TUNABLE OPTICAL SOURCES

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TUNABLE OPTICAL SOURCES

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Scientific Personnel

on

U. S. Army Research Office (Durham)

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I. RESEARCH OBJECTIVES

This grant supports research into new methods and techniques for the generation of tunable radiation across wide regions of the electromagnetic spectrum. During the past semiannual period progress in both vacuum ultraviolet and tunable infrared generation has been considerable. This report describes the work in both of the above research areas.
II. TUNABLE INFRARED GENERATION

A. Introduction

In the last report the infrared nonlinear properties of CdSe for mixing were described. Generation of wavelengths between 9\(\mu\) and 27\(\mu\) is possible in CdSe with good efficiency. One drawback to CdSe is inadequate birefringence for generation of infrared wavelengths shorter than 9\(\mu\). Fortunately, a chalcopyrite crystal, AgGaSe\(_2\), has recently been grown which does have adequate birefringence to phasematch in the near infrared.

B. AgGaSe\(_2\)

The properties of AgGaSe\(_2\) are described in a paper submitted for publication (see Appendix A). Mixing experiments to generate 7\(\mu\) to 15\(\mu\) have also been described in a paper presented at the first tunable laser spectroscopy conference at Vail, Colorado in July 1973. This paper is reproduced as Appendix B.

Briefly, AgGaSe\(_2\) has a high nonlinear coefficient, phasematches for mixing to generate between 3\(\mu\) and 18\(\mu\) radiation, and phasematches for SHG for fundamental wavelengths between 3\(\mu\) and 13\(\mu\). AgGaSe\(_2\) is grown by the standard vertical Bridgeman method and low loss < 0.04 cm\(^{-1}\) single crystals up to 15 mm in length have been obtained. These qualities make AgGaSe\(_2\) particularly attractive as a phasematchable infrared nonlinear crystal within its 0.7\(\mu\) to 18\(\mu\) transparency range.
AgGaSe$_2$ forms an ideal match to a LiNbO$_3$ parametric oscillator source for generation of $3\mu$ to $18\mu$ radiation. A detailed study of a widely tunable coherent spectrometer based on a Nd:YAG pumped LiNbO$_3$ parametric oscillator has been completed. The basic results of the study are given here.

C. High Energy Widely Tunable Infrared Source

This section describes a unique combination of known methods and devices such that an extended $0.3\mu - 2\mu$ and $7\mu - 100\mu$ coherent tunable radiation source is possible. The device is based on a Nd:YAG laser pump source, a singly resonant LiNbO$_3$ parametric oscillator and mixing in four nonlinear crystals, AgGaSe$_2$, CdSe, LiNbO$_3$, and LiIO$_3$. It is expected that the device will achieve continuous scanning at $0.1$ cm$^{-1}$ bandwidth at 10 mJ energy per pulse at 10 pps in the near infrared and visible and corresponding performance with the energy reduced by the Manley-Rowe factor in the intermediate and far infrared. Spectral bandwidths of the order of $0.001$ cm$^{-1}$ appears likely for narrow tuning ranges of approximately $1$ cm$^{-1}$.

The features never before achieved that are unique to this source are:

1. 10 mJ energy per pulse
2. Wide infrared tuning range
3. Use of only 1 set of mirrors
4. Unique bandwidth control and local tuning methods
5. Rapid wide range tuning
6. Good frequency stability
The pump source is a Nd:YAG oscillator electro-optically Q-switched using a KD*P pockels cell of standard design. The oscillator is operated TEM<sub>00</sub> mode and substantially single frequency by proper aperture and etalon control. Nd:YAG lasers meeting this requirement are presently in operation.

The Nd:YAG laser may be followed by a double pass Nd:YAG amplifier. The amplifier increases the Nd:YAG laser energy from 10 mJ to between 100 and 450 mJ depending on the filling factor of the amplifier rod. For this case the rod diameter is 6 mm and the length is 30 mm. Experimental verification of these results has been demonstrated. If required, a further increase in energy output can be achieved with a second amplifier rod 1 cm in diameter and 30 mm in length. Figure 1 shows a schematic of the Nd:YAG pump source.

The LiNbO<sub>3</sub> parametric oscillator operates in the singly resonant mode with tuning achieved by crystal rotation. Figure 2 illustrates the schematic of the oscillator including bandwidth control elements. Figure 3 shows the tuning curves versus crystal angle for a fixed temperature near 120°C.

The LiNbO<sub>3</sub> parametric oscillator is the key element in the chain of tuning elements that follow. Therefore, threshold, conversion, efficiency, tuning method, and bandwidth will be considered in detail.

The gain of the LiNbO<sub>3</sub> parametric oscillator is limited by the available laser pump energy or by the crystal damage threshold. We will investigate the gain limitations for off-angle phasematched operation, and compare it with 90° phasematched operation.
FIG. 1.—Schematic of the 1.06 μm Nd:YAG laser-amplifier source.
FIG. 2—Full scale schematic of the angle tuned LiNbO$_3$ singly resonant parametric oscillator.
FIG. 3—Tuning curve for the LiNbO₃ parametric oscillator vs. crystal angle. The mirror reflectance range is indicated.
The gain of a parametric amplifier is given by\(^2\)

\[ G = \Gamma^2 t^2 = \left( \frac{2\omega_0^2 d^2}{\pi n_1 n_2 \varepsilon_0^3} \right) P_{30} t k_0 (1 - \varepsilon^2)^2 \bar{h}(B, \xi) \]  
(1)

In the plane wave limit with \( B = 0 \)

\[ \bar{h}(0, \xi) \to \xi = t/b \]  
(2)

so that

\[ G = \Gamma^2 t^2 = \left( \frac{\omega_0^2 d^2}{\pi n_1 n_2 \varepsilon_0^3} \right) P_{30} \frac{2t}{\pi} k_0 (1 - \varepsilon^2)^2 \frac{t}{b} \]  
(5)

since

\[ \frac{b}{k_0} = \omega_0^2 \]  
(4)

and for Gaussian beams

\[ A = \frac{\pi \omega_0^2}{2} \]  
(5)
For double refraction limited focusing

\[ \overline{h}(B, \xi) \approx \frac{\overline{h}_{\text{mm}}(0)}{1 + t/t_{\text{eff}}} \approx \frac{t_{\text{eff}}}{t} \]  

(6)

In this case the gain as a function of power is independent of crystal length. However, the gain does improve with \( I^2 \) as a function of intensity since

\[ \frac{\pi w_0^2}{2} = \frac{\pi}{16} \rho^2 t^2 \]  

(7)

is the useful maximum focal area. The effective interaction length is

\[ t_{\text{eff}} = \frac{\lambda_0}{2n_0^2} \overline{h}_{\text{mm}}(0) \approx \frac{\lambda_0}{2n_0^2} \]  

(8)

When the focal area determined by the crystal damage intensity equals that given by walk-off considerations, the use of 90° phasematched crystals is no longer required to maximize gain. Figure 4 shows the damage limited focal area. Also plotted are the 90° phasematched areas for a 5 cm crystal and the areas for 45° phasematched crystals of various lengths.

For areas greater than the walk-off area at a given crystal length, the plane wave gain formula applies. Thus for a 2 cm crystal, 1 mJ of energy is required at 1 J/cm² damage limit to reach the plane wave gain.

In this limit of loose focusing

\[ \overline{h}(B, \xi) = \frac{t/b}{1 + t/t_{\text{eff}}} \approx \frac{t}{b} \]  

(9)
FIG. 4—Damage limited focal areas vs. input pump energy for LiNbO₃.
The plane wave gain approximation applies for input energies greater than 8 mJ at \( l = 5 \) cm.
so that the gain reduces to

\[ G = \frac{K \beta_0 l^2 (1 - \delta^2)^2}{(\pi \omega_0^2/2)} \]  

(10)

for both 90° and off-angle phasematched crystals. For example, for 5 cm long crystals the gain is maximum at 0.1 mJ for 1 J/cm² damage threshold at 90° phasematching. For 45° phasematching, the gain is maximum for energies greater than 8 mJ. At this energy, the gain for off-angle phasematching equals that of 90° phasematching for the limiting input intensity and there is no requirement for the use of 90° crystals.

The calculated gain for the parametric oscillator is \( \Gamma l^2 = 0.32 \) at 1 MW/cm² for a 5 cm crystal. At the 80 MW/cm² burn-density limit, the parametric oscillator gain at degeneracy is

\[ \Gamma l^2 = 1.0 \quad l = 1 \text{ cm} \]
\[ = 4.0 \quad = 2 \text{ cm} \]
\[ = 9.0 \quad = 3 \text{ cm} \]
\[ = 16.0 \quad = 4 \text{ cm} \]
\[ = 25.0 \quad = 5 \text{ cm} \]

For efficient operation, gains greater than 4 are adequate. Presently available LiNbO₃ y-axis boules allow crystal lengths up to 5.0 cm. For longer crystals, special boules can be grown either along the y-axis or in the \((01\overline{4})\) direction. We have recently evaluated a \((01\overline{4})\) grown boule
and have shown that ruby crystals up to 5 cm in length are available at 45° phasematching angle.

The important conclusion reached here for the first time, is that parametric oscillator operation at 45° phasematching has the same gain characteristic as 90° phasematched operation for pump energies greater than 10 mJ. The electro-optic Q-switched Nd:YAG laser source meets this requirement even without the following amplifier. The amplifier does provide a significant increase in output energy that may improve the usefulness of this source for certain experiments. It is, however, not required for the successful operation of the widely tunable device.

Rise time considerations due to the short pump pulse length dictate a short oscillator cavity. However, since the equivalent loss due to rise time varies as cavity length, and the gain varies as \( i^2 \), it is advantageous to use the longest available crystal lengths.

The output of the parametric oscillator tunes between 1.5\( \mu \) and 3.7\( \mu \) using a single set of reflecting optics. This basic frequency range can be extended to cover the 3\( \mu \) to 18\( \mu \) region in AgGaSe\(_2\) and the 10\( \mu \) to 27\( \mu \) region in CdSe. Various sum generation processes also are possible in LiNbO\(_3\) and LiIO\(_3\). For example, the SHG of the idler in LiNbO\(_3\) covers the 1.06\( \mu \) \( \rightarrow \) 1.6\( \mu \) region, and the SHG of the signal in LiNbO\(_3\) covers the 0.75\( \mu \) \( \rightarrow \) 1.06\( \mu \) region. These processes angle phasematch and should be \( \sim 30\% \) efficient. In addition, 1.06 + idler in LiNbO\(_3\) and 1.06 + signal in LiNbO\(_3\) cover the 0.7\( \mu \) \( \rightarrow \) 0.8\( \mu \) and 0.6\( \mu \) \( \rightarrow \) 0.7\( \mu \) spectral range. Due to the high 1.06\( \mu \) power available these steps are also efficient. The above steps all involve a single angle phasematched LiNbO\(_3\) crystal. There may not be any
requirement to generate wavelengths shorter than 6000 Å; however, by use of a second crystal to sum the oscillator and its second harmonic in LiIO₃, the spectral range from 3300 Å to 7000 Å can also be covered. Figure 5 illustrates the spectral range versus phasematching angle reached by the LiNbO₃ parametric oscillator and the following mixers and sum generators.

For infrared generation by mixing we consider the LiNbO₃ parametric oscillator as a source of radiation at the signal and idler frequencies. The output energy of the oscillator at degeneracy is assumed to be 30% of the input pump energy. Two output energy ranges are possible, 3 mJ per pulse without the Nd:YAG amplifier, and 100 mJ per pulse with the Nd:YAG amplifier. Table I shows the estimated output power versus parametric oscillator frequency at the signal and idler waves.

The conversion efficiency for parametric mixing is given by

$$\left( \frac{\omega_1}{\omega_2} \right) I^2 f^2 = \frac{P_1}{P_2} \left( \frac{\omega_{1R}}{\omega_p} \right) = \left( \frac{\omega_1}{\omega_2} \right) \frac{2\omega_1 \omega_2 |d|^2 f I^2}{n_1 n_2 \epsilon_0 c^3}$$

where $\omega_1$ = infrared output, $\omega_2$ = idler frequency, and $\omega_p$ = signal frequency.

For CdSe and AgGaSe₂, the conversion efficiency for a pump wavelength at 1.833 μm is given by

$$I^2 f^2 \left( \frac{1\text{MW}}{\text{cm}^2} \right) \text{CdSe} = 0.006 \quad I = 1 \text{ cm}$$

$$I^2 f^2 \left( \frac{1\text{MW}}{\text{cm}^2} \right) \text{AgGaSe}_2 = 0.020 \quad I = 1 \text{ cm}$$
FIG. 5—Spectral range vs. crystal angle for the LiNbO$_3$ oscillator and following nonlinear crystal harmonic, sum, and mixer generators.
TABLE I

Estimated Output Energy of the LiNbO$_3$ Parametric Oscillator Source

<table>
<thead>
<tr>
<th>WAVELENGTH</th>
<th>10 mJ PUMP</th>
<th>300 mJ PUMP</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.5 μ</td>
<td>2.12 mJ</td>
<td>70.5 mJ</td>
</tr>
<tr>
<td>1.6 μ</td>
<td>2.00</td>
<td>66.5</td>
</tr>
<tr>
<td>1.8 μ</td>
<td>1.75</td>
<td>58.2</td>
</tr>
<tr>
<td>2.1 μ (deg)</td>
<td>3.00 mJ (s + i)</td>
<td>100.0 mJ (s + i)</td>
</tr>
<tr>
<td>2.5 μ</td>
<td>1.27</td>
<td>42.0</td>
</tr>
<tr>
<td>3.0 μ</td>
<td>1.06</td>
<td>35.0</td>
</tr>
<tr>
<td>3.5 μ</td>
<td>0.91</td>
<td>30.0</td>
</tr>
</tbody>
</table>
for phasematching near the 60° direction. In either crystal walk-off is
not a problem so that \( I_3 \) is limited by the crystal burn density. For
CdSe \( I_3 \leq 50 \text{ MW/cm}^2 \) and for AgGaSe\(_2\) \( I_3 \leq 10 \text{ MW/cm}^2 \). The maximum con-
version efficiencies are therefore

\[
\gamma^2 I_{\text{MAX}}^2 (\text{CdSe}) = 30\% \quad l = 1 \text{ cm}
\]

\[
\gamma^2 I_{\text{MAX}}^2 (\text{AgGaSe}_2) = 20\% \quad l = 1 \text{ cm}
\]

This improves as \( l^2 \) in the present focusing limit. The actual output
energy per pulse versus wavelength is shown in Table II.

Mixing in AgGaSe\(_2\) and CdSe is straightforward.\(^3,4\) The only requirement
is for proper crystal phasematching by angular rotation. Figure 6 shows
the phasematching peak obtained by mixing 1.318\(\mu\) and a 0.659\(\mu\) pumped
LiNbO\(_3\) parametric oscillator in AgGaSe\(_2\). The width of the peak is
\(24 \text{ cm}^{-1} \) at 1000 cm\(^{-1}\). Figure 7 shows the measured mixed output wave-
lengths of this device when the parametric oscillator is tuned. In the
present mixer, a single crystal cut at 62° phasematches over the 3.5\(\mu\) to
18\(\mu\) spectral range, as illustrated in Fig. 5.

CdSe also phasematches over its entire useful range with the use of
a single crystal cut at 70°. Due to lack of transparency and birefrin-
gence, 27\(\mu\) is the longest phasematched wavelength generated in the mid-
infrared.

The angular tolerance for phasematching is large enough that mechan-
ical or simple electrical tracking is possible without active feedback
# TABLE II

Expected Output Energies for Mixing in CdSe and AgGaSe$_2$

<table>
<thead>
<tr>
<th>INPUT WAVELENGTHS</th>
<th>OUTPUT WAVELENGTHS</th>
<th>OUTPUT ENERGY (10 mJ)</th>
<th>OUTPUT ENERGY (300 mJ)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>AgGaSe$_2$</strong> $l = 1$ cm $l^2/l^2 = 20%$</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.65 $\mu$m</td>
<td>3.05 $\mu$m</td>
<td>3.5 $\mu$m</td>
<td>$\theta = 75^\circ$</td>
</tr>
<tr>
<td>1.70</td>
<td>2.90</td>
<td>4.0</td>
<td>$\theta = 68^\circ$</td>
</tr>
<tr>
<td>1.75</td>
<td>2.70</td>
<td>5.0</td>
<td>$\theta = 62^\circ$</td>
</tr>
<tr>
<td>1.85</td>
<td>2.50</td>
<td>7.0</td>
<td>$\theta = 52^\circ$</td>
</tr>
<tr>
<td>1.95</td>
<td>2.35</td>
<td>10.0</td>
<td>$\theta = 49^\circ$</td>
</tr>
<tr>
<td><strong>CdSe</strong> $l = 1$ cm $l^2/l^2 = 30%$</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.95 $\mu$m</td>
<td>2.35 $\mu$m</td>
<td>10.0 $\mu$m</td>
<td>0.10</td>
</tr>
<tr>
<td>degenerate</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>15.0</td>
<td></td>
<td></td>
<td>0.063</td>
</tr>
<tr>
<td>20.0</td>
<td></td>
<td></td>
<td>0.044</td>
</tr>
<tr>
<td>25.0</td>
<td></td>
<td></td>
<td>0.04</td>
</tr>
</tbody>
</table>
OUTPUT WAVELENGTH ($\mu$)

\[ \lambda_\perp(\mu) \]

MIXING IN AgGaSe$_2$

$\lambda = 3.4 \text{ mm}$
$\theta = 55^\circ$

$0.224 \mu$ - 24.6 cm$^{-1}$

LiNbO$_3$ TEMPERATURE

FIG. 6--Phasematching peak for mixing in AgGaSe$_2$. 
FIG. 7—Measured output wavelength for mixing 1.3\textmu{}m and a LiNbO$_3$ parametric oscillator in AgGaSe$_2$. 

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stabilization. To minimize optical components, the mixing crystals are rotated about an axis $45^\circ$ to the vertical. In this way half of the oscillator output is properly polarized for mixing. The mixed output can be selected with an InAs filter for both AgGaSe$_2$ and CdSe.

The possible methods of extending the parametric oscillator wavelength into the visible are discussed next. The conversion efficiencies are calculated for second harmonic generation in LiNbO$_3$, LiIO$_3$, and KDP. Since the oscillator covers a tuning range greater than two to one, there are no gaps in the generated sum and harmonic spectrum.

Second harmonic generation in LiNbO$_3$ phasematches for fundamental wavelengths between 1.2$\mu$m and 3.6$\mu$m. The angle tuning curve for SHG of the parametric oscillator signal and idler is shown in Fig. 5. For SHG the input polarization is ordinary and the output is extraordinary. A polarizer and filter can be used to filter the fundamental from the generated harmonic. The conversion efficiency to the harmonic equals the gain of the oscillator or

$$\frac{P_{SH}}{P_F} = \frac{1}{I}$$

where $I = 1 \text{ cm}$

$$\lambda = 2.1\mu$$

$$I = 80 \text{ MW/cm}^2$$

Thus for a crystal 2 cm in length, the second harmonic conversion is well into the nonlinear conversion limit given by $\tanh^2(\Gamma l)$. In practice, external SHG of a plane wave source results in a conversion efficiency of
between 30% - 50%. Assuming a 40% conversion efficiency, the generated SH energies are listed in Table III.

According to Fig. 4, the plane wave focusing limit applies for input energies > 1 mJ for 2 cm crystals, and > 8 mJ for 5 cm crystals. Therefore, the 10 mJ Nd:YAG pump source provides adequate parametric oscillator energy for efficient second harmonic generation.

Sum generation in LiNbO₃ against the 1.06μ pump also phasematches. In this case good efficiency is possible due to the 7 mJ and 200 mJ of 1.06μ energy available. For sum generation the conversion efficiency in the low gain limit is again \( \frac{P_{\text{SUM}}}{P_{\text{IN}}} = \left( \frac{\omega_{\text{SUM}}}{\omega_{\text{IN}}} \right)^2 \sin^2 \Gamma l \).

Since \( \Gamma l \geq 1 \) it is expected that all of the oscillator energy can be up-converted to the 0.615 → 0.82μ spectral region. In summary, the oscillator can be up-converted to a wavelength region between 0.62μ and 1.5μ with a single angle phasematched crystal of LiNbO₃. This spectral range is important since it cannot be directly reached by other tunable sources such as diode lasers or dye lasers.

For generation of shorter visible and ultraviolet wavelengths down to 3500 Å, LiIO₃ can be used as a nonlinear crystal. Figure 8 shows the phasematching angles for SHG in LiIO₃. Figure 5 shows the phasematching angles for SHG of the doubled parametric oscillator. It is informative to determine the required pump energy for high conversion efficiency in LiIO₃.
### TABLE III

Generated Second Harmonic Energies

<table>
<thead>
<tr>
<th>S.H. WAVELENGTH</th>
<th>10 mJ PUMP</th>
<th>300 mJ PUMP</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.75 µ</td>
<td>0.85</td>
<td>28.0</td>
</tr>
<tr>
<td>0.80 µ</td>
<td>0.80</td>
<td>26.0</td>
</tr>
<tr>
<td>0.90 µ</td>
<td>0.70</td>
<td>23.0</td>
</tr>
<tr>
<td>1.0 µ</td>
<td>0.60</td>
<td>20.0</td>
</tr>
<tr>
<td>1.2 µ</td>
<td>0.51</td>
<td>16.8</td>
</tr>
<tr>
<td>1.5 µ</td>
<td>0.42</td>
<td>14.0</td>
</tr>
<tr>
<td>1.7 µ</td>
<td>0.35</td>
<td>12.0</td>
</tr>
</tbody>
</table>
LiIO$_3$ DOUBLING ANGLE vs WAVELENGTH

FUNDAMENTAL WAVELENGTH ($\mu$m)

INTERNAL CRYSTAL ANGLE

FIG. 8. Measured SHG phasematching angles for LiIO$_3$. 
The conversion efficiency in LiIO$_3$ is

\[ r^2l^2 = 0.0055 \left( \frac{1 \text{MW}}{\text{cm}^2} \right) \quad l = 1 \text{ cm} \]

\[ r^2l^2 = 0.022 \left( \frac{\text{MW}}{\text{cm}^2} \right) \quad l = 1 \text{ cm} \]

For a 1 cm crystal, the walk-off limited focal area is

\[ \frac{nw^2}{2} = \frac{\pi}{16} \rho^2 l^2 \quad \rho = 0.07 \]

\[ = 10^{-3} \text{ cm}^2 \quad l = 1 \text{ cm} \]

The burn density of LiIO$_3$ is 100 MW/cm$^2$. Therefore, the conversion efficiency is

\[ r^2l^2 \left( \frac{100 \text{ MW}}{\text{cm}^2} \right) = 0.55 \quad \lambda_f = 1.5 \mu \]

and

\[ r^2l^2 \left( \frac{100 \text{ MW}}{\text{cm}^2} \right) = 2.2 \quad \lambda_f = 0.69 \mu \]

at an input power greater than 0.1 MW or an input energy greater than 2 mJ per pulse. Table III shows that the 10 mJ Nd:YAG source results in output energies near 0.8 J at the SH of the oscillator. Thus SHG
in 1 cm of LiIO\(_3\) will be limited to near 20% efficiency. For the 300 mJ pump source, adequate energy is available for efficient (~30%) SHG of the doubled parametric oscillator. The wavelength range is therefore extended to 3300 Å by two crystals of LiIO\(_3\) cut for proper angular phasematching.

Second harmonic generation in angle phasematched KDP has been considered in detail in a short unpublished note.\(^4\) The important parameters are summarized here for completeness. Figure 9 shows the phasematching angles for KDP and ADP. Wavelengths down to 2600 Å are phasematched by SHG and down to 2200 Å by sum generation of the fourth harmonic of 1.06\(\mu\) and tunable radiation near 1\(\mu\).\(^5\)

Figure 10 shows the calculated SHG efficiency in KDP for a 1 cm length crystal versus input intensity. For harmonic generation between 5200 Å and 6000 Å

\[
\frac{P_{SH}}{P_F} = 8 \times 10^{-4} \rightarrow 4 \times 10^{-3} \left(\frac{1\text{MW}}{\text{cm}^2}\right) \quad t = 1 \text{ cm}
\]

The burn density of KDP is greater than 500 MW/cm\(^2\) so that for optimum off-angle focusing given by

\[
\frac{na^2}{2} = \frac{\pi}{16} \rho^2 t^2 \quad \rho = 0.03
\]

\[
= 1.64 \times 10^{-4} \quad t = 1 \text{ cm}
\]
FIG. 9--Phasematching angles for KDP and ADP.
OPTIMUM FOCUSING IS ASSUMED SUCH THAT
\[ \frac{\pi w_0^2}{2} = \frac{\pi}{16} \rho^2 \lambda^2 \]

\[ \lambda_{eff} = 0.3 \text{ mm} \]
\[ \rho = 0.029 \text{ rad} \]

KDP CONVERSION EFFICIENCY FOR SHG

\[ \frac{P_{SH}}{P_F} = I_{l} l^2 \text{ at } I (\text{MW/cm}^2) \]
\[ l = 1 \text{ cm} \]

FIG. 10--Calculated SHG efficiency in KDP vs. pump wavelength.
the required peak power to achieve the burn density limit is

$$P_{\text{pump}} = 80 \text{ kW}$$

The conversion constant is thus

$$t^2l^2 = 0.40 \rightarrow 2.0 \quad t = 1 \text{ cm}$$

At 80 kW and 15 nsec the required pump energy is 1.2 mJ. Again, efficient conversion to the ultraviolet is possible with the 300 mJ Nd:YAG pump source. With the 10 mJ pump source sum generation against the second harmonic of the pump must be used to achieve efficient conversion.

In summary, the generation of visible and near ultraviolet is a useful extension of the efficient widely tunable infrared parametric oscillator source. The LiNbO$_3$ SHG step is expected to be near 30% efficiency for wavelengths in the 6100 Å to 1.5μ region. LiIO$_3$ can be used to extend the generated wavelengths to 3300 Å. Beyond the near ultraviolet either KDP or ADP can be used. The conversion efficiency can be increased by using sum and mixing against the harmonics of 1.06μ. The shortest wavelength that phasematches is 2200 Å in ADP reached by sum generation of the fourth harmonic of 1.06μ at 2660 Å and a tunable source near 1μ.

The 1.06μ Nd:YAG laser pumped LiNbO$_3$ parametric oscillator forms a nearly ideal primary source for widely tunable 2200 Å to 1.5μ radiation by second harmonic and sum generation, 1.5μ to 3.7μ by parametric oscillation, and 3.0μ to 27μ by phasematched mixing.
In this section we have described a unique widely tunable, high energy, pulsed, tunable coherent source. The device is based on an angle tuned 1.06μ pumped LiNbO₃ parametric oscillator whose features are described for the first time. The oscillator's basic 1.5μ to 3.7μ frequency range is extended toward the infrared by mixing in AgGaSe₂, CdSe, and LiNbO₃. It is extended to the visible and ultraviolet by second harmonic and sum frequency generation in LiNbO₃, LiIO₃, and KDP. The parametric oscillator source is conservatively estimated to be 30% efficient when pumped with a 10 mJ per pulse or 300 mJ per pulse Nd:YAG laser. Similarly, the following mixing and sum generation steps are also shown to be near 30% efficient. The parametric oscillator followed by a crystal of AgGaSe₂, CdSe, and LiNbO₃ thus efficiently tunes over a spectral range between 0.62μ and 27μ. Since all processes are angle phase-matched, the tuning rate can be rapid.

The gain bandwidth of the oscillator is near 10 cm⁻¹. The oscillator can be frequency narrowed by use of two internal etalons or a birefringent crystal plus etalon. It is expected that continuous scanning with 1 cm⁻¹ resolution is possible. For higher resolution, the tuning range is approximately 1 cm⁻¹, and for single mode operation near 0.1 cm⁻¹, the oscillator cavity free spectral range. The use of continuous helium-neon lasers for frequency stabilization is described, as are possible methods of convenient frequency measurement.

The combination of wide tuning range at high pulse energies is a unique feature of the tunable coherent source described in this paper. At this time, no other single device approaches these features. In
addition, the Nd:YAG pump laser and all optical and nonlinear optical elements operate at or slightly above room temperature and have no inherent properties that limit the useful operating life with the exception of the flashlamps used to pump the Nd:YAG laser and amplifier. Based on present lifetime data, the flashlamps last to $10^7$ pulses or over 100 days of continuous operation at 10 pps. Thus in addition to its unique spectral properties, the system described here has inherently long operational life with minimum required maintenance.
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5. R. L. Byer, "SHG in KDP and ADP".

6. R. L. Herbst, "Sum Generation in ADP".

- 31 -
III. GENERATION OF VACUUM ULTRAVIOLET AND SOFT X-RAY RADIATION

During the past report period the following work has been achieved on this project: (a) we have successfully generated the shortest coherent radiation to date at 887 Å via third harmonic generation of 2660 Å radiation in argon; (b) we have developed a theory on higher-order polarizabilities; and (c) we have proposed an experiment for the generation of radiation below 300 Å.

A schematic of the experimental set-up for generating 887 Å radiation is shown in Fig. 1. A single 30 psec wide pulse is switched out of a train of mode-locked Nd:YAG laser pulses and is frequency doubled twice in successive KDP crystals to 2660 Å. The available power at 2660 Å is \( \sim 5 \times 10^7 \) watts peak. This radiation is focused to a spot size of 35 µm in diameter at the output end of the gas cell. The nonlinear media was Ar at a pressure of 20 Torr. Since no window material is transparent at this wavelength, differential pumping was used between the cell exit and the entrance to the VUV spectrometer. Detection was done with a Xe ionization chamber. At an incident power density of \( 10^{13} \text{ W/cm}^2 \), the observed conversion efficiency was only \( 10^{-7} \) and the signal was too low to allow a determination of whether Ar is positively or negatively dispersive for this process.
FIG. 1--Experimental set-up for generation of 887 Å radiation.
To extend nonlinear optical techniques into the soft x-ray region, we considered the use of higher-order nonlinear optical polarization which might allow fifth, seventh, or higher order harmonic generation. We used the density matrix approach to examine the relative magnitude of higher-order polarizations subject to the condition that the applied electric field strength does not exceed the multi-photon absorption or ionization limit. Analysis shows that if the generated frequency is sufficiently close to an upper level of the atom that this level determines both the coherence length and also the multi-photon absorption limit on the incident applied intensity, then the conversion efficiency is independent of the order of the nonlinear optical polarizability employed, and also of the oscillator strengths and positions of the intermediate levels. If intermediate levels have smaller oscillator strengths or resonant denominators, the incident applied field is allowed to increase to yield the same conversion efficiency. Calculations are performed for harmonic generation in Xe and Li$^+$ and are shown in Table I. From this table we see that higher-order polarizations may equal or exceed lower order polarizations. The results of these calculations along with the analysis are published in Physical Review Letters, and is included as Appendix C of this report. Recently the fifth order processes $5 \times 5320 \, \AA \rightarrow 1064 \, \AA$ and $h \times 5320 \, \AA + 1.06 \mu \rightarrow 1182 \, \AA$ have been demonstrated experimentally in xenon. The experimental conversion efficiencies are low compared to theoretical predictions. However, for theory to hold, the media must be negatively dispersive and the applied power density must be approaching the multi-photon absorption or ionization limit. These
CONVERSION EFFICIENCY AND LIMITING POWER DENSITY

<table>
<thead>
<tr>
<th>Process</th>
<th>Specie</th>
<th>( (P/A)_{\text{max}} ) (W/cm(^2))</th>
<th>Efficiency (Percent)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( 3 \times 5320 \text{ \AA} \rightarrow 1773 \text{ \AA} )</td>
<td>Xe</td>
<td>( 1.9 \times 10^{12} )</td>
<td>( .08 )</td>
</tr>
<tr>
<td>( 5 \times 5320 \text{ \AA} \rightarrow 1064 \text{ \AA} )</td>
<td>Xe</td>
<td>( 1.9 \times 10^{12} )</td>
<td>( .05 )</td>
</tr>
<tr>
<td>( 5 \times 1142 \text{ \AA} \rightarrow 236 \text{ \AA} )</td>
<td>Li(^+)</td>
<td>( 1.7 \times 10^{15} )</td>
<td>( .002 )</td>
</tr>
<tr>
<td>( 7 \times 1182 \text{ \AA} \rightarrow 169 \text{ \AA} )</td>
<td>Li(^+)</td>
<td>( 1.7 \times 10^{15} )</td>
<td>( .004 )</td>
</tr>
<tr>
<td>( 15 \times 2660 \text{ \AA} \rightarrow 177 \text{ \AA} )</td>
<td>Li(^+)</td>
<td>( 3.5 \times 10^{15} )</td>
<td>( 4 \times 10^{-7} )</td>
</tr>
</tbody>
</table>

TABLE I--Limiting power density and conversion efficiency for some higher-order nonlinear process.
conditions may not be satisfied in those early experiments. More rigorous experiments including a better choice of the nonlinear media and addition of electrodes in the gas cell to determine degree of ionization will be conducted in the near future.

Based on the theory on higher-order polarizabilities, we have proposed a new experiment for generating radiation shorter than 300 Å.

The $2p^5(^2P_1^0) 6s$ level of Na$^+$ at 274 Å is 1.2 Å (1581 cm$^{-1}$) below the 39th harmonic of 1.06μ at 272.8 Å. Thus the fifth order process

$$4 \times 1182 \, \text{Å} + 3547 \, \text{Å} \rightarrow 272.8 \, \text{Å}$$

will be negatively dispersive. Estimates show that if the 1182 Å radiation is focused to a density of $1.2 \times 10^{14}$ W/cm$^2$, then in one coherence length the conversion efficiency from 3547 Å radiation to 272.8 Å radiation will be $2 \times 10^{-4}$. Thus with $10^8$ watts peak at 1182 Å and a singly ionized sodium density of $10^{17}$ ions/cm$^3$, $10^8$ photons will be generated corresponding to a peak power of about 150 W at 272.8 Å. Experimentally, ionization of sodium will be accomplished by the incident 1182 Å laser pulse. At ion densities of $10^{17}$ ions/cm$^3$, recombination times are several nanoseconds and avalanche breakdown power densities are in excess of $10^{15}$ W/cm$^2$.

The uncertainties involved with this experiment include the validity of the higher-order polarizabilities theory, the coherence of the radiation generated by atoms spaced more than one wavelength apart, and the ability to maintain a column of singly ionized vapor. These problems will be studied during the coming quarter along with the construction of a miniature sodium heat-pipe oven and generation of high power 1182 Å radiation in a mixture of xenon and argon.
Work on this project is jointly supported by the Office of Naval Research and the U.S. Air Force Cambridge Research Laboratories.
APPENDIX A

SECOND HARMONIC GENERATION AND INFRARED MIXING IN AgGaSe₂

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SECOND HARMONIC GENERATION AND INFRARED MIXING IN AgGaSe₂


ABSTRACT

We have continuously tuned between 7 µm and 15 µm by mixing the output of a LiNbO₃ parametric oscillator in the chalcopyrite AgGaSe₂. We have doubled a CO₂ laser with 2.7% efficiency which agrees very well with the expected efficiency and verifies the high optical quality of the 1.53 cm long AgGaSe₂ crystal. The measured transparency range, indices of refraction, and nonlinear coefficient of $d_{36} = 38 \times 10^{-12}$ m/V show that AgGaSe₂ is a useful infrared nonlinear material phase-matchable over the entire 3 µm to 18 µm infrared region.
SECOND HARMONIC GENERATION AND INFRARED MIXING IN AgGaSe$_2$

Since the first demonstration of phasematched second harmonic generation (SHG) in AgGaSe$_2$, the nonlinear properties of the ternary semiconductors with chalcopyrite structure have been widely studied.\textsuperscript{2-6} Their large nonlinear susceptibilities together with adequate birefringence to achieve phasematching make them attractive for nonlinear optical devices. Nonlinear mixing has been demonstrated in ZnGeP$_2$, AgGaSe$_2$, CdGeAs$_2$ and recently AgGaSe$_2$.\textsuperscript{11,12}

AgGaSe$_2$ single crystals are grown by the vertical Bridgemen method after the starting materials are presynthesized in an amorphous carbon boat contained in a sealed quartz crucible. The presynthesized stoichiometric mix with a melting point of approximately 860$^\circ$C is then transferred to a quartz crucible heavily coated with pyrolytic carbon for a pre-growth run at 2 mm per hour rate through a 40$^\circ$C/cm temperature gradient. The top and bottom of the resulting boule are then removed prior to the actual growth run which takes place in the same vertical furnace but at a slower growth rate of 0.2 mm per hour. After growth the crucible is cooled to room temperature at 25$^\circ$C per hour. The resulting 14 mm diameter single crystals typically show a gallium rich region near the seed end followed by approximately a 2 cm useful AgGaSe$_2$ single crystal region and a silver rich top section. Early crystals showed a precipitate which resulted in a 2 cm$^{-1}$ scatter loss. In recent crystals the scatter loss has been significantly reduced with a corresponding reduction in loss to near 0.04 cm$^{-1}$. All crystals have high resistivity and good optical transparency from the bandgap at 0.71 $\mu$m to the two phonon absorption edge at 18 $\mu$m. A particularly attractive feature of AgGaSe$_2$ is the ease with which single crystals can be grown.
We have measured the nonlinear coefficient of AgGaSe$_2$ relative to GaAs at 10.6 $\mu$m. Two methods used for relative nonlinear coefficient measurement are the Maker fringe method$^{13}$ and the wedge technique.$^{14,15,6}$

In both cases, the second harmonic power in the weak focusing low loss limit is given by

$$P(2\omega) = K \left[ \frac{d_{\text{eff}} \, t_2 \, t_1^2 \, E^2}{n_\omega^2 - n_{2\omega}^2} \right]^2 \left[ 1 - F \left( \frac{\pi}{\ell_c(\theta)} \right) \cos \left( \frac{\pi \ell}{\ell_c(\theta)} \right) \right]$$

(1)

where $K$ is a constant, $P(2\omega)$ is the second harmonic power, $d_{\text{eff}}$ is the effective nonlinear coefficient, $t_1$ and $t_2$ are the crystal transmittances at the fundamental and harmonic, $E$ is the fundamental field, and $F(x) = 2J_1(x)$ is a visibility factor with $\Lambda = w_0 \tan \alpha$, where $w_0$ is the fundamental spot size. Here $\alpha$ is the wedge apex angle and $\ell$ the sample thickness and it is assumed that the fundamental beam is incident normal to the input face of the wedge. The Maker fringe method is useful for low index materials with large birefringence. The wedge method is suited for small birefringence large index materials. For the wedge method the coherence length is given by

$$\ell_c = \frac{\lambda}{4(n_{2\omega} - n_\omega)} = \frac{\lambda}{2} \Delta y \tan \alpha$$

(2)

where $\Delta y$ is the wedge translation distance between SHG extrema. For our crystal samples the coherence lengths are expected to be near 100 $\mu$m for GaAs and 200 $\mu$m for AgGaSe$_2$ at 10.6 $\mu$m.

We used a (001) oriented AgGaSe$_2$ wedge for the nonlinear susceptibility measurement relative to two GaAs reference samples. GaAs material supplied by Coherent Radiation Laboratories was cut in a (001) direction, and (111) oriented wedge was cut from Monsanto material. Both GaAs samples were
chromium compensated to a high resistivity of about $10^7 \, \Omega \, \text{cm}$. With the
laser polarization parallel to the (110) direction, $E_x = E_y = E_o / \sqrt{2}$
and $P = P_z = d_{36} E_o^2$ so the $d_{\text{eff}}$ for the (001) cut AgGaSe$_2$
and GaAs samples are $d_{36}$ and $d_{36} = d_{14}$ respectively. For the (111)
cut GaAs, with the laser polarization along (111) direction,
$E_x = E_y = E_z = E_o / \sqrt{3}$, and so $P = 2/\sqrt{3} d_{14} E_o^2$ and the $d_{\text{eff}}$ in
this case is $2/\sqrt{3} d_{14}$. A summary of the parameters are given in
Table I. The coherence length of GaAs is measured to be $107 \pm 2 \, \mu m$
and $109 \pm 3 \, \mu m$ for the (001) and (111) cut samples. This is in
excellent agreement with published values in references 18 and 19 of
$107 \pm 5 \, \mu m$ and $107 \pm 1 \, \mu m$. The measured coherence length of AgGaSe$_2$
is $237 \pm 15 \, \mu m$. This compares favorably with a calculated value of
$255 \pm 50 \, \mu m$, based on Boyd et al.'s index data with an assumed accuracy
of the third decimal place in the index. For the analysis we used an
extension of Eq. (1) given in reference 19 which includes a factor due to
crystal loss. The AgGaSe$_2$ nonlinear coefficient measured relative to GaAs
is
$$R_{001} = \frac{d_{36}(\text{AgGaSe}_2)}{d_{14}(\text{GaAs})} = 0.33 \pm 2\%$$
and
$$R_{111} = \frac{d_{36}(\text{AgGaSe}_2)}{d_{14}(\text{GaAs})} = 0.32 \pm 18\%$$

These values are in good agreement with Boyd et al.'s value of $0.37 \pm 10\%$
and with Kildal's recent measurement. With $d_{14}(\text{GaAs}) = 117 \times 10^{-12} \, \text{m/V}$
and using the average of the two ratios we obtain $d_{36}(\text{AgGaSe}_2) = 38 \times 10^{-12} \, \text{m/V}$. 
**TABLE I**

Measurement of AgGaSe$_2$ SHG Nonlinear Coefficient

<table>
<thead>
<tr>
<th>Crystal Orientation</th>
<th>GaAs (001)</th>
<th>GaAs (111)</th>
<th>AgGaSe$_2$ (001)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wedge Angle</td>
<td>$11^\circ;13'$</td>
<td>$16^\circ;2'$</td>
<td>$15^\circ;53'$</td>
</tr>
<tr>
<td>$d_{\text{eff}}$</td>
<td>$d_{14}$</td>
<td>$2\sqrt{3}d_{14}$</td>
<td>$d_{36}$</td>
</tr>
<tr>
<td>$\alpha_1$</td>
<td>0.2 cm$^{-1}$</td>
<td>0.2 cm$^{-1}$</td>
<td>2 cm$^{-1}$</td>
</tr>
<tr>
<td>$\alpha_2$</td>
<td>0.3 cm$^{-1}$</td>
<td>0.3 cm$^{-1}$</td>
<td>3 cm$^{-1}$</td>
</tr>
<tr>
<td>$\lambda_c$ (µm) measured</td>
<td>$107 \pm 2$</td>
<td>$109 \pm 3$</td>
<td>$237 \pm 15$</td>
</tr>
<tr>
<td>$R = \frac{d_{36}(\text{AgGaSe}<em>2)}{d</em>{14}(\text{GaAs})}$</td>
<td>1</td>
<td>1</td>
<td>$0.33 \pm 25%$</td>
</tr>
</tbody>
</table>

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We have also performed phase-matched SHG of 10.6 μ using a 60° cut AgGaSe₂ crystal. The measured phase-matching angle of 57.5° ± 0.5° is in good agreement with the calculated value of 55° ± 0°. The expected phase-matched SHG conversion efficiency is

\[ \frac{P_{2\omega}}{P_{\omega}} = r^2 l^2 = \left( \frac{2\omega^2 \epsilon_{\text{eff}}}{\pi n_2^2 n_2 \epsilon_0 c^3} \right) P_{\omega} l k \omega h(B, \xi) \]  

where the powers are defined inside the crystal, \( \epsilon_{\text{eff}} = d_{36} \sin \theta_m \), \( l \) is the crystal length, \( k = 2\pi n_\omega/\lambda \), and \( h(B, \xi) \) is the Boyd and Kleinman focusing factor which reduces to \( l/b = l/\omega_0^2 k \) in the loose focusing limit.

For a low loss AgGaSe₂ crystal 1 cm in length in the loose focusing limit \((l/b < 1)\) the calculated SHG conversion efficiency is \( r^2 l^2 = 0.75\% \) at 1 MW/cm². Using a TEA CO₂ laser operating in a TEM₀₀ mode as a source, we measured the absolute SHG efficiency generated in a high quality 1.54 cm long AgGaSe₂ crystal. The average input and output powers measured with an Eppley thermopile were 2.82 mW and 76 μW, which corresponds to 1.6 kW and 44 W of peak power at the fundamental and second harmonic. The experimentally observed conversion efficiency for the incident intensity of 1.68 MW/cm² is 2.68%. Using \( d_{36} = 38 \times 10^{-12} \text{ m/V} \), \( l = 1.54 \text{ cm} \) and \( h(B, \xi) = 0.925 \frac{l}{b} \) which corresponds to the focal spot size of 250 μ, the expected conversion efficiency is 2.76%. This measurement can be considered as a separate absolute determination of the nonlinear coefficient of AgGaSe₂. The nonlinear coefficient is found to be

\[ d_{36} = 40 \pm 1 \times 10^{-12} \text{ m/V} \]
which agrees very well with the previous measurement made relative to GeAs.

AgGaSe₂ phasematches for SHG for fundamental wavelengths between 3 μ and 13 μ. The SHG efficiency of AgGaSe₂ is significantly better than proustite, for example, due to both a factor of three increase in the nonlinear coefficient and the small birefringence which allows increased interaction lengths without aperture length limitations.

AgGaSe₂ has adequate birefringence to phasematch over an extended infrared spectral range for tunable wavelength generation by mixing. For mixing a convenient tunable pump source is a LiNbO₃ parametric oscillator mixing against fixed frequency Nd:YAG laser. For our experiment we used a collinear geometry. The acoustic Q-switched Nd:YAG laser tuned to 1.32 μ is internally doubled with a LiIO₃ crystal to generate 0.659 μ which pumps the temperature tuned LiNbO₃ oscillator. The oscillator output in the 1.5 - 1.7 μ range mixes with the remaining collinear 1.32 μ beam in the AgGaSe₂ crystal. The AgGaSe₂ is angle phasematched by rotation on a geared stage.

The mixing efficiency is given by

\[
\frac{P_{IR}}{P_{osc}} = \left( \frac{\omega_{IR}^2 \omega_{eff}^2 L^2}{\pi n_p n_{osc} n_{IR} c^3 \epsilon_0} \right)^{1/4} \frac{P_p}{P_{osc}} \sin^2 \left( \frac{\Delta k L}{2} \right)
\]

where the pump wavelength is 1.32 μ, \( A = \pi/2 \left( \omega_{osc}^2 + \omega_p^2 \right) \) and \( \theta_m \) is the phasematching angle. For a 1 cm AgGaSe₂ crystal at a pump intensity of 1 MW/cm² at 1.32 μ, the conversion efficiency is \( P_{IR}/P_{osc} = 1.2\% \left( \omega_{IR}/\omega_{osc} \right) \).

Figure 1 shows the generated mixed output from 7 μ to 15 μ. Beyond 15 μ our HgCdTe detector is response limited. Figure 2 shows the phasematching peak generated by mixing in a fixed AgGaSe₂ crystal by a tunable LiNbO₃.
oscillator pump. The characteristic \( \text{sinc}^2 \left( \frac{\Delta k}{2} \right) \) phasematching peakwidth agrees with that calculated from the dispersion of AgGaSe\(_2\).

A plot of the phasematching angle vs LiNbO\(_3\) oven temperature showed a nearly linear relation over a wide 7 \( \mu \) to 12 \( \mu \) spectral range. We therefore used a stepping motor and synchronously rotated the AgGaSe\(_2\) crystal to phasematch with a 1\( ^\circ \)C per minute temperature scanned LiNbO\(_3\) parametric oscillator. In this way the spectrum between 7 \( \mu \) and 12 \( \mu \) was continuously tuned in eight minutes. The output bandwidth of this coherent source is 2 cm\(^{-1}\) which is determined by the parametric oscillator's 2 cm\(^{-1}\) gain bandwidth.

Figure 3 shows a spectrum of polystyrene as an example of the continuous scanning capability of this source. The spectrum was taken using a dual channel differential boxcar with two HgCdTe detectors. The mixed output is detected with better than a 30 db signal to noise ratio with a peak to peak variation of less than 10\% at a repetition rate between 10 - 25 pps.

When mixing against 1.32 \( \mu \), AgGaSe\(_2\) does not have adequate birefringence to phasematch at wavelengths shorter than 7 \( \mu \). Based on phasematching calculations with the aid of Boyd et al's., index of refraction data, mixing against wavelengths 1.5 \( \mu \) and longer allow complete coverage of the infrared. As an example, a 1.06 \( \mu \) pumped LiNbO\(_3\) parametric oscillator with degeneracy near 2.12 \( \mu \) angle tunes over a 1.5 \( \mu \) to 3.7 \( \mu \) range. AgGaSe\(_2\) phasematches for mixing the signal and idler waves to generate 3 \( \mu \) to 18 \( \mu \) for phasematching angles between 80\(^\circ\) and 50\(^\circ\). This example shows the unique phasematching properties of AgGaSe\(_2\) for extended infrared generation by mixing.
In conclusion, we have measured the nonlinear coefficient of AgGaSe$_2$ and demonstrated phasematched SHG of a CO$_2$ laser as a verification of crystal quality and potential use as a second harmonic generator. Using a LiNbO$_3$ parametric oscillator as source, we have generated continuously tunable output between 7 µ and 15 µ by mixing in AgGaSe$_2$. This experiment demonstrates the useful phasematching and nonlinear properties of AgGaSe$_2$ for infrared generation.

ACKNOWLEDGEMENT

We wish to acknowledge the assistance of Dr. R. Route and R. Raymaker for growth of the AgGaSe$_2$ crystals.

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FIGURE CAPTIONS

1. The 7 μ to 15 μ mixing output in angle phasematched AgGaSe$_2$ pumped by a 1.318 μ Nd:YAG laser mixing with a .659 μ pumped LiNbO$_3$ parametric oscillator.

2. Phasematched mixing peak generated in AgGaSe$_2$ held at a fixed angle.

3. The spectrum of polystyrene taken with the AgGaSe$_2$ mixer (top) and Perkin Elmer Spectrophotometer (bottom).
AgGaSe$_2$

MEASURED TUNING CURVE

$\lambda_p = 1.318 \mu$

$\lambda_s (\mu)$

$\lambda_x (\mu)$

$\theta$ (deg)

- 13 -
In “M...”,

**POWER**

**OUTPUT WAVELENGTH (μ)**

- 8.68
- 9.10
- 9.52
- 10.07
- 10.81

**MIXING IN AgGaSe₂**

- $l = 3.4 \text{ mm}$
- $θ = 55°$

**24.6 cm⁻¹**

**LIPO₃ TEMPERATURE**

- 370
- 369
- 368
- 367
- 366
POLYSTYRENE SPECTRUM
0.05 mm

(a)

(b)

WAVELENGTH (μ)

100 %
AgGaSe$_2$

MEASURED TUNING CURVE

$\lambda_p = 1.318 \mu$

$\lambda_s(\mu)$

$\lambda_s(\mu)$

$\theta$ (deg)

- 55° CUT CRYSTAL
- 75° CUT CRYSTAL

DETECTOR LIMIT
AgGaSe$_2$

MEASURED TUNING CURVE

$\lambda_p = 1.318 \mu$

$\lambda_x(\mu)$

$\lambda_s(\mu)$

$\theta$ (deg)

- 55° CUT CRYSTAL
- 75° CUT CRYSTAL
APPENDIX B

PARAMETRIC OSCILLATORS
by
Robert L. Byer
for
Laser Spectroscopy Conference
Vale, Colorado, June 1973

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PARAMETRIC OSCILLATORS

I. INTRODUCTION

Parametric oscillators and parametric mixing and sum generation devices offer the widest tuning range of known coherent sources. This paper reviews the present state of parametric devices with a bias toward their use in spectroscopy. In addition to tuning range, bandwidth and bandwidth narrowing methods are considered. The discussion includes the properties of new infrared nonlinear materials that permit parametric tuning over the entire infrared spectrum. Finally, application of parametric oscillators to spectroscopy is illustrated and predictions of future tuning range and output performance is discussed.

LiNbO$_3$ optical parametric oscillators are now in wide use. The properties of parametric oscillators have been reviewed by Harris$^1$ and recently by Smith$^2$ and Byer.$^3$ Parametric oscillator sources cover a spectral range from 0.4 $\mu$m to 0.8 $\mu$m with ADP$^4$, 0.6 $\mu$m to 3.5 $\mu$m with LiNbO$_3$$^5$, 2 $\mu$m and 9.6 $\mu$m to 11 $\mu$m in CdSe$^6$ and 1.22 $\mu$m to 8.5 $\mu$m with proustite.$^7$ LiNbO$_3$ is the best developed parametric oscillator and is the only oscillator available commercially.

If we include mixing and sum generation in our general definition of parametric sources, then these three frequency processes satisfy the energy and momentum conservation conditions

\[ \omega_3 = \omega_2 + \omega_1 \]  \hspace{1cm} (1)

\[ k_3 = k_2 + k_1 \]  \hspace{1cm} (2)
The interaction takes place in the nonlinear material with a gain or conversion efficiency given by

\[ G = r^2 l^2 = \left( \frac{2 \omega_0^2 d^2}{\pi n_0^2 n_3 c} \right) P_{30} \ell k_0 (1 - \delta^2)^2 \bar{h}(B, g) \]  

(3)

where \( \omega_0 \) is the degenerate angular frequency, \( d \) is the nonlinear coefficient in mks units

\[ d(n) = \left( \frac{3 	imes 10^4}{4 \pi} \right) \text{cm/statvolt} \]

\( P_{30} \) is the pump power, \( \ell \) the crystal length,

\[ k_0 = \frac{2\pi n_0}{\lambda_0} \]  

(4)

and

\[ (1 - \delta^2) = \omega_1 \omega_2 / \omega_0^2 \]  

(5)

is the degeneracy factor, and \( \bar{h}(B, g) \) is the Boyd and Kleinman focusing factor.

For parametric oscillators and mixing experiments, the gain reduces to

\[ G(\ell) = r^2 l^2 \text{sinc}^2 \left( \frac{\delta k \ell}{2} \right) \]  

(6)

in the low gain limit and to

\[ G(\ell) = \frac{1}{4} \exp 2P \ell \]  

(7)
in the high gain limit. Here \( \text{sinc}^2(\Delta k l/2) \) is the phase mismatch factor which leads to an expression for the bandwidth of the interaction. For sum generation the conversion efficiency is the same in the low conversion limit but varies as \( \sin^2 \pi \ell \) in the high conversion limit.

Equation (3) shows that focusing determines the mixing conversion efficiency and parametric gain through the focusing parameter \( h(B, \xi) \) which describes coupling between gaussian modes as a function of the double refraction parameter

\[
B = \frac{1}{2} \rho (\ell k_o)^{\frac{1}{3}}
\]

(8)

and the focusing parameter

\[
\xi = \ell/b
\]

(9)

where the confocal parameter

\[
b = \frac{W_0^2 k_o}{2\pi n_o} = \frac{W_0^2}{\lambda_o}
\]

(10)

Here \( W_0 \) is the gaussian beam electric field radius such that the power in the gaussian beam is related to the peak intensity by

\[
P = I_o (\pi W_0^2/2)
\]

(11)

The double refraction parameter is a function of the double refraction
angle \( \rho \) given by
\[
\tan \rho = \frac{n^2}{2} \left[ \frac{1}{n^e(s)^2} - \frac{1}{(n^o)^2} \right] \sin 2\theta
\] (12)

where \( \theta \) is the propagation direction with respect to the optic axis and we have assumed \( n^e < n^o \) or a negative uniaxial crystal.

In terms of the aperture length
\[
\ell_a = \frac{W_0 \sqrt{\pi}}{\rho}
\] (13)

the double refraction parameter can be written as
\[
B = \frac{\sqrt{\pi}}{2} \frac{\ell}{\ell_a} \xi^{-\frac{1}{2}}
\] (14)

For parametric interactions \( \bar{h}(B, F) \) can usually be approximated by one of its limiting forms. In the near field approximation with negligible double refraction
\[
\bar{h}(B, \xi) \rightarrow \xi \cdot \left( \xi < 0.4 \, , \, \xi < \frac{1}{6B^2} \right)
\] (15)

For confocal focusing where \( \xi = 1 \)
\[
\bar{h}(0,1) \rightarrow 1
\] (16)

which corresponds to the near field focusing limit first discussed by Boyd and Ashkin\(^8\). In fact, the maximum value of \( \bar{h}(B, \xi) = \bar{h}_{mm}(0,2.84) = 1.068 \) for \( \xi = 2.84 \) instead of \( \xi = 1 \). However, practical considerations usually limit focusing such that \( \xi < 1 \).
When double refraction is important the gain reduction factor is closely approximated by the expression\(^9\)

\[
\bar{h}_{mm}(B) \approx \frac{1}{1 + \left(\frac{4B^2}{\pi}\right)}
\]  

(17)

which can be rewritten as

\[
\bar{h}_{mm}(B) \approx \frac{1}{1 + \left(\frac{l}{l_{\text{eff}}}\right)}
\]  

(18)

where the effective interaction length is given by

\[
l_{\text{eff}} = \frac{\lambda_0}{2 n_0 \rho^2}
\]  

(19)

In the limit of strong double refraction where \(l/l_{\text{eff}} > 1\) the focusing parameter becomes

\[
\bar{h}_{mm}(B) \rightarrow \frac{l_{\text{eff}}}{l} \quad \left(B^2/4 > \xi > 2/B^2\right)
\]  

(20)

so that the conversion efficiency as a function of input power is independent of crystal length. In addition, large double refraction maintains \(\bar{h}_{mm}(B)\) constant over a wide range of \(\xi\). Thus to minimize crystal damage problems \(\xi\) can be chosen at the least value consistent with maximum \(\bar{h}_{mm}(B)\). This value is given by

\[
\xi > \frac{2}{B^2}
\]  

(21)

which yields a corresponding focal spot size

\[
W_0 \leq \frac{1}{2\sqrt{2}} \rho l
\]  

(22)
and corresponding area

\[ \pi \frac{w^2}{2} \leq \frac{\pi}{16} \rho^2 \ell^2 \]  \hspace{1cm} (23)

Double refraction due to non-collinear phasematching results in a serious reduction of \( \rho^2 \ell^2 \) for power limited pump conditions. For example, for LiNbO\(_3\) at room temperature, phasematched at \( \theta = 43^\circ \) for a 1.06 \( \mu \)m pump source, \( \rho = 0.037 \) radians and \( B = 4.7 \ell^\frac{1}{2} \). The gain is reduced by \( \pi/4B^2 = \ell/\ell_{\text{eff}} \) which in this case is 28 times for a 1 cm crystal and 140 times for a 5 cm crystal compared to the 90\(^\circ\) phasematched case. For this case \( \ell_{\text{eff}} \) is only .36 mm and \( \xi \) can vary between 5.5 > \( \xi \) > 0.09 without affecting the gain. This corresponds to a confocal parameter variation between 11 cm and .2 cm. For experimental ease and minimum incident intensity at the LiNbO\(_3\) crystal the 11 cm confocal focusing would be used. The pump intensity varies as \( \ell^2 \) in agreement with Eq. (23).

For high power pumping conditions where more than adequate pump power is available, the minimum focal area may be dictated by the crystal damage intensity. Most semiconductor materials show surface damage at near 1J/cm\(^2\). For other nonlinear materials this energy density may approach 4J/cm\(^2\). For focusing determined by incident pump energy density with areas larger than that given in Eq. (23), the double refraction gain reduction is correspondingly smaller. In this case, 90\(^\circ\) phasematching maintains only the advantages of larger pump acceptance single and larger effective nonlinear coefficient.
Table I lists selected nonlinear materials and their properties of interest in parametric interactions. Of particular interest for infrared generation is LiNbO$_3$ proustite, CdSe and the four chalcopyrite crystals AgGaS$_2$, AgGaSe$_2$, ZnGeP$_2$ and CdGeAs$_2$. The characteristics of tunable sources based on these materials are considered in detail by Byer.\cite{3}
<table>
<thead>
<tr>
<th>MATERIAL (point group pump wavelength)</th>
<th>$d \times 10^{12}$ (m/V)</th>
<th>$n_0$</th>
<th>$n_{-1}$</th>
<th>$\theta_m$</th>
<th>$\theta$</th>
<th>$d_{eff, 12} \times 10^{-2}$</th>
<th>$\sigma_{eff, 3} \times 10^{24}$</th>
<th>$\sigma_{p, eff}$ (cm$^2$/Watt)</th>
<th>$\sigma_{p, eff}$ (Watt/cm$^2$)</th>
<th>$I_{burn}$ (Watt/cm$^2$)</th>
<th>Transmission Range (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CdSe, $k_{2+$ (K2m)</td>
<td>$\lambda_p = 5.3$ μm</td>
<td>$d_{36} = 236$</td>
<td>3.31</td>
<td>+0.06</td>
<td>2.05</td>
<td>0.05</td>
<td>393 (d sin $\theta$</td>
<td>661</td>
<td>+4</td>
<td>$3.8 \times 10^{-4}$</td>
<td>.013</td>
</tr>
<tr>
<td>2μm, $k_{2+$ (K2m)</td>
<td>$\lambda_p = 1.83$ μm</td>
<td>$d_{36} = 73$</td>
<td>3.11</td>
<td>+0.08</td>
<td>1.59</td>
<td>0.00</td>
<td>62.2 (d sin $\theta$</td>
<td>127</td>
<td>-9</td>
<td>$1.8 \times 10^{-3}$</td>
<td>.05</td>
</tr>
<tr>
<td>AgGaSe$<em>2$, $k</em>{2+$ (K2m)</td>
<td>$\lambda_p = 1.83$ μm</td>
<td>$d_{36} = 33$</td>
<td>2.02</td>
<td>-0.32</td>
<td>1.59</td>
<td>0.01</td>
<td>27 (d sin $\theta$</td>
<td>42</td>
<td>-7</td>
<td>$5.2 \times 10^{-4}$</td>
<td>.02</td>
</tr>
<tr>
<td>CdSe, $k_{2+$ (K2m)</td>
<td>$\lambda_p = 1.83$ μm</td>
<td>$d_{31} = 15$</td>
<td>2.45</td>
<td>+0.09</td>
<td>90.0</td>
<td>0.00</td>
<td>57</td>
<td>2</td>
<td>1.3</td>
<td>$1.3 \times 10^{-3}$</td>
<td>.09</td>
</tr>
<tr>
<td>AgGaS$<em>2$, $k</em>{2+$ (K2m)</td>
<td>$\lambda_p = .946$ μm</td>
<td>$d_{36} = 12$</td>
<td>2.62</td>
<td>-0.04</td>
<td>1.64</td>
<td>0.17</td>
<td>10.8 (d sin $\theta$</td>
<td>9.2</td>
<td>-1</td>
<td>$2.3 \times 10^{-4}$</td>
<td>.013</td>
</tr>
</tbody>
</table>

TABLE I
Nonlinear Coefficient, Figure of Merit, and Gain for Nonlinear Crystals

---

Note: The table above provides detailed information about nonlinear coefficients, figures of merit, and gains for various nonlinear crystals. Each entry includes the material type, pump wavelength, nonlinear coefficient, figure of merit, and gain parameters.
Table I continued

<table>
<thead>
<tr>
<th>MATERIAL (point group pump wavelength)</th>
<th>$d \times 10^{12}$ (m/V)</th>
<th>$n_o/n_{ee}$</th>
<th>$n_e-n_o$</th>
<th>$\theta_o$</th>
<th>$\theta$</th>
<th>$d_{eff} \times 10^{-2}$</th>
<th>$d_{eff}^{2}/n_{e}^{2}$</th>
<th>$f(\theta)$ eff (cm)</th>
<th>$T^{2} / 1$ Watt</th>
<th>$T^{2} / 1$ M$^{2}$/cm$^{2}$</th>
<th>$I_{burn}$ (M$^{2}$/cm$^{2}$)</th>
<th>Transmission Range (\mu m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ag$_3$As$_2$ (3m) $\lambda_p = 1.06$ \mu m</td>
<td>$d_s = 11.6^c$</td>
<td>2.76</td>
<td>2.94</td>
<td>-0.223</td>
<td>0.078</td>
<td>4.0</td>
<td>8.2</td>
<td>-0.007</td>
<td>$9.0 \times 10^{-6}$</td>
<td>0.011</td>
<td>12 - 40</td>
<td>0.60 - 13</td>
</tr>
<tr>
<td>LiNbO$_3$ (3m) $\lambda_p = 532$ \mu m</td>
<td>$d_{31} = 6.25^k$</td>
<td>2.24</td>
<td>2.16</td>
<td>-0.01</td>
<td>0.0</td>
<td>$d_{31}$</td>
<td>3.38</td>
<td>$\ell = 5$ cm</td>
<td>$2.1 \times 10^{-2}$</td>
<td>1.28</td>
<td>50 - 140</td>
<td>0.35 - 4.5</td>
</tr>
<tr>
<td>ADP ($\frac{1}{2}2$m) $\lambda_p = 532$ \mu m</td>
<td>$d_{36} = 5.3^e$</td>
<td>1.93</td>
<td>1.14</td>
<td>-0.048</td>
<td>0.0</td>
<td>$d_{36}$</td>
<td>0.100</td>
<td>$\ell = 5$ cm</td>
<td>$2.9 \times 10^{-3}$</td>
<td>0.13</td>
<td>&gt; 1000</td>
<td>0.20 - 1.1</td>
</tr>
</tbody>
</table>

References to Table I:

b) Hyar et al (1971)
c) Boyd et al (1972a)
e) Boyd et al (1971a)
f) Feichtner and Roland (1972)
g) Boyd et al (1971c)
h) Herbst and Hyer (1971)
i) Boyd et al (1971c)
j) Hyer and Harris (1968)
k) Bjorkholm and Siegman (1967)
l) Francois (1966)
II. EXTENDED INFRARED TUNING

Of particular interest to spectroscopists is the extended tuning
range available from parametric devices. In addition, bandwidth and
techniques for bandwidth narrowing and ultimately single frequency oper-
ation are important.

There has been considerable progress recently in extending the tuning
range of parametric oscillators. However, to date the most reliable para-
metric oscillator uses LiNbO$_3$ at 90° phasematching with temperature tuning.
This source covers with good efficiency and operating stability the spectral
region from 0.6 μ to 3.5 μ with the second harmonic of a Q-switched Nd:YAG
laser pump source operating at .532 μ, .561 μ and .659 μ. Figure 1
shows the experimental tuning curve for the .695 μ pump wavelength. Also
shown are the wavelengths generated by internal SHG and sum generation using
LiIO$_3$. This singly resonant oscillator typically operates at 30% conversion
efficiency with a gain bandwidth of 1.5 to 2 cm$^{-1}$. Peak powers of 300 W
at average powers of 30 mW are typical operating parameters. Although
historically parametric oscillators have operated with small excess gain, the
gain of LiNbO$_3$ parametric oscillators may be so high that they may find
application as single pass parametric amplifiers. For example, recently a
single pass gain of 60 db was measured experimentally for a .695 μ pumped
LiNbO$_3$ crystal 5 cm long. The amplifier was used to amplify a 1 mW 1.15 μ
HeNe laser source to 1 kW peak power. The 1 kW output pulse represented
10% of the input pump power. As expected the amplifier showed temporal pulse
narrowing of the amplified 1.15 μ HeNe source to one third of the 60 nsec
pump pulse length. Simultaneous spatial narrowing was also observed. The
potential applications for such a high gain amplifier include amplification of
low power narrow bandwidth diode laser sources for saturation spectroscopy, and amplification of infrared sources prior to detection by dark current limited infrared detectors. Investigations along these lines is continuing.\textsuperscript{12}

Although LiNbO\textsubscript{3} is transparent to 5 \( \mu \)m parametric oscillation becomes increasingly more difficult beyond 3.5 \( \mu \)m due to decreasing gain. Recently infrared parametric oscillation has been demonstrated in CdSe\textsuperscript{6} and proustite.\textsuperscript{7,13,19} However, neither of these materials are available with adequate crystal length for convenient oscillator operation. An additional limitation to infrared oscillator operation is the lack of a "fused-silica" type mirror substrate material and high optical quality dielectric coatings. These difficulties have combined such that infrared generation by mixing appears to be the more favorable route to a widely tunable infrared source.

The output power obtained by mixing is

\[
\frac{P_1}{P_2} = \frac{a_1}{a_2} r^2 \Delta l^2 \text{sinc}^2 \left( \frac{\Delta k \ell}{2} \right)
\]

(24)

Thus, though visible dye lasers may be convenient tunable sources there are not the optimum pump source for mixing for two reasons: the reduction in mixing efficiency by the Manley-Rowe factor, and the transparency requirements in both the infrared and visible for the nonlinear material. For infrared generation by mixing, the LiNbO\textsubscript{3} parametric oscillator more closely fits the source requirements.

We have recently performed two mixing experiments to illustrate the advantages of widely tunable infrared generation by mixing. Figure 2 shows the wavelengths obtained by mixing in CdSe. The tunable pump source was two
LiNbO$_3$ oscillators operating within the same optical cavity pumped by .695 $\mu$. One crystal was tuned while the other was held fixed at 1.833 $\mu$. The mixer phasematched between 9.6 $\mu$ and 25 $\mu$. However, the detector response cut-off at 13.5 $\mu$.

CdSe is unique in that it has a wide transparency range .75 $\mu$ - 25 $\mu$ and 70 $\mu$ to submillimeter wavelengths combined with a large nonlinear coefficient and high crystal quality. The small birefringence of CdSe allows phasematched far infrared generation as shown in Fig. 3. However, the birefringence is inadequate for phasematching across the entire near infrared. For this spectral region crystals belonging to the chalcopyrite group appear particularly useful.

The nonlinear and phasematching properties of the ternary II - IV - V$_2$ and I - III - IV$_2$ chalcopyrite (4$\overline{2}$ m point group) crystals have been determined. At this time four of the thirty compounds appear particularly useful for infrared nonlinear optical applications. These crystals are AgGaS$_2$, AgGaSe$_2$, ZnGeP$_2$ and CdGeAs$_2$. The properties of these crystals including phasematching are reviewed in reference 3. Table I lists their nonlinear properties and transparency ranges. In general, the chalcopyrites have a very high nonlinearity. AgGaS$_2$ and ZnGeP$_2$ are transparent between .6 - 12 $\mu$ and .7 - 12 $\mu$ respectively.

We have concentrated our efforts on AgGaSe$_2$ and CdGeAs$_2$ due to their extended infrared transparency .7 - 18 $\mu$ and 2.3 - 18 $\mu$ and unique phasematching properties. In addition, AgGaSe$_2$ shows useful crystal growth properties and is available in reasonable quality crystals over 1 cm$^3$ in volume.
Figure 4 shows the 7 μ to 15 μ tuning range generated by mixing in AgGaSe₂. The output bandwidth was less than 2 cm⁻¹ reflecting the bandwidth of the .695 μ pumped LiNbO₃ parametric oscillator source. The unique features of this experiment were its simplicity and rapid, continuous tuning. The experimental arrangement consisted of collinear geometry with a Q-switch Nd:YAG laser operating at 1.32 μ internally doubled with LiIO₃ to generate .659 μ. The .659 μ pumped the singly resonant LiNbO₃ parametric oscillator. The oscillator output mixed in the AgGaSe₂ with the collinear 1.32 μ with phasematching achieved by proper rotation of the AgGaSe₂ crystal. Figure 5 shows a phasematching angle. The LiNbO₃ temperature scanned at 1°C/min and the AgGaSe₂ synchronously rotated to continuously tune 7.5 μ to 12 μ in 10 minutes. The scanning was repeatable with approximately a 10% peak to peak fluctuation in output pulses and a signal to noise greater than 1000 in the HgCdTe detector. A demonstration polystyrene spectrum was scanned to illustrate the repeatability of this coherent spectrometer.

The above description of tuning ranges illustrates that it is now possible with only three nonlinear crystals and a Q-switched Nd:YAG laser source to generate .6μ to 3.5 μ by parametric oscillation in LiNbO₃, 3 μ to 18 μ by mixing in AgGaSe₂ and 10 μ to 25 μ and 70 μ to 1000 μ by mixing in CdSe. The question of bandwidth and frequency control is the next important question in spectroscopic application of these sources.

III. BANDWIDTH

The gain bandwidth of a parametric oscillator is determined by the \( \text{sinc}^2 \left( \frac{\Delta k l}{2} \right) \) phasematching factor. Expanding \( \Delta k \) in terms of frequency
and letting
\[ \frac{\Delta k \ell}{2} = \pi \] (25)

define the bandwidth we have
\[ \Delta \nu \text{ (cm}^{-1}) = \frac{1}{c \beta_{12} \ell} \] (26)

where
\[ \beta_{12} = \begin{vmatrix} \delta k_1 & \delta k_2 \\ \delta a_1 & \delta a_2 \end{vmatrix} \]
\[ = \frac{1}{c} \left[ n_2 - n_1 + \lambda_1 \frac{\partial n_1}{\partial \lambda_1} - \lambda_2 \frac{\partial n_2}{\partial \lambda_2} \right] \]
\[ \approx \frac{\Delta n}{c} \] (27)

Thus the gain bandwidth is approximately given by
\[ \Delta \nu \text{ (cm}^{-1}) \sim \frac{1}{\Delta n \ell} \] (28)

where \( \Delta n \) is the crystal birefringence. Figure 6 shows the measured gain bandwidth of a .659 \( \mu \) pumped LiNbO\(_3\) singly resonant oscillator.

Similar to other coherent sources, the parametric oscillator can be frequency narrowed to oscillate in a single axial mode. The frequency narrowing methods include thermally tuned etalon,\(^{21}\) tilted etalon,\(^{22}\) Smith and the duel Smith interferometer\(^{23}\) and birefringent filter.\(^{24}\) The first
three methods have been demonstrated with good results. For example, Wallace \textsuperscript{21} reports that a .92 cm\(^{-1}\) free spectral range, finesse of 7.8, thermally tuned etalon effectively controls the oscillator bandwidth to a single axial mode with long term frequency stability of 30 MHz or 0.001 cm\(^{-1}\). The commercial LiNbO\(_3\) parametric oscillator is available with this frequency control option and has been used in a series of experiments.\textsuperscript{26} The use of a thermally tuned etalon is dictated by the small parametric oscillator cavity spot size which does not permit tilted etalon use.\textsuperscript{27} The disadvantage of the thermal etalon is the slow thermal time constant and difficulty in stabilizing the etalon at the frequency of interest.

These thermally tuned etalon difficulties can be overcome by using a beam expanding telescope within the oscillator cavity to permit the use of a tilted etalon. Recently experiments were performed to demonstrate this frequency narrowing method.\textsuperscript{22} Figure 7 shows a schematic of refractive and reflective beam expanding telescopes. These telescopes used inexpensive Edmonds optics but operated satisfactorily to expand the beam from 100 \(\mu\) to 600 \(\mu\). Figure 8 shows the tuning capability achieved with a 2.85 cm\(^{-1}\) free spectral range, finesse of four tilted etalon. The bandwidth was less than the 0.5 cm\(^{-1}\) spectrometer resolution. Based on previous work with thermal etalons, bandwidth narrowing should be less than 0.1 cm\(^{-1}\) and approaching single frequency operation. The 2.85 cm\(^{-1}\) interval could be rapidly scanned in a convenient and repeatable manner illustrating the advantage of the tilted etalon. The use of a beam expanding telescope is required for the present confocally focused low power LiNbO\(_3\) oscillators. Operation of higher power oscillators dictates a larger oscillator cavity mode radius so that the beam expander would not be necessary.
Although birefringent elements have been proposed for use in parametric oscillators, they have not yet been demonstrated. However experiments are presently in progress and based on their hoped for positive results, a combination birefringent filter and tilted etalon may provide the most convenient frequency narrowing method for future parametric oscillator devices.

IV. APPLICATIONS TO SPECTROSCOPY

Spectroscopic applications of tunable coherent sources covers a wide range of chemical, biological and physical systems. Rather than review the range of applications to which parametric oscillators have been applied, I will briefly describe our work which is related to remote air pollution monitoring using tunable infrared sources.28,29

Using a .532 μpumped LiNbO₃ parametric oscillator operating in the 2.3 μ region, we have measured pressure broadening and absorption coefficients of the \( V'' = 0 \rightarrow V' = 2 \) CO overtone transition. Figure 9 illustrates the observed absorption spectrum taken by continuously scanning the oscillator wavelength with a resolution of 0.1 cm⁻¹. The detection system used is a dual differential boxcar integrator followed by ratio electronics.

Figure 10 shows the measured absorption coefficient and cross section vs CO pressure for the overtone transition. Similar data was taken for nitrogen pressure broadened CO up to 1 atm pressure. Extending the results to higher pressures is illustrated by Fig. 11.

Using the observed absorption spectra, the pressure broadening in CO is determined to be \( 0.62 \times 10^{-3} \) cm⁻¹ Torr⁻¹ for the \( V'' = 0 \rightarrow V' = 2 \) transition for the \( P(2) - P(4) \) rotational levels.
The above discussion illustrates just one application of parametric sources. As the tuning range, output energy and bandwidth improve a wider use of parametric devices can be expected. In particular, applications to long path spectroscopy, chemical transfer rate spectroscopy and optical pumping spectroscopy can be expected.

V. FUTURE DEVELOPMENTS

If I may speculate for a moment, I would like to describe a potential coherent infrared source that looks particularly promising. The system is based on a Nd: YAG oscillator-amplifier pump source operating Q-switched at 1.06 μ. This source is capable of 400 mJ output at up to 40 pps. Figure 12 shows the computed tuning curve for a LiNbO₃ parametric oscillator directly pumped by 1.06 μ. The output of this oscillator provides an ideal match to the phasematching properties of AgGaSe₂. Figure 13 illustrates the resulting tuning range achieved by mixing. Of particular interest from the device standpoint, is rapid tuning by crystal rotation and the requirement for only one set of mirrors reflecting between 1.6 μ and 2.1 μ for the LiNbO₃ singly resonant oscillator. These phasematching curves illustrate the potential for a high energy continuously tunable 1.6 μ to 18 μ source based on well developed Nd:YAG laser and LiNbO₃ oscillator technology.

In conclusion, parametric oscillator and mixing sources are now finding their way out of the laboratory and into an increasing number of spectroscopic applications. Their convenient operating characteristics, relatively high peak power and adequate bandwidth control coupled with a very wide tuning range assure increased future application as tunable coherent sources.
REFERENCES


20. H. Kildal, (private communication).


24. S.E. Harris, (private communication).


32. M. Yarborough, (private communication).


FIGURE CAPTIONS

1. Experimental tuning curves for a 0.659 μm pumped LiNbO₃ parametric oscillator. Also shown are the up-converted wavelengths obtained with an internal LiIO₃ crystal.

2. Measured difference output in CdSe. The tunable pump source was 2 LiNbO₃ oSRO operating within a single cavity pumped by 0.659 μm of a doubled Nd:YAG laser. One oscillator was tuned while the second was held at 1.833 μm.

3. Far infrared phasematching in CdSe.

4. 7 μ - 15 μ output in AgGaSe₂ pumped by 1.318 μ mixed against a .659 μ pumped LiNbO₃ parametric oscillator.

5. Plot of AgGaSe₂ phasematching angle vs LiNbO₃ parametric oscillator temperature showing the proper crystal rotation for 7.5 μ to 12 μ continuous tuning.

6. Measured bandwidth for a 0.659 μm pumped LiNbO₃ SRO. The calculated linewidth for the 5 cm crystal is 1.60 cm⁻¹.

7. Beam expanding telescopes to allow the use of a tilted etalon for frequency narrowing a LiNbO₃ parametric oscillator.

8. Tilted etalon tuned .659 μ pumped LiNbO₃ parametric oscillator. The etalon had a 2.85 cm⁻¹ free spectral range and a finesse of four.
9. CO overtone spectrum taken with a LiNbO$_3$ parametric oscillator at
0.1 cm$^{-1}$ resolution at a 1 m absorption path length.

10. Absorption coefficient and cross sections at peak of P(3) line in
V = 0 $\rightarrow$ V = 2 transition of CO.

11. Pressure broadening of the CO overtone transition.

12. Angle tuning curve for a 1.06 $\mu$m LiNbO$_3$ parametric oscillator.

13. 3 - 18 $\mu$m AgGaSe$_2$ mixing source pumped by a LiNbO$_3$ singly resonant
parametric oscillator.
FIGURE 1

WAVELENGTH (µm)

λ₁

λ₅

λ₁/₂

λ₅/₆

λ₅ + λ₆ (SUM)

LINBO₃ CRYSTAL TEMPERATURE (°C)
FIGURE 2

CdSe MIXING

$\lambda_p = 1.833 \mu m$
MEASURED TUNING CURVE

\( \lambda_p = 1.318 \mu \)

\( \lambda_s (\mu) \)

\( \lambda_s (\mu) \)

FIGURE 4
\[ \lambda_0 = 0.659 \, \mu \text{m} \quad 0.85 \text{ cm}^{-1} \]

\[ \lambda_s = 0.9412 \, \mu \text{m} \quad 1.55 \text{ cm}^{-1} \]

\[ \lambda_1 = 2.1988 \, \mu \text{m} \quad 1.65 \text{ cm}^{-1} \]

**FIGURE 6**
ETALON NARROWED PARAMETRIC OSCILLATOR

TELESCOPE

LiNbO₃ OVEN

(a)

(b)

FIGURE 7
ETALON TUNED OSCILLATOR

BANDWIDTH < 0.5 cm⁻¹
LIMITED BY SPECTROMETER RESOLUTION

FIGURE 8
CO OVERTONE SPECTRUM

\[ V'' = 0 \rightarrow V' = 2, 600 \text{ Torr} \]

- P BRANCH
- R BRANCH

\[ 1 \text{ cm}^{-1} \]

FIGURE 9
Cross Section \( \sigma_{\text{max}} \) (cm\(^{-2}\))

\begin{align*}
\sigma_{\text{max}} &= \frac{\alpha_{\text{max}}}{N \cdot \text{TOT}} \\
\alpha_{\text{max}} &= 10^{-2} \\
\text{CO PRESSURE IN TORR} &\leq 800 \\
\text{ABSORPTION COEFFICIENT } \alpha_{\text{max}} \text{ (cm}^{-1}\text{)} &\geq 2.0
\end{align*}
CO overtone spectrum

$V'' = 0 \rightarrow V' = 2$

100 psi

220 psi

400 psi

Figure 11
OSCILLATOR TUNING CURVE
\( \lambda_p = 1.065 \mu \)

CRYSTAL ORIENTATION -- \( \theta \)

MIRROR REFLECTION RANGE

OPTIC AXIS

LiNbO_3

\( T = 126^\circ C \)
FIGURE 13

AgGaSe$_2$ ANGLE (deg)

$\lambda_{\text{Mix}} (\mu \text{m})$

$\lambda_{\text{osc}} (\mu \text{m})$

LiNbO$_3$ ANGLE (deg) AT $T = 126^\circ C$

3-18$\mu$ AgGaSe$_2$ MIXER

SCALE CHANGE

EQUAL WAVELENGTH

MIRROR REFLECTANCE RANGE
APPENDIX C

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Generation of Vacuum-Ultraviolet and Soft—X-Ray Radiation Using High-Order Nonlinear Optical Polarizabilities*

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The harmonic or sum-frequency power generated in the last coherence length of a low-density atomic species is calculated subject to the condition that the applied electric field be bounded by the multiphoton absorption or ionization limit. It is shown that higher-order polarizations may equal or exceed lower-order polarizations. Calculations are given for generation at 1773 and 1064 Å in Xe, and at 236, 169, and 177 Å in Li*.

In recent years, picosecond-time-scale laser systems have evolved to the point where it is readily possible to produce focused optical pulses with power densities which are greater than the multiphoton ionization threshold of single atoms, and which at the same time have energy densities low enough that inverse bremsstrahlung (avalanche) ionization of the species does not occur. By using the third-order nonlinear polarizability of low-pressure xenon, and operating at peak power densities which approach the multiphoton ionization limit \( P/L \approx 5 \times 10^{12} \text{ W/cm}^2 \), picosecond laser pulses at 3547 Å have recently been used to produce third-harmonic radiation at a conversion efficiency of 3%.

In this Letter, I consider the relative magnitude of the higher-order nonlinear optical polarizabilities; i.e., \( \phi^{(3)} \cdot E^3 \), \( \phi^{(4)} \cdot E^4 \), etc.; where the applied electric field strength, \( E \), is bounded by the condition that it not exceed the multiphoton absorption or ionization limit of the atom. It is shown, for many practical systems where the electronic transition frequencies to ground are greater than the frequency of the applied laser fields, that at incident power densities which approach the multiphoton ionization limit, the higher-order polarizations may equal or exceed lower-order polarizations. There is also often a basic invariance, where the harmonic or sum-frequency power generated in the last coherence length of an atomic species is independent of the position and oscillator strengths of the intermediate levels, and of the order of the nonlinear polarizability involved. As a first experimental test of these ideas, Kung et al. have recently demonstrated the fifth-harmonic process 5320 Å — 1064 Å in low-pressure xenon. (We consider an atomic system with certain transition frequencies to ground denoted by \( \omega_{01}, \omega_{02}, \ldots, \omega_{0n} \). We assume that optical radiation at frequencies \( \omega, \omega_2, \ldots, \omega_n \) is applied to the system (for \( n \)-th harmonic generation \( \omega = \omega_1 + \omega_2 + \cdots + \omega_n \)). We assume that a single path through the atomic levels dominates the nonlinear optical susceptibility. For a gas with \( N \) atoms/cm\(^3\), the dipole moment at the sum frequency \( \omega = \omega_1 + \omega_2 + \cdots + \omega_n \) is approximately given by

\[
\phi^{(n)}(\omega) = N \frac{\mu_{01} \mu_{12} \cdots \mu_{n-1n} \mu_{nn} \cdot E(\omega_1) \cdot E(\omega_2) \cdots E(\omega_n)}{A'(\omega - \omega_0) \cdot (\omega_1 + \omega_2 - \omega_0) \cdots (\omega_n - \omega_0)}
\]

(1)

where \( \mu_{ij} \) are the dipole matrix elements connecting the various levels (0 denotes ground, and is the
only level which is populated).  We calculate the power density \( P/A(\omega_a) \) which is generated in one coherence length at the sum frequency. (The coherence length is \( L_c = \frac{\pi}{\Delta k} \), where \( \Delta k \) is the difference in the propagation vectors of the driving polarization and the free electromagnetic wave at \( \omega_s \).) Experimentally, this is the power density which will be generated when a Gaussian laser beam is focused to the center of a negatively dispersive media with a confocal parameter equal to \( L_c \). We assume that the sum frequency \( \omega_s \) is sufficiently close to \( \omega_a \), that this transition, by itself, approximately determines \( L_c \); then

\[
L_c = 2\pi(\omega_s - \omega_a)/n_w s \mu_n^2 \tag{2}
\]

where \( \eta = (\mu_e^2_{\nu})^{1/2} \). From Maxwell’s equations, the power density generated in one coherence length of atoms is \( P/A(\omega_s) = (1/2\pi^2)n_w s^2|E|^4|I_c|^2 \). Define

\[
\gamma_{\ell} = (n_w s \mu_n^2)^2, \quad \Delta \omega_{1} = \omega_a - \omega_1 - \omega_s = \ldots = \omega_{\ell}.
\]

Using Eqs. (1) and (2), the conversion efficiency from the highest applied frequency \( \omega_a \) to the sum frequency \( \omega_s \) is given by

\[
\mathcal{S} = \frac{P/A(\omega_s)}{P/A(\omega_a)} = 4\gamma_0\gamma_12 \ldots \gamma_{n-2, n-1} \frac{\mu_{n-1, n}}{\mu_{n-1, n}} \tag{3}
\]

The maximum conversion efficiency to \( \omega_a \) is determined by the maximum allowed value of \( E(\omega_a), E(\omega_1), \ldots , E(\omega_n) \). These are assumed to be limited by the \( \ell \)-th order absorption probability \( \mathcal{W}(\nu) \) which, again subject to the assumption of a single dominant path, is given by

\[
\mathcal{W}(\nu) = \frac{1}{2}\pi^2 n_w s \mu_n^2 \rho_\nu \frac{E(\omega_a)^2}{E(\omega_a)/A} \tag{4}
\]

where \( \rho_\nu \) is the density of states of the upper transition. Note that the single-photon cross section for absorption of \( \omega_s \) by the transition \( \omega_a \) is given by \( \sigma_\nu(\omega_a) = n_w s \mu_n^2 \rho_\nu / 2\pi \). Using Eq. (4), Eq. (3) may be written

\[
\mathcal{S} = \frac{\mathcal{W}(\nu)}{\sigma_\nu(\omega_a)} = \frac{\frac{\mathcal{W}(\nu)}{\sigma_\nu(\omega_a)}}{2\pi^2 n_w s \mu_n^2 \rho_\nu \frac{E(\omega_a)^2}{E(\omega_a)/A}} \tag{5}
\]

where \( \mathcal{J}(\omega_a)/A \) is the incident energy density at the highest applied frequency \( \omega_a \). The second equality in Eq. (5) follows by multiplying numerator and denominator by the length of the laser pulse, \( \Delta \nu \), and allowing the applied fields to increase until \( \mathcal{W}(\nu) \Delta \nu = \frac{1}{2} \), i.e., \( 50\% \) of the atoms are excited to the upper level. (It is assumed that \( \Delta \nu \) is shorter than the decay time of the upper level.) The quantity \( \mathcal{W}(\nu) / \omega_a \) is often termed the saturation energy density, and is that density which if incident from the outside would approximately saturate the transition.

Note that this conversion efficiency is independent of the order of the nonlinear polarizability, and also of the oscillator strengths and positions of the intermediate levels. If intermediate levels have smaller oscillator strengths or resonant denominators, the incident applied fields are allowed to increase to yield the same conversion efficiency.

The foregoing has assumed that the generated frequency \( \omega_a \) is sufficiently close to some upper level \( \omega_n \), and that this level both determines the coherence length and most severely limits the allowable incident power density. More generally, the maximum allowable power density will be determined by multiphoton absorption to some other discrete level, or, most often, by multiphoton ionization to the continuum. Eq. (3) still applies, but the maximum allowable fields are now shown to be determined by the condition that

\[
\gamma_0 \gamma_12 \ldots \gamma_{n-2, n-1} \frac{1}{8} \frac{\mathcal{W}(\nu)}{\sigma_\nu(\omega_a)} \frac{1}{v/A(\omega_a)} \tag{6}
\]

where \( q \) denotes that level or point in the continuum which most severely limits the allowable fields. The quantity \( \gamma_0 \gamma_12 \ldots \gamma_{n-2, n-1} \) is then substituted into Eq. (3) to determine the conversion efficiency. (If \( q = n \), then Eqs. (6) and (3) combine to give Eq. (5).)

Before applying the foregoing, two qualifications are in order. First, at the level of applied electric field strengths, Stark shifts may be significant. In principle, these can be included in the frequency denominators. In practice, allowing that the electric field is a free variable, the predicted conversion efficiencies are not very sensitive to the exact position of the upper atomic levels. There are also certain questions with regard to the applicability of the perturbation theory at these high field strengths. These same questions apply to multiphoton ionization theories, which experimentally have proven to be reasonably accurate.

As a first example, consider the third-harmonic process at 3547 Å - 1182 Å in xenon. To evaluate Eq. (6), I choose the four-photon path 5p\[1S\]0-6s\[1S\]|1\rangle - 6p\[1P\]|0\rangle - 7s\[1S\]|1\rangle - 2-continuum\[2S\] as that which will most severely bound the allowable incident power density. I assume unity oscillator strength for all transitions and estimate \( \sigma_{2\nu} - \text{continuum} \approx 3 \times 10^{-18} \text{ cm}^2 \). Then assuming an incident 30-psec pulse at 3547 Å yields \( P/A \approx 1.32 \times 10^{13} \text{ W/cm}^2 \). At this density, Eq. (3) predicts a conversion efficiency of 0.34\%. Experimentally, us-
ing tight focusing to the center of a xenon cell at a pressure of 3 Torr, a conversion efficiency of 0.9% has been measured.

A number of other examples of the theory are summarized in Table I. The first two are concerned with generation of vacuum ultraviolet radiation in Xe. Assuming an incident laser pulse with a peak power of 10^6 W, then to exceed the multiphoton ionization limit we must focus to a power density, In Xe. Assuming an incident laser pulse. At ion densities of 10^15 atoms/cm^3, recombination times are several nanoseconds, and each atom need be ionized only once during the incident laser pulse. Because of the tight focus, this will require only about 10^-8 of the incident pulse energy.

Even at its lower efficiency, the process 15×2660 Å-177.3 Å may be an attractive early source of coherent soft-x-ray radiation. It makes use of a fortunate coincidence with the 1s^2[1s] 0-3p[1p] 1 transition of Li+ at 178.015 Å (2160 cm^-1 below the generated frequency). As a result of longer coherence lengths in this region of the spectrum, it is almost essential that coincidences of this type be utilized. Assuming an incident peak power of 10^10 W, to attain the limiting power density, the laser must be focused to a confocal parameter = 0.43 cm. For L_c = confocal parameter, at an oscillator strength of 0.07 (equal to that of the comparable 1s-3p transition in He), this requires an ion density of 1.5×10^18 ions/cm^3. At this high density the condition on inverse bremsstrahlung ionization is close to being violated.

By using sum-frequency processes, one photon of a tunable dye laser might be utilized to allow close frequency coincidences and thus to reduce the required ion or atom density. Sum-frequency processes might also be used to inject high-power, lower-frequency radiation and thus to reduce the required power density at the highest applied frequency. Phase-matching techniques may also be used to increase the conversion efficiencies of Table I.


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### Table I. Conversion efficiency and limiting power density for some higher-order nonlinear processes.

<table>
<thead>
<tr>
<th>Process</th>
<th>Species and path</th>
<th>Limiting P/A (W/cm^2)</th>
<th>Conversion efficiency (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>3×5320 Å-1773 Å</td>
<td>Xe^+, 5p-6s-5p-6s-5p-8d-c</td>
<td>1.94×10^2</td>
<td>0.084</td>
</tr>
<tr>
<td>5×5320 Å-1064 Å</td>
<td>As above</td>
<td>As above</td>
<td>0.051</td>
</tr>
<tr>
<td>5×1182 Å-236 Å</td>
<td>Li^+, 1s-2s-1s-2p-3s-2p-3s-4p-c</td>
<td>1.68×10^3</td>
<td>0.062</td>
</tr>
<tr>
<td>7×1182 Å-169 Å</td>
<td>As above</td>
<td>As above</td>
<td>0.004</td>
</tr>
<tr>
<td>15×2660 Å-177 Å</td>
<td>Li^+, (1s-2s)-(2p-3s)-1s-3p-4d-c</td>
<td>3.47×10^3</td>
<td>4×10^-7</td>
</tr>
</tbody>
</table>

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