AD NUMBER
AD002089

NEW LIMITATION CHANGE

TO
Approved for public release, distribution unlimited

FROM
Distribution: No Foreign

AUTHORITY

"Normal closure 30"

THIS PAGE IS UNCLASSIFIED
Technical Note No: G.W.225

A Pulse-Operated Auto-Correlator

By

Major F.W. Stoneman, R. SIGS.,

and D.E. Verrian
A Pulse-Operated Auto-Correlator

by


and

D.E. Verrian

SUMMARY

A pulse-operated auto-correlator offers advantages over other forms of correlator in its comparative simplicity and its ability, under certain conditions of use, to provide a complete correlogram without the necessity of recording the input data.

The system involves the storage of information on a series of condensers connected to the contact banks of two uniselectors, the wipers of which can be rotated at the same speed but with any desired angular separation, equivalent to the required values of $\tau$, the correlation interval. Theoretically the results obtained are accurate for a repetitive function if the sampling rate is more than three the highest frequency component.

A test instrument has been built which demonstrates that the principle is sound, and provides the basis of a practical machine. The main difficulties requiring further investigation are listed in the conclusions.
LIST OF CONTENTS

1 Introduction 3
2 Basic Principles 3
3 Practical Circuits 6
4 Control Circuit 7
5 Test Results 7
6 Conclusions 8
Advance Distribution 9
Detachable Abstract Cards

LIST OF APPENDICES

Operation of the Summator
Appendix I
Control Circuit Operation
Appendix II

LIST OF ILLUSTRATIONS

Basic Principle 1(a)
Modified Circuit 1(b)
Storage Circuit 2(a)
Multiple Storage 2(b)
Overall Circuit 3
Summator 4(a)
Control of Relays M and N 4(b)
Control Circuit 5
Graph of \(-\frac{1}{\sin \frac{2\pi}{n}}\) against \(n\) 6
1 Introduction

The construction of correlograms from recorded data by graphical methods is both tedious and lengthy. An instrument operated from continuous inputs may be somewhat complicated and must be used in conjunction with a recorder.

A model pulse-operated machine has been constructed which, apart from the multiplying and integrating components (common to any auto-correlator), employs only relays and simple electronic circuits.

2 Basic Principles

The operation is based upon the storage of samples of the input signal on a number of condensers. If the number of stores available is adequate to "record" the entire signal, all the points on the correlogram may be obtained without the use of additional recording devices.

2.1 Defining the auto-correlation coefficient as:

\[ \tau = \lim_{A \to \infty} \frac{1}{A} \int_{0}^{A} f(t) \cdot f(t + \tau) \, dt \]

then for a sinusoidal function \( y = \sin \omega t \)

\[ \tau = \lim_{A \to \infty} \frac{1}{2} \left[ \cos \omega t - \frac{1}{\omega A} \sin \omega A \cdot \cos (\omega + \tau) \right] \]

\[ = \frac{1}{2} \cos \omega t \] (1)

Now if the input is sampled \( r \) times at intervals \( t' \) then:

\[ y_{r} = \sin r \omega t' \]

and

\[ \tau = \lim_{n \to \infty} \frac{1}{n} \sum_{r=1}^{n} \sin r \omega t' \cdot \sin [\omega (r t' + \tau)] \]

\[ = \frac{1}{2} \cos \omega t \cdot \lim_{n \to \infty} \frac{1}{2n} \sum_{r=1}^{n} \cos [2 r t' + \tau] \] (2)

\[ \sum_{r=1}^{n} \cos (2 r t' + \tau) \]

represents the sum of a series of vectors having successive angular separations of \( \frac{4 \pi}{T} \) where \( T \) is the periodic time of the sine wave. For \( t' \ll T \) this sum will tend to zero at each complete
cycle and hence the second term of the expression for \( V_1 \) will be zero. For larger values of \( t' \) the same effect will be apparent until \( t' = \frac{T}{2} \) when the angular separation becomes \( 2\pi \) and the vectors add. However for \( t' < \frac{T}{2} \) (that is, more than 2 samples per cycle) the second term is zero and
\[
V_1 = \frac{1}{2} \cos \omega \tau .
\]

2.2 In practice of course neither \( a \) in Equation (1) nor \( n \) in Equation (2) will be infinite. An error will therefore be apparent of magnitude dependent upon the length of data available.

It can be shown that if \( m \) is the number of samples per cycle then the second term of Equation (2):

\[
= \frac{1}{2n} \sin \frac{2\pi n}{m} \cos \left( \omega \tau + 2\pi \frac{n+1}{m} \right) \sin \frac{2\pi}{n}
\]

\[
= \frac{1}{2} C \cos (\omega \tau + \phi) \quad \text{for specific values of } n \text{ and } m .
\]

Thus compared with the true auto-correlation coefficient the error has an amplitude of \( 100\% \) and a phase angle \( \phi \).

\( 'n' \) must be integer but \( 'm' \) may have any value \( (> 2.0) \). If \( \frac{n}{m} \) is integer then Equation (3) becomes zero. In practice it will not be practicable to ensure this condition and in any case for a complex waveform \( 'm' \) varies for each frequency component and hence it is safest to assume that \( \sin \frac{2\pi n}{m} \) has its maximum value of unity. The magnitude of the error will therefore be determined mainly by the factor:

\[
C' = \frac{1}{n \sin \frac{2\pi}{m}}
\]

Fig. 6 shows the graph of \( \frac{1}{n \sin \frac{2\pi}{m}} \) plotted against \( m \) and for \( m > 2 \) it will be seen to have a minimum at \( m = 4 \) when \( \sin \frac{2\pi}{m} = 1 \). Hence the maximum error for a sampling rate of 4 per cycle will be \( \frac{100}{n} \% \) relative to unity, and will vary between this value and zero according to \( \sin \frac{2\pi n}{m} \).

As an example consider a sampling rate of 25 per second and a frequency of 4 cycles per second.

Then
\[
m = 6.25 .
\]
From Fig. 6:-

\[ c' = \frac{1.2}{n} \]

and for a maximum error of 1%:

\[ \frac{1.2}{n} \times 100 = 1 \quad \text{or} \quad n = 120 \text{ samples}. \]

Hence the data length should be a minimum of \( \frac{120}{6.25} = 20 \) cycles.

However

\[ \frac{n}{m} = \frac{120}{6.25} = 19.2 \]

and

\[ \sin 2\pi \times 19.2 = 0.94 . \]

Theoretically the error will therefore be reduced by the factor 0.94, but for 119 samples the factor will be 0.06 and for 121 samples 0.7. In practice it is thus better to assume the worst case - that is \( \sin 2\pi \frac{n}{m} = 1 \).

Now if there is a component frequency at 1 cycle per second, it will be seen that \( m = 25 \) and for \( n = 120 \)

\[ 100 \times c' = \frac{4.1}{120} \times 100 = 3.4\% . \]

To reduce the error at this frequency to 1% it would therefore be necessary to increase the number of samples to about 500.

Thus for repetitive functions which can be analysed into a series of harmonics the auto-correlation coefficient may be obtained by sampling provided that \( m > 2 \) for the highest frequency component, and the error can be reduced to a desirable maximum by choice of suitable sampling rates and/or length of data. This is not necessarily true for a random input but forms a useful guide; if the data under consideration is obtained from a system which rejects by filtering action any frequencies greater than \( \frac{1}{\tau} \), then the sampling rate must be greater than \( 10 \) per second, and the minimum length of data for a reasonable degree of accuracy can be estimated.

2.3 A simple circuit arrangement is illustrated at Fig.1(a). Two uniselectors, controlled by a pulse drive so that they step round together, have their corresponding contacts connected to each other and to storage condensers. With the stored voltages proportional to instantaneous values of the data, the uniselector wipers apply the two required potentials to a multiplier. Switching is arranged so that the multiplier output is connected to the summator (integrator) once each time the wipers come to rest on a pair of contacts. If the uniselectors are synchronised so that they are both connected to the same condenser at the same instant, the output of the summator, when all the condensers have been sampled, is a measure of the auto-correlation coefficient for \( \tau \) equal to zero. By advancing one wiper so that it stops a fixed number of contacts in front of the other one, an output equivalent to another value of \( \tau \) is obtained.
2.4. As shown in Fig. 1(a), the arrangement is suitable for the case when there are an adequate number of condensers to store the whole input data without the use of an additional recorder. Provided that the leakage is negligible, readings for all the available values of $\tau$ can be obtained from successive revolutions of the wipers. A limit to the method is imposed by the number of contacts or condensers available. A modification by means of which the system can operate from a recording is shown at Fig. 1(b); a second contact bank of the first uniselector is used and the wiring arranged so that a condenser charged at (e.g.) contact 4 is connected to the multiplier via contact 5 (i.e., one step later). The charge must be stored only until the second uniselector has passed the equivalent contact; the operating time may therefore be increased indefinitely using as many revolutions of the uniselector as desired - the limitation is that $\tau$ can be increased only to the equivalent of one revolution.

2.5 For an input lasting for, say, 30 seconds with a highest frequency component of 5 cycles per second, a minimum of 300 storages is necessary to obtain an auto-correlogram without employing a recorder. If however the data is recorded, a 50 contact uniselector can be used - with a sampling rate of 4 per cycle (20 per sec), 12 revolutions will be necessary, and the maximum value of $\tau$ will be restricted to $1/12$ of the recording (2\frac{1}{2} sec). If the input contains higher frequencies, measurements can be made by slowing down the replay speed of the recorder (or increasing the sampling rate), but the number of revolutions will be increased accordingly, reducing the maximum value of $\tau$; an alternative is to deal with the recording in several portions to obtain the value of $\tau$ required, averaging out the correlogram from the individual results.

3 Practical Circuits

3.1 The basic storage circuit is shown at Fig. 2(a), the condenser being connected to the grid of a cathode-follower. The use of this arrangement for each store would be extravagant, and also has the disadvantage that grid current and additional leakage in the valve assembly increases the rate of discharge. A more suitable method is illustrated at Fig. 2(b); each condenser is connected only to its appropriate uniselector contact. A single cathode follower in the wiper circuit suffices for all the condensers (see also Appendix I, paragraph 2.1).

3.2 The overall arrangement is shown at Fig. 3.

3.21 With the multiple-bank switches $S_3$ and $S_2$ set to position 1, the data will be stored on the condenser as the wiper of contact bank $A_B$ rotates. The maximum time available is equivalent to one revolution of the uniselector. The remainder of the circuit is inoperative during this cycle.

3.22 For correlation, $S_c$ is moved to position 2. On depressing the "start" control relay $C$ will operate its contacts, removing the zeroing earth from the summator and connecting the cathode follower and multiplier in circuit. After one revolution $P$ operates, providing the output as a D.C. signal; relay $C$ drops out and a new value of $\tau$ can be set up by advancing the wiper of $A_B$. This process is continued until the required number of points on the correlogram have been obtained.

3.23 With $S_c$ at position 3 the circuit is set up for use with a recorder. On operating the "start" control the first value of the input signal is stored on condenser 1 via contact C of $A_B$. Meanwhile the inputs to the cathode followers are both zero from condenser 0. At the next step, the second value of the input is stored in condenser 2, and condenser 1 is connected to the cathode followers. This process may be
continued for as many revolutions of the uniselectors as desired, because a new input to a condenser will automatically cancel the previous stored value. The whole process must now be repeated, commencing at the same point on the recording, but with vipers $A_A$ and $A_B$ (mechanically joined) advanced for a different value of $\tau$.

3.3 Fig.4(a) shows the summator circuit. When relay $M$ operates the contacts $M_2$ and $M_3$ close and the input voltage is stored on the condenser associated with cathode follower $CF_2$. When $M$ releases this voltage is maintained at the output but, via contact $M_4$, is also stored at $CF_1$. When $M$ closes again, the previous output at $CF_1$, together with the new input value are added in the amplifier $AMP_1$ and stored at the output. There is a sign reversal in $AMP_1$ and consequently a further reversal is required ($AMP_2$) to obtain the correct sign at $CF_1$. In the operation $M_4$ must open before $M_3$ closes to prevent the loop from being closed; when $M$ releases $M_3$ must open before $M_2$ and before $M_4$ closes. Further information on the summator is included at Appendix I.

3.4 The multiplier employed was of the diode squarer type, having an output range of 0 to 60 volts for inputs of 0 to 50 volts D.C. It was discovered during tests that a considerable error was introduced due to ripple on the multiplier output, which of course was not apparent when measuring the mean output on a D.C. meter. The summator however accepts the instantaneous value when contact $M_3$ (Fig.4(a)) opens and consequently extra precautions were taken to suppress the ripple.

4 Control Circuit

The control arrangements were designed to meet the following conditions.

4.1 Simple "START-STOP" buttons to operate for each of the three conditions of paragraph 3.2.

4.2 A "ZERO" reset, to restore the uniselectors to their home contacts and discharge all condensers.

4.3 Switches to preset the value of $\tau$.

4.4 A "RESET $\tau$" control to restore the uniselectors to their initial positions for a preset value of $\tau$.

The basic circuit is shown at Fig.5 and a description of the operation is in Appendix II.

5 Test Results

5.1 To provide a simple test an input approximating to a sine wave was used. The amplitude was 30 volts and the equivalent sampling rate was 12 per cycle (or 300 per contact of the uniselectors). A single cycle was an adequate data length for test purposes as under these conditions each cycle is merely a repetition of its predecessor; as $\frac{n}{m}$ equals unity $\sin 2\pi \frac{n}{m}$ is zero and the error is zero.
5.2 Typical results were:

<table>
<thead>
<tr>
<th>$\tau$</th>
<th>Summator Output $A$</th>
<th>Summator Output $B$</th>
<th>$A$</th>
<th>$B$</th>
<th>$\cos \tau$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>117.7</td>
<td>114.4</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>30</td>
<td>101.4</td>
<td>98.0</td>
<td>0.362</td>
<td>0.359</td>
<td>0.666</td>
</tr>
<tr>
<td>60</td>
<td>58.2</td>
<td>55.6</td>
<td>0.494</td>
<td>0.486</td>
<td>0.5</td>
</tr>
<tr>
<td>90</td>
<td>1.1</td>
<td>0.6</td>
<td>0.009</td>
<td>0.005</td>
<td>0</td>
</tr>
</tbody>
</table>

5.3 Although the values of $\cos \tau$ given by the two runs A and B agree closely with the theoretical values, it will be noted that the actual readings vary appreciably. It was discovered during the tests that these discrepancies were due to long term drift of the amplifiers and cathode followers.

6 Conclusions

6.1 Although the tests carried out were limited, they were adequate to demonstrate that the principle is sound and achievable in practice.

6.2 The following difficulties and sources of error were noted:

6.21 Summator drift of cathode followers. Although the actual drift may be small the effect on the summator output can be considerable as the error is additive every time the summator relay operates; moreover the linearity is upset. The most critical adjustment was found to be the zero setting of cathode follower $C^P_1$ (Fig. 4(a)).

6.22 Amplifier drift. Long term drift has an effect similar to that of a zero error. If consistent results are to be obtained drift-stabilised amplifiers should be used.

6.23 Multiplier. For many purposes a multiplier having a high percentage accuracy relative to the maximum output is satisfactory. When used in a correlator however, one input may be zero and the other large - or both may be small - and the accuracy relative to the true product for these inputs must be high, especially with regard to any change brought about by altering the signs of the inputs. Care must be taken to adjust the multiplier used to meet this requirement.

6.24 Condenser leakage. In the condensers associated with cathode followers as storage circuits it is shown in Appendix I that leakage due to negative grid current is the main difficulty. In the case of the condensers storing the input signal, the performance is adequate provided good quality condensers are used and care is taken in maintaining good insulation; a discharging effect however was noted due to the rotation of the uniselectors (connected to cathode followers) - this appeared to be due to the input capacity of the cathode follower (including the wiring), as the effect was most apparent when successive condensers were charged to potentials of opposite sign.

6.3 These investigations have not been carried out in sufficient detail to produce a practical instrument. The results however indicate that the principle is sound and that with more effort a comparatively simple, accurate and flexible machine could be built at a reasonable cost.
Attached:

Appendices I and II.

Drg. Nos. GW/E/4054 to 4058.

Detachable Abstract Cards.

Advance Distribution:

Chief Scientist
CGWL
CS(A)
PDSR(A)
DGTD(A)
EDG
DCD
D Inst RD
DG of A
DWR(D)
GWAB (Dr. R.C. Knight)
TPA/TIB - 100
Director, RAE
DD(E)
DD(A)
RFD - 2
Radio
Arm
Patents
Elec Eng
IAF
Instn
Math Services
GWTV - 2
Library
APPENDIX I

Operation of the Summator

1. Control of relay M

The pulse drive operating the uniselector relays is connected via auxiliary contact banks A, and B, (Fig.4(b)). At the beginning of the pulse the uniselector relays are energised but the wipers do not move and a circuit is therefore completed to relay M, which operates. As contact M, closes, relay N is energised and is held closed via N, . As M, closes M is de-energised and opens. At the end of the operating pulse N drops out and the wipers step forward one contact, resetting the circuit ready for the arrival of the subsequent pulse. This arrangement ensures that M operates after the beginning of the pulse and releases before the end of the pulse (i.e. whilst the wipers are stationary on the appropriate contacts). The duration for which M remains closed depends upon the operating times of relays M and N and upon the adjustments of contacts M, and N, ; during tests of the circuitry the duration was set to approximately 35 milliseconds. By inclusion of switch Sc, the process can be halted if desired at the end of the uniselector revolution; at position 2, M will not be operated on contact 49, but relay P will be energised instead, connecting the summator output to a voltmeter (Fig.3). With Sc, in position 3, relay M is reconnected into circuit at contact 49 and the summating process can continue for subsequent uniselector revolutions.

2. Accuracy

2.1 The simple storage circuits are dependent for their accuracy upon the amount of condenser leakage and cathode follower drift. The former is not important in the summator circuit as the whole operation takes only a matter of seconds; by careful selection, condensers were obtained which showed negligible leakage over a period of 10 minutes. Drift due to negative grid current is however important; with contact M, (Fig.4(a)) open, so that the condenser is connected only to the cathode follower grid, a reverse grid current of 1 pA will cause a change of potential of +1 volt per second on a 1 μF condenser. By careful selection of the valve and adjustment of the cathode follower, a drift of 1 volt in 45 minutes was achieved; in this case such a performance should be satisfactory if the maximum possible range of the summator is utilized and the operating time is restricted to 30 seconds or so. It should be noted that the drift of CF, is not so important, as the condenser is isolated only for the short period (about 35 ms) that M, is open; for the remainder of the period between pulses the condenser is maintained at its correct voltage by the output of CF,.

2.2 The effect of gain of individual components and cathode follower zero errors can be very important. If gains a, b, c, d and e (Fig.4(a)) are used and there are zero errors x and y on CF, and CF, then (neglecting sign reversals in the amplifiers):-

\[ V_{o1} = (V_1 + ex) \; ab + y \; \quad as \; \quad VL_1 = x \]

\[ V_{o2} = (V_2 + c) \; od + x = [(V_1 + ex) \; ab + y] \; od + x \]

and

\[ V_{o2} = [V_2 + c \; [(V_{1+ex} \; ab + y) \; od + x)] \; ab + y \].

-10-
Put ab = r and cd = s, and let it be assumed that the circuit has been adjusted for no output zero error and Vo₂ = 2Vo₁ when V₁ = V₂, then:

\[ 2 [(V₁ + ex) r + y - V₂ + e + ex] a + xl \]

\[ r - y \]

which will be satisfied if the overall gain e.r.s is unity, and x and y are of opposite sign.

Then with V₁ = V₂ the summator will appear to be linear. For V₁ ≠ V₂ this will not be so and in the case when V₁ = -V₂, Vo₂ will be \( 2(e rx + y) \) instead of zero.

The complete circuit will be linear if x and y are zero and the total gain e.r.s is unity. In practice however it is preferable to have both r and es each unity as otherwise a zero error x may be overlooked. For example, let y = 0, r = 0.9, s = 1 and e = \( \frac{1}{0.9} \). Then

\[ Vo₁ = \left( V₁ + \frac{x}{0.9} \right) 0.9 = 0.9 V₁ + x \]

\[ Vo₂ = 0.9 (V₁ + V₂) + 2x \]

and 2Vo₁ = Vo₂ if V₁ = V₂, but Vo₂ = 2x if V₁ = -V₂.

Thus for x ≠ 0 the characteristic of the summator will be a diamond shaped "hysteresis" loop. Having initially adjusted the gains to unity, rapid checks can be made during operation by adjusting the output to zero with the "zero" switch operated and then applying inputs +X, -X, -X and +X. Vo₂ and vo₄ should be zero; any discrepancy can be removed by adjusting the zero control of CF₁.

2.3 By taking reasonable care in the selection of components and lining up, an overall performance should be obtained having an error of less than 1% of the maximum output over the range ±50 volts.
APPENDIX II

Control Circuit Operation

1 "Start-Stop"

1.1 Operation of the "START" button energises relay C (Fig. 5) which is self-holding via contact C₁. Contacts C₂ and C₃ connect the operating coils A and B of the two uniselectors to a pulse voltage whose frequency can be adjusted to meet the required sampling or operating rate. Additional contacts of C (Fig. 3) remove earths from the multiplier inputs which are then connected to the wipers of uniselector contact banks Aₜ and Bₜ, and also remove the "zeroing-earth" from the summator.

1.2 Operation of the "STOP" button merely releases relay C, stops the uniselectors and zeros the multiplier and summator. In positions 1 and 2 of the control switch Sc (Fig. 4(b)), to meet the conditions of paragraphs 3.21 and 3.22, the uniselectors are required to stop at the last contact of A (not necessarily the last contact of B if τ > 0). When C is operated contact C₄ (Fig. 5) applies a positive potential to contact 49 of Aₜ; when the wiper reaches this point relay L operates, releases C by the opening of contact L₂ and is itself released when C₄ reverts to its off position; a separate switch S₉ is included to remove this facility when not required.

2 "Zero" Reset

On operating the "ZERO" button, relay D operates and holds via contact D₉. Positive voltages are applied via Dₙ to the homing contacts Aₜ and Bₜ of the uniselectors A and B, which commence to rotate automatically. The positive voltage on wiper Bₜ is ineffective until the home position (contact 0) is reached, whereupon relay F operates via Dₙ and is held by Fₙ. When Fₙ opens the operating potential is removed from Bₙ and the uniselector B stops. When D is operated, wiper Aₜ (Fig. 3) is earthed so as to discharge all the condensers; for this to be effective uniselector A must complete a second revolution when homing if it is further advanced than contact 1. This is achieved by a similar arrangement as for uniselector B, by relay E connected to contact 0 of Aₜ, but the circuit is made ineffective until relay G, associated with contact 1, has operated. Thus if Aₜ is at rest on any contact from 2 to 49, on the operation D, D₃ will apply a positive voltage to Aₜ and the wiper will hunt round. On arriving at contact 1, G will operate via D₅ (holding via Gₙ) and contact Gₙ will close the circuit to relay E which will operate the next time the wiper arrives at contact 0, and stop the uniselector in this position. When both E and F are operated relay D is released (contacts Eₙ and F₉) and relays E, F and G release (contacts D₃ and D₉) thus restoring all the relays to their off condition. Contacts D₅ and D₆ are to prevent false operation of other controls when D is operated and vice versa.

3 Preset τ

3.1 To simplify and speed up the operation of the correlator it is desirable that homing facilities be provided on the uniselectors so that the wiper of B returns to the zero contact and that of A to any selected contact equivalent to the required value of τ for the next run.
3.2 The homing facilities are provided by relays $H$, $J$ and $K$ (see paragraph 4 below) and the control of the value of $T$ by switches $S_A$ and $S_B$. $J$ responds to a positive voltage on wiper $A_A$ (Fig.5) and is connected by the multi-position switch $S_A$ so that the wiper halts at contact $0, 5, 10, 15$ etc. as selected. In practice $J$ is a slow operating relay and it is convenient to make connections from $S_A$ to contacts $49, 45, 40, 44$ etc. allowing the uniselector an extra step before it stops.

3.3 Use is made of relay $L$ (already employed in the STOP system - paragraph 1.2) to select individual positions between $0$ and $5, 5$ and $10$ etc. If $S_A$ is set to $5$ and $S_B$ to $2$ (i.e. required value of $T = 7$), wiper $A_A$ will stop at contact $5$ under the influence of relay $J$, but as soon as $H$ releases relay $L$ is connected via $H_5$ to $A_A$ and will operate from the positive voltage applied to contact $5$ from $S_B$ position $1$. Contact $L_1$ steps $A$ forward, but $L_2$ prevents $B$ from being energised. $L$ will drop out immediately $A_A$ moves away from contact $5$, but as the positive voltage appears on contact $6$ from $S_B$ position $2$, $L$ will operate again and $A$ will move on to position $7$. Contact $7$ is isolated so that no further operation of $L$ will occur and the wiper will remain at $7$.

4 Reset

4.1 To reset $T$ to repeat a run, or to home the uniselector to a new value of $T$ (paragraph 3 above), a homing circuit separate from the "ZERO" reset is employed as $A$ is not normally required to return to contact $0$.

4.2 Uniselector $B$ is always required to return to contact "0" so that relay $F$ used for the ZERO-reset can also be employed for this purpose. On depressing the RESET $T$ control $H$ operates and $K$ is operated via $H_6$. $K_4$ in parallel with $D_4$ connects $F$ into circuit and the operation is exactly the same as in the case of the ZERO-reset.

4.3 When $H$ operates, $H_5$ connects positive voltage to wiper $A_A$ and the uniselector $A$ hunts round due to closing of contact $H_6$. On the operation of $J$ at the contact selected by $S_A$, $A$ will cease to step round due to the opening of $J_2$. $H$ will release immediately $J$ operates and to prevent premature halting of $B$, $K$ is arranged not to release until $F$ has operated ($K_5$ and $F_4$ in parallel with $H_6$).
FIG. 1(a) BASIC PRINCIPLE.

FIG. 1(b) MODIFIED CIRCUIT.
FIG. 2 (a) STORAGE.  FIG. 2 (b) MULTIPLE STORAGE.

FIG. 3. OVERALL CIRCUIT.
FIG. 4(a) SUMMATOR.

FIG. 4(b) CONTROL OF RELAYS M AND P.
FIG. 5. CONTROL CIRCUIT.
FIG. 6. GRAPH OF $\frac{1}{\sin \frac{2\pi}{M}}$ AGAINST M.
LEACIIABLE ABSTRACT CARDS

These abstract cards are inserted in RAE Reports and Technical Notes for the convenience of Librarians and others who need to maintain an Information Index.

Detached cards are subject to the same Security Regulations as the parent document, and a record of their location should be made on the inside of the back cover of the parent document.
Theoretically the results obtained are accurate for a repetitive function if the sampling rate is more than twice the highest frequency component.

A test instrument has been built which demonstrates that the principle is sound, and provides the basis of a practical machine. The main difficulties requiring further investigation are listed in the conclusions.

Theoretically the results obtained are accurate for a repetitive function if the sampling rate is more than twice the highest frequency component.

A test instrument has been built which demonstrates that the principle is sound, and provides the basis of a practical machine. The main difficulties requiring further investigation are listed in the conclusions.