COMPARISON OF THE HYADES, COMA, AND PLEIADES CLUSTERS BASED ON PHOTOELECTRIC u,v,b,y and Hβ PHOTOMETRY*

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On the basis of photoelectric U,B,V photometry, Johnson and Knuckles (1955) carried out a comparison of the distribution in the (U-B) vs. (B-V) diagram of members of the Hyades and Coma clusters. They concluded that the Coma cluster members show an ultraviolet excess relative to the Hyades stars that amounts to $0^m035$ for (B-V) around $+0^m4$. They suggested that this photometric effect might be caused by a difference in the chemical composition of members of the two clusters.

Strömgren (1958) in the Stellar Populations volume, with the use of his original metallic-line index, also showed that the Hyades and Coma cluster stars are different. The difference in both cases suggests that the metal/hydrogen ratio is lower for the Coma cluster stars than for the Hyades stars.

Since both of these clusters are young Population I and are of approximately the same age, it is important to investigate further the question of differences in chemical composition. For the color-index range (B-V) = $0^m4$ to $0^m6$ the main sequence stars in the two clusters are practically unevolved, i.e. they are very close to the zero-age line defined by the beginning of the hydrogen burning phase. For this color-index range, the indices (b-y), $m_1$, and $c_1$ of photoelectric u,v,b,y photometry, and the index $\beta$ of photoelectric H$\beta$ photometry, should yield significant information
regarding the chemical composition of the cluster stars.

These photometric systems have been discussed in some
detail by Strömgren (1963a,b) and by Crawford (1958,1960).

The comparison of the Hyades and Coma clusters presented
here is based on photoelectric u,v,b,y and Hβ photometry of
79 Hyades members and 35 Coma cluster stars, carried out by
the authors and Miss Jeannette Mander at the Kitt Peak
National Observatory.

We assume that interstellar reddening is negligible for
the members of the two clusters, and, since we are comparing
stars that are practically unevolved, we must attribute
differences found for the Hyades and Coma stars to differences
in chemical composition. Comparison of the two clusters is
made through an examination of the following relations:
$c_1$ vs. $β$, $(b-y)$ vs. $β$, $m_1$ vs. $(b-y)$ and $(u-b)$ vs. $(b-y)$.

Figure 1 shows the $β$ vs. $c_1$ relation of the Hyades. The
solid line indicates the zero-age main sequence. Figure 2
shows the same relation for Coma. Figure 3 shows the $c_1$ vs.
$(b-y)$ relation for the Hyades and Figure 4 for Coma.

Consider now the $(u-b)$ vs. $(b-y)$ relation. From the
photometry of the Hyades stars, we can derive a standard
$(u-b)$ vs. $(b-y)$ relation for the $(b-y)$ range in question.
The result is given in Table 1. Then for each Coma star with
its measured $(b-y)$ we list the$(u-b)$ from the Hyades relation
and the difference \( \Delta (u-b) \). A positive \( \Delta (u-b) \), i.e. an ultraviolet excess, is found for all Coma stars in the (b-y) range considered. The average value is +0.061.

We thus confirm the result obtained by Johnson and Knuckles that the Coma cluster stars have an appreciable ultraviolet excess when compared to the Hyades stars. Since it is known from a comparison of values of \( \Delta (u-b) \) and \( \Delta (U-B) \) from metal-poor stars (Strömgren, 1964) that the \( \Delta (u-b) \) scale is on the average 1.6 times wider than the \( \Delta (U-B) \) scale for the color-index range in question, we conclude that there is good agreement between the average values of the ultraviolet excess found in the two investigations.

We now turn to the \( c_1 \) vs. \( \beta \) relation. Again we derive a standard relation from the Hyades stars. Table 2 shows the normal points and the mean relation. Table 3 derives \( \Delta c_1 \) values for individual Coma stars. The average value is -0.027; again an ultraviolet excess is indicated. Analogous treatment of the indices \( m_1 \) and (b-y) gives an average value of \( \Delta m_1 \) of +0.010 for the Coma stars relative to a standard relation defined by the Hyades stars. Finally we examine in similar fashion the (b-y) vs. \( \beta \) relation given in Table 3. Here is is found that the average difference between (b-y) for equal \( \beta \) for the Coma and Hyades stars amounts to -0.007.

The comparison of the results of the photoelectric u,v,b,y
and Hβ photometry of Hyades and Coma cluster stars thus clearly shows that the member stars differ in chemical composition.

We turn now to a discussion of the problem of quantitative determination of the differences in question. On general grounds we would expect that the observed photometric effects are largely due to differences in the helium/hydrogen ratio and of the heavy-element content to the hydrogen content. Such differences affect the internal constitution of the stars, hence their radii and luminosities, and therefore also the effective temperature and surface gravity that determine the properties of the atmospheres. Thus the differences in chemical composition influence the emitted spectrum both by the internal constitution and through the direct effect of the absorption line spectrum, and in this connection the blanketing effect.

For B and A stars the changes in the emitted spectrum, and in particular the changes of specified photometric indices, with chemical composition can be computed quantitatively through the combination of results obtained in stellar-interior and stellar-atmosphere calculations (cf. e.g. Strömgren (1964) and Kelsall and Strömgren (1964)). For the color-index range in question the situation is less favorable. Neither the stellar-interior nor the stellar-atmosphere calculations available at the present time have the accuracy required for our purpose. However, the goal is well-defined, and it is expected
that the situation will improve a good deal during the next few years.

In view of this uncertainty, we limit our discussion to comments on two questions. Consider the values of $\Delta (u-b)$ and $\Delta m_1$ found above from the photometric comparison in the Hyades and Coma cluster stars. From studies based on a comparison of the Hyades with metal-poor stars, a ratio of $\Delta (u-b)$ to $\Delta m_1$ of about three has been found. It would therefore appear that the relation between $\Delta (u-b)$ and $\Delta m_1$ is not linear, since the ratio is about 6 in the Hyades-Coma comparison, where the difference in metal content is considerably smaller than in the case of the metal-poor stars. For metal-contents that do not differ strongly from that of the Hyades, $\Delta (u-b)$ is thus an index of metal content that is much more sensitive than $\Delta m_1$. It should be emphasized, however, that precisely when the aim is the evaluation of relatively small differences in metal content, the (u-b)-method can be used safely only when independent knowledge of the difference in absolute magnitude is available, for (u-b) is sensitive to absolute magnitude. In our discussion of the unevolved Hyades and Coma cluster stars this, however, is the case.

Although the stellar-interior and stellar-atmosphere calculations are not very accurate for the late-F and early-G stars considered here, it is still possible to interpret the
phenomenon of the relatively high sensitivity of $\Delta (u-b)$ to changes in metal content in the range of metal contents characterized by small variation from the Hyades value. Suppose that the relative metal content is reduced by a small amount from the Hyades value. This reduction influences the radius and the luminosity, and the value of the surface gravity for a given effective temperature. The change in surface gravity goes in the direction that gives a smaller Balmer discontinuity, and hence an ultraviolet excess is produced, which is added to the effect of reduced absorption-line blanketing in the ultraviolet, and hence $\Delta (u-b)$ varies relatively strongly with the metal content. For larger reductions of the metal content, the $\Delta (u-b)$ produced via the change in surface gravity is less pronounced.

The quantities $\Delta (u-b)$, $\Delta c_1$, and $\Delta m_1$ derived from the photometry are indicators of the metal/hydrogen ratio. We can now ask the question, Is it possible in principle to derive both the change in the metal/hydrogen ratio and in the helium/hydrogen ratio? In the case of the Hyades-Coma comparison the outlook is not promising, for here we do not know from observation the difference in absolute magnitude on the zero-age line for equal effective temperature. Consider, however, the comparison of Hyades stars and Population I field stars of relatively large trigonometric parallaxes.
again in the color-index range \((B-V) = +0^m4\) to \(0^m6\). We calibrate the \(c_1\) vs. \((b-y)\) diagram for field stars in terms of absolute magnitude, \(M_V\). Next we find \(M_V\) values for the Hyades stars from photometrically determined \(c_1\) and \((b-y)\) values. Finally, we compare the photometric values with the \(M_V\) values derived from the cluster motion (cf. van Bueren (1952)). The average residual turns out to be small, \(0^m2\), and in view of possible systematic errors in the trigonometric and cluster parallaxes, we must admit that this residual might not be significant. (The need for high quality astrometric data is evident.) However, if we accept this value, we arrive at the conclusion that the helium/hydrogen ratio is higher for the Hyades than for the average of Population I field stars. The effect goes in the same direction as that derived by Eggen (1963) from a study of visual-binary masses for Hyades stars. However, the effect indicated by the \(M_V\) residual given above is smaller, and it appears safe to conclude from our discussion that there is no very large difference in the helium/hydrogen ratio for the Hyades stars, as compared to the average Population I field star.

In discussing the \((b-y)\) vs. \(8\) relation for unevolved stars, we found that the difference in \((b-y)\) for given \(8\) caused by the difference in metal content between the Hyades and the Coma cluster stars is small. This result means that the
actual variation of the metal/hydrogen ratio found among
young Population I stars does not seriously affect the
determination of (b-y) from \( \beta \) for unevolved stars. Hence we
have here a reliable method for the determination of intrinsic
colors and excesses. We have applied this method to the
Pleiades stars in the \( \text{B}-\text{V} \) range \( \text{B}-\text{V} = +0.4 \) to \( +0.6 \).
Forty-two stars were observed and the average excess found was
\( +0.035 \) in (b-y). This value corresponds to \( +0.050 \) in (B-V).
The range in \( E(B-V) \) is from 0 to 0.1. We wish to point out
that the average reddening determined in this way agrees very
well with that determined from U,B,V, photometry of B-type
stars in the Pleiades (Mitchell and Johnson (1957)). This
agreement indicates that the adopted \( (U-B)_0 \) vs. \( (B-V)_0 \) relation
for the B-type stars cannot be much in error. Figure 5 shows
the \( \beta \) vs. \( c_1 \) relation for the Pleiades, and Figure 6 the
\( c_1 \) vs. (b-y) relation.

Having determined individual reddenings for the Pleiades
stars, we can apply reductions for interstellar reddening to
the indices \( (u-b) \), \( c_1 \), and \( m_1 \), and thereafter carry out a
comparison between the Pleiades and the Hyades analogous to
that made between the Coma cluster and the Hyades. There is
at present some uncertainty in the dependence of interstellar
extinction upon wavelength. However, an analysis carried out
on the basis of the reddening-law derived by Whitford (1958)
leads to the conclusion that the Pleiades and the Hyades have very nearly the same metal/hydrogen ratio.

The data for all three of these clusters will be presented in detail and discussed further in separate publications.
Table 1

The (u-b), (b-y) Relation for the Unevolved Hyades and Coma Stars

<table>
<thead>
<tr>
<th>Unevolved Hyades Relation</th>
<th>Unevolved Coma</th>
</tr>
</thead>
<tbody>
<tr>
<td>(b-y)</td>
<td>(u-b)</td>
</tr>
<tr>
<td>0.310</td>
<td>1.366</td>
</tr>
<tr>
<td>0.320</td>
<td>1.388</td>
</tr>
<tr>
<td>0.330</td>
<td>1.410</td>
</tr>
<tr>
<td>0.340</td>
<td>1.432</td>
</tr>
<tr>
<td>0.350</td>
<td>1.454</td>
</tr>
<tr>
<td>0.360</td>
<td>1.476</td>
</tr>
<tr>
<td>0.370</td>
<td>1.498</td>
</tr>
<tr>
<td>0.380</td>
<td>1.526</td>
</tr>
<tr>
<td>0.357</td>
<td>1.374</td>
</tr>
<tr>
<td>0.303</td>
<td>1.311</td>
</tr>
<tr>
<td>0.369</td>
<td>1.445</td>
</tr>
<tr>
<td>0.345</td>
<td>1.378</td>
</tr>
<tr>
<td>0.315</td>
<td>1.307</td>
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</table>

13 Stars 0.061
Table 2

The $c_1$, $\beta$ Relation for the Hyades Stars

<table>
<thead>
<tr>
<th>Group</th>
<th>n</th>
<th>(b-y)</th>
<th>$c_1$</th>
<th>$\beta$</th>
<th>$m_1$</th>
<th>$\beta$</th>
<th>$c_1$</th>
<th>(b-y)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>8</td>
<td>0.276</td>
<td>0.472</td>
<td>2.677</td>
<td>0.170</td>
<td>2.600</td>
<td>0.319</td>
<td>0.385</td>
</tr>
<tr>
<td>B</td>
<td>8</td>
<td>0.292</td>
<td>0.443</td>
<td>2.661</td>
<td>0.174</td>
<td>2.610</td>
<td>0.339</td>
<td>0.370</td>
</tr>
<tr>
<td>C</td>
<td>9</td>
<td>0.329</td>
<td>0.399</td>
<td>2.638</td>
<td>0.179</td>
<td>2.620</td>
<td>0.350</td>
<td>0.356</td>
</tr>
<tr>
<td>D</td>
<td>6</td>
<td>0.348</td>
<td>0.373</td>
<td>2.626</td>
<td>0.185</td>
<td>2.630</td>
<td>0.380</td>
<td>0.341</td>
</tr>
<tr>
<td>E</td>
<td>7</td>
<td>0.358</td>
<td>0.362</td>
<td>2.622</td>
<td>0.193</td>
<td>2.640</td>
<td>0.400</td>
<td>0.327</td>
</tr>
<tr>
<td>F</td>
<td>5</td>
<td>0.375</td>
<td>0.327</td>
<td>2.604</td>
<td>0.212</td>
<td>2.650</td>
<td>0.420</td>
<td>0.312</td>
</tr>
</tbody>
</table>

$c = 0.319 + 2.03 (\beta - 2.600)$

$(b-y) = 0.385 - 1.46 (\beta - 2.600)$
Table 3

The $c_1$, $\beta$, (b-y) Relations for the Hyades and Coma Stars

<table>
<thead>
<tr>
<th>Group</th>
<th>n</th>
<th>(b-y)</th>
<th>$c_1$</th>
<th>$\beta$</th>
<th>$c_1$(Hy)</th>
<th>$\Delta c_1$</th>
<th>(b-y)</th>
<th>$\Delta(b-y)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>4</td>
<td>$0.282$</td>
<td>$0.434$</td>
<td>$2.672$</td>
<td>$0.465$</td>
<td>$-0.031$</td>
<td>$0.280$</td>
<td>$+0.002$</td>
</tr>
<tr>
<td>B</td>
<td>6</td>
<td>$0.321$</td>
<td>$0.365$</td>
<td>$2.635$</td>
<td>$0.390$</td>
<td>$-0.025$</td>
<td>$0.334$</td>
<td>$-0.013$</td>
</tr>
<tr>
<td>C</td>
<td>6</td>
<td>$0.362$</td>
<td>$0.310$</td>
<td>$2.608$</td>
<td>$0.335$</td>
<td>$-0.027$</td>
<td>$0.373$</td>
<td>$-0.011$</td>
</tr>
</tbody>
</table>

Coma
References

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_________. 1964, unpublished.
Figure 1 The $\beta$ vs $c_1$ relation for Hyades stars. The line is the zero-age main sequence relation.
Figure 2  The $\beta$ vs $c_1$ relation for Coma stars.
Figure 3 The $c_1$ vs (b-y) relation for the Hyades stars.
Figure 4 The $c_1$ vs (b-y) relation for Coma stars.
Figure 6 The $c_1$ vs ($b-y$) relation for the Pleiades stars.