Acoustic Measurement of the Mechanical Properties of Thin Material Specimens

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**Title:** Acoustic Measurement of the Mechanical Properties of Thin Material Specimens

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**Abstract:**
An acoustic technique is presented which permits accurate measurement of the dynamic Poisson's ratio, and the Young's, shear, and bulk moduli for a specimen which exists as a thin (<10 mil) layer. This technique should prove especially useful in situations where a bulk specimen is either not readily available or would not properly reflect the properties of the material when configured as a thin layer. The report includes a detailed discussion of the theory underlying the technique. As a test, three materials which could be easily formed into both a thin specimen and a thick specimen were selected. The technique was then used to determine the Poisson's ratio and acoustic velocities of the material constituting each thin specimen. These values were then contrasted to those of the bulk specimens obtained in a more conventional manner. The technique, as presented, could be extended for a number of applications, including the cure monitoring of adhesives.
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I. INTRODUCTION

The Poisson's ratio for a material can be determined from the ratio of the acoustic shear velocity to the longitudinal velocity. These velocities can often be easily measured using conventional ultrasonic time-of-flight techniques. Over the years, however, difficulties associated with making velocity measurements on thin attenuative specimens have forced ultrasonic researchers to become more innovative. For example, in an early effort to measure the velocity of both transverse and longitudinal waves in a buna-N vulcanizate as a function of temperature, Nolle and Sieck (Ref. 1) employed a method involving the use of solid transmission media to conduct pulses into a thin, flat specimen. The error associated with the acoustic measurement, however, was estimated in the report to be as high as 5% and 10% for the longitudinal and shear wave data, respectively. Cunningham and Ivey (Ref. 2) improved upon the aforementioned technique by incorporating a double acoustic path comprised of two separate specimens. Again, however, a number of experimental difficulties (e.g., producing uniform sample bond lines) contributed to significant measurement error. More recently, Kinra and Dayal (Ref. 3) report combining standard fast Fourier transform (FFT) methods with conventional ultrasonics to measure the longitudinal phase velocity in specimens of submillimeter thicknesses. Their report includes a brief summary and comparison of their technique to techniques recently developed by others, including the resonance method of Chang et al. (Ref. 4) and the phase insensitive tone-burst spectroscopic method of Heyman (Ref. 5).

This report presents a simple ultrasonic resonance technique which permits measurement of the Poisson's ratio of thin adhesive material specimens. The acoustic shear and longitudinal velocity are also determined. This technique is characterized by a number of advantages. For example, the Poisson's ratio measurement accuracy is limited only by that of the resonant frequency; the Poisson's ratio is independent of the thickness of the specimen. Also, the same specimen and transducer pair are used to determine both the shear and longitudinal response. In addition, a fluid medium is employed to couple sound into the specimen, thereby eliminating many of the problems associated with the bonding of transducers.
II. THEORY

The treatment which follows will be directed toward making Poisson's ratio measurements on thin (several mils thick) material specimens. The Poisson's ratio for a material can be determined through measurement of its acoustic velocities using the relation:

$$\sigma = \frac{c_1^2 - 2c_s^2}{2c_1^2 - 2c_s^2},$$

where $\sigma$ is the Poisson's ratio, and $c_1$ and $c_s$ are the longitudinal and shear acoustic velocities, respectively.

Consider first the semi-infinite medium (labeled Medium 1), with acoustic impedance $Z_1$, as depicted in Figure 1. If a thin layer of a second medium, Medium 2, with acoustic impedance $Z_2$, is placed in contact with the left side of Medium 1, the input impedance of the composite system (Medium 1 + Medium 2) is given by the complex relation:

$$Z_{21} = \frac{Z_2Z_1 \cos (x_2\beta_2) + j Z^2_2 \sin (x_2\beta_2)}{Z_2 \cos (x_2\beta_2) + j Z_1 \sin (x_2\beta_2)}$$

where $j$ is the imaginary index and for Medium 2, $x_2$ is the thickness, $\beta_2 = 2\pi/\lambda_2$ is the propagation constant, and $\lambda_2$ is the acoustic wavelength (Ref. 6). Note that in the derivation of Eq. (2), a steady state condition (continuous plane wave stimulation of the system of frequency, $f$) was assumed. Wavelength is related to frequency according to the relation, $c = \lambda_2 f$, where $c$ is the acoustic velocity (either shear or longitudinal) in Medium 2.

Next, consider what happens when a third (semi-infinite) medium, Medium 3, is placed in contact with the left side of Medium 2, as is also depicted in Figure 1. If this medium has the same acoustic impedance as that of Medium 1, then the stress wave reflection coefficient $R$ is given by the relation:

$$R = \frac{Z_{41} - Z_1}{Z_{41} + Z_1} = \frac{Z_2Z_1 \cos (x_2\beta_2) + j Z^2_2 \sin (x_2\beta_2) - Z_1(Z_2 \cos (x_2\beta_2) + j Z_1 \sin (x_2\beta_2))}{Z_2Z_1 \cos (x_2\beta_2) + j Z^2_2 \sin (x_2\beta_2) + Z_1(Z_2 \cos (x_2\beta_2) + j Z_1 \sin (x_2\beta_2))}$$
Figure 1. A thin medium of acoustic impedance $Z_2$, sandwiched between two semi-infinite media. Medium 3 sees the composite system formed by Medium 1 and Medium 2 as having an input acoustic impedance of $Z_{21}$. 
The coefficient of acoustic power transfer $P_T$ across Medium 2 can now be calculated:

$$P_T = 1 - |R|^2 = \frac{4 \frac{Z_2^2}{Z_1^2}}{(Z_1^2 + Z_2^2)^2 \sin^2 \left(\frac{2\pi x f}{c}\right) + 4 \frac{Z_2^2}{Z_1^2} \cos^2 \left(\frac{2\pi x f}{c}\right)},$$

where the substitution $\beta_2 = 2\pi c/f$ has been applied.

In Figure 2, $P_T$ is plotted as a function of frequency for the case where Media 1 and 3 are aluminum ($Z_1 = 17$ rayls) and Medium 2 is water ($Z_2 = 1.48$ rayls). It can be seen that the condition of maximum power transmission occurs when $f = f_{rl} = nc/2x_2$, where $n$ is an integer. This behavior can be expected whenever $Z_2$ is higher than both $Z_1$ and $Z_3$ or lower than both $Z_1$ and $Z_3$ (as in this case). If $Z_2$ falls midrange between $Z_1$ and $Z_3$, maximum power transmission occurs when $f = f_{rl} = (n+1)c/4x_2$. Note that Medium 2 was assumed to be lossless in the derivation of Eq. (4). Taking attenuation into account, one would expect the amplitude of the local maxima to decrease with increasing $n$. The expression for Poisson's ratio [Eq. (1)] can now be rewritten as

$$\sigma = \frac{f_{rl}^2 - 2f_{rs}^2}{2f_{rl}^2 - 2f_{rs}^2},$$

where $f_{rs} \propto c_2/2x_2$ and $f_{rl} \propto c_1/2x_2$ are determined from the condition of maximum power transmission for shear and longitudinal acoustic waves, respectively.
Figure 2. The coefficient of acoustic power transmission across Medium 2 as a function of frequency [Eq. (4)] for the three-layer system depicted in Figure 1, where $Z_1 = Z_3 = 17$ rayls (Al) and $Z_2 = 1.48$ rayls ($H_2O$).
III. TECHNIQUE

The experimental apparatus is depicted in Figure 3. Two aluminum blocks were cut from square rod stock, each having a 74° and 90° face with respect to one side of the block. A milled finish was determined to be adequate on the 74° faces. The 90° faces were lapped to ensure that the surfaces were flat. A thin, uniform layer of the specimen being tested was sandwiched between the 90° faces. The spacing between these faces and, hence, the specimen thickness, was determined by two identical stainless steel wire spacers. To hold this Al/specimen/Al sandwich together, a small rubber O-ring was stretched over a set of threaded pegs located on each of two opposite sides of the sandwich as shown. The depth of thread for these pegs was less than 0.125 inch. The resultant Al/specimen/Al sandwich was set upon a fixture (not included in Figure 3 for clarity) and submerged in a water tank in order to be centered between a pair of 5 MHz plane wave, through-transmission ultrasonic transducers. The fixture was designed to permit rotation of the specimen with respect to the transducers. The apparatus is designed to approximate the conditions leading to the derivation of Eq. (4). The Al blocks correspond to Media 1 and 3, the specimen to Medium 2.

To perform measurements, one transducer was stimulated to propagate a tone-burst (single frequency) longitudinal drive pulse (water will not support a shear wave). The fixture was aligned so that this pulse would strike the first 74° face of the Al/specimen/Al sandwich at a particular angle of incidence \( \theta_i \) to its normal, giving rise to both a longitudinal and a shear wave pulse within the aluminum, with angles of emergence \( \theta_l \) and \( \theta_s \), respectively. The emergence angles for a particular \( \theta_i \) can be determined by the well-known Snell's law analog,

\[
\frac{\sin \theta_i}{V_s} = \frac{V_w}{\sin \theta_s} \quad \text{and} \quad \frac{\sin \theta_i}{V_1} = \frac{V_w}{\sin \theta_1} .
\]

where \( V_w \) is the acoustic velocity in water, and \( V_s \) and \( V_1 \) are the acoustic velocities for shear and longitudinal waves in aluminum, respectively.

In the first phase of the experiment, \( \theta_i \) was set at \( \sim 3.7^\circ \), so that the longitudinal pulse transmitted through the first 74° face would strike the Al/specimen interface at normal incidence. This pulse would then travel through the remainder of the Al/specimen/Al sandwich to produce a
Figure 3. The experimental apparatus as described in the text. As indicated, this is a top view. The Al/specimen/Al sandwich extends 1.5 inches into the page. The transducers and O-ring are bisected by a plane parallel to that of the page and 0.75 inch into the page.
signal at the receive transducer, as depicted in Figure 4a. This signal will be referred to as the longitudinal response. Because the longitudinal velocity in Al exceeds that of the shear, the longitudinal response was the first signal detected after each drive pulse. This first signal was followed by others due to the shear wave transmitted through the first 74° face and various internal reflections within the sandwich. The duration of the drive pulse was chosen to be ~1.5 μs, which was short enough to permit temporal separation of the various signals, yet long enough to allow reverberations within the thin specimen layer to approximate a steady state (i.e., these reverberations did not significantly affect the lengths of the pulses). The amplitude of the longitudinal response was measured as a function of frequency (between 2 and 8 MHz). To isolate the effect of the specimen, the Al/specimen/Al sandwich was then replaced with a solid Al block of the same dimensions, and the measurement was repeated. This second set of data was divided into the first set. The resultant data set was then normalized and plotted. Peaks in the amplitude vs. frequency plot—which, in accordance with Eq. (4), occur when \( f = f_{\text{rl}} = nc/2x \)—were then used to determine \( c_l \), the longitudinal acoustic velocity of the specimen.

In the second phase of the experiment, \( \theta_1 \) was set to ~7.5°, so that the direction of the transmitted shear wave was normal to the Al/specimen interface, as depicted in Figure 4b. The first signal resulting from this normal shear pulse will be referred to as the shear response. Following each drive pulse, the shear response was preceded by not only the longitudinal response, but also by other signals resulting from internal reflections involving the faster longitudinal pulse. To positively identify the shear response, one could increase \( \theta_i \) beyond the critical angle for longitudinal wave production in the aluminum, so that the shear response would be the first remaining signal. One could then track this signal while decreasing \( \theta_1 \) to the appropriate value. The frequency dependence of the shear response amplitude was then measured, normalized, and plotted in the same manner as that of the longitudinal response amplitude. Peaks in this plot, occurring when \( f = f_{\text{rs}} = nc/2x \), were then used to determine the shear acoustic velocity of the specimen, \( c_s \).
Figure 4. Ray diagrams for the apparatus depicted in Figure 3. The specimen thickness has been enlarged for clarity. In (a), to measure $c_1$, a pulse is emitted with a wavevector at $3.7^\circ$ to the normal for the $74^\circ$ face. Mode conversion at the surface results in a longitudinal wave pulse (denoted by L) which traverses the Al/specimen/Al sandwich in a direction normal to the Al/specimen interface. This is the first signal to reach the receive transducer. A slower shear wave pulse (denoted by S) is also generated. As indicated, this pulse gives rise to a number of additional pulses (both shear and longitudinal). Care must be taken to identify the signal of interest. To generate a shear wave pulse normal to the Al/specimen interface, the configuration displayed in (b) was used.
IV. RESULTS

Before both $c_s$ and $c_l$ were measured in a material, a simpler system having no shear response was tested. An $\text{Al/H}_2\text{O}/\text{Al}$ sandwich with wire spacers that had a diameter of $x_2 = 1.016 \times 10^{-4}$ m (4 mils) was prepared. It should be emphasized that in this case (and all cases that follow), the 90° faces on the Al blocks were lapped flat with 600 grit garnet. Earlier tests, using blocks which had not been lapped, yielded results which were not satisfactory. In Figure 5, the frequency response of the $\text{Al/H}_2\text{O}/\text{Al}$ sandwich and a solid Al standard are plotted as boxes and circles, respectively. The second plot was divided into the first plot and normalized to produce the solid curve. The importance of this correction (for the transducer response and attenuation in the Al) is obvious. The peak in the solid curve, at $f_R = 7.3$ MHz, was used to calculate $c_l = 2f_R x_2 = 1483$ m/s for water, in excellent agreement with the literature value.

Three materials—Black Wax (BW), Five Minute Epoxy (FME), and Crystalbond (CB) adhesive—were selected for measurement of both $c_s$ and $c_l$. These materials were easily obtained and could be easily formed into both a thin specimen, as needed for this experiment, and a thick specimen, for comparative purposes. The longitudinal response and shear response data for the thin Black Wax specimen are plotted in Figure 6. The raw data were corrected, as outlined above, to produce these curves. The wire spacers used for the Al/BW/Al sandwich had a diameter of $2.39 \times 10^{-4}$ m (9.4 mils). The longitudinal response exhibits a peak at 4.8 MHz, corresponding to a longitudinal velocity of 2290 m/s. The shear response curve exhibits four equally spaced peaks, corresponding to $n = 1, 2, 3, \text{and } 4$ in the relation; $f_{s_n} = n c_s/2x_2$. As expected, the amplitude of these peaks decreases with increasing $n$, due to attenuation within the black wax. Note that the data become less reliable as one pushes the limits on the operating range of the transducer (see the circle plot of Figure 5). The positions of the shear peaks correspond to a shear velocity of $c_s = 1120$ m/s. As mentioned earlier, a thick specimen of black wax was also prepared with the approximate dimensions of $2.5 \times 2.5 \times 0.66$ cm. The longitudinal and shear velocities of this specimen were measured using a standard through-transmission, ultrasonic technique. Table 1 compares the values thus obtained to those for the thin specimen, along with similar results which were obtained for
Crystalbond adhesive and Five Minute Epoxy. The entries for Poisson's ratio were calculated using Eq. (5).
Figure 5. Sample data for an Al/H₂O/Al sandwich. The wire spacers for this sandwich had a diameter of $x_2 = 1.016 \times 10^{-4}$ m (4 mils). The circles result from a measurement of the frequency response of a solid aluminum standard of the same dimensions as the sandwich. Dividing the data from the standard into the raw Al/H₂O/Al data (boxes) corrects for both the attenuation due to the aluminum and the transducer response, thereby isolating the effect of the H₂O layer. The resulting solid curve exhibits a peak at 7.3 MHz, which can be used to calculate $c_1 = 2f_r x_2 = 1483$ m/s for water, in close agreement with the book value, 1483 m/s (Ref. 6).
Figure 6. Data for black mounting wax. The wire spacer had a diameter of $2.39 \times 10^4$ m (9.4 mils).
Table 1. Comparison of Velocities Measured for Thin and Thick Specimens

<table>
<thead>
<tr>
<th>Sample</th>
<th>$c_l$ (10^5 cm/s)</th>
<th>$c_t$ (10^5 cm/s)</th>
<th>$\sigma$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Thin</td>
<td>Thick</td>
<td>Thin</td>
</tr>
<tr>
<td>BW$^a$</td>
<td>2.29</td>
<td>2.23</td>
<td>1.12</td>
</tr>
<tr>
<td>CB$^b$</td>
<td>2.33</td>
<td>2.3</td>
<td>1.12</td>
</tr>
<tr>
<td>FME$^c$</td>
<td>2.7</td>
<td>2.7</td>
<td>1.25</td>
</tr>
</tbody>
</table>

$^a$Black wax.
$^b$Crystalbond adhesive.
$^c$Five Minute Epoxy.
V. DISCUSSION

It can be observed that for the three materials tested, the resonance technique for thin specimens described in this report leads to values for $c_1$, $c_2$, and $\sigma$ which compare well with values determined using thicker specimens and a conventional through-transmission ultrasonic method (Table 1). The two techniques yield values that differ by only a few percent. This difference falls within the uncertainty ascribed to the conventional measurement. When used to measure the acoustic velocity of water, the resonance technique yielded a value essentially equivalent to that reported in the literature. Sources of error for the resonance technique include error in determination of the resonant frequency, wire thickness, and sample alignment, or nonuniformities in the specimen thickness, which lead to a broadening of the resonance. The resonant frequency can be determined more accurately by sampling with a finer frequency increment. Problems with specimen alignment can be mitigated through a well-designed apparatus and careful experimentation. The wire thickness is important for determination of the velocities but drops out of the equation for the Poisson's ratio.

The resonance technique presented should prove particularly useful for measurement of the mechanical properties of materials which exist (perhaps only) as thin (subwavelength) layers, such as adhesives or highly attenuative materials. The use of a fluid couplant medium provides for uniform and repeatable coupling of the sound into the specimen. The capability for measuring both velocities on a single sample becomes especially useful when multicomponent polymer systems are being tested, because of the variations within and between batches. In addition to the Poisson's ratio and acoustic velocities, if the density, $\rho$, of the specimen is known, the Young's, shear, and bulk moduli, $E$, $\mu$, and $K$, can also be calculated via the familiar relations,

$$E = \frac{\rho c_1^2(1 - 2\sigma)(1 + \sigma)}{1 - \sigma}, \quad \mu = \rho c_s^2 \quad \text{and} \quad K = \frac{E}{3(1 - 2\sigma)}.$$  \hspace{1cm} (7)

It is implicit that the properties measured are dynamic. In many instances, however, the temperature of the specimen and/or the frequency of measurement can be arranged so that the measurement occurs well above or below the glass transition.

In addition to the aforementioned applications, a number of enhancements and/or extensions of the technique can be envisioned. Instead of using a tone-burst signal and
sweeping the frequency, one might instead use a broadband pulse and Fourier transform the received signal. One could then effectively get all the information from a single pulse. The technique could also be arranged to study or monitor the cure of adhesives.
REFERENCES


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