Two major research activities were carried out during this grant period. The first was participation in the DUCK94 field experiment to investigate nearbed fluid motions and resulting sediment resuspension in the surf zone. Data were collected over two three-week periods, in August and October 1994, and included concurrent measurements of velocity and suspended sediment profiles at three cross-shore locations and under a variety of wave and current conditions.

The second activity was participation in a controlled wave basin experiment to investigate turbulence generated under breaking waves (galley proof attached). Vertical profiles of turbulence intensity were estimated from velocity fluctuations. Beneath broken waves, turbulence intensity was found to be high throughout the water column and to increase both toward the bed (due to boundary shear) and the sea surface (due to wave breaking). In a simple model using eddy viscosity profiles determined from the turbulence intensities, the surface turbulence generated by wave breaking would cause suspended sediments to be distributed higher into the water column than existing models would predict considering turbulence generated only at the bottom boundary. This redistribution of suspended sediment would have a significant impact on sediment flux in the surf zone.

At present we are analyzing the DUCK94 data set in two ways. First, the eddy viscosity profiles from the wave basin experiment are being used to understand observed suspended sediment profiles and particle flux. Second, cross-shore flux divergence of sediment is being used to explain observed changes in the beach profile (i.e., net deposition and erosion).
From: Director, Office of Naval Research, Seattle Regional Office, 1107 NE 45th St., Suite 350, Seattle, WA 98105

Subj: RETURNED GRANTEE/CONTRACTOR TECHNICAL REPORTS

1. This confirms our conversations of 27 Feb 97 and 11 Jul 97. Enclosed are a number of technical reports which were returned to our agency for lack of clear distribution availability statement. This confirms that all reports are unclassified and are “APPROVED FOR PUBLIC RELEASE” with no restrictions.

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ROBERT J. SILVERMAN
Estimation of Turbulence-Dissipation Rates and Gas-Transfer Velocities in a Surf Pool: Analysis of the Results from WABEX-93

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Abstract

As part of the 1993 Wave Basin Experiment (WABEX-93), water velocities and gas fluxes were measured in a surf pool in Irvine, California, under plunging and spilling waves with heights up to 1.2 m. Vertical profiles of turbulence-dissipation rates were estimated from the velocity measurements made with an Acoustic Doppler Velocimeter (ADV). The ADV measured three components of velocity at a sampling rate of 25 Hz. Turbulence-dissipation rates were estimated from the magnitude of the wavenumber spectra of vertical velocity using the universal form for the inertial subrange. Dissipation rates beneath unbroken waves were found to be low in magnitude and uniform in the vertical. Beneath broken waves, dissipation rates were found to be significantly higher in magnitude throughout the water column and to increase toward the water surface. Near-surface dissipation rates beneath breaking waves were found to follow an exponential dependence on whitecap coverage for all but one wave height condition. This suggests that whitecap coverage can be used to scale increases in dissipation rate for breaking waves. The gas transfer velocity due to turbulence generated by near-surface currents and nonbreaking waves, and the gas transfer velocity due to turbulence generated by breaking waves have been estimated from their respective dissipation rates. These transfer velocities have been used with the bubble-mediated transfer velocity to predict the total gas transfer velocity in the surf pool. Predicted gas transfer velocities agree well with measured gas transfer velocities.

1 Introduction

The flux of gases to or from bodies of water can be estimated as the product of the air-water concentration difference, $\Delta C$, of a gas and its transfer velocity, $k_L$. Because of the difficulties associated with direct oceanic measurements of $k_L$, it is often calculated from parameterizations derived empirically from wind speed. High surface winds generate surface currents and breaking waves, which generate bubbles and affect mixing. As part of an experiment designed to help develop a method for estimating $k_L$ at high wind speed, gas fluxes and turbulence were measured in a large outdoor...
surf pool. A more complete description of the experiment and the gas-flux measurements can be found in Asher et al. [1995] and Wanninkhof et al. [1995].

Results from the gas-exchange measurements suggest that $k_L$ can be partitioned into a component due to near-surface turbulence generated by currents and nonbreaking waves ($k_M$), one due to turbulence generated by breaking waves ($k_T$), and one due to bubble-mediated transfer ($k_B$). For gas evasion with $\Delta C$ much less than zero, $k_L$ can be written in terms of the fractional area of whitecap coverage, $W_C$, as

$$k_L = (k_M + W_C(k_T - k_M)) + W_C k_B$$  \hspace{1cm} (1)

Asher et al. [1995] showed that (1) could be applied to gas transfer measured in the surf pool using an explicit functional form for $k_B$ developed using data collected in a whitecap simulation tank. Although (1) provided reasonable estimates of $k_L$ in the surf pool, it was observed to systematically underpredict $k_L$ when $W_C$ was small. Asher et al. [1995] hypothesized that this discrepancy was caused by incorrectly parameterizing the dependence of $k_M$ and $k_T$ on $W_C$.

Equation 1 was derived by assuming that $k_M$ and $k_T$ were constant and not functions of $W_C$. Because $k_M$ and $k_T$ are determined by the vertical structure and intensity of the near-surface aqueous-phase turbulence, they are constant only if the turbulence in the surf pool is constant as $W_C$ changes. However, it is reasonable to expect that the turbulence associated with breaking waves increases with wave height and that the background turbulence levels in the surf pool will increase with increasing wave energy. The present study confirms that the turbulence-dissipation rate increases with wave height. Furthermore, the increase in dissipation rate can be scaled using the whitecap coverage of the breaking waves, and inclusion of turbulence-dissipation rates in estimating $k_M$ and $k_T$ improves the ability of (1) to predict gas transfer velocities.

2 Experiment

As part of the 1993 Wave Basin Experiment (WABEX-93), estimates of turbulence-dissipation rates were made in the Hurricane Harbor surf pool at Wild Rivers Waterpark in Irvine, California, under breaking waves with heights up to 1.2 m (see Asher et al. [1995] for details of the surf pool and wave generation). The objective of the measurements described here was to obtain velocity profiles and pressure measurements at multiple locations in the surf pool with resolution sufficient to estimate profiles of turbulence-dissipation rate.

Turbulence-dissipation rates were estimated from velocity measurements made with a SonTek acoustic-doppler velocimeter (ADV). The ADV measured
three components of velocity in a 0.5-cm$^3$ sampling volume located 10 cm below the probe, minimizing the effect of the sensor on the flow field. Measurements were recorded at 25 Hz for runs lasting approximately 300 s (70-100 waves). Because the wave field was highly repeatable, profiles were made by compositing data from three to seven runs, each with the instrument mounted at the same horizontal location but at a different elevation. Profiles were obtained at three locations across the surf zone under spilling and plunging waves generated at four energy levels by the wavemaker, with nominal unbroken wave heights of 0.3, 0.6, 0.9 and 1.2 m. Figure 1 is a schematic drawing of Hurricane Harbor showing the three ADV measurement locations, denoted A, B, and C. Simultaneous measurements of pressure were made with a precision strain-gage located on the bottom directly beneath the ADV. When ADV measurements were made very close (<15 cm) to the bottom the pressure transducer was located ~30 cm to the side. Video images of the water surface were recorded and later used to determine wave type and breaker location.

3 Data Analysis

Flow beneath waves can be separated into three components: mean, periodic (wave), and fluctuating (turbulence) components. The objective of the data analysis was to quantify the turbulence component. Several approaches were considered. In laboratory studies with highly repeatable waves, all velocity deviations from the ensemble-mean wave velocity can be attributed to turbulence (Nadaoka et al. [1983]). Although waves in the surf pool ap-
peared quite regular, the detailed pressure measurements showed wave-to-wave variations in pressure. Irregularity in the wave field was most likely caused by the combined effects of variability in the wavemaker, seiching of the pool, reflected waves, and episodic outbreaks of a rip current. Estimates of turbulence based on deviations from the ensemble-mean velocity were precluded because they would overestimate turbulence by including non-turbulent, pressure-induced fluctuations. An alternative approach for extracting turbulence from velocity records involves the portion of the records associated with wave-induced variations of the water-surface (Kitaigorodskii et al. [1983], Agrawal and Aubrey [1992]). This frequency-domain method assumes that velocity variations that are coherent with pressure fluctuations are caused by two-dimensional progressive waves, and that noncoherent velocity fluctuations can be attributed to turbulence. However, the technique is prone to error if waves have directional spread (Herbers and Guza [1993]). We instead used the inertial dissipation method of George et al. [1994], modified to take advantage of the nearly regular wave field and the measurement capabilities of the ADV.

3.1 Data Processing

One advantage of the ADV was its ability to rapidly re-establish good velocity measurements after the loss of acoustic signals in bubble plumes or during subaerial exposure in the trough of a wave. Initial processing identified and rejected data from times when the ADV was exposed or large amounts of bubbles were present. A preliminary criterion for rejection was based on the correlation coefficient between the transmitted acoustic signal and the received backscattered signal. Data-rejection rates increased from near zero at depth to as much as 37% near the surface under larger waves. Acceptable data for 70 to 100 successive waves were phase aligned using the peak in the cross covariance of the slope of the pressure signal, and ensemble means and standard deviations for three velocity components and pressure were estimated (Figure 2). An iterative check on data was then performed: data were rejected if the velocity magnitude exceeded 3.7 standard deviations about the ensemble mean at each phase in the wave, and ensemble statistics were recalculated. Finally, mean and root-mean-square (RMS) velocities were determined for acceptable data from each data run.

3.2 Estimates of Dissipation Rates

In steady flow with isotropic, fully-developed turbulence, kinetic energy is transferred from the mean flow to large eddies, then to small eddies, and is finally dissipated by viscosity. Under these conditions, the turbulence-dissipation rate can be estimated by the magnitude of the wavenumber spectra in the inertial subrange, which takes the form:
where $k$ is wavenumber, $E(k)$ is wavenumber spectral density, $\varepsilon$ is the turbulence dissipation rate, and $\alpha$ is the Kolmogorov constant. The inertial subrange extends from large eddies, the scale of which is typically determined by physical dimensions of the flow (e.g., depth) to the Kolmogorov microscale, which is determined by kinematic viscosity and dissipation rate.

Estimates of dissipation rate were made for the surf pool data using (2), and assume that the turbulence was fully developed and isotropic. The vertical component of the ADV velocity signal was used to calculate dissipation rates because it had the highest signal-to-noise ratio of the three components. Spectral estimates were obtained using a windowing and ensemble-averaging (Welch) method. Because data were removed during initial processing, the spectra for each windowed time series was computed using a method appropriate for irregularly spaced data (Press et al. [1992]). Entire data windows were omitted if more than 50% of the data points were missing. Spectral estimates were obtained by first detrending the data by subtracting out the ensemble-mean periodic (wave) velocity component, then computing spectra on a windowed data segment extending over three successive waves, and finally ensemble-averaging the spectra. Windowed segments were overlapped 67%. This procedure yielded spectral estimates with resolved bandwidths of 0.16 Hz and 156 degrees of freedom for typical time series containing 80 waves.

The time-series data at a fixed point were used to estimate the energy-density spectrum as a function of frequency, not wavenumber. The frequency spectra were converted to wavenumber spectra using Taylor's hypothesis of frozen turbulence, assuming that the time scale of turbulent fluctuations was long compared with the time scale of the motion advecting the eddy past the sampling point. The RMS orbital velocity was used as the advective velocity for the conversion from measured frequency spectra to wavenumber spectra (Agrawal et al. [1992]). An example of the wavenumber spectra generated from the vertical velocity data is shown in Figure 3.

Turbulence-dissipation rates ($\varepsilon$) were estimated from the magnitude of the wavenumber spectra in the inertial subrange using (2). For each data run, the wavenumber spectra were individually inspected and the magnitude of the spectra in the range over which the theoretical $-5/3$ slope was found was used to estimate the dissipation rate (typically between radian wavenumbers of 0.4 and 1.5 cm$^{-1}$).

4 Turbulence Dissipation Results

Profiles of $\varepsilon$ beneath plunging waves are shown in Figures 4a and 4b, and beneath spilling waves in 4c. Elevation is normalized by the water depth,
Figure 2: Ensemble-average velocities and pressure under plunging wave of nominal height 0.9 m at location A, 53 cm ab: a Alongshore velocity. b Cross-shore velocity. c Vertical velocity. d Pressure.

so that a normalized elevation of 1.0 is at the mean water surface. Under unbroken waves, ε profiles were generally low in magnitude and vertically uniform. Beneath plunging waves measured at location A (Figure 4a), ε was highest near the surface and increased with increasing wave height. Dissipation rates were also seen to increase with increasing wave height throughout the water column.

Profiles of ε at location B (Figure 4b) are similar to profiles at location A (Figure 4a), although the mid-water column ε are higher at B, and there is at B little difference in ε between the 0.9-m and 1.2-m wave conditions. Strong rip currents at B could be responsible for the increase in the ε for the mid-water column compared with A. Alternatively, the increased distance from breaking (cross-shore location) at B could have allowed homogenization of turbulence through the water column. Similar values of ε for wave heights
of 0.9 m and 1.2 m could indicate a saturation value for $\varepsilon$ at some distance from the break point. At B, velocity measurements were made very close to the pool bottom, and observed increases in $\varepsilon$ are likely associated with shear-induced turbulence in the bottom boundary layer (Figure 4b).

Beneath spilling waves at location C (Figure 4c), profiles of $\varepsilon$ show more variation, possibly because spilling waves were less regular. Like $\varepsilon$ measured beneath plunging waves at B, $\varepsilon$ was high in the middle of the water column but, in contrast to measurements of $\varepsilon$ at B, $\varepsilon$ measured beneath spilling waves at C did not appear to reach saturation near the surface.

4.1 Characteristic Dissipation Rates

Dissipation rates from two depths were used to characterize turbulence generated by breaking waves ($\varepsilon_T$), and background mechanical turbulence generated by currents and nonbreaking waves ($\varepsilon_M$). The $\varepsilon_T$ was taken to be the $\varepsilon$ interpolated at a normalized elevation of 0.8 for the plunging waves, and 0.65 for the spilling waves (upper limit of measurements). These depths are consistent with the assumption that the dominant length scale for turbulence generated by wave breaking is proportional to the breaking wave amplitude. It was assumed that the characteristic $\varepsilon_T$ and $\varepsilon_M$ for gas exchange in the entire surf pool were less than $\varepsilon_T$ and $\varepsilon_M$ at location A and greater than $\varepsilon_T$ and $\varepsilon_M$ at location B beneath plunging waves, and that the characteristic
\(\varepsilon_T\) and \(\varepsilon_M\) were approximately equal to \(\varepsilon_T\) and \(\varepsilon_M\) at location C beneath the spilling waves. Values for \(\varepsilon_T\) are listed in Table 1 for the two wave types and four wave heights. The dissipation rate for turbulence generated by non-breaking waves and currents, \(\varepsilon_M\), was determined at a normalized elevation of 0.2 (Table 1). This level was generally below the region of large gradients in the \(\varepsilon\) profiles. Turbulence generated in the bottom boundary layer was observed below this level (Figure 4b), but does not appear to influence \(\varepsilon\) above normalized elevations of 0.1.

4.2 Dissipation Rates and Whitecap Coverage

The area-weighted fractional coverage of actively breaking waves, \(W_C\), was measured in the pool (Asher et al. [1995]), and values are listed in Table

Figure 4: Vertical profiles of turbulence-dissipation rate, \(\varepsilon\), beneath a plunging waves at location A, b plunging waves at location B, and c spilling waves at location C, of nominal waveheights 0.3, 0.6, 0.9, 1.2 m.
Table 1: Turbulence-dissipation rates and whitecap coverage

<table>
<thead>
<tr>
<th>Wave Type</th>
<th>Nominal Height</th>
<th>$\varepsilon_M$ (cm$^2$/s$^3$)</th>
<th>$\varepsilon_T$ (cm$^2$/s$^3$)</th>
<th>$W_C$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Plunging</td>
<td>1.2 m</td>
<td>75</td>
<td>499</td>
<td>7.15</td>
</tr>
<tr>
<td>Plunging</td>
<td>0.9 m</td>
<td>45</td>
<td>299</td>
<td>3.96</td>
</tr>
<tr>
<td>Plunging</td>
<td>0.6 m</td>
<td>2</td>
<td>66</td>
<td>2.01</td>
</tr>
<tr>
<td>Plunging</td>
<td>0.3 m</td>
<td>0.6</td>
<td>0.8</td>
<td>0.00</td>
</tr>
<tr>
<td>Spilling</td>
<td>1.2 m</td>
<td>65</td>
<td>428</td>
<td>2.90</td>
</tr>
<tr>
<td>Spilling</td>
<td>0.9 m</td>
<td>21</td>
<td>152</td>
<td>2.51</td>
</tr>
<tr>
<td>Spilling</td>
<td>0.6 m</td>
<td>5</td>
<td>6</td>
<td>0.54</td>
</tr>
<tr>
<td>Spilling</td>
<td>0.3 m</td>
<td>1</td>
<td>2</td>
<td>0.00</td>
</tr>
</tbody>
</table>

1. Figure 5 is a log-normal plot of $\varepsilon_T$ versus $W_C$ from the data in Table 1. $\varepsilon$ for spilling waves at all four heights and $\varepsilon_T$ for breaking waves with heights of 0.3 m, 0.6 m, and 0.9 m were found to follow the same exponential dependence on $W_C$. This suggests that $W_C$ can be used to scale increases in $\varepsilon_T$ caused by breaking waves. It is not clear why $\varepsilon_T$ for the 1.2-m plunging breaking waves does not follow the same dependence as the other seven wave conditions, but it should be noted that these conditions presented the most difficult data-analysis problems, and many data points during the times of high velocities were eliminated. As a result, maximum dissipation rates could have been underestimated.

5 Parameterization of Gas Transfer Velocities

Lamont and Scott [1970] showed that for gas exchange across an unbroken water surface, $k_L$ could be estimated using $\varepsilon$. Using their relation, $k_M$ and $k_T$ can be written as

$$k_X = B S c^{-1/2} (\varepsilon_X v)^{1/4} (X = M, T)$$ (3)

where $B$ is a dimensionless constant, $S c$ is the Schmidt number of the gas (equal to the ratio of kinematic viscosity to molecular diffusivity), $v$ is the kinematic viscosity of water, and $\varepsilon_M$ and $\varepsilon_T$ are the dissipation rates of the wave-current-generated turbulence and the breaking-generated turbulence, respectively. In support of (3), Asher and Pankow [1986] found that $k_L$ for transfer of carbon dioxide (CO$_2$) through a cleaned water surface scaled linearly with $\varepsilon^{1/4}$. They also found that $B$ was equal to 0.65.

Asher et al. [1995] measured $k_L$ for CO$_2$, helium (He), nitrous oxide (N$_2$O), and sulfur hexafluoride (SF$_6$) as a function of $W_C$ in the surf pool. They developed an empirical parameterization of $k_L$ using (1) by assuming $k_M$ and $k_T$ were constant with increasing $W_C$ and taking $k_B = b_1\alpha^{-0.042} S c^{-0.35}$. As
can be seen in Figure 5 however, $\varepsilon_M$ and $\varepsilon_T$ were not constant with increasing $W_C$, and (3) shows $k_M$ and $k_T$ will also increase. Therefore, it is not surprising that Asher et al. [1995] found that parameterizing $k_L$ using (1) and assuming that $k_M$ and $k_T$ were constant was unsatisfactory.

The dissipation rates listed in Table 1 were used to calculate $k_M$ and $k_T$ using (3) and assuming $B$ would be a constant fit by the data. These transfer velocities were substituted into (1) to account for the effect of the increase in turbulence with increasing $W_C$. Written explicitly, $k_L$ in the wave basin can be parameterized as

$$k_L = B(\varepsilon_M \nu)^{1/4} + W_C \left( (\varepsilon_T \nu)^{1/4} - (\varepsilon_M \nu)^{1/4} \right) S_C^{1/2} + b_1 W_C \alpha^{-0.643} S_C^{-0.35} \quad (4)$$

The resulting model was then fit using least-squares linear regression to the measured $k_L$ data from Asher et al. [1995] to determine the coefficients $b_1$ and $B$ in (4). This fit results in $B = 0.58$ and $b_1 = 6.30$ m s$^{-1}$ with a coefficient of determination of 0.84. The value of $B$ found for the WABEX-93 data is in good agreement with that determined by Asher and Pankow [1986].

Figure 6 shows the result of fitting (4) to the surf pool data by plotting $k_L$ for CO$_2$, He, N$_2$O, and SF$_6$ calculated using (4) versus the experimentally determined value. There is excellent agreement between the calculated and measured $k_L$ values. Asher et al. [1995] found a reduced chi-squared ($\chi^2$) of
192 for the constant $k_M$ and $k_T$ parameterization. The $\chi^2$ for the data in Figure 6 was 70, which shows that including the effects of increasing turbulence with increasing $W_C$ improves the predictive accuracy of a parameterization based on (1).

The parameterization given in (4) can also be used to estimate the fraction of $k_L$ that is due to turbulence and the fraction of $k_L$ that results from bubble-mediated processes. For SF$_6$ for a 0.9-m spilling wave, turbulence processes accounted for 38% of the total transfer velocity and bubble processes were 62% of the total. In contrast, the turbulence fraction for CO$_2$ under the same conditions was 46% and the bubble fraction was 54%. The decreased importance of bubble-mediated transfer for CO$_2$ compared with SF$_6$ agrees with the model predictions of Memery and Merlivat [1985]. Their results indicated that $k_B$ for a soluble gas such as CO$_2$ would be less than $k_B$ for an insoluble gas like SF$_6$.

6 Conclusion

Turbulence dissipation rates were found to increase with increasing wave height for spilling and plunging waves. The surface dissipation rates scaled as an exponential function of whitecap coverage for spilling waves with nominal heights of 0.3 m, 0.6 m, 0.9 m, and 1.2 m and for plunging waves with nominal heights of 0.3 m, 0.6 m and 0.9 m. For reasons that are not clear at present, the surface dissipation rate for plunging waves with a height of 1.2 m did not follow this exponential scaling.

Asher et al. [1995] found that parameterizing $k_L$ for CO$_2$, He, N$_2$O, and SF$_6$ assuming $k_M$ and $k_T$ were constants did not provide a satisfactory fit with the measured surf pool data ($\chi^2 = 192$). Substitution of the direct estimates of $k_M$ and $k_T$ from (3) and dissipation rates estimated from the surf pool measurements improved the agreement between measured and predicted $k_L$ values ($\chi^2 = 70$).

In the surf pool, increases in $W_C$ were caused by increases in height of the breaking wave. It could be expected that a similar process occurs under oceanic conditions, where increasing wind speed leads to larger wave size and higher whitecap coverage. The success of the approach described here suggests that successful application of (1) to ocean conditions will require knowledge of $k_B$ and the dependence of $k_M$ and $k_T$ on wind speed. Although this complicates the parameterization of $k_L$ in the ocean, it will provide an accurate estimation of the effect of the turbulence and bubbles generated by breaking waves on air-sea gas fluxes.

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