METHOD OF DETERMINING THE COEFFICIENT OF VISCIOUS FRICTION

by

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The author gives a method of determining the coefficient of viscous friction in hydraulic elements, based on utilization of the properties of frequency phase diagram, the method permitting measurements in actual operating conditions of the element. A measuring system for the case of a control slide value is proposed. [APi107874]
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METHOD OF DETERMINING THE COEFFICIENT OF VISCOUS FRICTION

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Abstract: A method for determining the coefficient of viscous friction in hydraulic elements is described, based on utilization of the phase frequency characteristic. This enables measurements to be made under the actual working conditions of the element. A measurement system for distributor valve is proposed.

Aim of Measurement and Some Fundamental Relationships

In hydraulic control the need frequently arises for describing the properties of dynamic elements of the types shown in Fig. 1.

![Fig. 1](image1.png)

Fig. 1. Examples of elements discussed in the article. a. Shutter; b. distributor valve.

![Fig. 2](image2.png)

Fig. 2. Two-element model.
In addition to its resemblance to the actual object, a mathematical model should have simplicity in order to facilitate its use in the analysis of the whole system. For this reason, the elements represented above are treated as linear, while the differential equations which describe their operation are limited to the second order. This means that we consider the motion of a mass elastically suspended in a viscous medium (Fig. 2). The motion equation has the form

\[ m \frac{d^2 x}{dt^2} + k_v \frac{dx}{dt} + Cx = F(t) \]  

(1)

where \( m \) is mass; \( k_v \) is substitute coefficient of viscous friction; \( C \) is rigidity of spring; \( F(t) \) is external force; \( t \) is time.

Equation (1) describes a concrete object when the constants are assigned suitable values. Difficulties arise in determining the value of coefficient \( k_v \). It can be determined on the basis of the phase frequency characteristic.

\[ \phi = \frac{k_v}{m \omega - C} \]  

(2)

where \( \phi \) is the phase shift; \( \omega \) is the pulse rate.

hence

\[ k_v = \frac{m \omega - C}{\omega} \phi \]  

(3)

If the phase angle \( \phi \) corresponding to a given pulse rate is known for known \( m \) and \( C \), the value of \( k_v \) can be determined.

Sometimes the aim of measurement is to determine the changes in \( k_v \) under changing operating conditions of the element, i.e. changing temperature.
When consecutive measurements are made at the same pulse rate \( (\omega_1 = \omega_0) \), we can use the formula

\[
\frac{k_{n+1} - k_n}{k_0} = \frac{1}{12 \, \gamma_1} \left( \frac{1}{12 \, \gamma_0} \right) \tag{4}
\]

**Measuring System**

The measurement of a moving mass and a fixed spring does not present any difficulties, and can be carried out with any desired accuracy. It is, however, considerably more difficult to determine the phase characteristic \( \Phi = \Phi(\omega) \), since changes in force and translation must be recorded. The measurement method will be discussed below using the example of the motion of the valve slide of a hydraulic proportional distributor (Fig. 4). The force causing movement in this case is due to the pressure differential acting on surface \( A \)

\[
F(t) = A \Delta p(t) = A \Delta p \cos(\omega t)
\]

where \( \Delta p_0 \) is the pressure differential amplitude.

Pressure difference changes can be readily recorded using an electric sensor.

Direct recording of the slide translation is impossible in practice due to the fact that the movement takes place in an enclosed, oil-filled space. In the literature (2) it is suggested that this difficulty be overcome by assuming a proportional relationship between translation of the slide and the speed of the servomotor being controlled by the separator in question. Apart from rather special cases, this approach has a fundamental shortcoming due to large error caused by the phase delay between slide translation and the speed changes of the servomotor. Better results are obtained by substituting the measurement of pressure drop at an opening made in the channel connecting the distributor intake ports for measurement of slide translation. There are two basic sources of error in determining the coefficient \( k_v \): indirect measurement of slide translation, which introduces an additional phase shift, and errors in determining the quantities in equation (3). Furthermore, it follows from equation (3) that the total error depends on the pulse rate because of variable weight coefficients of the partial errors.

Determination of the optimum conditions through calculation is somewhat difficult. Good results are obtained by carrying out a series of measurements within a range of pulse rates for which the phase angle is contained within the limits

\[-60^\circ < \gamma < -30^\circ\]

and averaging out the values of \( k_v \) so obtained.

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Fig. 4. Measurement system for a proportional distributor slide.

[Key: 1 - measurement of]

Bibliography


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