APERTURE ANTENNA EFFECTS AFTER PROPAGATION THROUGH STRONGLY DISTURBED RANDOM MEDIA

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1 February 1984

Technical Report

CONTRACT No. DNA 001-83-C-0021

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**REPORT DOCUMENTATION PAGE**

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<th>REPORT NUMBER</th>
<th>DNA-TR-84-80</th>
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<tr>
<td>TITLE (and Subtitle)</td>
<td>APERTURE ANTENNA EFFECTS AFTER PROPAGATION THROUGH STRONGLY DISTURBED RANDOM MEDIA</td>
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<tr>
<td>AUTHOR(S)</td>
<td>Dennis L. Knepp</td>
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<tr>
<td>PERFORMING ORGANIZATION NAME AND ADDRESS</td>
<td>Mission Research Corporation PO Drawer 719 Santa Barbara, California 93102-0719</td>
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**ABSTRACT**

A strongly disturbed layer of ionization irregularities that is used as a propagation channel for radio waves can degrade the propagating wave and thereby affect the resulting measurements at the receiving antenna. The antenna aperture itself also affects measurements of the received signal by its inherent averaging process. Here an analytic solution for the two-position, two-frequency mutual coherence function, valid in the strong-scatter limit, is used to characterize the propagation.
20. Abstract (Continued)

channel. The channel itself consists of a thick slab of anisotropic electron density irregularities that are elongated in the direction parallel to the earth's magnetic field.

Analytic expressions are obtained that give the effect of the aperture antenna on measurements of received power, decorrelation time (or distance), mean time delay, time delay jitter and coherence bandwidth. These quantities are determined as functions of the aperture diameter and of the angle between the magnetic field and the direction of propagation. It is shown that in strong turbulence aperture averaging can be a significant factor in reducing the received power by angular scattering loss, increasing the observed signal decorrelation time via aperture averaging, and reducing the time delay jitter by suppression of signals received at off-boresight angles.

Results are presented for two cases. One-way propagation through an ionospheric communication channel is considered where both transmitter and receiver utilize aperture antennas. This result is easily extended to the case that one of the antennas is an omnidirectional point source, corresponding to the usual case of transionospheric satellite communication from a small satellite antenna to a large ground based receiver. The second case involves transmission and reception of a radar signal that travels through a disturbed ionospheric channel to a target located in free space. This case is applicable to the situation of a large antenna aboard a space based radar or to the case of a ground based defense radar.
SUMMARY

In this report analytic expressions are derived for the effect of aperture antennas on measurements of signals that have propagated through strong anisotropic turbulence. Results are given for the effect of Gaussian apertures on measurements of received signal power, decorrelation distance (or time), mean time delay and time delay jitter. The geometries considered correspond to the case of a single, one-way propagation path between two aperture antennas located in free space and separated by a layer of turbulence and to the case of a monostatic radar where radar and target are on opposite sides of a strong scattering layer.

All calculations depend on the analytic solution for the two-position, two-frequency mutual coherence function for spherical wave propagation in an anisotropic layer of electron density irregularities. The analytic solution for propagation in a thick layer is derived here using the quadratic phase structure-function approximation valid for strong turbulence. This result is then specialized to a thin phase-screen approximation to facilitate analytic calculation of the effects of apertures.

It is shown that antennas that are larger in diameter than the decorrelation distance that would be measured by an omnidirectional antenna can experience significant angular scattering loss and exhibit increased measurements of decorrelation distance, and decreased measurements of mean time delay and time delay jitter. Increased measurements of signal decorrelation distance are caused by the averaging effect of the antenna aperture that smooths (eliminates) the small scale signal fluctua-
tions. Decreased measurements of mean time delay and time delay jitter are caused by the action of the aperture to cut off signal contributions that originate from off-boresight angles and have therefore experienced more time delay than experienced over more direct signal paths.

Generally, the effects of aperture averaging first begin to be significant for aperture sizes that approach ten times the decorrelation distance measured with a point antenna. For even larger apertures, the aperture has a significant effect on the received signal at the antenna output that can be computed using the formulas and curves provided herein.
PREFACE

The author is indebted to Dr. Robert W. Stagat of Mission Research Corporation and to Dr. Leon A. Wittwer of the Defense Nuclear Agency for their helpful discussions regarding this work.
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SECTION 1
INTRODUCTION

Large high-gain antennas are used in many radar and communications applications to increase the energy collected, to increase angular accuracy, and to provide protection against jamming. If the wavefront at the antenna aperture experiences scintillation, large apertures can act to average the signal and thereby modify the observed signal properties. In the late fifties Wheelon (1957, 1959) obtained the well-known aperture smoothing effect for the measurement of phase fluctuations by a finite circular aperture. Since then, various investigators have studied the aperture smoothing effect on intensity scintillations in the optics regime (Fried, 1967; Tatarskii, 1971; Homstad et al., 1974) and also the related effect of optical beam wave propagation to an infinitesimal receiver (Lee and Harp, 1969; Ishimaru, 1969). Knepp (1975) obtained results for the effects of an antenna aperture on measurements of the in-phase and quadrature components and their spatial derivatives, for the case of weak scattering.

Scintillation or rapid variations in the amplitude, phase, and angle-of-arrival of a propagating wave is often observed over satellite links at VHF and UHF. Scintillation can also be observed at frequencies as high as the GHz range (Pope and Fritz, 1971; Skinner et al., 1971; Taur, 1976) and is occasionally severe, even at L-band (Fremouw et al., 1978). However, aperture averaging is not generally important at satellite frequencies (UHF-GHz) under ambient or naturally perturbed ionospheric conditions.
Worst case or Rayleigh amplitude scintillation is likely to occur if the ionosphere is highly disturbed, as for example by high altitude nuclear explosions (Arendt and Soicher, 1964; King and Fleming, 1980) or by chemical releases (Davis et al., 1974; Woicott et al., 1978). Increased electron concentrations and the irregular structure of the ionization can lead to intense Rayleigh signal scintillation at frequencies as high as the 7-8 GHz SHF band (Knepp, 1977). Consequently, the effects of scintillation are important to any UHF through SHF communications or radar system that must operate through an ionospheric channel and that may have to operate in highly disturbed propagation environments.

For cases of severe scintillation where the signal varies across the area of the receiving aperture, the effect of the aperture can be significant. It is well known that an aperture antenna acts to cut off energy that is incident at off-boresight angles where the antenna gain is reduced. This effect may also be viewed as the result of averaging or coherent processing of the electromagnetic field intercepted at the aperture location. In this report the effects of aperture averaging are analytically calculated for the case where Gaussian antenna beams are used by transmitter and receiver. Results are presented for two different physical situations. One-way propagation through an ionospheric communication channel is considered where both transmitter and receiver utilize aperture antennas. This result is easily extended to the case that one of the antennas is a point source, corresponding to the usual case of trans-ionospheric satellite communications. The second antenna geometry corresponds to transmission and reception of a radar signal that travels through an ionospheric channel to a target located in free space. This corresponds to the situation of a long-range ground or space based radar. It is shown that aperture averaging can greatly affect measurements of scattering loss, signal decorrelation time, mean time delay and time delay jitter. Simple analytic expressions are given for all these quantities in terms of the geometry of the propagation path and the severity and structure of the ionization irregularities.
To obtain results applicable to a general geometry of the line-of-sight relative to the field aligned ionization structure, it is necessary to obtain an analytic solution for the two-position, two-frequency, mutual coherence function (MCF) for spherical wave propagation through a thick layer of anisotropic electron density irregularities. It is assumed here that strong scattering conditions prevail and that the quadratic approximation to the phase structure-function is valid.

This approximation was used by Sreenivasiah et al., (1976) and by Sreenivasiah and Ishimaru (1979) for the cases of plane wave and beam wave propagation in homogeneous turbulence. More recently the two-position, two-frequency mutual coherence function was obtained for spherical wave propagation using the extended Huygens-Fresnel principle (Fante, 1981). Although the quadratic structure-function approximation can sometimes lead to difficulties (Wandzura, 1980) it is appropriate for the two-frequency mutual coherence function but not for calculation of higher moments of the field (Fante, 1980). Fante (1981) discusses the accuracy of the quadratic structure-function approximation for the case of atmospheric turbulence with a Kolmogorov power spectrum. He has found that the accuracy is a function of the irregularity power spectrum and of the strength of the turbulence (Private Communication, 1982), with accuracy increasing for stronger scattering.

This aspect of the work here is a generalization of an earlier calculation (Knepp, 1983(b)) valid only for isotropic turbulence. As in the former study, the results here are specialized to the case of a thin phase-screen approximation to the thick scattering medium. With this simplification, analytic results are obtained for the received impulse response function to a transmitted power delta function. Then results may
easily be determined for the mean time delay and time delay jitter for strong, anisotropic turbulence in the thin phase-screen approximation. Results for these quantities in this approximation have previously been shown (Knepp, 1983(b)) to closely approximate the results for a thick scattering layer for the case of isotropic turbulence.

The effects of Gaussian antennas on measurements of received power, decorrelation time (or distance), mean time delay, time delay jitter and coherence bandwidth are determined. It is shown that aperture averaging can reduce observed signal power, increase observed decorrelation time and be a significant factor in reduced observed time-of-arrival jitter at the antenna output.
SECT. 2
FORMULATION

In this section the solution for the two-position, two-frequency mutual coherence function is presented for transmitter and receiver located on opposite sides of a thick layer of anisotropic electron density irregularities. In the next section this result is utilized to determine the effect of transmitting and receiving antennas on measurements of the received signal.

Consider a monochromatic spherical wave $E(\vec{r},z,\omega,t)$ which originates from a transmitter located at $(0,0,-z_t)$ and propagates in free space in the positive $z$ direction where it is incident on an ionization irregularity layer which extends from $0 \leq z \leq L$. After emerging from the layer at $z = L$, the wave then propagates in free space to a receiver located at $(0,0,z_r)$. This thick layer geometry is shown in Figure 1. As the wave propagates, its phase substantially behaves as $(-i<k>+i\omega t)$ so write

$$E(\vec{r},z,\omega,t) = U(\vec{r},z,\omega) \exp\{i(\omega t-\int<k>(z')dz')\} \tag{1}$$

where $<k>(z)$ is the mean wave number given by

$$<k>(z) = \frac{\omega}{c} (1 - N_e/n_c)^{1/2} = k (1 - k^2/p^2)^{1/2} \tag{2}$$

where $c$ is the speed of light in a vacuum, $N_e$ is the mean ionization density, $n_c$ is the critical electron density and is related to the classical electron radius $r_e$ by $n_c = \pi/(\lambda^2 r_e)$, ($r_e = 2.82 \times 10^{-15}$ m).
Figure 1. Propagation of signals through a disturbed transionospheric channel.

In the case that the transmitted waveform is no longer a monochromatic wave, but can be expressed as a waveform modulated on a carrier, the two-position, two-frequency MCF $\Gamma$ is of interest. $\Gamma$ is important for the calculation of pulse propagation in a random medium and it serves as a basis from which to calculate the important power impulse response function and its moments. Under the Markov approximation, $\Gamma$ is found to satisfy (Yeh and Liu, 1977; Knepp, 1983(b)).

$$\frac{3\Gamma}{3z} = \frac{1}{2(k_{d}^{2} - k_{d}^{2}/4)} [k_{d}v_{d}^{2} + \frac{1}{4} k_{s}v_{s}^{2} - 2k_{s}v_{s}v_{d}]\Gamma$$

$$- \frac{1}{8} \left[ \frac{2k_{d}^{4}}{k_{1}k_{2}} A(c, n) - \left( \frac{1}{k_{1}^{2}} + \frac{1}{k_{2}^{2}} \right) k_{p}A(0) \right] \Gamma = 0$$

(3)
where $\nabla_s$ and $\nabla_d$ are the gradient operators in the sum and difference coordinate system. Here $\Gamma = \langle U(x_1, y_1, z, \omega_1) U^*(x_2, y_2, z, \omega_2) \rangle$ which is written as $\Gamma(\xi, n, z, \omega_d)$ after the sum and difference transformation. The standard transformations

$$x = \frac{(x_1 + x_2)}{2}, \quad \zeta = x_1 - x_2$$

$$y = \frac{(y_1 + y_2)}{2}, \quad n = y_1 - y_2$$

$$k_s = \frac{(k_1 + k_2)}{2}, \quad k_d = k_1 - k_2$$

are used to obtain Equation 3. In addition, it has been assumed that the frequencies of interest are much greater than the plasma frequency. The quantity $k_s$ is the wavenumber at the carrier frequency, $k_s = \omega_0/c$.

The function $A(\vec{p})$ is the integral of the autocorrelation function of electron density fluctuations, $B_\xi$, in the direction of propagation

$$A(\vec{p}_1 - \vec{p}_2) = \int B_\xi(\vec{p}_1 - \vec{p}_2, z') dz'$$

(4)

where $\vec{p}_1 - \vec{p}_2 = (x_1 - x_2, y_1 - y_2)$ and $\xi = \Delta N_e / \langle N_e \rangle$ so that

$$A(\vec{p}_1 - \vec{p}_2) = 2\pi \int \int \exp[i\vec{K}_\perp \cdot (\vec{p}_1 - \vec{p}_2)] \phi_\xi (\vec{K}_\perp, K_z = 0) d^2 K_\perp$$

(5)

where $\phi_\xi$ is the power spectrum of electron density fluctuations. Equations 4 and 5 depend upon the validity of the Markov approximation where it is assumed that the electron density fluctuations are delta-correlated in the direction of propagation (Fante, 1975). That is $B_\xi(\vec{p}_1 - \vec{p}_2, z_1 - z_2) = A(\vec{p}_1 - \vec{p}_2) \delta(z_1 - z_2)$. 

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The unknown two-frequency MCF may be written as $\Gamma = \Gamma_1\Gamma_0$ (Knepp, 1983(b)) where $\Gamma_0$ is the exact free space solution in the parabolic approximation. Substitution of $\Gamma = \Gamma_1\Gamma_0$ into Equation 3 and neglect of near-zone terms yields a differential equation with terms containing the factors $\partial \Gamma_1 / \partial X$ and $\partial \Gamma_1 / \partial Y$. Since the boundary condition at $z = 0$, $\Gamma_1(\zeta, \eta, z=0, \omega_d) = 1$, is independent of $X$ and $Y$, the derivatives with respect to these quantities may be neglected. The change of variables $z' = z + z_t$, $\theta = \zeta / z'$, $\phi = \eta / z'$, and the additional substitution $\Gamma_1 = \Gamma_2 \Gamma_3$ where

$$\Gamma_3 = \exp \left\{ - \frac{1}{8} A(0)(z' - z) k_b \left( \frac{1}{k_1} - \frac{1}{k_2} \right)^2 \right\}$$

(6)

and the replacements

$$a = \frac{1}{2} \frac{k_d}{k_s}$$

(7a)

$$b = \frac{1}{2} \frac{k_p}{k_s}$$

(7b)

$$v = (abA_2)^{1/2} z' = a_1 z'$$

(8a)

$$\mu = \left( \frac{1}{a^2 b A_2} \right)^{1/4} \eta = a_2 \theta$$

(8b)

$$\varepsilon = \left( \frac{1}{a^2 b A_2} \right)^{1/4} \phi = a_2 \phi$$

(8c)

enable one to write the equation for $\Gamma_2$ as

$$\frac{\partial \Gamma_2}{\partial v} = \frac{1}{v^2} \left( \frac{\partial^2}{\partial u^2} + \frac{\partial^2}{\partial \varepsilon^2} \right) \Gamma_2 - \left( \mu^2 + \Delta^2 \varepsilon^2 \right) v^2 \Gamma_2 = 0$$

(9)
where $A(\zeta, n)$ has been expanded in a truncated Taylor series

$$A(\zeta, n) = A_0 + A_2 \zeta^2 + \Delta^2 A_2 n^2$$  \hspace{1cm} (10)

(see appendix). This is the quadratic phase structure function approximation. The difference wave number $k_d$ has also been neglected with respect to $k_s$. The effect of this assumption is to restrict the validity of the solution to a small range of wavelengths centered about $k_s$.

**Thick Layer Solution**

An analytic solution of the form

$$\Gamma_2 = f(v) \exp\{-g(v)u^2-h(v)v^2\}$$  \hspace{1cm} (11)

may be substituted into Equation 9 to obtain three equations, the first consisting of terms that are factors of $u^2$, the second consisting of factors of $v^2$, and the third independent of $u$ and $v$. These equations may be solved exactly for $\Gamma_2$, and the results substituted into Equation 3 to yield

$$\Gamma_1(0, \phi, z'=L+z_t, \omega_d) = F \exp\{- (A-Bt)^2 - (A-\Delta Bt') \phi^2\}$$  \hspace{1cm} (12)

where

$$F = \exp\left(-\frac{\sigma^2 \omega_d^2}{2\omega_0^2}\right) B_{a_1}(L+z_t)$$

$$\times \left[\frac{\Delta}{(B_{a_1} z \cosh B_{a_1} L + \sinh B_{a_1} L)(\Delta B_{a_1} z \cosh \Delta B_{a_1} L + \sinh \Delta B_{a_1} L)}\right]^{1/2}$$  \hspace{1cm} (13)
In transcribing Equation 6 for \( \Gamma_3 \), the relationship between the coefficient \( A_0 \) and the phase variance \( \sigma^2 \) given by Equation A-6a is utilized. Equation A-5 gives the expression for the quantity \( \Delta \) in terms of the geometry of the line-of-sight relative to the magnetic field direction.

To complete the solution, it is necessary to solve for \( \Gamma_1 \) in the region \( L \leq z \leq z_r \) (see Figure 1). Equation 12 serves as the boundary condition at \( z' = L + z_t \). Since the region \( z' > L + z_t \) corresponds to free space with no ionization, Equation 3 is appropriate after the \( \Gamma_0 \) substitution is included, insertion of the \( z', \theta \), and \( \phi \) substitutions, and deletion of the last term involving the function \( A \) that is zero in free space.
The Fourier transform

\[ \Gamma_1(\theta, \phi, z', \omega_d) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} e^{i(K_\theta \theta + K_\phi \phi)} \]

\[ \times \tilde{\Gamma}_1(K_\theta, K_\phi, z', \omega_d) \, dK_\theta dK_\phi \]

may be substituted into the suitably modified Equation 3 to obtain the algebraic equation

\[ \frac{3\tilde{\Gamma}_1}{\partial z'} + i \frac{k_d}{2} \frac{1}{k_s^2} \left( \frac{K_\theta^2 + K_\phi^2}{z'} \right) \hat{\Gamma}_1 = 0 \]  

Equation 20 may be solved, and the boundary condition Equation 12 applied at \( z' = L + z_t \) with the result

\[ \tilde{\Gamma}_1(K_\theta, K_\phi, z_t + z_r, \omega_d) = \tilde{\Gamma}_1(K_\theta, K_\phi, L + z_t, \omega_d) \]

\[ \times \exp[-i\gamma(K_\theta^2 + K_\phi^2)] \]

where

\[ \gamma = \frac{1}{2} \frac{k_d}{k_s^2} \frac{(z_r - L)}{(L + z_t)(z_t + z_r)} \]  

The final result may then be obtained by taking the Fourier transform of Equation 12 to obtain \( \hat{\Gamma}_1(K_\theta, K_\phi, z_t + z_r, \omega_d) \) and then taking the inverse Fourier transform of Equation 21. The required integrals are easily found, and the result may be written as
\[
\Gamma_1(\zeta, n, z_t + z_r, \omega_d) = \frac{F}{[(1 + i4\gamma(A - Bt)) (1 + i4\gamma(A - A\Delta Bt'))]^{1/2}} \\
\times \exp \left\{ -\frac{\zeta^2(A - Bt)/(z_t + z_r)^2}{1 + i4\gamma(A - Bt)} - \frac{n^2(A - A\Delta Bt')/(z_t + z_r)^2}{1 + i4\gamma(A - A\Delta Bt')} \right\}
\]  (23)

Equation 23 is the result for \( \Gamma_1 \) after propagation through a thick layer characterized by anisotropic electron density irregularities. The full solution for the two-position, two-frequency MCF is obtained by multiplication by \( \Gamma_0 \), the free space MCF. Since \( \Gamma_0 \) is not affected by the random layer, it may be ignored here.

Thin Phase-Screen Approximation

Much simplification is possible if the thick scattering layer is replaced by an equivalent thin phase-screen of infinitesimal thickness and the same overall phase variance. To the first order, in the thin phase-screen approximation

\[
\cosh \Delta \alpha_{1L} = 1
\]  (24a)

\[
\sinh \Delta \alpha_{1L} = \Delta \alpha_{1L}
\]  (24b)

\[
\tanh \Delta \alpha_{1L} = \Delta \alpha_{1L}
\]  (24c)

Utilizing these approximations as well as Equations 8a-c and Equation 18 for \( a_1 \), \( a_2 \), and \( \beta \), the two-position, two-frequency MCF is found in the thin phase-screen limit as
$$\Gamma_1(z_t, z_r, n, \sigma, \omega_d) = \left[ \frac{1}{1+i \frac{\omega_d}{\omega'}} \left( 1+i \frac{\omega_d}{\omega'/\Delta^2} \right) \right]^{1/2}$$

$$= \exp \left\{ -\frac{\Delta^2}{2 \omega_0^2} \exp \left\{ -\frac{z_t^2 / z_0 \Delta^2}{\frac{\Delta^2}{\omega_0^2} + 1+i \frac{\omega_d}{\omega'/\Delta^2}} \right\} \right\}$$

(25)

where

$$\begin{align*}
\Delta^2 &= \frac{(z_t + z_r)^2 A_0}{z_t^2 \sigma^2 A_2} \\
\omega' &= -\frac{\pi \omega_0 (z_t + z_r) A_0}{\lambda z_r z_t \sigma^2 A_2}
\end{align*}$$

(26)

Equations 25-27 are valid for any anisotropic power spectrum for which, in the strong scattering limit, the phase structure-function can be expanded in the form of Equation 10. For the anisotropic Gaussian power spectrum of interest in this work, $A_0/A_2 = -r_0^2$, where $r_0$ is the axial scale size of the elongated irregularities as discussed in the appendix. The parameter $\lambda$ is a measure of the decorrelation distance of the complex electric field as measured in the plane of the receiver; $\omega'$ is the coherence bandwidth and will be shown to be inversely proportional to the time delay jitter; $\sigma_\phi$ is given in the appendix as the phase standard deviation imposed on the wave by the phase-screen.
In this Section, appropriate expressions are derived to obtain the effect of the antenna aperture on measurements of the properties of the received signal during strong scintillation conditions. The first geometry considered is that of a spherical wave that propagates through the disturbed layer to a receiving aperture antenna. Results for this case are then easily extended to the case of a transmitting and receiving antenna and then to the case of a monostatic radar geometry.

Consider the geometry shown in Figure 2 where the aperture is located in the receiver plane, z = z_r. If the incident field in the plane of the antenna is $U(\rho, z_r, \omega)$, then the complex voltage envelope at the antenna output may be expressed as (Price, Chesnut and Burns, 1972)

$$v(\rho_0, z_r, \omega) = \int U(\rho', z_r, \omega) A_r^*(\rho' - \rho_0) \, d^2\rho'$$  \hspace{1cm} (28)

where $U$ is the solution to the parabolic wave equation at location $\rho'$ in the receiver plane for a monochromatic signal of frequency $\omega$, $\rho_0$ is the location of the center of the aperture antenna and $A_r^*$ is the complex antenna weighting function.

Equation 28 gives the output voltage from an aperture antenna pointed in the z-direction for a transmitted monochromatic waveform of radian frequency $\omega$. If the transmitted waveform is a pulse waveform modulated on a carrier, the transmitted signal can be expressed as

$$s(\tau) = \Re \{m(\tau) \exp(i\omega_0 \tau)\}$$  \hspace{1cm} (29)
where \( \omega_0 \) is the carrier radian frequency and \( m(\tau) \) is the modulation waveform. After passage through a layer of irregularities, the received signal may be written (Knepp, 1983(a)) in the absence of an antenna, as

\[
\begin{align*}
    r(\rho, z_p, \tau) &= \text{Re}\left\{ e(\rho, z_p, \tau) \exp(i \omega_0 \tau) \right\} \\
    &= M(w) U(\rho, z_p, \omega + \omega_0) \exp(\i \omega_\tau) d\omega
\end{align*}
\]

The quantity \( e \) is called the complex envelope of the received waveform. \( M(\omega) \) is the Fourier transform of the transmitted modulation waveform and is given by

\[
M(\omega) = \int m(\tau) \exp(-i \omega \tau) d\tau
\]
In order to obtain the effect of the antenna on the received time-domain waveform, the received complex envelope $U$ in Equation 31 is replaced by the expression for $v$ given by Equation 28. Thus the received time-domain signal at the antenna output may be written as

$$e(\vec{p}_0, z_r, \tau) = \frac{1}{2\pi} \int M(\omega)U(\vec{p}', z_r, \omega + \omega_0)$$

$$\times A^*(\vec{p}_1 - \vec{p}_0)\exp(i\omega \tau) d^2\vec{p}' d\omega$$

(33)

In the case that the receiving aperture is an omnidirectional point antenna, $A^*$ is a delta function and the received complex envelope given by Equation 33 is identical to the result given by Equation 31.

For the case that the transmitted signal power has a delta function behavior in delay, $m(\tau)m^*(\tau) = \delta(\tau)$, the correlation function of the received power can be expressed as

$$\langle e(\vec{p}_1, z_r, \tau)e^*(\vec{p}_2, z_r, \tau) \rangle = G(\vec{p}_1 - \vec{p}_2, \tau)$$

$$= (2\pi)^4 \int S(\vec{K}, \tau)|A_p(\vec{K})|^2 \exp[iK \cdot (\vec{p}_1 - \vec{p}_2)] d^2K$$

(34)

where $S(\vec{K}, \tau)$ is the generalized power spectrum (Knepp and Wittwer, 1984) defined as the Fourier transform of the MCF,

$$S(\vec{K}, \tau) = \frac{1}{8\pi^3} \int \Gamma(\vec{p}_d, \omega_d) \exp(-iK \cdot \vec{p}_d + i\omega_d \tau) d\vec{p}_d d^2\omega_d$$

(35)

and $A_p(\vec{K})$ is the Fourier transform of the weighting function of the receiving aperture

$$A_p(\vec{K}) = \frac{1}{4\pi^2} \int A_p(\vec{p}) \exp(-iK \cdot \vec{p}) d^2\vec{p}$$

(36)
The vector \( \vec{K} \) is given as \( k \sin \theta (\cos \phi \hat{i} + \sin \phi \hat{j}) \) for the geometry shown in Figure 2.

To obtain Equation 34, use is made of the fact that the MCF depends on only the differences in position and frequency. A detailed derivation similar to the above appears in Ishimaru (1978). Note that the dependence of the power impulse response function, \( G \), on the receiver distance \( z_r \) has been omitted for notational convenience.

Equation 34 can be written in another very useful form with the substitution

\[
\hat{r}(K, \omega_d) = \frac{1}{4\pi^2} \int \hat{r}(\vec{\rho}_d, \omega_d) \exp(-i\vec{K} \cdot \vec{\rho}_d) d^2 \rho_d
\]  

(37)

where \( \hat{r}(K, \omega_d) \) is the Fourier transform of the MCF. If \( \hat{r} \) is used in Equation 34 one obtains

\[
G(\vec{\rho}_1 - \vec{\rho}_2, \tau) = (2\pi)^3 \int \hat{r}(K, \omega_d)|A_r(K)|^2 \exp[iK \cdot (\vec{\rho}_1 - \vec{\rho}_2) + i\omega_d \tau] d\omega_d d^2 K
\]  

(38)

It will be seen that Equation 38 is preferable for the evaluation of the effects of apertures on mean time delay and time delay jitter.

For later usage, it is noted that the function \( \hat{r}(K, \omega_d) \) may be obtained directly from Equation 25 as

\[
\hat{r}(K, \omega_d) = \frac{\kappa^2}{4\pi\Delta} \exp \left\{ \frac{\sigma^2 \omega^2_{\phi_d}}{2\omega^2_0} \right\} \times \exp \left\{ -\frac{\kappa^2 z^2}{4} \left( 1 + \frac{\omega_d}{\omega_0} \right) - \frac{\kappa^2 z^2}{4\Delta^2} \left( 1 + \frac{\omega_d}{\omega' / \Delta^2} \right) \right\}
\]  

(39)
Aperture Weighting Function

Let the antenna possess a Gaussian beam pattern with gain function

\[ G(\theta) = G_0 \exp \left( -\frac{\theta^2}{\theta_r^2} \right) \]  

(40)

where the receiver beamwidth \( \theta_r \) is related to the effective aperture diameter \( D \) by \( \theta_r^2 = \left( \frac{\lambda}{D} \right)^2 \left( \frac{4\pi n^2}{\lambda} \right) \) and \( \lambda \) is the wavelength at the carrier frequency. With this choice of beamwidth \( G(\lambda/2D) = G_0/2 \) so that this Gaussian aperture has approximately the same 3 dB beamwidth as a uniformly illuminated circular antenna. The antenna gain pattern is the square of the transform of the aperture response function defined earlier. Thus

\[ A_r(\overline{K}) = G_0^{1/2} \exp \left( -\frac{\theta^2}{2\theta_r^2} \right) \]  

(41)

The Fourier transform relationship of Equation 36 may be used and the small angle approximation invoked to obtain the aperture weighting function and its Fourier transform as

\[ A_r(\overline{p}) = 2\pi k^2 a^2 G_0^{1/2} \exp \left( -k^2 p^2 \theta_r^2 / 2 \right) \]  

(42)

and

\[ A_r(\overline{K}) = G_0^{1/2} \exp \left( -K^2/2k^2 \theta_r^2 \right) \]  

(43)

Before proceeding, it is useful to note that the effect of an aperture antenna is immediately apparent from the form of Equation 38. With a point or omnidirectional antenna, the beamwidth is large in Equation 43 and \( A_r(\overline{K}) \) is constant. Therefore, with a point antenna, the aperture angular response function is not important in Equation 38. It is apparent that the receiving aperture acts to modify the value of \( r \) such that

\[ \tilde{r}_d(\overline{K},\omega_d) = \tilde{r}_r(\overline{K},\omega_d) |A_r(\overline{K})|^2 \]  

(44)
where the subscript \( a \) on \( \Gamma \) denotes that this expression contains the effect of the receiving aperture. The subscript \( r \) on \( \Gamma \) on the right hand side of Equation 44 refers to the case here that the receiver is located at \( z_r \). This equation is an explicit expression of the well known result that an aperture modifies the angular spectrum of the received signal.

Case of Transmitting and Receiving Antennas

Equations 34 and 38 give the received power impulse response function for the case of an omnidirectional spherical wave transmitter and a receiving aperture antenna with aperture angular response function \( A_r(\overline{K}) \). A transmitting aperture antenna is easily included in Equations 34 and 38 since its only effect is to reduce the region of the phase-screen that is illuminated. This is accomplished by including an additional antenna angular response function \( A_t(\overline{K}z_r/z_t) \) where \( A_t(\overline{K}) \) is the response function of the transmitter with beamwidth \( \theta_t \) and where the factor \( z_r/z_t \) transforms the antenna angle utilized by the transmitter to the angle observed by the receiver. This transformation is equivalent to the observation that a ray transmitted from location \(-z_t\) at the angle \( \theta \) and that scatters from the thin layer is observed by the receiver at angle \( \theta' = z_t \theta/z_r \). For this case one may write

\[
\hat{r}_{tr}(\overline{K},\omega_d) = \hat{r}_r(\overline{K},\omega_d) |A_r(\overline{K})|^2 |A_t(\overline{K}z_r/z_t)|^2 \tag{45}
\]

where the subscript \( tr \) refers to the fact that this expression includes the effects of both transmitting and receiving apertures. Since the one-way propagation path here again utilizes a receiver at \( z_r \), \( \Gamma \) on the right hand side again appears with the subscript \( r \).
For the later calculations of scattering loss, mean time delay and time delay jitter, Equation 38 is evaluated at $\bar{\nu}_1 - \bar{\nu}_2 = 0$ where Equation 45 is substituted for the factors $\hat{r}(\bar{K}, \omega_d) |A_r(K)|^2$. That is, for the one-way propagation path with both transmit and receive apertures

$$G_{tr}(0, \tau) = (2\pi)^3 \int \hat{r}_{tr}(\bar{K}, \omega_d) \exp(i \omega_d \tau) d^2 \omega_d \quad (46)$$

For evaluation of the effect of an aperture antenna on the measured signal decorrelation distance, the necessary function is the two-position, single frequency MCF given by the Fourier transform of Equation 37 as

$$\hat{r}(\bar{K}, 0) = \int \hat{r}_{tr}(\bar{K}, 0) \exp(i \bar{K} \cdot \bar{d}) d^2 K$$

The use of $\hat{r}_{tr}$ includes the effect of both transmitting and receiving apertures.

**Case Of Monostatic Radar**

Now consider the case that the two-antenna geometry above is replaced by a monostatic radar geometry. In the radar case, the solution is facilitated by considering two one-way propagation paths. Let the radar antenna be located at $(0,0,-z_t)$ and also let the antenna angular response function be given by $A_t$ with beamwidth $\theta_t$ on both transmission and reception. First consider the one-way propagation path from the transmitter antenna to the target located at $(0,0,z_r)$. For this path, the effect of the aperture antenna is obtained from Equation 45 with the omission of $A_r$, since the point target accepts energy incident from all directions. That is,

$$\hat{r}_{m1}(\bar{K}, \omega_d) = \hat{r}_{r}(\bar{K}, \omega_d) |A_t(\bar{K}z_r/z_t)|^2 \quad (48)$$
where the subscript \( ml \) refers to the first one-way propagation path for the monostatic radar geometry.

Now consider the second one-way propagation path from the target back to the receiver. This is the propagation geometry initially considered in this report except for the interchange of receiver and transmitter location. For this one-way propagation path, \( f' \) is replaced by \( f_0 \) appropriate to the one-way propagation path from \( z_r \) to \(-z_t\). Thus

\[
\hat{\Gamma}_{m2}(\bar{K},\omega_d) = \hat{\Gamma}_{t}(\bar{K},\omega_d)|A_0(\bar{K})|^2
\]  

(49)

Note that the occurrence of \( A_0 \) here as well as in Equation 48 signifies the use of the same aperture antenna (with beamwidth \( \theta_0 \)) for reception as well as transmission. The only effect of the reversal of the direction of propagation is an interchange of \( z_r \) and \( z_t \) in the calculation of the MCF. This interchange has the effect of replacing \( f_0 \) in Equation 39 with the term \( f'_0 = z_r z_0 / z_t \).

In the case of the monostatic radar geometry under consideration, the principle of reciprocity states that the propagating signal takes the same path over each of the one-way propagation paths. This is true provided that the random medium is "frozen" for the duration of the signal traversal.

The power impulse response function for the signal received at the target due to a transmitted delta function of power from the radar is given by Equation 38 as

\[
G_1(\omega, \tau) = (2\pi)^3 \int \hat{\Gamma}_{ml}(\bar{K}, \omega_d) \exp(i\omega_d \tau) d^2K d\omega_d
\]  

(50)
If a delta function of power is transmitted from the target, the power impulse response function at the radar receiver is given by a similar expression

\[ G_2(0,\tau) = (2\pi)^3 \int \Gamma_{m2}(\vec{k}, \omega_d) \exp(i\omega_d \tau) d^2k d\omega_d \]  

(51)

The net power impulse response function after transmission of a delta function from the antenna, scattering from the target, and propagation over both of the one-way paths is given as the convolution (Ishimaru, 1978)

\[ G_m(0,\tau) = \int G_1(0,\tau') G_2(0,\tau-t') d\tau' \]  

(52)

where the subscript \( m \) refers to the monostatic radar geometry. Using the convolution theorem, it is easy to show that

\[ G_m(0,\tau) = (2\pi)^7 \int \Gamma_{m1}(\vec{k}, \omega_d) d^2k \int \Gamma_{m2}(\vec{k}', \omega_d) d^2k' \exp(i\omega_d \tau) d\omega_d \]  

(53)

This equation is the equivalent of Equation 46 for the case of the one-way propagation path.

The above considerations apply to the calculation of the power impulse response function \( G_m(0,\tau) \) for the case of monostatic radar. For this geometry the signal decorrelation distance is easily obtained as a simplification of the previous development for the one-way propagation path. For a monostatic radar, the decorrelation distance is obtained by transmission of a signal to the target and observation of the scattered signal at two spatial locations in the plane of the receiver. The point target acts as a transmitter of a spherical wave which is then observed by
the radar receiver. For a small target and frozen irregularities, there is no dependence of signal decorrelation distance on the one-way propagation path from the transmitter to the target. The necessary two-position, single frequency MCF is given in a form similar to Equation 47 as

$$\Gamma(\vec{p}_d, 0) = \int \hat{r}_{m2}(\vec{K}, 0) \exp(iK \cdot \vec{p}_d) d^2K$$

(54)

where $\hat{r}_{m2}$ is given by Equation 49 and includes the effect of the receiving radar antenna. It will be shown that evaluation of the analytic form of the expression $\Gamma(\vec{p}_d, 0)$ immediately yields the signal decorrelation distance in this strong scatter calculation.
SECTION 4
RESULTS

In this section the derivations presented in Section 3 are utilized to obtain analytic expressions for several properties of the received signal as measured at the output of the appropriate aperture antenna.

Angular Scattering Loss

An antenna aperture acts to coherently collect the energy incident upon the antenna and to deliver it to the receiver. In the transmitting mode a directive antenna is designed to transmit energy only over a selected angular region. In the receiving mode this same directive antenna accepts energy only from a narrow range of angles. Thus, relative to an omnidirectional point antenna, a directive antenna will experience what is referred to as angular scattering loss when the signal at the aperture exhibits scintillation. This angular scattering loss arises from angle-of-arrival jitter present in the incident wavefront that may cause energy to arrive at the antenna propagating at angles greater than those accepted by the receiving aperture.

A different but equivalent way to view the effect of a receiving antenna aperture is as a coherent integrator of the signal arriving on the aperture face. If the antenna is pointing towards the source of an undisturbed plane wave, then the antenna output is maximum. If there are fluctuations in the signal phase across the aperture or the incident wavefront is tilted relative to the antenna boresight direction, the coherent integrator output is decreased.
It is convenient to compute the angular scattering loss as the ratio of the total power received with an antenna (or antennas) to that received with an omnidirectional antenna that experiences no loss. In both cases the transmitted signal power is taken as a delta function in delay. The angular scattering loss may be written as

\[
\text{loss} = \lim_{\theta_t, \theta_r \to 0} \frac{\int G(0, \tau) d\tau}{\int G(0, \tau) d\tau}
\]

where the power impulse response function \( G \) is given by Equation 46 for the one-way path with both transmit and receive antennas and by Equation 52 for the monostatic radar case.

The integral of Equation 46 with respect to \( \tau \) is easily evaluated using the identity \( \int \exp(i\omega_0 \tau) d\tau = 2\pi\delta(\omega_0) \). This leaves a two-dimensional integral of \( \hat{I}(K, 0) \) over angle which involves easily found integrals of Gaussian functions. The result may be written as

\[
\text{loss} = \left( 1 + \frac{2\sigma_{\theta x}^2}{\theta_t^2} + \frac{2\sigma_{\theta x'}^2}{\theta_t^2} \right)^{1/2} \left( 1 + \frac{2\sigma_{\theta y}^2}{\theta_r^2} + \frac{2\sigma_{\theta y'}^2}{\theta_r^2} \right)^{1/2}
\]

where \( \sigma_{\theta x} \) and \( \sigma_{\theta y} \) are the standard deviations of the theoretical angle-of-arrival fluctuations in the \( x \)- and \( y \)-directions over the propagation path from \(-z_t\) to \(z_r\). The quantities \( \sigma_{\theta x'} \) and \( \sigma_{\theta y'} \) are the same standard deviations calculated for the one-way propagation path from \(z_r\) to \(-z_t\) (see appendix). The quantities \( \theta_t \) and \( \theta_r \) are the 3 dB beamwidths of the transmitting and receiving antennas, respectively.
The expression for angular scattering loss given by Equation 56 contains the effects of variations of the properties of the propagation medium and of the geometry of the propagation path. To show this result pictorially, let the antenna beamwidths be identical and let the equivalent phase-screen be located midway between transmitter and receiver. In this case \( \gamma_0' = \gamma_0 \). To simplify matters further, write the antenna beamwidth in terms of the diameter as discussed earlier. Write the angle-of-arrival jitter as a function of the signal decorrelation distance using the expressions given in the appendix. These substitutions give

\[
2\sigma^2_{T_x}/\sigma^2_0 = 0.28 D^2/\gamma_0^2 \quad \text{and} \quad 2\sigma^2_{T_y}/\sigma^2_0 = 0.28 D^2/\gamma_0^2 \quad \text{(1)}
\]

In order to separate the geometric effects of inclination angle variations from aperture averaging effects, define \( \gamma_p \) as the decorrelation distance for propagation parallel to the magnetic field line. The quantity \( \gamma_p \) is invariant with respect to changes in the inclination angle and is given from Equation 26 and A-6b by \( \gamma_p = \sqrt{\Delta z} \). The results remain a function of the axial ratio \( q \) which is here taken as 15 as suggested by Wittwer (1979).

Figures 3(a-b) show the angular scattering loss in decibels as a function of the relative antenna size, \( D/\gamma_p \) and of the inclination angle. In Figure 3(a) the inclination angle between the magnetic field and the direction of propagation is shown for values of 0°, 15°, 30°, 45° and 90°. In Figure 3(b) the relative antenna size takes the values of 1, 3, 10, 30, and 100. It is seen in both figures that only when the antenna diameter is large with respect to the decorrelation distance is the angular scattering loss significant. Small inclination angles cause increased values of the observed phase standard deviation \( \sigma_\phi \) and thus give increased angular scattering and increased scattering loss as shown. An increase in the inclination angle causes a decrease in \( \sigma_\phi \) and an effective increase in the decorrelation distance \( \gamma_0 \); therefore, the amount of angular scattering loss decreases.
Figure 3. Angular scattering loss for one-way path with transmit and receive aperture antennas; a) versus relative antenna size; b) versus inclination angle.
For the case of a monostatic radar, the power impulse response function is given by Equation 52 as the convolution of the power impulse response functions of each of the one-way propagation paths. A simple change of variables is utilized to reduce the integral \( \int G_m(0, \tau) \, d\tau \) to the product of two integrals of \( G_1 \) and \( G_2 \). These integrals are easily performed using the delta function identity discussed previously with resulting angular scattering loss:

\[
\text{loss} = \left( 1 + \frac{2 \sigma^2_{\theta x}}{\theta^2_t} \right) \left( 1 + \frac{2 \sigma^2_{\theta y}}{\theta^2_t} \right) \quad (57)
\]

where \( \theta_t \) is the radar antenna 3 dB beamwidth. A comparison of this result to Equation 56 shows that the addition of a second one-way propagation path essentially squares the scattering loss.

Figures 4(a-b) show the angular scattering loss for the case of a monostatic radar geometry as a function of the inclination angle and of the relative antenna size \( D/k_p \). Here \( k_p \) is the decorrelation distance observed for propagation parallel to the magnetic field along the path from \((0,0,z_r)\) to \((0,0,-z_f)\). The overall behavior of scattering loss is quite similar to that exhibited in Figure 3. The major difference observed is the increased loss caused by the additional one-way propagation path from the target back to the radar.

**Signal Decorrelation Distance**

As another aspect of the aperture averaging effect, an aperture can act to increase the measured decorrelation distance at the antenna output. This observed increase is caused by the averaging effect of the coherent integration that smooths the more rapid fluctuations. To obtain
Figure 4. Angular scatter loss for monostatic radar; a) versus relative antenna size; b) versus inclination angle.
the signal decorrelation distance for the one-way propagation path from $(0,0,-z_t)$ to $(0,0,z_r)$, it is necessary to perform the integration specified in Equation 47. Fortunately, $\Gamma$ given by Equation 45 is the product of simple Gaussian functions. The integral is available in standard tables and the resulting expression contains the factor $(-\zeta^2/\zeta_{ox}^2 - \eta^2/\zeta_{oy}^2)$ where the decorrelation distances in the $x$- and $y$-directions (see Figure A-1) are

$$\xi_{ox} = \xi_0 \left(1 + \frac{2\sigma_\theta^2}{\sigma_r^2} + \frac{2\sigma_\theta^2}{\sigma_t^2}\right)^{1/2}$$

(58)

$$\xi_{oy} = \frac{\xi_0}{\Delta} \left(1 + \frac{2\sigma_\theta^2}{\sigma_r^2} + \frac{2\sigma_\theta^2}{\sigma_t^2}\right)^{1/2}$$

(59)

If small apertures are used so that the beamwidths are large with respect to the theoretical angle-of-arrival standard deviations, the parenthetical expressions above are unity leaving $\xi_{ox}$ and $\xi_{oy}$ in agreement with the coefficients of $\xi_0$ and $\eta_0$ given in Equation 25 with $\omega_d$ set to zero.

Figures 5 and 6 show the relative signal decorrelation distances $\xi_{ox}/\xi_0$ and $\xi_{oy}/(\xi_0/\Delta)$ in the $x$- and $y$-directions for the case of identical transmit and receive antennas separated by a centrally located scattering layer. The quantities $\xi_0$ and $\xi_0/\Delta$ are the values of decorrelation distance in the $x$- and $y$-directions, respectively, that are observed with omnidirectional antennas. In the figures the results are again shown as a function of the ratio of antenna diameter to the decorrelation distance for propagation parallel to the magnetic field direction.
Figure 5. Relative signal decorrelation distance in the x-direction for one-way path with transmit and receive aperture antennas; a) versus relative antenna size; b) versus inclination angle.
Figure 6. Relative signal decorrelation distance in the y-direction for one-way path with transmit and receive aperture antennas; a) versus relative antenna size; b) versus inclination angle.
Figures 5(a-b) show the relative decorrelation distance in the x-direction as functions of \( D/D_p \) and inclination angle \( \psi \). Apertures with diameters less than the decorrelation distance do not affect measurements of the signal decorrelation distance. It is evident that apertures large with respect to \( D_p \) can greatly increase the measured decorrelation distance (relative to an omnidirectional antenna) for sufficiently strong angular scattering.

It is immediately evident that the decorrelation distance is not reciprocal. With omnidirectional antennas the decorrelation distances in the two orthogonal directions, \( l_{ox} \) and \( l_{oy} \), are dependent on the path geometry as given by Equation 26. These values are not reciprocal; \( l_{ox} \) and \( l_{oy} \) are measures of the average distance between fades in the receiver plane and consequently depend on geometry.

In the case of the monostatic radar, the signal decorrelation distances may be obtained directly from Equations 58 and 59 by using the parameters appropriate to only the second one-way propagation path with transmitter (target) at \((0,0,z_r)\). The results are

\[
l_{ox} = l_0' \left( 1 + \frac{2\sigma^2_{\alpha x}}{\sigma^2_{\alpha}} \right)^{1/2}
\]

\[
l_{oy} = l_0' \left( 1 + \frac{2\sigma^2_{\alpha y}}{\sigma^2_{\alpha}} \right)^{1/2}
\]

where \( l_0' \) and \( l_0'/\Delta \) are the signal decorrelation distances in the x- and y-directions that correspond to the one-way propagation path from a source in the \( z_r \) plane to a receiver in the \(-z_t \) plane. Figures 7-8 show \( l_{ox} \) and \( l_{oy} \) for a monostatic radar as a function of normalized antenna diameter and the angle between the magnetic field and the direction of propagation. The results are similar to those shown in Figures 5-6.
Figure 7. Relative signal decorrelation distance in the x-direction for monostatic radar; a) versus relative antenna size; b) versus inclination angle.
Figure 8. Relative signal decorrelation distance in the y-direction for monostatic radar; a) versus relative antenna size; b) versus inclination angle.
Mean Time Delay and Time Delay Jitter

In the same manner that an aperture antenna with a small beamwidth neglects or averages out energy incident at off-boresight angles to reduce the received power, it also acts to reduce the measured time delay and time delay jitter. This reduction occurs because the energy arriving from directions away from boresight typically travels over longer paths than the more direct signal. These longer paths require a longer propagation time for that portion of the received signal and hence contribute to increased \(<T>\) and \(\sigma_T\) values. If this energy is neglected by an aperture antenna, then the signal at the output will be characterized by smaller \(<T>\) and \(\sigma_T\) than that measured by an omnidirectional (point) antenna.

Now define the mean time delay, \(<T>\), as

\[
<T> = \frac{\int G(0,t)\tau dt}{\int G(0,t)dt}
\]  \(\text{(62)}\)

and define the time delay jitter, \(\sigma_T\), by the second moment

\[
\sigma_T^2 = \frac{\int G(0,t)\tau^2 dt}{\int G(0,t)dt} - <T>^2
\]  \(\text{(63)}\)

where \(G(0,t)\) is the power impulse response measured at the output of the receiving antenna due to an impulse of power originating from the transmitter.

To compute \(<T>\) and \(\sigma_T\) for the one-way propagation path with transmit and receive aperture antennas, it is convenient to utilize Equation 46 for the power impulse response function. The integrals of \(\tau\) and \(\tau^2\) give first and second derivatives of delta functions which yield first and second derivatives of \(r_{tr}(K,\omega_d)\). These derivatives are evaluated at zero \(\omega_d\) as a result of the \(t\) integration. The remaining integration with respect to \(K\) is easily performed. The results may be written as
\[<\tau> = \frac{1}{2\omega'} \left[ \left( 1 + \frac{2\sigma_y^2}{\theta_p^2} + \frac{2\sigma_x^2}{\theta_t^2} \right)^{-1} \right. \\
+ \Delta^2 \left( 1 + \frac{2\sigma_y^2}{\theta_p^2} + \frac{2\sigma_y^2}{\theta_t^2} \right)^{-1} \right]^{(64)} \\
\sigma^2 = \frac{\sigma_0^2}{\omega_0^2} + \frac{1}{2\omega'^2} \left[ \left( 1 + \frac{2\sigma_y^2}{\theta_p^2} + \frac{2\sigma_y^2}{\theta_t^2} \right)^{-2} \right. \\
\left. + \Delta^4 \left( 1 + \frac{2\sigma_y^2}{\theta_p^2} + \frac{2\sigma_y^2}{\theta_t^2} \right)^{-2} \right]^{(65)} \]

Figure 9 shows the effect of aperture antennas on the observed mean time delay by showing the mean time delay normalized by the value observed with omnidirectional antennas, \((1+\Delta^2)/(2\omega')\). In the figure, transmit and receive apertures are identical and the equivalent phase-screen is assumed to be located midway between the antennas. Figure 9(a) shows the relative mean time delay as a function of \(D/\ell_p\) for values of the inclination angle of 0°, 15°, 30°, 45° and 90°. It is seen that large apertures can have a significant effect in reducing the observed mean time delay, particularly when the direction of propagation is close to the magnetic field direction. In Figure 9(b) the abscissa and the parametric quantity are interchanged relative to Figure 9(a).

Figures 10(a-b) show the effect of aperture antennas on the observed time delay jitter \(\sigma_\tau\). Here \(\sigma_\tau\) is normalized to its value for omnidirectional transmit and receive antennas \([(1+\Delta^4)/(2\omega'^2)]^{1/2}\). It is further assumed that the ratio \(\sigma_\phi/\omega_0\) is small, as is always the case for GHz and higher frequencies. At \(\psi = 0^\circ\) the antenna aperture has identical effects on \(\sigma_\tau\) and \(<\tau>\). At other values of the inclination...
Figure 9: Relative mean time delay for one-way path with transmit and receive aperture antennas; a) versus relative antenna size; b) versus inclination angle.
Figure 10. Relative time delay jitter for one-way path with transmit and receive aperture antennas; (a) versus relative antenna size; (b) versus inclination angle.
angle $\psi$, the results shown in Figure 10 are similar but not identical to those shown in Figure 9. The decreased measurements of $<\tau>$ and $\sigma_\tau$ are the result of the action of the antenna to exclude signal energy incident from off-axis directions that arrives later than energy that propagates over the direct path.

For the general case that the power impulse response function is given as the convolution of two other functions as by Equation 52, it is easy to perform the required $\tau$ integrations to obtain

\[
<T_m> = <T_1> + <T_2>.
\]

\[
\sigma_{\tau m}^2 = \sigma_{\tau 1}^2 + \sigma_{\tau 2}^2
\]

These results state that the mean time delay and time delay variance are the sums of the values obtained over each of the two one-way propagation paths. The required one-way values may be obtained from Equations 64-65 with attention to the direction of propagation and antenna placement. The final results are

\[
<T> = \frac{1}{\omega} \left[ \left( 1 + \frac{2\sigma_x^2}{\theta_x'} \right) + \Delta^2 \left( 1 + \frac{2\sigma_y^2}{\theta_y'} \right) \right]^{-1}
\]

\[
\sigma^2 = \frac{2\sigma_x^2}{\omega} + \frac{1}{\omega^2} \left[ \left( 1 + \frac{2\sigma_x^2}{\theta_x'} \right)^{-2} + \Delta^2 \left( 1 + \frac{2\sigma_y^2}{\theta_y'} \right)^{-2} \right]
\]
Figures 11-12 show the values of mean time delay and time delay jitter for an aperture antenna normalized to their values for an omni-directional antenna. Again the factor $\frac{c}{\omega_0}$ is assumed small for this monostatic radar case. These normalized results are very similar in form to those presented in Figures 9-10 and again show the dramatic effect of a large aperture antenna that operates in strong scattering conditions.

**Coherence Bandwidth**

The coherence bandwidth is appropriately chosen as the inverse of the time delay jitter exhibited by the received waveform due to a transmitted power that is a delta function in delay (Knepp, 1983(b)). In the cases considered here where $\frac{\sigma_\phi}{\omega_0}$ is small, the effects of antenna apertures on the measured coherence bandwidth are easily obtained from Equations 65 and 69. The results for the one-way propagation path with transmit and receive antennas and for the monostatic radar case are given as the reciprocal of the values shown in Figures 10 and 12, respectively.
Figure 11. Relative mean time delay for monostatic radar; a) versus relative antenna size; b) versus inclination angle.
Figure 12. Relative time delay jitter for monostatic radar; a) versus relative antenna size; b) versus inclination angle.
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IONIZATION IRREGULARITY DESCRIPTION

The ionization irregularities are assumed to be elongated along the direction of the earth's magnetic field as shown in Figure A-1. The electromagnetic wave propagates in the negative z direction. The magnetic field vector lies in the y-z plane at an angle of \( \psi \) with respect to the z axis. The ionization irregularities are assumed rotationally symmetric with autocorrelation function

\[
B_\xi(r,s) = \frac{\sigma_N^2 e}{\langle N_e \rangle^2} \exp \left\{- \frac{r^2}{r_0^2} - \frac{s^2}{(qr_0)^2} \right\}
\]

(A-1)

Figure A-1. A single irregularity elongated along the magnetic field line in the y-z plane.
where $s$ is measured along the magnetic field direction and $r$ is measured perpendicular to this direction. The quantity $q$ is known as the axial ratio (Briggs and Parkin, 1963) and $r_0$ is the correlation distance or irregularity scale size.

The $s$, $r$ coordinate system may be related to the $x$, $y$, $z$ system by the equations $s^2 = (y \sin \psi + z \cos \psi)^2$ and $r^2 = x^2 + (y \cos \psi - z \sin \psi)^2$. Using the above transformation the irregularity correlation function may be expressed in the $x$, $y$, $z$. This expression can easily be integrated according to Equation 6 to obtain the function $A(\zeta, \eta)$ as

$$A(\zeta, \eta) = \frac{\sigma_N^2 \sqrt{\pi} q r_0}{\langle N \rangle \times \left( \frac{2}{\pi} q^2 \sin^2 \psi \cos^2 \psi \right)^{1/2}} \times \exp \left\{ - \frac{r^2}{r_0^2} - \frac{\eta^2}{r_0^2 (q^2 \sin^2 \psi \cos^2 \psi)} \right\}$$

(A-2)

The above equation is essentially Equation 10 in Briggs and Parkin (1963). $A(\zeta, \eta)$ is easily expanded in a Taylor series and, retaining only terms up to the quadratic, one obtains Equation 10 in the text where

$$A_0 = \frac{\sigma_N^2 \sqrt{\pi} q r_0 \Delta}{\langle N \rangle \times \left( \frac{2}{\pi} q^2 \sin^2 \psi \cos^2 \psi \right)}$$

(A-3)

$$- \frac{\sigma_N^2 \sqrt{\pi} q \Delta}{\langle N \rangle \times \left( \frac{2}{\pi} q^2 \sin^2 \psi \cos^2 \psi \right)}$$

(A-4)
This same formalism may also be applied to irregularity power spectra that are non-Gaussian. For the case of a power-law PSD the coefficients $A_0$ and $A_2$ are different than above but behave in essentially the same manner as a function of the outer scale size as long as the three-dimensional in-situ electron density PSD falls off at least as rapidly as $k^{-4}$.

Phase Standard Deviation

For an ionized medium, the phase standard deviation is given as the integral of the irregularity autocorrelation function along the direction of propagation (Salpeter, 1967). The result may be written as (Knepp, 1983(b))

$$\sigma_\phi^2 = \frac{1}{4} k_0^4 L A_o / k_0^2$$

or

$$\sigma_\phi^2 = \sqrt{\pi} (\lambda r_e)^2 q A_o L n_e^2$$

Theoretical Angle-Of-Arrival Fluctuation

Consider a plane wave traveling in the negative $z$-direction and incident in the $x$-$y$ plane at an angle $\theta$ from the $z$-axis. The electric field is given by $E(x,y) = E_0 \exp \{i[k(\sin \theta x + \cos \theta z)] \}$ where the $\exp(i\omega t)$ time dependence is suppressed. The angle-of-arrival measured along the $x$-axis is computed as
\[
\theta_x = \frac{1}{ikE_0} \frac{\partial E(x,z)}{\partial x} \tag{A-7}
\]

This computation gives \(\sin \theta\) which, in the small angle limit, is approximately \(\theta\).

In the case of interest here the incident field is given as the solution to the parabolic wave equation and the angle-of-arrival may be measured in the \(x\)-direction as

\[
\theta_x = \frac{1}{ikU_0} \frac{\partial U(p,z,\omega)}{\partial x} \tag{A-8}
\]

with a similar expression for \(\theta_y\). Here the measurement depends on the frequency. At a single frequency the rms value of \(\theta_x\) is related to the second derivative of the two-position MCF (Papoulis, 1965, p. 317)

\[
\sigma_{\theta_x}^2 = \frac{1}{k^2} \left. \frac{\partial^2 \Gamma(z,\eta,\omega_d=0)}{\partial \zeta^2} \right|_{\zeta=\eta=0} \tag{A-9}
\]

With a similar equation for \(\sigma_{\theta_y}\). For the case of propagation from a transmitter in the \(-zt\) plane to a receiver in the \(zt\) plane, \(\sigma_{\theta_x}\) and \(\sigma_{\theta_y}\) may be obtained from derivatives of Equation 25 in the text as \(\sigma_{\theta_x} = \sqrt{\pi}/(k\delta_s)\) and \(\sigma_{\theta_y} = \sqrt{\pi}/[k(\delta_s/\Delta)]\).

For the case of propagation from a transmitter in the \(zt\) plane to a receiver in the \(-zt\) plane, the interchange of transmitter and receiver may be taken into account by substituting \(t'\) for \(t\) where \(t' = z_t t_0/z_r\). This substitution gives the angle-of-arrival fluctuation over the reversed path as \(\sigma_{\theta_x'} = \sqrt{\pi}/(k t'_0)\) and \(\sigma_{\theta_y'} = \sqrt{\pi}/[k(t'_0/\Delta)]\).
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