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EVANSTON IL DEPT OF CIVIL ENGINEERING J D ACHENBACH
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| 20. ABSTRACT (Continue on reverse side if necessary and identify by block number) | A summary and a bibliography are presented of the investigations on dynamic effects on fracture in elastic and elastic-plastic materials which were carried out at Northwestern University under the sponsorship of the Air Force Office of Scientific Research during the period July 1, 1978 - September 30, 1983. Two main areas are investigated: high rate loads on bodies containing cracks, and fast fracture and crack arrest. Inertial and crack tip plasticity... (over)
effects are investigated for a stationary crack under rapid loading. Dynamic
analysis of fast fracture and crack arrest using a Dugdale model is formulated
and numerically solved. Elastodynamic stress intensity factors are investigated
for various subsurface crack geometries, including Mode III analytical solutions
and approximate mixed Mode I-II solutions. Elastic-viscoelastic fast fracture
and crack arrest are studied using Bodner-Partom constitutive modeling. Crack
kinking under stress wave loading is analyzed rigorously for Mode III, and
mixed Mode I-II is approximated.
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DYNAMIC EFFECTS ON FRACTURE

FINAL REPORT

by

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1. Research Objectives

The research work on this project has been concerned with dynamic effects on fracture. Two main areas have been investigated: "high-rate loads on bodies containing cracks," and "fast fracture and crack arrest."

Dynamic effects become important if the external loads give rise to propagating mechanical disturbances (as for impact loads and explosive charges) which can strike a crack and cause crack propagation. Spalling is an example of a fracture phenomenon caused by the rapid application of loads. Dynamic effects become also important if a crack propagates very rapidly, so that rapid motions are generated in the solid. Even though in most cases fracture studies should focus on the prevention of crack propagation, cracks sometimes become unstable despite the best attempts for prevention. Both for brittle and ductile materials, it is then important to know whether high speeds of crack propagation can be expected, what the dynamic interaction with the geometry of the body will be, and most importantly how a rapidly propagating crack can be arrested.

A summary of the research objectives of the completed project is

DYNAMIC EFFECTS ON FRACTURE

I. HIGH-RATE LOADS ON BODIES CONTAINING CRACKS.
   I-A: Computation of elastodynamic stress intensity factors.
   I-B: Influence of plastic yielding on the dynamic stress field near a crack tip.
   I-C: Conditions for crack propagation under dynamic loading conditions.

II. FAST FRACTURE AND CRACK ARREST.
   II-A: Computation of elastodynamic stress intensity factors for rapidly propagating cracks.
   II-B: Analysis of plastic deformations near a rapidly propagating crack tip.
   II-C: Application of fracture criteria to compute crack-tip speeds.
   II-D: Arrest of rapidly propagating cracks.
   II-E: Crack forking and kinking of rapidly propagating cracks.
The work has evolved through four stages which were stated in the original proposal. These stages are

**Stage 1:** Development of analytical and numerical methods to analyze dynamic effects on crack-tip fields.

**Stage 2:** Comparison of crack-tip fields for linear elasticity and various constitutive models of elasto-plastic and visco-plastic material behavior.

**Stage 3:** Comparison of various fracture criteria.

**Stage 4:** Application of fracture criteria and the formulation of conditions for initiation of crack propagation, continued crack propagation and crack arrest, as well as for crack kinking and crack forking under dynamic conditions.

From the point of view of the Air Force, the technological significance and relevance of the completed research derives from the fact that it is at the present time either technically or economically not feasible to manufacture so that cracks never occur in factory-new structures, or after a period of service. It is, therefore, necessary to be able to estimate the stability of flaws, the propagating characteristics for fast fracture and the arrest mechanisms for rapidly propagating cracks, under a variety of loading conditions which should include conditions generated by impact loads and explosive charges.

2. **Summary of Completed Research**

The research completed on this Project has been reported in a number of papers, which have been (or will be) published in Technical
The research results are briefly summarized as follows.

2.1 Effects of Plasticity on Near-Tip Fields

Under rapid loading conditions the mass density of a material affects the fields of stress and deformation near a crack tip. For such dynamic problems plastic deformation in the immediate vicinity of a crack tip was investigated in [1]* for a stationary crack. Deformation theory was employed for the first phase of the loading when the fields are increasing monotonically with time. The general character of the near-tip fields was analyzed both with respect to its variation with time and with polar angle. The non-linear near-tip fields were related to the linearly elastic far-field by means of a path-independent integral.

In [2], deformation theory was applied to a thin plate containing a through-crack. The in-plane normal stresses were assumed to be tensile, but with a non-uniform variation through the thickness of the plate, as a result of bending and a dominant extension. The nonlinear near-tip fields (which are singular) have been analyzed asymptotically on the basis of plate theory. It was found that the angular variations of the near-tip fields are just the same as for generalized plane stress. Assuming small-scale yielding a path-independent integral, which is valid in a region close to the crack edge, was used to connect the nonlinear near-tip fields with the corresponding singular parts of the linear fields. It was shown that the nonlinear behavior near the crack edge significantly affects the through-the-thickness variations of the near-tip fields. The singular parts of the in-plane stresses tend to become more uniform through the thickness of the plate with stronger strain hardening.

*Numbers in brackets refer to the list of publications in Appendix A.
For dynamic fracture problems plastic deformation in the immediate vicinity of a crack-tip was investigated in [3]. Both stationary and propagating crack tips were considered. For a stationary crack tip, deformation theory was employed for the first phase of the loading when the fields are increasing monotonically with time. The general character of the near-tip fields was analyzed both with respect to its variation with time and with polar angle. The non-linear near-tip fields were related to the linearly elastic far-field by means of a path-independent integral. In the second part of the paper we considered rapidly propagating cracks. The near-tip fields for various models of material behavior were discussed. In particular, some earlier work by Achenbach and Kanninen for a rapidly propagating Mode-III crack, in a material which displays strain hardening was reviewed. In the last part of the paper the fields near a rapidly propagating crack-tip in an elastic perfectly-plastic material was considered for the case that inertia terms are of importance. The system of governing equations in the plastic region was presented and shown to be hyperbolic in nature. As a first approximation the steady-state case with respect to the moving crack-tip was considered and an asymptotic analysis of the near-tip field was carried out.

A dynamic analysis of fast fracture and crack arrest based on the Dugdale model was presented in [7]. Numerical approaches by the finite difference method have been considered in [13] and [18].

2.2 Computation of Elastodynamic Stress-Intensity Factors

The effect of proximity of a boundary on elastodynamic stress intensity factors has been investigated in [4] for a surface-breaking crack, and in [14] for a subsurface crack parallel to the surface of a half-space. In recent work we have also considered a subsurface crack which is oriented under an arbitrary angle with the surface of a half-space, see [16].
The configurations that have been considered, are two dimensional with deformations in plane strain. Systems of coupled singular integral equations for the Mode-I and Mode-II dislocation densities have been derived. These equations have been solved numerically for the cases of time-harmonic uniform tension and uniform shear applied at the surface of the half-space. The ratios of elastodynamic to elastostatic stress intensity factors have been computed. The results display the dependence on the frequency and on the ratio $d/a$, where $d$ is the distance from the upper crack tip to the free surface and $a$ is the crack length. For small angles of inclination with the free surface, and for small values of $d/a$, time-harmonic excitations of the body may induce quite strong resonance vibrations of the layer between the crack and the free surface. Such resonance vibrations give rise to substantial increases in both the Mode-I and Mode-II stress intensity factors. These resonance effects were investigated in some detail for the parallel crack in [14].

A three-dimensional stress analysis problem for a surface-breaking crack was considered in [17]. A half-space containing a surface-breaking crack of uniform depth, oriented normal to the surface, was subjected to three-dimensional dynamic loading. The elastodynamic stress analysis problem was decomposed into two problems which are symmetric and antisymmetric, respectively, relative to the plane of the crack. The formulation of these problems was subsequently reduced to singular integral equations for the corresponding dislocation densities, namely, a single integral equation for the symmetric problem and a set of coupled integral equations for the antisymmetric problem. The systems of integral equations were solved numerically. The dislocation densities directly yield the stress-intensity factors. As an example an applied stress field with harmonic variation along the crack length and exponential decay with crack depth was considered. The dependence of the stress intensity factors on the frequency and on the wavelength in the crack direction has been displayed by numerical results.
2.3 **Fast Fracture and Crack Arrest in an Elastic-Viscoplastic Material.**

In this work, we have investigated both the effects of plastic deformation near a propagating crack tip and dynamic effects due to high crack-tip speeds. The constitutive equations that have been employed define an elastic viscoplastic material. The constitutive model, which was proposed by Bodner and Partom does not require the statement of a separate yield criterion, nor is it necessary to consider loading and unloading separately. Plastic deformations always exist, but they are negligibly small when the material behavior should be essentially elastic.

The geometry that has been considered is a two-dimensional one of a thick strip which contains a rapidly propagating semi-infinite crack in its center-plane. The faces of the strip were subjected to uniform in-plane displacements, so that the crack propagates in Mode-I. A steady-state situation relative to the moving crack tip has been assumed. The plastic deformations near the crack tip, the residual plastic strains in the wake of the crack tip and other field variables have been obtained directly from the complete solution without the assumption of small scale yielding.

Detailed results have been given in [5], [6] and [11]. The method of solution is numerical and involves an iterative procedure which is continued until a steady state solution is reached, in which the equation of motion, the flow rules and the boundary conditions are satisfied simultaneously. The method is based on a finite difference procedure which is unconditionally stable and has a second order accuracy.

In the special case of a perfectly elastic strip the problem possesses an analytical solution which has been employed to check the accuracy of the numerical method, and excellent agreement has been obtained.

Typical effects due to viscoplastic constitutive behavior have been studied by comparisons with the corresponding elastic fields. The effects of high crack-tip speeds, which are directly related to the strain-rate
dependence of the material, have been studied by comparisons of solutions for three crack-tip velocities. The influence of the inertia term in the governing equations has been studied by comparisons with the corresponding quasi-static solutions. In particular, the dependence on the crack-tip speed of the plastic zone in the vicinity of the crack tip, the level of plastic straining, the amount of dissipative plastic work and the crack-opening displacements have been examined.

In [9] and [12] the transient problem of deceleration and arrest of a rapidly propagating crack tip has been investigated for a crack which initially propagates in an elastic solid but then enters a region of viscoplastic material properties. Of particular interest in the dynamic arrest problem is the plastic strain just ahead of the arresting crack tip. This strain has been computed as a function of time. Within the context of a critical strain criterion it has been assumed that the crack tip will arrest if this strain does not exceed a certain critical value.

2.4 Crack-Kinking under Stress-Wave Loading

When a stress pulse strikes a crack, the crack may be induced to propagate, but not necessarily in it's own plane. In earlier work, it has been attempted to explain kinking of a crack at finite kinking angles. In work completed on this project, [10] and [15], we have reconsidered the two-dimensional configuration of an initially stationary crack which kinks under an angle $\kappa_7$ with it's original plane. We have discussed earlier results for Mode III, and we have proposed a way to approximate the elastodynamic stress intensity factors for the Mixed Mode I-II case.

The tip of the kinked crack is assumed to propagate at a constant velocity $c_F$, and kinking is initiated at an angle $\kappa_7$ at the instant that an incident disturbance first strikes the original crack tip. These two assumptions render the solution self-similar. Three cases have been considered corresponding to incidence of either an anti-plane transverse wave, an in-plane transverse wave or a longitudinal wave.
The elastodynamic stress intensity factors have been computed as functions of the crack tip speed, $c_F$, the kinking angle, $\kappa\pi$, and the angle of wave incidence $\alpha\pi$. For a given angle of incidence, the elastodynamic stress intensity factors have been used to compute the corresponding energy fluxes into the propagating crack tip.

Mode-III problems of the kind formulated in [10] can be solved rigorously. Results for Mode-III kinking under an arbitrary angle were given earlier. The corresponding mixed Mode I-II problems have, however, as yet eluded a rigorous analytical solution.

For the mixed Mode I-II problems we have proposed a simple approximation to the solution of the superposition problem. The approximation is based on an observation from the exact Mode-III solution of the analogous superposition problem, that for an important range of kinking angles the elastodynamic stress intensity factor of the kinked crack is affected more by the dependence on $\kappa$ of the loading on the new crack faces than by the wedge geometry at the original crack tip. This observation then suggests that in first approximation we may ignore the wedge geometry altogether, and we may compute elastodynamic stress intensity factors by considering a crack propagating in its own plane but where the new crack faces are subjected to tractions corresponding to the kinking crack.

For the Mode-III case the approximation of the elastodynamic stress intensity factor for the kinked crack can be checked by comparisons with exact results. The range of kinking angles $\kappa\pi$ for which the approximation gives good results turns out to be surprisingly large. For the mixed Mode I-II case comparisons with the numerical results have been carried out, and satisfactory agreement has been obtained. No rigorous mathematical proof of the approximation's validity is given in this paper. It is, however, to be
expected that the results correspond to the first order terms in a perturbation procedure for small kinking angle.

The results of this work suggested that the approximation could be used to analyze crack kinking at gradually increasing angles and at time-varying crack tip speeds. The details of that analysis have been completed [19]. Publication [19] also includes a study of the actual conditions for crack kinking by the use of the criterion of the balance of rates of energies.

3. **Interactions**

Lectures and presentations on research carried out on this Project have been listed in Appendix B.

4. **Professional Personnel**

J. D. Achenbach - Principal Investigator

Contributing to the research efforts for various periods of time:

- J. Aboudi - Visiting Scholar
- J. Dempsey - Post-Doctoral Research Associate
- P. Burgers - Post-Doctoral Research Associate
- Y.C. Angel - Post-Doctoral Research Associate
- L.M. Keer - Cooperating Faculty
- T. Bubenik - Research Assistant
- D. Mendelsohn - Research Assistant
- V. Dunayevsky - Research Assistant
- H.K. Chung - Research Assistant
- M.K. Kuo - Research Assistant
- W. Lin - Research Assistant
5. Graduate Degrees

T. Bubenik: Ph.D. Theoretical and Applied Mechanics, 1979
now at Exxon Production Res. Co., Houston, TX

now at Ohio State University

now at Standard Oil Company Research Center,
Cleveland, Ohio

H.K. Chung: Ph.D. Civil Engineering, 1982
now at National Central University, Chungli, Taiwan
Appendix A: Publications


Appendix B: Lectures and Presentations


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