DETERMINATION OF THEORETICAL SAMPLING EFFICIENCIES FOR ASPIRATED PARTICULATE MATTER THROUGH THE DRES LARGE-VOLUME SAMPLER (U)

by

Irene Miskew and Stanley B. Mellsen

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NOTATION

C particle concentration in the sample, g cm\(^{-3}\)

C\(_D\) particle concentration in the free stream, g cm\(^{-3}\)

d particle diameter, cm

D distance from the inlet to the outlet cross section of the collection tube, cm

h thickness of the collection tube wall at the outlet cross section, cm

L length of coaxial boundary tube, cm

r radial co-ordinate of particle position, cm

r\(_A\) radius of coaxial boundary tube, cm

r\(_B\) radius of collection tube at exit, cm

r\(_C\) inlet radius of cone, cm

r\(_p,\infty\) radial co-ordinate of particle position far upstream, cm

r\(_s,\infty\) far upstream radius of the stream tube that impinges on the collection tube circumference, cm

t time, seconds

u\(_r\) radial component of local fluid velocity, cm sec\(^{-1}\)

u\(_z\) axial component of local fluid velocity, cm sec\(^{-1}\)

U fluid velocity in collection tube, cm sec\(^{-1}\)

U\(_A\) fluid velocity at boundary tube entrance, cm sec\(^{-1}\)

U\(_B\) fluid velocity at collection tube exit, cm sec\(^{-1}\)

U\(_C\) fluid velocity at boundary tube exit, cm sec\(^{-1}\)

U\(_i\) fluid velocity at inlet of sampler, cm sec\(^{-1}\)

v\(_r\) radial component of local particle velocity, cm sec\(^{-1}\)

v\(_z\) axial component of local particle velocity, cm sec\(^{-1}\)

z axial co-ordinate (origin at collection tube inlet) of particle position, cm
The following are dimensionless:

- \( C_D \): drag coefficient for spheres
- \( G(1), G(2), G(3), G(4) \): dependent variables solved for by numerical integration, they represent \( v_x, v_y, z \) and \( r \) respectively
- \( E_m \): collection efficiency of sampling tube
- \( H \): thickness of collection tube wall, \( h/r_A \)
- \( i, j \): grid point co-ordinates in the radial and axial directions respectively
- \( i_B, j_B \): grid point co-ordinates of the edge of the collection tube inlet
- \( j_0 \): axial grid point co-ordinate of a particle at the far upstream position
- \( K \): inertia parameter of particle
- \( \bar{r} \): radial co-ordinate of particle, \( r/r_c \)
- \( \bar{r}_{p, u} \): radial co-ordinate of particle position far upstream, \( r_{p, u}/r_c \)
- \( \bar{r}_{s, u} \): far upstream radius of the stream tube that impinges on the collection tube circumference, \( r_{s, u}/r_c \)
- \( R \): radial co-ordinate used in calculating the stream function field, \( r/r_A \)
- \( Re \): spherical particle Reynolds number in flow in the proximity of the collection tube
### NOTATION (Cont'd)

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tr>
<td>$Re_0$</td>
<td>spherical particle Reynolds number in free stream</td>
</tr>
<tr>
<td>$u_r$</td>
<td>radial component of local fluid velocity, $du/dr$</td>
</tr>
<tr>
<td>$\bar{u}_z$</td>
<td>axial component of local fluid velocity, $du/d\bar{z}$</td>
</tr>
<tr>
<td>$v_r$</td>
<td>radial component of local particle velocity, $d\bar{r}/dt$</td>
</tr>
<tr>
<td>$\bar{v}_z$</td>
<td>axial component of local particle velocity, $d\bar{z}/dt$</td>
</tr>
<tr>
<td>$\bar{z}$</td>
<td>axial co-ordinate (origin at collection tube inlet) of particle, $z/r_c$</td>
</tr>
<tr>
<td>$\bar{z}_0$</td>
<td>axial co-ordinate of particle far upstream, $z_0/r_c$</td>
</tr>
<tr>
<td>$Z$</td>
<td>axial co-ordinate used in calculation of the stream function field, $z/r_A$</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>ratio of collection tube radius to boundary tube radius, $r_B/r_A$</td>
</tr>
<tr>
<td>$\beta$</td>
<td>length of coaxial boundary tube, $L/r_A$</td>
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<tr>
<td>$\gamma$</td>
<td>distance from the inlet to the outlet cross section of the collection tube, $D/r_A$</td>
</tr>
<tr>
<td>$\delta$</td>
<td>distance from inlet of boundary to inlet of collection tube, $\beta - \gamma$</td>
</tr>
<tr>
<td>$\tau$</td>
<td>time, $tU_A/r_c$</td>
</tr>
<tr>
<td>$\phi$</td>
<td>dimensionless group independent of particle position, $Re_0^2/K$</td>
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<tr>
<td>$\psi$</td>
<td>stream function, $\psi/\lambda U_A r_A^2$</td>
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ABSTRACT

Sampling and collection efficiencies are calculated for a large-volume air sampler under conditions of anisokinetic as well as isokinetic flow. A mathematical model developed to evaluate a tapered-tube sampling probe was modified to obtain results for the large-volume sampler, using various particle sizes and flow velocities. These results should facilitate the prediction or correction of sampling errors in field and laboratory experiments.
1. **INTRODUCTION**

In order to assess the effectiveness of a specific large-volume air sampler (cyclone scrubber), the instrument's ability to collect samples of finely-divided particulate matter must be determined. These samples can come from still or moving airstreams, and can vary both in particle size distribution and in concentration. The bio-sampler under evaluation consists of an air inlet cone and collection unit, and is designed to operate at a capacity of 1000 litres (air) per minute. (It is described fully in Suffield Technical Note No. 311).

Sampling from streams of suspended particulates is representative only if the size distribution and content of particles in the sample are identical to those of particles in ambient air at the point of sampling. The sampling system may give rise to three different types of error (Vitols, 1964) due to:

1. particles failing to enter the sampling cone in representative concentrations;
(2) particles being deposited between the air inlet cone and the collection location; and
(3) particles being shattered, aggregated or incompletely retained by collection devices.

When the velocity of gas entering the inlet cone is exactly the same as the far-upstream velocity of the gas ('isokinetic' sampling), particles will enter the sampler in representative concentrations. Otherwise, errors of the first type will occur as the result of anisokinetic sampling.

The purpose of this report is to describe the modification of a mathematical model devised formerly for calculating the error due to anisokineticity (Mellsen, 1979) of a sampling probe developed and used at DRES. The model, previously applied to a straight, tapered tube is herein adapted to the funnel-shaped inlet cone of a specific large-volume air sampler, and as such, calculates the sampling and collection efficiencies produced by varying upstream gas velocity and particle size.

2. DEFINITION OF THE PROBLEM

As explained in Suffield Technical Paper No. 499 (Mellsen, 1979), the problem of finding the sampling and collection efficiencies is one of determining the values of the upstream particle and fluid radii. The upstream particle radius, \( r_{p,m} \), is defined as the radius of the limiting particle trajectory envelope which encompasses all particles (of any given diameter) entering the sampler. The upstream fluid radius, \( r_{s,m} \), is the radius of the stream tube impinging on the outer circumference of the inlet cone, and containing the total volume of air passing through the sampler. The sampling efficiency, proportional to the areas of upstream particle envelope and fluid stream tube, can then be calculated:

\[
\frac{C}{C_0} = \frac{\left(r_{p,m}\right)^2}{\left(r_{s,m}\right)^2} \tag{Eq. 1}
\]

where \( C_0 \) is the upstream particle concentration and \( C \) is the particle concentration in the sample; the collection efficiency is given by:

\[
E_m = \frac{\left(r_{p,m}\right)^2}{r_c^2} \tag{Eq. 2}
\]
where \( r_c \) is the radius at the inlet of the cone.

Inertial and drag forces may cause particles flowing far upstream of the collection inlet to deviate from stream lines on arriving at the cone, where the fluid velocity may be changing markedly. Thus, in obtaining the true free stream concentration of particles and the sampling efficiency, the two different values of upstream particle radius and upstream fluid radius must be known. When the free stream velocity, \( U_A \), is less than the sampler inlet velocity, \( U_i \) (i.e. \( \frac{U_A}{U_i} < 1 \)), some particles originally inside the limiting stream tube will pass outside the sampler, whereas for \( \frac{U_A}{U_i} > 1 \), some particles originally outside the stream tube will be drawn into the sampler.

3. DESCRIPTION OF THE SAMPLER

The part of the large-volume air sampler which determines stream function values and hence, affects sampling and collection, is the air inlet cone (Figure 1). With an inlet radius of 2 1/2 inches, the cone converges to a straight tube of inside radius 3/8 inch, through a funnel shaped by the intersection of three circular arcs. The entire inlet cone is 6 inches long, the converging section being 4 inches and the straight tube, therefore, 2 inches. The wall of the cone is 1/16 inch thick, but although this was taken into account in the calculation of the velocity \( U_c \), the wall thickness was neglected in the computations leading to the array of stream function values. Since a grid unit in the array represents 1/8 inch, the cone wall thickness of 1/16 inch would have little effect on stream function values, but would make computing procedures unnecessarily complicated.

The three circular arcs defining the shape of the inlet cone are (numbers in inches):

\[
(X_1 - 2 \ 5/16)^2 + (Y_1 - 3 \ 5/8)^2 = (24)^2 \quad \text{at inlet} \quad \text{(Eq. 3)}
\]
\[
(X_2 - 4 \ 3/8)^2 + (Y_2 - 6 \ 15/32)^2 = (6)^2 \quad \text{in middle} \quad \text{(Eq. 4)}
\]
Newton's Method was used to determine the two intersection points (between Equations 3 and 4, and Equations 4 and 5), with initial values for the iterative technique found by inspection of a drawing of the curve.

4. EQUATIONS OF MOTION

The equations of motion were established in a previous report (Mellsen, 1979), but are included here for completeness.

The motion of an individual particle has been shown (Vitois, 1964 and Batchelor, 1956) to be determined by the following ordinary differential equations:

\[
d\frac{\nu_r}{dt} = \frac{C_D \text{Re}(\overline{u_r} - \overline{v_r})}{24 \text{K}} \quad \text{(Eq. 6)}
\]

\[
d\frac{\nu_z}{dt} = \frac{C_D \text{Re}(\overline{u_z} - \overline{v_z})}{24 \text{K}} \quad \text{(Eq. 7)}
\]

where \( \text{Re} = \text{Re}_0 \left[ (\overline{u_r} - \overline{v_r})^2 + (\overline{u_z} - \overline{v_z})^2 \right]^{1/2} \quad \text{(Eq. 8)} \)

\[
K = \frac{\nu \ \text{d}^2 U_A}{18 \pi r_c} \quad \text{particle inertia parameter} \quad \text{(Eq. 9)}
\]

\[
\text{Re}_0 = \frac{U_A d_p}{\nu} \quad \text{free stream Reynolds number} \quad \text{(Eq. 10)}
\]

The symbols are defined in the notation section near the front of this report and the basic geometry of the flow system is illustrated in Figure 2.

Several assumptions are inherent in the use of Eqs. 6 and 7 for calculating the collection and sampling efficiencies due to a stream of particles, including:

(a) uniform particle distribution;

(b) no gravitational or electrostatic forces of consequence;

(c) monodisperse spherical particles with diameter very small
in relation to the inlet diameter of the sampler; and

d) free stream flow that is steady, incompressible and irrotational.

The drag coefficient is a function of Reynolds number and is available in the form of definitive empirical equations (Davies, 1945). These equations are stated as follows:

\[
\text{Re} = \frac{C_D \text{Re}^2}{24} - 2.3363 \times 10^{-4} (C_D \text{Re}^2)^2 + 2.0154 \times 10^{-6} (C_D \text{Re}^2)^3 - 6.9105 \times 10^{-9} (C_D \text{Re}^2)^4 \tag{Eq. 11}
\]

for \( \text{Re} < 4 \) or \( C_D \text{Re}^2 < 140 \)

\[
\log_{10} \text{Re} = -1.29536 + 9.86 \times 10^{-1} (\log_{10} C_D \text{Re}^2) - 4.6677 \times 10^{-2} \]

\[
(\log_{10} C_D \text{Re}^2)^2 + 1.1235 \times 10^{-3} (\log_{10} C_D \text{Re}^2)^3 \tag{Eq. 12}
\]

for \( 3 < \text{Re} < 10^4 \) or \( C_D \text{Re}^2 < 4.5 \times 10^7 \)

5. AIR FLOW FIELD EQUATIONS

These equations were stated and explained in an earlier report (Mellsen, 1979), but are again shown for the sake of thoroughness.

The equations of fluid velocity were derived from the stream function for ideal flow over and through the sampler. To solve the problem, an outer boundary was used around the collection cone in the form of a coaxial tube of radius \( r_A \) (Figure 3), which was chosen large enough so that the effect of the boundary tube on flow in the proximity of the sampler is negligible. The collection cone was inserted a distance \( D \) into the downstream end of the boundary tube. Since the flow is axisymmetric only a radial plane containing both tubes had to be considered.

The fluid enters the boundary tube with steady velocity \( U_A \), and separates into a central stream with velocity \( U_b \) at the exit and \( U_i \) at the entrance of the sampler, and an annular stream, with velocity \( U_c \),
at the downstream end of the boundary tube. The axial velocities \( U_A \), \( U_B \), \( U_C \) and \( U_i \) are uniform. Also, there is no radial flow at the end cross sections.

The boundary conditions on the flow can now be completely specified so that the flow field can be obtained by solution of the equation of the stream function.

The axially symmetric stream function \( \psi(r,a) \) (Batchelor, 1967) satisfies:

\[
\frac{\partial^2 \psi}{\partial r^2} + \frac{1}{r} \frac{\partial \psi}{\partial r} + \frac{\partial^2 \psi}{\partial z^2} = 0 \tag{Eq. 13}
\]

The two velocity components (Figure 2) are given by:

\[
u_z = \frac{1}{r} \frac{\partial \psi}{\partial r} \tag{Eq. 14}
\]

\[
u_r = -\frac{1}{r} \frac{\partial \psi}{\partial z} \tag{Eq. 15}
\]

When \( U_A \) and \( U_B \) are specified, continuity gives \( U_C \) as follows:

\[
U_C = \frac{U_A - \alpha^2 U_B}{1 - \left[ \frac{r_B + h}{r_B} \right]^2} \tag{Eq. 16}
\]

where \( \alpha = \frac{r_B}{r_A} \) (Eq. 17)

and \( h \) is the thickness of the collection tube wall.

For uniform velocity profiles, the stream function is of the form:

\[
\psi = \frac{1}{2} \omega r^2 \tag{Eq. 18}
\]

To allow for greater generality, the stream function and the geometric variables are restated in the following dimensionless form:
The boundary values for the stream function and the geometric configuration in terms of the dimensionless variables are shown in Figure 4.

The axially symmetric stream function equation (Figure 13) becomes:

$$\frac{\partial^2 \psi}{\partial R^2} - \frac{1}{R} \frac{\partial \psi}{\partial R} + \frac{\partial^2 \psi}{\partial Z^2} = 0$$  \hspace{1cm} (Eq. 25)

6. DISCRETIZATION SCHEME FOR THE AIR FLOW FIELD

The equation for the axially symmetric stream function (Eq. 25) is discretized as follows:

$$\frac{\psi_{i-1,j} - 2\psi_{i,j} + \psi_{i+1,j}}{\Delta R^2} + \frac{\psi_{i+1,j} - \psi_{i-1,j}}{2\Delta R^2} = 0$$ \hspace{1cm} (Eq. 26)

$$\frac{\psi_{i,j-1} - 2\psi_{i,j} + \psi_{i,j+1}}{\Delta Z^2} = 0$$

where \(i\) and \(j\) are the grid point numbers in the \(R\) and \(Z\) directions respectively (Figure 5). Eq. 26 can be rearranged to give a simple equation by choosing a square grid so that \(\Delta R\) and \(\Delta Z\) are equal. The resulting equation, which is suitable for Gauss-Seidel iteration.
(Carnahan et al., 1969), is given as follows:

\[
\psi_{i,j} = \frac{\psi_{i-1,j} + \psi_{i+1,j} + \psi_{i,j-1} + \psi_{i,j+1}}{4}
\]

(Eq. 27)

\[
\frac{\psi_{i+1,j} - \psi_{i-1,j}}{8i}
\]

Eq. 27 can be applied to all interior points, which are defined as points for which the nearest boundary is at least one grid unit away.

In dealing with points on or surrounding the boundary described by the sampling cone (for which the nearest boundary in either the horizontal or vertical direction is less than one grid square away), a Taylor series expansion was used (Carnahan et al., 1969) and the following finite difference equations derived. (The first applies to points below or to the left of the curved boundary, and the second, to points above or to the right of the boundary.)

\[
\psi_{i,j} = \frac{ab}{a+b} \left[ \frac{\psi_{i,j-1}}{b+1} + \frac{\psi_{i-1,j}}{a+1} + \frac{\psi_{i,j}}{a(a+1)} + \frac{\psi_{i+1,j}}{b(b+1)} - \frac{\psi_{i-1,j-1}}{2(a+1)} \right] 
\]

(Eq. 28)

\[
\psi_{i,j} = \frac{ab}{a+b} \left[ \frac{\psi_{i,j+1}}{b+1} + \frac{\psi_{i+1,j}}{a+1} + \frac{\psi_{i,j}}{a(a+1)} + \frac{\psi_{i+1,j}}{b(b+1)} - \frac{\psi_{i+1,j-1}}{2(a+1)} \right] 
\]

(Eq. 29)

where \( a \) is the vertical distance \((0 < a \leq 1)\) to \( \psi_{v} \) and \( \psi_{v} \) represents (for points below the curve) either the boundary \( \psi \)-value (if the boundary lies between \( \psi_{i,j} \) and \( \psi_{i+1,j} \)) or the adjacent \( \psi \)-value \((\psi_{i+1,j})\). (For points above the curve, \( \psi_{v} \) takes either the boundary value or the value of \( \psi_{i-1,j} \).)

In the horizontal direction, \( b \) is similarly defined as the distance \((0 < b \leq 1)\) to \( \psi_{H} \) and \( \psi_{H} \) is the closer of the two \( \psi \)-values, the boundary value and the adjacent value \((\psi_{i,j+1} \) for points below the curve and \( \psi_{i,j-1} \) for points above it).

The grid size was chosen from past experience (Mellsen, 1979) so that each grid unit (both horizontally and vertically) represents 1/8 inch. Transferred to the grid (Figure 5), the straight tube radius, \( r_{b} \), then corresponds to 3 units, the inlet radius, \( r_{c} \), is 20 units, the boundary
tube radius, $r_A$, is 120 units (to be located a distance of five times the inlet radius outward from the edge of the cone), the complete length of the inlet cone, $y$, is 48 units, and the distance to the upstream end of the boundary tube, $x$, is 152 units (so as to be more than seven inlet radii upstream of the collection inlet). Specifying the boundary tube radius and the distance to the upstream boundary in this way ensures that the behaviour of the flow be as if the inlet cone were situated in free space and the particles coming from such a distance upstream as not to be affected by the cone.

The stream function was obtained by Gauss-Seidel iteration using Equation 27, 28 and 29. The boundary conditions were set initially at the centerline, at the boundary tube wall and inlet, and at the outlet, and held constant throughout the iterative procedure. Any point not falling on either one of these boundaries or the wall of the inlet cone was initialized to zero. A Fortran program (listed in Appendix A) was written to perform the calculations on an IBM 370 computer.

A special routine (adapted from Carnahan et al, 1969) to handle points near the curved wall of the inlet cone had to be incorporated into the Fortran program. This routine first labels points as being one of four types (see Figure 6) by finding the highest point, JMAX (the maximum within the boundary), for each row, I, and classifying points according to the horizontal and vertical distances to the curve (B and A, respectively):

$$B = AK - \sqrt{RK^2 - ((I-1) - BK)^2 - (J-1)}$$
(Eq. 30)

$$A = BK - \sqrt{RK^2 - ((J-1) - AK)^2 - (I-1)}$$
(Eq. 31)

where I and J are the coordinates of the point, and AK, BK and RK assume the values of the $\alpha$, $\beta$ and r in the equation,

$$(X - \alpha)^2 + (Y - \beta)^2 = r^2$$
(Eq. 32)

from the particular circular arc (Eqs. 3, 4 and 5) defining the curve at that point. The distance, A, is then found for every point in each row, starting at JMAX and decreasing along the row until an interior point is reached, and the procedure is repeated on the right side of the curve, using JMIN(I) (the minimum above the boundary, neglecting the wall thickness of the cone):
JMIN(I) = JMAX(I) + 1  

(Eq. 33)

and continuing until the upper interior point is reached. The horizontal and vertical distances are now defined by:

BO = 1 - B  

(Eq. 34)

AO = (I-1) - [BK - \sqrt{BK^2 - (J-AK)^2}]  

(Eq. 35)

The coefficients of the \( \psi \)-values in Equations 28 and 29 are then calculated using A and B (for Eq. 28) or AO and BO (as a and b in Eq. 29).

Type IV points are assigned the boundary value and held fixed through the program. For the other types (I, II and III), the values of \( \psi_v \) and \( \psi_H \) can then be determined and the iteration performed according to Eq. 28 (for points below the curve) or Eq. 29 (for points above the curve). For example, for a Type II point, \( \psi_{i,j} \), below the curve, \( \psi_v \) would assume the value of the boundary and \( \psi_H \), the value of \( \psi_{i+1,j} \), while if \( \psi_{i+1,j} \) were above the curve, \( \psi_v \) would again assume the boundary value, but \( \psi_H \) would become \( \psi_{i,j-1} \).

7. **SOLUTION OF THE EQUATIONS OF MOTION**

From Section 2 of this report, as in a prior paper (Mellsen, 1979), the problem is to find the upstream particle and fluid radii, \( r_{P,v} \) and \( r_{S,v} \), respectively, in order to calculate the sampling and collection efficiencies. In the same dimensionless form of Equations 6 and 7, the value of \( \bar{r}_{P,v} \) (notation) was found by an iterative procedure called the half interval method (Carnahan et al, 1969). The value of \( r_{P,v} \) for a critical particle was estimated far upstream, the path followed to the plane of the cone inlet and the miss distance (from the edge of the inlet) calculated. Next, the aforementioned half interval method was applied to determine a better initial estimate, the path again followed to the plane of the inlet, and another miss distance calculated. This was repeated several times until sufficient accuracy was achieved. The initial upstream position in a plane perpendicular to the flow direction was located far enough from the inlet so that free stream conditions would prevail. A distance of seven inlet radii upstream of the inlet was considered adequate on the basis of the five inlet radii serving the case of straight tube sampling (Batchelor, 1956).
The path of an individual particle was determined step-by-step by applying a fourth order Runge-Kutta method (Carnahan et al., 1969) to the equations of motion (Eqs. 6 and 7). The values of Re and K in these equations were easily found for each new step by direct substitution of previously determined values into Eqs. 8, 9, and 10, but the value of \( C_D \text{Re} \) in Eqs. 6 and 7 had to be calculated in each step by numerical solution of the definitive empirical equations (Eqs. 11 and 12). This was done using Newton's method (Carnahan et al., 1969) for finding the zero of a function. The values of \( \bar{u}_r, \bar{u}_z \) were calculated in each step from the stream function field as follows:

\[
\bar{u}_r = \frac{\psi_{i,j-1} - \psi_{i,j+1}}{4(i-1)(\Delta R)^2} \quad \text{(Eq. 36)}
\]

\[
\bar{u}_z = \frac{\psi_{i+1,j} - \psi_{i-1,j}}{4(i-1)(\Delta R)^2} \quad \text{(Eq. 37)}
\]

where \( i \) and \( j \) define the grid point of the particle position. Since the inlet radius of the sampler was chosen to be 20 grid units, these are given by:

\[
i = 1 + 20 \bar{r} \quad \text{(Eq. 38)}
\]

\[
j = j_0 + 20(\bar{z} - \bar{z}_0) \quad \text{(Eq. 39)}
\]

where \( j_0 \) and \( \bar{z}_0 \) are the starting point values of \( j \) and \( \bar{z} \). The values of \( i \) and \( j \) obtained from Eqs. 38 and 39 were rounded off to the nearest lower integer value in each calculation. The value of \( \bar{r}_{S,s} \) was obtained directly from the stream function by:

\[
\bar{r}_{S,s} = \frac{\Delta R(i-2)r_A}{r_C} \sqrt{\frac{\psi_{i,j}}{\psi_{i-1,j}}} \quad \text{(Eq. 40)}
\]

calculated at the lowest value of \( i \) satisfying:

\[
\psi_{i,j} > \psi_{i_C,j_C} \quad \text{(Eq. 41)}
\]

where \( i_C \) and \( j_C \) define the grid point at the edge of the collection cone inlet. The calculations to obtain the solutions were done with an
IBM 370 Computer by means of a Fortran program, the listing of which is shown in Appendix B. The sampling and collection efficiencies given by Eqs. 1 and 2 were also obtained by this program after the values of \( r_p \) and \( r_s \) had been calculated.

8. **RESULTS**

**Method of Analysis**

A stream function array was computed for each of the following ratios of \( U_B : 400, 400, 400, 400, 400 \) and 400. Because of the funnel shape of the sampler, tapering from an inlet radius of 2½ inches to a straight-tube radius of 3/8 inch, a velocity of \( U_B = 400 \) implies an inlet velocity of 9. This means that the sampling velocity ratios \( \frac{U_A}{U_i} \) are 1/9, 1/3, 1, 3 and 6. When the sampler operates at its design capacity of 1000 \( k/\min \), the values of \( U_B \) and \( U_i \) then become \( U_B = 5847.482 \) cm/s and \( U_i = 131.5683 \) cm/s, so that \( U_A \) varies from 14.62 cm/s \( \left( \frac{U_A}{U_i} = \frac{1}{9} \right) \) to 789.4 cm/s \( \left( \frac{U_A}{U_i} = 6 \right) \).

A broad range of particle sizes, of diameters, 6, 10, 20, 50, 100, 200 and 500 microns, composing monodisperse fields, was analyzed for each stream function array. Results were tabulated and plotted in graphs of sampling efficiency versus inertia parameter (Figure 7; \( \frac{C}{C_0} \) vs \( \log K \)), collection efficiency versus inertia parameter (Figure 8; \( E_m \) vs \( \log K \)), and sampling efficiency versus sampling velocity ratio (Figure 9; \( \frac{C}{C_0} \) vs \( \frac{U_A}{U_i} \)).

**Discussion**

The validity of the mathematical model has been discussed and reported (Mellsen, 1979). Results of the present work (Table of Results) show the sampling efficiency of a uniform field of 20 micron spherical particles, in a wind that is six times the sampling inlet velocity, to be in error by over 30% \( \left( \frac{C}{C_0} = 1.306 \right) \). Since smaller particles are carried more readily with the air stream, the sampling of small particles gives
rise to smaller error. The exact errors for very small particles cannot be determined by this model because computing errors increase with decreasing particle size (Mellsen, 1979), the reason being that as particle size decreases, a larger number of calculations is required.

The case of isokinetic sampling, where free stream velocity matches inlet velocity \( \frac{U_A}{U_1} = 1 \), should be characterized by both sampling and collection efficiencies equal to 1 \( \left( \frac{C}{C_0} = 1, E_m = 1 \right) \). This is displayed quite well by the predicted values of the model. For example (Table of Results), a 6 micron-particle field indicates an error of only 1.7\% \( \left( \frac{C}{C_0} = 1.017 \right) \), and a 100 micron-particle field, of 2.5\% \( \left( \frac{C}{C_0} = .9748 \right) \).

Although the model cannot be used for the prediction of efficiencies in completely still air, very low free stream velocities can be handled. The lowest free stream velocity currently tested and plotted is 14.62 cm/s, but if desired, lower velocities might be tried. The effect of varying free stream velocity while keeping the sampling velocity constant is clearly illustrated in Figure 9 for selected particle sizes.

9. CONCLUSIONS

The effect of anisokineticy on sampling with the DRES large-volume air sampler is sufficient to produce significant errors in sampling and collection efficiencies. A mathematical model, formerly applied to a straight, tapered-tube sampling probe, was modified to be applied to the specific large-volume sampler developed at DRES. The results from the model can serve to predict the magnitude of sampling errors. Several free stream velocities for a fixed sampling rate were evaluated with a number of monodisperse fields of suspended particles. Therefore, if the wind velocity and particle size and density are known, the results of this model can be used in correcting measured samples.
10. **REFERENCES**

<table>
<thead>
<tr>
<th>Author(s)</th>
<th>Year</th>
<th>Title</th>
<th>Publisher/Source</th>
</tr>
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</table>
NOTES

1. CONTOUR DIMENSIONS ARE APPROXIMATE. TRANSITION AND POINTS OF TANGENCY SHOULD BE SMOOTH.

2. Cone to have 1/16" thick wall.

FIGURE 1: DESIGN DRAWING OF LARGE VOLUME AIR SAMPLER
FIGURE 2: CO-ORDINATE SYSTEM FOR AXIAL FLOW IN THE PROXIMITY OF THE COLLECTION Cone
\[ \psi = 1 - \frac{U_C}{U_A} (1 - R^2) \]

\[ \psi = 0 \]

\[ \psi = \frac{U_B}{U_A} R^2 \]

\[ \psi = \frac{U_B}{U_A} \alpha^2 \]

\[ \beta \]

\[ \gamma \]

\[ \delta \]

\[ R = 0 \]

\[ \text{FIGURE 4: STREAM FUNCTION BOUNDARY CONDITIONS} \]
FIGURE 6: TYPES OF BOUNDARY POINTS
FIGURE 7: EFFECT OF VELOCITY RATIO ON SAMPLING EFFICIENCY

FREE STREAM CONCENTRATION
SAMPLE CONCENTRATION

INERTIA PARAMETER $K = \frac{\rho \pi A}{18 \mu}$
FIGURE 8: EFFECT OF VELOCITY RATIO ON COLLECTION EFFICIENCY
**TABLE I RESULTS**

<table>
<thead>
<tr>
<th>$U_B$</th>
<th>$U_A$</th>
<th>$U_A$ (cm/s)</th>
<th>$d$ (cm)</th>
<th>$K$</th>
<th>$C/C_0$</th>
<th>Em</th>
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</thead>
<tbody>
<tr>
<td>400/9</td>
<td>1/9</td>
<td>14.62</td>
<td>.05</td>
<td>1.787</td>
<td>.3754</td>
<td>2.749</td>
</tr>
<tr>
<td></td>
<td>.02</td>
<td>.2860</td>
<td>.07149</td>
<td>.6708</td>
<td>4.912</td>
<td></td>
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<tr>
<td></td>
<td>.01</td>
<td>.01787</td>
<td>.01787</td>
<td>.8487</td>
<td>6.215</td>
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<tr>
<td></td>
<td>.005</td>
<td>.002860</td>
<td>.002860</td>
<td>.9358</td>
<td>6.853</td>
<td></td>
</tr>
<tr>
<td></td>
<td>.001</td>
<td>.0007149</td>
<td>.0007149</td>
<td>.9592</td>
<td>7.024</td>
<td></td>
</tr>
<tr>
<td></td>
<td>.0006</td>
<td>--</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

| 400/3 | 1/3   | 43.86        | .05      | 5.362 | .4645    | 1.243 |
|       | .02   | .8579        | .2145    | .6418 | 1.717    |
|       | .01   | .05362       | .05362   | .8014 | 2.144    |
|       | .005  | .008579      | .008579  | .9223 | 2.486    |
|       | .002  | .002145      | .002145  | .9681 | 2.590    |
|       | .001  | .0007721     | .0007721 | .9773 | 2.615    |
|       | .0006 | --           |          |      |          |    |

| 400/9 | 1/1   | 131.6        | .05      | 16.09 | .8950    | 1.004 |
|       | .02   | 2.574        | .6434    | .9286 | 1.042    |
|       | .01   | .1609        | .1609    | .9748 | 1.094    |
|       | .005  | .02574       | .02574   | 1.007 | 1.130    |
|       | .002  | .006434      | .006434  | 1.015 | 1.139    |
|       | .001  | .002316      | .002316  | 1.016 | 1.140    |
|       | .0006 | --           |          |      |          |    |

| 400/27 | 3/3   | 394.7        | .05      | 48.26 | 1.628    | .9822 |
|        | .02   | 7.721        | 1.930    | 1.595 | .9624    |
|        | .01   | 1.930        | 1.930    | 1.516 | .9142    |
|        | .005  | 1.4826       | 1.4826   | 1.356 | .8182    |
|        | .002  | .07721       | .07721   | 1.161 | .7005    |
|        | .001  | .01930       | .01930   | 1.072 | .6466    |
|        | .0006 | .006949      | .006949  | 1.063 | .6413    |

| 400/54 | 6/6   | 789.4        | .05      | 96.51 | 2.071    | .9805 |
|        | .02   | 15.44        | 3.861    | 2.029 | .9608    |
|        | .01   | 3.861        | 3.861    | 1.930 | .9137    |
|        | .005  | 9.651        | 9.651    | 1.699 | .8045    |
|        | .002  | 1.544        | 1.544    | 1.306 | .6185    |
|        | .001  | 1.544        | 1.544    | 1.154 | .5464    |
|        | .0006 | .01390       | .01390   | 1.102 | .5217    |

$U_B = 5847.482$ cm/s, $U_I = 131.5683$ cm/s

UNCLASSIFIED
APPENDIX A

COMPUTER PROGRAM FOR CALCULATING THE STREAM FUNCTION
COMMON PB1(12),IT13,URAT,UA,RA,NPR,NZ,UBL
COMMON INT,INDEX,ITER,RC,NRC,NPRC,NPN
READ(8)J,ITER,INTVL
1 INDEX = 1
CALL SR24
IF (INDEX .GT. 1) THEN
  WRITE (PB1,ITERS,URAT,UA,RA,NPR,NZ,UBL)
  READ(8)J,ITER,INTVL
  INDEX = INDEX + 1
END IF
CONTINUE

SUBROUTINE REPP1
COMMON PB1(12),IT13,URAT,UA,RA,NPR,NZ,UBL
COMMON INT,INDEX,ITER,RC,NRC,NPRC,NPN
WRITE(7)PB1(1),ITER,INT MLS
WRITE(7)PB1(1),ITER,INT MLS
RETURN

END

SUBROUTINE SR24
COMMON PB1(12),IT13,URAT,UA,RA,NPR,NZ,UBL
COMMON INT,INDEX,ITER,RC,NRC,NPRC,NPN
READ(8)J,ITER,INTVL
WRITE(7)PB1(1),ITER,INT MLS
WRITE(7)PB1(1),ITER,INT MLS
RETURN

END

THIS SUBROUTINE CALCULATES THE STREAM FUNCTION FOR FLOW THROUGH TWO CONCENTRIC PIPES WITH A FUNNEL-SHAPED INSIDE PIPE

SUBROUTINE SR24
COMMON PB1(12),IT13,URAT,UA,RA,NPR,NZ,UBL
COMMON INT,INDEX,ITER,RC,NRC,NPRC,NPN
READ(8)J,ITER,INTVL
WRITE(7)PB1(1),ITER,INT MLS
WRITE(7)PB1(1),ITER,INT MLS
RETURN

END

READ(8) J, INDEX, INT MLS
WRITE(7) PB1(1), ITER, INT MLS
WRITE(7) PB1(1), ITER, INT MLS
CALCULATE AND WRITE DIMENSIONLESS PARAMETERS

ALPHA = RA/R
BETA = R/A
DELTA = BETA/ALPHA
UCR = UB*CF/1.0 - ((URAT*0.5)/UB)*ALPHA**2
UAT = UB/UB
UCR = UCR/UCR
WRITE(6,201)ALPHA,BETA,DELTA,URAT,UCR
READ(7),RD,RA,PSID/(1.0/RA**2)

END
ESTABLISH BOUNDARY POINTS

NP2=N1+1
NPB=NR+1
DELRI=1.0/FLOAT(NR)
XRE=1*0.5L/0.5L+N0.5L
NPB=NPB+1
XRB=ALPHA*N0.5L
NPB=NPB+1
NPRB=NPB+1
NPRC=NR+1

IF PSI IS PARTIALLY CALCULATED AND IN FILE
GO DIRECTLY TO FURTHER ITERATIONS
IF(INDEX)I.17
CONTINUE

ESTABLISH INITIAL GUESSES FOR STREAM FUNCTION
AND SET BOUNDARY CONDITIONS ON CENTRE LINE
AND INLET OF OUTSIDE PIPE

DO 2 I=1,11
PSI(I,1)=R*(RI+DELRI)**2
DO 2 J=2,NP2
PSI(I,J)=0.0

2 SET BOUNDARY CONDITION AT OUTLET OF INSIDE PIPE

DO 3 I=1,NPRB+1
PSI(I,1)=R*(RI+DELRI)**2

3 SET BOUNDARY CONDITION AT OUTLET OF OUTSIDE PIPE

DO 4 I=1,NPRB
PSI(I,1)=1.0-UCRA*(1.0*(RI+DELRI)**2)

4 SET BOUNDARY CONDITION AT NECK OF INSIDE PIPE

DO 5 J=M-PH,NP2
PSI(NPRB,J)=PS1

5 SET BOUNDARY CONDITION AT WALL OF OUTSIDE PIPE

DO 6 J=1,NP2
PSI(NPRB,J)=1.0

6 SET BOUNDARY CONDITION AT FUNNEL WALL

7 MNPB=NPB
MNPH=NPB-2
KIA=1,2,3,4,5
CALL ACCEPT(X23,Y23,R2,R3,B2,3,4,R3)

CALL ACCEPT(X12,Y12,R1,R2,B1,A2)

1 CALL BOUNDARY(Z1,A1,R1,R2,B1,A2)

DO 7 I=1,NPRB
J=J+1
JN=J+NP2

IF (JNE+JN)43 J=63,62,61
CONTINUE

COMPUTE SUCCESSIVELY BETTER APPROXIMATIONS FOR
THE STREAM FUNCTION AT ALL GRID POINTS. ITERATING BY
THE STAGGERED MODEL METHOD UNTIL THE CONVERGENCE CRITERION
IS SATISFIED

8 EPS=0.0
ITER=0
ITER=ITER+1
DO 6 I=1,NR
J=1,NP2
JN=J+NP2
C

10 IF (1 - NPR) 17, 1A, 19
20 IF (J - JNPR) 11, 17, 20
30 IF (J + 1 - JNPR) 11, 17, 20
40 IF (1 - JNPR) 11, 17, 20
50 IF (1 - JNPR) 11, 17, 20
60 GO TO 60
70 CONTINUE
80 IF (1 - JNPR) 11, 17, 20
90 GO TO 70
100 IF (1 - JNPR) 11, 17, 20
110 GO TO 110
120 IF (1 - JNPR) 11, 17, 20
130 GO TO 130
140 IF (1 - JNPR) 11, 17, 20
150 GO TO 150
160 IF (1 - JNPR) 11, 17, 20
170 GO TO 170
180 IF (1 - JNPR) 11, 17, 20
190 GO TO 190
200 IF (1 - JNPR) 11, 17, 20
210 GO TO 210
220 IF (1 - JNPR) 11, 17, 20
230 GO TO 230
240 IF (1 - JNPR) 11, 17, 20
250 GO TO 250
260 IF (1 - JNPR) 11, 17, 20
270 GO TO 270
280 IF (1 - JNPR) 11, 17, 20
290 GO TO 290
300 RETURN
SUBROUTINE for determining boundary points and intercepts

SUBROUTINE BNDPTS(M, N, JR, JMAX, ITYPE, C, D, E, F, G, H, Y12, Y23, JRO, A1, B1, 
IR, R1, R2, R3, A3, B3, R3)
DIMENSION JR(20), JMAX(20), ITYPE(20, 32), C(20, 32), D(20, 32), 
E(20, 32), F(20, 32), G(20, 32), H(20, 32), JRO(20), JMIN(20)
EPS = 1.0E-6
MP = M + 1

LOCATE extreme right point
(1, JMAX(I)) and determine its type

JMAX(1) = N + 2
JMIN(1) = N + 2
IF (F(JMIN) = 1) MP1
IF (F(JMAX) = 1) MP2

10 IF (F(JMIN) = Y12) 12, 12, 13
12 AK = 1
BK = B1
RKR = 1
GOTO 16
13 AK = 2
BK = B2
RKR = 2
GOTO 16
14 AK = 3
BK = B3
RKR = 3
GOTO 16
15
16 XORD = AK = SQRT(RK**2 - (F(JMIN) - BK)**2)
JM = XORD + EPS
JMM = JMM + 1
J = JMAX(I)
GOTO 16

32 IF (A + 1) 5, 5, 1
IF (A - 1) 6, 6, 6
CONTINUE
ITYPE(I, J) = 1
CONTINUE

5 CONTINUE
ITYPE(I, J) = A/(A+B)
D(J, J) = 1/(B+1, 0)
E(J, J) = 1/(A+B)
F(J, J) = 1/(A+B)
H(J, J) = 1/(A+B)
G(J, J) = 1/(A+B)
IF (AO + 1) 30, 30, 35
35 ITYPE(JP1) = 3
AO = AO + 1
GOTO 37
39 ITYPE(JP1) = 1
CONTINUE
C(JP1) = AO*BO/(AO+BO)
E(JP1) = 1/(BO+1)
F(JP1) = 1/(AO+1)
G(JP1) = 1/(AO+1)
H(JP1) = 1/(BO+1)
7 CONTINUE
LOCATE BOUNDARY POINTS OF TYPE 2

SUBROUTINE FOR FINDING INTERCEPTS OF CIRCULAR ARC

END
APPENDIX B

COMPUTER PROGRAM FOR SOLVING THE EQUATION OF MOTION
//MOTION JOB (0162, 1012) T.now, ITEN=0,0,20)
//MOB LEVEL: 1 CLASS: TIME=0.20
//#MOB LEVEL: 1 CLASS: INTERVAL=0.20
//EXEC FORTEK, FORRIZE, FORTIZ OPTIMIZE=0)
//SYSTRAN OD SYSTOUT
//PORT SYSTOD SYSTOUT
//DIMENSION G(4), D(3)
1 READ DC, DP, RHO, SIGMA, XMU, UB, TN
WRITE (6, 201) G, LFT, G, IR, SIGMA, DTAU, NIBP, NBBP, NX
ESTABLISH PHYSICAL PROPERTIES FOR CALCULATING COLLECTION

DF IS CYLINDER DIAMETER, CM
RHO IS FLUID DENSITY, GM/CC
SIGMA IS ABSOLUTE SURFACE TENSION, CM/CC
UB IS FREE STREAM VELOCITY, CM/SEC
TN IS STARTING RATIO L/R = C(3)
READ(5, *) DC, DP, RHO, SIGMA, XMU, UB, TN
IF CORRECTED STREAM FUNCTION VALUES ARE ALREADY IN TEMPORARY
READ(5, *) ISOP
2 CONTINUE
CALCULATE STREAM FUNCTION, APPLY VELOCITY SOLUTION
READ(5, **) D(3)
WRITE (6, 301) D(3)
3 CONTINUE
UA IS FREE STREAM VELOCITY, CM/SEC
UA = UB / UAT
RE = RHO * 0.9 * XMUA / XMU
P = RE / (XMU + DC)
WRITE (6, 302) RE, XMUA, XMU, UA, UB, TN
ESTABLISH GRID STEP SIZE
NR = NPR / FLOAT(NP)
DELT = 1.0 / FLOAT(NR)
R = RARC = 0.001
HALF INTERVAL ITERATION FOR INITIAL G6 VALUE
DO 21 ITER = 1, NX
SET AND PRINT INITIAL CONDITIONS
M80
NSTEP = 0
10 TAU = 0
G8ER = Float(1)
NGER = G8ER
G8ER = GMFT + G8IR / 2.0
G8ER = GMFT + G8IR / 2.0
J = 0
NR = NPR / (NRC - 1)
RE = (1 - 1) / (1 - 1)
U = (1 - 1) / (1 - 1)
G = 1
RE = (U - G(2)) ** 2 + (U - G(1)) ** 2 = 0.5
IF ON ITER = N (NP)
5 CONTINUE
6 CONTINUE
7 CONTINUE
WRITE (4, 251) ITER, G, LFT, G, ZER, G, IR, DTAU, G(1), G(2), G(3), G(4), UZ, UR,
1 XEKE
CALL ON RUNGE KUTTA SUBROUTINE
CONTINUE
M=M+1
CALL BM2(P4, DG, TAU, DTAU, IRUNG, M)
IF(IRUNG=1)110, 10
I = 1*IC(XCDRE)**2 + (UZ-G(1)**2)**0.5
XCDRE*CDE(RE)
DG(1)=(XCDRE)/(24.0*XX)**(UZ-G(1))
DG(2)=(XCDRE)/(24.0*XX)**(UR-G(2))
DG(3)=G(1)
DG(4)=G(2)
GO TO 1
CONTINUE
M=0

CALCULATE FLUID VELOCITY AT PARTICLE POSITION
I = 1+IPX4(RC*G(4))
J = 1+IPX4(RC*(G(3)-G3ZER))
U2=FLOAT(I+1)
UR=(PSI(I,J+1)-PSI(I,J))/FDRG**R
UR=(PSI(I,J+1)-PSI(I,J))/FDRG**R
PRINT SOLUTIONS
IS = ITER/N1BP*N1BP
IF(IS=ITEN)11, 11
CONTINUE
IF(ITER-1)12, 12
CONTINUE
IF(NSTEP-NSOP)17, 17
CONTINUE
NSSTEP=0
TAU = TAU + 0.0001
WRITE(6,204)TAU,G(1),G(2),G(3),G(4),UZ,UR,XCDRE
INTEGRATE ACROSS ANOTHER STEP IF REQUIRED
H1S=G(3)
IF(H1S)8, 8, 8
CONTINUE
FIND INTERVAL HALF WITH THE SIGN CHANGE
IF((G(4)-1.0)*SIGNL=0.0)19, 19
CONTINUE
CONTINUE
CONTINUE
CONTINUE
CONTINUE
CONTINUE
CONTINUE
CONTINUE
WRITE(6,204)TAU,G(1),G(2),G(3),G(4),UZ,UR,XCDRE
CALCULATE THE COLLECTION EFFICIENCY
WRITE(6,209)G4ZER
EM = G4ZER**2
WRITE(6,206)EM
CALCULATE THE SAMPLING EFFICIENCY
RSINF = SQRT(PSI(NPRC,NPZB)**RA/RC)
PSIH = PSI(NPRC,NPZB)
GO TO 25
IF(PSI(I,J))25, 25
CONTINUE
PSIH = FLOAT(I=2)*SQRT(PSIHT/PSI(I,J)+10)**DELR*RA/RC
GO TO 28
CONTINUE
WRITE(6,210)RSINF
C=M=G4ZER/RSINF**2
WRITE(6,207)CR
READ(5,*)NSTP
IF(NSTOP)1, 30
STOP
30 STOP
FORMATS FOR OUTPUT STATEMENTS

200 FORMAT(1H1,37X,40M COLLECTION EFFICIENCY OF A CIRCULAR TUBE/
1 H10)
201 FORMAT(10M0GALEF =, F10.6/10M GA RIT =, F10.6/10M SIG NL =, I1/
1 F0.0/10M DATA =, F10.6/10M NS8P =, I1/10M NX =, I1/
2 10M P =, I1/10M UB =, I1/10M IMA =, I1)
202 FORMAT(10MO RES =, F12.7/10M XX =, E12.6/
1 10M P =, E10.4/10M DC =, F10.6/10M DP =, F10.7/10M RM0 =, F10.6/10M XN =, F10.4/
2 10M UB =, F10.4/10M IMA =, I1)
203 FORMAT(10MO ITER =, I13/10M GALEF =, F10.6/10M GA RIT =, F10.6/10M SIG NL =, I1/
1 F0.0/10M DATA =, F10.6/10M SIG NL =, F10.6/10M UA =, F10.6/10M U =, F10.4/
2 10M UB =, F10.4/10M IMA =, I1)
204 FORMAT(10M0ITER =, I13/10M GA LEF =, F10.6/10M GA RIT =, F10.6/10M SIG NL =, I1/
1 F0.0/10M DATA =, F10.6/10M SIG NL =, F10.6/10M UA =, F10.6/10M U =, F10.4/
2 10M UB =, F10.4/10M IMA =, I1)
205 FORMAT(10M0ITER =, I13/10M GA LEF =, F10.6/10M GA RIT =, F10.6/10M SIG NL =, I1/
1 F0.0/10M DATA =, F10.6/10M SIG NL =, F10.6/10M UA =, F10.6/10M U =, F10.4/
2 10M UB =, F10.4/10M IMA =, I1)
206 FORMAT(10M0ITER =, I13/10M GA LEF =, F10.6/10M GA RIT =, F10.6/10M SIG NL =, I1/
1 F0.0/10M DATA =, F10.6/10M SIG NL =, F10.6/10M UA =, F10.6/10M U =, F10.4/
2 10M UB =, F10.4/10M IMA =, I1)
207 FORMAT(10M0ITER =, I13/10M GA LEF =, F10.6/10M GA RIT =, F10.6/10M SIG NL =, I1/
1 F0.0/10M DATA =, F10.6/10M SIG NL =, F10.6/10M UA =, F10.6/10M U =, F10.4/
2 10M UB =, F10.4/10M IMA =, I1)
208 FORMAT(10M0ITER =, I13/10M GA LEF =, F10.6/10M GA RIT =, F10.6/10M SIG NL =, I1/
1 F0.0/10M DATA =, F10.6/10M SIG NL =, F10.6/10M UA =, F10.6/10M U =, F10.4/
2 10M UB =, F10.4/10M IMA =, I1)
209 FORMAT(10M0ITER =, I13/10M GA LEF =, F10.6/10M GA RIT =, F10.6/10M SIG NL =, I1/
1 F0.0/10M DATA =, F10.6/10M SIG NL =, F10.6/10M UA =, F10.6/10M U =, F10.4/
2 10M UB =, F10.4/10M IMA =, I1)
210 FORMAT(10M0ITER =, I13/10M GA LEF =, F10.6/10M GA RIT =, F10.6/10M SIG NL =, I1/
1 F0.0/10M DATA =, F10.6/10M SIG NL =, F10.6/10M UA =, F10.6/10M U =, F10.4/
2 10M UB =, F10.4/10M IMA =, I1)
211 FORMAT(10M0ITER =, I13/10M GA LEF =, F10.6/10M GA RIT =, F10.6/10M SIG NL =, I1/
1 F0.0/10M DATA =, F10.6/10M SIG NL =, F10.6/10M UA =, F10.6/10M U =, F10.4/
2 10M UB =, F10.4/10M IMA =, I1)

END SUBROUTINE GTPSI

FUNCTION CORE(RE)
C
C THIS FUNCTION COMPUTES THE PRODUCT OF DRAG COEFFICIENT
C AND REYNOLDS NUMBER FOR A SPHERE AS A FUNCTION OF
C REYNOLDS NUMBER
C
C CONSTANT COEFFICIENTS
A3=2.0154*1.E+00 A4=6.9105*1.E-09
A5=1.2953 B1=-9.861*1.E+01
B2=4.6677*1.E+02 B3=1.1235*1.E+03
C
CHOOSE THE APPROPRIATE POLYNOMIAL
IF(RE+4.0)2,7
C
INITIAL ESTIMATE
2 IF(RE+0.60001)3,4,4
C CORE = 0.0
GO TO 30
4 K=24.*RE
C
BEGIN NEWTON METHOD ITERATION
```
DO 6, ITER5=1, 20
FFX = A2 * X - 2 * A1 * X ** 2 + A3 * X ** 3 + A4 * X ** 4 - X
DELX = FF / FFX
X = DELX

CHECK FOR CONVERGENCE
EP = 1.E-06
10 EPABS = EP, DELX / X = EPBS = 5.5
10 CONTINUE
GO TO 20

INITIAL ESTIMATE
X = 1.0
ELOG = 0.301030
LOG = LOG(CONGID) + ELOG

BEGIN NEWTON METHOD ITERATION
DO 20, ITER5 = 21, 20
FREQ = A2 * X + 2 * A3 * X ** 2 + A4 * X ** 3
10 FREQ = A2 * X + 2 * A3 * X ** 2 + A4 * X ** 3
DELX = FF / FFX
X = DELX

CHECK FOR CONVERGENCE
EP = 1.E-06
IF (ABSS (DELX / X) = EP) 22, 22, 24
CONTINUE
RETURN

FORMATS FOR OUTPUT STATEMENTS
202 FORMAT (160D NO CONVERGENCE)

SUBROUTINE SM22 (N, YF, X, IRUNG, X)
END

FOURTH ORDER RUNGE KUTTA METHOD
FOR N FIRST ORDER ODE
DIMENSION PH1 (50), SAVY (50), Y (50), F (50)
GO TO (2, 3, 4, 5, 6, 7)
PASS 1
2 IRUNG = 1
RETURN

PASS 2
3 DO 22, J = 1, N
PH1 (J) = Y (J)
22 Y (J) = SAVY (J) + 0.5 * H * F (J)
X = X + H
IRUNG = 1
RETURN

PASS 3
4 DO 33, J = 1, N
PH1 (J) = PH1 (J) + 0.25 * H * F (J)
33 Y (J) = SAVY (J) + 0.25 * H * F (J)
IRUNG = 1
RETURN

PASS 4
5 DO 44, J = 1, N
PH1 (J) = PH1 (J) + 0.9 * F (J)
44 Y (J) = SAVY (J) + 0.9 * F (J)
X = X + H
IRUNG = 1
RETURN

PASS 5
6 DO 55, J = 1, N
Y (J) = SAVY (J) + (PH1 (J) + F (J)) * H / 6.0
55 IRUNG = 2
RETURN

END
```

Sampling and collection efficiencies are calculated for a large-volume air sampler under conditions of anisokinetic as well as isokinetic flow. A mathematical model developed to evaluate a tapered-tube sampling probe was modified to obtain results for the large-volume sampler, using various particle sizes and flow velocities. These results should facilitate the prediction or correction of sampling errors in field and laboratory experiments.
**KEY WORDS**

Particulate Sampling
Collection Efficiency
Sampling Probe

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