THE DISTANCE DEPENDENCE OF REGIONAL PHASE DISCRIMINANTS

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## The Distance Dependence of Regional Phase Discriminants

A number of proposed discriminants for distinguishing the character of seismic sources use the amplitude of the phase Pn as a reference. The merit of Pn is that it constitutes the onset of regional seismograms, but the behaviour of the arrivals at an individual station can be quite complex. Results from long-range refraction experiments in Eurasia suggest that the complexity arises from the superposition of a number of sub-phases returned from fine-scale structure in the uppermost mantle. The behaviour is consistent with fine scale horizontal variations superimposed on a gentle increase in seismic velocity with depth, so that equivalent one-dimensional models will show multiple low velocity zones. Long range refraction data for Sn is much less common but similar trends can be discerned. As frequency increases such complexity is likely to become more important. Sn is often observed at distances beyond 300 km but emerges from Sg(Lg) much less clearly in general than Pn emerges from Pg. However some refraction profiles in the Finnish Shield areas show very clear Sn arrivals at short distances. The differences in character can be associated with differing velocity gradients for S in the uppermost mantle. The variability in Sn behaviour means that it may prove difficult to generate discriminants based on e.g. Pn/Sn amplitude which can be readily transportable between different regions.
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INTRODUCTION

A number of the techniques which have been proposed for discriminating between different types of seismic sources at regional distances depend on the relative amplitudes of different P and S phases. Although the phase denoted in discrimination work as Lg is frequently the largest phase on a regional seismogram, it is known to be sensitive to variations in crustal structure. As a result attention has been transferred to Sn as a representative of the S wave radiation from the source, and comparison has been made with the Pn phase to characterise the P radiation.

However, detailed observations of the amplitude behaviour of Pn and Sn frequently show a very different dependence in the range 200 - 300 km away from the source. Whilst Pn is clear and separates distinctly from the rest of the P wavefield, Sn is often not discernable until distances around 300 km. Such behaviour has been observed on refraction surveys in Europe and from regional events in southeastern Australia.

In order to look at the causes of this behaviour and the way in which the Pn and Sn amplitudes vary with distance we have examined a wide range of long-range refraction profiles from the Eurasian area. We have also investigated the influence of topography at the crust-mantle boundary on the amplitude distribution to be expected from mantle phases such as Pn, Sn.

THE PHYSICAL CHARACTER OF REGIONAL PHASES

The analysis techniques used in discrimination work tend to label prominent arrivals on regional seismograms with simple descriptors (e.g. Pn, Pg, Sn, Lg) based in large part of the properties observed at regional arrays. However, in order to understand the way in which the relative amplitudes of such arrivals change with range we need to work with a more direct physical description of the propagation processes which give rise to the classes of regional arrivals.

Kennett (1989b) has shown how a description of the propagation processes involved in the major regional phases can be made in terms of reflection and transmission operators for propagation in a laterally heterogeneous medium. Figure 1 sketches the classes of ingredients which have to be taken into consideration in the representation of the mantle phases - both the propagation characteristics of the crust and the mantle have to be known for effective modelling. In addition the development of suitable computational approximations for such operators is dependent on a knowledge of the fine structure of the seismic arrivals.

The phase and group velocity definitions used for phases such as Pg, Lg do not fit in easily with the phase assignment schemes used by many location schemes, which are based on direct ray modelling of the possible propagation paths. However, with only a modest amount of effort, it has proved possible to modify the output of the new *iasp91* travel time routines which implement the travel time tables of Kennett & Engdahl (1991), to provide specific values of the phase and group velocities associated with the conventional phase names. An example of a script file generated by this process is displayed in figure 2. As has been previously noted by a number of authors (see e.g. Kennett 1985) the definition of Lg as a phase with a group velocity of 3.5 km/s is appropriate because of the
Figure 1: A schematic representation of the propagation processes which need to be included in the description of mantle phases (after Kennett 1989b).
Figure 2: Script file display for the adaptation of the iasp91 travel time routines to display phase and group velocities in order to compare the ray based assignments of conventional location procedures with the discrimination phases Pg, Lg.
mutual interference of many multiple S reflections within the crust, but this means that a phase association via ray definition will shift quite rapidly between different phases with distance. A similar problem tends to happen with Sn as the distance increases, the amplitude of the waves returned from the mantle diminish and fall below the coda of P, but the surface multiples remain visible and can be confused with the true arrival Sn (Kennett 1985). The reinforcement of the surface multiples occurs because there are a number of different physical propagation paths which have the same time behaviour.

In addition, the generic descriptions Pn, Sn used for mantle phases are not necessarily an accurate description of the character of the arrivals which are actually picked from a regional seismogram. As we shall see below, long-range refraction experiments ascribe significant substructure to the "Pn" arrival between 200 and 800 km. The interaction of these multiple arrivals from the mantle and surface multiples gives a complex structure of propagation processes which are reflected in the visual complexity of regional seismograms.

An inexpensive and convenient tool for assessing the way in which different types of propagation effects can interact to build up the patterns seen on an individual seismogram is provided by WKBJ seismograms (Chapman 1978) for a horizontally stratified model. Unlike methods based on the full reflection response of the medium, the different classes of propagation paths have to be specified separately. As a result there is a significant initial effort in assembling the ray code descriptions which control the class of physical processes which are included, but once this is done the computation of seismograms is very rapid. Further there is no difficulty in isolating the contribution of different processes by modifying the choice of ray codes. An example of the WKBJ synthetics for a simple crustal model representative of a shield region is presented in figure 3, together with the group velocity trajectories associated with the array definitions of Pg, Lg. As expected these trajectories cut across a sequence of multiple arrivals representing P and S wave reflections within the crustal waveguide.

For this WKBJ example the ray codes were chosen so that up to 4 surface multiples of each major ray path would be included. This includes reflection from each of the boundaries in the model or refracted (diving) waves below interfaces. The theoretical seismograms are presented with trace normalisation, and clearly display the significance of multiples of the mantle phases at greater distance. The multiple reflected waves in the crust tend to asymptote to the expected trajectory of Lg and we can see that we would expect systematic errors from the group velocity definition of Lg for distance ranges close to the critical point of successive multiples of the reflection from the crust mantle boundary. As more and more multiples contribute to the wavefield the association of the maximum S amplitude with the specific group velocity of Lg improves. However for epicentral distances less than 400 km it would be preferable to attempt to associate the observed Lg arrival with the theoretical times for Sg or SgSg.

It may be possible to introduce a partial allowance for lateral heterogeneity into the WKBJ calculation by introducing systematic perturbations to the central phase functions which are currently constructed for horizontally stratified model. Such a procedure will be investigated over the next year.
Figure 3: WKBJ synthetic seismogram for a simple crustal model representative of a shield region. Up to 4 crustal multiples are allowed for reflection from each interface or for diving waves. The P and S wave calculations were carried out separately and superimposed in plotting.
OBSERVATIONS OF MANTLE PHASES

A number of authors have noticed that the onset of the Sn phase around 200 km can be difficult to pick by comparison with the equivalent Pn phase even for those situations where the P coda is low. These observations come from a wide range of stable tectonic environments. For example, the phase association procedure used for locating earthquakes in southeastern Australia only declares an Sn phase when the estimated distance is greater than 300 km because of the difficulty in obtaining reliable picks at shorter distances. The amplitude of the energy return from the mantle is dictated by the size of the velocity gradients for P and S waves in the uppermost part of the mantle. The pattern of observations for Sn with a low amplitude arrival around 200 km but greater amplitude at ranges beyond 300 km, suggests that the S wave gradient is low in the uppermost mantle and then increases at a depth of 10 or so kilometres below the crust-mantle boundary. Recently Gajewski et al (1990) have shown that this pattern of slow emergence of Sn is observed on many refraction profiles in western Europe in zones with a similar geologic setting to Eastern Australia i.e. regions affected by mountain-building episodes in the last 300 Ma. They have associated the differences in velocity gradient for P and S with a possible differences in mineral composition with depth. Such geologic environments also occur in much of the Soviet Union. As we shall see later in some areas of Precambrian rocks Pn and Sn are observed with comparable clarity, so that there may well be differences in the nature of the uppermost mantle which depend on the geological history of the region being studied. Gajewski et al (1990) also noted differences in the character of Sg phases compared with the corresponding Pg arrivals.

There are only a limited number of experiments in which both P and S propagation can be tracked to significant distances with a station spacing close enough for the evolution of the wavefield to be judged. Most of these cases are for explosions, but there a very limited number of earthquake observations. During the operation of a linear array of seismographs in southeastern Australian during the southern summer of 1989/1990 we were fortunate to record both an earthquake (FF) and a quarry blast (SM) which lie along the line of the profile. The corresponding record sections are displayed in figure 4 together with an inset map of the array configuration. The general character of the wavefield is very similar although there are differences in the P radiation (by accident a nodal plane for P wave radiation from the Fitzroy Falls earthquake passes through the line of the array). On each section we can see the change in phase velocity with the emergence of the Pn arrivals but the corresponding emergence of the Sn phase cannot be reliably tracked. The amplitude of the P coda is quite high and there is little difference in frequency content between the P and S wave fields. This example gives a good illustration of the merits of multi-station recording. Where close station spacing was achieved there is a good correlation of the records at successive and phases can be readily identified. Even for the isolated distant station identification of arrivals is simplified by extraction from closer distances. In the first period after the installation of a new regional station it would be highly desirable to build up a record section from available sources so that the structure in the neighbourhood of that station can be calibrated.
Figure 4: Recordings of an earthquake (FF) and a quarry blast (SM) along the same array of portable seismographs in southeastern Australia. In each case the Pn phase can be clearly observed even though the earthquake phase are close to a node for P, it is much more difficult to detect the Sn arrival even with a number of records.
A further example of a detailed set of earthquake observations at regional ranges is provided by the recording of an earthquake in Scotland during the long-range refraction experiment conducted in 1974. The earthquake was displaced from the line of the profile but there is still an very useful set of observations from 70 to 290 km away from the event (figure 5). There is a clear mantle S arrival with a rather emergent onset which in this case can be tracked back to the cross over with the Sg phase. Figure 5 displays the onset of both the P and S wave portions of the wavefield as recorded on vertical component seismometers. The travel times superimposed on the S wave section are derived from a model of the crustal P wave velocity determined by refraction work by assuming a ratio of P and S velocities of \( \sqrt{3} \). These theoretical times are in reasonable agreement with the S wave section, though the predicted times for Sn may be a little early. The general character of the P and S fields is similar but in this case the ratio of the mantle to crustal amplitudes is larger for S than P.

In order to see whether the pattern of propagation of the mantle phases is consistent from region to region and also to investigate the evolution of the Sn/Pn amplitude ratio with distance we have searched for refraction recordings with good S wave arrivals in the distance range from 100 - 1000 km. Although much of the long-range profiles in Europe were originally recorded with three-component sensors, most of the interpretations have been based on the P wave data from the vertical component records and relatively few S wave sections have been published. However, sufficient S wave data exists for us to be able to begin to make a comparison of the propagation characteristics of the P and S wave field.

As an example we present in figure 6 a comparison of P and S recordings at ranges from 200 - 800 km (Hirn, 1977) from a profile of instruments deployed across France to record a large explosion fired in the sea off Brest. The record sections are phased to concentrate attention on the mantle arrivals which in nuclear monitoring work we would normally term Pn and Sn. However we can see clearly from figure 6 that such phases have significant substructure and the almost constant apparent velocity is built up from a sequence of en-echelon phases which progressively become first arrivals as the distance increases. The interpretation of such arrivals in terms of a one-dimensional velocity model leads to very complex velocity distributions with multiple low-velocity zones (see e.g. Kind 1974), but it is very likely that much of the complexity arises from lateral heterogeneity in the structure in the upper most mantle (Fuchs & Schulz, 1976). A similar pattern of complex structure within the wavegroup characterised by Pn can be seen in the record sections presented by Yegorkin & Chernyshov (1983) from peaceful nuclear explosions in the Soviet Union (fig 13).

In figure 7 we illustrate the pattern of rays associated with the class of model which has been proposed to explain the complexity of the observed mantle arrivals. A weak gradient zone below the Moho is terminated by a low velocity zone (which is needed to get a suitable delay for arrivals from greater depth). This leads to a relatively weak Pn arrival from the uppermost mantle which is supplanted at greater distance by the P1 phase returned from depth, and at even greater ranges by PII. The observations of Gajewski et al (1990) relate to the Pn, Sn arrivals from the uppermost mantle and not to these arrivals from greater depth. The arrivals P1, PII, S1, SII are frequently more energetic and are the phases which
Figure 5: $P$ and $S$ wave sections for the vertical component of displacement for an earthquake in northwestern Scotland recorded during the long-range refraction profile through the British Isles. The reduction velocity for the $P$ section is 8 km/s, and for the $S$ section it is 4.62 km/s (after Kaminiski et al 1974).
Figure 6: Three component record sections for a large explosive shot off the French coast recorded across a long range profile in France (after Hrn 1977). Reduction velocity for the Z section is 8 km/s, whereas for the L and T sections the velocity is 4.62 km/s.
Figure 7: Ray diagram illustrating the way in which a mantle structure with a number of gradient zones can give rise to a sequence of phases returned from the mantle with an apparent en-enchelon behaviour in time.
would be designated in discrimination work as Pn, Sn because an individual seismogram is not sufficient to recognise the substructure of the wavefield.

In general the quality of S data from explosive sources is not very good because the P coda is energetic and so we are looking for S arrivals against a relatively noisy background. However some experiments, especially in Precambrian terrains where the shear velocities are relatively high, do give a very good representation of the S wavefield even on vertical component instruments. Figure 8 shows the locations of three refraction profiles in Fennoscandia which have good quality S arrivals.

Figure 9 shows P and S wave sections from the same shotpoint point A in a Finnish-Polish refraction experiment SVEKA across part of the Baltic Shield in southern Finland (Luosto et al 1984, Grad & Luosto 1987). The S arrivals are very clear and give a good general agreement with the pattern of the P arrivals. In this case the crust is rather thick and the transition from Moho reflections to refractions occurs at the end of the profile. Interestingly the reflection from the Moho around 160 km offset is clearer on the S wave section. Rg is only visible to 100 km.

The quality of the S records in figure 9 is surpassed by the remarkable set of records from a further Finnish-Russian experiment BALTIC which lay further to the southeast (closer to the Russian border). The data from shot point B is shown in figure 10 and at first sight is difficult to distinguish which is the P and which is the S profile (other than by examining the timing of the Rg phase). The correspondence of the phases is exceptionally close and here, at least, there is a very distinct Sn arrival beyond 200 km. The reversed profile from shotpoint G has less clear Pn and Sn arrivals with a cross over around 3020 km. Despite the pronounced topography on the Moho (see e.g. Bannister, Ruud & Husebye 1991), good mantle arrivals are seen on these profiles.

A further experiment in northern Finland and Sweden, the POLAR profile (Luosto et al 1989) shows uniformly good S propagation from all shot points including those with fairly small charges. A record section from shotpoint A at the southern end of the line is shown in figure 11. In this area it would appear that the Moho is very sharp because of the very distinct PmP. SmS arrivals which can be seen to connect directly into the Pn, Sn phases at greater distance. This profile lies relatively close to the Arcoss array for which there are generally very clear observations of S phases from the mine blasts on the Kola peninsula. This geologic province is the oldest in Fennoscandia and it would appear that attenuation is rather low.

A comparison of the three sets of P and S record sections presented in figs 9-11 shows noticeable differences in the character of the wavefield. For the SVEKA profile (fig 9) there are strong direct Pg and Sg phases extending out to 200 km, where they are overtaken by the Pn and Sn phases. The reflection from the crust mantle boundary is more distinct for S than for P, indeed it is quite difficult to correlate the P wave arrival to distances smaller than 180 km where the corresponding S reflection is very clear.

For the BALTIC profile (fig 10) which is again in southern Finland, Pg and Sg are clear but by comparison less energetic than for SVEKA. In this case both the prograd e and retrograde travel time branches associated with reflection and refraction at the crust-mantle boundary can be clearly seen for both P and S. The
Fig. 1. DSS profiles: b = Finlap; c = Barents Sea; d = Pechenga-Umbozero; e = Pechenga-Kostamuksha; f = Kem-Tulos; g = Baltic; h = Sveka; i = Sylen-Porvoo; j = Ladoga; k = Polar; l = Kem-Uchta; m = Eläijärvi-Lahnaslampi. SF = Svecofennian Domain; KA = Karelian; BE = Belomorian Province; KO = Kola Peninsula Province; CA = Caledonides; LGB = Lapland Granulite Belt; LBB = Ladoga-Bothnian Bay Zone; RJ = Viborg Rapakivi Granite Intrusion (tectono-geological map by Korsakova et al., 1987).

Figure 8: Configuration of the SVEKA and BALTIC and POLAR refraction experiments in Fennoscandia.
Figure 9: Comparison of P and S record sections from the SVEKA refraction profile in Finland using vertical component seismometers, the traces are amplitude normalised. The reduction velocity for the P section is 8 km/s, and for the S section it is 4.62 km/s (after Luosto et al 1984, Grad& Luosto 1987).
Figure 10: Comparison of P and S record sections from the BALTIC refraction profile in Finland using vertical component seismometers, the traces are amplitude normalized. The reduction velocity for the P section is 8 km/s, and for the S section it is 4.62 km/s
Figure 11: Comparison of P and S record sections from the POLAR refraction profile in northern Fennoscandia using vertical component seismometers, the traces are amplitude normalised. The reduction velocity for the P section is 8 km/s, and for the S section 4.62 km/s (after Luosto et al 1989).
strength of the mantle arrivals near the crossover at 180 km leads to strong suppression of the Pg and Sg arrivals in these amplitude normalised displays.

For the POLAR profile (fig 11) the exceptional strength of the reflected energy from the Moho suppresses the display of Sg, in particular between 120 and 160 km. If a phase association were to be made in this case on the maximum S amplitude it would be displaced by 2-3 seconds from the assumed trajectory for Ig and could well lead to significant mislocation of an event. The mantle arrivals are weaker than for the BALTIC profile and we can see the Pg and Sg arrivals grade into the PmP and SmS arrivals as would be predicted by standard crustal models.

The map of refraction profiles in Fennoscandia indicates a number of profiles within the Soviet Union, with a relatively dense shotpoint spacing. Unfortunately almost all the Deep Seismic Sounding experiments carried out within the USSR have used analogue recordings. Relative close station spacing e.g. 100 m with a 5 km recording spread has enabled close correlation of features on the seismograms. Attention has largely been focussed on the time relations of the different features and in published accounts only very limited descriptions of the amplitude behaviour are provided. It is therefore quite difficult to extract systematic information on the character of the wavefield.

A very interesting experiment was carried out by Jentsch (1979). He hand digitised a very large number of Russian recordings from a DSS profile in the southern Ukrainian shield, and then attempted to apply conventional one-dimensional interpretation techniques to this data. Figure 12 displays a portion of the record section which displays both the P and S energy. The source for the recordings were multiple explosive charges in separate holes. A notable feature of these records is the relatively short correlation distance for the amplitude along individual phases. Although general trends are clear, there are significant variations in amplitudes over distances little larger than the aperture of a regional array of the Noress/Arccess type; these often correlate between the P and S phases but do not always coincide in range. We therefore certainly need to be cautious in interpreting amplitude ratios between different phases from individual seismograms. For discrimination purposes the stability of an amplitude ratio estimate based on a number of closely spaced stations is certainly to be preferred to even a single three component station. Mini-arrays with a few vertical component sensors surrounding a central three-component systems would seem highly desirable in this context.

Yegorkin & Chernyshov (1983) have presented record sections for P waves along DSS profiles in northern Siberia (to 1700 km) and central Asia (to 900 km). The typical spacing of traces is to 10 km and a portion of the Siberian line is reproduced in fig 13. The patterns of P wave propagation for the onset of the seismogram are similar to those seen on long-range refraction profiles in Europe. The energy return from the mantle consist of a number of distinct arrivals which can be correlated over substantial distances. It would appear that the recording interval used in these very long range refraction experiments was too short to include the S arrivals from the mantle as well.

THEORETICAL STUDIES

In association with the observational studies we have also considered ways in which the behaviour of the Pn and Sn can be modelled with allowances for the
Figure 12: Portion of a record section assembled from hand-digitised seismograms from a detailed DS5 profile across the southern Ukrainian shield with reduction velocity 6 km/s. The amplitude variability across the very close trace spacing (around 200 m) illustrates the problems involved in trying to use the ratios of different seismic phases as measures of source radiation patterns (after...
Figure 13: Portion of the record section from a DSS profile in northern Siberia, the reduction velocity is 8.2 km/s (after Yegorkin & Chernyshov 1983).
effect of lateral heterogeneity. As we have seen above, we cannot neglect the influence of free surface multiples and so we cannot easily separate the modelling of mantle phases from the problem of wave propagation in the crustal waveguide.

For Sn we can adapt the coupled mode scheme previously used by Kennett (1986) for modelling Lg wave propagation in the crust with allowance for coupling to Sn, by simply enlarging the number of modes considered and thus the phase velocity span which can be modelled. For propagation up to 3-4 Hz this would require coupling calculations spanning up to 200 modes (i.e. 200 coupled complex differential equations). Such calculations are feasible for many frequencies on a supercomputer but are rather time consuming, and even so we are restricted to slight perturbations of the crust-mantle boundary.

In principle, the mode coupling procedure can also be extended to the Pn and Pg parts of the wavefield but this would require more than a 1000 modes for frequencies higher than 2 Hz and as such does not present an attractive route. If full account is taken of the possibility of reflection we would need to solve a differential equation for a 1000x1000 complex matrix: even with the most efficient algorithms this would be very difficult on current computers.

We have therefore been looking at alternative representations of the seismic wavefield which exploit the idea of coupling between different horizontal wavenumbers (which underlies the mode coupling procedure) but which use an alternative expansion of the field in orthogonal functions. A suitable basis set exists if the free surface can be neglected and so could be used for propagation to around 300 km. However no satisfactory solution has yet been found to allow inclusion of surface reflections. We will continue to investigate methods for modelling the propagation of the mantle phases over the next year.

One aspect of the character of Pn and Sn which has proved amenable to modelling is the influence of topography at the crust-mantle boundary. In the Finnish example above there is substantial topography at the Moho, and the long-range refraction profile along the length of the British Isles (Bamford et al, 1976) has also shown significant topography at this level. For high frequency waves, an approximation to the effects of an irregular boundary can be made by introducing a generalised transmission coefficient whereby a single incident plane wave couples into a spray of plane waves on the other side of the interface.

This approach can be introduced into a modification of the reflectivity method, in which ray techniques are used to transfer energy from the source to the irregular boundary and from that boundary to the receiver; but a full calculation is made in a horizontally layered structure lying beneath the crust-mantle boundary. However, the amplitude kernel in the plane wave response for this region is modulated by the redistribution associated with the generalised transmission coefficients on entry and exist from the mantle. The method assumes that the top of the reflection zone averages to a flat level assumed in the reference model; this can give rise to slight inaccuracies in the amplitude and timing of waves reflected at the underside of the interface. The dominant arrivals corresponding to diving waves will be correctly represented.

The amplitude distance behaviour for a model derived from the Moho topography of Bamford et al (1976) is displayed in fig 14, together with the form of the crust-mantle interface for propagation from north to south and from south to north. These amplitudes are compared with those calculated for a laterally
uniform reference model and have been derived from the synthetic seismogram sections in Figure 15, which have been calculated using a phase velocity window from 8.1 to 10.0 km/s in all cases. This window corresponds to purely propagating waves in the layer immediately below the crust-mantle interface and allows direct comparison between flat and perturbed topography at the Moho.

The results for the reference model (with horizontal layering and a Moho depth of 32.5 km), are indicated in fig 14 by the solid circles, open squares are used for propagation from north to south, and open triangles are used for propagation from south to north. The fluctuations introduced by the presence of topography are significant but in general less than the typical variability in observed amplitudes. The offset distance from the Moho to the recording point at the surface is about 45 km, so the amplitude symbol will be displaced from the relevant topography. The major change from the reference model is a shift of the amplitude peak near 300 km to shorter distances and an enhancement of the amplitude minimum near 400 km range.

These features are clearly seen in the record sections of the theoretical seismograms in fig 15. The effect of topography is to give a pronounced concentration of energy near 300 km accompanies by reduced amplitudes near 400 km. If we were to interpret the NS and SN record sections in terms of horizontally stratified models, we can see that the resulting velocity models would differ significantly from the reference models. In particular, to change the peak in P1 amplitudes a more pronounced velocity inversion would be required.

These calculations show the effect of topography on the P wavefield, and we can anticipate similar effects for S waves. However, unless the velocity ratio between P and S waves is a constant throughout the medium, the propagation paths for P and S waves will differ. The focussing and defocussing effects associated with topography can therefore be displaced slightly between the P and S wave patterns which will give rise to fluctuations in the ratios of amplitudes of mantle P and S waves and so complicate use as a discriminant.

CONCLUSIONS

We have been able to demonstrate that the amplitude behaviour of Pn and Sn with distance is quite complex and that it is necessary to look at the anatomy of the phases in order to understand the potential performance of some regional discriminants. In detail the Pn and Sn phases tend to break up into a sequence of overlapping branches associated with fine structure in the upper part of the lithosphere. Anomalously low Sn amplitudes can arise between 200 and 300 km away from the source.

The current class of regional phase discriminants based on averaged behaviour of seismic phases such as Pn and Sn could give misleading results in some distance ranges because of the way in which the peak amplitudes in the requisite time windows shift between different wave groups. Such effects are difficult to pick up from isolated earthquakes or mine blasts but are evident in long range refraction profiles or comparable record sections.

It will be difficult to assess the amplitude behaviour of the Pn and Sn phase for the area around a particular receiver site without careful calibration, and the analysis of regional phases will need to be adapted to take the nature of the particular phases into consideration. The maximum amplitude within a
Figure 14: Amplitude distance behaviour for topography at crust-mantle boundary. Solid circles indicate calculations for reference model at right with a Moho depth of 32.5 km. Open squares indicate propagation from north to south and open triangles propagation from south to north.
Figure 15: Record sections of synthetic seismograms illustrating the effect of topography at the crust-mantle boundary. R reference structure; NS propagation from north to south; SN propagation from south to north. No scaling is applied with range.
specified group velocity window may not be the best measure of the P or S wave content of the seismogram.

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