SPACE-BASED BLUE–GREEN LASER

J. C. Hsia, M. W. McGeoch and D. E. Klimek
AVCO EVERETT RESEARCH LABORATORY, INC.
a Subsidiary of Avco Corporation
Everett, MA. 02149

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<td>Abstract</td>
<td>An experimental and theoretical program has been completed which thoroughly characterizes the e-beam sustained discharge HgBr laser. The preliminary design of a 100 Hz, 2 J HgBr laser has been performed. From measurements of HgBr fluorescence efficiency as a function of E/N the primary laser excitation process has been identified as the collisional excitation of HgBr₂ by electrons. A self-consistent set of excitation cross sections is</td>
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derived from the experiment. The formation efficiency of HgBr(B)
in a discharge is 6%. The stimulated emission cross section at
502 nm is measured to be $1.6 \times 10^{-16}$ cm$^2$. Absorbing species are
identified as HgBr(X) (absorption cross section $5 \times 10^{-20}$ cm$^2$ at
520 nm) and HgBr$^+$ (2 $\times 10^{-18}$ cm$^2$ at 520 nm). The maximum laser
intrinsic efficiency is measured to be 3.3%. The maximum elec-
trical efficiency is 2.4%. Lasing energy density is 2 J/l in a
HgBr$_2$/Ar mix. Maximum lasing energy is 9.8 J. Detailed design
conditions are given for a 100 Hz, 2 J HgBr e-beam sustained
discharge laser, of overall efficiency 1.2%.
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I. INTRODUCTION

This report covers the Phase I contract performance period from June 9, 1980 to June 8, 1981. All the program objectives were achieved, and indeed the demonstrated HgBr laser electrical efficiency of 2% was rather higher than had been predicted before the work began. The HgBr single pulse laser energy was scaled to 10 J.

In the course of this work we have substantially advanced the kinetic understanding of the HgBr laser, and in this report we present the first detailed description of the excitation mechanism by direct electron impact on HgBr$_2$.

From our extensive parametric studies we have identified the dominant kinetic processes (quenching, absorption, and attachment) which govern the HgBr laser behavior in an e-beam sustained discharge. A model has been developed which predicts laser performance to an accuracy of ± 10%.

In the second half of this report we apply the discharge model to the design of a 2 J, 100 Hz long life HgBr laser system. Our conclusion is that such a design is entirely feasible. The precise control that is possible in e-beam sustained discharges allows a conservative design of the laser cavity and flow loop within a compact overall system.

In conclusion, the e-beam sustained HgBr laser has been demonstrated to be efficient and powerful. An approach to design has been developed which is relevant to a wide range of potential applications.
II. TECHNICAL PROGRESS

A. KINETIC MODEL AND EXPERIMENTS

1. Introduction

An extensive range of experiments has been performed in order to understand the HgBr laser kinetics and discharge characteristics. This has been successful to the extent that there are no remaining uncertainties in the laser modeling which might otherwise affect the design.

The main achievements have been to demonstrate laser electrical efficiency over a wide range of operating conditions and to generate a model of the laser performance which is capable of predicting laser efficiency to within ± 10% accuracy.

Because of its importance in the model, a detailed study has been made of the HgBr*(B) formation process and the first complete set of electronic excitation cross sections has been derived from the experiments. Use of this set in a Boltzmann code has given a complete description of the formation efficiency as a function of applied electric field and HgBr₂ number density.

The experiments were performed on two different machines. The small-scale device had an e-beam entry aperture of 1 x 23 cm and discharge spacing of 1 cm. The 1 m device had an e-beam aperture of up to 10 x 100 cm and a discharge spacing of 4.5 to 8 cm. The discussion is divided into Section II-A-2 which deals exclusively with experiments on the small-scale device and the associated kinetic modeling, and Section II-A-3 which covers the 1 m device experiments and modeling.
2. Small-Scale Experiments

a. Experimental Methods

The discharge chamber is shown in Figure 1. The e-beam voltage was 125 to 150 kV and its current density was controlled by attenuator screens in the range 0.5 A/cm² to 2.5 A/cm². The discharge anode had a Chang profile to give a field uniform to ± 10% over a 1.1 cm width. The chamber was kept at 220°C and HgBr₂ density was varied by controlling the temperature of a 'sidearm' reservoir.

The discharge was driven either by a capacitor or a "PFL," a pulse forming line consisting of paralleled cables with a nominal impedance of 3.36 Ω. The capacitor circuit is shown in Figure 2 and typical waveforms are shown in Figure 3. The PFL circuit is shown in Figure 4 and typical waveforms in Figure 5. The "square topped" nature of the PFL pulse was important in determining steady-state fluorescence and laser behavior, and contributed much to the precision of the kinetic modeling.

For the purpose of gain and absorption measurements a tunable dye laser was employed as shown schematically in Figure 6. The measurement of small absorptions required a double-pass configuration. This was actually collinear, although separated in Figure 6 for clarity.

Voltage and current measurements were estimated to be better than ± 10% accurate. Sidelight fluorescence was viewed through a bandpass filter by vacuum photodiode. Laser output was monitored by photodiode and calorimeter.

The foil material was 'Kapton', 2 mil thick, aluminized on the side facing the e-beam cathode. Windows were fused silica. The magnetic guide field was 1 kG. Throughout the experiment the e-beam, driven by a dc charged cable, functioned very reliably. This reliability was a major factor in the completion of extensive parameter variations in both discharge conditions and gas mix.

b. Modeling of HgBr*(B) Formation Process

In the first report of a discharge HgBr laser, (1) Schimitschek and Celto suggested that the excitation mechanism
Figure 1. Detail of the Small-Scale Laser Chamber
Figure 2. Schematic of Small-Scale E-Beam and Discharge Circuit
Figure 1. Small-Scale E-Beam and Capacitor Discharge Characteristics
Figure 4. Schematic of Small-Scale Cable PFL

NOM IMPEDANCE = 3.356 Ω
(20 TORR HgBr$_2$ / 2 AMA Ar)

ELECTRICAL COUPLING EFFICIENCY $\approx 0.75$

Figure 5. Typical Laser Discharge, Sidelight and Output Characteristics with Cable PFL
Figure 6. Apparatus for Gain and Absorption Experiments
might be a collisional dissociation of HgBr$_2$ by electrons analogous to the well known photodissociation process. They did not, however, estimate a rate constant for electronic excitation. In 1978 Allison and Zare (2) reported absolute measurements for the electronic excitation of HgBr$_2$ to give HgBr(B-X) fluorescence, which gave a cross section $\sigma < 1 \times 10^{-20}$ cm$^2$ for electrons between 5 and 25 eV and a peak cross section at $\sim$ 200 eV of only $1 \times 10^{-19}$ cm$^2$. Because of these small cross sections several later authors sought to explain HgBr laser action in N$_2$/Ne mixes and Xe/Ne mixes in terms of (a) electronic energy transfer from excited N$_2$ or rare gas species to HgBr$_2$, (3,4) or (b) recombination (5) of HgBr$^+$. It was also suggested (6) that HgBr$^*$ (B) could be formed in an attachment process producing Br$^-$. 

Our preliminary experiments showed an approximately equal formation efficiency in any of the rare gas buffers Ne, Ne(10% Xe), Ar, Ar (5% Xe), and moreover strong HgBr(B-X) fluorescence was observed in Ar buffer at E/N values where the excitation of the Argon resonance levels (Ar$^*$ $^3$P$_1$, $^3$P$_2$) at 11.5 eV was extremely small. The inference was that here Ar$^*$ could not be involved in the production of HgBr$^*$ (B), whether by a Penning

process to HgBr$^+$ followed by recombination, or by a direct energy transfer such as Ar$^*$ + HgBr$_2$ + HgBr$^*$ (B). (In any case, Chang and Burnham$^{(3)}$ had not observed any HgBr(B+X) fluorescence from HgBr$_2$ in the presence of Ar($^3$P$_2$) metastable atoms). It was concluded that the primary HgBr$^*$ (B) formation process, at least in Argon buffers, had to be a direct electronic excitation of HgBr$_2$.

Three candidate processes were considered for this role:

1. **Inelastic Collision**

   \[ \text{HgBr}_2 + e^- \rightarrow \text{HgBr}_2^* + e^- \rightarrow \text{HgBr}^*(B) + \text{Br} + e^- \]

2. **Ion Channel**

   \[ \text{HgBr}_2^+ + e^- \rightarrow \text{HgBr}^*(B) + \text{Br} \]

3. **Attachment**

   \[ \text{HgBr}_2 + e^- \rightarrow \text{HgBr}^*(B) + \text{Br}^- \]

Process (2) and (3) were not compatible with our experimental observations. In particular, our measurements of absolute fluorescence efficiency and attachment rate coefficient led us to conclude that the Attachment Channel (3) was 10 to 20 times too slow to explain the observed fluorescence power. The Ion Channel (2) implied discharge ionization rates that were incompatible with the stable attachment-dominated discharge that we observed over a wide F/N range. Also, no delay in fluorescence was observed ($\tau_{\text{delay}} < 10$ ns) which would have necessitated an Ion Channel recombination rate of $\sim 100$ times greater than rates typical of dissociative recombination.

We concluded that Inelastic Collision was the dominant HgBr$^*$ (B) formation process in Argon buffers, and attempted to synthesize a realistic set of HgBr$_2$ electronic cross sections to describe the process and allow extension of the modeling to other gases.
As a starting point we had available cross-section measurements\(^7\) of the attachment process \(\text{HgBr}_2 + e^- \rightarrow \text{HgBr}(X) + \text{Br}^-\) and also of the ionization process \(\text{HgBr}_2 + e^- \rightarrow \text{HgBr}^+ + 2e^-\). As trial Inelastic Collision processes we chose \(\text{HgBr}_2\) dipole allowed processes which appeared in optical absorption at \(\sim 5\) eV, \(\sim 6.4\) eV and \(\sim 7.9\) eV. These will be discussed in turn.

5 eV Process: In optical absorption this extends\(^8\) from 250 nm down to 210 nm and has been associated\(^9,10\) with the photodissociation of \(\text{HgBr}_2\) into only non-fluorescing products, probably\(^11\) \(\text{HgBr}(X) + \text{Br}\). Although the 230 nm optical absorption is assigned\(^11\) to the \(1^1 \Sigma_g^+ \rightarrow 1^1 \Sigma_u^+\) transition, nearby \(3^3 \Sigma_u^+\) and \(3^3 \Sigma_u^+\) states are also accessible by electronic collision and could provide the dominant contribution to the excitation cross section near 5 eV because of the relatively peaked behavior of singlet-triplet processes near threshold. We, therefore, assumed that the 5 eV process peaked at 6.5 eV and had unit branching to \(\text{HgBr}(X) + \text{Br}\).

6.4 eV Process: This corresponds to a band between 190 and 210 nm in optical absorption, which leads to \(\text{HgBr}^*(B)\) fluorescence with unit quantum efficiency.\(^8\) Its assignment\(^11\) of \(1^1 \Sigma_g^+ \rightarrow 1^1 \Sigma_u^+\) has been confirmed by a measurement\(^12\) of the polarization dependence of \(\text{HgBr}^*(B)\) fluorescence following photodissociation at 193 nm. We assume that the electronic excitation cross-section peaks at \(\sim 4\) times the threshold energy by analogy with other singlet-singlet transitions. Also, we suppose

\begin{itemize}
  \item \textbf{References:}
  \begin{enumerate}
    \item Wiegand, W.J., UNR Report B60-9,4784-1 (1960).
    \item \textit{Wiegand}, K., Z. Phys. 76, p. 801 (1932); 77, p. 157 (1932).
  \end{enumerate}
\end{itemize}
that in the 6.4 eV process HgBr$_2$ dissociates rapidly ($\gg 10^9$/s) into HgBr$^*$ (B) with unit branching, by analogy with photodissociation.

7.9 eV Process: There is a very large process at 7.9 eV in the electron energy loss spectrum for HgBr$_2$.\(^{(13)}\) Also at 159 nm (7.8 eV) there is a strong optical absorption\(^{(9)}\) which leads to fluorescence in the 270-250 nm region. Accordingly we give this process a singlet-singlet shape of cross section, peaking four times above threshold, but with zero branching to HgBr$^*$ (B). We shall refer to this HgBr$_2^*$ (7.9 eV) state as the HgBr$_2$ 'complex' level and use it both as the terminal level of dissociative recombination and as a reservoir for a two-step ionization process. As a first estimate we give the levels in the 'complex' an average $10^8$ sec$^{-1}$ decay rate, with 0.5 branching to HgBr$_2$(X) and 0.5 to HgBr(X) + Br. The exact value of the decay rate has no influence on the laser modeling predictions.

Given this trial set of three inelastic processes, and using the UTRC attachment and ionization cross sections a fit could be made to our experimental fluorescence versus E/N data. For this purpose an established Boltzmann code was used, which handled elastic, inelastic, ionization and attachment processes. A tested set of Argon cross sections was employed, the only really operative one of which, that for momentum transfer being very accurately known. It was verified that the code predicted experimental pure Ar drift velocities to better than 1% accuracy. The following routine was used to achieve the fit to data shown in figure 7:

1. The magnitude of the 7.9 eV complex cross section was varied until ionization equalled attachment at the experimental argon E/N of $4.0 \times 10^{-16}$ cm$^2$ (for 0.8 sec$^{-1}$ HgBr$_2$ ionization).

Figure 7. HgBr*(B) Formation Efficiency as a Function of E/N
2. The magnitudes of the 5 and 6.4 eV processes were adjusted in tandem until the observed fluorescence efficiency and voltage dependence were fitted by the 6.4 eV process.

Figure 7 shows that a good fit was obtained, which tends to confirm the three-process assumption. It was not possible to fit the data accurately with a two-process model (i.e., leaving out the 5 eV process) because the 6.4 eV excitation would then peak at \( E/N \approx 6 \times 10^{-17} \text{ Vcm}^2 \) and not at the higher experimental value.

Vibration, rotation and elastic processes for HgBr\(_2\) were tried, but had negligible effect on the excitation rates or drift velocity for \( E/N > 1 \times 10^{-17} \text{ Vcm}^2 \). They were therefore omitted from the cross-section set, which is shown in Figure 8. In order to give better agreement of the computed attachment rate (Figure 28) with the Avco experiment, the UTHC attachment cross section was scaled up by 1.1. The best fit cross-section set is shown in Figure 8. It is difficult to put accurate estimates on the magnitude of the 5, 6.4 and 7.9 eV cross sections, because assumptions have been made about shape and branching ratio. If these assumptions are correct, then the magnitudes are determined to a tolerance of \( \pm 50\% \). However, the predictive power of the cross-section set in HgBr\(_2\)/Ar mixes is considerably more accurate than this, being determined by the experimental error bounds of \( \pm 10\% \) on formation efficiency.

c. Comparison with Experiment in Different Gases

Argon: The discharge fractional power to each process is shown in Figure 9. The 6.4 eV process takes only 13% of the power at its maximum, and the largest process is the dissociation of HgBr\(_2\) via the 5 eV channel. There is still almost a 10% argon elastic loss in the \( 5 \times 10^{-17} \cdot 1 \times 10^{-16} \text{ Vcm}^2 \) E/N range of most interest to lasing. The effect of this elastic loss becomes apparent in Figure 10 where the HgBr\(_2\) percentage is varied. The formation efficiency declines at low HgBr\(_2\) concentration because of increasing Ar elastic loss. At the E/N for most efficient
Figure 8. HgBr$_2$ Electronic Cross Sections from Fitting Procedure
Figure 9. Computed Discharge Fractional Power vs E/N
Figure 10. Computed Formation Efficiency vs HgBr$_2$ Concentration
lasing ($\sim 1 \times 10^{-16} \text{Vcm}^2$) Figure 10 shows that the efficiency of formation is predicted to optimize at $\sim 0.8\% \text{HgBr}_2$, which is also the experimental optimum lasing concentration.

The drift velocity predictions are shown in Figure 11. The drift velocity is increased dramatically by the presence of \text{HgBr}_2, an effect which is traceable to the 5 and 6.4 eV cross sections principally, because electrons return to an energy region of low elastic loss following collisions. The comparison of discharge impedance with experiment (Section II-A-2-n) indicates that there is definitely an enhancement of drift velocity over that in pure Ar.

**Neon:** The computed fluorescence efficiency in neon is shown in Figures 12 and 13. It peaks at lower E/N than in argon but is of approximately the same magnitude. Experimental points lie slightly below the theoretical curve, but the qualitative behavior is well predicted. Remembering that the ionization/attachment balance was used to fit the 7.9 eV process in Ar, the predicted point of arcing in neon (Figure 14) is in excellent agreement with the highest E/N that can be achieved in a stable discharge in neon (Figure 13).

**Neon, 10\% Xe:** The computed fluorescence efficiency for this mixture is compared with experiment in Figure 15. Both theory and experiment lie between the pure Ne and pure Ar cases, in good qualitative agreement. However, in order to obtain this fit an assumption had to be made concerning the effective branching ratio from Xe* to HgBr$_2$. Experiments have shown (3) a unit branching ratio for the process

$$\text{Xe}^*(3\text{P}_2) + \text{HgBr}_2 \rightarrow \text{HgBr}^*(B) + \text{Xe} + \text{Br}$$

However, the branching ratio for Xe*($3\text{P}_1$) is not known, nor is the relative discharge production ratio of $3\text{P}_1$ to $3\text{P}_2$ well known. The present theoretical curves assume that only 10\% of all
Figure 11. Computed Drift Velocity vs HgBr$_2$ Concentration
Figure 12. Computed Fluorescence Efficiency for Various Buffer Gases
Figure 13. Theoretical and Experimental Fluorescence for Argon and Neon Buffers
Figure 14. Computed Single-Step Arcing Fields for Argon and Neon

RELATIVE FLUORESCENCE EFFICIENCY

E/N (V cm⁻²)

0 1 2 3 4 5 6

10⁻¹⁷ 10⁻¹⁶

0.8% Hg Br₂

IONIZATION EXCEEDS ATTACHMENT

Ne Ar
Figure 15. Theoretical and Experimental Fluorescence for Neon, 10% Xenon and Argon, 5% Xenon Buffers
discharge excitation of Xe*($^{3}P_{1}$, $^{3}P_{2}$) contributes to HgBr* (B) by a process with unit branching. At E/N = 8 $\times$ 10$^{-17}$ Vcm$^{2}$, Xe* accounts for 40% of the HgBr* (B) fluorescence in the Ne, 10% Xe mix.

Argon, 5% Xe: This mix showed a higher fluorescence efficiency than pure Ar in our experiments. The theoretical curve, again with 30% Xe* branching, is shown in Figure 15. At E/N = 1.4 $\times$ 10$^{-16}$ Vcm$^{2}$ the Xe* contributes ~ 35% of the HgBr* (B) fluorescence.

Because in both Ar*, 5% Xe and in Ne, 10% Xe the HgBr* (B) fluorescence is well modeled, even for substantial Xe* contributions, further confidence is gained in the HgBr$_2$ cross-section set. However, the prospects for using higher Xe concentrations to obtain higher laser efficiency are not good, in view of the low (30%) utilization of Xe* excitation.

d. Specific Fluorescence with Different Buffer Gases

At constant e-beam current density of 0.5 A/cm$^2$, different buffer gas mixtures were used in the capacitor driven discharge. The fluorescence of each mix was integrated over the stable discharge duration before arcing and plotted against discharge electric field (Figure 16). These curves are a measure of the relative lasing specific energy to be expected in the different buffer gases. Although the Ne, 10% N$_2$ buffer gives the highest potential specific energy, the relative fluorescence efficiency (Figure 17) is five times less than for any of the rare gas buffers. The poor fluorescence efficiency in Ne, 10% N$_2$ led us to discontinue work on this mix.

e. Laser Performance with Different Buffers: Choice of Argon

Although the fluorescence efficiency is very constant for different rare gas buffer mixtures, the lasing performance and discharge stability are substantially different. Relative laser intrinsic efficiency is shown in Table 1 for 0.8% HgBr$_2$ in 2 Aramagat of various buffer mixes. Also included is a 1.6% HgBr$_2$ in 1 Aramagat Ar data point.
Figure 16. Integrated Fluorescence with Different Buffers at Constant E-Beam
Figure 17. Experimental Relative Fluorescence Efficiencies for Different Buffers
## Table 1. Relative Laser Intrinsic Efficiency of Different Mixes

<table>
<thead>
<tr>
<th>Buffer Gas</th>
<th>Percent HgBr₂</th>
<th>E/N (V/cm²)</th>
<th>Relative Intrinsic Efficiency</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 Amag Ar</td>
<td>0.8%</td>
<td>1.1 x 10⁻¹⁶</td>
<td>1.0</td>
</tr>
<tr>
<td>2 Amag Ar, 3% Xe</td>
<td>0.8%</td>
<td>1.0 x 10⁻¹⁶</td>
<td>0.74</td>
</tr>
<tr>
<td>2 Amag Ne</td>
<td>0.8%</td>
<td>6.4 x 10⁻¹⁷</td>
<td>0.69</td>
</tr>
<tr>
<td>2 Amag Ne, 5% Xe</td>
<td>0.8%</td>
<td>6.7 x 10⁻¹⁷</td>
<td>0.61</td>
</tr>
<tr>
<td>1 Amag Ar</td>
<td>1.6%</td>
<td>9.2 x 10⁻¹⁷</td>
<td>0.74</td>
</tr>
</tbody>
</table>
The highest laser output energy and highest efficiency were both achieved with the pure Ar buffer. The addition of Xe to either Ar or Ne had the effect of reducing laser efficiency rather sharply. This appears to be the consequence of a Xe$_2$ molecular absorption at the laser wavelength, although this point was not pursued in the present study.

The data for 1 Amagat Ar is almost identical to that for 2 Amagat Ar + 3% Xe, both showing lower efficiency and energy loading than for 2 Amagat Ar. In our kinetic model the efficiency difference at 1 Amagat Ar is explained by a lower deactivation rate for the lower laser level.

The sidelight depression for the Ne buffer indicated a slower deactivation rate of the lower laser level than for Ar. This fact, coupled with the relatively lower energy loading obtainable in Ne ($\sim$ 0.5 of that in Ar) implied that in order to achieve specific energies of up to 2 J/l in Ne, a Ne density of 4 Amagat would be required. By contrast, Argon gives 2 J/l at 2 Amagat.

**f. Framework of Laser Kinetic Model for Argon/HgBr$_2$**

Coupled rate equations were written for the populations of atomic and molecular species, ions, electrons, and the spatially averaged cavity photon flux (averaged in the propagation direction). The photon equation is derived in Ref. 14. A list of the species followed is given in Table 2. The populations of HgBr$_2$ (6.4 eV) and HgBr$_2$ (5 eV) states were assumed negligible because of their fast relaxation into products. The coupled equations were solved using the Gear routine "DIFSUB" for stiff systems. Solution time was typically 2 s on an IBM 3700.

Excitation rates for the HgBr$_2$ processes were computed by a Boltzmann routine which had been tested carefully for a wide variety of gases against experiment and other codes. In order to avoid repetitious calculations of Boltzmann solutions, a rates table was compiled for ranges of HgBr$_2$ concentration and kN.
TABLE 2. LIST OF SPECIES FOLLOWED IN KINETIC MODEL

Ar, Ar*, Ar₂*, Ar⁺, Ar₂⁺

HgBr₂, HgBr₂** (7.9 eV), HgBr₂⁺

HgBr (X) v ≈ 0, HgBr (X) v ≈ 22, HgBr (B)

Br, Br₂, Br⁻, electron density, photon flux
Stepwise voltage changes were applied to the discharge to approximate the smooth experimental waveform. At each voltage change the table was consulted by log-log interpolation to derive new excitation rates, drift velocity, characteristic energy, and ionization and attachment rates. The errors introduced by the interpolation were \( \leq 5\% \).

In order to model the effects of nonuniform e-beam deposition in the anode to cathode direction, the space was divided into 8 segments and a separate laser kinetic code was run in each segment. The segment \( E/N \) values were calculated by an iteration procedure which used the running electron density in a segment and consulted the Boltzmann table for the drift velocity. This segmentation with ordinary differential equation solutions is appropriate when

\[
v_d t_p \leq d
\]

where \( v_d \) is the electron drift velocity, \( t_p \) is the duration of the discharge pulse and \( d \) is the thickness of a segment. If Eq. (1) were not satisfied, the proper accounting of particle flux between segments would require the use of a partial differential equation approach. Further, the segmented model does not account for optical flux between segments, and is therefore only strictly applicable to plane-plane optical cavities where the individual segment has a large Fresnel number. The comparison with the 1 m x 8 cm cavity experiments is valid by these criteria.

The existence of simultaneous lasing on the 502 and 504 nm lines has been considered. Because the saturation flux is almost identical for these lines (see Section II-A-2-h) for the experimental gain cross section they obey the same photon equation. Also, because of our experimental evidence (from single

line extraction, Section II-A-2-o) and other work on narrow band operation, (15) the terminal vibrational levels are considered to be homogeneously broadened. As a consequence we may add the photon equations for 502 and 504 nm to obtain a single equation which represents the flux integrated over lasing wavelength. This will be compared to experiments which are "broadband," but it also accurately represents the single wavelength behavior of the system.

The dominant kinetic processes are shown in Figure 18. The experimental evidence for this scheme will be described, process by process, with modeling of the experiment where appropriate.

9. Formation Efficiency: Absolute Measurement

The arguments for direct excitation have been given in Section II-A-2-b. However, the absolute value of formation efficiency has not been discussed in detail. An absolute measurement of formation efficiency was made in order to "close the circle" of the separate measurements of quenching, absorption and laser efficiency.

Using the "cable gun" pulser with a 1 x 1.2 cm discharge cross section, sidelight was measured in a geometry defined by two circular apertures (Figure 19). The photodiode was calibrated (+15%) using repetitively-pulsed dye laser (at 502 nm) of measured pulse shape and average power. Uncertainty in the collection volume was +10% after corrections had been made for the transverse variation of the discharge as determined by photography. The discharge current and voltage monitors each had an uncertainty of <10%. The time dependence of fluorescence was accurately modeled by the kinetic code (Figure 20) in order to derive the formation efficiency. In this calculation electron quenching of HgBr\(^{+}\)(B) was zero (Experiment, Section II-A-2-j) and quenching by HgBr\(_2\) was given the rate \(2.0 \times 10^{-10}\) cm\(^3\) sec\(^{-1}\) (16,17).

Figure 18. Kinetic Scheme for HgBr$_2$/Argon Laser
Figure 19. Geometry for Absolute Fluorescence Measurement

\[ V_{\text{eff}} = \frac{\pi}{4} \frac{(r_1 r_2)^2}{D^2} \cdot W \]

HgBr\* DENSITY = \( \frac{S}{F} \cdot \frac{1}{V_{\text{eff}}} \cdot \frac{\tau_r}{h \nu} \)

S = PHOTODIODE SIGNAL
F = PHOTODIODE RESPONSE & FILTER TRANS.
\( \tau_r \) = RADIATIVE LIFETIME
Figure 20. (a) Experimental and Modeled Voltage and Current Waveforms
(b) Observed and Calculated Sidelight Fluorescence (without Lasing)
The formation efficiency (= fluorescence power without quenching/discharge power) was determined to be 4.5% (error ± 30%) for 0.8% HgBr₂ in Ar at E/N = 1.2 x 10⁻¹⁶ V cm⁻². This value is too low (by 30%) to explain the observed lasing efficiency when it is used in the complete kinetic model with absorptions. The prediction of laser efficiency will be discussed in Sections II-A-3-c and II-A-3-d where a higher formation efficiency (6.1%) is chosen as a more accurate fit to experiment.

h. Gain Measurement: Stimulated Emission Cross Section

Gain measurements were made on the small-scale device at wavelengths throughout the HgBr band. A tunable dye laser of bandwidth 1 cm⁻¹ was aligned down the discharge axis and its 5 ns pulse was delayed to probe the gain at various times before, during and after the discharge pulse.

1) Measured Small Signal Gain versus Wavelength

Data was taken through the peak of fluorescence in the capacitor driven discharge (Figure 21). The principal gain peaks were at 502 and 504 nm, and gain was observed to vary smoothly near the peaks, indicating a merging of rotational-vibrational transitions at least over the 1 cm⁻¹ bandwidth sampled by the probe laser. At 2 Amagats the pressure broadening of individual lines is also ~1 cm⁻¹ so that this gain measurement did not miss any very narrow high-gain line structure.

Taking the measured HgBr*(B) population in identical experimental conditions (Section II-A-2-g) and allowing for lower level HgBr*(X) ν = 22 population the stimulated emission cross section was found to be \( \sigma_{SE} = 2.1 \times 10^{-16} \text{ cm}^2 \) ± 35%. However, the measured HgBr*(B) population appears to be an underestimate. Using the more accurate formation efficiency of 6.1% (Section II-A-2-g) we obtain \( \sigma_{SE} = 1.6 \times 10^{-16} \text{ cm}^2 \) ± 20% at 502 nm.

2) Stimulated Emission Cross Section by Other Methods

(a) The HgBr fluorescence profile was recorded on a multi-channel analyzer. The details of the band center profile were taken from the data in Figure 21. Using
HgBr LASER IS TUNABLE OVER 100 Å RANGE
MEASURED SMALL-SIGNAL GAIN vs WAVELENGTH

Figure 21. Measured Small-Signal Gain Near Band Center
\[ \int \sigma d\lambda = \frac{\lambda^4 A}{8\pi C} \]

where \( A \) equals spontaneous emission rate, \( \lambda \) equals wavelength, we calculate the peak \( \sigma_{SE} = 2.0 \times 10^{-16} \text{ cm}^2 \pm 30\% \).

(b) The lasing buildup time is obtained from sidelight fluorescence (Figure 27) and the simulation of this buildup time from spontaneous noise levels required \( \sigma_{SE} = 1.6 \times 10^{-16} \text{ cm}^2 \pm 30\% \).

3) Measured Small-Signal Gain versus Time

With the dye laser tuned to 502 nm the temporal behavior of the gain was studied. As expected, the gain precisely followed the sidelight (Figure 22). This behavior indicated that there was a steady state rapid depopulation of the lower laser level, as was confirmed in the measurement of sidelight depression (Section II-A-2-k).

i. Absorption Measurements

The dye laser was employed in a double pass collinear arrangement and tuned between 530 nm and the line center at 502 nm. Because of residual gain between 502 and 515 nm, absorption measurements were only made between 515 and 530 nm. Residual gain precluded any measurement on the blue side of the line down to 470 nm.

Figure 23 shows the time dependence of the absorption at 520 nm. During the discharge there was a linearly rising absorption, which averaged 0.3%/cm. (In the same experiment the gain reached 10%/cm).

Before the start of the discharge a low absorption of ~0.1%/cm was seen, and this was present with just the e-beam on. At the end of the discharge there was a rapidly growing absorption which was correlated with the discharge arc and persisted for several tens of nsec. In a similar experiment with the PFN driven
Figure 22. Small-Signal Gain vs Sidelight as a Function of Time
Figure 23. (a) Experimental and Modeled Voltage and Current Waveform
(b) Experimental and Computed Absorption for Capacitor Circuit
discharge (Figure 24), arcing was suppressed by the early voltage fall and the absorption did not increase after the discharge pulse, but decreased to a steady value, which held for at least 700 ns.

From the above data we identified the most probable absorbing species as HgBr$_2^+$ (the dominant ion), and HgBr(X). Further evidence on the intrinsic laser efficiency as a function of e-beam current density also confirmed the assignment of an absorption to HgBr$_2^+$. It had been expected from the structure of HgBr that a visible HgBr(X A) absorption would exist. A similar process has been predicted for HgC$^+$ and degrades the HgC$^+$ laser efficiency.

The kinetic code was run with varying absorption cross sections for the two processes, to give the theoretical curves in Figures 23 and 24. From this procedure, the measured absorptions at 520 nm are

$$\sigma(\text{HgBr}_2^+) = 2 \times 10^{-18} \text{cm}^2$$

$$\sigma(\text{HgBr}(X)) = 5 \times 10^{-20} \text{cm}^2$$

In our initial modeling of the lasing behavior at 502 nm, it was assumed that the 520 nm absorptions applied. This was suggested by the less than 30% variation of the measured absorptions from 510 to 515 nm, and, in case of the HgBr(X A) absorption, the expectation that the absorption is a broad continuum.$^{(18)}$ All aspects of the lasing behavior are modeled reasonably well using these absorptions. However, detailed modeling of the intrinsic laser efficiency as a function of e-beam current density (Section II-A-3-c) and also of the electrical efficiency, Section II-A-3-k) has led us to use $\sigma(\text{HgBr}(X) = 3 \times 10^{-20} \text{cm}^2$, $\sigma(\text{HgBr}_2^+) = 2 \times 10^{-18} \text{cm}^2$ at 502 nm.

Figure 24. Experimental and Computed Absorption for PFL Circuit
The relative excitation curves of Figure 9 show that over 80% of the discharge power goes into the production of HgBr(X), which absorbs.

j. Electron Quenching

An upper bound was placed on the rate constant for HgBr*(B) + e− → HgBr(X) + e− of KQ = 5 x 10^{-9} cm^3 sec^{-1}. Using the PFM driven discharge (Section II-A-2-a), the e-beam current density was varied between 0.6 A/cm^2 and 2.4 A/cm^2, and the fluorescence efficiency monitored. In order to have an accurate comparison between the different e-beam cases, an externally controlled e-beam attenuator was used, which allowed different current densities to be used with the same gas fill of HgBr_2 (0.8%) and Ar.

The data is shown in Figure 25, where the e-beam current density has been translated into electron density using the kinetic code. When KQ = 0, the fluorescence rises slightly with increasing e-beam, due to the recombination channel into HgBr*(B). Kinetic code runs for KQ = 1 x 10^{-8} cm^3/sec are shown (dashed curve), giving an upper bound on KQ of 5 x 10^{-9} cm^3 sec^{-1}. This result is for a typical operating E/N, where the characteristic electron energy from the Boltzmann calculation is 6.3 eV.

k. Lower Level Deactivation

The existence of a relatively high sideload level during lasing is evidence for a 'bottleneck' in the deactivation of HgBr*(X) v = 22, the lower laser level.

In experiments with a PFM driven discharge, sideload was monitored as a function of e-beam current density, with and without lasing. The lasing was with HgBr* − → HgBr(X) to avoid rapid pulse build-up and high intrinsic flux. Traces of sideload fluorescence with and without lasing are shown in Figure 26 data which shows a somewhat similar dependence as shown in Figure 1. The sideband peak to peak current density was 0.40 independent of the laser power.
Figure 25. Fluorescence vs Electron Density: an Upper Bound on Electron Quenching
Figure 26. Experimental Sidelight Depression as a Function of Discharge Power
A computer simulation of the same experiment is shown in Figure 27. The lower laser level was given the deactivation process HgBr(X) v' + Ar → HgBr(X)v" + Ar with a rate constant of \(6.0 \times 10^{-12}\) cm\(^3\)/sec.

The simulated sidelight depression varied between 0.35 and 0.37, at different discharge powers. A correction was applied to the experimental sidelight depression to allow for the transverse variation in discharge power, which accounted for less intense lasing in the discharge fringe regions. After this correction the true experimental sidelight depression in the most intense region of lasing was estimated to be 0.35, which was used to fit the deactivation constant.

1. **Recombination**

It was estimated that the dominant discharge ion species was HgBr\(^+\), and that recombination occurred principally via HgBr\(_2\) \(\overset{4}{e} \rightarrow \text{HgBr}_2^{**}\) followed by dissociation on a rapid timescale into:

1. HgBr\(^*(B)\) with branching 0.2
2. HgBr(X) + Br with branching 0.8

By analogy with similar processes the recombination was estimated to be:

\[
10^{-6} \left(\frac{T_{\text{GAS}}}{\varepsilon}\right)^{\frac{1}{2}} \text{cm}^3 \text{sec}^{-1}
\]

where \(T_{\text{GAS}}\) is the gas temperature and \(\varepsilon\) is the electron characteristic energy (\(\text{eV}\)). Because the characteristic energy was in the range of 5 eV, the effective recombination rate coefficient was \(~ 1 \times 10^{-7}\) cm\(^3\)/sec\(^{-1}\). This gave the observed attachment-dominated discharge conditions (Section II-A-2-n), except possibly at the higher e-beam current densities (\(\geq 2\) A/cm\(^2\)), where there were indications that a slightly lower recombination coefficient might apply.
Figure 27. Computed Sidelight Depression as a Function of Discharge Power
In principle, dissociative attachment could occur by two processes:

1. \[ \text{HgBr}_2 + e^- \rightarrow \text{HgBr(X)} + \text{Br}^- \]
2. \[ \text{HgBr(X)} + e^- \rightarrow \text{Hg} + \text{Br}^- \]

However, theoretical analysis\(^{(19)}\) has shown that there is no curve crossing to allow process (2) to occur, and that it should have a very low rate. The attachment rate for process (1) had been the subject of a number of measurements,\(^{(6,7,20)}\) not all in agreement, so a new measurement was undertaken in discharge conditions relevant to the HgBr laser. The capacitor driven discharge was run at relatively low E/N (4.5 x 10\(^{-17}\) Vcm\(^2\)) and the current was monitored following the e-beam termination. The current decayed exponentially and an attachment rate of 1.1 x 10\(^{-10}\) cm\(^3\)/sec was deduced at the operating E/N. This value was close to that predicted by the Boltzmann code, using 1.1 times the UTRC cross section (Section II-A-2-b).

Experimental constraints prevented accurate attachment measurements at either higher, or lower E/N values. The predicted attachment rate (Figure 28) was relatively constant through the operating E/N range. However, in later experiments on the 1 m device clear evidence emerged for a slope on the attachment rate in the sense that it increased with applied field, with a slope of ~1 in the E/N range 5 x 10\(^{-17}\) - 7 x 10\(^{-17}\) Vcm\(^2\). This is seen in Figure 33(B) where the applied voltage increases after 150 ns and the current dips. Possible explanations for this discrepancy are:

1. The attachment cross section may be modified by vibrational excitation of HgBr\(_2\).
2. A second attachment channel exists via an excited HgBr\(_2\) state, which has been missed in the UTRC cross-section measurement.

---

Figure 28. Computed Attachment vs E/N, and Experimental Point
Further refinement in the discharge modeling will require a re-examination of attachment as a function E/N.

n. Discharge Impedance and Arcing

(1) Discharge Impedance

The kinetic model was able to give a good prediction of the discharge impedance, as determined by experiments with the PFN driven discharge. Without a two-step ionization process we obtained the solid lines in Figure 29. In order to remove discharge geometrical factors and e-beam deposition from this comparison of the model with experiment a separate experiment was performed in pure Ar, which has a precisely known drift velocity and zero attachment. In pure Ar the measured discharge impedance agreed with theory to within 15%, at an e-beam current density of 0.55 A/cm². If we believe that the attachment rate is known to within 20% then it follows that the drift velocity in HgBr₂ mixtures has been predicted correctly to within ± 30%, confirming its calculated two times enhancement over that in pure Ar.

(2) Two-Step Ionization

In Figure 29 the experimental points stop at the E/N at which the discharge arced before the termination of the 120 ns PFN pulse. At the highest e-beam current density the arcing occurred at a substantially lower E/N. This is not explicable by a single-step ionization process, but is characteristic of a two-step ionization process. From photography on the small-scale discharge and streak photography on the 1 m experiment the arcing was shown to be volumetric, rather than in spatial channels.

A two-step process was added to the model by giving a direct ionization process to the 7.9 eV HgBr₂** state. Because the threshold for this process was only 2.7 eV and the characteristic electron energy was 5 eV the process was given a constant rate, independent of E/N. The dashed curves in Figure 29 show the effect of a two-step process rate of $2 \times 10^{-8}$ cm³/sec. (This value is of course dependent on our assumption of a blanket $10^8$ sec⁻¹ decay rate for the 7.9 eV state.) With the two-step process it is possible to cause discharge arcing at decreasing E/N as...
Figure 29. Experimental and Computed Discharge Current. Broken curve includes two-step ionization process.
the e-beam current density increases, in qualitative agreement with experiment. The slope of the computed two-step curves (Figure 29) is too high, but would be modified in the right direction by the use of an attachment rate which increased with increasing $E/N$, as suggested in Section II-A-2-m.

In conclusion, there is good evidence for a two-step volumetric arcing process as the primary limitation on discharge energy loading. The kinetic model predicts discharge impedance to $\pm 20\%$ in the $1 \text{ A/cm}^2$ e-beam range, which is adequate for design purposes, since either $\text{HgBr}_2$ concentration, total pressure, or e-beam current density may be used for "fine tuning" of the discharge impedance, if necessary.

In conclusion, there is good evidence for a two-step volumetric arcing process as the primary limitation on discharge energy loading. The kinetic model predicts discharge impedance to $\pm 20\%$ in the $1 \text{ A/cm}^2$ e-beam range, which is adequate for design purposes, since either $\text{HgBr}_2$ concentration, total pressure, or e-beam current density may be used for "fine tuning" of the discharge impedance, if necessary.

**o. Injection and Single Line Lasing**

Injection serves the twofold purpose of decreasing the laser flux buildup time and locking the oscillator frequency to the injected frequency. In the small-scale experiments the buildup time without injection was $\sim 25 \text{ ns}$, as seen for example in Figure 26. An experiment was performed with a pulsed dye laser tuned to 502 nm to explore the possibilities for increased energy extraction and single line operation.

Without frequency selection the small-scale laser oscillated with an energy ratio 502 nm (62\%):504 nm (38\%). With a 10 ns $10^4 \text{ W}$ pulse of bandwidth $\Delta \lambda < 0.1 \text{ R}$ at 502 nm injected at the beginning of the discharge the energy ratio changed to 502 nm (80\%): 504 nm (20\%) with a frequency narrowing to $\Delta \lambda < 1 \text{ R}$ at 502 nm. Without injection the bandwidth of both lines was $\Delta \lambda \approx 6 \text{ A}$.

Additionally an increase of 10\% (40 to 44 mJ) occurred in the total output energy. A higher injection power would have been needed to extract the further 10\% of energy still being lost through buildup time.

Figure 30 shows the sidelight and laser pulses at 504 and 504 nm, with and without injection. A measure of the effect is the decrease in the initial sidelight level, which is due to a higher intracavity flux at early times.
LASER OUTPUT WITH AND WITHOUT INJECTION AT 502 nm

<table>
<thead>
<tr>
<th>NO INJECTION</th>
<th>WITH INJECTION</th>
</tr>
</thead>
<tbody>
<tr>
<td>TOTAL SIDELIGHT</td>
<td>TOTAL SIDELIGHT</td>
</tr>
<tr>
<td>504 nm LASER</td>
<td>504 nm LASER</td>
</tr>
</tbody>
</table>

Figure 30. Sidelight and Laser Output vs Injected Power
Evidence from this experiment and also from other work shows that complete energy extraction will be possible on a single line (502 nm) at very nearly the same efficiency as is observed with two wavelength extraction. This is good evidence for the rapid vibrational mixing of the terminal laser levels, which already is thought to be faster than the $3 \times 10^8$ sec$^{-1}$ overall decay of the lower laser level (Section II-A-2-k).

In conclusion, energy loss due to cavity buildup time can be recovered; energy can be extracted in one line with little loss in efficiency; and narrow banding down to 0.2 Å should not present any problem.

p. Voltage Standoff Recovery

The flow velocity required for the gas moving through the discharge region is established by two criteria. One is the amount of time required for the recovery of medium homogeneity. The other is the distance that discharge heated gas must be moved after each pulse so that there is no possibility of arcing through this hot gas region during the next pulse. Since the flow power goes up as the cube of the flow velocity, it is important to determine the lower bound on the flow velocity (flush factor) set by each of these criteria. The potential difficulty of downstream arcing through the discharge heated gas was investigated by a series of experiments conducted on the small-scale device.

In these experiments, two voltage pulses were applied to the discharge electrodes. The first with the normal e-beam current, and the second, 2.5 to 5 ms later, without the e-beam. The voltage applied during the first pulse was the normal 6 kV/cm. In excess of 10 kV/cm could be applied during the second pulse without seeing any signs of breakdown. Since the 2.5 ms pulse separation correspond to a 400 Hz rep-rate, it is clear from these experiments that when e-beam controlled discharge is used arcing through discharge heated gas is not a consideration in establishing the gas flow velocity in the HgBr laser system.
1. L M Device Experiments

a. Summary

An extensive range of experiments has provided a solid database for HgBr laser modeling and scaling predictions:

1. Discharge power has been supplied by
   a) Capacitor
   b) 150 ns 0.6 \(\Omega\) Cable PPN
   c) 300 ns 0.6 \(\Omega\) Cable PPN
   d) 300 ns modified PPN

2. E-beam current density has been varied from 0.5 A/cm\(^2\) to 4 A/cm\(^2\).

3. Discharge polarity, magnetic field, HgBr\(_2\) density and e-beam voltage have been varied as parameters.

4. The laser pulse shape, energy and output spatial distribution have been measured.

5. Streak photographs have been taken to explore the onset of arcing and its dependence on the above parameters.

6. The e-beam spatial deposition pattern has been measured.

The lasing performance will be discussed in more detail in subsequent sections. Here we give the efficiency definitions and summarize the best lasing performance. All data is with Argon buffer at 2 Amagat.

Definitions:

Electrical efficiency = \(\frac{\text{laser output energy}}{\text{energy stored in PPN}}\)

Intrinsic efficiency = \(\frac{\text{laser output energy}}{\text{discharge energy during lasing}}\)

The latter definition is useful because there is a < 10 ns delay between discharge power and fluorescence power, and the fluorescence decay rate (including quenching) is \(\sim 1 \times 10^8\) sec\(^{-1}\).

The electrical efficiency is less than the intrinsic efficiency for four principal reasons:

1. A portion of the energy can be stored in the PPN and discharge.

The most important of these is estimated to be

\[A_{\text{vco}} < \text{VPP} \leq \text{VPP}\]
2. Energy is reflected from the discharge back into the PFN by impedance mismatch. This loss tended to be higher for the highest e-beam cases.

3. Energy is lost during the buildup time for lasing. This is typically 30 to 60 ns in the present experiments.

4. Energy is lost if an arc prematurely terminates the discharge before the PFN has unloaded.

Highlights:
1. Maximum Energy: 9.8 J at 1.9% electrical efficiency (3.0 ns modified PFN, 2.6 J/μs)
2. Maximum Intrinsic Efficiency: 3.2% at 7.0 J (300 ns modified PFN, 1.4 J/μs)
3. Maximum Electrical Efficiency: 2.4% at 3.5 J (150 ns PFN, 0.7 J/μs)

Experimental Equipment and Methods
The experimental scheme is shown in Figure 31. Details will be noted under separate headings.

Laser Cavity: The total cavity volume was 40 ft³. Its body was of stainless steel, with viton and PTFE "O" rings and window cages. Two 7" fused silica windows were aligned accurately parallel to the laser mirrors, which were plane, and mounted externally. All the results to be discussed were taken with a 99% reflector and a 35% reflector at a separation of 206 cm. The body of the cavity was heated to 450°F and the HgBr₂ density was set by the temperature of a "sidearm" reservoir.

Electrodes: The electrode next to the e-beam foil was a stainless plane mesh of 50% transmission, and hole size 1 mm. The other electrode had a change profile designed for a 10% uniformity in electric field over a width of 7 cm. Its material was stainless steel. Beyond a machine stop-noise, no special care was taken to ensure a clean surface, and it fact electrode roughness had no effect on discharge current shape, even when the polarity was reversed. The electrode profile was...
E-BEAM CONTROLLED DISCHARGE PUMPING

SCREEN DISCHARGE CATHODE
ACTIVE VOLUME
DISCHARGE ANODE

E-BEAM

 FOIL

J6728
was normally 4 cm, but was reduced to 4.5 cm for the experiment on
impact energy loading as a function of e-beam deposition uni-
versity. The electron beam was 1.5 cm overall.

Experimental: The e-beam had a maximum voltage of 320 kV, total
current of 2 mA and was pulsed with a pulse duration of 1 µs.
For 1 cm of target density, the A cm² was reduced to the
value at 0.25 cm of water for the purposes of attenuation.
An Amat 200 system was used. The filament current was
increased with a certain amount. Better measurements of energy
were available if the target and the gas in the gas were made
by using a permanent magnet. Two experiments were set up in
the experiments.

A summary report and the report of Amat 200 was
presented in the summary report.
ENERGY STORED = 3.25 J/ns AT 90 kV
TOTAL SERIES INDUCTANCE \approx 40 \text{nH}

T_R \approx 35 \text{ ns}
Z_0 \approx 0.6 \Omega

Figure 32. Schematic of 1 m Cable Pulser
voltage and current were compatible with the 0.6 PFN impedance and accurately calibrated charge voltage.

**Laser Energy Measurement**: The calorimeter was a Scientech Model 36-0401, 4" thermopile used with a Model 36-4002 indicator. The following methods of calibration were used:

1. Use of dc substitution power to heat the 91.281 Ω Manganin wires embedded in the calorimeter head. The dc supply voltage was calibrated with an HP Model 6920B calibrator (+ 1% traceable to NBS). A correction for 98% absorption in the visible was applied. The overall calibration accuracy was ± 2%.

2. Pulsed substitution energy from a capacitor (known to ± 5%) charged to a known voltage (+ 1%) and discharged into the manganin heater wires. Overall accuracy ± 5.4%.

3. Comparison with another Model 36-0401 calorimeter.

In the measurement of laser output energy the entire laser beam impinged on the calorimeter surface and no assumptions were made on its spatial homogeneity.

The laser temporal pulse shape was measured with a Hamamatsu Model R617-02 vacuum photodiode terminated into 50 and displayed on a Tektronix Model 7844 oscilloscope.

**Efficiency of Energy Transfer**: Typical voltage, current and laser intensity traces are shown in Figure 33. In that figure, part A resulted from the use of a simple PFN which consisted of the paralleled cables described in this section. The discharge impedance dropped by approximately a factor of 2 during the pulse. Part B refers to the use of a matched impedance line pulser, referred to here as a modified PFN, where the net result is an extremely good average impedance match to the discharge. The present experiment has demonstrated that ~ 95% energy transfer can be achieved from a cable energy storage device to a typical laser discharge load where impedance is falling off. In the case of the Ruby laser an added advantage of keeping E/N high is the relatively greater laser efficiency at high E/N.
(A) SIMPLE PFN

(B) MODIFIED PFN

DISCHARGE VOLTAGE SIMPLIFIED CURVE
DISCHARGE CURRENT SIMPLIFIED CURVE
Without the modified PFN, laser intrinsic efficiency was substantially lower in the second half of the pulse.

c. Laser Intrinsic Efficiency

The intrinsic efficiency is defined in Section II-A-3-a. Figure 34 shows the observed intrinsic efficiency as a function of E/N and e-beam current density. We note that the experimental efficiencies lie below the curve (dashed line) derived from the formation efficiency as a function of E/N (Section II-A-2-b) multiplied by 0.65, the energy extraction in the absence of absorption (Section II-A-2-c). At increasing current density the ion absorption (Section II-A-2-a) reduced the intrinsic efficiency. The kinetic code predictions are shown in Figure 35 for 0.6% HBr, 1.0 Amulet Ar and 0.3% reflectivity output mirror. Further computer simulation verified that 0.15 was the optimum output reflectivity for the e-beam current density of 1.7 Am, and close to optimum for the other cases. From the comparison with experiment Figure 34 we conclude that the ion absorption has been accurately modeled, but that possibly the HBr/Xe absorption could be improved by a factor of 2 or 3, etc. The detected gas mixture is shown in Table I.
1.8 AMAG. Ar, 0.8% HgBr₂

E-Beam
- 0.9 A/cm²
- 1.7 A/cm²
- 4.0 A/cm²

MAX 7.5 J
MAX 9.8 J
MAX 6.5 J

LASING 1 → 2 J/l
VOLUME 5 l
Figure 7: Computed Intrinsic Efficiency vs E/N
Figure 36. Experimental Laser Energy vs PFN Stored Energy
Figure 37. Shot-to-Shot Reproducibility of Laser Output
The fractional variation was less in the 8 J to 10 J energy range because of the relatively smaller contribution of the calorimeter zero fluctuation at these energies.

There was a slight decline in output during this sequence, which we believe was due to the use of a stainless steel chamber and viton "O" rings which upset the HgBr equilibrium chemistry by binding Br atoms. There are several possible ways in which Br depletion can reduce the laser efficiency:

1. By leaving free Hg or Hg\(_2\)Br\(_4\) in the vapor phase, which alters the electron energy distribution and hence the excitation efficiency of the 6.4 eV HgBr\(_2\) process.

2. By causing the production of volatile bromides which absorb at the laser wavelength.

3. By reducing the HgBr\(_2\) density (at an E/N value where the formation efficiency reduces with reduced HgBr\(_2\)).

A further, less likely, possibility is that chamber outgassing produced enough N\(_2\) to affect the formation efficiency. As little as 0.5% N\(_2\) in Ar reduced the formation efficiency by 20% in an experiment on the small-scale device.

Contamination issues are addressed in Section III-J of the proposed 2 J design.

f. Discharge Energy Loading Limits

During the course of the 1 m experiments insight was gained into the factors affecting energy loading in HgBr\(_2\)/Ar sustained discharges. Streak photography confirmed that the arcing which limited energy loading was truly volumetric and indicated its dependence on the uniformity of e-beam deposition.

The deposition uniformity will be defined as the ratio of deposition at the electrode furthest from the e-beam entry foil to the deposition adjacent to that foil. A measurement of deposition, described below, gave a uniformity of 0.6 for the 0.5 mm anode-cathode spacing and a uniformity of 0.4 for the 1.0 mm spacing. The uniformity was estimated to be 0.4 for the 2.0 mm spacing of the small-scale experiment.
The energy loading for a given e-beam current and deposition uniformity was a weak function of either E/N in the range $5 \times 10^{-17} - 8 \times 10^{-17}$ Vcm$^2$, or HgBr$_2$ concentration in the range 0.4% to 1%. This suggested the graphical presentation in Figure 38 for the experimental energy loading limits. Maximum energy loading occurs at $\sim 2$ A/cm$^2$. The physical reason for such a maximum is the rise of a two-step ($n_e$ dependent) arc-in process as the e-beam increases, which offsets the stability gained by having a source-dominated ionization rate.

The discharge energy loading degrades with decreasing deposition uniformity, but is still tolerably good at 0.6, where most of the 1 m device experiments were performed. The major effect of nonuniformity is to cause high electric fields in regions of low deposition, which then have a higher ionization rate. As the electron density becomes more uniform, the power input to the thin deposition regions is relatively increased, leading to a two-step ionization runaway. The streak photography supports this picture, as does the spatially-dependent modeling described below.

Figure 38 represents the upper bound in discharge energy loading that applies for any given pair of e-beam and deposition uniformity. It is necessary to accurately predict the uniformity for the purpose of testing, and thus capability of the chamber layout and discharge uniformity control.

A diffusion equation (1.1) is solved for the electric fields, and

$$E(r) = \frac{\phi}{\sigma}$$

where $E(r)$ is the electric field at a point $r$, $\phi$ is the potential at that point, and $\sigma$ is the conductivity. This equation is solved numerically, and the resulting fields are used to calculate the energy loading and deposition uniformity.
2 AMAG. Ar, 0.5 → 1% HgBr₂

UNIFORMITY 0.9

UNIFORMITY 0.6

ENERGY LOADING

DISCHARGE ENHANCEMENT

E-BEAM A/cm² (ENTRY SIDE)
Figure 11. Electrical Characteristic Comparison
In subsequent studies, it was found that the introduction of a spatial distribution of the impinging ion flux, with a reduction of the energy spread, led to a significant improvement in the performance of the target. A computer simulation, as described in Section 11-A-1, predicted that the device could operate with spatial uniformities greater than 1%, differing from a uniform volumetric arc.
Figure 40. Streak Photograph of Spatial Arc Caused by Nonuniform Deposition

CONDITIONS

2 AMAGAT Ar
15 torr HgBr₂
E BEAM 15 A cm², ENTERING THROUGH ANODE
ANODE CATHODE SPACING 8 cm
CABLE VOLTAGE 70 kV, PFN 150 ns
The beam current proved to be a good monitor of e-beam energy input, as the increase in discharge voltage. Low Light concentrations were used (4 x 10^3 erg/cm^2) in the ArA fast Ar. It was verified that the beam intensity was linear to e-beam current density. Also, the time scale for beam formation from excited states were sufficiently fast to give time-resolved depo-
sition, during the e-beam pulse.

Pulse beam was viewed by photomultiplier through a narrow collimator and two aligned pinholes which gave a spatial resolution of 0.1 cm in the deposition volume. Vertical and horizontal scans were made through the discharge aperture and iso-
deposition contours interpolated between data points. Care was taken to shield the photomultiplier from x-rays, and a small correction was made for the measured effect of the steady applied magnetic field on PMT gain.

Data were taken for a uniform 2G magnetic field case (Figure 41) and also for a diverging field case (600 G at the e-beam entry side and 500 G at the opposite electrode (Figure 42).

The highest discharge energy loading was actually achieved using the diverging field, for a reason connected with the self-
field of the discharge current (up to 300 G) which was in a direction to slightly pinch the e-beam in the discharge cell. This effect does not show up in the deposition experiment, where there is no discharge current. However, it is evident in the spatial dependence of the laser output on applied magnetic field (Section II-A-3-i). Evidently, the diverging field counteracts the pinching effect, to create optimum discharge uniformity.

In general, the magnetic field is necessary to obtain the best overall efficiency from the sustained discharge HgBr laser, for the following reasons:

1. By guiding the e-beam into the cell through the foil aperture, the e-beam power requirement is minimized.
Figure 41. Measured E-Beam Deposition with Uniform Magnetic Field
Figure 42. Measured E-Beam Deposition with Diverging Magnetic Field
The accurate prediction of the evaporation rate is clearly important in the process, which is discussed below.

1. Modeling of E-beam Deposition

Using an e-beam deposition code which has been developed under internal funding we are able to predict deposition in good agreement with the present experiment. The results of such a computation are shown in Figure 44, which applies to precisely the experimental conditions of Figure 41. The same code has also given excellent agreement with another well-documented deposition experiment at 600 kV without a magnetic field.

Without going into details of the code at this point we shall use its results to design the magnetic guide fields which control the discharge volume, confident of a deposition accuracy of better than ± 10%.

2. Laser Output Spatial Profile

Photographic measurements were made of the laser output on a white screen at 2.5 m beyond the output mirror. The laser cavity was plane-plane and produced a well-collimated beam whose intensity profile reflected the spatial distribution of discharge power across the laser aperture. The film was calibrated for quantitative intensity measurements by the use of known neutral density filters.
Figure 43. Computed E-Beam Deposition for Uniform 1 KG Magnetic Field
The pulse duration is too short for a discharge to develop, if the electrons move only with a fraction of the ionization of the discharge.

This result re-emphasizes the importance of accurate deposition modeling (Section II-A) since it shows precisely what is required to achieve an essentially spatial uniformity in the 2 J design. We note that the discharge self-fields are ~100 G, and that we are designing for a 4 KG guide field, so that the e-beam deposition is not affected by self-fields in that case.

k. Modeling of Anode-Cathode Variation in Lasing

The laser output spatial profiles (Section II-A-3-j) show a pronounced intensity variation between anode and cathode. The cause of this is the nonuniformity of e-beam deposition, which
Figure 44. Measured Spatial Distribution of Laser Output with 800 G Magnetic Guide Field
Figure 45. Measured Spatial Distribution of Laser Output with No Magnetic Guide Field
leads to an initially higher E/N near the larger electrodes and hence to more efficient lasing. The reasons for this are as follows:

(1) Higher E/N causes increased extraction efficiency.
(2) Higher initial gain causes increased extraction.

In addition, the discharge power Ri increases slightly with E/N because the current density is increasing in the anode-cathode direction. The combined effect of increased extraction and increased Ri cause the observed gratation in the laser buildup with the very strong function of the electrode area and E/N.

The laser buildups obtained when the laser was operated on observed anode-cathode intensity pattern. The laser was divided into eight segments, in each of which a different laser was run, with the appropriate E/N and Ri at a given condition. The application of the model to one such case is given II-A-1.

The application of the model to the electrodes will be discussed. The measured decommissioned E/N at the II-A-1 has been shown. The computed evolution of the E/N distribution field is shown in Figure 16, where it is noted that the initial field distribution rapidly relaxes into a more uniform distribution which persists stably for the duration of the 10-ns applied pulse at constant 2.0 kV total anode-cathode voltage. This is accounted for by the relatively higher ionization rate in the burn E/N region. The energy distribution from the same run is shown in Figure 17, for t = 150 ns and t = 100 ns. We note that good overall agreement is obtained in the anode-cathode energy variation, apart from the edge regions near the electrode which suffer optical losses in the experiment, but not in the simulation. At 150 ns it is striking to note that the variation is much greater, and this is traceable to the substantially faster laser buildup in the region of low deposition.

We conclude that the reasons for the observed anode-cathode laser variation are well understood and that the code will predict
Figure 46. Computed Evolution of Local Field Between Anode and Cathode
E-BEAM 17 A/cm² 0.6% Hg Br₂
DISCHARGE 32 kV 1.8 AMAG. Ar

**EXPERIMENT**
(9.8 J, 19%)

**THEORY**
(9.6 J, 1.95%)

Distance (cm)

0 1 2 3 4 5 6 7 8

Laser Output, Joules/Segment

Relative Deposition

1.0 94 88 .82 .76 .70 .66 .60

160 ns

AVCO EVERETT
this variation accurately for different e-beam deposition uniform-
ities. In the proposed 2 J design the deposition uniformity is
0.8 and the presence of injected light eliminates the buildup dif-
ferences, so that an energy uniformity of better than 0.95 is pre-
dicted in the anode-cathode direction.

The laser electrical efficiency was discussed in Section
II-A-3-d, but modeling of the efficiency has been delayed to the
present section to include correctly the anode-cathode variation.
As seen in Figure 47 the electrical efficiency is predicted to be
1.95%, after allowance has been made for an energy transfer factor
of 0.95 from the PPN to the discharge. In order to obtain this
agreement with experiment, the formation efficiency (Section
II-A-2-g) had to be modified to 6.1%, slightly higher than the
5.3% used in the cross section derivation, and higher again than
the 4.3% derived from the absolute fluorescence measurement. How-
ever, the errors in the absolute fluorescence measurement are con-
sidered to be ± 30%, whereas the measurement of laser electrical
efficiency is accurate to better than ± 10%. For design purposes
we employ the 6.1% formation efficiency, which gives best agree-
ment with the observed laser efficiency (both intrinsic and
electrical).
III. PRELIMINARY DESIGN OF 2 J, 100 Hz HgBr LASER

A. DESIGN REQUIREMENTS

The preliminary design presented in the following sections meets all the specifications outlined in Table 3. While the lifetime specification is $10^8$ shots, design solutions have always been chosen which are compatible with an ultimate $10^{10}$ shot lifetime.

A number of the subsystems have already been tested to a $10^7-10^8$ shot lifetime under other AERL programs or in other laboratories.

The discharge parameters chosen for 2 J operation have already been explored on the 1 m device experiments (Section II-A-3) in which energy scaling to 9.8 J at 1.9% electrical efficiency was demonstrated. The laser kinetic model (Section II-A) has been verified to a precision of $\pm 10\%$ over a wide range of discharge conditions, and therefore the overall efficiency prediction of 1.19% (Section III-K-I) can be stated with confidence.

It is to be noted that the present 200 W system is only one choice out of a wide spectrum of point designs which can be generated from the generic sustainer discharge concept demonstrated here. For instance, a 10 J, 100 Hz system could have been designed at similar operating efficiency using identical technology.

B. OVERVIEW OF DESIGN

The design considerations were dominated by the available intrinsic efficiency and specific energy loading in the laser active medium. The intrinsic efficiency can experimentally be as high as 3.3% (Section II-A-3-c) with argon as the buffer gas. From the comparison of energy loading in different buffer gases (Section II-A-2-e) it emerged that argon was decisively superior as a buffer when compared to Ne, Ar + 5% Xe, Ne + 10% Xe, giving
### TABLE 3. DESIGN SPECIFICATIONS

<table>
<thead>
<tr>
<th>Specification</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Output Pulse Energy</td>
<td>2 J</td>
</tr>
<tr>
<td>Average PRF</td>
<td>100 Hz</td>
</tr>
<tr>
<td>Interpulse Recovery Time</td>
<td>&lt; 5 ms</td>
</tr>
<tr>
<td>System Efficiency</td>
<td>&gt; 1%</td>
</tr>
<tr>
<td>Beam Divergence (at 80% point)</td>
<td>10 x DL</td>
</tr>
<tr>
<td>Beam Uniformity ± (%)</td>
<td>20</td>
</tr>
<tr>
<td>Bandwidth</td>
<td>0.1 nm</td>
</tr>
<tr>
<td>Lifetime (&gt; 90% power)</td>
<td>10^8 shots</td>
</tr>
<tr>
<td>Wavelength</td>
<td>450 - 510 nm</td>
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<tr>
<td>Wavelength Stability</td>
<td>± 0.01 nm</td>
</tr>
<tr>
<td>Pulse-to-Pulse Intensity Jitter</td>
<td>&lt; (± 10%)</td>
</tr>
</tbody>
</table>
an energy loading of up to 60 J/\text{Amag}. Because it was desirable to work at high discharge enhancement ratio (= discharge power/e-beam power), the discharge design point chosen in Section III-C was not at the highest energy loading point, but was set at 33 J/\text{Amag} where an e-beam current density as low as 0.6 A/cm\textsuperscript{2} could be used (Section II-A-3-f).

The geometry of the laser active medium was chosen after several design iterations in which the overall system efficiency and the optical beam uniformity were calculated. The penetration depth allowed for the e-beam was a compromise between the need for a good deposition uniformity (Section II-A-3-f) and the competing requirement for a high aspect ratio to minimize the flow power. Essential to the deposition uniformity was uniform, reasonably high magnetic field.

The flow loop design (Section III-E) was driven by the optical homogeneity requirements. It was found that 10 X DL could be achieved easily with a very compact flow loop. A detailed plan of this is presented in Figure 57. The principal features of the flow design are sidewall acoustic wave suppression, an upstream velocity stabilizer, and a downstream heat exchanger. Additional medium uniformity was achieved by boundary layer suction upstream of the anode plate.

An unstable optical resonator was chosen (Section II-F) because it offered the required overall beam quality (further discussed in Section III-K). Spectral control was obtained by injection at the required frequency. Injection also raised the optical extraction efficiency by 11%. The injection oscillator itself had only a modest drive power of 240 W (electrical) and was specified as an avalanche discharge laser of simple and rugged design. Detailed consideration was given to the mode matching between the injection oscillator and the unstable resonator.
The e-beam design (Section III-G) was based on a thermionic emitter, which could either be grid-controlled at high voltage (300 kV) or pulsed for the laser duration of 250 ns by a high-voltage pulse transformer. The most important aspect of the design was its resemblance to long-life high-vacuum modulator tubes, which have been adequately proven in other space applications.

A dc magnetic field coil was included in the design in order to increase the laser efficiency and beam uniformity. It acted principally by controlling the discharge shape (as discussed in Section II-A-3-h) and through this it increased the optical beam interception of the discharge power to 92% (Section III-c) and decreased the flush factor to 1.75 (minimum) or 3.5 (average) (Section III-E). For highest efficiency a superconducting magnet was specified, and in Section III-H its design is discussed in some detail. Advantage was taken of the recent development of efficient refrigerators for space usage.

Discharge modulator design is discussed in Section III-I, where the Blumlein and Simple Changed Line circuits are contrasted. It is concluded that the line circuit will better favor long thyratron lifetime. A lumped element PFN was designed which gave the rapid risetime and falltime required for high laser electrical efficiency.

The question of gas chemistry and cleanup is covered in Section III-J. The major problems are identified and the design allows for continuous gas cleanup and monitoring, with a limited makeup of fresh HgBr₂.

Overall system performance is discussed in Section III-K, where an overall laser efficiency of 1.19% is demonstrated.

C. LASER ACTIVE MEDIUM DESIGN

1. Geometrical Trade-off

In this subsection we present qualitatively the trade-offs which lead to the chosen design point for active medium geometry. The flow power decreases with increasing laser specific energy (J/đ) but higher specific energy requires increased e-beam
(Section II-A-3-f). Taking into account the aspect ratio trade-off (below) an optimum specific energy of 1.5 J/l was chosen.

The aspect ratio is \( H/W \) where \( H \) is the discharge anode to cathode dimension and \( W \) is the discharge width in the flow direction. The flow power is minimized for high aspect ratio, since the flow power scales as \( (Wf)^3 \), where \( f \) is the "flush factor". However, the e-beam deposition uniformity must equal 0.8 for the design energy loading, and good uniformity is more easy to achieve with a low aspect ratio.

The physical value of \( H \) is determined by the e-beam maximum voltage constraint and the computed deposition uniformity (Section III-C-3). The e-beam voltage should be high relative to the foil voltage loss. It should also be high in order to minimize the e-beam current and thereby the cathode heater requirements within the total ionization power requirement. We have adopted a 300 kV practical e-beam voltage maximum, and thereby set \( H \) at 6 cm, in order to have good deposition uniformity.

In order to reduce the flow power we have set \( W = 4 \) cm. At 1.5 J/l and 2.25 J potential laser output (actual output discussed below), the active volume must be 1.5 l, implying a length \( L_A \) of 62.5 cm.

The dimensions of the design point laser active medium are: \( H = 6 \) cm, \( W = 4 \) cm, \( L_A = 62.5 \) cm.

2. Laser Efficiency

The code prediction of laser efficiency has been accurately verified in Section II-A-3-k, where it compares well with experiment. The same code has been run for the design point discharge in order to predict electrical efficiency and optimum output coupling. A constant 30 kV has been applied to the discharge representing an operating \( E/N = 0.9 \times 10^{-16} \) Vcm\(^2\). The deposition uniformity is designed to be 0.8, as discussed in more detail below. For our 1.5 l discharge volume, lasing with a specific energy of 1.5 J/l, we require a discharge total energy of 100 J.
Through the dependence of discharge energy on e-beam current density (Section II-A-3-f), we are required to have $J_{EB} \geq 0.6 \, \text{A/cm}^2$ for the requisite energy loading (at 2 Amagat). This consideration leads to the choice of $J_{EB} = 0.6 \, \text{A/cm}^2$ within the discharge. In order to deliver 100 J in 250 ns into the chosen discharge geometry, the impedance must be tuned by varying the concentration of HgBr$_2$ down to 0.32%.

The laser electrical efficiency for these conditions is plotted in Figure 48 as a function of output mirror reflectivity (for a plane-plane cavity). Also shown is the laser energy, numerically equal to the efficiency for the 100 J discharge input. In this calculation a factor of 0.95 has already been inserted, as an estimate of the coupling efficiency from PFN energy to discharge energy. This factor is justified by the experiments we have performed, and has indeed been included in the efficiency modeling of Section II-A-3-k.

The computed electrical efficiency of Figure 48 includes an injected power level of 10 kW/cm$^2$ at the beginning of the pulse, which raises the electrical efficiency by 13%, as discussed in Section III-F. This accounts for the increase over the 2.0% observed electrical efficiencies (Section II-A-3-d). The computed impedance variation is shown in Figure 49.

It is to be noted that 1 m device experimental data exists for the conditions: $J_{EB} = 0.9 \, \text{A/cm}^2$; [HgBr$_2$] = 0.4%; $E/N = 0.9 \times 10^{-16} \, \text{Vcm}^2$ and deposition uniformity 0.8 (anode-cathode spacing 4.5 cm). In this experiment an electrical efficiency of 1.95% was recorded at a specific energy of 1.6 J/J without injection. This is close to the design point and verifies the efficiency predictions in that region.

The modeling described above assumes that the discharge profile is a perfect "top hat" in the direction perpendicular to the anode-cathode axis. In practice there is a narrow roll-off region.
Figure 48. Design Point Energy and Electrical Efficiency vs Output Coupling
Figure 49. Computed Impedance Evolution for Design Point Discharge
which lies outside the optical resonator volume, leading to small losses. This loss factor is calculated accurately in the following section, in which the anode-cathode deposition uniformity is also derived.

3. E-Beam Deposition Profiles

Using the code which has been experimentally verified (Section II-A-3-i) deposition has been calculated for the 4 kG design point magnetic guide field. The transverse isodeposition contours are shown in Figure 50. The cathode plane lies at 1 cm and the anode lies at 7 cm. The cathode screen transmission is unity in this simulation, but is accounted for correctly in the total e-beam energy budget. The anode is given an electron reflection coefficient of 0.3, corresponding to its high Z composition. The primary electron voltage is 300 kV and the simulation includes the scattering and energy losses due to a 1/2 mil Ti foil at 0 cm. The argon density is 2 Amag. Each contour represents 5% of the peak deposition.

Deposition profiles derived from Figure 50 but transverse to the anode-cathode axis are shown in Figure 51. These profiles determine the discharge power profile to a very large extent. Because of two-step discharge ionization, the central 4 cm of the discharge is enhanced by ~ 50% relative to the wings. With allowance for this we may use Figure 51 to show that the 4 x 6 cm optical aperture will intercept the discharge transverse power distribution with 92% efficiency.

4. Anode-to-Cathode Uniformity

Use of the segmented laser model (Section II-A-3-k) allows us to predict the anode-to-cathode variation of laser output power, again assuming plane-plane optics for the purpose of discussion. With an injected laser power of 10 kW/cm² (the result is very insensitive to the precise level of injection) we compute that lasing near the cathode will be at 0.96 of the intensity near the anode, for a deposition uniformity of 0.8.
Figure 50. Isodeposition Contours for Design Point
DEPOSITION PROFILES TRANSVERSE TO THE ANODE–CATHODE AXIS, AT VARIOUS DEPTHS, $B = 4 \, \text{kG}$

Figure 51. Deposition Profiles Transverse to the Anode–Cathode Axis, at Various Depths
The overall spatial uniformity of the laser output will be discussed in Section III-K. At present we note that from consideration of the discharge power distribution alone, the intensity is very nearly uniform from anode to cathode, but has a profile in the transverse direction given on average by the "4 cm" curve of Figure 51. Apart from a slight "roll-off" in the edge 0.1 cm, the intensity uniformity meets the ± 20% V specification, insofar as it is controlled by the discharge power distribution. It is mentioned above that only 8% of the discharge power is not accessed by the 4 x 6 cm optical aperture. This factor reduces the electrical efficiency to 2.08%, giving an actual design output of 2.08 J.
D. LASER CAVITY DESIGN

In this section we describe the details of the laser cavity design together with the various requirements that led to this design. The major components of the cavity include (1) the discharge electrodes, (2) current, and (3) high-voltage feedthroughs.

1. Discharge Electrodes

It has been shown in experiments performed on the 1 m device (see Section II-A-3-j) that if the electric field produced by the discharge electrodes is kept uniform (+5%) in the region of the e-beam, then the discharge energy deposition is determined solely by the e-beam. In the present electrode configuration the electrodes are designed to provide uniform electric fields in the central 4 cm e-beam region. The edges of the electrodes where field enhancement (30% higher than the field at the center) occurs, are brought out to regions where the computed e-beam deposition is <5% of that on the e-beam midplane. A half-cross-section view, in the plane perpendicular to the optical axis, of the electrodes is shown in Figure 52. Also shown are computed vacuum electric field values on the electrode surfaces.

It has also been shown in the 1 m device experiments (see Section II-A-3-i) that the preferred discharge polarity is to have discharge current flow co-linear with the e-beam, that is, to have the cathode closest to the e-gun. In this configuration the discharge electric field is in the direction to accelerate the e-beam electrons. This partially counteracts e-beam stopping by the gas and improves e-beam deposition uniformity.

The cathode must be partially transmitting to the e-beam. It must also be partially transparent to the flow in order that the gas in the region between the foil and cathode is flushed to remove the e-beam heated gas. To prevent the discharge from reaching the foil and to avoid damage from localized pressure waves generated in the event of a constricted discharge arc, the foil must be separated from the cathode by a gap. On the 1 m device a spacing of 1 cm was found to be sufficient for this.
Figure 52. Equipotential Plot of Discharge Region
the foil routinely survived arcs (generated with the capacitor
discharge circuit) with greater than 10 kJ stored energy dissi-
pated in the arc. In the present design the discharge energy is
limited by the PFN to 100 J, so the conditions are much less se-
vere. In addition, arcing is only expected to occur if there is a
fault in the e-beam. In our discharge circuit design we will in-
corporate a discharge inhibit circuit which will prevent discharge
voltage from being applied when an e-gun fault is detected. How-
ever, a spacing of 1 cm is chosen here for safety.

The cathode is heated by the e-beam and by the discharge.
Active cooling is required to cool the cathode to keep its average
temperature to within 0.5°C of the core flow so that the temper-
ature disturbance in the active medium is minimized (see Section
III-E).

The cathode design chosen consists of parallel 1 mm outside
diameter tubes oriented in the flow direction, spaced 1/3 cm apart
in the optical axis direction. The geometrical transmission of
the e-beam through this structure is therefore 67%.

Since the cathode is made up of parallel tubes rather than a
smooth surface, the field produced will be nonuniform close to the
cathode surface. The field produced by such an arrangement can be
calculated.\(^{(21)}\) In Figure 53 we show an equipotential plot in
the vicinity of the cathode. For the present design the electric
field nonuniformity is calculated to be \(\leq 2\%\), 2 mm away from the
cathode surface. Similar nonuniformities existed in the 1 m ex-
periments (see Section II-A-3-i) and were found not to affect dis-
charge stability.

The side of the cathode facing the e-gun will be heated by
the e-beam. Assuming all of the intercepted e-beam power is de-
posited in the surface of the tubes, the heating power per cm\(^2\)
is \(J_b V_{eb}\), where \(J_b\) is the beam current density through the

Figure 53. Equipotential Plot in the Region Near the Cathode
foil and $V_{eb}$ is the beam voltage. For the present design the average power loading on the cathode by the e-beam is $\approx 6$ W/cm$^2$ on the surface of the cathode tubes. On the side facing the anode, the cathode will be heated by the discharge. The power deposited by the discharge is a small fraction of $J_d V_{sh}$, where $J_d$ is the discharge current density on the cathode tube surface and $V_{sh}$ is the cathode sheath voltage drop. In the present design $J_d \approx 120$ A/cm$^2$ and $V_{sh}$ is estimated to be $\approx 300$ V.\(^{22}\) The average power deposited on the cathode tubes by the cathode fall is then a fraction of 1 W/cm$^2$. Active cooling is provided by coolant flow in the cathode tubes to maintain their temperature to within 0.5°C. The instantaneous surface temperature rise immediately after the e-beam pulse can be calculated using the time-dependent heat diffusion equation. For platinum this temperature rise is estimated to be $\approx 70°C$. The corresponding temperature rise on the discharge side is negligible. The instantaneous surface temperature rise will decay by conduction into the tubes in $\mu$s time scale and will not present a problem.

The cathode surface will be bombarded by energetic ions during the discharge and some sputtering will occur. For refractory metals the sputtering rate is typically 10 $\mu$g/coulomb.\(^{23}\) For this application in $10^8$ pulses at 120 A/cm$^2$ and 250 ns pulses, the erosion is estimated to be $3.0 \times 10^{-2}$ g/cm$^2$ of cathode surface or about 0.6 mil loss. The tube used will have a wall thickness of at least 6 mils so sputtering will not be a problem for cathode integrity. Clearly, for $10^{10}$ pulse lifetime the problem is more severe. The solution will be to make the solid electrode the cathode. In this case the e-beam voltage will have to be raised about 60 kV to achieve the same e-beam deposition uniformity.


Any sputtered metal will be carried by the flow and be deposited on the heat exchanger surfaces. On the average the gas flow will hit about $\approx 10$ such surfaces on each trip around the loop. The amount of sputtered metal that may be coated out on the optical windows can be estimated as follows. The total amount of metal sputtered in $10^8$ pulses is given by

$$M = I \cdot \tau_p \cdot 10^8 \cdot 10^{-5} \text{ g/coulomb}$$  \hspace{1cm} (2)$$

where $I$ is the discharge current and $\tau_p$ is the discharge pulse length. In this case $I = 10^4$, and $\tau_p = 250$ ns, therefore $M = 2.5$ g. The total surface area of the flow loop is $A \approx 2.7 \times 10^5$ cm$^2$. Since the gas sees $\approx 10$ surfaces each time around the flow loop, the coating thickness $T$ on the windows is then given by

$$T = \frac{M}{A} \cdot \frac{1}{\rho} \cdot e^{-10 \cdot P}$$  \hspace{1cm} (3)$$

where $\rho = 21$ g/cm$^3$ is the density of platinum, and $P$ is the surface sticking probability. Taking a sticking probability of 0.3 (a conservative estimate) we get a coating thickness of 2.2 $\mu$m. The effect of such a thin coating on window transmission is negligible. For $10^{10}$ shot lifetime, a well-filtered boundary layer shield flow at the windows may be necessary.

2. **Current Returns**

In order to maximize the laser electrical efficiency, the risetime of the discharge circuit must be kept small, compared to the pulsewidth. As we indicate elsewhere, we can allocate $30$ nH to the cavity and its connectors. This puts a constraint on the allowable inductance in the laser cavity. To minimize inductance the current returns for the discharge must be placed close to the discharge channel. This necessitates bringing the current return through the flow via a set of bars. As in the 1 m experiments, in
In this design the anode is pulsed to high voltage while the cathode is held at ground potential. The current returns are then also at ground potential. In order to prevent arcing between the anode and the current returns a minimum spacing is required. For the mixtures used in this laser the maximum holdoff field has been measured in both the cable gun and meter device experiments and was found to be $> 12$ kV/cm. The maximum designed discharge voltage on the anode is 32 kV. To allow for local field enhancement around the current return bars and to allow a safety margin, the minimum spacing between the current returns and anode is chosen to be 5 cm.

Symmetric current returns are placed up and down stream from the discharge channel (see Figure 54). If the spacing of the current return bars is kept small compared with their distance to the discharge channel, then the return current can be approximated by a continuous current sheet for inductance calculations. In this case, with symmetric current returns, the circuit inductance is given by

$$L \leq \frac{\mu_0}{4} \frac{A}{\ell}$$  \hspace{1cm} (4)

where $A$ is the area enclosed by the current returns and $\ell$ is the length of the discharge region in the optical direction. For the present design $A = 300$ cm$^2$ and $\ell = 62.5$ cm. The inductance is calculated to be $\approx 15$ nH. To keep the current return bar spacing small compared with their distance to the discharge channel, 15 3/16 in diameter current return bars spaced 4 cm apart are used per side in this design.

In order to minimize disturbance to the flow the current return bars are placed inside alumina tubes with the outside shaped like airfoils. The pressure drop then is negligible.
Figure 54. Discharge Electrode Geometry
3. High Voltage Feedthroughs

The high-voltage feedthroughs support and provide connections from the discharge modulator to the anode. Five parallel feedthroughs are used along the anode to minimize inductance. These are similar in design to those used in the 1 m device. Five centimeter long alumina sections are used for voltage standoff. In the laser mixture surface breakdown in ceramic was found not to be a problem, so the 5 cm insulator length allowed should standoff >60 kV, which is a factor of two greater than the maximum discharge voltage used. Therefore, breakdowns in the region at the back of the anode should not be a problem.

The feedthroughs will be operating at cavity temperature. The output cables from the discharge modulator will not be capable of withstanding this temperature so that connectors will be required to take up the temperature drop. To avoid inductance problems the connectors can be made to be like coaxial transmission lines, all the way up to the feedthroughs (see Figure 54). The impedance of the connectors can be matched to that of the modulator output cables. The connectors then add negligible inductance to the circuit. Since the discharge impedance is ≈ 3 Ω, with 5 feedthroughs, the connectors should be made like 15 Ω coaxial lines. This can easily be accomplished with metalized alumina tubes.

The total inductance of the discharge cavity including all the connectors will therefore be ≤ 30 nH. This value is used in our discharge modulator design (see Section III-I).
E. FLOW-LOOP DESIGN

The laser device is specified such that 80% of the energy at the output aperture is confined in a beam of total angle which is ten times that of the first Airy disc. The associated constraints on phase front errors at the output aperture are assessed here. This allowed phase front error is related to laser medium homogeneity requirements, and this in turn is used to determine acoustic wave suppression and thermal homogeneity requirements in the gas. Acoustic attenuator design features are also developed. Thermal homogeneity requirements are coupled to flow-loop design in the following section.

1. Phase Distortion

To estimate the allowable phase errors for a system far from the diffraction limit a sinusoidal phase error was assumed, for which the equations for maximum spot size are easily developed. Phase variation across a circular aperture is considered in the form,

$$\psi = A \left[ 1 - \cos \left( \frac{2\pi Nr}{D} \right) \right]$$

(5)

where $r$ is radial position across the aperture.

$D$ is the aperture diameter

$N$ is the number of periods across a diameter

$2A$ is the peak-to-peak phase variation.

If this is used to simulate separate eddies with a normalized scale length

$$L = \frac{1}{2} N$$

(6)

then

$$\psi = A \left[ 1 - \cos \left( \frac{\pi r}{LD} \right) \right]$$

(7)
For large wavefront errors diffraction is ignored and only the maximum wavefront slope is considered

\[ \psi' = \frac{\pi A}{LD} \]  

(8)

The condition that this be equal to 10 times the diffraction half-angle for a perfect lens, yields

\[ \frac{\pi A}{LD} = \frac{(10) 1.22 \lambda}{D} \]

(9)

\[ A = \frac{12.2 \lambda L}{\pi} \]

\[ \frac{2A}{\lambda} = (0.78) (XDL) L \]

where (XDL) is the ratio of far field spot diameter to Airy disc diameter. Thus the allowable peak-to-peak error (2A) depends linearly on L and for example if L = 0.1 and XDL = 1 times diffraction limit,

\[ \frac{2A}{\lambda} = 0.78 \text{ waves} \]  

(10)

2. Flow System Design Criteria

The laser gas, which is initially at temperature 490<sup>0</sup>K and a density of two amagats, undergoes an electrical energy deposition of 61.5 J/\(\text{torr}\) for a period of 250 ns to produce a laser energy density of 1.5 J/\(\text{torr}\). The gas is predominantly argon, hence the temperature rise during this event at a constant volume is \(T_2 - T_0\) = 62.4° C. Subsequent expansion of heated cavity gas is accurately represented as isentropic, thus final pressure relaxation to ambient reduces temperature in the ratio \(T_f/T_2 = 0.953\) (temperatures in <sup>0</sup>K). The final excess gas temperature is then \((T_f - T_C) = 36.4^0\text{C}\) after relaxation of a pressure pulse of strength \((p_f - p_C)/p_C = 0.128\). The internal energy decrease
during relaxation appears as compressive work done on the remainder of the gas in the flow-loop. This compression work, which is the difference between net deposited energy and remaining internal energy after relaxation, $\Delta W = 29.4 \, \text{J} / \ell$, is distributed partly as energy dissipation in acoustic wave attenuators and partly as recompression work on a hot gas slug as it cools in passage through a heat exchanger. The above energy considerations combine with cavity dimensions and pulse rate for the basis of loop thermal conditioning described below. The pulse overpressure combines with cavity dimensions and medium homogeneity requirements for the basis of acoustic attenuator design described below.

Beam quality is sufficient to meet targeting requirements if the PTP phase front variation is $0.78$ waves for ordered disturbances on a periodic scale of $1.6$ cm according to Eq. (10). If this distortion combines equal contributions from optics and from cavity gas, this relates to cavity homogeneity through

$$\frac{\phi}{2\pi} = \frac{2\ell_0}{\lambda} \beta \left( \frac{\rho}{\rho_r} \right) \left( \frac{\Delta \rho}{\rho} \right) = 0.55 \text{ waves} \quad (11)$$

where $\ell_0$ is distance between cavity windows = $70$ cm; $\lambda = 0.5 \, \mu\text{m}$; $\rho / \rho_r = 2$ amagats; $\beta = 2.8 \times 10^{-4}$. Thus,

$$\left( \Delta \rho / \rho \right)_{\text{PTP}} = 3.4 \times 10^{-4} \quad (12)$$

If this ordered gas distortion is budgeted equally between uncorrelated thermal and pressure wave distortions, the medium homogeneity requirement for each is

$$\left( \frac{\Delta \rho}{\rho} \right)_{\text{PTP}} = 2.43 \times 10^{-4} \quad (13)$$
Since the ordered distortion used in deriving Eq. (13) has an associated scale of 1.6 cm, the maximum gradient in density is limited to

$$\frac{\Delta \rho}{\rho} \leq 5 \times 10^{-4} \text{ cm}^{-1}$$

(14)

This form is most useful in assessing allowed boundary layer, ordered, thermal distortions. In ordered periodic distortions of arbitrary period \( \Lambda \), beam quality constraints limit the product of the LHS of Eq. (13) and \( \Lambda^{-1} \) to a constant value

$$\left(\frac{\Delta \rho}{\rho}\right)_{\text{PTP}} \Lambda^{-1} \leq 1.61 \times 10^{-4} \text{ cm}^{-1}$$

(15)

This form is useful in assessing allowed, ordered, thermal and pressure disturbances in the bulk flow. If thermal disturbances of scale \( \Lambda \) are randomly distributed in space, beam quality constraints confine the product of the LHS Eq. (15) and \( \Lambda/2\pi \) to a constant value; thus

$$\frac{\Delta \rho}{\rho} \Lambda^{-1/2} \leq 1.91 \times 10^{-3} \text{ cm}^{-1/2}$$

(16)

This form is useful in assessing allowed thermal disturbances carried by disordered turbulent flow.

The active cavity length in the flow direction is \( L = 4.0 \text{ cm} \). Development of design is based on a minimum interpulse interval of 5.0 ms and an associated flush factor of 1.75 to yield a flow velocity of 14 m/sec. The active cavity length in the pump direction is \( L = 6.4 \text{ cm} \); however, the full flow dimension is \( L = 7.45 \text{ cm} \) for reasons discussed below. The active cavity length along the optical axis is 62.5 cm, however, electrode termination and protection of windows from \( e \)-beam dictate a flow dimension \( L = 75 \text{ cm} \). The choice of a design flush factor, \( FF = 1.75 \)
should be conservative. Voltage standoff measurements in the
presence of previously discharge heated gas suggest lower flush
factors are permissible (see Section II-A-2-p).

For reference, the performance parameters and cavity geom-
etry described above are repeated in Table 4.

a. Muffler Performance Predictions

Pressure wave attenuation will be achieved by perforated
wall segments in the flow channel both upstream and downstream
from the laser cavity. This muffler configuration, when backed
with closed cells containing a dissipative material, has been
studied theoretically at AERL under IRAD support. Experimental
studies have also been conducted under DARPA support as part of
the XeF laser program. This modeling, which is the basis of the
present system design, is validated by these measurements. In the
case of small pulse overpressures appropriate to the present
application, a geometrical similarity parameter, \( L' \), allows a cor-
relation of results for use as a design tool.

\[
L' = \frac{H}{2} \cdot \frac{C_D}{C} \cdot \frac{\Delta P_i}{\gamma P} - \frac{\alpha}{\gamma} \cdot \frac{1}{c}
\]  

(17)

where geometrical parameters are defined in Figure 55; \( C_D \) is the
discharge coefficient through orifices in the perforated plate;
\( \Delta P_i/P_c \) is the incident pressure wave strength and \( \gamma \) is the
ratio of gas specific heats = 1.67. At the present system cavity
Mach number of 0.034 the zero Mach number solutions are appropri-
ate and results are presented in Figure 56. The ratio of exit to
inlet wave strength is shown for the design value of the ratio of
incident wave to upstream muffler length, \( \lambda/\ell_m = 1/5 \), and for
several values of the ratio of backing depth to flow channel
height, \( h/H \), as a function of normalized muffler length. For the
### Table 4. Laser Cavity Operating Conditions

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
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</thead>
<tbody>
<tr>
<td>Cavity Temperature, ( T_c )</td>
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<tr>
<td>Molecular Weight, ( m )</td>
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<tr>
<td>Ratio of Specific Heats, ( \gamma )</td>
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<tr>
<td>Sound Speed, ( a_c )</td>
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<td>Gas Density (2 Amagats), ( \rho_c )</td>
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<td>Viscosity, ( \mu_c )</td>
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<td>Minimum Interpulse Spacing</td>
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<td>Cavity Flow Length, ( l_f )</td>
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</tr>
<tr>
<td>Minimum Flush Factor, ( FF_{\text{min}} )</td>
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<td>Average Pulse Rate, PRF</td>
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<tr>
<td>Average Flush Factor, ( FF )</td>
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<td>Cavity Flow Velocity, ( u_c )</td>
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<tr>
<td>Reynolds Number (per meter), ( Re )</td>
<td>( 1.47 \times 10^6 ) m⁻¹</td>
</tr>
<tr>
<td>Laser Energy Density, ( e )</td>
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</tr>
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<td>Electrical Energy Deposited in the gas, ( e_{e} )</td>
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</tr>
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<td>Pulse Overpressure, ( \Delta p/p )</td>
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<tr>
<td>Gas Temperature Rise After Pressure Relaxation</td>
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<tr>
<td>Laser Cavity Dimensions, ( f'p'p'o' )</td>
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<td>Flow Length Along Pump Direction, ( l_p )</td>
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<td>Flow Length Along Optical Axis, ( l_o )</td>
<td>70 cm</td>
</tr>
<tr>
<td>Average Gas Temperature Rise</td>
<td>7.6°C</td>
</tr>
<tr>
<td>Acoustical Power Deposited in the Upstream Muffler</td>
<td>1.1 kW</td>
</tr>
</tbody>
</table>
Figure 55. Flow Channel Mufflers with Finite Backing Volume
Figure 56. Transmitted Peak Wave Strength Through Perforated Side Wall Muffler
selected $h/H = 2.0$ a minimum in the ratio of transmitted to incident wave strength of 0.18 is observed for $l_m/L = 3.4$. Since the upstream muffler length is $l_m = 20$ cm and incident wave strength is approximately half the cavity pulse overpressure, $\Delta p_i/p_c = 0.064$, Eq. (17) provides the specification of effective upstream muffler transparency $C_D = 0.086$. The upstream transmitted wave passes through a converging nozzle and is reflected from a plate/film velocity stabilizer of 40% geometrical blockage. This reflected wave, which is of strength $\sim 0.20$ that of the incident wave, returns through the muffler and is attenuated by another factor of 0.50 according to the modeling basis for Figure 56. Thus, the upstream pressure wave would show a peak overpressure of $1.15 \times 10^{-4}$ upon reentry to the cavity. This return pressure pulse is distributed over a length of order $l_m/2 = 10$ cm, consequently, the product

$$\frac{\Delta p}{p_c} \Lambda^{-1} = \frac{1}{\gamma} \frac{\Delta p}{p_c} \Lambda^{-1} = 6.9 \times 10^{-5} \text{ cm}^{-1}$$

is well within the medium homogeneity requirements of Eq. (15). A similar analysis of the downstream muffler shows that single-pulse pressure disturbances are suitably attenuated for purposes of medium homogeneity for this compact muffler geometry. Other considerations in selection of muffler geometrical features include growth of upstream boundary layers and incorporation of a diffuser in the downstream muffler as well as overall system component arrangements. These considerations are discussed below.
4. Flow-loop Design Approach, Arrangements and Sizing

Laser cavity operating conditions have been discussed above and are summarized in Table 4. Medium homogeneity requirements have also been discussed. Flow-loop design is based on these requirements and the requirements of (1) efficient operation for low flow power demand, (2) compactness for ultimate space board application, (3) compatibility with the hot reactive laser gas environment, and (4) reliability of loop components and peripheral equipment for long lived, maintenance-free operation. This section addresses the areas of thermal conditioning of the gas loop, flow-loop pressure drop, flow power requirements, and liquid coolant loop requirements.

For reference, two section views of the laser flow-loop are shown in Figures 57 and 58. Major flow elements are (1) muffler and diffuser downstream from the cavity for purposes of pressure wave attenuation and flow pressure recovery, (2) heat exchanger for removal of deposited electrical energy and dissipated flow power, (3) converging transition to circular flow cross section, (4) vaned turn, (5) fan and drive, (6) fan diffuser, (7) vaned turn, (8) diverging transition from circular to rectangular cross section, (9) velocity stabilizer to provide uniform velocity in the cavity, (10) converging nozzle, and (11) upstream muffler. Arrangements, performance requirements and component sizing are discussed in the following sections.

5. Cavity Thermal Conditioning Requirements

Gradients in cavity temperature for ordered disturbances at uniform pressure are limited by Eq. (14) as,

\[ \nabla T/T \leq 5 \times 10^{-4} \text{ cm}^{-1} \tag{19} \]

Cavity temperature nonuniformity at uniform pressure, for an ordered disturbance of scale \( A \), is limited by Eq. (15) as,

\[ \nabla T \leq 0.25 \circ C \text{ cm}^{-1} \]

AVCO Everett
Figure 57. Sectional View of the Laser Flow Loop, Side View
Figure 58. Sectional View of the Laser Flow Loop, Upstream View
\[(\Delta T/T)_{PTP} \leq 1.61 \times 10^{-4} \Lambda \text{ (cm)} \quad (20)\]

\[(\Delta T)_{PTP} \leq 0.079^\circ C \Lambda \text{ (cm)} \quad (21)\]

Disordered thermal disturbances of scale \( \Lambda \) are limited by Eq. (16) as,

\[\Delta T \leq 0.94^\circ C \Lambda^{1/2} \text{ (cm)} \quad (21)\]

5. **Boundary Layer Thermal Control Requirements**

Between the velocity stabilizer and the cavity, differences between gas and wall temperatures will produce ordered average temperature variations in wall boundary layers superimposed on a disordered turbulent temperature field. Here, ordered and disordered boundary layer temperature variations are examined independently with constraints imposed by Eqs. (19) and (21), respectively. After flow contraction through a nozzle or area ratio 2.5 the flow channel boundary layers may be assumed to originate at the entry to the upstream muffler (See Figure 57). Turbulent boundary layer growth along a smooth wall is given by Schlichting\(^24\) as

\[\delta (x) = 0.37 \times \text{Re}_x^{-1/5} \quad (22)\]

where \( \delta \) is boundary displacement thickness, \( x \) is distance from the origin and \( \text{Re}_x \) is Reynolds number based on \( x \). At the upstream edge of the cavity electrode, \( x = 22 \text{ cm} \), thus \( \delta = 0.64 \text{ cm} \). This value is appropriate for the solid wall, however, for the perforated wall a thickness of twice this value is assumed, \( \delta_p = 1.29 \text{ cm} \).

The velocity variation through the boundary layer is given by Schlichting as,

\[ \frac{u}{u_c} = (y/\delta)^{1/7} \]  \hspace{1cm} (23)

where \( y \) is distance normal to the wall. Reynold's analogy between velocity and temperature variations in the boundary layer provides the approximation

\[ \frac{T(y) - T_c}{T_w - T_c} \approx \frac{u_c - u(y)}{u_c} \]  \hspace{1cm} (24)

where \( T_w \) is the uniform wall temperature. Temperature gradient is related to \((y/\delta)\) through Eqs. (23) and (24) as

\[ \frac{dT}{dy} = \frac{T_w - T_c}{u_c} \frac{du}{dy} = -\frac{T_w - T_c}{7\delta (y/\delta)^{6/7}} \]  \hspace{1cm} (25)

Equation (25) when constrained by Eq. (19), indicates that a portion of the boundary layer near the wall will not contribute to useful laser energy extraction and this portion grows with increasing \((T_w - T_c)\). Equations (19) and (25) combine to give the extent of unuseable boundary layer flow as

\[ \frac{\delta}{\delta} = \left( \frac{T_w - T_c}{1.75\delta} \right)^{7/6} \]  \hspace{1cm} (26)

Equation (26) is plotted in Figure 59 for boundary layer thickness at laser cavity entry. The solid flow channel wall may be held to within 0.5°C of the cavity gas temperature without difficulty, thus indicating a lost portion in useable channel flow of 0.25 cm.
Figure 59. Boundary Layer Portion of Unacceptable Beam Quality vs Wall to Cavity Temperature Difference
However, the discharge cathode will stand off by 1.0 cm from this wall for reasons discussed in the next section. Thus, even this exclusion is of no consequence. The perforated wall must be held to within 0.6°C of the cavity gas temperature if we wish to limit the rejected portion of the boundary layer to 0.25 cm. This may be achieved only if active cooling is provided in the backing volume of the upstream muffler, where as much as 1100 W of acoustical energy may be deposited.

Furthermore, boundary layer suction is proposed immediately upstream from the discharge anode to further reduce this ordered boundary layer temperature gradient. A portion 0.25 cm in height will be removed by the slit conduit shown in Figure 60. This removal of 20% of the boundary layer thickness will essentially restart the turbulent boundary layer, although disordered turbulence from the current boundary layer will survive. This disordered turbulence may carry temperature variation as large as (T_w - T_a) = 0.6°C. On a scale order of the remaining boundary layer thickness = 1.0 cm. Equation (21) shows that this flow region satisfies cavity medium homogeneity requirements.

6. Treatment of Foil and Discharge Electrodes

Various heating contributors and loads to foil, discharge cathode and discharge anode are listed in Table 5. The foil will be recessed 1.0 cm behind the discharge cathode to prevent foil failure in the event of arcing. The cathode will be constructed as a row of cooling tubes so that main channel gas flow will carry only heated gas between foil and cathode. In this configuration foil heating of the gas is not an issue for cavity medium homogeneity, so attention is here focused on the cathode.

Cathode tubes of 1.6 mm outside diameter are spaced at 3.3 cm on centers. Tube ends are curved into coolant flow headers as shown in Figure 60. Straight tube segments parallel to the flow direction are 7 cm long and boundary layers grow along outsides of these tubes to a thickness of ~1.5 mm at mid-span, i.e., at the center of the laser cavity. Tube heating occurs mainly over the
Figure 60. Section to Show Details in the Region of the Laser Cavity
## Table 5. Heating Loads on Foil and Discharge Electrodes

<table>
<thead>
<tr>
<th>Element</th>
<th>Source</th>
<th>Heating Load</th>
</tr>
</thead>
<tbody>
<tr>
<td>Foil:</td>
<td>E-Beam</td>
<td>0.72 W/cm²</td>
</tr>
<tr>
<td></td>
<td></td>
<td>180 W</td>
</tr>
<tr>
<td>Discharge Cathode</td>
<td>E-Beam</td>
<td>2.73 W/cm²</td>
</tr>
<tr>
<td></td>
<td></td>
<td>683 W</td>
</tr>
<tr>
<td></td>
<td>Discharge</td>
<td>0.5 W/cm²</td>
</tr>
<tr>
<td></td>
<td></td>
<td>125 W</td>
</tr>
<tr>
<td></td>
<td>Gas Convective Cooling</td>
<td>47 W</td>
</tr>
<tr>
<td></td>
<td>Total</td>
<td>855 W</td>
</tr>
<tr>
<td>Discharge Anode:</td>
<td>E-Beam</td>
<td>1.10 W/cm²</td>
</tr>
<tr>
<td></td>
<td></td>
<td>276 W</td>
</tr>
<tr>
<td></td>
<td>Discharge</td>
<td>0.5 W/cm²</td>
</tr>
<tr>
<td></td>
<td></td>
<td>125 W</td>
</tr>
<tr>
<td></td>
<td>Gas Convective Cooling</td>
<td>47 W</td>
</tr>
<tr>
<td></td>
<td>Total</td>
<td>448 W</td>
</tr>
</tbody>
</table>
central 4.0 cm of span where e-beam and discharge are active. For
flat wall boundary layers Eq. (26) defines the unuseable portion
due to unacceptable medium homogeneity. For the present boundary
layer growth along a tube row, temperature varies periodically
along lines parallel to the optical axis, and the path averaged
difference between local and cavity temperature is approximately
half the maximum difference at each tube station. Therefore for
local allowed temperature gradients at tube stations the RHS of
Eq. (19) is replaced by 0.50°C cm⁻¹ and Eq. (26) is replaced by

\[
\frac{Y}{\delta} = \left( \frac{T_w - T_c}{3.5 \delta} \right)^{7/6}
\]  

(27)

If the entire 1.3 mm of boundary layer flow is excluded from the
laser cavity the allowed average tube wall temperature excess is
obtained from Eq. (27) as,

\[
T_w - T_c = 0.46°C
\]  

(28)

This requirement has influence on design of the liquid side of the
cathode tubes.

The discharge anode with upstream boundary layer suction is
shown in Figure 60. If a turbulent boundary layer is started at
the suction slit, its thickness at electrode center is, \( \delta =
0.15 \) cm. If the entire renewed boundary layer is excluded from
the laser cavity the allowed anode wall temperature excess is
given by Eq. (26),

\[
T_w - T_c = 0.26°C
\]  

(29)
Temperature uniformity in the anode will be maintained by liquid coolant channels spaced at intervals of 1.0 cm and arranged parallel to the flow direction. Coolant will be conveyed by spreaders at upstream and downstream ends of these channels, as shown in Figure 60. If coolant channels are spaced at intervals, w, and are of diameter, d, the wall temperature variation is quadratic between channels with the form

$$ T(x) - T_0 = \frac{q}{2kt} (hw - x^2) \quad (30) $$

where $q$ is anode heat flux = 1.79 W/cm$^2$; $k$ is anode thermal conductivity which for copper is 3.77 W/cm°C; and $x$ is distance from a coolant tube. The maximum temperature difference is at mid-span, $x = h/2$,

$$ T_m - T_0 = \frac{q}{8k} \frac{h^2}{t} \quad (31) $$

If channel spacing is 1.0 cm the temperature uniformity requirement Eq. (29) is satisfied by Eq. (31) for a coolant passage diameter of 0.23 cm.

7. Heat Exchanger Performance Requirements

The heat exchanger shown in Figure 57 at the downstream end of the flow channel serves the purpose of removal of deposited electrical energy and flow dissipation energy from the gas stream. The heat exchanger is potentially a major contributor to flow-loop power requirements but this is somewhat alleviated by increasing the flow entry area as for example in Figure 57. Heat exchanger effectiveness is controlled primarily by the ratio of flow length to a transverse characteristic dimension, hydraulic diameter. Pressure drop, $(p_i - p_e)$, hence flow power is controlled primarily by this ratio times the flow speed to the third power. Heat exchanger performance is correlated with the following expression,
\[
\frac{P_i - P_e}{\frac{1}{2} \rho u_m^2} = 4f \frac{\zeta}{d_h} = N \frac{p^{2/3}}{r} \ln \frac{T_i - T_w}{T_e - T_w}
\]  (32)

where \( \rho \) is gas density; \( u_m \) is average gas speed at the minimum heat exchanger flow cross section; \( \zeta \) is heat exchanger length in the flow direction.

\[
d_h = \frac{4A_f}{A_w}
\]  (33)

is the hydraulic diameter; \( A_f \) is the minimum flow cross section; \( A_w \) is heat exchanger surface area; \( \Pr \) is Prandtl number = \( \frac{C_p u}{k} \). Heat exchanger effectiveness, \( S \), is a measure of the degree of equilibration of the gas to wall temperature, \( T_w \), in transit through the heat exchanger,

\[
S = \frac{T_i - T_w}{T_e - T_w}
\]  (34)

The friction factor \( f \) is weakly dependent on Reynolds number in turbulent flow. The heat exchanger efficiency, in terms of effectiveness per unit power expenditure at fixed flow conditions, is proportional to \( N^{-1} \), which is also weakly dependent on Reynolds number. This parameter \( N \) has a value of 2.0 in Reynolds analogy between heat transfer and pressure drop for unseparated flow, therefore this value is viewed here as ideal lower limit.

Flow power is given as

\[
P = V(\rho_i - \rho_e)
\]  (35)
where $\dot{V}$ is the volumetric flow rate $= u_1 A_1$; $u_1$ is HX entry flow speed and $A_1$ is the entry flow cross section. It is convenient to combine Eqs. (32) and (35) in the following arrangement,

$$p = \dot{V}^3 A_c^{-2} \left( \frac{A_c}{A_1} \frac{N}{\sigma} \right)^2 \left( \frac{\rho}{2} \frac{P_r^{2/3}}{r} \right) \ln S$$  \hspace{1cm} (36)

where $\sigma$ is the ratio $A_f/A_1$ and $A_c$ is flow cross section in the laser cavity. The term $(N/\sigma)^2$ is primarily controlled by heat exchanger geometry and to a weaker extent by Reynolds number, and the term $(\rho/2)P_r^{2/3}$ is a property of the gas. In this form one sees that a fixed flow rate, $\dot{V}$, cavity area $A_c$ and fixed HX effectiveness, $S$, the flow power is proportional to the product of geometrical features $\left( \frac{A_c}{A_1} \frac{N}{\sigma} \right)^2$.

A comparison of three types of heat exchangers was made on the basis of this product: (1) fin/tube, (2) staggered, bare, round tubes, and (3) aligned, flattened tubes. In the hot chemical reactive environment of the HgBr$_2$ laser, special attention must be given to soldering, brazing and degree of complexity of geometrical forms. Since these three types of heat exchangers are fabricated with a minimum amount of soldering or brazing, and since they are assembled from preformed flat and cylindrical stock, they appear well suited to the present application. On the basis of effectiveness, $S$, the fin tube heat exchangers are preferred, provided their fabrication features are compatible with the laser environment. If the fin tube class were not compatible with the laser environment, flattened tubes, which are of much simpler construction, may be a reasonable alternative if accompanied by increased inlet area. For present design consideration

---

the fin tube unit 8.0-3/8 T\( \frac{25}{25} \) was selected with an inlet area to cavity flow area ratio of 4.0. This area ratio was selected after design by iteration of the entire flow loop, with consideration given to the trade-off between large inlet area and achievable uniformity of flow over this inlet. Consideration was also given to device compactness and to the fraction of flow-loop pressure drop attributed to diffuser and heat exchanger.

The electrically heated gas temperature, after pressure relaxation, exceeds initial cavity temperature by 36.4°C (Table 4). If electrically heated and unheated gas slugs are specified to exit the heat exchanger at \( T_c + 6 \)°C and \( T_c - 6 \)°C, respectively, the the average wall temperature and HX effectiveness can be simply calculated as, \( T_w = T_c - 9 \)°C and \( S = 3.0 \). The coolant liquid temperature rise in a counter flow heat exchanger is independently selected as 6°C to provide the HX temperature maps of figure 61.

8. Flow Conditioning

Flow-loop design is based on (1) efficient operation for low power demand, (2) compactness for ultimate space based application, (3) compatibility with the hot reactive laser gas environment, and (4) reliability of loop components and peripheral equipment for long lived, maintenance free operation. The loop design must, of course, satisfy the cavity medium homogeneity requirements discussed previously. Design was carried out in an iterative fashion to arrive at a balance between compactness and flow efficiency. Potential sources of large head losses, such as the diverging flow section downstream from the cavity and heat exchanger, received special consideration to design detail to bring these losses into balance. This section discusses the basis for design features which are shown in Figure 57.

Cavity geometry and flow conditions of Table 4 provide a flow rate and cavity dynamic head of
Figure 61. Gas and Liquid Average Temperature vs Distance Through the Heat Exchanger
\[ V = 0.720 \, \text{m}^3/\text{sec} \]
\[ q_c = \frac{1}{2} \rho u_c^2 = 350 \, \text{n/m}^2 \]

It is useful at the outset to estimate the magnitude of flow-loop power in relation to overall device power requirements. For this purpose consider a fan efficiency of \( \eta_f = 70\% \), an electric motor efficiency of \( \eta_m = 85\% \) and a mechanical transmission (i.e., bearing and seal efficiency) \( \eta_p = 90\% \). Then, for each flow-loop pressure drop of one cavity dynamic head, the fan electrical power required is

\[ P = \eta_f^{-1} \eta_m^{-1} \eta_p^{-1} \frac{1}{2} \rho u_c^2 = 470 \, \text{W} \]

Of the total available power of 20 kW, one-half is given to the discharge. If 20\% of the remaining 10 kW is given to all aspects of the flow-loop, the total loop pressure drop should be safely designed to less than three cavity dynamic heads. With care in design of critical components the compact flow-loop of Figure 17 is compatible with this goal, and hence it provides a fair balance between flow efficiency and system compactness.

a. Cavity Diffuser Design Criteria

The cavity diffuser is incorporated in the downstream collector as shown in Figure 17. It serves the purpose of partial recovery of cavity dynamic pressure and of providing improved uniformity in flow distribution to the entry of a heat exchanger of large area ratio, \( D_{HX} = A_{down}/A_{up} = 4.0 \). The perforated diffuser wall diverges from the downstream edge of the discharge pipe. Space limitations allow a spacing of the solid wall to begin where shown in Figure 17.
The perforated wall divergence angle is 3.5°, which is an established value for maintenance of attached flow in conventional diffusers. The region of performance of this diffuser is shown in the performance map of Reneau, et al.,(26) which is presented here as Figure 62. The ratio of downstream muffler length, M, to cavity length in the pump direction, p, is 6.0. Boundary layer suction at the upstream edge of the anode was discussed above as a means of maximizing the utilization of the discharge region for laser energy extraction. The renewed boundary layer growth reaches a displacement thickness of 0.3 cm at the diffuser inlet, to provide the ratio δ/p = 0.04. The two lines a-a in Figure 62 show that the boundary of the zone for flow attachment depends on this ratio and the design point is well within this zone. Tests which formed the basis of Figure 62 showed little sensitivity to Reynolds number over a range of from 1.5 x 10³ to 5 x 10⁴ based on the length M. These results, therefore, appear valid for the present case where Re = 10⁵.

The area ratio of flow exit to inlet, for the perforated wall segment is 1.37. Pressure recovery through this diffuser is obtained by interpolation of measurements by Reneau, et al.,(26) as

$$C_p = \frac{p_2 - p_c}{q_c} = 0.4$$

(39)

where p² is diffuser exit static pressure, and p_c and q_c are cavity static and dynamic pressures. If one assumes the total loss of surviving dynamic pressure at the diffuser exit, one obtains a stagnation pressure loss.

Figure 62. Flow Regimes in Straight-Wall, Two-Dimensional Diffusers
This loss may be compared with the potential loss of a full cavity dynamic head in the absence of a diffuser. Furthermore the diffuser provides improved uniformity of flow to the heat exchanger, and thus enhances its flow efficiency. Entry flow uniformity is also the motive in inclusion of splitter plates, and in the tailoring of entry fins, and in the inclusion of divergence in the solid flow channel wall as shown in Figure 57.

The above basis for diffuser design and the predicted performance may appear conservative. However, this system has the uncommon features of (1) perforated diffuser wall, (2) periodic pressure transients resulting from cavity pressure relaxation, and (3) a large and unsymmetrical flow impedance immediately downstream from the diffuser. For these reasons it is proposed that preliminary tests be conducted to determine the flow performance of the diffuser and heat exchanger.

1. Heat Exchanger Design Criteria

The method for heat exchanger performance is discussed in detail in Section III-1.1. Investigation for the details of flow entry into the entrance of the cavity hence flow efficieny, splitter plates, wall entry into four flow segments, and flow through tailoring vanes for this design, determine performance. These extensions are required to ensure that dynamic entry between entry pressure, and the other conditions.
The design entry area is four times the cavity flow cross section, \( D_{HX} = 4.0 \). The pressure drop through the heat exchanger is obtained from Eq. (32) using the characteristics of HX type 8.0 - 3/8 T\(^2\) [25] and the selected effectiveness \( S = 3 \) in Eq. (34).

\[
\frac{\Delta P}{q_c} = \frac{\Delta P}{q_m q_i q_c} = \frac{\Delta P}{2 \rho u_m^2} \left( \frac{u_m}{u_i} \frac{u_i}{u_c} \right)^2
\]

(41)

\[
\frac{\Delta P}{q_c} = \frac{1}{2 \rho u_m^2} (\sigma D_{HX})^{-2} = \frac{8.8}{D_{HX}^2} = 0.55
\]

The length of the heat exchanger in the flow direction is obtained from Eq. (32) as

\[
i = 24.6 \ d_h = 8.9 \ \text{cm}
\]

(42)

c. Transition Sections, Turns and Return Leg

Downstream from the heat exchanger the flow passes through a transition section from rectangular to circular flow cross section. The circular cross-sectional area is selected to be twice the cavity flow cross section, \( D = 2 \). This choice is based again on iterative design with selection based on a balance between loop compactness and flow power. This transition is followed by a vaned turn as shown in Figure 57. Vanes are inserted to control fine scale mixing as discussed in Section III-E-8-b and also to provide uniform flow to the driving fan. At the low operating Reynolds number of \( 4.4 \times 10^4 \) based on vane chord, flow separation is anticipated, hence vanes will contribute little to gain in pressure recovery through the turn. Consequently, the pressure loss through the subsequent vaned turn, i.e., each predicted to equal one local dynamic head,
\[ \frac{\Delta P}{q_c} = \frac{\Delta P}{q} \ , \ \frac{q}{q_c} = \frac{\Delta P}{q_c} \cdot \frac{1}{\rho^2} = 0.25 \]  \hfill (43)

The contracting transition suffers little head loss so it is simply included with return leg wall losses. Wall losses are estimated on the basis of fully developed pipe flow with a diameter of 36 cm, a Reynolds number of \(2.6 \times 10^5\) and a length of 2.0 m

\[ \frac{\Delta P_0}{q_c} = 4f \frac{1}{d} \frac{1}{D^2} = 0.11 \frac{1}{D^2} = 0.03 \]  \hfill (44)

The diverging transition contains splitter plates to provide a uniform distribution of flow to the plenum located upstream from the velocity stabilizer. These splitter plates serve to provide uniform entry conditions to the velocity stabilizer but do not aid in pressure recovery through the transition. Consequently, one entry dynamic head is assumed to be lost in this transition

\[ \frac{\Delta P_0}{q_c} = \frac{1}{\rho^2} = 0.25 \]  \hfill (45)

d. **Fan and Fan Diffuser**

A specific fan selection cannot be made until a detailed system design is completed. For present flow power considerations a vane-axial fan of \ (~30 cm (12 in.)) diameter may be fabricated to meet present flow rate and pressure head requirements with an associated fan efficiency of \(\eta_f = 70\%\). Uniform flow entry is provided by vanes in the upstream turn followed by a straight flow length of one blade diameter and a slight flare at the fan entry. Efficient fan operation requires that it be followed by a fan diffuser. If the fan inlet area is 63\% of the approach area in the
circular duct as in Figure 57, the entry dynamic pressure is 2.5 times that of the approach flow

\[ q_i = 2.5q = 2.5q_c \frac{1}{D^2} = 0.63q_c \]  

(46)

For reference it is noted that with no fan diffuser one may suffer stagnation pressure loss of 0.63 cavity dynamic heads. A diffuser divergence total angle of 5.5° was chosen for the outer diffuser wall, and a nozzle taper of 4.9° was chosen with an abrupt truncation at the entry to the downstream turn (see Figure 57). This configuration is appropriate to maintenance of attached flow and one may conservatively estimate the diffuser head loss at 40% of the fan inlet dynamic pressure, i.e.,

\[ \frac{\Delta P_o}{q_i} = 0.4 \]

or

\[ \frac{\Delta P_o}{q_c} = \frac{\Delta P_o}{q_i} \frac{q_i}{q} \frac{q}{q_c} = \frac{1}{p^2} = 0.25 \]  

(47)

e. Velocity Stabilizer

A flow impedance is inserted at the upstream end of the converging nozzle for purposes of suppressing large-scale turbulence and providing flow to the cavity with uniform velocity. This is indicated at a heat exchanger in Figure 57 so that it may provide fine-scale control, if necessary, to cavity temperature level and uniformity. For present purposes it may be viewed simply as an impedance which introduces a pressure loss of three entry dynamic heads,
\[ \frac{\Delta P}{\rho} = \frac{\rho}{q_1} \cdot \frac{q_1}{q_c} = \frac{3}{p_{VS}} \]  

(48)

where \( p_{VS} \) is the flow area ratio between stabilizer inlet and cavity. This is also the nozzle area ratio, which is chosen as 1.9, again on the basis of balance between system compactness and flow-loop power.

f. Nozzle, Upstream Muffler and Boundary Layer Suction

The nozzle is formed by the arcs of two circles of radius equal to the area ratio of 2.5. The ratio of inlet height to length is 3/4. Parallel entry and exit flow and arc tangency at the junction complete the design specification. Head losses in the nozzle are insignificant.

This nozzle geometry provides sufficiently rapid expansion to restart the boundary layer at its exit. Head loss in the upstream muffler is determined by assuming smooth wall boundary growth on the solid walls and rough wall boundary layer growth along the perforated wall, or approximately

\[ \frac{\Delta P}{\rho} = 4 \cdot C_f \cdot \frac{\rho}{k} = 4 \cdot \frac{3}{2} \cdot C_f \cdot \frac{\rho}{k} \]

\[ d_h = 2 \cdot \left( \frac{\rho}{k} \cdot \frac{1}{\rho} \right) = 13.3 \text{ cm} \]

(49)

\[ C_f = 0.7 \delta \]
where $\delta$ is the smooth wall displacement thickness at the cavity cathode, given in Section III-E-5 as 0.64 cm. Thus,

$$\frac{\Delta P}{q_c} = 0.06 \quad (50)$$

A portion of the boundary layer from the upstream muffler wall will be removed to maximize the utilization of electrically heated gas in contributing to laser energy. This removed gas, which is 3.5% of the total cavity flow, is drawn to the fan inlet by the existing static pressure drop. Power required to achieve this is thus a fixed portion, 3.5%, of the total fan power and appears as a multiplier $\sigma_{BL} = 1.035$ in the final determination of power requirements.

9. Summary

Loop stagnation pressure losses are summarized in Table 6 in forms with unspecified values of heat exchanger, return leg, and velocity stabilizer area ratios, and in forms with design values of 4.0, 2.0 and 2.5, respectively. Small losses to return leg walls and upstream muffler have been omitted. A scaling relation is seen to result

$$\frac{\Delta P_o}{q_c} = 0.6 + \frac{8.8}{D_{HX}^2} + \frac{4.0}{D^2} + \frac{3.0}{D_{VS}^2} \quad (51)$$

This relation was developed early in the design study and was used to provide the balanced design of component losses shown in the table.

The design total stagnation pressure loss

$$\Delta P_o/q_c = 2.63 \quad (53)$$
<table>
<thead>
<tr>
<th>Element</th>
<th>$\Delta P_{0}/q_{c}$</th>
<th>$\Delta P_{0}/q_{c}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Diffuser</td>
<td>0.6</td>
<td>0.60</td>
</tr>
<tr>
<td>Heat Exchanger</td>
<td>$8.8 \frac{D}{HX}$</td>
<td>0.55</td>
</tr>
<tr>
<td>Vaned Turns (2)</td>
<td>$2.0 \frac{D}{-2}$</td>
<td>0.50</td>
</tr>
<tr>
<td>Expansion Transition</td>
<td>$1.0 \frac{D}{-2}$</td>
<td>0.25</td>
</tr>
<tr>
<td>Fan Diffuser</td>
<td>$1.0 \frac{D}{-2}$</td>
<td>0.25</td>
</tr>
<tr>
<td>Velocity Stabilizer</td>
<td>$3.0 \frac{D}{VS}$</td>
<td>0.48</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td></td>
<td><strong>2.63</strong></td>
</tr>
</tbody>
</table>
combines with Eq. (38) for a determination of loop power

\[ P = \eta_f^{-1} \eta_b^{-1} \eta_m^{-1} V q_c \frac{\Delta P_o}{q_c} \sigma_{BL} \]  

(53)

where \( \sigma_{BL} = 1.035 \) as discussed in Section III-E-8-f. Practical efficiencies for fan, drive train and motor are 70\%, 90\% and 85\%, respectively. The design value for electric power demand to drive the flow-loop is then,

\[ P = 1.29 \text{ kW} \]  

(54)

Additional power requirements to drive the liquid coolant loop are discussed below.

9. Fan and Drive Train Requirements

The design loop pressure drop of Eq. (52) is referenced to cavity pressure by

\[ \frac{\Delta P}{P} = \frac{\Delta P}{q_c} \frac{q_c}{P} = \frac{\Delta P}{q_c} \frac{\gamma}{2} M_c^2 = 2.63 \frac{\gamma}{2} M_c^2 \]  

(55)

Operating conditions given in Table 4 provide a cavity Mach number \( M_c = 0.034 \) and volumetric flow rate \( \dot{V} = 0.746 \text{ m}^3/\text{sec} \). Thus,

\[ \frac{\Delta P}{P} = 2.5 \times 10^{-3} \]  

(56)

These operating requirements are referenced to ambient condition and standard English operating units for fan design as

\[ \dot{V} = 1580 \text{ cfm (cubic feet per minute)} \]  

(57)

\[ \Delta P = 1.0 \text{ in. w (inches of water)} \]  

(58)
Operating speed regime may be obtained from the following performance correlation

\[ \frac{dP}{p} = K \gamma M_t^2 \]  

(59)

where \( K \) is the fraction of peak head at which blade stall occurs and \( M_t \) is blade tip Mach number. A choice of \( K = 0.05 \) and Eq. (56) provide a tip Mach number from Eq. (59) and a tip speed from the laser gas sound speed of 412 m/sec.

\[ M_t = 0.173, \quad u_t = 71.3 \text{ m/sec} \]  

(60)

If the blade disc outside diameter is 30 cm the corresponding rotational speed is

\[ f = 4540 \text{ rpm} \]  

(60)

Specific fan selection cannot be made until flow-loop design is finalized. However, fabrication of vane-axial fans for military and space application predict a fan efficiency in excess of 70% for the above operating conditions.

10. Liquid Coolant Loop Design

Silicone heat transfer fluids meet present operating temperature requirements and easily meet current space application lifetime requirements when operated in the absence of air. They are also very compatible with all conventional materials used in coolant loops. Candidate materials are Dow-Corning products SYLTERM 444 and DC550. Analysis here is based on the properties of type 444 fluid.

The coolant loop is designed to remove total electrical power deposited in the gas and in the structure as well as flow power dissipated in the flow loop. Total dissipated power from electron gun, discharge and flow dissipation are listed in Table 7.
### TABLE 7. HEAT LOAD SOURCES AND DISTRIBUTION

**SOURCES**

<table>
<thead>
<tr>
<th>Source</th>
<th>Power (kW)</th>
</tr>
</thead>
<tbody>
<tr>
<td>E-Beam</td>
<td>$P_e = 2.25$</td>
</tr>
<tr>
<td>Discharge</td>
<td>$P_d = 9.50$</td>
</tr>
<tr>
<td>Flow</td>
<td>$P_f = 1.00$</td>
</tr>
<tr>
<td>Total</td>
<td>$P_t = 12.75$</td>
</tr>
</tbody>
</table>

**DISTRIBUTION (REMOVAL)**

<table>
<thead>
<tr>
<th>Source</th>
<th>Power (W)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Foil</td>
<td>180 W</td>
</tr>
<tr>
<td>Discharge Cathode</td>
<td>855 W</td>
</tr>
<tr>
<td>Discharge Anode</td>
<td>448 W</td>
</tr>
<tr>
<td>Upstream Muffler</td>
<td>1100 W</td>
</tr>
<tr>
<td>Exterior Walls</td>
<td>450 W</td>
</tr>
<tr>
<td>Heat Exchanger</td>
<td>9687 W</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>12.75 kW</strong></td>
</tr>
<tr>
<td><strong>External Heat Exchanger</strong></td>
<td><strong>12.30 kW</strong></td>
</tr>
</tbody>
</table>
This deposited power will be removed by cooling at various locations in amounts listed in Table 7. Component locations are shown in Figure 57 with exception of the upstream muffler HX and external HX. Wall temperature requirements for various elements, discussed in Section III-E-4, have varying tolerances which are best met by independent element flow and temperature control as shown schematically in Figure 63.

Cathode and anode wall temperature constraints demand accurate liquid temperature control. This will be accomplished with a reservoir (sump) whose temperature will be controlled by wall cooling and regulated heat exchange with the external HX. Additional control will be provided by separate regulation of liquid flow rates to cathode and anode. The higher liquid inlet temperature to the anode as compared to the cathode will be accomplished by anode supply line cooling.

The upstream muffler wall must be held to within 0.6°C of cavity temperature. The muffler heat exchanger will be located in the muffler backing volume, hence liquid temperature control is more relaxed. Wall temperature control will be achieved by regulated liquid flow rate based on wall temperature monitoring.

The loop heat exchanger will have regulated liquid flow and cavity gas temperature will be the control monitor. The external heat exchanger will be air cooled in the breadboard design. The small fan required is not considered in the power budget since it will be replaced by radiation cooling the space application.

Pump power requirements for the liquid demand of each element have been computed on the basis of flow demands and specific element geometries. Geometric details of elements have been discussed in Section III-E-4. The major power demand is the cooling of the discharge cathode tubes. This is a result of the load requirements, the ΔT constraint and the small tube inside diameter of 0.071 cm over the 4.0 cm long region of e-beam operation. A low value of pump efficiency of 33% is anticipated since flow settling is the basis of temperature control. Drive motors of
Figure 63. Liquid Coolant Loop Operation Schematic
such small power demand are realistically expected to have efficiencies of \( \sim 75\% \). The design liquid loop electrical power requirements are

\[
P = \eta_p^{-1} \eta_m^{-1} \times 68.5 \, \text{W} = 274 \, \text{W}
\]  

11. **Flow-Loop Design Summary**

Allowed phase errors at the output aperture have been assessed for specified laser targeting requirements. These allowed errors have been budgeted equally between optics distortions and cavity medium inhomogeneities. Cavity medium inhomogeneities were budgeted equally between thermal distortions and pressure wave distortions. Flow-loop thermal conditions and pressure wave suppression designs were carried out on this basis. Predicted overall cavity inhomogeneities are 64\% of that budgeted to meet performance requirements. This implies that the optical axis may be scaled up by a factor of 2.5 while still remaining within the allowed budget.

In addition to cavity medium homogeneity requirements and device performance requirements, the flow-loop design approach addresses (1) efficient operation for low power demand, (2) compatibility for ultimate space based application, (3) compatibility with the hot reactive laser gas environment, and (4) reliability of loop components and peripheral equipment for long lived, maintenance free operation.

Flow-loop electrical power demand for the considered compact loop design is predicted to be

\[
P_f = 1.29 \, \text{kW}
\]
\[ P_e = 0.27 \text{ kW} \] (63)

Total flow-loop electrical power demand of 1.56 kW is 15.6% of the electrical power demanded by the discharge. An increase in the cavity scale in the flow direction from 4.0 to 6.0 cm is predicted to require a total flow power which is \(~20\%\) of that for the discharge.
F. OPTICS AND INJECTION LASER

1. Approach

The system must have a spectral width of < 1 Å, average power of 200 W, beam quality better than 10 times the diffraction limit, and efficiency > 1%. A free running HgBr laser has a spectral width of about 6 Å, hence spectral control is necessary. The beam quality requirement dictates the use of an unstable resonator.

An unstable resonator generally has energy moving outwards from its axis in such a way that the light cannot be collimated in both directions. The angular diversity that occurs in such devices makes the normal frequency selective devices impractical. The problem might be solved by using a ring resonator with unidirectional flow of energy; but that approach is rejected because of the extra complication and loss of efficiency.

A practical system can be configured either as a Master Oscillator followed by a Power Amplifier (MOPA), or as a master oscillator followed by an Injection Locked Oscillator (ILO). The MOPA approach has two major advantages. Firstly, the injected pulse may be much shorter than the final output pulse, and secondly, much higher amplification is available by this route. The success of the injection approach does rely on the medium having sufficient homogeneous broadening. Results of the injection experiments during Phase I of this program (see Section II-A-2-a) confirm the homogeneous broadening. The approach has been proven to give high amplification without sacrifice of beam quality, using a wide variety of active media. (27-29) It has been


demonstrated to work well when injecting unstable resonators.\textsuperscript{(30-31)} The injection reduces the buildup time of the injected oscillator with a resulting increase in output energy.\textsuperscript{(32)} A few watts of injected power are ample to give good spectral locking of the type of laser proposed, but the discussion of the next section will demonstrate the desirability of injecting considerably more power from this master oscillator, to reduce buildup time in the ILO.

2. Resonator for the Injection Locked Oscillator (ILO)

Analysis of the laser cavity trade-offs leads to choice of an unstable resonator of length 1 m, and transverse dimensions of 6 by 4 cm. The active medium will be 62.5 cm long by 6 by 4 cm. The requirements are met by the confocal unstable resonator shown schematically in Figure 64. It has a magnification ratio of 1.67 and a corresponding feedback of 36\%. It uses mirrors with radii of curvature of 5 and 3 m. Since it has confocal geometry it will have a collimated output, and thus utilize the medium efficiently.

The transient buildup of the lasing is discussed in Appendix A. The buildup time of this ILO without injection, if restricted to 1 A spectral width, would exceed 50 ns. It is shown that injection of 3 kW will save 35 ns of this buildup time. Based upon the nominal 250 ns pulse, this reduction in the delay time will add 13\% to the energy of the output, as well as giving spectral control without adding any lossy elements in the resonator. The savings in buildup time and consequential increase in output of the laser, for various values of injected power, are listed in Table A-1 and plotted in Figure 65.


Figure 64. Proposed Resonator for Unstable ILO (Schematic)
Figure 65. Increased Output of ILO vs. Injected Power
The injection must span the critical time during the pumping cycle when the gain first appears and the transient buildup commences. Light injected before this time, or after, will be ineffective. The system can be regarded as behaving like a multipass power amplifier immediately after the injection. The beam quality of the initial output is dominated by the beam quality of any portion of the injected light that sufficiently matches the mode structure of the unstable resonator to survive in the resonator long enough to be amplified to high level before exiting. Thereafter the feedback will take over as the source of the lasing, and the mode characteristics of the unstable resonator will impose themselves more and more strongly. At this point any further injection will be insignificant compared with the energy already circulating in the resonator.

One might question whether the optical lengths of the master-oscillator and the ILO should be precisely matched, so that the longitudinal modes are correspondingly matched in frequency. The longitudinal intermode frequency interval for these resonators will be about 150 MHz, hence there will be about 500 such modes circulating. If the resonators are not closely matched, there will be overlap between a sufficient number of these modes for efficient injection. However there is a more important consideration helping us, in that the round trip gain of the ILO is sufficiently high during the transient buildup time that the resonant properties of the ILO will not have a significant filtering action on the injected longitudinal modes during that portion of the cycle. The resonant properties of the ILO will become important later in the cycle when the active medium goes into saturation and the net round trip gain becomes unity, because only at that time do the fines in the successive passes have nearly equal intensity so that the interference effects become significant. In other words, the longitudinal matching is not a problem.

Clearly however the injected light must have the required spectral characteristics for surviving many passes of the ILO and

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then emerging with the required beam quality. This problem will be addressed in the next section.

3. Injection Interface

The ILO will be injected through a coupling mirror that is shared between the master oscillator and the ILO, for maximum efficiency. Otherwise a large portion of the injecting laser's output would be lost by reflection on entering the ILO.

An inherent property of unstable resonators is that the light traveling in opposite directions does not repeat itself, whereas in a stable resonator the light does repeat itself. This presents a dilemma when trying to match the transverse modes from a stable resonator into those of an unstable one.

This problem has been addressed by Goldhar et al. (32) They have developed a recipe for ensuring satisfactory spatial mode matching when injecting an unstable resonator from a stable resonator using a shared mirror. Given that the mode of the stable resonator has to have its wavefront match the surface of the shared mirror, the recipe requires choosing the size of the injected spot such that when it reaches the opposite mirror its radius of curvature R closely matches the geometric wavefront of the expanding mode of the unstable resonator. They verified experimentally that this does work, achieving good injection locking and near diffraction limited output from the injected laser.

When this recipe is applied to the proposed resonator of Figure 6, it yields an optimum spot radius \( w \), for the lowest order Gaussian mode of the stable resonator at the shared mirror, to be 0.49 mm. We have analyzed the subsequent evolution of such a fundamental mode, after injection, using the Kogelnik and Li formulation for the propagation of such a mode. (33) The beam was

tracked after repeated bounces from the opposing mirrors until it reached a radius where it would exit from the unstable resonator. The result is plotted as the lowest curve in Figure 66. The ratio w/R is plotted against the spot radius w for the propagating beam at the successive interactions with the mirror that is in the exit plane. This ratio w/R is the semi-angle of the geometric divergence of the beam. For comparison, the semi-angle of the diffraction limit, λ/2w, is plotted as a dashed line that appears immediately above the first plot. It is clear that a Gaussian beam injected through the shared mirror with a fundamental spot radius of 0.49 mm will indeed successfully inject the laser and result in an output beam that is very nearly diffraction limited.

Also plotted in Figure 66 are the results of a similar analysis of beams that are injected through the shared mirror with fundamental Gaussian spot radii of 2 and 0.2 mm. It can be seen that, although these have greater divergence than in the optimum situation, they will still emerge with less than 5 times diffraction limited divergence. The additional plot for a 5 mm Gaussian radius injected spot shows that it will have divergence approaching 20 times the diffraction limit. It is clear that, while a radius of about 0.5 mm is ideal, a factor of two either way is not too critical in this application, but a greater mismatch should be avoided.

The above analysis shows that if a fundamental Gaussian spot of about 0.5 mm spot radius is injected as described during the critical time when the gain is first appearing, then it will make multiple passes in the resonator, growing on each pass by the magnification ratio, until it emerges with much the same beam quality as that with which it entered (assuming no medium distortions). A higher order mode entering at the same place and with its wavefront matched to the same shared mirror, must likewise match the same wavefront curvature on the opposing mirror, and hence can be expected to expand in the same manner. It however will start with a larger diameter and hence will make a lesser number of passes.
Figure 25. Divergence of injected Gaussian TEM$_{00}$ mode as it propagates in 1LO
before it exits. Hence it will see less gain and be discriminated against. It follows that the light that first emerges from the injected oscillator will have a higher proportion of the energy in the lower order mode than that which was injected. Subsequently the spatial filtering action of the feedback mechanism will come into play, and the output will become more and more dominated by the characteristics of the unstable resonator (see Section III-k).

4. Master Oscillator for Injection

It now remains to design a suitable oscillator for providing the injection signal, having as its output mirror the shared one of 3 m radius of curvature. It should have a Gaussian fundamental mode of ~ 0.5 mm spot radius at this mirror.

A stable resonator which meets these objectives is shown schematically in Figure 67. The Kogelnik and Li type analysis\(^{(3)}\) gives the parameters that are tabulated in Figure 67. The 0.52 mm spot radius at the shared mirror is a sufficiently good match to ensure successful injection, as shown in the preceding section. Further details of the design are discussed in Appendix B.

It is anticipated that an aperture of ~ 1.4 mm diameter, placed as indicated in the resonator, will allow sufficient modes to oscillate so that the laser is not too critical in its alignment, and yet will give a beam quality from this oscillator that is within two times the diffraction limit. Such details will finally be optimized experimentally.

5. Spectral Control

A diffraction grating will have adequate spectral selectivity to ensure a width of < 1 Å. It will use a substrate of Corning 7940 or Schott Zerodur, which both have temperature expansion coefficient of ~ 3 × 10\(^{-6}\)/°C. This will ensure spectral stability over a temperature range > +/- 100°C. It will need adjustment capability with a precision and stability of 2 arc sec to the center of the HgBr line, and then maintain the tuning stable within 0.1 Å. The development to spectral widths of 0.2 Å...
Figure 67. Proposed Master Oscillator for Injection ILO (Schematic)
or less (Appendix C) can be done either with a diffraction grating at a higher angle of incidence or with an intracavity etalon. A suitable etalon would have a spacing of about 1 mm. Trade-offs in the selection will involve efficiency, stability and ease of control. The technology for the spectral control is well developed within AERL as a result of the extensive experience over a period of 10 years with the JNAI program for isotope separation, where spectral widths and absolute wavelength accuracy of < 0.02 Å have been routinely achieved, with corresponding stability.

6. Choice of Shared Mirror between Resonators

There is a conflict between desiring a high reflectance for this mirror to reduce leakage of lasing light from the unstable resonator, and desiring a lower reflectance to increase the efficiency of the injecting laser.

Commercially available diffraction gratings have only 80% guaranteed absolute diffraction efficiency at the wavelength of 5000 Å. When higher efficiencies are cited they invariably turn out to be "relative" values, or for the infrared. This drives the optimum reflectance for the output mirror (which is this shared mirror) to < 90%, as illustrated by the curve of Figure 68, which plots the anticipated output power of the oscillator versus the reflectance. Diffraction gratings with higher efficiency are within the state of the art. However it is questionable whether the small increase in overall efficiency of the system would warrant much effort in this direction.

It is technically feasible to design the mirror with a reflectance locally in the region of the injection, and higher reflectance elsewhere. However analysis shows that the gain to be achieved in the overall output, compared with best optimization with a uniform mirror, would be only 2×. Hence the additional risk to the beam quality, and the complication, is not justified.

The trade-off in selection of the mirror reflectance is heavily influenced by the relationship between injected power and resultant increase in efficiency of the unstable resonator, which
Figure 68. Power for Master Oscillator vs Reflectance
is shown in Figure 65. The data from Table 8 and Figure 65 are combined in a plot 'A' of Figure 69, to show the increase of ILO efficiency as a function of the shared mirror reflectance, excluding the effect of leakage of ILO light through the shared mirror. This additional loss is plotted as curve 'B' of the same figure. Curve 'C' is obtained from the difference, and shows the net efficiency increase of the ILO, from the injection, as a function of the shared mirror reflectance. A choice of 98% is sufficiently close to optimum, and will increase the output of the system by 13%, as a result of the injection.

Higher reflectance than 98%, while giving a little more efficiency, would be unwise because scatter and absorption losses and problems would then start becoming significant.

The combination of spectral control and added efficiency that come from the ILO approach makes it very attractive for this application.

7. Injection Laser

For system simplicity we choose an avalanche discharge laser similar to that built at NOSC. \(^{(34)}\) However in the place of UV preionization we would use corona discharge preionization using a "corona bar" behind one of the discharge electrodes. This technique has worked well with small discharge pumped rare gas-halide lasers. \(^{(25)}\) It has the advantage of not requiring spark sources which may be difficult to make for long life operation.

The laser small-signal gain and pulse length is expected to be similar to those of the NOSC device. In this case to achieve a cm gain for 75 ns pulse length, a mixture of Ne/N\(_2\) HgBr\(_2\) will be used with a discharge energy input of 100 J/cm. For the assumed 20 x 1 x 1 cm volume the input power will be 200 W.

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\(^{34}\) Mohr, R., private communication.

\(^{25}\) Niles, R. private communication.
Figure 69. Increased Output of ILO vs. Reflectance of Shared Mirror
at 100 pps. Allowing for an electrical circuit efficiency of 0.8
the power consumed by the injection laser will be 240 W.

The flow required for the injection laser can be taken from
the main flow loop. The flow required will be of order of 1/4 of
the main flow and will be neglected here.
G. E-BEAM

1. Design Approach and Rationale

The operating parameters of the e-beam are listed in Table 8. In this section, we will first discuss the general approach of the e-beam design, in view of the overall device requirements. This will be followed by a more detailed description of our preliminary design of the e-beam system, including two main options for electrical pulsing.

The important elements of the design are:

- Thermionic Dispenser Cathode
- Bakeable Vacuum System
- Conduction Cooled Titanium Foil Window
- Grid Switched dc or Externally Pulsed High Voltage Options.

The rationale for these choices are as follows:

**Thermionic Dispenser Cathode** was chosen as the most viable candidate for achieving a broad area uniform emission of 2 A/cm² for the required $10^8$ pulses, being scalable to $10^{10}$ pulses and lifetimes of several times $10^4$ hrs. Near term requirements can be met and exceeded based on already demonstrated cathode performance, including verified heater power consumption of $\leq 6$ W/cm².

**Bakeable Vacuum System** has been incorporated into the design of the e-gun to ensure reliable activation and efficient cathode performance. A base vacuum of $\leq 10^{-9}$ torr, and $\leq 10^7$ steady-state vacuum under e-beam operation is considered as a realistic design goal. This can be achieved using standard high-vacuum technology with oil-free pumps, all metal seals and ceramic bushings with a bake-out capability of 350°C. Further reduction of outgassing can be achieved by electron bombardment cleanup, if necessary.

**Conduction Cooled Titanium Window** is selected to provide long life under cyclic stresses as required for the present application. The relatively modest foil loading of $\sim 2$ W/cm² can be handled by a pure titanium foil, but increased heat conductivity is achieved by coating the foil with a thin layer of copper.
<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Voltage</td>
<td>300 kV</td>
</tr>
<tr>
<td>Emission Density (Cathode)</td>
<td>2 A/cm²</td>
</tr>
<tr>
<td>Current Density (Gas)</td>
<td>1 A/cm²</td>
</tr>
<tr>
<td>Pulse Duration</td>
<td>0.25 µs</td>
</tr>
<tr>
<td>Rise, Fall, Droop</td>
<td>max 10%</td>
</tr>
<tr>
<td>Area</td>
<td>250 cm²</td>
</tr>
<tr>
<td>Total Current (Gas)</td>
<td>250 A</td>
</tr>
<tr>
<td>Impedance</td>
<td>1200 Ω</td>
</tr>
<tr>
<td>Pulse Energy</td>
<td>20 J</td>
</tr>
<tr>
<td>Rep. Rate</td>
<td>100 Hz</td>
</tr>
<tr>
<td>Average Power</td>
<td>2000 W</td>
</tr>
<tr>
<td>Life</td>
<td>$10^8$ pulses</td>
</tr>
</tbody>
</table>
Grid Switched and Externally Pulsed High-Voltage Options are considered as two possible alternatives for powering the e-gun. Key components to be considered are the step-up transformer, required for the external pulsing, and the graded bushing for the grid switched approach. The preliminary design of the e-gun structure can be adapted for either method, being conservatively sized for dc voltage standoff. Selection of externally pulsed high voltage would, however, allow a more compact design of the gun.

3. E-gun Design Description
   a. Vacuum Chamber

   The vacuum chamber for the e-gun is a cylindrical vessel with hemispherical ends, as shown in Figure 70. It has two large openings for the foil system and the negative high-voltage terminal ports for attaching pumps and gauges. The chamber is a vessel under external pressure, and therefore, is liable to failure due to elastic instability. In view of the discontinuous structure created by the large cutouts, the shell is designed with a big safety factor on buckling. The chamber is constructed of stain-
less steel and uses metal seals in accordance with standard high-vacuum technology practice.

   The interior of the chamber will be ground and polished to a smooth surface in order to minimize both electrical stress and corona. Final finishing is by a Divorse dip process which
   removes all defects of the surface and produces a finish similar to electropolishing. The average electric field at 300 kV is
   limited with maximum value at the negative terminal of 33 kV/cm.

   b. High-Voltage Terminal

   The high-voltage terminal, also shown in Figure 70, has the
   negative high-voltage terminal and is also constructed of
   stainless steel. The jacket section in the center of the unit is the attraction of the high voltage bushing. On the front
   side, the negative high-voltage terminal serves as the unit of
the high-voltage bushing, split and the joint 2/8 reachable
   from the back, accommodating the internal parts.
Figure 70. E-Gun Schematic Drawing
The cathode forms one wall of a copper liquid cooled box, and is indirectly heated by tungsten filaments. The 4 cm x 6.25 cm dispenser cathode assembly consists of modular blocks as shown in Figure 71. The heaters are operated at 1400°C or less to ensure long life. A stack of heat shields behind the cathode provides thermal insulation in order to conserve heater power. Space behind the cathode box is utilized for electrical connections and cooling pipes.

**c. High-Voltage Bushing**

The high-voltage bushing will be a brazed ceramic and metal ring structure which must stand off 300 kVdc voltage, provide mechanical support for the e-beam terminal, and which must also have sufficient temperature capability to permit bakeout. There are accelerating tube sections commercially available which have suitable characteristics. The bushing shown in Figure 70 would operate at an average electric field of 15 kV/cm. A coaxial line (solid or cable) from the high-voltage power supply terminates inside the bushing. This coaxial line will be made to carry heater power, control power and coolant connections inside the inner conductor as required. Also, inside the bushing a high impedance grading resistor chain must be provided for dc operation. If pulsed operation is adopted, the bushing will be capacitively self- grading and no resistor chain will be necessary. The interior of the bushing will be filled with SF₆ at a few atmospheres pressure to make its voltage capability at least as good as the vacuum side. It is assumed that the coaxial line and grading resistor will be removed during bakeout.

**d. Pumping Bakeout and System**

The required base vacuum of $\leq 10^{-9}$ torr will be achieved with an oil-free pumping system, metallic seals throughout, and bakeout at 350°C. The roughing system will consist of a pump and cryogenic absorption pumps. Valves and a control system is provided to control and monitor the system. The expected outgas rate is $\sim 10^{-11}$ torr l/sec/cm² outgas, or $\sim 200$ l/sec, which can be provided by an
Figure 71. Dispenser Cathode Assembly Schematic
ion pump of standard type. This pumping capacity should also be sufficient to handle the anticipated gas load due to surface desorption by electron bombardment and be able to maintain a steady-state background level of $< 10^{-7}$ torr during e-beam operation, assuming a desorption coefficient of about $10^{-2}$ molecules/electron.

The e-gun chamber has been designed so that it may be separated from the laser cavity and enclosed in an oven for bakeout. The baking temperature of $350^\circ$C is consistent with the temperature capabilities of all components including the foil support structure.

e. **Foil and Foil Support**

The foil system consists of a titanium alloy foil of 0.5 mil thickness supported by a perforated plate having ~3/16-in. diameter circular holes and a geometrical transmission factor of ~50%. Considering the size and operating conditions of this device the proposed foil system is designed to provide simple and effective cooling and adequate fatigue life.

The foil material, Ti-6Al-4V, has excellent strength in the temperature range the foil will experience. Its fatigue strength and notch sensitivity are well known at this time and the use of annealed material provides a significant degree of ductility which will allow the foil of yield to accommodate possible imperfections in the machining of the support plate.

The support plate will be made of beryllium-copper 10 alloy to secure a combination of good structural strength at operating temperature and high thermal conductivity to permit a simple cooling system. An equilateral triangular hole layout will be used to maximize the open area of the foil structure.

3. **E-Beam Pulsed Power**

The pulsed power needed for e-beam operation, see Table 8, is modest in terms of energy per pulse and average power, however, the 300 J/pulse must be delivered in an approximately square pulse of 0.25 $\mu$s duration at 300 kV with high efficiency. It is also
required that the power supply and its components has long life expectancy, at least $10^8$ pulses, and a degree of reliability consistent with other subsystems in order to meet the overall systems reliability specification. It is logical to examine the total reliability of the power supply and e-gun in view of the possible design trade-offs. The most evident trade-off is between internal grid-switching of the gun and external high-voltage pulsing.

a. **Internal Grid Switching Option**

This option puts the main burden on the gun design in terms of its dc voltage holdoff capability, failure modes and possible damage, and ability to recover from arcing. The critical components in terms of survivability is the high-voltage bushing and the foil. The bushing must have dc grading and should not be designed for higher electric fields than ~ 25 kV/cm. The foil should be designed with sufficient protection against arcing such as provided by the drift space between anode and foil shown in Figure 70. Also, provisions must be made to interrupt the prime power source within one interpulse time, or < 5 ms. This can be done with an SCR controller in the prime XF-rectifier circuit.

The high-voltage power supply itself in this case is simply an RC or LC charged capacitor that has to store ~ 5 times the pulse energy or ~ 100 J at 300 kV to limit the droop to ~ 10%. Rise and fall times can be made short and are principally limited by the inductance and capacitance of the gun structure and the grid pulser circuit, which operates at low (10-15 kV) voltage and typically uses a thyratron switched PFN to produce the desired pulse duration.

b. **External High-Voltage Pulsing**

Compared to the grid switched dc e-gun, the short pulse length will allow much high stress levels to be used in the design of an externally pulsed e-beam. Vacuum stress levels of $\geq 60$ kV/cm are used in this case for commercial vacuum tubes operating at the 300 kV level, such as klystrons. The impedance level of ~ 1000 $\Omega$. 
is also typical of high power klystrons and commercial pulse modulators exist that are designed for $\geq 10^9$ pulses. The main difference between this application and typical klystron tubes is approximately 10 times shorter pulselength. The critical component for our system would be the step-up transformer required to get from $\sim 40$ to 300 kV with $< 25$ ns rise and fall time. Although we see no fundamental reason why this transformer could not be built, it is not a shelf item and would require development and testing. It should be designed with a bifilar secondary winding for providing filament power; this would eliminate the separate isolation transformer needed for the dc scheme. A possible hybrid approach would also be worth considering, i.e., using a combination of external pulsing and grid switching. The relative timing of the two switches can be used as a means to optimize the pulse shape and energy transfer efficiency of the e-beam system.

c. E-Beam Power Requirement

The overall power requirement of the e-beam system is dominated by the high-voltage power supply and the heaters for the thermionic dispenser cathode. The average e-beam power is 2 kW. A conservative estimate of the transfer efficiency of prime power into the e-beam is 80%. The power requirement on the high-voltage power supply is therefore 2.5 kW. The total area of the dispenser cathode is 250 cm$^2$. The projected power consumption of the cathode for the design vacuum conditions, is 2.7 W/cm$^2$ in radiation from the emitting area, or 675 W. Radiation losses from other areas of the cathode structure are estimated to be 200 W and conduction will contribute another $\sim 400$ W. The overall power consumption of the 250 cm$^2$ cathode would therefore be 1.3 kW. This makes the overall power requirement for the e-beam system 3.8 kW.
H. MAGNETIC FIELD DESIGN

1. Field Requirement

In the present design a magnetic field is used to guide and confine the e-beam from the e-gun cathode through the e-gun grid, e-gun anode, foil support structures and active laser volume. The guide field serves the following functions:

Firstly, the magnetic field prevents beam spreading in the active volume due to scattering from the foil and laser medium. This improves the e-beam energy deposition uniformity both along the e-beam and transverse to the e-beam. It also allows for sharper edge definition of the discharge so that less discharge energy is wasted in the weakly pumped fringe regions where no useful laser energy is extracted. These issues have been addressed in Section III-C. For this the field strength should be maximized.

Secondly, it prevents pinching of the e-beam due to a transverse self-magnetic field produced by the discharge which would otherwise constrict the discharge, and lead to a highly nonuniform energy disposition. For this the applied field needs to be much greater than the discharge self-field.

In the present design we have chosen a field intensity of 4 T. This is a compromise between keeping the magnetic stresses on the field coil from being excessive and the desire to have better edge definition on the discharge volume. With this field intensity beam steering by self-magnetic field of the e-beam is negligible in the e-gun and beam pinching in the discharge is negligible.

The size of the field coil was chosen to be 120 x 70 cm measured on the center of the winding. This allows the magnet to be conveniently fitted around the e-gun and also produces a field with acceptable divergence in the discharge region.

A computer simulation of a single current loop was used to obtain the amount of current required and the uniformity of the field generated in the discharge region. The loop center was 15 cm above the center of the discharge region, (Z direction)
± 60 cm long (X direction) and ± 35 cm wide (Y or flow direction), see Figure 72. It was found that $3.62 \times 10^5$ A-turns are required to produce a field of 4,000 G at the center of the discharge region. The strength of the coil needed for other field values can be obtained by direct proportion.

2. **Field Uniformity**

Table 9 gives data for the field uniformity in the discharge region. The origin of the X, Y, Z coordinates is the center of the discharge region, (Figure 72) 15 cm below the plane of the current loop. $B_z$ is the field in the Z or principal direction. $B_z/B_x$ is the ratio of the field at right angles to $B_z$, to its principal value. We are particularly interested in the magnetic field in the gas flow or X-direction because this determines the divergence of the beam in the Y-direction. The ratio of $B_x$ to $B_z$ is shown in the last column. This table shows that the greatest spreading of the B-field is in the Y-direction, amounting to about 7.5% of the principal field. However, in the important X-direction, the spreading is only of the order of one-half percent or less.

3. **Coil Design**

The overriding consideration in designing a magnet coil is the conservation of electric power. For this reason, the only coil that could be seriously considered is a superconducting coil in which the principal use of electric power is for refrigeration. A permanent magnet could not be chosen for this application because of the large magnetizing force required. Also, coil configurations which include windings on both sides of the discharge region are considered to be quite impractical in view of (a) the increased refrigeration which is roughly proportional to the number of coil units and (b) the large intercoil compressive forces that would have to be taken through the dewar insulation and across the gas duct. This would further increase the required refrigeration because of heat leaks in the structures supporting the coils, and would greatly complicate the construction of the gas duct.
Figure 72. Magnetic Field Coordinates
<table>
<thead>
<tr>
<th>x cm</th>
<th>y cm</th>
<th>z cm</th>
<th>$B_z$ (10^3 G)</th>
<th>$B_x/B_z$</th>
<th>$B_y/B_z$</th>
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<td>0.006</td>
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<td>-0.157</td>
<td>0</td>
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<td>0.005</td>
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<td>4.72</td>
<td>-0.124</td>
<td>0.005</td>
</tr>
</tbody>
</table>
flow duct. On the other hand, a simple superconducting loop can provide the required magnetic field with only a small amount of refrigeration, and no reaction forces on external objects provided that they are nonmagnetic.

A typical superconducting coil assembly is shown in Figure 7. Details of the design could, of course, be left to the coil manufacturer. However, this figure illustrates some of the considerations that determine the coil size and the required refrigeration. The superconductor, may be either niobium-titanium, or niobium-tin, both commercially available materials. Niobium tin has the advantage that it can operate at a higher temperature and therefore uses less refrigeration power. However, both types of superconductor can be accommodated without straining the state of the art and without exceeding 1 kW of power.

A niobium-titanium coil operating between 4.2° and 4.5° in a bath of liquid helium is chosen for illustration. Consider that the solid has a cross section of 6.5 x 6.5 cm and an ampere-turn value of 3.6 x 10⁵ so that a 4,000 G field would be obtained in the laser discharge region. The peak magnetic field at the surface of the conductor bundle is given by

$$B_{\text{max}} = \frac{nI \mu_0}{4D}$$

where \(D\) is the height of a square winding. With \(nI = 3.6 \times 10^5\), \(B_{\text{max}} = 1.75 \times 10^4\) G. This is a reasonable and conservative peak field for a superconductor. The windings are subjected to an internal compression of 2.0 atm, well within the capability of common insulating materials and common superconducting wires. Therefore, the winding can be layer built with porous glass cloth used as interlayer insulation and for the distribution of liquid helium in the windings. The conductor itself can be insulated with formvar or similar material.
Figure 73. Typical Superconducting Coil Assembly
It is important to choose a fine wire so that the current per turn is small. In this illustrative design, the wire chosen is niobium 46% titanium and a copper to superconductor ratio of 1:1. The wire diameter is 0.020 in. and the current supplied is 200 A. At a peak field of 20,000 G, this conductor can carry 266 A and therefore it is conservatively loaded. The overall packing factor in the coil is 0.065 which is extremely low and therefore there is ample room for interlayer insulation. The reason that so low a current is chosen is because the principle source of heat to the superconducting coil is the power generated in the leads that conduct current to the coil. In a space environment, the upper terminal of the leads could be fixed at the temperature of the dewar radiation shield, ~ 80°K and the lower terminal at 4.2°K. Under these conditions, the heat generated in a pair of suitably designed leads is 0.0015 W/A (this is half the power generated for leads operating from 4° to 300°).

Thus, with 200 A, 0.3 W is generated merely in the power leads.

4. Dewar Construction

The dewar can consist of three concentric containers made of polished stainless steel. Each container is fabricated in two parts joined by seam welding. The inner container holds the coil and liquid helium. The intermediate container is a radiation shield at about 80°K. Cooling for this temperature is automatic with no liquid from the refrigeration cycle. The outer container is at whatever environmental temperature is encountered in the satellite. The assumption here is that it will be ~ 300°K. The space between the three containers are evacuated and several layers of lightly flocked superinsulation are used in these spaces to limit radiation heat transfer even more than would be obtained with simple polished surfaces. This type of construction is quite standard. The radiation heat transfer from the liquid helium container with this type of insulation is estimated at 0.018 W. A larger source of heat leak is by conduction in the tubing of the
turrets used for introducing the current leads and the liquid helium transfer tube. For example, if the helium container turret consists of two tubes 1.5 in. diameter, by 0.010 in. thick, by 8 in. long, the estimate is that these will consume 0.089 W of refrigeration. Thus the total refrigeration requirement for this coil is calculated to be 0.41 W. A 1/2 W refrigerator will provide an adequate margin of safety.

During high G-loading, the mechanical forces of the three container can be supported by snubbers in the vacuum space, designed to limit motion, but making no direct contact under normal circumstances.

For a space environment, the helium container should be kept full and all boil off taken through the current leads and returned to the refrigeration system. The weight of the coil, liquid helium, dewar, but excluding the refrigerator is estimated at 32.5 kg.

5. Refrigerator Power

A ground based commercial refrigerator supply 1 W of refrigeration at 4 K would consume ~ 3 kW. However, for space applications, the efficiency has been very greatly improved.

R.W. Breckinridge, Jr. (16) has constructed the critical part of a refrigerator for space applications and has tested it. It produces 1 W of refrigeration at 3.6 K and consumes 1300 W. The efficiency at 4.5 K would be slightly higher and Dr. Breckinridge estimated that 650 W would be the input power requirement for 1 W of refrigeration. This refrigerator weighs 100 lbs and occupies a space of 10 in. x 24 in. x 26 in. The refrigeration cycle is a reverse Claude cycle with double ended, reciprocating engines.

The coil charging supply will provide 200 A at 3.6 K.

16. Breckinridge, R.W., Jr., AFFDL-TR-68-59, Oct. 1968, "Experim-
entary Development of a 1 W, 3.6 K, Reciprocating Refrigerator for Space Applications." (A.D. Little, Cambridge, MA.)
2. Use of Nuclear Heat

The design has prepared for nuclear steam applications and, except for the refrigerator, every item in commercially available and conservatively sized. Therefore, there is no need to select the more expensive, but more reliable, which is the trend today. Work to be continued still experimental.

Nonetheless, a nuclear steam plant is constructed with the same considerations. The operation at low, yet reliable, is being regarded the thermal performance. This makes the nuclear steam plant a cost effective and attractive option for energy production.
I. PULSE DISCHARGE MODULATOR DESIGN

1. Circuit Topology

In designing the discharge modulator for the HgBr Phase II laser, two types of discharge circuit were considered: Blumlein and line pulser.

a. Blumlein Circuit

Figure 74 is a schematic diagram of the laser using a Blumlein circuit to pulse the discharge. The Blumlein circuit has the advantage that the output voltage into a matched load is equal to the charging voltage, \( V_0 \). Into an open circuit the Blumlein gives twice the charging voltage. This occurs when the wave initiated by the thyratron is reflected at the open circuit and the voltage between the grounded side of the load and the common side of the energy storage line then goes from \( +V_0 \) to \( -V_0 \). Since the ungrounded side of the load is at \( -V_0 \) with respect to the common side of the energy storage line, the voltage across the load (open circuit) will be \( 2V_0 \).

A disadvantage of the Blumlein circuit is that the switch current is twice the current into a matched load. This occurs because the voltage across the load and the charging voltage are equal but the thyratron sees \( Z_B \), the stripline impedance, whereas the load impedance is \( 2Z_B \). This places more stringent requirements on thyratron \( \frac{d^2}{dt^2} \) and inductance. The voltage produced during the rising part of the pulse by a Blumlein circuit across a matched load can be shown to be

\[
V = V_0 \left( 1 - e^{-\frac{4Z_B}{L_s} \frac{t}{L_L}} - \frac{Z_B}{L_s} t - e^{-\frac{4Z_B}{L_L} \frac{t}{L_s}} \right) \tag{65}
\]

where \( L_L = \) load inductance

\( Z_B = \) switch inductance
Figure 74. Blumlein Circuit
Therefore, the time constant associated with the switch is $T = \frac{L_s}{Z_B}$.

b. **Line Pulser Circuit**

Figure 75 is a schematic diagram of the line pulser circuit, an alternative to the Blumlein for exciting the laser discharge. In this circuit a section of line is charged to twice the desired load voltage. When the switch is closed the charged line section is connected to the load. The resulting voltage into a matched load is half the charging voltage. However, a compensating advantage of this circuit is that the switch current is equal to the current in the load. In this circuit the voltage produced during the rising portion of the pulse across a matched load can be shown to be:

$$V = \frac{V_0}{2} \left( 1 - e^{-\frac{2Z_0}{L_L + L_s}} \right)$$

The time constant associated with the switch inductance is then $T = \frac{L_s}{2Z_0}$. However, since $Z_0$ (line pulser) = 2$Z_B$ (Blumlein) the inductance which can be accepted in the line pulser circuit is 4 times that in the Blumlein. An examination of the circuit verifies that the thyratron sees an impedance of $2Z_0$ in the line pulser circuit.

The thyratron operating conditions for both the Blumlein and line pulser circuits were discussed with the three major thyratron manufacturers in the western world, EG&G, English Electric Valve and ITT. They all preferred the higher voltage, lower current conditions in the line pulser circuit.

2. **Networks**

We shall discuss the design criteria for lumped element networks for the line pulser circuit.
Figure 75. Line Pulser
Figure 76 shows the classical Guillemin five section networks. Since in our modulator design the inductance of the capacitors is small but the thyatron does have significant inductance, a design in which the thyatron inductance can be included as part of the network would be preferred. This eliminates the type C and F networks from consideration. The type D requires coupling between the inductors to give the required mutual inductances. This will be difficult to achieve at the low inductance values required. The type A network would meet our requirements but the series configuration will tend to give excessive stray inductance and the uncharged capacitors add weight without storing energy. This leaves the type B network which meets all our requirements with no significant disadvantages.

In order to simplify the design a number of test cases were analyzed using the Control Data Syscap network analysis program. The energy storage subsystem will consist of eight identical pulse forming networks with one terminal of each network connected to the common thyatron and the other terminal connected to one of eight output cables. The analysis was performed on one of the eight parallel networks. For comparison purposes a simple five section "transmission line" network was analyzed as shown in Figure 77. The overshoot and slow fall time are characteristic of this network. Figure 78 shows the performance of the unmodified B network. Figure 79 shows a variation of the B network with the first four capacitors and inductors equal, the last capacitor twice the others and last inductor a variable.

The version shown in Figure 79(c) was chosen for further analysis. In Figure 80 the first inductor is varied while the other components are kept constant. This shows that increasing the output inductor improves performance by reducing overshoot. A conceptual drawing of a stripline connected pulse forming network is shown in Figure 81.

1. Thyatrons

The factors which influence thyatron operation at high di/dt levels have only been recently understood. The major factors that determine the rate of current rise are 1) the trigger...
Figure 76. Equivalent Forms for Five-Section Guillemin Voltage-Fed Network. Multiply the values of the inductances by $Z_N T$ and the values of the capacitances by $\tau/Z_N$. The inductances are in henrys and the capacitances in farads if pulse duration $\tau$ is expressed in seconds and network impedance $Z_N$ in ohms. (Adapted from "Pulse Generators," G.N. Glasoe and J.V. Lebacqz, Boston Technical Publishers, Lexington, MA 1964.)
Figure 77. Transmission Line Pulse Forming Network
Figure 78. Performance of Unmodified Type B Network
Figure 79. Performance of Modified Type B Network
Figure 80. Performance of Modified Type B Network with Change in Output Inductor
Figure 81. Conceptual Drawing of Pulse Forming Network Configuration
plasma density and distribution at the onset of commutation (determined by the grid configuration and the method of triggering),
2) the plasma growth rate (determined by the fill gas pressure), and 3) the effective inductance (determined by the distribution of
the internal discharge as well as by the geometry of the tube and its external current return). (37)

To achieve minimum switching delay and maximum circuit
int, the tube must be designed for such operation and the cor-
rect method of triggering must be used.

To obtain the best initial conditions for commutation, the
trigger discharge must establish a relatively high plasma density
near the cathode surface. To obtain low inductance, the discharge
must be spread over the cathode surface to the maximum extent. To
aid this process, an auxiliary (or priming) grid is used. The
auxiliary grid is located between the cathode and the control
grid, and its geometry is designed to confine the trigger plasma
near the cathode.

To fully form the discharge before commutation, the auxil-
iary discharge is prepulsed at a high current level. A high
current auxiliary grid prepulse is necessary but not sufficient to
achieve high di/dt. When the ion density near the grid baffle a-
peratures reaches a value of \( \sim 10^{11} \) ions/cm\(^3\), the tube will com-
mutate, regardless of the state of the discharge near the cathode.
If a weak auxiliary current is used (e.g, 20 to 100 mA), trigger-
ing density will not be reached, and a separate control grid pulse
must then be used to trigger the tube. It has been reported that
\( \Delta V_{th} \) is lower when the trigger pulse is applied to the control
grid as opposed to the auxiliary grid. (38)

(37) Turnquist, D., Caristi, R., Friedman, S., Merz, S., Plante,

(38) Friedman, S., Goldberg, S., Hamilton, J., Merz, S., Plante,
P., and Turnquist, D., Proc. IEEE Thirteenth Pulse power Mod-
To prevent premature commutation, negative control grid bias is used. The effect of the bias is to lengthen the time available for the auxiliary current to grow and to spread ion the cathode. A small bias (-20 V) produces a small 4% increase in commutation delay, but a large 25% increase in \( \frac{di}{dt} \).\(^{(37)}\)

A new model has been developed for the hydrogen thyratron that can predict the behavior of thyratron-switched pulse circuits. It is assumed that the thyratron can be modeled by two series elements 1) a constant inductance, dependent only on geometry, and 2) an exponentially falling resistance or voltage, with a time constant \( \tau_i \) dependent only on gas pressure.\(^{(37)}\)

Thyratron specifications contain a "Plate Breakdown Factor," \( \text{Pb} \), intended to limit anode dissipation to tolerable levels. Although it has long been recognized that this factor is inadequate to describe the problem, it has only recently been possible to quantify anode dissipation in high \( \frac{di}{dt} \) circuits. The results of this analysis is to replace the old \( \text{Pb} \) factor with a new factor, defined as

\[
\pi_b = \text{voltage} \times \text{repetition rate} \times \frac{\text{di/dt}}{(\text{epu prr} \times \text{di/dt})}
\]

The model described in Ref. 37 has been used to calculated anode heating when switching a transmission line charged to a voltage, \( V \). Defining a circuit time constant, \( L/Z \) (with \( L \) the total switch and connecting inductance, and \( Z \) the total impedance of the line plus the load directly across the switch), it can be shown that the anode dissipation energy per pulse, \( W \), is a function of \( \tau_i/\tau_L \) as shown in Figure 82, and the power dissipation is directly proportional to \( \pi_b \).\(^{(37)}\) Anode dissipations consistent with the above calculation have been observed in practice for tubes operated at high \( \frac{di}{dt} \). At a few tens of kilovolts with a fast circuit, the anode dissipation can become substantial, i.e., several hundred watts per kilohertz of repetition rate. The magnitude depends critically on \( \tau_i \), normally for thyratrons about 30 ns (corresponding to a 20 ns fall time). This can be reduced to at least 20 ns at higher pressures (> 0.6 torr). On the other
Figure 82. Anode Heating in a Transmission Line Circuit  
(Adapted from Ref. 37)
hand, reduction of pressure can cause much higher $r_i$, with the resultant high dissipation causing excessive anode heating. Thy- ratrons for fast switching applications must therefore operate at relatively high fill pressures to minimize anode dissipation as well as to promote high $di/dt$.

If the initial plasma conditions are properly established during triggering, and the resistive fall limit is not reached, then the self-inductance of the tube and its current return will dominate the switching operation. The inductance can be calculated from the physical dimensions of the discharge and the current return, making the assumption that the discharge fills the tube to the diameter of the grid apertures.

Some recent results at Los Alamos have shown that the number of pulses that a thyratron can switch before ceasing operation under high $di/dt$ operation is a function of repetition rate in some thyratrons. Examination of the thyratron components after testing at high $di/dt$ and high-repetition rates shows erosion of the tips of the cathode structure. The tubes used (EG&G) have a complex interleaved cathode structure designed to give the maximum cathode area in the minimum space. This suggests that the current under high $di/dt$ operating conditions is supplied primarily by the tips of the cathode structure. At high-repetition rates heated generated at the tips of the cathode structure would not have time to thermalize and spread uniformly throughout the cathode structure, thus resulting in excessive temperatures at these points and therefore erosion. This further suggests that thyratrons with a less complex and more rugged cathode structure may have longer lifetimes under high $di/dt$ and high repetition rate conditions.

The thyratron manufacturer ITT can supply a thyratron which meets our design point requirements in the line pulser configuration. The ITT data is derived from thyratrons on the Stanford 39. Private Communication, McDuff, G., 1981.
linear accelerator where ~10^7 hr of life data has been obtained. For the design point conditions the thyratron lifetime extrapolates to 2 \times 10^4 hr at 100 Hz, which is 7 \times 10^9 pulses.

4. **Modulator Efficiency**

The loss power of individual modulator components has been calculated in detail and is summarized in Table 10. The modulator delivers a power of 10 kW to the laser discharge, and hence its overall efficiency is 89%.
### TABLE 10. ENERGY BUDGET FOR MODULATOR

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<th>Loss (W)</th>
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<td>High-Voltage Rectifier Diodes</td>
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<tr>
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<td>Conduction</td>
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<tr>
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<tr>
<td>Commutation</td>
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<tr>
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<tr>
<td>Control Circuitry</td>
<td>100</td>
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<tr>
<td><strong>TOTAL</strong></td>
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J. GAS CLEANUP/MAKEUP

1. Chemical Processes

In order to efficiently use the HgBr laser for space applications it will be necessary to reuse the laser mixture many times. The most extended efforts to address the issue of the gas mixture recyclability involve experiments currently underway at NOSC.\(^{(40)}\) The drop-off in output power as a function of time is analyzed for a UV preionized discharge pumped laser \(^{(40)}\) which is repetitively-pulsed at \(\sim 40 \text{ pps}\). The laser mixture, \(\text{HgBr}_2/\text{N}_2/\text{Ne}\), is circulated around a flow-loop to remove the excess heat produced in the discharge. When the laser is turned on the output energy is \(\sim 35 \text{ mJ/pulse}\). This corresponds to an intrinsic efficiency of 0.7\%. This is near optimal for this type a system operated in a single pulse mode.\(^{(41)}\) The laser power drops to the half power point in about 45 min, or 110,000 shots. The ratio of the discharge volume to the flow volume is about 1 to 300, so that each discharge volume \((\sim 45 \text{ cm}^3)\) can be used \(\sim 350\) times before the power drops to 50\%. This suggests that in order to maintain the output to at least 90\% of its initial value, 1.5\% of the mix must be continually replaced or purified.

The laser system proposed here has an average discharge volume flush factor of 3.5 (flush factor of 1.75 at 200 Hz) so that, after accounting for the higher \(J/l\), \(\sim 0.7\%\) of the flow must be processed. Figure 83 shows the correlation between the fraction of the flow removed and the mass of \(\text{HgBr}_2\) which must be handled for \(10^8\) shots. From this graph it can be seen that if 0.7\% of the flow is processed, 800 kg of \(\text{HgBr}_2\) must be either replaced or purified and returned to the system.

\(^{40}\) Celto, J.E., private communications.

Figure 83. Amount of HgBr₂ Processed vs. Fraction of the Flow Removed
In order to evaluate what possible purification or replenishment procedures are necessary and to see how to make improvements on the recyclability, it is necessary to look at the chemical reactions involved in the regeneration of HgBr$_2$ from the excitation products. Model calculations indicate that $\sim 20\%$ of HgBr$_2$ molecules in the discharge region will end up as HgBr(x) and Br. The following reactions are then possible from the interaction of HgBr and Br:

(a) HgBr + HgBr $\rightarrow$ Hg$_2$Br$_2$ (g)
(b) Br + Br $\rightarrow$ Br$_2$
(c) HgBr + Br $\rightarrow$ HgBr$_2$
(d) HgBr + HgBr $\rightarrow$ Hg + HgBr$_2$
(e) HgBr + Br $\rightarrow$ Hg + Br$_2$

The rate constants for reactions (a) and (b) have been measured and found to be $1.5 \times 10^{-30}$ cm$^6$ sec$^{-1}$ (42) and $1 \times 10^{-32}$ cm$^6$ sec$^{-1}$ (43), respectively. The rate constants for the other reactions are not known so that it is difficult to estimate the relative importance of these processes. However, reasonable estimates of the rate constants would indicate that these processes would go to completion in a few tenths of a millisecond. This would then leave a mixture of HgBr$_2$, Hg, Br$_2$ and HgBr in the argon buffer gas.

There is the possibility that Hg$_2$Br$_2$ could react ion-molecule with Br$_2$

$$\text{Hg}_2\text{Br}_2 + \text{Br}_2 \rightarrow 2\text{HgBr}_2$$

or with Br

$$\text{Hg}_2\text{Br}_2 + \text{Br} \rightarrow \text{HgBr}_2 + \text{HgBr}$$

However a large portion will most likely condense on the walls of the flow-loop. Then, depending on the local Hg density, the Hg$_2$Br$_2$ will remain on the walls as a solid or decompose into

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Hg and HgBr_2. The deposition of Hg_2Br_2 in the flow-loop was observed in the NOSC (40) apparatus as soon as the laser was turned on. Data for the vapor composition (44) over Hg_2Br_2 also indicates that, under the temperature and HgBr_2 pressure conditions of the proposed system, if the local Hg pressure rises to 0.4 torr, Hg will react with HgBr_2 to condense out as Hg_2Br_2.

Br_2 will react with the solid Hg_2Br_2 at the walls.

(f) Hg_2Br_2(s) + Br_2 + 2HgBr_2

This process was observed in supplementary experiments at NOSC. (40) Also possible is the direct reaction

Hg + Br_2 + HgBr_2

However, it is expected that, as was the case for Hg + C_2, (45) this reaction will occur only at the walls and thus the rate is limited by the collision frequency with the walls.

The processes outlined thus far show how the system can return completely to the thermodynamically favored state of pure HgBr_2 in argon. However, there is not sufficient data to determine the rate of the final recombination process and thus it is not known what the quasi-equilibrium concentrations of Hg and Br_2 will be in the following system. Since Hg could interfere with the HgBr*(B) production and Br_2 could be a significant absorber, it is important to determine the rates of the wall reactions under the proposed conditions.

What is clear from this analysis is that if either Br_2 or Hg is removed from the cycle, then a decrease in laser output will result. Therefore, the materials used in the laser system must not only be unreactive with HgBr_2, but also with Hg and Br_2. Reactivity could result in a loss of HgBr_2 or the production of absorbers such as Br_2 or a volatile metal halide. The NOSC laser apparatus had tungsten and stainless steel in contact with the flowing gas.

Since tungsten reacts with $\text{Br}_2$ at their temperature\(^{(40)}\) and stainless steel will react with both $\text{Br}_2$ and $\text{HgBr}_2$, reactions with these metals is a likely cause for the decrease in laser output they observed.

Experiments designed to test various metals for use as electrode material were conducted at Westinghouse Laboratories.\(^{(46)}\) Electrodes made from the material to be tested were vacuum sealed inside a quartz cell with enough $\text{HgBr}_2$ to fully vaporize and provide a pressure of 1-2 torr at the 175°C operating temperature. Discharge voltage was capacitively coupled to the electrode from a 100 kHz high-voltage supply. The electrode materials tested were stainless steel (304, 316), molybdenum, platinum, and nickel. Of these, only platinum allowed extended running of the discharge without loss of $\text{HgBr}^*(B)$ fluorescence. With the other materials the $\text{HgBr}^*$ fluorescence severely decayed in a few hours with an accompanying appearance of several mercury emission lines.

The results of these experiments indicate that platinum will be a good material to coat the metal surfaces in the laser cavity and flow-loop. Additional evidence in support of this comes from data on the surface chemistry of platinum. Measurements of the mercury vapor decomposition pressure for various platinum mercury amalgams\(^{(47)}\) indicated that at the maximum mercury pressure allowed by the $\text{Hg}_2\text{Br}_2$ condensation (0.4 torr), no amalgam was formed.

Possible reactivity of platinum with bromine is not clear. $\text{Br}_2$ is known to react with Pt\(^{(48)}\) at \(\sim 150^\circ\text{C}\) to form $\text{PtBr}_4$. However, this compound is unstable above $180^\circ\text{C}$ and $\text{PtBr}_2$ is formed. This compound is likewise unstable above $250^\circ\text{C}$. Unfortunately, both gold and platinum show a maximum in

\(46.\) Private communications.

\(47.\) Jung, V. G. and Dorthoudak, T., Metallkd., 2., 64, 715 (1971).

the rate of corrosion in Cl₂ at the temperature at which the corresponding chloride decomposes. The success of the Westinghouse experiments with platinum electrodes is most likely due to the reaction of the PtBr₂ formed with Hg to form the more stable HgBr₂. In this way, platinum may play an important role as a catalyst to enhance the otherwise slow recombination Hg + Br₂.

With the return of platinum metal to the surface by the reaction of PtBr₂ with Hg there will be no net loss of platinum. However it is not clear what affect this process may have on the protective function of a platinum coating. In the flow-loop, the coating can be made thick enough so that the integrity of the coating can be maintained.

It is clear from this discussion that all the metal surface should be coated with platinum. The electrical insulators for the electrode support can be made out of alumina. Because of the porous nature of the surface of this material, it may be necessary to allow for a certain amount of seasoning during the laser setup phase, but there is no evidence to suggest any reactivity between alumina and the other species present. The MgF₂ overcoating on the cavity windows is expected to be likewise inert.

By constructing the cavity and flow-loop out of materials which do not chemically interfere with the reaction mix it should be possible to greatly improve on the recyclability over that observed in the NOSC experiments.

However, additional problems could arise from outgassing of H₂ from the metal surface. The H₂ will react with Br₂ to form HBr. There are two possible sources of the H₂. One is the hydrogen dissolved in the stainless steel during the fabrication process and the second is hydrogen introduced into metal during electroplating.

The first source can be taken care of by baking all the metal parts prior to electroplating. The outgassing rate has been measured for stainless steel baked under varying conditions.\(^{(50)}\) In order to keep the pressure of HBr to \(<10\%\) of the HgBr\(_2\) density in \(10^8\) shots, it will be necessary to limit the outgassing rate to \(<1 \times 10^{-9}\) torr liter cm\(^2\) sec\(^{-1}\). The data in Ref. \((50)\) indicates that this outgassing rate at 490\(^{\circ}\)K can be obtained by baking the stainless steel for 16 hr at 400\(^{\circ}\)C.

The amount of the \(\text{H}_2\) infused into the stainless steel during electroplating can not be handled in the same manner because the integrity of the coating may not withstand the high temperatures necessary for the outgassing process. However, since the electroplating is done for only a few hours at near room temperature, the amount of time to release this gas will be correspondingly short, especially after bringing the laser system up to the operating temperature.

The difficulties of outgassing \(\text{H}_2\) can be taken care of by baking all metal parts before plating and by allowing the final system to be pumped on at operating temperature for a few days before running the laser.

2. Gas Cleanup System

The discussion above has indicated that the use of nonreactive materials such as platinum, alumina, and glass in the laser system should allow the laser mix to be recycled indefinitely. Some difficulties however could arise such as porosity or cracking in the metal protective coating, unexpected secondary reactions, or slow outgassing of some components. These processes could introduce impurities into the flow stream and thus reduce the laser output during the course of the long life test.

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For this reason, the flow-loop will be equipped with a system for trapping out all the material from a certain fraction of the flow and replenishing it with pure HgBr₂. By analyzing the material trapped, it will be possible to determine the source of any such impurity so that modification can be implemented accordingly. It should then be possible to reduce the fraction of processed flow to the point where the trapped material can be thrown away. If this is not possible then the analysis can be used to design an HgBr₂ purification scheme.

A schematic of the trapping/replenishing system is shown in Figure 84. A fraction of the flow enters the system from the high pressure portion of the flow-loop. In this first segment of the purification line there will be a set of sapphire windows which will allow transmission spectra to be taken of the gas flow. This information will be used to monitor the HgBr₂ density as well as detect and identify impurities. A throttle valve in the line will be used to control the fraction removed. The gas then enters the trap. Most of the possible contaminant will have low enough vapor pressures to be effectively trapped at room temperature. This includes, in addition to the HgBr₂, materials like metal halides and organic oils and greases. If analysis of the gas flow indicates lower temperatures are necessary, a second trap will be added in series. At this point the gas is reheated by using a portion of the laser waste heat removed by the main heat exchanger in the flow loop. Pure HgBr₂ supply canister is adjusted to provide the correct HgBr₂ density in the laser system. The fresh HgBr₂ Ar mix is then returned to the system on the low pressure side of the flow-loop.

The system will be designed to handle 5 x 10⁻⁵ of HgBr₂. This is the amount of HgBr₂ which would have to be added to the system in 5 x 10⁻⁵ of the flow was processed for 10⁸ sec of operation. However, because the trapping system will be used as a diagnostic tool in the early phases of testing, it will be designed to effectively trap out 10⁻⁴ of the flow over a correspondingly shorter period of time.
Figure 84. Schematic of Flow Purification Cycle
The amount of power which must be extracted from the gas mix in the trap is approximated by the following expression

$$ Q = \dot{n}_{\text{Ar}} C_p \Delta T + \dot{n}_{\text{HgBr}_2} \Delta H_{\text{subl}} $$

where $\dot{n}_{\text{Ar}}$ and $\dot{n}_{\text{HgBr}_2}$ are the molecular flow of argon and HgBr$_2$, respectively, $C_p$ is the heat capacity of argon, $\Delta H_{\text{subl}}$ is the heat of sublimination of HgBr$_2$ and $\Delta T$ is the temperature. If the fraction of the flow processed is $5 \times 10^{-5}$, and the trap is kept at $300 \, ^\circ\text{K}$ then the power removed from the flowing gas is 14 W. This power can be dissipated by a 150 cm$^2$ radiator at room temperature.
K. OVERALL SYSTEM DESCRIPTION AND PERFORMANCE

In this section we want to (a) summarize the overall operating characteristics of the laser system, (b) summarize the design issues associated with long lifetime reliability, and (c) relate the features of our design to an actual space based SLC application.

1. Efficiency

In Table II, we have listed the power consumption of each subsystem for the design operating conditions.

First, the discharge power listed represents the average power consumed by the entire pulsed power system in transferring a net 10 kW from wall plug to the laser device terminals. At these terminals, the laser device is projected at 2.06% efficiency so we calculate 208 W output. The power consumption figures consider power supply transformer and diode losses, charging inductor and storage capacitor losses, switching losses and the filament heater requirements for the thyatron switches. Also, trigger generator losses are included in the power consumption figure for the pulsed power, thus it is a true wall plug calculation considering all inputs to this system.

The second power in the table is the wall plug power consumed by the pumping systems as required to provide cooling flows for the heat exchanger and the main flow. These systems are sized for an average 100 Hz but the main loop flow is sized for a maximum interpulse time (i.e., 200 Hz flow capacity). The pumps and fans efficiencies are rated at conservative values. The main loop fan has been designed to provide flow for a conservative flow factor of 1.75 and also provides the excess flow required for the cathodes, gas cleanup, etc.

The heat exchanger pressure drops and corner turning pressure losses in the flow-loop are based upon accepted design calculation approaches. Thus, we believe the calculated loop pump power losses represent an accurate design estimate. The heat exchanger cooling flow power calculation is based upon accepted design methods and similarly should be an accurate estimate.
### TABLE 11. TOTAL POWER CONSUMPTION 2 J/PULSE

<table>
<thead>
<tr>
<th>Component</th>
<th>Power (kW)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Discharge Pulse</td>
<td>11.29</td>
</tr>
<tr>
<td>Flow-Loop</td>
<td>1.56</td>
</tr>
<tr>
<td>E-Gun</td>
<td>3.59</td>
</tr>
<tr>
<td>Magnet</td>
<td>0.65</td>
</tr>
<tr>
<td>Injection Laser</td>
<td>.24</td>
</tr>
<tr>
<td>Controls</td>
<td>.2</td>
</tr>
<tr>
<td><strong>TOTAL</strong></td>
<td><strong>17.53 kW</strong></td>
</tr>
<tr>
<td>Laser Output Power</td>
<td>208 W</td>
</tr>
<tr>
<td>Overall Efficiency</td>
<td>1.19%</td>
</tr>
</tbody>
</table>
Cooling fluid pump power can be significantly reduced by special pump development not proposed here. However, additional losses may be required to circulate the coolant to radiators on the spacecraft. As these powers are liable to be small, we consider these two issues to be a wash.

The third power listed in Table 11 is the power consumed by the e-beam. This power includes the actual e-beam current, the heater losses, all foil transmission losses and the losses associated with the e-beam power supply and modulator. We do not include the power associated with the vacuum pumps, even though it is relatively negligible, since we feel this would not be an issue for the space based SLC laser.

The fourth power consumption listed is associated with the superconducting (SC) magnet. In this case we refer to a NASA design report for the projected cooling requirements for a spaced based 4°K refrigeration system. This reference provides a design value for the spacecraft bus power necessary to provide our projected requirement of SC cooling at 4°K.

The fifth power listed in Table 11 is the power required for the narrowband oscillator. This is an overall figure based upon reasonable design estimates for this system.

We have also included an arbitrary 200 W allowance for controls, alignment systems, etc. As these systems would be solid state and inherently low loss, this seems generous.

The total power consumed by all components necessary to make the laser work in the space based environment is 17.5 kW. The projected power out is 208 W. The projected overall efficiency is 1.28.

2. Beam Quality

In the proposed design narrowband single transverse mode light is injected into the unstable cavity oscillator for the first 30 ns of the 250 ns pulse. Provided that the injected frequency is at the gain maximum of the 504 nm band the transverse round trip gain at this maximum will be unity, and the signal power will not increase further in amplitude, i.e., it will be

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loss. The frequency stability is thus assured throughout the pulse. Further discussion of this is given in Appendix C.

It is possible to estimate the phase and amplitude uniformity of the unstable oscillator output during the latter 200 ns of the pulse. This is controlled by imperfection in the optics and phase distortion in the gaseous medium. Medium distortion is discussed in Section III-E-1. As a starting point the modes of the design point resonator have been computed using the standard integral methods. Figure 85 shows the computed\(^\text{(51)}\) lowest order mode intensity profile in the smaller transverse dimension (4 cm). The 6 cm dimension shows smaller peak-to-peak intensity fluctuations. Phase excursions across the mode are \(\pm 10^0\).

When a random phase perturbation is introduced to the resonator there is a degree of multiplication of the error during the several transits made before exit. Because the light passes through different transverse positions the errors are not always cumulative, but add in an appropriate rms fashion. A treatment has been given\(^\text{(52)}\) for aberrations which are uniform along the optical axis and which are separable in the x and y coordinates. The aberration \(F(x,y)\) in the plane just before the convex feedback mirror and in the limit of a geometric mode, is given by

\[
F(x,y) = \sum_{k=1}^{\infty} \alpha_k (F'_{xk} x^k + F'_{yk} y^k) \quad (67)
\]

where \(\alpha_k\) = effective number of optical passes of \(k\)th order aberration

\(51.\) AERL Resonator Code

Figure 85. Computed Intensity Profile for 4 cm Dimension of Design Point Unstable Resonator
\[ M = \frac{1}{\sqrt{1-L_c^2}} \]

The geometric output coupling is given by

\[ F'_{xk}, F'_{yk} = \text{one pass } k^{\text{th}} \text{ order aberration coefficients of power series expansion of aberration.} \]

The coefficients \( a_k \) are plotted in Figure 86 as a function of \( M \) and \( k \). For our design point \( M = 1.67 \) and the scale length for phase perturbations is such that \( 2 < k < 4 \) applies, so we derive an aberration multiplier of 2 from Figure 86.

At this point it is appropriate to specify the phase uniformity requirement to give a 10 (XDL) far field divergence. In the first instance we consider the effect of the output mirror obscuration on the far field pattern.

The relationship between the normalized phase error correlation length \( (L) \) and the allowable peak-to-peak variation in waves \( (2A/\lambda) \) is given fairly well by the geometric sinusoidal approximation (drived in Section II-E-1):

\[ \frac{2A}{\lambda} = (0.78) \, (\text{XDL}) \, (L) \]

where \( (\text{XDL}) \) is \( 0.2 \) and \( A \) is the amplitude of the optical perturbation \( (80\% \text{ of energy within (XDL)}) \). This result follows from three separate treatments which give consistent results:

1. Assumption of sinusoidal phase error
2. Use of a random phase error with a Gaussian distribution over the aperture
3. Computer simulation with specific bumpy wavefronts

by this criterion using the anticipated perturbation normalized scale length \( L = 0.2 \) we find the maximum allowable peak-to-peak variation = 1.5\( \lambda \) waves. When we fold in the aberration multiplier of 2, we require a single pass homogeneity of 0.78 waves.
Figure E. Aberration Multiplier for Fast Aisle Reflectors. These represent the effective number of passes seen by a particular order aberration.
The present design for 10 (XDL) allows the use of a centered output coupling mirror. The effect of a centered obscuration on the far field energy distribution\(^{(53)}\) is shown in Figure 87. The resonator design point has \(L_c = 1 - M^2 = 0.67\). From Figure 87 we note that 95% of the far field energy lies within 10 (XDL) and 90% lies within 5 (XDL).

When we fold together the effects of center obscuration and random phase-front error at the exit plane, the rms addition modifies the optics plus medium homogeneity requirement downward to \(\sim 0.70\) waves in a single pass. It is to be noted that the use of a corner obscuration is substantially better than a center obscuration and that it should be considered for the production of higher quality beams, when they are required.

From above, both the mode phase front and the centered obscuration contribute appreciably < 10 (XDL) to the far field divergence. The principle contributors to far field divergence are medium homogeneity and optical imperfection, which between them must contribute < 0.70 waves, peak-to-peak across the resonator aperture. In Section III-E, 0.55 waves have been allowed for medium inhomogeneity due to the gas flow, and the predicted phase-front distortion is rather less than this. The surface flatness of the intracavity windows and the laser mirrors can be as good as \(\lambda/10\) within current polishing technology. There are two windows within the cavity (4 surfaces) and two mirrors (equivalent to 4 surfaces). The window material, sapphire, can have good bulk optical homogeneity (\(\lambda/10\) in selected pieces). An rms addition leads to the optics phase front error = 0.22 waves. This is less than the optics budget of 0.43 waves which is allowed after the 0.55 waves flow budget is removed from the total 0.70 waves (rms addition).
Figure 87. Far Field Encircled Energy as a Function of Spot Size, for Centered Feedback Mirror Resonator
The near-field intensity profile has diffraction fluctuations near the edges (Figure 85), which will wash out in the far field and in any case can be greatly reduced by "softening" the mirror edge. From Section III-C-1 the discharge uniformity is good to ± 20% over the whole aperture, and this will apply to the near-field laser output, given the small allowed phase perturbations and the correspondingly small angle perturbations on geometric rays.

Thus, we project that the beam quality requirement of 50% of the beam energy within 10X diffraction limit far-field divergence can be met comfortably by the present design.

3. Lifetime

For this design we have addressed several key issues in order to project the $10^8$ lifetime required of this laser.

First, we have addressed the issue of pulsed power component selection required to achieve $10^8$ shots, with ultimate capability of $10^{10}$ shots.

We have elected thyratrons to drive our system as these devices are known to provide reliable, predictable operation for times exceeding $10^9$ pulses in radar and other applications. Under the conditions of our proposed design we project, based upon manufacturer's data, ~ $8 \times 10^9$ shot lifetime. Longer life, if necessary, can be achieved via redundancy and this is implicit in our approach.

The other components of the modulator circuit are inductors, diodes, etc., operating under no particular stress. Thus, as is usual in power supplies, if their environment is properly controlled, these components should provide many years of service reliability.

The modulator for the e-beam involves ~ 20 J/pulse if the e-beam is pulsed. Thus the modulator can be one-tenth of the discharge modulator by coupling it to the e-beam via a pulse transformer. While the pulse e-beam voltage is large, 300 kV, it is not excessive and should not represent a lifetime issue for this transformer after reasonable development.
The e-beam itself has unknown quest ons concerning vacuum breakdown. As the energy available on a vacuum arc-over is small (~ 20 J), negligible damage to the electrodes is expected from a vacuum arc. Data exists for ion accelerators used in neutral beam injectors (for magnetic fusion) which indicates rapid voltage standoff recovery to the original operating conditions when little energy is involved in an arc. Thus, while occasional "tics" may occur, the system should recover and they should be very infrequent; much less than 1% of the pulses.

The most often mentioned concern with e-beam sustained discharges is survivability of "that thin foil." This concern is addressed in our design in two ways. First, we indicate that experience with the Phase I cavity shows that arcs of very large energy do not damage the foil. This observation is consistent with many other devices at AERL where 10's of kilojoules are required in an arc to the electrodes to cause collateral foil damage. As we will have only 100 J available/pulse we anticipate no foil problems from arcs.

The other potential source of problems for a "thin foil" is the pressure induced stress. The static stresses and the temperatures involved in this laser design lead to negligible creep for the foil material chosen. Thus, creep is not a lifetime issue. Dynamic stresses have been calculated and shown to be within safe limits even when extrapolated to 10^10 shots.

The final key issue in long duration running/reliability is the impact of HgBr_2 and its fragments on the loop components and the impact of any resulting corrosion products on laser performance.

Data is limited concerning this corrosion. However, we have designed for the best known materials and anticipate that the resultant corrosion will be very low. To meet the present program objective, we need to reduce the buildup of poisons in the laser cavity by only a factor of about 100 over NOSC data. The experiment on which the NOSC data was taken was made of such materials as stainless steel.
Westinghouse data shows stainless is a very bad actor in 
HBr$_2$ discharges, while platinum, quartz, glass, etc., are not. 
Thus, since we are designing with these latter materials, we be-
lieve our design approach will achieve the desired results.
APPENDIX A
BUILDUP OF LASING AND SAVINGS FROM INJECTION

1. SUPER RADIANCE

Whenever optical gain is achieved in a medium as a result of stimulated emission, there is always an accompanying super-radiance consisting of amplified spontaneous emission.

It can be shown that the spectral radiance from such a super-radiating medium (in the case of high gain $G$ and of large ratio between population of upper and lower states of the transition) can be expressed, \(1\)

$$B = \frac{2\hbar c^3}{3} \cdot G(\nu),$$  \hspace{1cm} (A-1)

where $c$ is the velocity of light in the medium in which the measurement of brightness is being made. Now suppose we collect all the power emitted through an aperture of area $A$, and within the diffraction-limited solid angle \(\theta = c^2/A\). Then the spectral power \(P\) collected is

$$P = A B \cdot \frac{2\hbar c^3}{3} \cdot G(\nu)$$ \hspace{1cm} (A-2)

Then the collected power \(P\) is

$$P = 2\hbar c \cdot G(\nu).$$ \hspace{1cm} (A-3)

Hence, in frequency interval $\nu$, the power $P$ emitted into the
diffraction angle (into both polarizations) is

$$P = 2h\nu \cdot G \cdot I_1.$$  \hspace{1cm} (A-4)

Around $5,000 \, \text{R}$, $h \cdot \nu \approx 47 \, \text{nW/R}$.

Hence, for the HgBr system under discussion, the equivalent
input power resulting from the spontaneous emission is $47 \, \text{nW/R}$
per polarization per spatial mode.

2. THE HgBr ILO

This device will be restricted to 1 $\text{R}$ spectral width and
will be better than ten times diffraction limited (i.e., $< 100$
spatial modes). Both polarizations will be allowed. Hence, the
equivalent input power from the spontaneous emission has an upper
bound $P_{sp}$ given by

$$P_{sp} = 9.4 \, \text{nW} \hspace{1cm} (A-5)$$

3. BUILDUP TIME

The buildup time can be estimated by calculating the number
of round-trips of the ILO needed to build from $P_{sp}$ to $P_{sat}$ (sat-
uration power). A lower bound can be obtained by assuming the
small-signal gain of 3.8%/cm turns on instantaneously. In the
early part of the pulse cycle, the loss $\alpha \approx 0.5%/\text{cm}$. The feed-
back is 36$, and the length of the active medium is 6.25 cm.

Hence, the net round-trip gain $G_1$ will be

$$G_1 = 0.36 \exp (2 \times 0.0375 \times 62.5) = 39 \hspace{1cm} (A-6)$$
The number of round trips to build to the saturation power of 4.6 MW will then be

\[ N = \frac{n \left( \frac{4.6 \times 10^6}{9.4 \times 10^{-6}} \right)}{n_{G1}} = 7.3 \quad (A-7) \]

Since the resonator is 1 m long, this gives a buildup time

\[ t = 49 \text{ ns} \quad (A-8) \]

The actual buildup time will be longer because we have ignored turn-on time on the pumping as well as saturation effects.

This buildup time can be markedly reduced by injecting power many orders in magnitude higher than the spontaneous equivalent input. To estimate the reduced value of the buildup time, the value of the injected power is substituted for the 9.4 LW in relation (A-7). The resultant buildup times are indicated in Table A-1.

4. ENERGY LOSS DURING BUILDUP

Suppose the total power in the active transverse modes is initially \( P_o \), either from spontaneous emission or from injection, and a time varying excess gain \( g(t) \) is applied. Then if there were no output coupling, the power would rise according to

\[ P = P_o \exp \left( \frac{L_n}{L_r} C \cdot \int g(t) \, dt \right) \quad (A-9) \]

or

\[ P = P_o \exp \left( \frac{L_n}{L_r} C \cdot g(t) \right) \]
<table>
<thead>
<tr>
<th>Power Injected</th>
<th>1 W</th>
<th>10 W</th>
<th>100 W</th>
<th>1 kW</th>
<th>10 kW</th>
<th>100 kW</th>
<th>No Injection</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. of Round</td>
<td>4.2</td>
<td>3.6</td>
<td>2.9</td>
<td>2.3</td>
<td>1.7</td>
<td>1</td>
<td>7.3</td>
</tr>
<tr>
<td>Trips Needed</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Buildup Time</td>
<td>28 ns</td>
<td>24 ns</td>
<td>19.5 ns</td>
<td>15 ns</td>
<td>11 ns</td>
<td>7 ns</td>
<td>49 ns</td>
</tr>
<tr>
<td>Saved</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
where $\bar{g}$ is the time averaged excess gain. When the output coupling is taken into account, this becomes

$$P = P_o \exp \left\{ \left( L \bar{g} - \ln M \right) \frac{\text{ct}}{L_r} \right\}. \quad (A-10)$$

Hence, the time taken to reach the saturation power $P_s$

$$\tau = \frac{L_r}{c (L_a \bar{g} - \ln M)} \cdot \ln \left( \frac{P}{P_o} \right). \quad (A-11)$$

The maximum power that could possibly be extracted from the medium is

$$P_m = A L_a g(t) \cdot \frac{P_s}{\text{sat}}$$

where $A$ is the cross-sectional area of the active medium and $\phi_s$ is the saturation flux density. Hence, the maximum energy lost during the buildup time is

$$E_{\text{lost}} = \frac{\bar{g}}{L_a} P_s \cdot \text{sat}.$$ 

Hence, from relation (A-11), we have

$$E_{\text{lost}} = \left( 1 - \frac{\ln M}{L_a \bar{g}} \right)^{-1} \cdot \frac{L_r}{c} \cdot P_s \ln \left( \frac{P_{\text{sat}}}{P_o} \right). \quad (A-13)$$

In general $L_a \bar{g} > \ln M$ during buildup (or else it won't buildup), hence we have

$$E_{\text{lost}} \approx \frac{L_r}{c} \cdot P_s \ln \left( \frac{P_{\text{sat}}}{P_o} \right). \quad (A-14)$$
The saturating flux density will be $\approx 1.9 \times 10^5 \text{ W/cm}^2$, so $P_s \approx 4.6 \text{ MW}$. From relation (A-5) the equivalent input from spontaneous emission is $9.4 \text{ W}$. Hence, if the ILO is not injected, then the value of $E_{\text{lost}}$ is $\sim 0.41 \text{ J}$.

The value of $E_{\text{lost}}$ can be reduced substantially by injection, as illustrated in Figure A-1 which shows a plot of $E_{\text{lost}}$ vs injection. It can be seen that injection of as little as $1 \text{ mJ}$ in a $100 \text{ ns}$ pulse will save more than $0.3 \text{ J}$ of $E_{\text{lost}}$. 
INJECTED ENERGY (50 ns PULSE)

0.5 jJ 5 jJ 50 jJ 0.5 mJ 5 mJ

EXTRACTABLE ENERGY LOST DURING BUILDUP E LOST JOULES

E LOST FOR NO INJECTION

INJECTED POWER

Figure A-1. Saving of Lost Energy by Injection
APPENDIX B

DESIGN OF MASTER OSCILLATOR FOR INJECTION

The master oscillator must inject the ILO through a shared mirror of high reflectance. It must inject a beam which is predominantly in the TEM$_{oo}$ mode with Gaussian spot radius of $\sim 0.5 \text{ mm}$. A stable resonator which meets these objectives is shown schematically in Figure 66. The Kogelnik and Li type analysis$^1$ gives the parameters that are tabulated in Figure 66. The 0.52 mm spot radius at the shared mirror is a sufficiently good match to ensure successful injection of the ILO.

It is anticipated that an aperture of $\sim 1.4 \text{ mm}$ diameter, placed as indicated in the resonator, will allow sufficient modes to oscillate so that the laser is not too critical in its alignment, and yet will give a beam quality from this oscillator that is within two times the diffraction limit. Such details will finally be optimized experimentally.

The expected power from this oscillator as a function of the reflectance of the shared mirror, is plotted in Figure 67. Curves are included for different values of the diffraction grating efficiency, and for an alternative design using only 10 cm length of active medium.

The curves of Figure 67 are obtained using the relation

$$\frac{\phi_{\text{out}}}{\phi_{\text{sat}}} = \frac{(1 - R_1)}{(1 + R_1)} \left( \frac{g_0}{\frac{1}{2L_a} \ln \left( \frac{1}{R_1 R_2} \right) + \alpha} \right).$$

(8-1)

---

The appropriate values of the parameters are listed in Table 5-1. The active area of the active medium is taken as the area of the injection spot (6.4 mm diameter) in the medium.

### Table 5-1. PARAMETERS FOR OSCILLATOR

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Saturation flux density</td>
<td>$1 \times 10^5$ W/cm²</td>
</tr>
<tr>
<td>Reflectance of shared mirror</td>
<td>92% - 99%</td>
</tr>
<tr>
<td>Effective reflectance of grating</td>
<td>70% - 90%</td>
</tr>
<tr>
<td>Small-signal gain</td>
<td>10%/cm</td>
</tr>
<tr>
<td>Loss</td>
<td>0.3%/cm</td>
</tr>
<tr>
<td>Length of active medium</td>
<td>10 cm, 20 cm</td>
</tr>
<tr>
<td>Output flux density</td>
<td>---</td>
</tr>
</tbody>
</table>

The need for a high reflectance for the output mirror, which is also the injection mirror for the ILO, drives the choice of reflectance to 98%. A diffraction efficiency of 80% is the appropriate value for a good commercially obtained grating at this wavelength. Hence, from Figure 67, the expected output of the oscillator will be about 3 kW, i.e., 0.15 mJ in a 50 ns pulse.
The laser bandwidth required for the Phase II program is 1 $\text{R}$. As a part of our Phase I work we have demonstrated efficient energy extraction in < 1 $\text{R}$ by using injection locking (see Section II-A-2-c). Therefore, we do not anticipate any problems in meeting the present bandwidth requirements. However, for the planned Phase III laser, a bandwidth of < 0.2 $\text{R}$ is required. This has thus far not been demonstrated. In this section we discuss the physics of narrow band energy extraction relevant to HgBr lasers and suggest techniques by which the required Phase III bandwidth may be attained.

The B($^2\Sigma^+$) - X ($^2\Sigma^+$) lasing transition of HgBr has been identified as predominantly a $v' = 0 \rightarrow v'' = 22$ transition, but no work has been done to clarify the effect of rotational fine structure or isotope shift. Both are examples of inhomogeneous phenomena which in principle could lead to detrimental effects in the operation of a laser amplifier designed to amplify a narrow-spectrum injected signal: If the injected signal interacts strongly with only a fraction of the molecular inversion then amplification of spontaneous emission may eventually lead to a loss of frequency locking. In this section we take a first look at the important inhomogeneities and estimate their effect on injection locking.

The B-X is a $^2\Sigma^+$ transition, a type whose rotational structure is well documented. The significant rotational quantum number is $K$, the total angular momentum quantum number is $K + 1/2$. The selection rule $\Delta K = 1$ leads to two branches a P and R branch. To determine the fine spectroscopy of HgBr (or any similar diatomic)
has ever been done with sufficient resolution to detect the rotational fine structure, but we can still estimate its magnitude. The position (in cm$^{-1}$) of the fine structure lines may be described by (1)

$$ v = v_e + 2 B m - (\Delta B) m^2 $$

where $v_e$ is the electronic frequency; $B$ the average of the rotational constant $(B_u + B_v)/2$ of the upper ($\upsilon$) and lower ($\zeta$) level; $\Delta B = B_v - B_u$; and

$$ m = K, \text{ for the P branch} $$

$$ = K, +1 \text{ for the R branch} $$

$$ K_\upsilon = 0, 1, 2 \ldots $$

The rotational constant of either electronic level may be estimated from

$$ B \approx \frac{\hbar}{8\pi^2 \mu r_e^2} $$

where $\mu$ is the reduced mass (57 amu) of HgBr and $r_e$ the internuclear separation of HgBr. To our knowledge $r_e$ has never been measured, but that of a similar diatomic, HgC$_2$, has been measured to be $2.2 \times 10^{-8}$ cm$^{-1}$. We expect $r_e$ to be very nearly the same for HgBr. Thus we obtain from Eq. (C-2)

\[ B = 0.07 \text{ cm}^{-1} \]  

From the empirical relationship \(^{(1)}\) between \( r_e \) and the vibrational constant \( r_e \)

\[ r_e^2 \cdot \cdot \cdot = \text{constant} \]  

and Eq. (C-2) we may now estimate the difference \( \Delta B \) between rotational constants to be

\[ \Delta B \approx 0.02 \text{ cm}^{-1} \]

where we have used the values \(^{(2)}\) \( r_e(X) = 187, r_e(B) = 135 \text{ cm}^{-1} \). Thus we estimate that \( B \approx 0.06 \text{ cm}^{-1} \).

The laser operates at a temperature of \( \sim 500^\circ \text{K} \). In thermal equilibrium the rotational-level population distribution of the B-level is given by

\[ N(k_u) \sim (2k_u + 1) e^{-B_u k_u (k_u + 1) \frac{\hbar c}{kT}} \]  

which for \( B_u = 0.05 \text{ cm}^{-1} \) and \( T = 500^\circ \text{K} \) peaks at \( k_u \approx 60 \).

This implies that about 100 upper rotational levels are significantly populated. Since the line strengths of the fine-structure transitions are proportional to \( k \) for \( k \gg 1 \), \(^{(1)}\) we expect the intensities of the transitions to be proportional to \( k_u N(k_u) \).

From Eq. (C-1) we estimate that the P and R branches are about 50 \text{ cm}^{-1} \wide and that they are separated by much less than their widths (about 10 \text{ cm}^{-1} \).

\[ Z. \text{ Wineland, } Z. \text{ Electroch. } 64, 761 (1960). \]
With sufficient resolving power the fine structure of the \( \Delta \nu = 0 \) transition could be resolved, since the separation between adjacent rotational lines is greater than the Doppler width \( \sim 0.2 \text{ cm}^{-1} \). In the absence of collisions, extraction of laser energy from a number of rotational lines could be difficult. Under higher density conditions \((2 \text{ Amagat At gas, } \sim 3 \times 10^{14} \text{ electrons/cm}^3, 300-\text{ns laser pulse})\) however, we estimate that collisions will continuously equilibrate the populations of the rotational levels, even if all the laser energy is being extracted on a small number of fine-structure transitions. The estimate is based on a comparison with \( \text{CO}_2 \), for which it is known\(^3,4\) that at a background density of \( \sim 1 \) Amagat the rotational-level equilibration time is \( \tau_R \approx 0.15 \text{ ns} \); extraction on a single line depletes one rotational level, which is continuously repopulated at a rate \( \dot{R} = f/\tau_R \), where \( f \) is the fractional thermal population in that level. Extrapolating to HgBr we expect an even shorter \( \tau_R \) (since the rotational levels are more closely spaced than those of \( \text{CO}_2 \)) and an \( f \) of 0.02, hence we expect \( \dot{R} \approx 4 \times 10^{11} \text{ cm}^{-2} \). This rate alone should suffice to continuously populate a single rotational level from which laser power is being extracted. The presence of electrons will increase \( \dot{R} \) still further and make this aspect of efficient single-line extraction even more promising. In addition, for simultaneous extraction from several levels \( \dot{R} \) is multiplied by the number of levels; it was possible to extract with a 1 cm\(^{-1} \) (0.2 \( \text{ cm} \)) spectral-width laser the number of levels involved is on the order of 10.

We turn our attention to the other major source of inhomogeneity: the isotope shift. The two isotopes of Br, Br\textsuperscript{79}, Br\textsuperscript{81}, of nearly equal abundance, are responsible for the largest shift \((37 \text{ cm}^{-1})\) which was resolved in the spectroscopic work.

The shifts due to the 5 isotopes of Hg are about a factor of 5 smaller and have not been resolved. Because of the large widths of the P and R branches (as discussed above) we expect that 1 cm$^{-1}$ bandwidth extraction from the various molecules containing different Hg isotopes to be possible. From the presently available information it is difficult to say whether 1 cm$^{-1}$ extraction from a medium containing both isotopes of Br will be as efficient as broadband extraction. Therefore, it may be necessary to use gas containing only one isotope of Br in a device designed to amplify as a 1 cm$^{-1}$ spectral width signal.

Finally, we remark on an aspect which in our opinion is the most likely to produce line broadening in an amplifier: The central frequency portion of the injected signal may strongly saturate the available gain, while the spectral wings of the injected signal may see a larger (less saturated) gain. This effect could conceivably introduce an increase by a factor of 2 in the spectral of the amplified signal over that of the injected light. Fortunately, this effect is easily overcome by injecting a signal with a spectral width narrower than that desired in the amplified signal and/or by carefully suppressing the spectral wings of the injected signal.
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