UNCLASSIFIED

AD NUMBER

ADB022406

LIMITATION CHANGES

TO:
Approved for public release; distribution is unlimited.

FROM:
Distribution authorized to U.S. Gov't. agencies only; Test and Evaluation; NOV 1976. Other requests shall be referred to Air Force Armament Laboratory, Attn: DLJC, Eglin Air Force Base, FL 32542.

AUTHORITY

USADTC ltr, 10 Dec 1979

THIS PAGE IS UNCLASSIFIED
THIS REPORT HAS BEEN DELIMITED
AND CLEARED FOR PUBLIC RELEASE
UNDER DOD DIRECTIVE 5200.20 AND
NO RESTRICTIONS ARE IMPOSED UPON
ITS USE AND DISCLOSURE.

DISTRIBUTION STATEMENT A

APPROVED FOR PUBLIC RELEASE;
DISTRIBUTION UNLIMITED.
LOAD ANALYSIS AND CRITICAL AREA
STRESS ANALYSIS OF THE 126-AR00036 AND
126-AR00037 PARACHUTE TESTERS WHEN
INSTALLED ON THE F-4C/D AIRCRAFT
CENTERLINE STATION

AIRCRAFT COMPATIBILITY BRANCH
MUNITIONS DIVISION

NOVEMBER 1976

FINAL REPORT: JULY 1976 TO OCTOBER 1976

Distribution limited to U. S. Government agencies only; this report documents test and evaluation; distribution limitation applied November 1976. Other requests for this document must be referred to the Air Force Armament Laboratory (DLJC), Eglin Air Force Base, Florida 32542.

AIR FORCE ARMAMENT LABORATORY
AIR FORCE SYSTEMS COMMAND • UNITED STATES AIR FORCE

EGLIN AIR FORCE BASE, FLORIDA
**Title:** Load Analysis and Critical Area Stress Analysis of the 126-AR00036 and 126-AR00037 parachute testers when installed on the F-4C/D aircraft centerline Station.

**Authors:** William W. Dyess, Jr.

**Performing Organization:** Aircraft Compatibility Branch (DLJC), Eglin Air Force Base, Florida 32542

**Controlling Office:** Air Force Armament Laboratory, Armament Development and Test Center, Eglin Air Force Base, Florida 32542

**Program Element:** 62602F

**Project:** JONAFSCG021

**Final Report:** July 1976 - October 1976

**Number of Pages:** 57

**Security Class:** UNCLASSIFIED

**Distribution Statement:** Distribution limited to U.S. Government agencies only; this report documents test and evaluation; distribution limitation applied November 1976. Other requests for this document must be referred to the Air Force Armament Laboratory (DLJC), Eglin Air Force Base, Florida 32542.

**Keywords:** Loads Analysis, Interface Area, Parachute Tester, Structural Analysis

**Abstract:**
This report documents the loads and critical stress analyses performed on the two stores: 126-AR00036 and 126-AR00037. These stores are two parachute testing vehicles used by the 6511th Test Sq/DORER for evaluation of various parachutes.
PREFACE

This report covers part of the work performed in support of Project AFSCG021 during the period July 1976 through October 1976 by the Structures Team of the Aircraft Compatibility Branch, Munitions Division, Air Force Armament Laboratory (AFATL), Eglin Air Force Base, Florida. Mr. William W. Dyess, Jr (DLIC) was program manager for the effort.

This report has been reviewed and is approved for publication.

FOR THE COMMANDER

Charles Petrides, GS-15
Technical Director
Munitions Division

(The reverse of this page is blank)
# TABLE OF CONTENTS

<table>
<thead>
<tr>
<th>Section</th>
<th>Title</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>INTRODUCTION.</td>
<td>1</td>
</tr>
<tr>
<td>II</td>
<td>AIR LOAD ANALYSES AND AERODYNAMIC DATA.</td>
<td>4</td>
</tr>
<tr>
<td></td>
<td>1. Design Captive Flight</td>
<td>4</td>
</tr>
<tr>
<td></td>
<td>2. Aerodynamic Coefficient Studies</td>
<td>4</td>
</tr>
<tr>
<td></td>
<td>3. Highest Air Load Case</td>
<td>12</td>
</tr>
<tr>
<td>III</td>
<td>INERTIAL LOADS.</td>
<td>15</td>
</tr>
<tr>
<td></td>
<td>1. General</td>
<td>15</td>
</tr>
<tr>
<td></td>
<td>2. Inertial Properties</td>
<td>15</td>
</tr>
<tr>
<td>IV</td>
<td>COMBINED LOADING ON VEHICLES AT CRITICAL AREAS.</td>
<td>19</td>
</tr>
<tr>
<td></td>
<td>1. General</td>
<td>19</td>
</tr>
<tr>
<td></td>
<td>2. Loads at Station 54 of 120-Inch Vehicle</td>
<td>19</td>
</tr>
<tr>
<td></td>
<td>3. Loads at Station 65 of 120-Inch Vehicle</td>
<td>19</td>
</tr>
<tr>
<td></td>
<td>4. Loads at Station 54 of 152-Inch Vehicle</td>
<td>22</td>
</tr>
<tr>
<td></td>
<td>5. Loads at Station 58 of 152-Inch Vehicle</td>
<td>22</td>
</tr>
<tr>
<td></td>
<td>6. Loads at Station 86 of 152-Inch Vehicle</td>
<td>23</td>
</tr>
<tr>
<td></td>
<td>7. Loads at Vehicle - Rack Interface of 120-Inch Vehicle</td>
<td>23</td>
</tr>
<tr>
<td></td>
<td>8. Loads at Vehicle - Rack Interface of 152-Inch Vehicle</td>
<td>23</td>
</tr>
<tr>
<td></td>
<td>9. Loads on Vehicle Fins</td>
<td>23</td>
</tr>
<tr>
<td>V</td>
<td>STRESS ANALYSIS ON VEHICLES AT CRITICAL AREAS</td>
<td>41</td>
</tr>
<tr>
<td></td>
<td>1. General</td>
<td>41</td>
</tr>
<tr>
<td></td>
<td>2. Weld at Station 54 of 120-Inch Vehicle</td>
<td>41</td>
</tr>
<tr>
<td></td>
<td>3. Skin at Station 65 of 120-Inch Vehicle</td>
<td>42</td>
</tr>
<tr>
<td></td>
<td>4. Weld at Station 54 of 152-Inch Vehicle</td>
<td>42</td>
</tr>
<tr>
<td></td>
<td>5. Skin at Station 58 of 152-Inch Vehicle</td>
<td>42</td>
</tr>
<tr>
<td></td>
<td>6. Weld at Station 86 of 152-Inch Vehicle</td>
<td>43</td>
</tr>
<tr>
<td></td>
<td>7. Strongback Area of 120-Inch Vehicle</td>
<td>43</td>
</tr>
<tr>
<td></td>
<td>8. Strongback Area of 152-Inch Vehicle</td>
<td>45</td>
</tr>
<tr>
<td></td>
<td>9. Joint at Vehicle Fin Root</td>
<td>46</td>
</tr>
<tr>
<td>VI</td>
<td>RECOMMENDATIONS AND CONCLUSIONS</td>
<td>49</td>
</tr>
<tr>
<td></td>
<td>REFERENCES.</td>
<td>50</td>
</tr>
</tbody>
</table>
# LIST OF FIGURES

<table>
<thead>
<tr>
<th>Figure</th>
<th>Title</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Outline Drawing of the 120-Inch Model</td>
<td>2</td>
</tr>
<tr>
<td>2</td>
<td>Outline Drawing of the 152-Inch Model</td>
<td>3</td>
</tr>
<tr>
<td>3</td>
<td>Captive Flight Envelope</td>
<td>5</td>
</tr>
<tr>
<td>4</td>
<td>The Aerodynamic Normal (Side) Force Coefficient Versus the Angle of Attack (Sideslip) for the 152-Inch Model</td>
<td>7</td>
</tr>
<tr>
<td>5</td>
<td>The Aerodynamic Pitching (Yawing) Moment Coefficient Versus the Angle of Attack (Sideslip) for the 152-Inch Model</td>
<td>8</td>
</tr>
<tr>
<td>6</td>
<td>The Aerodynamic Normal (Side) Force Coefficient Versus the Angle of Attack (Sideslip) for 120-Inch Model</td>
<td>9</td>
</tr>
<tr>
<td>7</td>
<td>The Aerodynamic Pitching (Yawing) Moment Coefficient Versus the Angle of Attack (Sideslip) for the 120-Inch Model</td>
<td>10</td>
</tr>
<tr>
<td>8</td>
<td>Crude and Conservative Distribution of Loads Existing on the 120-Inch Model</td>
<td>11</td>
</tr>
<tr>
<td>9</td>
<td>Crude and Conservative Distribution of Loads Existing on the 152-Inch Model (Station 54)</td>
<td>13</td>
</tr>
<tr>
<td>10</td>
<td>Crude and Conservative Distribution of Loads Existing on the 152-Inch Model (Station 86)</td>
<td>14</td>
</tr>
<tr>
<td>11</td>
<td>Design Limit Load Factor for Fuselage-Mounted Stores as per Reference 2.</td>
<td>20</td>
</tr>
<tr>
<td>12</td>
<td>Maximum Resultant for Inertial Load Factor ($\eta$) and Aerodynamic Angle</td>
<td>21</td>
</tr>
<tr>
<td>13</td>
<td>Maximum Axial Force on the Aft Lug Versus Dynamic Pressure for the 120-Inch Vehicle</td>
<td>25</td>
</tr>
<tr>
<td>14</td>
<td>Maximum Axial Force on the Forward Lug Versus Dynamic Pressure for the 120-Inch Vehicle</td>
<td>26</td>
</tr>
<tr>
<td>15</td>
<td>Maximum Side Force on the Aft Lug Versus Dynamic Pressure for the 120-Inch Vehicle</td>
<td>27</td>
</tr>
<tr>
<td>16</td>
<td>Maximum Side Force on the Forward Lug Versus Dynamic Pressure for the 120-Inch Vehicle</td>
<td>28</td>
</tr>
<tr>
<td>17</td>
<td>Maximum Vertical Force on the Aft Lug Versus Dynamic Pressure for the 120-Inch Vehicle</td>
<td>29</td>
</tr>
<tr>
<td>18</td>
<td>Maximum Vertical Force on the Forward Lug Versus Dynamic Pressure for the 120-Inch Vehicle</td>
<td>30</td>
</tr>
<tr>
<td>19</td>
<td>Maximum Aft Sway Brace Reaction Versus Dynamic Pressure for the 120-Inch Vehicle</td>
<td>31</td>
</tr>
</tbody>
</table>
LIST OF FIGURES (CONCLUDED)

<table>
<thead>
<tr>
<th>Figure</th>
<th>Title</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>Maximum Forward Sway Brace Reaction Versus Dynamic Pressure for the 120-Inch Vehicle</td>
<td>32</td>
</tr>
<tr>
<td>21</td>
<td>Maximum Axial Force on the Aft Lug Versus Dynamic Pressure for the 152-Inch Vehicle</td>
<td>33</td>
</tr>
<tr>
<td>22</td>
<td>Maximum Axial Force on the Forward Lug Versus Dynamic Pressure for the 152-Inch Vehicle</td>
<td>34</td>
</tr>
<tr>
<td>23</td>
<td>Maximum Side Force on the Aft Lug Versus Dynamic Pressure for the 152-Inch Vehicle</td>
<td>35</td>
</tr>
<tr>
<td>24</td>
<td>Maximum Side Force on the Forward Lug Versus Dynamic Pressure for the 152-Inch Vehicle</td>
<td>36</td>
</tr>
<tr>
<td>25</td>
<td>Maximum Vertical Force on the Aft Lug Versus Dynamic Pressure for the 152-Inch Vehicle</td>
<td>37</td>
</tr>
<tr>
<td>26</td>
<td>Maximum Vertical Force on the Forward Lug Versus Dynamic Pressure for the 152-Inch Vehicle</td>
<td>38</td>
</tr>
<tr>
<td>27</td>
<td>Maximum Aft Sway Brace Reaction Versus Dynamic Pressure for the 152-Inch Vehicle.</td>
<td>39</td>
</tr>
<tr>
<td>28</td>
<td>Maximum Forward Sway Brace Reaction Versus Dynamic Pressure for the 152-Inch Vehicle</td>
<td>40</td>
</tr>
<tr>
<td>29</td>
<td>Fin Attach Detail</td>
<td>47</td>
</tr>
</tbody>
</table>

LIST OF TABLES

<table>
<thead>
<tr>
<th>Table</th>
<th>Title</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Modified Values of αs and βs for the Four Centerline-Mounted Flight Maneuvers Condition With Varying q</td>
<td>6</td>
</tr>
</tbody>
</table>

(The reverse of this page is blank)
SECTION I

INTRODUCTION

The Aircraft Compatibility Branch of the Air Force Armament Laboratory is responsible for reviewing and issuing flight recommendations on all stores flown on Air Force Systems Command aircraft (Reference 1). This report documents the loads and stress analysis performed on two parachute testing vehicles (126-AR00036 and 126-AR00037) used by the 6511th Test Squadron at El Centro, California. These vehicles, a 120-inch model and a 152-inch model, are shown in Figures 1 and 2, respectively. This analysis was necessitated by a request to increase the maximum allowable flight speed of the F-4C/D aircraft with these stores installed on the centerline station.

The assumptions made in the analysis are as follows:

1. The vehicle was assumed to be of homogeneous mass distribution from the center of gravity (cg) forward and from the cg aft. This will generate conservative shears and moments but, due to the composition of the vehicle, the assumption is not unreasonable.

2. A reduced cg and cg, as defined in MIL-A-8591D (Reference 2), are used. These reduced values were recommended by McDonnell Aircraft Co. for F-4 centerline application (Reference 3).

3. The maximum stress in the skin would occur just forward or just aft of the lug-strongback section. This is due to assumption 1 and the manner in which the loads are transmitted through the strongback area. Since the section forward of the lug-strongback area is solid material and would have a small moment applied, it is of little concern since the margins would be very high. Thus the only skin area to be investigated will be that just aft of the lug-strongback section.

4. The internal structure in rear of vehicles is not load bearing. This assumption must be made since no engineering drawing exists and thus exact load relationships cannot be determined. This assumption will result in a conservative stress analysis.
MATERIAL: Nose section is a 2000-pound general-purpose bomb casing, 1/2-inch steel forward-most volume contains 1.2 ft³ of solid lead. Final 66 inches is 1/4-inch 1020 cold rolled mild steel.

WELD: A butt weld joins these sections.

Figure 1. Outline Drawing of the 120-Inch Model
MATERIAL: Nose section is a 2000-pound general-purpose bomb casing, 1/2-inch steel. First 18 inches are filled with solid lead. Final 98 inches are 1/4-inch 1020 cold rolled mild steel.

WELD: Nose and aft cylinders are butt welded.

Figure 2. Outline Drawing of the 152-Inch Model
SECTION II
AIR LOAD ANALYSES AND AERODYNAMIC DATA

1. DESIGN CAPTIVE FLIGHT

The design captive flight envelope is limited to Mach 0.98. To determine the aerodynamic angles to be used in the analyses, the equations presented in Reference 2, as modified by McDonnell Aircraft Company information presented in Reference 3, are used with dynamic pressure (q) values taken from the perimeter of the captive flight envelope as shown in Figure 3. These equations (with angles in degrees) for the centerline mounted condition are:

- Points (1) and (3) (Reference 2)
  \[
  \alpha_s = -3 \text{ to } \frac{13,000}{q} \\
  \beta_s = \pm \frac{6500}{q}
  \]

- Points (2) and (4) (Reference 2)
  \[
  \alpha_s = 0 \text{ to } -\frac{13,000}{q} \\
  \beta_s = \pm \frac{6500}{q}
  \]

Table 1 shows the various values of \( \alpha_s \) and \( \beta_s \) for the four points when the q is varied from 2400 lbf/ft\(^2\) to 800 lbf/ft\(^2\). Considering the design envelope, q can be held at 1200 lbf/ft\(^2\).

2. AERODYNAMIC COEFFICIENT STUDIES

The first study was performed to determine the freestream aerodynamic coefficients for these two models. Figures 4 through 7 depict these coefficients as a function of the angle of attack or sideslip. In addition, a value of 0.4 was used for the axial force coefficient for both models.

The second study computed the distributed aerodynamic loads over the body. For the first case the 120-inch model was segmented at the weldment of station 54. The results of this study are shown in Figure 8. Load distribution for the 152-inch model was considered in two ways: First with a
Figure 3. Captive Flight Envelope
### Table 1. Modified Values of $\alpha$s and $\beta$s for the Four Centerline-Mounted Flight Maneuvers Condition with Varying $q$

<table>
<thead>
<tr>
<th>$q$ (lbf/ft²)</th>
<th>$\alpha$ 1 and 3 (deg)</th>
<th>$\alpha$ 2 and 4 (deg)</th>
<th>$\beta$s 1, 2, 3, and 4 (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>800</td>
<td>-3 to 16.25</td>
<td>-16.25 to 0</td>
<td>±8.13</td>
</tr>
<tr>
<td>1000</td>
<td>-3 to 13.00</td>
<td>-13.00 to 0</td>
<td>±6.50</td>
</tr>
<tr>
<td>1200</td>
<td>-3 to 10.83</td>
<td>-10.83 to 0</td>
<td>±5.42</td>
</tr>
<tr>
<td>1400</td>
<td>-3 to 9.29</td>
<td>-9.29 to 0</td>
<td>±4.64</td>
</tr>
<tr>
<td>1600</td>
<td>-3 to 8.13</td>
<td>-8.13 to 0</td>
<td>±4.06</td>
</tr>
<tr>
<td>1800</td>
<td>-3 to 7.22</td>
<td>-7.22 to 0</td>
<td>±3.61</td>
</tr>
<tr>
<td>2000</td>
<td>-3 to 6.50</td>
<td>-6.50 to 0</td>
<td>±3.25</td>
</tr>
<tr>
<td>2200</td>
<td>-3 to 5.91</td>
<td>-5.91 to 0</td>
<td>±2.95</td>
</tr>
<tr>
<td>2400</td>
<td>-3 to 5.42</td>
<td>-5.42 to 0</td>
<td>±2.71</td>
</tr>
</tbody>
</table>
Aerodynamic reference point is 13 inches aft of forward lug

Aerodynamic reference area is 414.72 square inches

Figure 4. The Aerodynamic Normal (Side) Force Coefficient Versus the Angle of Attack (Sideslip) for the 152-Inch Model
Aerodynamic reference point is 13 inches aft of the forward lug.

Aerodynamic reference length is 23.04 inches.

Aerodynamic reference area is 414.72 square inches.

Figure 5. The Aerodynamic Pitching (Yawing) Moment Coefficient Versus the Angle of Attack (Sideslip) for the 152-Inch Model.
Aerodynamic reference point is 13 inches aft of forward lug.

Aerodynamic reference area is 414.72 square inches.

Figure 6. The Aerodynamic Normal (Side) Force Coefficient Versus the Angle of Attack (Sideslip) for 120-Inch Model.
Aerodynamic reference point is 13 inches aft of the forward lug

Aerodynamic reference length is 23.04 inches

Aerodynamic reference area is 414.72 square inches

Figure 7. The Aerodynamic Pitching (Yawing) Moment Coefficient Versus the Angle of Attack (Sideslip) for the 120-Inch Model
where:

\[ N_1 = 215 \text{ lb} \]
\[ N_2 = 325 \text{ lb} \]
\[ S_1 = 215 \beta \text{ lb} \]
\[ S_2 = 325 \beta \text{ lb} \]
\[ W_1 = 0.551W \text{ lb} \]
\[ W_2 = 0.449W \text{ lb} \]
\[ W = \text{Weight of 120-Inch Model} \]

Figure 8. Crude and Conservative Distribution of Loads Existing on the 120-Inch Model
break at the weldment of station 54, shown in Figure 9; and, second, with a break at the weldment of station 86, shown in Figure 10. These analyses were conservative in nature.

3. HIGHEST AIR LOAD CASE

Using the constraints of the problem and the data in Table 1, it can be seen that the maximum angle of attack is 10.83 degrees and the minimum angle of attack is -10.83 degrees. Also, the maximum and minimum angle of sideslip is ±4.64 and -4.64 degrees, respectively. Merely calculating the loads corresponding to these angles may not suffice. In fact, MIL-A-8591D states that all angles in the range should be examined. The reason for this requirement is to insure that if the force or moment curves should break, i.e., change slope abruptly, the final answer will still depict the highest values possible.
where:

\[ N_5 = 213 \text{ lb} \]
\[ N_6 = 458 \text{ lb} \]
\[ S_5 = 213 \text{ lb} \]
\[ S_6 = 458 \text{ lb} \]
\[ W_5 = 0.405 \text{ W lb} \]
\[ W_6 = 0.595 \text{ W lb} \]
\[ W = \text{Weight of 152-Inch Model} \]

Figure 9. Crude and Conservative Distribution of Loads Existing on the 152-Inch Model (Station S4)
where:

\[
\begin{align*}
N_9 &= 860 \text{ lb} \\
N_{10} &= 323 \text{ lb} \\
S_9 &= 860 \text{ lb} \\
S_{10} &= 323 \text{ lb} \\
W_9 &= 0.727 W \text{ lb} \\
W_{10} &= 0.273 W \text{ lb}
\end{align*}
\]

Figure 10. Crude and Conservative Distribution of Loads Existing on the 152-Inch Model (Station 86)
SECTION III
INERTIAL LOADS

1. GENERAL

Both models must be capable of sustaining the inertial loads as predicted by MIL-A-8591D. The particular section of this specification employed was that pertaining to stores carried on the centerline of an aircraft. No modifications of the inertial parameters were made corresponding to those made with regard to the aerodynamic coefficients in Section II.

2. INERTIAL PROPERTIES

The weights and centers of gravity (cg) of all sections of interest must be computed. Continuing in the view of using simplifying but conservative assumptions, assume that the model is of homogeneous mass distribution fore and aft of the cg. This means that half of the total weight of the model in question is evenly distributed along the space forward of the cg and half of the weight aft. Thus, the linear weight for the 120-inch model can be computed as

\[ W_{120}^{a} = \frac{1}{2} \frac{W}{120-46 1/2} \]

\[ W_{120}^{f} = \frac{W}{147} \]

\[ W_{120}^{e} = \frac{W}{93} \]

where

\[ W_{120}^{a} \] is the linear weight of the section aft of the overall cg of the 120-inch model

\[ W_{120}^{f} \] is the linear weight of the section forward of the overall cg of the 120-inch model

\[ W \] is the weight of the model

and the linear weight for the 152-inch model can be computed as
\[
W_{1\text{152}}^a = \frac{1}{2} W/(152 - 31) \\
W_{1\text{152}}^f = \frac{W}{242} \\
W_{1\text{152}}^f = \frac{W}{62}
\]

where

\[W_{1\text{152}}^a\] is the linear weight of the section aft of the overall cg of the 152-inch model

\[W_{1\text{152}}^f\] is the linear weight of the section forward of the overall cg of the 152-inch model.

Now with these linearized weights, it is possible to obtain the values desired. Representative values are shown in Figures 8 and 9 and calculations are as follows:

a. Station 0 to Station 54 of the 120-inch vehicle

\[W_1 = (46 1/2) W_{1\text{120}}^f + (54 - 46 1/2) W_{1\text{120}}^a\]

\[W_1 = 0.551W\]

\[(cg)_1 = 26.44 \text{ (Station)}\]

b. Station 54 to Station 120 of 120-inch vehicle

\[W_2 = (120 - 46 1/2) W_{1\text{120}}^a\]

\[W_2 = 0.449W\]

\[(cg)_2 = 87.00 \text{ (Station)}\]
c. Station 0 to Station 65 of 120-inch vehicle

\[ W_3 = (46 \ 1/2) W_{120}^f + (65 - 46 \ 1/2) W_{120}^a \]

\[ W_3 = 0.626W \]

\[ (cg)_3 = 29.79 \text{ (Station)} \]

d. Station 65 to Station 120 of 120-inch vehicle

\[ W_4 = (120 - 65) W_{120}^a \]

\[ W_4 = 0.374W \]

\[ (cg)_4 = 92.50 \text{ (Station)} \]

e. Station 0 to Station 54 of 152-inch vehicle

\[ W_5 = (31) W_{152}^f + (54 - 31) W_{152}^a \]

\[ W_5 = 0.595W \]

\[ (cg)_5 = 19.81 \text{ (Station)} \]

f. Station 54 to Station 152 of 152-inch vehicle

\[ W_6 = (152 - 54) W_{152}^a \]

\[ W_6 = 0.405W \]

\[ (cg)_6 = 103.00 \text{ (Station)} \]
g. Station 0 to Station 58 of 152-inch vehicle

\[ W_7 = (31) W_{152}^f + (58 - 31) W_{152}^a \]

\[ W_7 = 0.612W \]

\( (cg)_{7} = 20.81 \) (Station)

h. Station 58 to Station 152 of 152-inch vehicle

\[ W_8 = (152 - 58) W_{152}^a \]

\[ W_8 = 0.388W \]

\( (cg)_{8} = 105.00 \) (Station)

i. Station 0 to Station 86 of 152-inch vehicle

\[ W_9 = (31) W_{152}^f + (86 - 31) W_{152}^a \]

\[ W_9 = 0.727W \]

\( (cg)_{9} = 28.93 \) (Station)

j. Station 86 to Station 152 of 152-inch vehicle

\[ W_{10} = (152 - 86) W_{152}^a \]

\[ W_{10} = 0.273W \]

\( (cg)_{10} = 119.00 \) (Station)
SECTION IV

COMBINED LOADING ON VEHICLES AT CRITICAL AREAS

1. GENERAL

To make the analysis as conservative as possible, the maximum angle of sideslip and attack were considered with the maximum inertial factors determined for a rolling-pull-out (RPO) maneuver. This is corner 2 of Figure 11. The aerodynamic angles are assumed to be of appropriate sense to allow the aerodynamic and inertial loads to couple.

Since the cross section is symmetrical, an equivalent load factor and aerodynamic angle as shown in Figure 12 can be obtained. In addition, the total weight spread of each vehicle will be examined.

2. LOADS AT STATION 54 OF 120-INCH VEHICLE

From Figure 8, the shear at the cross section would be

\[ S_{54/120} = N_2 + W_2 \]

\[ = 215\alpha + 0.449 \, W_\eta \]

\[ = 215 \times (11.78) + (0.449) \times (2600) \times (8.79) \]

\[ = 12,794 \, \text{lb} \]

and the moment would be

\[ M_{54/120} = (89 \times \frac{1}{2} - 54) \, N_2 + (87 - 54) \, W_2 \]

\[ = (35.5) \, N_2 + (33) \, W_2 \]

\[ = 428,538 \, \text{in-lb} \]

3. LOADS AT STATION 65 OF 120-INCH VEHICLE

From Figure 8, the shear at the cross section would be

\[ S_{65/120} = N_4 + W_4 \]

\[ = 215\alpha + 0.374 \, W_\eta \]

\[ = 215 \times (11.78) + (0.374) \times (2600) \times (8.79) \]

\[ = 11,080 \, \text{lb} \]
Figure 11. Design Limit Load Factor for Fuselage-Mounted Stores as per Reference 2
Figure 12. Maximum Resultant for Inertial Load Factor ($\eta$) and Aerodynamic Angle
and the moment would be
\[ M_{65/120} = (89.5 - 65) N_4 + (92.5 - 65) W_4 \]
\[ = 297,104 \text{ in-lb} \]

4. LOADS AT STATION 54 OF 152-INCH VEHICLE

From Figure 9, the shear at the cross section would be
\[ S_{54/152} = N_6 + W_6 \]
\[ = 458\alpha + 0.595 W_7 \]
\[ = 458 (11.78) + (0.595) (6275) (8.79) \]
\[ = 32,818 \text{ lb} \]
and the moment would be
\[ M_{54/152} = (106.68 - 54) N_6 + (103 - 54) W_6 \]
\[ = 1,892,330 \text{ in-lb} \]

5. LOADS AT STATION 58 OF 152-INCH VEHICLE

From Figure 9, the shear at the cross section would be
\[ S_{58/152} = N_8 + W_8 \]
\[ = 458\alpha + 0.388 W_7 \]
\[ = 458 (11.78) + (0.388) (6275) (8.79) \]
\[ = 26,796 \text{ lb} \]
and the moment would be
\[ M_{58/152} = (106.68 - 58) N_6 + (105.00 - 58) W_6 \]
\[ = 1,268,487 \text{ in-lb} \]
6. LOADS AT STATION 86 OF 152-INCH VEHICLE

From Figure 10, the shear at the cross section would be

\[ S_{86/152} = N_{10} + W_{10} \]

\[ = 323\alpha + 0.273 W_n \]

\[ = 323 (11.78) + 0.273 (6275) (8.79) \]

\[ = 18,862 \text{ lb} \]

and the moment would be

\[ M_{86/152} = (121.56 - 86) N_{10} + (119 - 86) W_{10} \]

\[ = 632,215 \text{ in-lb} \]

7. LOADS AT VEHICLE - RACK INTERFACE OF 120-INCH VEHICLE

A run using the procedures of MIL-A-8591 was accomplished. The results of this analysis are presented in Figures 13 through 20. The support data for these relationships may be obtained from the author upon request.

8. LOADS AT VEHICLE - RACK INTERFACE OF 152-INCH VEHICLE

An analysis similar to the one above was accomplished for the 152-inch vehicle. The results are presented in Figures 21 through 28. The support data may be obtained from the author upon request.

9. LOADS ON VEHICLE FINS

The fins for both vehicles have a wetted surface area of 150 square inches each (6x25). Assuming that the maximum normal force coefficient will not exceed the flat plate drag coefficient of 1.28 the maximum normal force \( N_F \) is computed as

\[ N_F = C_N q A \]

\[ N_F = (1.28) (1200) (1.04) \]

\[ N_F = 1600 \text{ lb} \]

The weight of the fin is unknown, but it is assumed that the inertial loads would be small compared to the aerodynamic loads.
Thus, conservatively assuming that the load is acting at the fin centroid, we have the following shear and moment at the fin root

\[
S = 1600 \text{ lb}
\]
\[
M = 3(1600)
\]
\[
M = 4800 \text{ in-lb.}
\]
**Figure 13.** Maximum Axial Force on the Aft Lug Versus Dynamic Pressure for the 120-Inch Vehicle
Figure 14. Maximum Axial Force on the Forward Lug Versus Dynamic Pressure for the 120-Inch Vehicle
Figure 15. Maximum Side Force on the Aft Lug Versus Dynamic Pressure for the 120-Inch Vehicle
Figure 16. Maximum Side Force on the Forward Lug Versus Dynamic Pressure for the 120-Inch Vehicle
Figure 17. Maximum Vertical Force on the Aft Lug Versus Dynamic Pressure for the 120-Inch Vehicle
Figure 18. Maximum Vertical Force on the Forward Lug Versus Dynamic Pressure for the 120-Inch Vehicle
Figure 19. Maximum Aft Sway Brace Reaction Versus Dynamic Pressure for the 120-Inch Vehicle
Figure 20. Maximum Forward Sway Brace Reaction Versus Dynamic Pressure for the 120-Inch Vehicle
Figure 21. Maximum Axial Force on the Aft Lug Versus Dynamic Pressure for the 152-Inch Vehicle
Figure 22. Maximum Axial Force on the Forward Lug Versus Dynamic Pressure for the 152-Inch Vehicle
Figure 23. Maximum Side Force on the Aft Lug Versus Dynamic Pressure for the 152-Inch Vehicle
Figure 24. Maximum Side Force on the Forward Lug Versus Dynamic Pressure for the 152-Inch Vehicle
Figure 25. Maximum Vertical Force on the Aft Lug Versus Dynamic Pressure for the 152-Inch Vehicle
Figure 26. Maximum Vertical Force on the Forward Lug Versus Dynamic Pressure for the 152-Inch Vehicle
### Figure 27. Maximum Aft Sway Brace Reaction Versus Dynamic Pressure for the 152-Inch Vehicle

<table>
<thead>
<tr>
<th>Dynamic Pressure (in)</th>
<th>Aft Sway Brace Reaction (in)</th>
</tr>
</thead>
<tbody>
<tr>
<td>200.02</td>
<td>64.737.90</td>
</tr>
<tr>
<td>400.00</td>
<td>64.942.79</td>
</tr>
<tr>
<td>599.99</td>
<td>61.147.69</td>
</tr>
<tr>
<td>799.98</td>
<td>57.352.29</td>
</tr>
<tr>
<td>999.96</td>
<td>53.557.49</td>
</tr>
<tr>
<td>1199.35</td>
<td>49.762.39</td>
</tr>
<tr>
<td>1399.94</td>
<td>45.967.29</td>
</tr>
<tr>
<td>1599.93</td>
<td>42.172.19</td>
</tr>
<tr>
<td>1799.91</td>
<td>38.377.09</td>
</tr>
<tr>
<td>1999.90</td>
<td>34.581.38</td>
</tr>
<tr>
<td>2199.89</td>
<td>34.581.38</td>
</tr>
</tbody>
</table>
Figure 28. Maximum Forward Sway Brace Reaction Versus Dynamic Pressure for the 152-Inch Vehicle
1. GENERAL

For the 0.25-inch skin, both at the welds and elsewhere, the moment of inertia is

\[ I = 0.25\pi (r_2^4 - r_1^4) \]

\[ I = 0.25\pi (11.5^4 - 11.25^4) \]

\[ I = 11.56 \text{ in}^4 \]

The maximum bending stress, \( F_b \), will occur at the greatest distance from the neutral axis, i.e., at \( r_2 \). The ultimate stress for the welds, \( F_{ub} \), is assumed at 45,000 psi and that for the skin, \( F_{sb} \), at 55,000 psi (Reference 4). For further conservation and to make the analysis non-redundant, assume the aft lug-sway brace combination does not react any of the shear load or moment being generated.

For the lug well analysis, assume that the lug well base is attached to the strongback area by a 0.375 fillet weld (Reference 5). Since the base is 3.5 inches in diameter, the total weld length is 11 inches.

2. WELD AT STATION 54 OF 120-INCH VEHICLE

To determine the maximum bending stress

\[ F_b = \frac{MC}{I} \]

\[ F_b = \frac{(428,538) (11.5)}{1156} \]

\[ F_b = 4263 \text{ psi} \]

Then the margin of safety is

\[ MS = \frac{45,000}{1.5 \times 4263} - 1 \]

\[ MS = \text{High} \]
3. SKIN AT STATION 65 OF 120-INCH VEHICLE

To determine the maximum bending stress

\[ F_b = \frac{M C}{I} \]

\[ F_b = \frac{(297,104) (11.5)}{1156} \]

\[ F_b = 2955 \text{ psi} \]

and the margin of safety is

\[ MS = \frac{55,000}{1.5 F_b} -1 \]

\[ MS = \text{High} \]

4. WELD AT STATION 54 OF 152-INCH VEHICLE

To determine the maximum bending stress

\[ F_b = \frac{M C}{I} \]

\[ F_b = \frac{(1,892,330) (11.5)}{1156} \]

\[ F_b = 18,825 \text{ psi} \]

and the margin of safety is

\[ MS = \frac{45,000}{1.5 F_b} -1 \]

\[ MS = 0.59 \]

5. SKIN AT STATION 58 OF 152-INCH VEHICLE

To determine the maximum bending stress

\[ F_b = \frac{M C}{I} \]

\[ F_b = \frac{(1,268,487) (11.5)}{1156} \]

\[ F_b = 12,619 \text{ psi} \]
and the margin of safety is
\[ MS = \frac{55,000}{1.5 F_b} - 1 \]
\[ MS = 2.91 \]

6. WELD AT STATION 86 OF 152-INCH VEHICLE

To determine the maximum bending stress
\[ F_b = \frac{MC}{I} \]
\[ F_b = \frac{632,215}{1156} \frac{(11.5)}{1156} \]
\[ F_b = 6289 \]
and the margin of safety is
\[ MS = \frac{45,000}{1.5 F_b} - 1 \]
\[ MS = 3.77 \]

7. STRONGBACK AREA OF 120-INCH VEHICLE

The shear in the lug well weld is
\[ F_s = \frac{P}{(11)(3/8)} \]
\[ F_s = 0.2424P \]
For the forward lug
\[ F_s = (0.2424) (32,400) \]
\[ F_s = 7854 \text{ psi} \]
and the margin of safety is
\[ MS = \frac{32,000}{(1.5)(7856)} - 1 \]
\[ MS = 1.72 \]
For the aft lug

\[ F_s^\prime \approx (0.2424) (30,000) \]

\[ F_s = 7272 \text{ psi} \]

and the margin of safety is

\[ MS = \frac{32,000}{(1.5)(7272)} \]

\[ MS = 1.93 \]

Now consider the skin surrounding the lug well and just beyond the weld. The diameter of this circle is

\[ d = 3.5 + 0.375 + 0.375 \]

\[ d = 4.25 \text{ inches} \]

Thus

\[ F_s = \frac{P}{\pi(4.25)t} \]

\[ F_s = 0.0749 \frac{P}{t} \]

For the forward lug area, the surrounding skin is 0.5 inch thick. Thus,

\[ F_s = 0.0749 \frac{32,400}{0.5} \]

\[ F_s = 4853 \text{ psi} \]

and the margin of safety is

\[ MS = \frac{32,000}{(1.5)(4853)} \]

\[ MS = 3.39 \]
For the aft lug area, the surrounding skin is 0.25 inch thick. Thus
\[ F_s = 0.0749 \frac{30,000}{0.25} \]
\[ F_s = 8988 \text{ psi} \]
and the margin of safety is
\[ MS = \frac{32,000}{(1.5)(8988)} - 1 \]
\[ MS = 1.37 \]

8. STRONGBACK AREA OF 152-INCH VEHICLE

The shear in the lug well weld is
\[ F_s = \frac{P}{(11)(3/8)} \]
\[ F_s = 0.2424P \]
For the forward lug
\[ F_s = (0.242)(86,000) \]
\[ F_s = 20,812 \text{ psi} \]
and the margin of safety is
\[ MS = \frac{32,000}{(1.5)(20,812)} - 1 \]
\[ MS = 0.025 \]
For the aft lug
\[ F_s = (0.242)(78,000) \]
\[ F_s = 18,876 \text{ psi} \]
and the margin of safety is
\[ MS = \frac{32,000}{(1.5)(18,876)} - 1 \]
\[ MS = 0.13 \]
Now consider the skin surrounding the lug well and just beyond the weld. The diameter of this circle is

\[ d = 3.5 + 0.375 + 0.375 \]
\[ d = 4.25 \text{ inches} \]

Thus

\[ F_s = \frac{P}{\pi(4.25)t} \]
\[ F_s = 0.0749 \frac{P}{t} \]

For the forward lug area, the surrounding skin is 0.5 inch thick. Thus

\[ F_s = 0.0749 \frac{86,000}{0.5} \]
\[ F_s = 12,882 \text{ psi} \]

and the margin of safety is

\[ MS = \frac{32,000}{(1.5)(12,882)} - 1 \]
\[ MS = 0.66 \]

For the aft lug area, the surrounding skin is 0.25 inch thick. Thus

\[ F_s = 0.0749 \frac{78,000}{0.25} \]
\[ F_s = 23,368 \text{ psi} \]

and the margin of safety is

\[ MS = \frac{32,000}{(1.5)(23,368)} - 1 \]
\[ MS = -0.09 \]

9. **JOINT AT VEHICLE FIN ROOT**

The fin is connected to the vehicle by a 1x1x1/8x28-inch angle iron. The leg attached to the vehicle is connected by a 1/8-inch fillet weld.
Figure 29. Fin Attach Detail
The other leg is connected to the fin by way of six 1/4-inch-diameter bolts designed to 120,000 psi in tension and 25,000 psi in shear. Assuming that the moment is reacted by the bolts coupled with the reaction at the skin-angle connection (see Figure 29) and that the bolt line is centered 1/2 inch from angle, then the following stress is computed.

\[ F_t = \frac{2N}{6A_b} + \frac{S}{6A_b} \]

where \( A_b \) is the area of the bolts

\[ F_t = \frac{(2)(4800)}{(6 \times 0.2)} + \frac{(1600)}{(6)(0.2)} \]

\[ F_t = 9333 \text{ psi} \]

and thus the margin of safety is

\[ MS = \frac{120,000}{(1.5)(9333)} - 1 \]

\[ MS = \text{High} \]

Now assume that weld reacts the moment as a couple with the edge of the angle then the shear is

\[ F_s = \frac{(1)M}{(1/8)(25)} \]

\[ F_s = \frac{4800}{(1/8)(25)} \]

\[ F_s = 1536 \]

Thus the margin of safety is

\[ MS = \frac{32,000}{(1.5)(1536)} - 1 \]

\[ MS = \text{High} \]
The load and subsequent stress analysis presented within this document resulted in sufficient margin of safety throughout the envelope to structurally recommend flight to the desired limits. The only weak area indicated by the analysis was the aft lug well area of the heaviest weight item. Since the 6511th Test Squadron already inspects this area after each flight it is not considered necessary to recommend any additional analysis of this area.

This analysis was meant to be, and is, a very rough analysis. Its purpose was to determine if these items could survive flight on an F-4 as cheaply and quickly as possible. To this end, large conservatisms have been brought into the analysis. Had any structural member shown failure during the analysis, a less conservative analysis would have been necessary. However, since no such significant problem was encountered, this additional study was not necessary.
REFERENCES


INITIAL DISTRIBUTION

<table>
<thead>
<tr>
<th>Institution</th>
<th>Quantity</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hq USAF/RIDQRM</td>
<td>2</td>
</tr>
<tr>
<td>Hq USAF/SAMI</td>
<td>1</td>
</tr>
<tr>
<td>AFSC/DLCA</td>
<td>1</td>
</tr>
<tr>
<td>ASD/ENFEA</td>
<td>1</td>
</tr>
<tr>
<td>DDC</td>
<td>2</td>
</tr>
<tr>
<td>NSWC/Tech Lib/White Oak</td>
<td>2</td>
</tr>
<tr>
<td>Naval Ordnance Stn/Tech Lib</td>
<td>1</td>
</tr>
<tr>
<td>USNWC/Code 533</td>
<td>1</td>
</tr>
<tr>
<td>AFATL/DL</td>
<td>1</td>
</tr>
<tr>
<td>AFATL/DLODL</td>
<td>9</td>
</tr>
<tr>
<td>AFATL/DLJ</td>
<td>1</td>
</tr>
<tr>
<td>AFATL/DLJC</td>
<td>10</td>
</tr>
<tr>
<td>AFATL/DLODR</td>
<td>1</td>
</tr>
<tr>
<td>AFATL/DLJA</td>
<td>1</td>
</tr>
<tr>
<td>6511th Test Sq/DORER</td>
<td>10</td>
</tr>
<tr>
<td>AUL (AUL-LSE-70-239)</td>
<td>2</td>
</tr>
<tr>
<td>TAWC/TRADOCLO</td>
<td>1</td>
</tr>
<tr>
<td>Ogden ALC/MMMM</td>
<td>2</td>
</tr>
<tr>
<td>AFIS/INTA</td>
<td>1</td>
</tr>
<tr>
<td>Hq TAC/DRA</td>
<td>1</td>
</tr>
<tr>
<td>Hq USAFE/DDQ</td>
<td>1</td>
</tr>
<tr>
<td>Hq PACAF/DDO</td>
<td>1</td>
</tr>
<tr>
<td>TAC/INA</td>
<td>1</td>
</tr>
<tr>
<td>US Army TRADOC Systems Analysis Activity/ATAA-SL</td>
<td>1</td>
</tr>
<tr>
<td>NSWC/Dahlgren Lab</td>
<td>1</td>
</tr>
</tbody>
</table>

(The reverse of this page is blank)