The Kelvin wave and the Madden-Julian Oscillation in aqua-planet simulations by the Naval Research Laboratory Spectral Element Atmospheric Model (NSEAM)

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5 December 2007

Submitted to Geophysical Research Letters

The Naval Research Laboratory (NRL) Spectral Element Atmospheric Model (NSEAM) with full physics included is used to investigate the organization and propagation of equatorial waves under the aqua-planet conditions. The sensitivity of the simulation to the distribution of the vertical levels and selected details of the model’s precipitation physics is discussed utilizing simulated convective precipitation with the aid of the time-longitude plots and spectral diagrams. It is shown that the Kelvin wave simulation depends strongly on the details of the vertical level distribution and the methods associated with the lifting condensation level. While significant variability is found among the aqua-planet simulations by global atmospheric models, the new model captures the essential interaction between the dynamics and physics of the atmosphere such that the simulated speed and spectrum of the eastward propagating Kelvin waves
The Kelvin Wave and the Madden-Julian Oscillation in Aqua-plant Simulations by the Naval Research Laboratory Spectral Element Atmospheric Model (NSEAM)
and the signature of the Madden-Julian Oscillation are as approximately predicted by simplified theory and limited observations.

1. Introduction

The US Navy has recently developed a new high-accuracy global atmospheric model, which scales efficiently on current and future state-of-the-art computing platforms: the Naval Research Laboratory (NRL) Spectral Element Atmospheric Model, or NSEAM. Its dynamical core [Giraldo and Rosmond, 2004] is based on “spectral element” methods projected to three-dimensional Cartesian coordinates, which effectively eliminate the pole singularity problem of spherical coordinates and combine the local domain decomposition property of finite-element methods with the high-order accuracy of spectral transform methods.

NSEAM can adopt any horizontal model grid, fixed or variable, and various time integrators such as Eulerian [Giraldo and Rosmond, 2004], semi-implicit [Giraldo, 2005], semi-Lagrangian [Giraldo et al., 2003], or hybrid Eulerian-Lagrangian semi-implicit [Giraldo, 2006] methods. Its spectral element formulation maintains the high-order accuracy of spherical harmonics that the current Navy’s global atmospheric model is based on, while it offers flexibility to use any form of variable grid to enhance horizontal grid resolutions in strategic regions. Its dynamical core scales efficiently, i.e., allows the use of large numbers of processors, and was validated using various barotropic and baroclinic test cases [Giraldo and Rosmond, 2004]. The model can be discretized...
vertically with any grid, but the mass and energy conserving flux-form of the finite-difference method on the terrain-following (σ) coordinate is first selected for comparison with existing models.

For this study, we modify and expand the NSEAM dynamical core to include the physics package used in the operational version of the Navy Operational Global Atmospheric Prediction System or NOGAPS (Hogan and Rosmond [1991]; see also Kim [2007] for a list of recent model physics improvements), but without the land surface parameterization. We select the hexahedral grid that consists of six faces of a hexahedron, each of which contains a desired number of quadrilateral elements [Giraldo and Rosmond, 2004]. The grid can be stretched to enhance the resolution of a selected region, e.g., the tropics.

Among the methods to validate an atmospheric model is to force the model under controlled and simplified sets of boundary and initial conditions so that the results can be interpreted in a relatively straightforward manner and also inter-comparable to those of other similar models although the correct solution is not quite known except by simplified theory and limited indirect observations. A good recent example is the aqua-planet experiments proposed by Neale and Hoskins [2001a, b] in which the earth is covered with flat water only. These experiments provide a useful and convenient test-bed for investigating the interaction between the dynamics and physics in atmospheric models.

In this study, we validate NSEAM by configuring it for aqua-planet experiments following Neale and Hoskins [2001a]. We perform various sensitivity experiments in order to improve the aqua-planet simulation. Sensitivity of aqua-planet simulations to horizontal resolution was studied previously. For example, Lorant and Royer [2001]
found from general circulation model (GCM) experiments that with higher resolution the
convective cells are more intensified and concentrated, being accompanied by improved
simulation of equatorial waves that modulate near-equatorial convection. Sensitivity of
aqua-planet simulations to vertical resolution was also studied earlier. For example,
Inness et al. [2001] compared between 19 and 30 (unevenly-spaced) layer versions of
their GCM and discussed its implications for Madden-Julian Oscillation (MJO) in view
of the moisture budget. They reported that the effect of convection is to moisten / dry the
lower troposphere in their 19 / 30 layer simulations, respectively. In the present study,
we investigate further sensitivity of the aqua-planet simulations to selected details of the
model such as the vertical distribution – as well as the resolution of the model levels
and the way the lifting condensation level (LCL) is calculated or used in the context of
the frequency and propagation of simulated Kelvin waves and MJO.

2. The Aqua-Planet Experiments

NSEAM is configured to perform aqua-planet simulations basically following the
Aqua-Planet Experiment (APE) Intercomparison Project recommendations [Neale and
Hoskins, 2001a, b]: The earth is covered with water with no orography, land or sea ice.
The sea surface temperature prescribed is zonally uniform and symmetric with respect to
the equator as in the “control” case of Neale and Hoskins [2001a] – see Fig. 1. Earth
eccentricity and obliquity are set to zero. The solar insolation is fixed to the equinoctial
condition with solar constant of 1365 Wm$^{-2}$. We include the diurnal cycle in this study.
CO₂ is prescribed to the amount of 348 ppmv following the Atmospheric Model Intercomparison Project (AMIP; Gates [1992]) II. The ozone is also taken from AMIP II and zonally averaged, but is symmetrized with respect to the equator for this study. Furthermore, we take the year 2005 averages of humidity and air temperature from the National Centers for Environmental Prediction / National Center for Atmospheric Research (NCEP/NCAR) Reanalysis data, which are also zonally-averaged and symmetrized with respect to the equator. We impose this latitudinal symmetry of the ozone, humidity and air temperature to remove the initial asymmetry so that any asymmetry that develops during simulation is due solely to the model physics.

The time integration is done semi-implicitly with second-order backward difference method. The time step is 300 s while the radiation parameterization is called every hour. We include a simple second-order hyper-viscosity for physics by generalizing the approach introduced in Giraldo [1999] with

\[
\frac{\partial q}{\partial t} = S(q) + \mu \nabla^2 q,
\]

where \(q\) is any prognostic physical variable, \(S\) represents the forcing, and \(\mu = 1 \times 10^6 \text{ (m}^2\text{s}^{-1})\) is the default value used in this study. For the horizontal grid, we choose 6 elements on one face in one direction and 8\(^{th}\) polynomial order of the basis functions (Fig.1). This horizontal resolution is roughly equivalent to the triangular spectral truncation at wavenumber 54 (i.e., T54) or 2.2°. We use 20 or 30 vertical levels, either evenly-spaced or unevenly-spaced in \(\sigma\) with the model top pressure of 1 hPa (Fig. 2). The simulations are run for one year with the first 30 days considered a spin-up period and excluded in the averages of 12-hour interval outputs.
3. The Simulation of Kelvin Waves and Madden-Julian Oscillation

Figure 3 shows time-longitude (or Hovmöller) plots of the convective precipitation averaged over the equator (5°S ~ 5°N) from simulation day 30 to 120. We found that after about 20 days, the simulations become very steady (at least for two years) and selected this 90-day interval to be compared with Fig. 3a of Neale and Hoskins [2001b]. There is clear difference between L20 (Fig. 3a) and L30 (Fig. 3b) evenly-spaced vertical level cases (L20e and L30e, hereafter) in the speed of the eastward-propagating waves (i.e., Kelvin waves) while the magnitude of the precipitation is similar. With L20e it takes about slightly more than two months in average for the Kelvin waves to circle the earth along the equator, but with L30e it takes more than four months. This speed difference can be explained by the greater vertical scale of the convective systems in the L20e case, which implies greater equivalent depth and higher vertical modes generated in this case. The vertical scale for both cases was estimated from the average cloud-top height, which was about twice higher in L20e than in L30e.

The propagation speeds of Kelvin waves in both L20e and L30e are fairly low compared with the observed atmospheric Kelvin waves (e.g., Masunaga et al. [2006]) and other simulations (e.g., Neale and Hoskins [2001b], Moncrieff et al. [2007]). However, changing the vertical structure of the model strongly influences the phase speed of the modeled waves. Figure 3c shows the Hovmöller diagram for L30u (L30 with unevenly-spaced levels), with tightly spaced levels near the surface and at the top of the atmosphere and loosely spaced levels in between (compare Figs. 2b and 2c). The
Kelvin wave propagation speed for L30u is higher than those for L30e and L20e and closer to the observed values.

The corresponding convective precipitation, averaged over about 11 months (days 30~365), reveals relatively narrow / broad and strong / weak distribution along the equatorial band with L30e / L30u case, respectively (implicitly shown in Figs. 3b and 3c; note the difference in the color scale). In order to understand this difference, we computed the difference of the moisture between these two cases and found the moisture over the equator in the lower troposphere (averaged over 700 ~ 950 hPa) was greater with L30u, implying that more moisture is available for L30u with the vertical intervals in this height range larger than L30e (σ~0.93 corresponds to 940 hPa; see Fig. 2).

We then compared the zonally averaged cumulus heating rate (also averaged over 700 ~ 950 hPa for days 30~365) between L30e and L30u, which is derived from the temperature tendency calculated by the Emanuel convective cloud parameterization used in our model [Emanuel and Zivkovic-Rothman, 1999; Peng et al., 2004]. There was a marked difference between the two cases; L30e showed the highest peak directly over the equator and secondary peaks over the middle latitudes whereas L30u showed the highest peaks over the middle latitudes and the sharp secondary peak over the equator. It turned out (not shown) that in L30e the moisture (although itself is less abundant) is more localized over the equator, the easterly winds are stronger over the equator and the meridional winds are stronger toward the equator, resulting in stronger and more localized low-level moisture convergence toward the equator and, consequently, stronger and more localized moisture convection and convective precipitation.
The spectral analysis of tropical waves introduced by Wheeler and Kiladis [1999] is an effective and convenient tool for investigating the organization and propagation of equatorial waves. Figure 4 compares the (equator-) symmetric component of the wavenumber-frequency decomposition divided by the background spectrum obtained using the simulated convective precipitation. The excessively low propagation speeds of L20e and L30e shown by the Hovmoeller plots (Figs. 3a, 3b) are confirmed in Figs. 4a and 4b whereas L30u (Fig. 4c) reveals much improved frequency compared with the theoretical lines obtained from the dispersion relations for a shallow water system (see the Fig. 4 legend for details).

Moreover, we find that the Kelvin wave propagation depends critically on details of the model physics; particularly those that involve vertical motion. First, we modify the Emanuel convective parameterization so that a thicker layer is used to determine the LCL. The Hovmoeller plot from this experiment with L30u is shown in Fig. 3d. The rather scattered cloud clusters that were present in L30u with the old LCL formulation (Fig. 3c) are now better organized with the new LCL formulation (Fig. 3d) while maintaining the dominant propagation speed of the old LCL case (Fig. 3c). Next, we change the limiting value of the specified temperature deficit at the LCL ($\Delta T_{\text{max}}$) in the Emanuel convective cloud parameterization from 0.9 to 1.2 K, which then enhances chance of the convection. The result (Fig. 3e) involves far stronger organization of the cloud clusters. It is interesting that increasing $\Delta T_{\text{max}}$ produces the bimodal structure of the eastward propagating perturbations with the slow moving waves propagating with the speed of MJO (marked by dashed lines) and faster waves corresponding to observed Kelvin waves (solid lines). When the precipitation fields are filtered for the observed
MJO and Kelvin wave modes, we can see the resemblance between the modified $\Delta T_{\text{max}}$ case and observed Kelvin and MJO modes, with more intense Kelvin waves developing during the “wet” MJO phase. This relationship is not present in other experiments presented in this study.

The Wheeler-Kiladis diagrams corresponding to these additional experiments are presented in Figs. 4d and 4e. It is apparent that with these physics modifications the wave spectrum patterns deviate more from the linear solutions (the theoretical lines) than the original case (Fig. 4c). It is perhaps due to a separation of the wave modes from pure Kelvin wave mode to a faster moving Kelvin wave mode and a slower moving mode. This is clearly seen as separated spectral peaks in Fig. 4e and additionally in Fig. 4f that is from another experiment with both the new LCL and $\Delta T_{\text{max}}$. The spectral peaks with periods greater than 30 days at eastward propagating wave numbers 1 and 2 are considered a signature of the MJO [Neale and Hoskins, 2001b]. Our spectrum (Fig. 4f, in particular) is fairly similar to that based on observed deep-storm cloudiness and rainfall (see Fig. 1e of Masunaga et al. [2006] and Fig. 10d of Cho et al. [2004], respectively).

In this regard, the slower moving mode, which is represented by the slower moving clusters (Figs. 3d, 3e) and the low frequency spectral peak (Figs. 4c, 4e, 4f), may be associated with the MJO. On the other hand, the spectral peak that appears at wave number 5 in Fig. 4d, which is also found in Fig. 3b of Neale and Hoskins [2001b], requires further investigation.

4. Concluding Remarks
Even under a controlled environment of the aqua-planet experiments, the propagation of equatorial waves vary widely among the models – even the simulated propagation directions of the equatorial waves are opposite in some models (see, e.g., Fig. 3 of Moncrieff et al. [2007]). This can be due to many reasons, but the convective cloud parameterization may be the prime suspect. Atmospheric models are sensitive to many details of the model, in particular to the physical parameterizations involving vertical motions of air parcels. Indeed, cumulus parameterization is considered one of the most dominant modeling components that generate uncertainties in large-scale atmospheric simulation (e.g., Tomita et al. [2005], Moncrieff et al. [2007]).

In this study we have explored such uncertainties utilizing our model, NSEAM. We have demonstrated that the simulations of convective activities can be quite different even with the same convective cloud parameterization depending on the distribution of vertical levels as well as they are sensitive to the details of the parameterization itself. For this reason, some standardization of vertical levels may be useful for more direct intercomparison among the models (e.g., for the APE). Furthermore, we have presented results demonstrating that the model can be calibrated to capture some basic characteristics of the Kelvin waves and MJO, which is encouraging considering the wide variability found among similar aqua-planet simulations.

Acknowledgments
The support from the sponsor, the Office of Naval Research under ONR Program Elements 0602435N and 0601153N is acknowledged. The comments from R. Hodur, S. Chang, and discussion with T. Hogan are appreciated. The computing time was provided jointly by the Naval Research Laboratory, Monterey, and the DoD NAVO MSRC (Naval Oceanographic Office Major Shared Resource Center) via the HPC program.

References


**Figure Captions**

Fig. 1. The sea surface temperature [K] prescribed for the aqua-planet experiments with NSEAM, proposed by *Neale and Hoskins* [2001a]. Superimposed are the hexahedral grid
points with 6 elements on one face in one direction and 8th polynomial order of the basis functions.

Fig. 2. The vertical grids used for the NSEAM aqua-planet simulations. (a) 20 evenly-spaced σ levels, (b) 30 evenly-spaced σ levels, and (c) 30 unevenly-spaced σ levels with tightly-spaced levels near the surface and the top and loosely-spaced intermediate levels.

Fig. 3. Time-longitude plot from days 30 to 120 of the convective precipitation [10⁻¹ mm/day] averaged for an equatorial band (5°S ~ 5°N) from the NSEAM aqua-planet experiments (a) L20e, (b) L30e, (c) L30u, (d) L30u with new LCL, and (e) L30u with modified ΔT_{max}. Note that a smaller contour interval is used for (c) ~ (e). The solid lines are drawn to help estimate the propagation speed of cloud clusters. The dashed lines in (d) and (e) are drawn to identify slower moving clusters distinguished from faster moving counterparts denoted by the solid lines.

Fig. 4. The symmetric component of the wavenumber-frequency decomposition of the convective precipitation following Wheeler and Kiladis [1999] for cases (a) L20e, (b) L30e, (c) L30u, (d) L30u with new LCL, (e) L30u with modified ΔT_{max}, and (f) L30u with both new LCL and modified ΔT_{max} for days 30 through 365. The straight lines denote the shallow-water dispersion relations for equatorial Kelvin waves as shown in Fig. 3b of Neale and Hoskins [2001b]. Also shown in (a) are the approximate Kelvin wave propagation speeds, which correspond to equivalent depths of 50, 25 and 12 m from left.
Figure 1

Ground Temperature [$10^{-1}$ K]
Figure 2
Figure 3
Figure 3 (cont.)
Figure 4
Figure 4 (cont.)
Figure 4 (cont.)