COMPILER GENERATION USING FORMAL SPECIFICATION OF PROCEDURE-ORIENTED AND MACHINE LANGUAGES

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FOREWORD

This technical report describes research accomplished under Project 4594 and is a revision of a paper presented by the authors at the 1967 Spring Joint Computer Conference held April 19th in Atlantic City.

The authors are indebted to Donald M. Gunn and Craig L. Schager, both for their significant contributions to this work and for their valuable suggestions regarding this paper.

This technical report has been reviewed by the Foreign Disclosure Policy Office (FMLI) and the Office of Information (FMLS) and is releasable to the Clearinghouse for Federal Scientific and Technical Information.

This technical report has been reviewed and is approved.

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ABSTRACT

A compiler generation system is described which is rigorously based and which allows formal specification both of the source (procedure oriented) languages and of the object (machine oriented) languages. An intermediate or "buffer" language, BASE, is interposed, reducing the required transformation techniques described. The system, so far, includes those elements in BASE necessary to produce ALGOL, FORTRAN, and JOVIAL compilers.
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1. INTRODUCTION

This paper reports on a recently developed compiler generation system which is rigorously based, and which allows formal specification both of source (procedure-oriented) languages (POLs) and of machine languages (MLs). Concepts underlying the system are discussed, an example correlating source language specification with system operation is given, and the status and potentialities of the system are discussed.

The crucial problem of compiler generation is the characterization of procedure-oriented languages; the process is of limited use unless such characterization allows machine-independent processing of programs in these languages (and hence allows invariance of the language itself from machine to machine). Our solution interposes between POL and ML a "buffer" or "intermediate" language, called BASE, thus reducing the required POL → ML transformation to two logically independent subtransformations:

(1) POL → BASE (called compilation)
(2) BASE → ML (called translation).

This arrangement isolates questions of POL characterization within the first transformation, and questions of ML characterization within the second transformation. BASE itself is an expandable set of non-machine-specific
operators, declarators, etc., expressed in a uniform "functional" or "macro" notation; the meaning or intent of such operators is arbitrary insofar as the compilation transformation is concerned. The POL → BASE transformation may then be regarded as a machine-independent conversion, from a grammatically rich format to a simple linear format.

2. **THEORETICAL BASIS**

   Within our system, a POL is characterized principally by a grammar (i.e., set of syntactic productions), and the consequent processing of programs in the POL is syntax-driven. To assure adequacy with respect to completeness ambiguity [b], and finiteness of analysis, our syntactic method is rigorously based. A grammatical model (the analytic grammar) was developed [8], which provides a rigorous description of syntactic analysis via formalization of the notion of a scan. Within this model, the selection process of a scanning procedure can be precisely stated, and thus made amenable to theoretical investigation. Some characteristics of this model are:

- all analytic languages are recursive
- all recursive sets are analytic languages

---

1. Each BASE operation, declarator, etc., consists of a three-letter operation code followed by \( n \geq 1 \) operand type specifier/operand pairs \( S_j/X_j \); e.g., FFF \( (S_1/X_1, \ldots, S_n/X_n) \).
• all phrase structure grammars are analytic grammars
• there is a simple sufficient condition under which an analytic grammar provides unique analyses for all strings.

The grammar in a POL specification permits certain abbreviations and orderings of productions (for convenience, brevity, and efficiency), but is nevertheless equivalent to a grammar using the simple scan $S_4$ of [8]. (An equivalent grammar using $S_4$ is obtainable via a simple construction.) Context-sensitive productions may be used. Our method guarantees uniqueness of analysis - it is impossible to embed syntactic ambiguity in a language specification. A simple test ensures finite analyses for all strings. Such a grammar is at least as inclusive as the context-sensitive phrase structure grammar, and there does not appear to be any grammatical structure which cannot be accommodated (grammars of ALGOL, JOVIAL, and FORTRAN were obtained without difficulty).

In fact, such grammars are sufficiently powerful to accommodate the notions of "definition" and "counting" (cf. [7] and the examples of [8]), but to actually do so is neither efficient nor expedient. Therefore, a POL characterization includes description of pertinent "internal operations" (see the example in this paper).

3. SYSTEM OVERVIEW

An overview of the generation system is shown in Figure 1. Using
this system, the transformation from a source language L to a machine language M is achieved as follows:

A specification of L - an abstract description of the syntactic structure, "internal processing rules," and "output code" for L - is written. This specification is processed by the compiler generation system to produce a tape of L - a set of data tables corresponding to the specification. The compiler for L is then formed by conjunction of the tape of L with a compiler model program, a table-directed processor which acts simply as a machine for interpreting the tape of L.
Similarly, a specification of M is written designating macro-expansions appropriate to M. This specification is processed by a translator generation system to produce a tape of M - data tables containing the specified macro-expansions. The translator for M then formed by conjunction of this tape with a translator model program, which expands BASE operations to sequences of instructions in M as directed by the tape of M.

4. COMPILATION SYSTEM DATA BASE

Processing of input strings (POL programs) by a generated compiler is intended to occur in two parts:

(a) preliminary conversion of "raw" input symbols to yield a "syntactic" or "construct" string, which represents the raw input for all further processing, and then

(b) step-by-step syntactic analysis, and (at each analysis step) performance of prescribed sets of internal operations, prescribed output of "code blocks," output of diagnostic messages, and (if desired) performance of additional auxiliary processes.

The internal operations in a POL specification assume a set of data entities (the "data base"), which are later manipulated as prescribed by a generated compiler. Each entry of the construct string (which represents the raw input during processing) contains a construct (or syntactic type or token) and an associated datum, which is originally derived from the raw input, but may be internally altered. The use of appropriate string handling routines allows effectively a construct string of unbounded length. Other data entities are:
(a) a set of function registers $F_i$, for storage and manipulation of "temporary" numeric data

(b) a set of symbol registers $S_i$, for manipulation of symbol strings.

(c) a property table of integer properties $P_i(J)$, for storage and manipulation of numeric data (e.g., number of dimensions) associated with "variables" in the input string. "Names" (i.e., contents of symbol registers) can be "defined" to the table to reserve table entries for associated data, and the table can be "searched." Defined names are placed in a property table index. The $J$th table entry consists of four properties $P_0(J), P_1(J), P_2(J), P_3(J)$. By convention, $P_0(J)$ is the syntactic class of the corresponding defined name.

See Figure 2 for further details.
5. POL SPECIFICATION AND COMPILATION SYSTEM OPERATION

The relation between a POL specification and the consequent compilation system processing is best shown via an example. Figure 3 shows a specification of the language LEMMA2 (first exhibited in Lemma 2 of [2]).

```
* FILE(LEMMA2) *
* SYMBOLS *
  (1)A   (1) (1)
  (1)B   (2) (2)
  (1)C   (3) (3)
  (1)D   (END) (4)
  (1)E   (NULL) (0)
  ((EOC)) (NULL) (0)
* END SYMBOLS *
* SYNTAX *
  001  (A)(B)(K) == (B)
  002  (B)(A)(A) == (B)(K)(A)
  003  (R)(A)(B) == (Q)
  004  (E)(B)(K) == (B)(X)(K)
  005  (E)(Q)(B) == (Q)
  007  (X)(B) == (K)(B)
  008  (X)(K) == (X)(B)
* END SYNTAX *
* INTERNAL FUNCTIONS *
  001  RTV F3 -2
  002  INC F3 1
  003  ASO -3 F3
  004  SET F5 1
  005  SET F6 2
  006  PUT SI VO(-1)
  007  SUF SI VO(D)
  008  DEF SI ((A))
  009  ASO 0 FO
  010  SET P1(F0) 1
  011  INC F5 1
  012  MPY F6 2
  013  PRN 1 S1
* END INTERNAL FUNCTIONS *
* CODE *
  001  BEGIN VR(0))
  002  PWRC/F6)
  003  PWRC/F6)
  004  AAA(C/R(-S))
  005  BBB(C/F5)
* END CODE *
* DIAGNOSTICS *
  0001  END OF SAMPLE ANALYSIS **********
  0002  END DIAGNOSTICS
  0003  END DATA
```

Figure 3. Specification of the LEMMA2 Language

2. The specification is shown in "reference" format, which differs trivially from the format used in machine processing of specifications.
which consists of sentences having the form

\[ A^m B^n A^m B^n C C C \]

where \( X^k \) signifies a sequence of \( k \) \( X \)'s. Some sentences of LEMMA2 are

\[ 'A A B B A A B B C C C' \]
\[ 'A A A A B B A A A A B B C C C' \]
\[ 'A A A B B B A A A B B B B C C C' \]

The specification contains five sections:

1. **Symbols** - specifies the preliminary conversion of input symbols and "reserved words" to construct string entries
2. **Syntax** - a set of syntactic productions for use in syntactic analysis
3. **Internal Functions** - the internal processing to be carried out at each analysis step
4. **Code** - the sequences of codes to be output at each analysis step
5. **Diagnostic Messages** - a set of messages for output

The sections containing internal functions, code and diagnostic messages are unnecessary in defining the language structure, but have been added to illustrate these mechanisms. The codes BEG, PWR, AAA and BBB appearing in the code section were invented expressly for this example; arbitrary BASE operation codes may be designated at will, since these codes are merely transmitted during compilation. The following discussion can be correlated with Figure 4, which shows the compilation analysis trace for a LEMMA2 program, together with resulting values of function registers and code output at each analysis step.
Each step of the analysis trace shows the string in the vicinity of the scan position, after application of the production, performance of internal functions, and code output.

The code output for production p precedes the trace line for production p.

Values of the first 20 function registers are shown at each analysis step: on line with construct F0 through F9, on line with datum F10 through F19.

Figure 4. Compilation of a LENIA2 Program
The conversion specified in the Symbols section, of raw input symbols to construct string format, is performed specifically to eliminate dependency of processing on particular machine character sets and hollerith codes. A construct string entry containing a construct and an associated datum replaces each input symbol (or symbol sequence constituting a reserved word); Figure 5 illustrates this process. An arbitrary numeric or hollerith datum may be specified. Data from the construct string may be used to construct symbol strings (names), but this usage is not dependent on the specific hollerith codes which are used.

Figure 5. Preliminary Symbol Conversion

- The number in parentheses on the left indicates the number of characters comprising the reserved word. The symbols of the reserved word follow.
- A construct (e.g., (END)) is specified for each symbol or reserved word. Use of the construct (NULL) specifies that no construct string entry is to be made; thus "blanks" are ignored above.
- A datum is specified for each symbol or reserved word. Either a numeric datum (e.g., (3)) or a hollerith datum (e.g., (h), where h is the desired hollerith datum) may be specified.
- The special notation ((EOC)) denotes the "end of card symbol", which in many languages is regarded as a punctuation mark. A representation of ((EOC)) must be given in every Symbols section.
The syntactic productions in a specification's Syntax section are applied (as determined by the compiler model's scan) to "rewrite" the construct string, in a step-by-step fashion (see Figure 6). The succession of these rewrites constitutes the syntactic analysis of the construct string. In selective productions from the set of Figure 6, the compiler model uses the "leftmost" scan of \([8]\), i.e., at each step the production chosen is the one whose "left side" occurs first (leftmost) in the construct string. Thus at the first analysis step, the substring chosen is BAA; at the second, ABK; and so on. To allow explicit reference to the data which accompany the constructs of the substring chosen, a scan position is defined (at each step) to occur at the last (rightmost) construct of the selected substring (see Figure 6).

At each analysis step, internal operations associated with the selected production are performed: function registers or properties within the
property table may be set, used, or arithmetically manipulated; character strings may be placed in, prefixed to, or suffixed to symbol registers, and so on. The Internal Functions section (see Figure 7) consists of sequences of internal functions operations. The first operation of each sequence has the label of the production for which action is taken. Thus the sequence RTV F3 -2, etc., is performed each time production 001 is selected.

### Figure 7. Performance of Internal Functions

- **SET F5 1** places the value 1 in the function register F5
- **PUT S1 V0(-1)** places the datum (regarded as hollerith) from construct string position (-1) - relative to the scan position - into the symbol register S1. All previous contents of S1 are deleted.
- **SUF S1 V0(0)** suffixes to the string in S1 the datum from construct string position 0.
- **DEF S1 ((A))** "defines" the string in S1 to the property table: a property table entry (say the n-th) is reserved, the string in S1 is entered into the property table index, together with the entry number n. The number representing the construct (A) is placed in P0(n), and n is placed in F0.
- **ASO 0 F0** "associates" the value in F0 with the construct in string position 0: the value F0 is placed in the datum of position 0.
- **SET P1 (F0) 1** places the value 1 in P1(F0), i.e., in P1(n).
Care has been taken in formulating the internal operations to achieve economy of means - simple operations, a minimum of system data entities, and a minimum of compiler model machinery. Such a formulation allows a simple compiler model program, while language complexities must be expressed within the language specification. Some anomalies of notation still remain from our earlier efforts, but it is planned to revise and clarify notation.

Operation sequences pertaining to different productions are independent of each other, since there is no "GOTO" operation (a "skip forward" is sometimes permitted). Thus a finite sequence of operations is performed at any analysis step.

Code may be output at any analysis step. Operation codes and operand type specifiers given in the Code section (see Figure 8) are merely

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**Figure 8. Output of a Code Sequence**
transferred to the output, while operands are inserted as specified.

The Diagnostic Message section contains a set of messages, which are output by PRN internal operations. The operation PRNI S1, which is executed for production 006, prints message 001 and the contents of S1.

6. TRANSLATION AND MACHINE SPECIFICATION

A translator for a given target machine (ML) produces, from an input program of BASE operations, an equivalent program in the target assembly language, in a format acceptable to the target assembler. The production of assembly language guarantees compatibility of the object program with the machine's monitor system, and allows the assumption in translation of system subroutines and macros.

A BASE program contains generalized item declarators, array declarators, etc., and generalized computation operators (e.g., ADD, SUB). Since data definition is explicit, the BASE computation operators do not take account of the data types involved in the operations. Thus for each computation operation, there is an equivalent set of standard suboperations: e.g., corresponding to ADD are the standard suboperations

"add a floating item to a fixed item"

"add a fixed item to a floating item"

and so on. Determination of the specific suboperation required for a given BASE operation, taking into account the data types involved, is performed within the translator.
Translation thus occurs in two parts:

(a) analysis of BASE operations by an analysis section, to derive equivalent sequences of standard suboperations,

followed by

(b) expansion of the standard suboperations by a macro-processor section, to produce assembly code.

A machine specification defines expansions of the standard suboperations. In other words, it defines for each standard suboperation an equivalent sequence of assembly language instructions. Embedded in these expansions are format specifiers, which cause the appropriate format to be generated. A machine specification is processed by the translator generation system to produce corresponding data tables, which are combined with the translator model program to form the desired translator. These data tables direct the expansions performed by the translator's macro-processor.

Parameters required by the expansions are furnished by the translator's analysis section via a communication table, from which they are retrieved as necessary by the macro-processor section. Within a machine specification, parameters are specified via position in this table.

Our present machine specification notation is processor-oriented, and not easily readable; however, it is planned to formalize this notation. Some typical macro definitions are shown in Figure 9, in a contemplated notation, as an illustration of the features provided in a machine specification.
LOADING ACC AND MQ WITH DOUBLE PRECISION OR COMPLEX NUMBER (FOR CDC 1604):

LOAD ACCUMULATOR (FOR IBM 7094 FAP):

Figure 9. Some Typical Macro Definitions

The translator model program, except possibly for one output procedure, is machine-independent. The analysis of BASE operations is dependent only on the operator, accumulator data type, and operand data type involved, while macro expansion is table-driven. All dependency on the target machine is isolated within the data tables used to direct expansions. Assembly code is output in the form of 80 column card images, which are almost universally acceptable by target assemblers. Unusual cases might require simple modification of the output procedure.

7. CONCLUSIONS

Using the syntactic model of [8], we have developed a system to formally characterize languages which are rich in grammatical structure.
and to subsequently process strings in such languages. Such processing can produce linear code (BASE language). The BASE language contains computation and data declaration operations sufficient to accommodate the functions of ALGOL, FORTRAN, and JOVIAL. BASE is expandable, so that more convenient or efficient operations may be introduced when these are desirable.

We have shown the feasibility of formally characterizing machine (assembly) language, and of machine-independent translation (BASE → ML). In sum, we have presented a rigorously based, machine-independent compiler generation system.

A consequence of these results is that language invariance can be maintained from machine to machine. It is possible to have a standard version of each procedure-oriented language, rather than machine-dependent variants.

The system is presently running on the CDC 1604 computer. Specifications of ALGOL, FORTRAN, and JOVIAL have been written, as has machine specification for the CDC 1604. The ALGOL and FORTRAN specifications have undergone tentative checkout and modification, as has the CDC 1604 specification. Preliminary comparisons of operating characteristics have been made. For a small number of short programs, our system produces object programs about the same size as do the manufacturer-supplied compilers, and requires between twice and three times the computer time. Since our system is a prototype, these results indicate that it may be possible to generate compiler/translator systems which have competitive efficiencies. We contemplate major operational
Aharges, without the sacrifice of theoretical rigour, which should increase system speed by a factor of between 3 and 5.

The compiler (POL BASE) portion of this system has other uses. The ability to formally characterize grammatically rich languages and to subsequently process strings in such languages is of importance wherever string-structure-dependent processing is required.
REFERENCES


A compiler generation system is described which is rigorously based and which allows formal specification both of the source (procedure oriented) languages and of the object (machine oriented) languages. An intermediate or "buffer" language, BASE, is interposed, reducing the required transformation techniques described. The system, so far, includes those elements in BASE necessary to produce ALGOL, FORTRAN, and JOVIAL compilers.

This paper was presented at the 1967 Spring Joint Computer Conference.
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