Calibration of Piezoelectric Driven Mirrors for Laser Resonators

Prepared by
R. L. VARWIG, R. L. SANDSTROM (Consultant), and C. P. WANG
Aerophysics Laboratory

21 September 1979

Prepared for
VICE PRESIDENT AND GENERAL MANAGER
LABORATORY OPERATIONS

THE AEROSPACE CORPORATION

19980309 341
CALIBRATION OF PIEZOELECTRIC DRIVEN MIRRORS FOR LASER RESONATORS

Prepared by
R. L. Varwig, R. L. Sandstrom (Consultant), and C. P. Wang
Aerophysics Laboratory

21 September 1979

Laboratory Operations
THE AEROSPACE CORPORATION
El Segundo, California 90245

Prepared for
VICE PRESIDENT AND GENERAL MANAGER
LABORATORY OPERATIONS
CALIBRATION OF PIEZOELECTRIC DRIVEN MIRRORS FOR LASER RESONATORS

Prepared

R. L. Varwig
R. L. Sandstrom

C. P. Wang

Approved

H. Mirels, Head
Aerodynamics and Heat Transfer Department

W. R. Warren, Jr., Director
Aerophysics Laboratory
ABSTRACT

A new technique for measuring small displacements of piezoelectric driven mirrors in which is employed an acousto-optic modulator and optical heterodyning has been applied to the calibration of piezoelectric driven mirror systems for laser resonator cavities. In this technique, a phase detector is used to measure the phase change when a mirror, driven by the piezoelectric translator, moves. Measurements obtained by means of this technique have been compared with measurements obtained with the traditional interferometer methods and have proven to be more precise. The increased precision was attributed to higher signal-to-noise ratios typically obtained with frequency-modulated, relative to amplitude-modulated, systems where intensity fluctuations exist in the system. The increased signal-to-noise ratio is advantageous when, as frequency increases, the output voltage from the driving power amplifier falls off. For a given amplifier, frequency response data of the piezoelectric driver-mirror combination can be determined at higher frequencies. In the case at hand, the frequency has been extended from 15 to 40 kHz.
ACKNOWLEDGMENTS

It is with pleasure that the authors recognize the contributions of Mr. Terry Felker, who provided technical support for the test program.
FIGURES

<table>
<thead>
<tr>
<th>FIGURE</th>
<th>DESCRIPTION</th>
<th>PAGE</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>Acousto-Optic Modulator Arranged to Measure Mirror Motions</td>
<td>4</td>
</tr>
<tr>
<td>2.</td>
<td>Phase Detector Calibration of PZT Units S/N-1 and -2 and Burleigh High-Frequency PZT Unit at 1 kHz</td>
<td>6</td>
</tr>
<tr>
<td>3.</td>
<td>Schematic Diagram for Measuring Displacement of Mirror with Zygo Interferometer when Driven by Piezoelectric Ceramic Normal to its Surface</td>
<td>8</td>
</tr>
<tr>
<td>4.</td>
<td>Fringe Pattern</td>
<td>9</td>
</tr>
<tr>
<td>5.</td>
<td>Typical Fringe Shift Pattern for Determining Calibration of PZT Unit S/N-2</td>
<td>10</td>
</tr>
<tr>
<td>6.</td>
<td>Frequency Response of 4 Folar PZT Units as Determined with Phase Detector</td>
<td>13</td>
</tr>
<tr>
<td>7.</td>
<td>Zygo Interferometer Calibration Measurements of S/N-1 and -2 and Burleigh High-Frequency PZT Units at 1 kHz</td>
<td>16</td>
</tr>
</tbody>
</table>
I. INTRODUCTION

Piezoelectric (PZT) ceramic components, either disks or cylinders, are used to drive the mirrors in laser resonator cavities to change the resonator length and, hence, the resonator frequency. Therefore, the calibration of the PZT unit, i.e., the change in length per unit drive voltage, must be known. The frequency response of the PZT unit and its electrical driver is also of importance in determining loop gain when the unit is used in a feedback control circuit for stabilizing the laser.

In this report, a new technique for measuring the small displacements required for PZT calibration is described in which an acousto-optic modulator and optical heterodyning are used. In this technique, zeroth- and first-order diffracted beams from the acousto-optic modulator serve as measuring and reference beams in a phase-detecting system used to measure a change in phase when a mirror driven by the PZT to be calibrated moves. The phase variation is obtained when the two beams are combined in a heterodyning technique. The resultant beat signal, carrying the phase modulation, is demodulated, and the signal is displayed on an oscilloscope.

Measurements obtained with this technique are compared with a traditional interferometer measurement. The advantages of each system are described.
II. MEASUREMENTS

A. ACOUSTO-OPTIC MODULATOR PHASE DETECTOR METHOD

The experimental arrangement for measuring small displacements with the acousto-optic modulator phase detector is shown in Fig. 1. An acoustic wave establishes a pattern of density variations in an acoustic medium, which then becomes a moving phase grating. An optical wave passing through the medium normal to the acoustic wave direction is split into N diffracted beams oriented according to \( \sin \theta_N = N \lambda / \Lambda \). Here, \( \lambda \) is the optical wavelength, \( \Lambda \) is the acoustic wavelength, and \( N \), an integer, is the order of diffraction. For a Flint glass acoustic medium, \( \Lambda = 87.7 \mu m \) for a 40-MHz acoustic wave; \( \lambda = 0.6328 \mu m \), so that \( \theta_1 = 0.41 \) deg, which agrees quite well with the measured value of 0.4 deg.

Light in the diffracted beams has vector components along the axis of acoustic propagation and, therefore, experiences a frequency shift as a result of the Doppler effect

\[
\omega_N = \omega + N\Omega
\]

where \( \omega \) and \( \Omega \) are the optical and acoustic frequencies, respectively. In the phase detector, as used here, the zeroth-and first-order diffracted beams are combined by a beam splitter-mirror combination so that they constructively interfere with each other. The photodetector, a 1P28 photomultiplier tube, by observing the signal, detects the beat-frequency signal between these two beams.

The PZT to be calibrated drives mirror normal to its surface. From geometrical considerations, the phase change in terms of wavelength and mirror displacement \( \Delta \) is

\[
m = \frac{2\Delta}{\lambda} \left[ 1 + 0\left(\frac{\beta}{2}\right)^2 \right]
\]

-3-
Fig. 1. Acousto-Optic Modulator Arranged to Measure Mirror Motions
where $\beta$ is the angle of incidence of the light on the mirror. Since $\beta$ is small (Fig. 1), the phase change as the mirror moves is $m = 2\Delta/\lambda$ or $2\pi(2\Delta/\lambda)$ rad or $(2\Delta/\lambda)360$ deg.

The phase is determined by means of the phase demodulator in Fig. 1. This circuit mixes the carrier signal, the beat frequency $\Omega$, containing the phase-varying modulation from the mirror perturbation, with a reference signal and provides the demodulated output (the difference frequencies) by low-pass filtering. The circuit is tuned to 5 MHz; therefore, a 35-MHz signal is beat with the 40-MHz carrier to provide a 5-MHz carrier. Similarly, the reference signal is obtained by beating the unmodulated 40-MHz driver signal with the 35-MHz signal. Sensitivity of the phase demodulator circuit is 200 deg/V, which was determined by use of a phase-shifting circuit that operated at 5 MHz and had as its output a 5-MHz signal with a shifted phase. The phase shift was set at $2\pi$ rad by comparing an input 5-MHz signal and a phase-shifted signal on an oscilloscope. Then, the phase-shifted signal was applied to the phase demodulator, and the output signal observed. The phase demodulator signal was 1.8 V for $2\pi$ or a 360-deg phase shift.

PZT calibration is determined by driving the mirror with an oscillating signal of known value $V_D$, the lower trace of Fig. 2. The phase variation is determined by the output of the phase demodulator $V_s$, the upper trace of Fig. 2. From these signal levels (in volts) plus the phase-demodulator calibration of 200 deg/V, the mirror calibration is

$$\text{Calib} = \left( \frac{200 \text{ deg}}{V} \right) \left( \frac{\lambda}{2} \right) \left( \frac{1}{360 \text{ deg}} \right) \frac{V_s}{V_D} = \frac{\lambda}{3.6} \left( \frac{V_s}{V_D} \right) \text{\mu m} \frac{\text{V}}{\text{m}}$$

Numerical results are discussed in a later section.
Phase Detector Calibration of PZT Units S/N-1, 2 and Burleigh High Frequency PZT Unit at 1 kHz

\[
\begin{align*}
\text{PZT UNIT - S/N-1} & \quad \text{PZT DRIVING SIGNAL } V_D = 18 \text{ V} \\
\text{PHASE DETECTOR SIGNAL } V_S &= 0.074 \text{ V} \\
\text{PZT UNIT - S/N-2} & \quad \text{PZT DRIVING SIGNAL } V_D = 19 \text{ V} \\
\text{PHASE DETECTOR SIGNAL } V_S &= 0.12 \text{ V} \\
\text{BURLEIGH PZT UNIT} & \quad \text{PZT DRIVING SIGNAL } V_D = 57 \text{ V} \\
\text{PHASE DETECTOR SIGNAL } V_S &= 0.095 \text{ V}
\end{align*}
\]

Fig. 2. Phase Detector Calibration of PZT Units S/N-1 and 2 and Burleigh High-Frequency PZT Unit at 1 kHz
B. CONVENTIONAL INTERFEROMETER METHOD

Traditional interferometer measurements were made for comparison by means of the arrangements shown in Fig. 3. Here, a Zygo interferometer (Zygo Corporation, Middlefield, Connecticut), which is a type of Fizeau interferometer, was used. A HeNe laser (0.6328 μm) is used as the light source, so that the coherence length is large. Straight fringes are formed by the wedge-shaped film between the reference mirror of the interferometer and mirror mounted on the PZT to be tested. These fringes are observed in the film plane of the interferometer, where a pinhole aperture and 1P28 photomultiplier tube are installed. When the mirror is driven normal to itself, the wedge thickness varies, causing the fringes to shift. By careful adjustment of the wedge angle, a single fringe can be obtained that covers the film plane (Fig. 4). Hence, the resolution of the fringe variation can be maximized. Fringe resolution is indicated in Fig. 4 by the relative size of the aperture and the fringe spacing. A typical fringe shift pattern obtained with this assembly is shown in Fig. 5. The lower trace of Fig. 5 is the driving voltage applied to the PZT-mirror unit and, therefore, represents the oscillatory motion of the mirror. The upper trace is the intensity variation as the fringe shown in Fig. 4 shifts across the detector aperture. Thus, starting at point A with the mirror moving in one direction, a bright fringe passes the aperture, point B. As the mirror continues in the same direction, the bright fringe shifts to dark, point C. At point D, the mirror motion is reversed. For a fringe shift from bright to dark, the length change is \( (1/2)\lambda \), but since both incident and reflected paths must be included, this distance corresponds to a mirror motion of one-fourth wavelength. Thus, a direct calibration of the PZT-driven mirror unit is obtained, i.e., the mirror moves \( \lambda/4 = 0.1582 \, \mu m \) for a signal change \( V_B - V_C = 140 \, V \), yielding a calibration of \( 1.13 \, \mu m/kV \). The capability for providing a direct calibration represents the chief advantage of the interferometer technique.
Fig. 3. Schematic Diagram for Measuring Displacement of Mirror with Zygo Interferometer when Driven by Piezoelectric Ceramic Normal to its Surface
Fig. 4. Fringe Pattern (In this case, a single fringe, in the Zygo interferometer is shown with the photo detector aperture image.)
Fig. 5. Typical Fringe Shift Pattern for Determining Calibration of PZT Unit S/N-2. (A complete shift from center of bright fringe B to center of dark fringe C is observed, which corresponds to $(1/4)\lambda = 0.1582 \, \mu m$. $\Delta V = V_B - V_C$ for this shift is 140 so that calibration is $1.13 \, \mu m/kV$)
Values from the calibration measurement for four PZT units with mirrors from both the phase detector and the Zygo interferometer are given in Table 1, together with the calculated or estimated values determined from the physical properties of the PZT units. These predictions are described in the appendix.

The measured values for the calibration factor for the units Serial No. 1 (S/N-1) and Serial No. 2 (S/N-2), which are two-disk units made from 1.27-cm-diameter (0.5 in.) by 0.127-cm-thick (0.05 in.) disks of a ceramic manufactured by Vernitron Corporation, Bedford, Ohio, and designated as PZT-5H, are different from each other by about a factor of two, which indicates that one of the two disks in the stack making up S/N-1 is disabled. Probably no contact has been established between one of the tabs on the unit and the silver plating deposited on each surface of the disk.

Frequency-response data for these PZT units are presented in Fig. 6. These data were obtained by plotting the ratio of the photomultiplier output signal to the driving voltage signal as a function of frequency. An hp 6827 bipolar power supply-amplifier serves as the driver amplifier for the laboratory-built S/N-1 and S/N-2 and the Burleigh high-frequency PZT units, whereas a Burleigh PZ-70 operational amplifier was used to drive the PZ-80 unit.

The Burleigh PZ-80, with its cylindrical construction and heavier mirror and retaining ring assembly, should have a lower resonant frequency relative to the disk-type PZT drivers, which is, in fact, observed. A resonant peak in the gain versus frequency curve occurs at about 4 kHz. The gain falls off rapidly beyond 4 kHz. Since the gain versus frequency curve is flat to 1 kHz, this unit should provide adequate response to that frequency. The other three units examined all appeared to remain flat to beyond 10 kHz. At between 15 and 30 kHz, the hp 6827 amplifier begins to fall off, which probably explains the bobble in the gain-frequency curves that appears to start at 15 kHz. There is a cutoff filter in the phase demodulator at 40 kHz. Hence, no measurements are obtained beyond this.
point. It can be concluded that these three PZT units along with their mirrors and amplifier can be used quite satisfactorily to a frequency of 15 kHz.

### Table 1. Calibration Factors Obtained for PZT Units

<table>
<thead>
<tr>
<th>PZT Unit</th>
<th>Zygo Calibration, $\mu$m/V</th>
<th>Phase-Detector Calibration, $\mu$m/V</th>
<th>Value Computed from PZT Property, $\mu$m/V</th>
</tr>
</thead>
<tbody>
<tr>
<td>Burleigh High Frequency</td>
<td>0.000394</td>
<td>0.000316</td>
<td>0.0003</td>
</tr>
<tr>
<td>Laboratory-Built S/N-1</td>
<td>0.000662</td>
<td>0.0012</td>
<td>0.0012</td>
</tr>
<tr>
<td>Laboratory-Built S/N-2</td>
<td>0.00151</td>
<td>0.00104</td>
<td>0.0012</td>
</tr>
<tr>
<td>Burleigh PZ-80</td>
<td>0.0049</td>
<td>0.00478</td>
<td>0.0043, 0.0096</td>
</tr>
</tbody>
</table>
Fig. 6. Frequency Response of Four PZT Units as Determined with Phase Detector
Data for the calibration of three PZTs have been obtained with the acousto-optic modulator phase detector and, for comparison, the Zygo interferometer. Oscilloscope records of these data are shown in Fig. 2 for the phase detector and in Fig. 7 for the interferometer. The advantage of the phase detector over the interferometer is obvious. Its signal-to-noise ratio is 40 times greater than that of the interferometer when referenced to the PZT driving signal, because in phase modulation, half of the noise is rejected by clipping of the input signal. Thus, the effect of fringe drift and jiggle, which the interferometer observes is reduced in the phase detector. In addition, the advantage of phase modulation over amplitude modulation is wider bandwidth. Also, more complex side-band frequency structure contributes to higher signal-to-noise ratio in the phase detector.

One of the objectives of this study is to obtain frequency-response data of the PZT mirror mount. These data are obtained by observing the phase detector or interferometer signal while increasing the signal frequency driving the PZT. As with all amplifiers, as frequency increases, a point is reached where the amplifier output voltage falls off. Thus, the signal driving the PZT is decreased so that the PZT displacement is reduced. With decreased mirror displacement, signal size is reduced so that signal-to-noise ratio decreases. The output voltage driving PZT S/N-2, for example, drops to 20 V at a frequency of 40 kHz. The phase-detector output is easily observed at 40 kHz. However, for the interferometer, a 20-V oscillation signal on the PZT would produce a signal less than one-third the signal observed (top trace for PZT S/N-2, Fig. 7). Such a value would be indistinguishable from the noise on this signal. As a result, one is unable to obtain frequency-response data at frequencies close to 40 kHz with the interferometer technique. The practical limit is probably closer to 15 kHz.
Fig. 7. Zygo Interferometer Calibration Measurements of S/N-1 and -2 and Burleigh High-Frequency PZT Units at 1 kHz. (Intensity variation results from fringe shift in interferometer.)
IV. SUMMARY

The phase detector devised by the Laboratory Operations, The Aerospace Corporation, has been applied to the problem of measuring small displacements for calibrating piezoelectric drivers for tuning laser cavities. The measurements were compared with those obtained from a traditional interferometer technique and found to be superior from the standpoint of signal-to-noise ratio. As a result of this superiority, frequency-response measurements of PZT units were pushed to higher levels with improved precision.
APPENDIX

CALCULATION OF PZT CALIBRATION

For a thickness mode vibration of a PZT unit, the electrical field and displacement or strain are in the same direction (Fig. A-1). The change in thickness $\Delta t$ is, therefore, given by $\Delta t = N d_{33} V$, where $N$ is the number of disks in the PZT stack and $d_{33}$ is the piezoelectric constant in the thickness direction. For PZT-5H, $d_{33} = 593 \times 10^{-12}$ m/V. $V$ is the voltage across each disk. The disks are connected electrically in parallel for PZT units S/N-1 and 2. This relation yields

$$\Delta t = 2(593) \times (10^{-5}) \, \mu m/V$$

$$= 0.00119 \, \mu m/V$$

for the PZ-80 unit, which is similar to a hollow cylinder in which the length changes for electric field applied normal to the cylinder walls (Fig. A-2). The change in length is determined according to

$$d_{31} = \frac{\Delta}{l} \frac{t}{V}$$

where $d_{31}$ is the piezoelectric constant for length change normal to electric field direction, $l$ is the cylinder length, and $t$ is the cylinder wall thickness. From Vernitron Corporation data, $d_{31}$ is between $123$ and $274 \times 10^{-12}$ m/V. The cylinder is 4.44 cm long, with a wall thickness of 0.127 cm. From these values, the displacement is

$$\Delta = 0.0043 \text{ to } 0.0096 \, \mu m/V$$
Fig A-1. Disk-Type PZT Element

Fig. A-2. Cylindrical-Type PZT Element
DISTRIBUTION

Internal

P. J. Ackman
R. M. Allman
J. W. Berkovec
J. M. Bernard
M. Birnbaum
R. A. Chodzko
J. G. Coffer
N. Cohen
E. F. Cross
M. K. Dubas
D. A. Durran
J. W. Ellinwood
M. Epstein
T. L. Felker
R. R. Giedt
D. J. Griep
R. W. F. Gross

K. E. Hagen
D. T. Hodges, Jr.
R. Hofland
M. A. Kwok
A. C. Liang
S. B. Mason
H. Mirels
D. H. Ross
P. L. Smith
D. J. Spencer
E. B. Turner
R. L. Varwig
C. P. Wang
W. R. Warren, Jr.
M. T. Weiss
J. S. Whittier
R. L. Wilkins

External

SAMSO
Attn: Lt. Col. Lindemuth (DYXT)
      Lt. J. C. Garcia (DYXT)
      Lt. Col. H. Shelton (YNAD)
      Mr. G. E. Aichinger (TM)
      Maj. Kosalka (LVO)
      Maj. Simondi (LVO)

AFWL
Kirkland AFB, NM 87117
Attn: Col. J. Rich (AR)
      Lt. Col. A. D. Maio (AL)
      Dr. P. Avizonis (AL)
      Capt. B. Crane (ALC)
      Dr. L. Wilson (ALC)
      Lt. Col. D. Olson (ALC)
      Mr. L. Rapagnani (ALC)

AVCO-Everett Research Laboratory
2385 Revere Beach Parkway
Everett, MA 02149
Attn: Dr. G. W. Sutton
      Dr. J. Daugherty
      Dr. R. Limpaecher

Bell Aerospace Textron
P. O. Box 1
Buffalo, NY 14240
Attn: Dr. W. Solomon/Mail Zone B-49
      Dr. J. W. Raymond/Mail Zone B-49
      Dr. R. J. Driscoll/Mail Zone B-49