holistic account. Figure 1 illustrates three extremely coarse-grained views of how perception and cognition interact. Part (a) depicts a classic stage model, in which separate processes occur in sequence. This is the straw man that CFH argue against. Part (b) depicts CFH’s account. The internal structure either is not identifiable in principle (the literal reading of CFH’s claims) or the parts interact so strongly that they cannot be studied in isolation (how CFH actually conduct their research). Part (c) depicts what we suggest is a more plausible account. The processes that build representations are interleaved with the processes that use them. On this view, there is value in studying the processes in isolation, as well as in identifying their connections with the rest of the system. We will return to this point in Section 3.

3. A comparison of some analogical processing simulations

Hofstadter’s claims concerning how to simulate analogical processing can best be evaluated in the context of the models. We now turn to the specific simulations under discussion, SME and Copycat.

3.1 Simulations using structure-mapping theory

Gentner’s (1983; 1989) structure-mapping theory of analogy and similarity decomposes analogy and similarity processing into several processes (not all of which occur for every instance of comparison), including representation, access, mapping (alignment and inference), evaluation, adaptation, verification and schema-abstraction. For instance, the mapping process operates on two input representations, a base and a target. It results in one or a few mappings, or interpretations, each consisting of a set of correspondences between items in the representations and a set of candidate inferences, which are
surmises about the target made on the basis of the base representation plus the correspondences. The set of constraints on correspondences include structural consistency, i.e., that each item in the base maps to at most one item in the target and vice-versa (the 1:1 constraint) and that if a correspondence between two statements is included in an interpretation, then so must correspondences between its arguments (the parallel connectivity constraint). Which interpretation is chosen is governed by the systematicity constraint: Preference is given to interpretations that match systems of relations in the base and target.

Structure-mapping theory incorporates computational level or information-level assumptions about analogical processing, in the sense discussed by Marr (1982). Each of the theoretical constraints is motivated by the role analogy plays in cognitive processing. The 1:1 and parallel connectivity constraints ensure that the candidate inferences of an interpretation are well-defined. The systematicity constraint reflects a (tacit) preference for inferential power in analogical arguments. Structure-mapping theory provides an account of analogy that is independent of any specific computer implementation. It has broad application to a variety of cognitive tasks involving analogy, as well as to tasks involving ordinary similarity comparisons, including perceptual similarity comparisons (c.f. Gentner & Markman, in press; Medin, Goldstone, & Gentner, 1993).

In addition to mapping, structure-mapping theory makes claims concerning other processes involved in analogical processing, including retrieval and learning. The relationships between these processes are often surprisingly subtle. Retrieval, for instance, appears to be governed by overall similarity, because this is an ecologically sound strategy for organisms in a world where things that look alike tend to act alike. On the other hand, in learning conceptual material a high premium is placed on structural consistency and systematicity, since relational overlap provides a better estimate of validity for analogical inferences than the existence of otherwise disconnected correspondences.

As Marr pointed out, eventually a full model of a cognitive process should extend to the algorithm and mechanism levels of description as well. We now describe systems that use structure-mapping theory to model cognitive processes, beginning with SME.

### 3.2.1 SME

SME takes as input two descriptions, each consisting of a set of propositions. The only assumption we make about statements in these descriptions is that (a) each statement must have an identifiable predicate and (b) there is some means of identifying the roles particular arguments play in a statement. Predicates can be relations, attributes, functions, logical connectives, or modal operators. Representations that have been used with SME include descriptions of stories, fables, plays, qualitative and quantitative descriptions of physical phenomena, mathematical equations, geometric descriptions, visual descriptions, and problem-solutions.

Representation is a crucial issue in our theory, for our assumption is that the results of a comparison process depend crucially on the representations used. We further assume that human perceptual and

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1Attributes are unary predicates representing properties of their argument which in the current description are not further decomposed. Examples include $\text{Red(ball32)}$ and $\text{Heavy(sun)}$
memorial representations are typically far richer than required for any one task\(^2\). Thus we do not assume that the representations given to SME contain all logically possible (or even relevant) information about a situation. Rather, the input descriptions are intended as particular psychological construals -- collections of knowledge that someone might bring to bear on a topic in a particular context. The content and form of representations can vary across individuals and contexts. Thus, the color of a red ball may be encoded as color(ball) = red on some occasions, and as red(ball) on others. Each of these construals has different implications about the way this situation will be processed (see Gentner, Rattermann, Markman, & Kotovsky, 1995, for a more detailed treatment of this issue).

This issue of the size of the construals is important. CFH (p. 200) argue that the mapping processes used in SME “all use very small representations that have the relevant information selected and ready for immediate use.” The issues of the richness and psychological adequacy of the representations, and of the degree to which they are (consciously or unconsciously) pre-tailored to create the desired mapping results, are important issues. But although we agree that more complex representations should be explored than those typically used by ourselves and other researchers -- including Hofstadter and his colleagues -- we also note three points relevant to this criticism: (1) SME’s representations typically contain irrelevant as well as relevant information, and misleading as well as appropriate matches, so that the winning interpretation is selected from a much larger set of potential matches; (2) in some cases, as described below, SME has been used with very large representations, certainly as compared with Copycat’s; and (3) on the issue of hand-coding, SME has been used with representations built by other systems for independent purposes. In some experiments the base and target descriptions to SME are written by human experimenters. In other experiments and simulations (e.g., PHINEAS, MAGI, MARS) many of the representations are computed by other programs. SME’s operation on these descriptions is the same in either case.

Given the base and target descriptions, SME finds globally consistent interpretations via a local-to-global match process. SME begins by proposing correspondences, called match hypotheses, in parallel between statements in the base and target. Not every pair of statements can match; structure-mapping theory postulates the tiered identicality constraint to describe when statements may be aligned. Initially, two statements can be aligned if either (a) their predicates are identical or (b) their predicates are functions, and aligning them would allow a larger relational structure to match. Then, SME filters out match hypotheses which are structurally inconsistent, using the 1:1 and parallel connectivity constraints of structure-mapping theory described in the previous section. Depending on context (including the system’s current goals, c.f. Falkenhainer 1990b), more powerful re-representation techniques may be applied to see if two statements can be aligned in order to achieve a larger match (or a match with potentially relevant candidate inferences).

\(^2\) See for example the discussion of the specificity conjecture in Forbus & Gentner (1989).
Mutually consistent collections of match hypotheses are gathered into a small number of global interpretations of the comparison called *mappings*[^3] or *interpretations*. For each interpretation, *candidate inferences* about the target -- that is, statements about the base that are connected to the interpretation but are not yet present in the target -- are imported into the target. An evaluation procedure based on Gentner's (1983) systematicity principle is used to compute an evaluation for each interpretation, leading to a preference for deep connected common systems (Forbus & Gentner, 1989).

The SME algorithm is very efficient. Even on serial machines, the operations involved in building networks of match hypotheses and filtering can be carried out in polynomial time, and the greedy merge algorithm used for constructing interpretations is linear in the worst case, and generally fares far better empirically. How does SME do at capturing significant aspects of analogical processing? It models the local-to-global nature of the alignment process (see Goldstone and Medin (1994) for psychological evidence). Its evaluations ordinally match human soundness judgments. It models the drawing of inferences, an important form of analogical learning. However, the real power of modeling analogical mapping as a separable process can best be seen in the larger simulations that use SME as a component. One of the first of these, and the one that best shows the use of analogy in building representations, is Falkenhainer’s Phineas.

### 3.2.2 Phineas: A simulation of analogical learning in physical domains.

Phineas (Falkenhainer, 1987, 1988, 1990a) learns physical theories by analogy with previously understood examples. Its design exploits several modules which have themselves been used in other projects, including SME, QPE (Forbus, 1990), an implementation of Qualitative Process theory (Forbus, 1984), and DATMI (Decoste, 1990),[^4] a measurement interpretation system. The architecture of Phineas is illustrated in Figure 2.

[^3]: Using a greedy merge algorithm, as described in Forbus & Oblinger (1990), and extended in Forbus, Ferguson, & Gentner (1994). Hofstadter (1995a) appears unaware of the use of this algorithm, “…certainly, the exhaustive search SME performs through all consistent mappings is psychologically implausible.” (p. 283).

[^4]: Another system, TPLAN (Hogge, 1987), a temporal planner, was used in some Phineas simulations for designing experiments.
In Phineas, SME was used as a module in a system that learns qualitative models of physical phenomena via analogy. Phineas' map/analyze cycle is a good example of how SME can be used in systems that interleave representation construction with other operations.

Figure 2: The architecture of Phineas.
The best way to illustrate how Phineas works is by example. Phineas starts with the description of the behavior of a physical system, described in qualitative terms. In one example, Phineas is given the description of the temperature changes that occur when a hot brick is immersed in cold water. Phineas first attempts to understand the described behavior in terms of its current physical theories, by using QPE to apply these theories to the new situation and qualitatively simulate the kinds of behaviors which can occur, and using DATMI to construct explanations of the observations in terms of the simulated possibilities. In this case, Phineas did not have a model of heat or heat flow, so it could not find any physical processes to explain the observed changes. In such circumstances Phineas turns to analogy to seek an explanation.

To derive an explanation, Phineas attempts to find an analogous behavior in its database of previously-explained examples. These examples are indexed in an abstraction hierarchy by their observed behaviors. Based on global properties of the new instance’s behavior, Phineas selects a potentially analogous example from this hierarchy. When evaluating a potential analog, Phineas uses SME to compare the behaviors, which generates a set of correspondences between different physical aspects of the situations. These correspondences are then used with SME to analogically infer an explanation for the new situation, based on the explanation for the previously understood situation. Returning to our immersed brick example, the most promising candidate explanation is a situation where liquid flow causes two pressures to equilibrate. To adapt this explanation for the original behavior Phineas creates a new process, \texttt{PROCESS-1} (which we'll call heat-flow for simplicity after this), which is analogous to the liquid flow process, using the correspondences between aspects of the two behaviors. In this new physical process, the relationships that held for pressure in the liquid flow situation are hypothesized to hold for the corresponding temperature parameters in the new situation.

Generating the initial physical process hypothesis via analogical inference is only the first step. Next Phineas must ensure that the hypothesis is specified in enough detail to actually reason with it. For instance, in this case it is not obvious what the analog to liquid is, nor what constitutes a flow path, in the new heat flow situation. It resolves these questions by a combination of reasoning with background knowledge about the physical world (e.g., that fluid paths are a form of connection, and that immersion in a liquid implies that the immersed object is in contact with the liquid) and by additional analogies. Falkenhainer calls this the \textit{map/analyze cycle}. Candidate inferences are examined to see if they can be justified in terms of background knowledge, which may in turn lead to further matching to see if the newly applied background knowledge can be used to extend the analogy further. Eventually, Phineas extends its candidate theory into a form which can be tested, and proceeds to do so by using the combination of QPE and DATMI to see if the newly-extended theory can explain the original observation.

We believe that Phineas provides a model for the use of analogy in learning, and indeed for the role of analogy in abduction tasks more generally. The least psychologically plausible part of Phineas' operation

\[\text{Examples of behavioral classifications include dual-approach (e.g., two parameters approaching each other) and cyclic (e.g., parameters that cycle through a set of values). The abstraction hierarchy is a plausible model of expert memory, but we believe our more recent MAC/FAC model would provide a more psychologically plausible model for most situations.}\]
is the retrieval component, in which a domain-specific indexing vocabulary is used to filter candidate experiences (although it might be a reasonable model of expert retrieval). On the other hand, Phineas' map/analyze cycle and its method of using analogy in explanation and learning are, we believe, plausible in their broad features as a psychological model.

The omission of Phineas from CFH's discussion of analogy (and from Hofstadter’s (1995a) discussions) is striking, since it provides strong evidence against their position. Phineas performs a significant learning task, bringing to bear substantial amounts of domain knowledge in the process. Phineas can extend its knowledge of the physical world, deriving new explanations by analogy, which can be applied beyond the current situation. Phineas provides a solid refutation of the CFH claim that systems that interleave a general mapping engine with other independently-developed modules cannot be used to flexibly construct their own representations.

3.2.3 Other simulations using SME

SME has been used in a variety of other cognitive simulations. These include

- **SEQL**: A simulation of abstraction processes in concept learning (Skorstad, Gentner, & Medin, 1988). Here SME was used to explore whether abstraction-based or exemplar-based accounts best accounted for sequence effects in concept learning. The input stimuli were representations of geometric figures.

- **MAC/FAC**: A simulation of similarity-based retrieval (Gentner & Forbus, 1991; Law, Forbus, & Gentner, 1994; Forbus, Gentner, & Law, 1995). In MAC/FAC, SME is used in the second stage of retrieval to model the human preference for structural remindings. The first stage is a simpler matcher whose output estimates what SME will produce on two structured representations and can be implemented in first-generation connectionist hardware in parallel, and thus has the potential to scale to human-sized memories. MAC/FAC has been tested with simple metaphors, stories, fables, Shakespeare plays\(^7\), and descriptions of physical phenomena.

- **MAGI**: A simulation of symmetry detection (Ferguson, 1994). MAGI uses SME to map a representation against itself, to uncover symmetries and regularities within a representation. MAGI has been tested with examples from the visual perception literature, conceptual materials,\(^8\) and combined perceptual/functional representations (i.e., diagrams and functional descriptions of digital logic circuits).

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\(^6\)In this connection, we must correct an inaccuracy. In Hofstadter’s (1995) reprint of CFH (1992), a disclaimer is added on page 185: “Since this article was written, Ken Forbus, one of the authors of SME, has worked on modules that build representations in “qualitative physics.” Some work has also been done on using these representations as input to SME.” But the use of these representations, and Phineas, was discussed in the Falkenhainer, Forbus, & Gentner (1989) paper cited by CFH.

\(^7\)The representations of fables and plays were supplied to us by Paul Thagard.

\(^8\)This includes its namesake example, a representation of O. Henry's "The Gift of the Magi."
• **MARS**: A simulation of analogical problem solving (Forbus, Ferguson, & Gentner, 1994). MARS uses SME to import equations from a previously-worked thermodynamics problem\(^9\) to help it solve new problems. MARS is the first in a series of systems we are building to model the range of expert and novice behaviors in problem solving and learning.

The last two systems use a new version of SME, ISME (Forbus, Ferguson, & Gentner, 1994), which allows incremental extension of the descriptions used as base and target (see Burstein (1988) and Keane (1990)).\(^{10}\) This process greatly extends SME’s representation-building capabilities.

### 3.3 Psychological research using SME

SME has been used to simulate and predict the results of psychological experiments on analogical processing. For example, we have used SME to model the developmental shift from focusing on object matches to focusing on relational matches in analogical processing. The results of this simulation indicate that it is at possible to explain this shift in terms of change of knowledge rather than as a change in the basic mapping process itself (Kotovsky & Gentner, 1990, in press). Another issue is that of competing mappings, as noted above. SME’s operation suggests that when two attractive mappings are possible, the competition among mappings may lead to confusion. This effect has been shown for children (Rattermann & Gentner, 1990; Gentner, Rattermann, Markman, & Kotovsky, 1995) and to some extent for adults (Markman & Gentner, 1993a). A third issue is that SME’s structural alignment process for similarity has led to the possibility of a new understanding of dissimilarity, based on alignable differences between representations (Gentner & Markman, 1994; Markman & Gentner, 1993b, 1996). In all these cases, SME has been used to verify the representational and processing assumptions underlying the psychological results. These studies suggest many different ways in which analogy may interact with other reasoning processes, including, but not limited to, representation construction.

### 3.4 Copycat: A model of high-level perception

Copycat operates in a domain of alphabetic strings (see CFH, Mitchell, 1993, and Hofstadter, 1995a, for descriptions of Copycat, and French, 1995 and Hofstadter, 1995a, for descriptions of related programs in different domains.). It takes as input problems of the form “If the string abc is transformed into abd, what is the string aabbcc transformed into?” From this input and its built-in rules, Copycat derives a representation of the strings, finds a rule that links the first two strings, and applies that rule to the third string to produce an answer (such as aabbdd). Copycat's architecture is a blackboard system (c.f.,

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\(^9\) Representations for the previously-worked problems are automatically generated by CyclePad (Forbus & Whalley, 1994), an intelligent learning environment designed to help students learn engineering thermodynamics. CyclePad is currently being used in education experiments by students at Northwestern, Oxford, and the US Naval Academy.

\(^{10}\) MAGI and MARS appeared after the CFH paper, so while they constitute evidence for the utility of modular accounts of analogy, we cannot fault CFH for not citing them (although this does not apply to SEQL, MAC/FAC, and Phineas). However, many of the main claims in the paper by CFH are repeated in later books by French (1995) and by Hofstadter (1995a) despite the availability of counterevidence.
Engelmore & Morgan, 1988; Erman, Hayes-Roth, Lesser, & Reddy, 1980), with domain-specific rules\textsuperscript{11} that perform three tasks: (1) adding to the initial representation, by detecting groups and sequences, (2) suggesting correspondences between different aspects of the representations, and (3) proposing transformation rules to serve as solutions to the problem, based on the outputs of the other rules. As with other blackboard architectures, Copycat's rules operate (conceptually) in parallel, and probabilistic information is used to control which rules are allowed to fire. Each of these functions is carried out within the same architecture by the same mechanism and their operation is “inseparable.”

Concepts in this domain consist of letters, e.g., a, b, and c; groups, e.g., aa, bb and cc; and relationships involving ordering -- e.g., successor, as in b is the successor of a. A property that both Mitchell and CFH emphasize is that mappings in Copycat can occur between non-identical relationships. Consider for example two strings, abc versus cba. Copycat can recognize that the first group is a sequence of successors, while the second is a sequence of predecessors. When matching these two strings, Copycat would allow the concepts successor and predecessor to match, or, in their terminology, to “slip” into each other. Copycat has a pre-determined list of concepts that are allowed to match, called the Slipnet. In Copycat, all possible similarities between concepts are determined a priori. The likelihood that a concept will slip in any particular situation is also governed by a parameter called conceptual depth. Deep concepts are less likely to slip than shallow ones. The conceptual depth for each concept is, like the links in the Slipnet, hand-selected a priori by the designers of the system.

The control strategy used in Copycat's blackboard is a form of simulated annealing. The likelihood that concepts will slip into one another is influenced by a global parameter called computational temperature, which is initially high but is gradually reduced, creating a gradual settling. This use of temperature differs from simulated annealing in that the current temperature is in part a function of the system’s happiness with the current solution. Reaching an impasse may cause the temperature to be reset to a high value, activating rules that remove parts of the old representation and thus allow new representations to be built.

4. Dimensions of Analogy

We see five issues as central to the evaluation of CFH's claims with regard to analogical processing:

1. How does perception relate to analogy?
2. How does flexibility arise in analogical processing?
3. Is analogy a domain-general process?
4. How should microworlds be used in the study of analogy?
5. How should the psychological plausibility of a model of analogy be assessed?

\textsuperscript{11}These rules are called “codelets” in papers describing Copycat.
This section examines these questions, based both on the comparison of SME, Phineas, and Copycat above, as well as drawing on the broader computational and psychological literature on analogy.

4.1 How does perception relate to analogy?

CFH argue that, because perception and comparison interact and are mutually dependent, they are inseparable and cannot be productively studied in isolation. But as discussed in Section 2.1, dependencies can arise through interleaving of processes; they need not imply “in principle” nonseparability. (After all, the respiratory system and the circulatory system are highly mutually dependent, yet studying them as separate but interacting systems has proven extremely useful.) Contrary to CFH’s claims, even Copycat can be analyzed in terms of modules that build representations and other modules that compare representations. Mitchell (1993) provides just such an analysis, cleanly separating those aspects of Copycat that create new representations from those responsible for comparing representations, and showing how these parts interact.

Hofstadter’s call for more perception in analogical modeling might lead one to think that he intends to deal with real-world recognition problems. But the high-level perception notion embodied in Copycat is quite abstract. The program does not take as input a visual image, nor line segments, nor even a geometric representation of letters. Rather, like most computational models of analogy, it takes propositional descriptions of the input, which in the case of Copycat consists of three strings of characters: e.g., \(abc \rightarrow abd; \ rst \rightarrow \ ?\). Copycat’s domain of operation places additional limits on the length and content of the letter strings. The perception embodied in Copycat consists of taking this initial sparse propositional description and executing rules that install additional assertions about sequence properties of the English language alphabet. This procedure is clearly a form of representation generation, but (as CFH note) falls far short of the complexity of perception.

So far we have considered what the high-level perception approach bundles in with analogical mapping. Let us now consider two things it leaves out. The first is retrieval of analogs from memory. Since Copycat’s mapping process is inextricably mixed with its (high-level) perceptual representation-building processes, there is no way to model being reminded and pulling a representation from memory. Yet work on case-based reasoning in artificial intelligence (e.g., Schank, 1982, Hammond, 1990; Kolodner, 1994) and in psychology (e.g., Gentner, Rattermann & Forbus, 1993; Holyoak & Koh, 1987; Kahneman & Miller, 1986; Ross, 1987) suggests that previous examples play a central role in the representation and understanding of new situations and in the solution of new problems. To capture the power of analogy in thought, a theory of analogical processing must go beyond analogies between situations that are perceptually present. It must address how people make analogies between a current situation and stored representations of past situations, or even between two prior situations.

Investigations of analogical retrieval have produced surprising and illuminating results. It has become clear that the kinds of similarity that govern memory access are quite different from the kinds that govern mapping once two cases are present. The pattern of results suggests the fascinating generalization that similarity-based memory access is a stupider, more surface driven, less structurally sensitive process than analogical mapping (Gentner, Rattermann & Forbus, 1993; Holyoak & Koh, 1987; Keane, 1988). In our research we explicitly model the analogical reminding process by adding retrieval processes to SME in a system called MAC/FAC (Many Are Called/ but Few Are Chosen) (Forbus, Gentner & Law, 1995).
Thagard, Holyoak, Nelson, & Gochfeld’s (1990) ARCS model represents the corresponding extension to ACME. Thus by decomposing analogical processing into modules, we gain the ability to create accounts which capture both perceptual and conceptual phenomena.

The second omission is learning. Copycat has no way to store an analogical inference, nor to derive an abstract schema that represents the common system (in SME’s terms, the interpretation of the analogy, or mapping). For those interested in capturing analogy’s central role in learning, such a modeling decision is infelicitous to say the least, although Hofstadter’s approach can be defended as a complementary take on the uses of analogy. A central goal in our research with SME is to capture long-term learning via analogy. We have proposed three specific mechanisms by which domain representations are changed as a result of carrying out an analogy: schema abstraction, inference projection, and re-representation (Gentner et al, in press). The fluid and incremental view of representation embodied in Copycat cannot capture analogy’s role in learning.

The holistic view of processing taken by Hofstadter’s group obscures the multiplicity of processes that must be modeled to capture analogy in action. This can lead to misunderstandings. In their description of SME, CFH state [p196] that “...the SME program is said to discover an analogy between an atom and the solar system.” We do not know who “said” this, but it certainly was not said by us. By our account, discovering an analogy requires spontaneously retrieving one of the analogs as well as carrying out the mapping. But this attack is instructive, for it underscores Hofstadter’s failure to take seriously the distinction between a model of analogical mapping and a model of the full discovery process.

12 A similar comment occurs in Hofstadter’s (1995) discussion of the “Socrates is the midwife of ideas” analogy analyzed by Kittay (1987) as simulated in Holyoak & Thagard’s ACME: ”At this point, the tiny, inert predicate calculus cores are conflated with the original full-blown situations, subtly leading many intelligent people to such happy conclusions as that the program has insightfully leaped to a cross-domain analogy…” Here too, the simulation was presented only as a model of mapping, not the full process of discovery.
It is worth considering how Falkenhainer’s map/analyze cycle (described in Section 3.2.2) could be applied to perceptual tasks. An initial representation of a situation would be constructed, using bottom-up operations on, say, an image. (There is evidence for bottom-up as well as top-down processes in visual perception: e.g. Marr (1982), Kosslyn (1994)). Comparing two objects based on the bottom-up input descriptions leads to the formation of an initial set of correspondences. The candidate inferences drawn from this initial mapping would then provide questions that can be used to drive visual search and the further elaboration of the initial representations. The newly-added information in turn would lead to additional comparisons, continuing the cycle.

Consider the two comparisons in Figure 3 (drawn from Medin, Goldstone, and Gentner (1993)) as an example. In the comparison between A and B in Figure 3, people who were asked to list the commonalties of these figures said that both have 3 prongs. In contrast, people who listed the commonalties of the comparison B and C in Figure 3 said that both items have 4 prongs. Thus, the same item was interpreted as having either 3 or 4 prongs depending on the object it was compared with. The initial visual processing of the scene would derive information about the contours of the figures, but the detection of the regularities in the portions of the contours that comprise the “hands” would be conservative, identifying them as bumps, but nothing more. When compared with the three-pronged creature, the hypothesis that the creature with the fourth bump has only three prongs might lead to the clustering of the three bumps of roughly the same size as prongs. When compared with the four-pronged creature, the hypothesis that the creature has four prongs might lead to the dismissal of the size difference as irrelevant. The map-and-analyze cycle allows representation and mapping to interact while maintaining some separation. Recently Ferguson has simulated this kind of processing for reference frame detection with MAGI (Ferguson, 1994). This example suggests that perceptual processing can, in principle, be decomposed into modular subtasks. A major advantage of decomposition is identifying what aspects of a task are general-purpose modules, shared across many tasks. The conjectured ability of candidate

Figure 3: An example of how comparison can be used to reduce visual ambiguity
inferences to make suggestions that can drive visual search is, we believe, a fruitful avenue for future investigation.

4.2 How does flexibility arise in analogical processing?

A primary motivation for Hofstadter’s casting of analogy as high level perception is to capture the creativity and flexibility of human cognition. CFH suggest that this flexibility entails cognitive processes in which “representations can gradually be built up as the various pressures evoked by a given context manifest themselves (p. 201).” This is clearly an important issue, worthy of serious consideration. We now examine the sources of flexibility and stability in both Copycat and SME.

We start by noting that comparisons are not infinitely flexible. As described in Section 4.1, people are easily able to view the ambiguous item (Figure 3b) as having 3 prongs when comparing it to Figure 3a and 4 prongs when comparing it to Figure 3c. However, people cannot view the item in Figure 3a as having 6 prongs, because it has an underlying structure incompatible with that interpretation. There are limits to flexibility.
Another example of flexibility comes from the pair of pictures in Figure 4. In these pictures the robots are cross-mapped: that is, they are similar at the object level yet play different roles in the two pictures. People deal flexibly with such cross-mappings. They can match the two pictures either on the basis of like objects, by placing the two robots in correspondence, or on the basis of like relational roles, in which case the robot in the top picture is placed in correspondence with the repairman in the bottom picture. Interestingly, people do not mix these types of similarity (Goldstone, Medin & Gentner, 1991). Rather, they notice that, in this case, the attribute similarity and the relational similarity are in opposition. SME’s way of capturing this flexibility is to allow the creation of more than one interpretation of an analogy. Like human subjects, it will produce both an object-matching interpretation and a relation-matching
interpretation. As with human judges, the relational interpretation will usually win out, but may lose to the object interpretation if the object matches are sufficiently rich (Gentner & Rattermann, 1991; Markman & Gentner, 1993a).

How does Copycat model the flexibility of analogy and the more general principle that cognitive processes are themselves “fluid”? In Copycat (and in Tabletop (French, 1995)), a major source of flexibility is held to be the ability of concepts to “slip” into each other, so that nonidentical concepts can be seen as similar if that helps make a good match. They contrast this property with SME’s rule that relational predicates (though not functions and entities) must be identical to match, claiming that Copycat is thus more flexible. Let us compare how Copycat and SME work, to see which scheme really is more flexible.

Like SME, Copycat relies on local rules to hypothesize correspondences between individual statements as part of its mapping operations. (Any matcher must constrain the possible correspondences; otherwise everything would match with everything else.) Recall from Section 3.4 that Copycat’s constraints come from two sources: a Slipnet and a notion of conceptual depth. A Slipnet contains links between predicates. For two statements to match, either their predicates must be identical, or there must be a link connecting them in the Slipnet. Each such link has a numerical weight, which influences the likelihood that predicates so linked will be placed in correspondence. (Metaphorically, the weight suggests how easy it is for one concept to “slip into another.”) These weights are pre-associated with pairs of concepts. In addition, each predicate has associated with it a conceptual depth, a numerical property indicating how likely it is to be involved in non-identical matches. Predicates with high conceptual depth are less likely to match non-identically than predicates with low conceptual depth.

Both the weights on predicate pairs (the Slipnet) and the conceptual depths of individual predicates are hand-coded and pre-set. Because these representations do not have any other independent motivation for their existence, there are no particular constraints on them, aside from selecting values which make Copycat work in an appealing way. This is not flexibility: it is hand-tailoring of inputs to achieve particular results, in exactly the fashion that CFH decry. Because of this design, Copycat is unable to make correspondences between classes of statements that are not explicitly foreseen by its designers. Copycat cannot learn, because it cannot modify or extend these hand-coded representations that are essential to its operation. More fundamentally, it cannot capture what is perhaps the most important, creative aspect of analogy: the ability to align and map systems of knowledge from different domains.

SME, despite its seeming rigidity, is in important ways more flexible than Copycat. At first glance this may seem wildly implausible. How can a system that requires identically in order to make matches between relational statements qualify as flexible? The relational identicality requirement provides a strong, domain-independent, semantic constraint. Further, the requirement is not as absolute as it seems, for matches between non-identical functions are allowed, when sanctioned by higher-order structure. Thus SME can place different aspects of complex situations in correspondence when they are represented as functional dimensions. This is a source of bounded flexibility. For example, SME would fail to match two scenes represented as louder(Fred, Gina) and bigger(Bruno, Peewee). But if the situations were represented in terms of the same relations over different dimensions -- as in greater(loudness(F), loudness(G)) and greater(size(B), size(P))
then the representations can be aligned. Moreover in doing so SME aligns the dimensions of loudness and size. If we were to extend the comparison -- for example, by noting that a megaphone for Gina would correspond to stilts for Peewee -- this dimensional alignment would facilitate understanding of the point that both devices would act to equalize their respective dimensions. We have found that online comprehension of metaphorical language is facilitated by consistent dimensional alignments (Gentner & Boronot, 1991; Gentner & Imai, 1992).

The contrast between SME and Copycat can be illustrated by considering what would happen if both systems were given the following problem with two choices:

If abc $\rightarrow$ abd then Mercury, Venus, Earth $\rightarrow$ ??

(1) Mercury, Venus, Mars or (2) Mercury, Venus, Jupiter

In order to choose the correct answer (1) SME would need representational information about the two domains -- e.g., the greater-than relations along the dimension of closeness to sun for the planets and for the dimension of precedence in alphabet for the letters. It could then choose the best relational match, placing the two unlike dimensions in correspondence. But no amount of prior knowledge about the two domains taken separately would equip Copycat to solve this analogy. It would have to have advance knowledge of the cross-dimensional links: e.g., that closer to sun could slip into preceding in alphabet. SME’s ability to place nonidentical functions in correspondence allows it to capture our human ability to see deep analogies between well-understood domains even when they are juxtaposed for the first time.

Despite the above arguments, we agree that there may be times when identicality should be relaxed. This consideration has led to our tiered identicality constraint, which allows non-identical predicates to match (a) if doing so would lead to a substantially better or more useful match, and (b) if there is some principled reason to justify placing those particular predicates in correspondence. One method for justifying non-identical predicate matches is Falkenhainer’s minimal ascension technique, which was used in Phineas (1987, 1988, 1990). Minimal ascension allows statements involving non-identical predicates to match if the predicates share a close common ancestor in a taxonomic hierarchy, when doing so would lead to a better match, especially one that could provide relevant inferences. This is a robust solution for two reasons. First, the need for matching non-identical predicates is determined by the program itself, rather than a priori. Second, taxonomic hierarchies have multiple uses, so that there are sources of external constraint on building them.

However, our preferred technique for achieving flexibility while preserving the identicality constraint is to re-represent the nonmatching predicates into subpredicates, permitting a partial match. Copycat is doing a simple, domain-specific form of rerepresentation when alternate descriptions for the same letter-string are computed. However, the idea of rerepresentation goes far beyond this. If identicality is the dominant constraint in matching, then analogizers who have regularized their internal representations (in part through prior rerepresentation processes) will be able to use analogy better than those who have not. There is some psychological evidence for this gentrification of knowledge. Kotovsky and Gentner (in press) found that 4-year-olds were initially at chance in choosing cross-dimensional perceptual matches (e.g., in deciding whether black-grey-
black should be matched with big-little-big or with a foil such as big-big-little). But children could come to perceive these matches if they were given intensive within-domain experience or, interestingly, if they were taught words for higher-order perceptual patterns such as symmetry. We speculate that initially children may represent their experience using idiosyncratic internal descriptions (Gentner and Rattermann, 1991). With acculturation and language-learning, children come to represent domains in terms of a canonical set of dimensions. This facilitates cross-domain comparisons, which invite further rerepresentation, further acting to canonicalize the child’s knowledge base. Subsequent cross-domain comparisons will then be easier. Gentner, Rattermann, Markman & Kotovsky (1995) discuss some mechanisms of re-representation that may be used by children. Basically, rerepresentation allows relational identicality to arise as out of an analogical alignment, rather than acting as a strict constraint on the input descriptions.

A second source of flexibility in SME, again seemingly paradoxically, is its rigid reliance on structural consistency. The reason is that structural consistency allows the generation of candidate inferences. Remember that a candidate inference is a surmise about the target, motivated by the correspondences between the base and the target. To calculate the form of such an inference requires knowing unambiguously what goes with what (provided by satisfying the 1:1 constraint) and that every part of the statements that correspond can be mapped (provided by satisfying the parallel connectivity constraint). This reliance on one-to-one mapping in inference is consistent with the performance of human subjects (Markman, in preparation). The fact that structural consistency is a domain-general constraint means that SME can (and does) generate candidate inferences in domains not foreseen by its designers. Copycat, on the other hand, must rely on domain-specific techniques to propose new transformation rules.

A third feature that contributes to flexibility is SME’s initially blind local-to-global processing algorithm. Because it begins by blindly matching pairs of statements with identical predicates, and allowing connected systems to emerge from these local identities, it does not need to know the goal of an analogy in advance. Further, it is capable of working simultaneously on two or three different interpretations for the same pair of analogs.

Is SME sufficiently flexible to fully capture human processing? Certainly not yet. But the routes towards increasing its flexibility are open, and are consistent with its basic operation. One route is to increase its set of re-representation techniques, a current research goal. Flexibility, to us, entails the capability of operating across a wide variety of domains. This ability has been demonstrated by SME. It has been applied to entire domains not foreseen by its designers (as described above), as well as sometimes surprising its designers even in domains they work in. Flexibility also entails the ability to produce different interpretations of the same analogy where appropriate. Consider again the example in Figure 4, which illustrates a typical cross-mapping. As we discussed earlier, human subjects entertain two interpretations, one based on object-matching and one based on relational-role matching. SME shows the same pattern, and like people it prefers the interpretation based on like relational roles, so that the robot doing the repairing is placed in correspondence with the person repairing the other robot (see Markman & Gentner, 1993a, for a more detailed description of these simulations). It should be noted that few computational models of analogy are able to handle cross-mappings successfully. Many programs, such as ACME (Holyoak & Thagard, 1989), will generate only a single interpretation that is a mixture of the relational similarity match and the
object similarity match. The problem cannot even be posed to Copycat, however, because its operation is entirely domain-specific. This, to us, is the ultimate inflexibility.

4.3 Is analogy a domain-general process?

A consequence of CFH’s argument that perception cannot be split from comparison is that one should not be able to make domain-independent theories of analogical processing. However, there is ample evidence to the contrary in the literature. In the genre of theories that are closest to SME, we find a number of simulations that have made fruitful predictions concerning human phenomena, including

ACME (Holyoak & Thagard, 1989)
IAM (Keane, 1990; Keane, Ledgeway, & Duff, 1994)
SIAM (Goldstone & Medin, 1994)
REMIND (Lange & Wharton, 1993)
LISA (Holyoak & Hummel, in press)

Even in accounts that are fundamentally different from ours, eg. bottom-up approaches such as one of Winston’s (1975) early models, or top-down approaches (Kedar-Cabelli, 1985; Greiner, 1988), there are no serious domain-specific models. This is partly because of the problems that seem natural to analogy. The most dramatic and visible role of analogy is as a mechanism for conceptual change, where it allows people to import a set of ideas worked out in one domain into another. Obviously, domain-specific models of analogy cannot capture this signature phenomenon.

There are grave dangers with domain-specific models. The first danger is that the model can be hostage to irrelevant constraints. One way to test the validity of the inevitable simplifications made in modeling is to triangulate, testing the model with a wide variety of inputs. Limiting a model to a specific domain dramatically reduces the range over which it can be tested. Another way to test the validity of simplifications is to see if they correspond to natural constraints. Surprisingly little effort has been made to examine the psychological plausibility of the simplifying assumptions that go into Copycat. Mitchell (1993) describes an initial experiment designed to see if human subjects perform similarly to Copycat in its domain. This study produced mixed results; more efforts of this kind would be exceedingly valuable. Likewise, French (1995) presents the results of some studies examining human performance in his Tabletop domain, in which people make correspondences between tableware on a table. Again, this effort is to be applauded. But in addition to carrying out more direct comparisons, the further question needs to be addressed of whether and how these domains generalize to other domains of human experience. At present we have no basis for assuming that the domain specific principles embodied in Copycat are useful beyond a narrow set of circumstances.

The second danger of domain-specific models is that it is harder to analyze the model, to see why it works. For example, Mitchell (1993) notes that in Copycat, only one type of relationship may be used to describe a created group. Thus, in grouping the ttt in the letter string rsssttt, Copycat sometimes describes it as a group of three things, and other times as a group of the letter T (to choose, it
probabilistically picks one or the other, with shorter strings being more likely to be described by their length than by their common letter). This is partly due to a limitation in the mapping rules for Copycat, which can only create a single matching bond between two objects. For example, it could create either a letter-group bond or a triad group bond between ttt and uuu, but not both. Why should this be? (Note that this is quite different from the situation with humans. People consider a match between two things better the more structurally consistent relations they have in common.) As far as we can tell, the ban on having more than a single mapping bond between any two objects is a simple form of the one-to-one matching criterion found in SME. This prevents one letter from being matched to more than one other, which in most aspects of Copycat’s operation is essential, but it backfires in not being able to create matches along multiple dimensions. Human beings, on the other hand, have no problem matching along multiple dimensions. In building domain-specific models the temptation to tweak is harder to resist, because the standard for performance is less difficult than for domain-independent models.

4.3 Micro-worlds and real worlds: Bootstrapping in Lilliput

A common criticism of Copycat is that its domain of letter strings is a “toy” domain, and that nothing useful will come from studying this sliver of reality. Hofstadter and his colleagues counter that that the charge of using toy domains is more accurately leveled at other models of analogy (like SME), which leave many aspects of their domains unrepresented. Our purpose here is not to cudgel Copycat with the toy domain label. We agree with Hofstadter that a detailed model of a small domain can be very illuminating. But it is worth examining Hofstadter’s two arguments for why SME is more toylike than Copycat.

First, Hofstadter with some justice takes SME and ACME to task because of the rather thin domain semantics in some of their representations. For example, he notes that even though SME’s representations contain labels like ‘heat’ and’water’, “The only knowledge the program has of the two situations consists of their syntactic structures …it has no knowledge of any of the concepts involved in the two situations.” (Hofstadter, 1995a, p. 278). This is a fair complaint for some examples. However, the same can be said of Copycat’s representations. Copycat explicitly factors out every perceptual property of letters, leaving only their identity and sequencing information (i.e., where a letter occurs in a string and where it is in an alphabet). There is no representation of the geometry of letters: Copycat wouldn’t notice that “b” and “p” are similar under a flip, for instance, or that “a” looks more like “a” than “a” does.

The second argument raised by Hofstadter and his colleagues concerns the size and tailoring of the representations. Although they acknowledge that SME’s representations often include information irrelevant to the mapping, CFH state:

“The mapping processes used in most current computer models of analogy-making, such as SME, all use very small representations that have the relevant information selected and ready for immediate use. For

13 However, SME escapes this charge for the representations it has borrowed from qualitative physics programs, which have a richly interconnected domain structure. (There is still, of course, no true external reference, but this is equally true for all the models under discussion.) See also Ferguson (1994), which uses visual representations computed automatically from a drawing program.
these programs to take as input large representations that include all available information would require a radical change in their design.” (CFH, p. 201)

Let us compare the letter string domain of Copycat with the qualitative physics domain of PHINEAS. There are several ways one might measure the complexity of a domain or problem:

- **Domain size:** How many facts and rules does it take to express the domain?
- **Problem size:** How many facts does it take to express the particular situation or problem?
- **Elaboration size:** How many facts are created when the system understands a particular problem?

In Copycat the domain size is easy to estimate, because we can simply count (a) the number of rules (b) the number of links in the Slipnet and (c) the number of predicates. In PHINEAS it is somewhat harder, because much of its inferential power comes from the use of QPE, a qualitative reasoning system that was developed independently and has been used in a variety of other projects and systems. In order to be as fair as possible, we exclude from our count the contents of QPE and the domain-independent laws of QP theory (even though these are part of Phineas’ domain knowledge). Instead, we will count only the number of statements in its particular physical theories. We also ignore the size of PHINEAS’ initial knowledge base of explained examples, even though this would again weigh in favor of our claim. Table 1 shows the relative counts on various dimensions.
The number of expressions is only a rough estimate of the complexity of a domain, for several reasons. First, higher-order relations may add more complexity than lower order relations. Copycat has no higher-order relations, while PHINEAS does. Further, PHINEAS does not have a Slipnet to handle predicate matches. Instead it uses higher-order relational matches to promote matching non-identical predicates. Second, ISA links and partonomy links are not represented in the same way in both systems. Finally, the representation changes significantly enough in Copycat that it is not clear whether to include all relations constructed over the entire representation-building period, or simply to take the maximum size of the representation that Copycat constructs at any one time.

So, in order to estimate the complexity fairly, we use the following heuristics. First, for domain complexity, we count the number of entities, the number of entity categories, the number of rules the domain follows, and the number of relational predicates used. Then, for problem complexity, we simply

<table>
<thead>
<tr>
<th></th>
<th>Copycat (IJK example)</th>
<th>PHINEAS (Caloric heat example)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Entities</td>
<td>26 letters and 5 numbers</td>
<td>10 predefined entities plus arbitrary number of instantiated entities</td>
</tr>
<tr>
<td>Entity Types</td>
<td>2</td>
<td>13 in type hierarchy</td>
</tr>
<tr>
<td>Relational Predicates</td>
<td>26</td>
<td>174 (including 50 Quantity relations)</td>
</tr>
<tr>
<td>Rules</td>
<td>24 rules (codelet types) and 41 slippages between predicates</td>
<td>64 rules. Also 10 views, and 9 physical processes (approximately 135 axioms when expanded into clause form).</td>
</tr>
</tbody>
</table>

Table 1: Relative complexity of Copycat and PHINEAS domain theories

<table>
<thead>
<tr>
<th></th>
<th>Copycat (IJK example)</th>
<th>PHINEAS (Caloric heat example)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Entities</td>
<td>9 entities</td>
<td>11 entities (7 in base, 4 in target)</td>
</tr>
<tr>
<td>Relations between entities</td>
<td>15 relations $^{14}$</td>
<td>88 relations (55 in base, 33 in target)</td>
</tr>
</tbody>
</table>

Table 2: Relative complexity of Copycat and PHINEAS demonstration problems.

The number of expressions is only a rough estimate of the complexity of a domain, for several reasons. First, higher-order relations may add more complexity than lower order relations. Copycat has no higher-order relations, while PHINEAS does. Further, PHINEAS does not have a Slipnet to handle predicate matches. Instead it uses higher-order relational matches to promote matching non-identical predicates. Second, ISA links and partonomy links are not represented in the same way in both systems. Finally, the representation changes significantly enough in Copycat that it is not clear whether to include all relations constructed over the entire representation-building period, or simply to take the maximum size of the representation that Copycat constructs at any one time.

So, in order to estimate the complexity fairly, we use the following heuristics. First, for domain complexity, we count the number of entities, the number of entity categories, the number of rules the domain follows, and the number of relational predicates used. Then, for problem complexity, we simply

$^{14}$The fifteen relations for the IJK example include 3 each of the leftmost, rightmost, and middle relations, 2 grouping relations, and 4 letter successor relations.
count the number of entities and the number of relations. For Copycat, we count the total number of relational expressions created, even when those expressions are later thrown away in favor of other representations.

For the domain comparison (Table 1), the results clearly show the relative complexity of PHINEAS when compared to Copycat. Copycat has a set of 31 entities (26 letters and 5 numbers), which are described using a set of 24 codelet rules and 41 slippages, represented in a description language containing only 26 predicates. PHINEAS, on the other hand, has a domain which contains 10 predefined entities (such as alcohol and air) as well as an arbitrary number of instantiations of 13 predefined entity types. There are 65 general rules in the domain theory, as well as multiple rules defined in each of 9 process descriptions and 10 view descriptions, for a total of approximately 112-160 rules (assuming that each process or view description contains an average of 3-5 rules (again, not counting the rules in the QPE rule engine itself)). The relational language of Phineas is much richer than Copycat’s, with 174 different predicates defined in its relational language (including 50 quantity types).

The problem complexity of PHINEAS is similarly much higher than Copycat’s. For example, take the first examples given for both PHINEAS in (Falkenhainer, 1988) and for Copycat in (Mitchell, 1993). For the IJK problem in Copycat, there are 9 entities that are described via 15 relational expressions (21 if you want to count the predicate matches created in the Slipnet). On the other hand, PHINEAS’ caloric heat example contains 11 entities (split between base and target) that are described via 88 relational expressions. Similar results may be obtained in comparing other examples from PHINEAS and Copycat.

Despite CFH’s claims that Copycat excels in representation-building, it seems clear that Phineas actually constructs larger and more complex representations.

**The dangers of microworlds**

Microworlds can have many advantages. But they work best when they allow researchers to focus on a small set of general issues. If chosen poorly, research in microworlds can yield results that only apply to a small set of issues specific to that microworld. The use of Blocks World in 1970s AI vision research provides an instructive example of the dangers of microworlds. First, carving off “scene analysis” as an independent module that took as input perfect line drawings was, in retrospect, unrealistic: Visual perception has top-down as well as bottom-up processing capabilities (c.f. recent work in animate vision (e.g. Ballard, 1991)). Second, vision systems that built the presumptions of the microworld into their very fabric (e.g., all lines will be straight and terminate in well-defined vertices) often could not operate outside their tightly constrained niche. The moral is that the choice of simplifying assumptions is crucial.

Like these 1970s vision systems, Copycat ignores the possibility of memory influencing current processing and ignores learning. Yet these issues are central to why analogy is interesting as a cognitive phenomenon. Copycat is also highly selective in its use of the properties of its string-rule domain. This extensive use of domain-specific information is also true of siblings of Copycat like French’s (1995) Tabletop.

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15 Some of the codelets and most of the slipnodes are really used for mapping, rather than representation-building, so we are actually overcounting the number of relevant rules here.
If we are correct that the analogy mechanism is a domain-independent cognitive mechanism, then it is important to carry out research in multiple domains to ensure that the results are not hostage to the peculiarities of a particular microworld.

5. How should the psychological plausibility of a model of analogy be assessed?

Both Hofstadter’s group and our own group have as their goal to model human cognition, but we have taken very different approaches. Our group, and other analogy researchers such as Holyoak, Keane, and Halford, follow a more-or-less standard cognitive science paradigm in which the computational model is developed hand-in-hand with psychological theory and experimentation. The predictions of computational models are tested on people, and the results are used to modify or extend the computational model, or in the case of competing models, to support one model or the other. Further, because we are interested in the processes of analogical thinking as well as in the output of the process, we have needed to “creep up” on the phenomena from several different directions. We have carried out several scores of studies, using a range of methods -- free interpretation, reaction time, ratings, protocol analysis, and so on. We are still a long way from a full account.

This research strategy contrasts with that of Hofstadter (1995a, p. 359), who states:

“What would make a computer model of analogy-making in a given domain a good model? Most cognitive psychologists have been so well trained that even in their sleep they would come up with the following answer: Do experiments on a large number of human subjects, collect statistics, and make your program imitate those statistics as closely as possible. In other words, a good model should act very much like Average Ann and Typical Tom (or even better, like an average the two of them).

Cognitive psychologists tend to be so convinced of this principle as essentially the only way to validate a computer model that it is almost impossible to talk them out of it. But that is the job to be attempted here.

We note in passing that most cognitive psychologists would be startled to see this characterization. The central goal of most cognitive psychologists to model the processes by which humans think. The job would be many times easier if matching output statistics were all that mattered.

Hofstadter (1995a, p. 354) goes on to propose specific ways in which Copycat and Tabletop might be compared with human processing. For example, answers that seem obvious to people should appear frequently in the program’s output, and answers that seem far-fetched to people should appear infrequently in the output; answers that seem elegant but subtle should appear infrequently but with a high quality rating in the program’s behavior. Further, if people’s preferred solutions shift as a result of a given order of prior problems, then so should the program’s solution frequencies and quality judgments. Also, the program’s most frequent pathways to solutions “should seem plausible from a human point of

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16 Examples are the comparison of MAC/FAC and ARCS as models of similarity-based retrieval (Forbus, Gentner & Law, 1995), the comparison of SME and ACME as accounts of analogical inference (Clement & Gentner, 1991; Markman, in press; Spellman & Holyoak, 1993), and comparisons of ACME, SME and IAM (Keane, Ledgeway, & Duff, 1994).

17 Burns (1996) has shown that such order effects do occur: people’s solutions preferences on letter-string analogies shift as a result of prior letter-string analogies.
view”. These criteria seem eminently reasonable from a psychological point of view. But Hofstadter (1995a, p. 364) rejects the psychologist’s traditional methods:

“Note that these criteria …can all be assessed informally in discussions with a few people, without any need for extensive psychological experimentation. None of them involves calculating averages or figuring out rank-orderings from questionnaires filled out by large numbers of people.”

“…such judgments [as the last two above] do not need to be discovered by conducting large studies; once again, they can easily be gotten from casual discussions with a handful of friends”

The trouble with this method of assessment is that it is hard to find out when one is wrong. One salubrious effect of doing experiments on people who don’t care about one’s hopes and dreams is that one is more or less guaranteed a supply of humbling and sometimes enlightening experiences. Another problem with Hofstadter’s method is that no matter how willing the subject, people simply don’t have introspective access to all their processes.

In explaining why he rejects traditional psychology methods, Hofstadter (1995a, p. 359) states:

“…Who would want to spend their time perfecting a model of the performance of lackluster intellects when they could be trying to simulate sparkling minds? Why not strive to emulate, say, the witty columnist Ellen Goodman or the sharp-as-a-tack theoretical physicist Richard Feynman?

…In domains where there is a vast gulf between the taste of sophisticates and that of novices, it makes no sense to take a bunch of novices, average their various tastes together, and then use the result as a basis for judging the behavior of a computer program meant to simulate a sophisticate.

He notes later that traditional methods are appropriate when one single cognitive mechanism, or perhaps the interaction of a few mechanisms, is probed, because these might reasonably be expected to be roughly universal across minds.

This suggests that some of these differences in method and in modeling style stem from a difference in goals. Whereas psychologists seek to model general mechanisms -- and we in particular have made the bet that analogical mapping and comparison in general is one such mechanism -- Hofstadter is interested in capturing an extraordinary thinker. We have, of course, taken a keen interest in whether our mechanisms apply to extraordinary individual thinkers. There has been considerable work applying structure-mapping and other general process models to cases of scientific discovery. For example, Nersessian (1992) has examined the use of analogies by Maxwell and Faraday; Gentner et al. (in press) have analyzed Kepler’s writings, and have run SME simulations to highlight key features of the analogies Kepler used in developing his model of the solar system.18 Dunbar (1995) has made detailed observations of the use of analogy in microbiology labs. These analyses of analogy in discovery suggest that many of the processes found in ordinary college students may also occur in great thinkers. But a further difference is that Hofstadter is not concerned with analogy exclusively, but also with its interaction with the other processes of “high-level perception”. His aim appears to be to capture the detailed performance of one or a few extraordinary individuals engaged in a particular complex task -- one with a strong aesthetic

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18 We hasten to state that we do not consider ourselves to have captured Kepler’s discovery process.
component. This is a unique and highly interesting project. But it is not one that can serve as a general model for the field.

6. Summary and conclusions

"We consider the process of arriving at answer wyz to be very similar, on an abstract level, to the process whereby a full-scale conceptual revolution takes place in science"

--- Hofstadter 1995, page 261

Hofstadter and his colleagues make many strong claims about the nature of analogy, as well as about their research program (as embodied in Copycat), and our own. Our goals here have been to correct misstatements about our research program and to respond to their claims about the nature of analogy, many of which are not supported or are even countermanded by data. CFH argued that analogy should be viewed as “high-level perception.” We believe this metaphor obscures more than it clarifies. While it appropriately highlights the importance of building representations in cognition, it undervalues the importance of long-term memory, learning, and even perception, in the usual sense of the word. Finally, we reject Hofstadter’s claim that analogy is inseparable from other processes. On the contrary, the study of analogy as a domain-independent cognitive process that can interact with other processes has led to rapid progress.

There are things to admire about Copycat. It is an interesting model of how representation construction and comparison can be interwoven in a simple, highly familiar domain, in which allowable correspondences might be known in advance. Copycat’s search technique, with gradually lowering temperature, is an intriguing way of capturing the sense of settling on a scene interpretation. Moreover there are some points of agreement: both groups agree on the importance of dimensions such as the clarity of the mapping, and that comparison between two things can alter the way in which one or both are conceived. But Copycat’s limitations must also be acknowledged. The most striking of these is that every potential non-identical correspondence -- and its evaluation score -- is domain-specific and hand-coded by its designers, forever barring the creative use of analogy for cross-domain mappings or for transferring knowledge from a familiar domain to a new one. In contrast, SME’s domain-general alignment and mapping mechanism can operate on representations from different domains and find whatever common relational structure they share. It has been used with a variety of representations (some built by hand, some built by others, some built by other programs) and has run on dozens if not hundreds of analogies whose juxtaposition was not foreseen by its designers. (True, its success depends on having at least some common representational elements, but this we argue is true of human analogists as well.) Further, Copycat itself contradicts CFH’s claims concerning the holistic nature of high-level perception and analogy, for Mitchell’s (1993) analysis of Copycat demonstrates that it can be analyzed into modules.

Debates between research groups have been a motivating force in the advances made in the study of analogy. For example, the roles of structural and pragmatic factors in analogy are better understood as a result of debates in the literature (see Clement & Gentner, 1991; Gentner & Clement, 1988; Holyoak, 1985; Keane, Ledgeway, & Duff, 1994; Markman, in preparation; Spellman & Holyoak, in press). However, these debates first require accurate characterizations of the positions and results on both sides of the debate. It is in this spirit that we sought to correct systematic errors in the descriptions of our work that appear in CFH and again in Hofstadter (1995a): e.g., the claim that SME is limited to small
representations that contain only the relevant information. As Section 3 points out, SME has been used with hand-generated representations, with representations generated for other analogy systems, and with representations generated by other kinds of models altogether (such as qualitative reasoners). SME has been used in combination with other modules in a variety of cognitive simulations and performance programs. In other words, SME is an existence proof that modeling alignment and mapping as domain-general processes can succeed, and can drive the success of other models. Although CFH never mention our psychological work (which shares an equal role with the simulation side of our research), we believe it too says a great deal about analogy and its interactions with analogy with other cognitive processes. In our view, the evidence is overwhelmingly in favor SME and its associated simulations over Copycat as a model of human analogical processing.
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