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**MEMRISTOR-BASED COMPUTING ARCHITECTURE: DESIGN
METHODOLOGIES AND CIRCUIT TECHNIQUES**

POLYTECHNIC INSTITUTE OF NEW YORK UNIVERSITY

MARCH 2013

FINAL TECHNICAL REPORT

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1.0 SUMMARY

Scientists have dreamed of information systems with cognitive human-like skills for years. However, constrained by the device characteristics and rapidly increasing design complexity under the traditional processing technology, little progress has been made in hardware implementation. The recently popularized memristor offers a potential breakthrough for neuromorphic computing because of its unique properties including nonvolatility, extremely high fabrication density, and sensitivity to historic voltage/current behavior.

In this project, we first investigated the memristor-based synapse design and the corresponding training scheme. Then, the design optimization and its implementation in multi-synapse systems were analyzed too. With the aid of sharing training circuit and self-training mode, the performance and energy can be significantly improved. At last, a case study of an arithmetic logic unit (ALU) was designed to demonstrate the hardware implementation of reconfigurable system built based on memristor synapses. All the circuit design, simulation, layout, and functionality verifications have been completed.

2.0 INTRODUCTION

Neuromorphic computing architectures imitate natural neurobiological processes by mimicking the highly parallelized computing architecture of the biological brain. To realize such a novel architecture in hardware, at least two conditions need to be satisfied at the technology level: *high integration density* and *ability to record the history of electric signals*. Neuromorphic computing architectures that have a large volume of memory and are adaptable to their environment have demonstrated great potential towards the development of high performance parallel computing systems [1]. Most of the research activities have focused on software or the system level using conventional Von Neumann computer architectures [2-3]. Developing a neuromorphic architecture at the chip level by mimicking biological systems is another important direction. However, a biological scale hardware implementation based on traditional CMOS devices requires extremely high design complexity and cost, which is impractical.

The existence of memristor was predicted as early as in 1971 [4], but the first physical realization that adopted that term was first reported thirty years later by Hewlett-Packard Laboratories (HP Labs) with their TiO₂ thin-film device [5]. It soon became clear that many more materials with memristive properties had been reported since the 1960's. Yet while these devices had some common behaviors, they each operated according to different physical phenomena. The unique properties of the memristor make it promising in neuromorphic computing systems. First, prototyped memristor devices have demonstrated scalability at sub-10 nm scales. Accordingly, the memristor memories can achieve a high integration density of $100\text{Gbits}/\text{cm}^2$, several orders higher than the popular flash memory technologies [4-5]. Second, the memristor device has an intrinsic and remarkable feature called "pinched hysteresis loop," which means it can "remember" the total

electric charge flowing through it [4,6]. Third, memristance remains unchanged when power is turned off. Consequently, memristor-based memory combined with the high-integration capability and the pinched hysteresis characteristics can be applied to a massively-parallel, large-scale neuromorphic computing processor architecture.

Many memristor-based circuit designs have been explored, such as crossbar nonvolatile memory [8] and FPGA [9]. Strukov *et al.* integrated digital memory, programmable Boolean logic circuit, and neuron networks within a 3D hybrid CMOS/memristor structure. Rajendran *et al.* proposed a memristor-based programmable threshold logic array [10] and used it in a synapse-neuron structure [11]. However, training circuits and training schemes for a memristor-based reconfigurable architecture design have not been fully explored yet.

Therefore, in this project, we investigated memristor-based reconfigurable design techniques. The structure is built upon single memristor-based synapse and the corresponding training circuit design. An 8-bit ALU design built on synapse structures was used as a case study to demonstrate its potential in developing a neuromorphic computing processor architecture. The ALU design composed of ~ 100 synapses can be adaptively trained to realize addition, subtraction, and binary counting functionalities. The circuit design, simulation, layout, and functionality verifications have been completed in the project.

3.0 METHODS, ASSUMPTIONS, AND PROCEDURES

3.1. Memristor Theory

Nearly forty years ago, Professor Chua predicted the existence of the memristor – the fourth fundamental circuit element, to complete the set of passive devices that previously included only the resistor, capacitor, and inductor [4]. The memristor uniquely defines the relationship between the magnetic flux (φ) and the electric charge (q) passing through the device,

$$d\varphi = M \cdot dq. \quad (1)$$

Considering that magnetic flux and electric charge are the integrals of voltage (V) and current (I) over time, respectively, the definition of memristor can be generalized as

$$\begin{aligned} V &= M(\omega, I) \cdot I \\ d\omega/dt &= f(\omega, I) \end{aligned} \quad (2)$$

where ω is a state variable and $M(\omega, I)$ represents the instantaneous memristance, which varies over time. For a “ideal” memristor, neither $M(\omega, I)$ nor $f(\omega, I)$ can be expressed only as a function of current I .

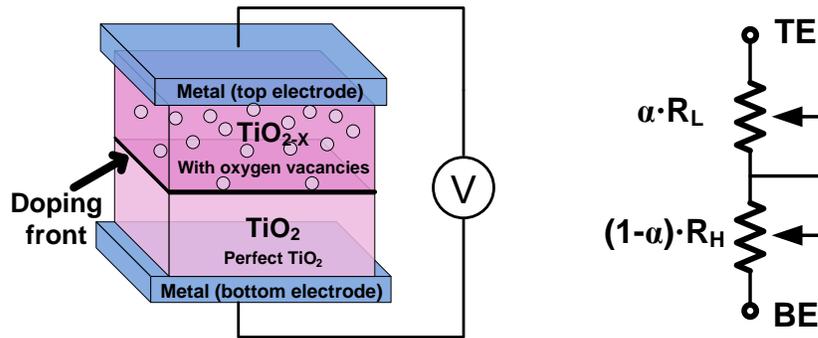
Based on this mathematical description, these devices remained primarily intellectual curiosities until HP Lab first used these relationships to describe the memristive switching effect created by moving the doping front along TiO_2 thin-film device [4]. Soon, more memristive systems were identified according to their behavior, to include spintronics [5-6], polymeric thin film [12-13], MgO based magnetic tunnel junctions (MTJ) [14-15], and AlAs/GaAs/AlAs quantum-well diodes [16].

An intrinsic and remarkable feature of the memristor is called “pinched hysteresis loop,” that is, memristors can “remember” the total electric charge flowing through them by changing their resistances (memristance) [17]. The unique properties create great opportunities in future system design. For instance, HP researchers proposed a memristor-based architecture, which could change the standard paradigm of computing by enabling calculations to be performed in the chips where data is stored, rather than in a specialized central processing unit [18]. Moreover, the applications of this memristive behavior in electronic neural network have been extensively studied [19-20].

Figure 1(a) illustrates the conceptual view of Pt/ TiO_2 /Pt structure: two orthogonal metal wires (Pt) serve as the top and bottom electrodes with a thick titanium dioxide film sandwiched in between. A perfect TiO_2 structure in its natural state is as an insulator. However, the conductivity of oxygen-deficient titanium dioxide (TiO_{2-x}) is much higher. By moving the doping front under proper electrical excitations, intermediate memristive states can be achieved. We use R_H and R_L to denote the total resistance when a TiO_2 memristor is fully undoped (maximum high resistance) and doped (minimum low resistance), respectively. The overall memristance is then the equivalent of two serially-connected resistors, as shown in Figure 1(b). That is

$$M(\alpha) = \alpha \cdot R_L + (1 - \alpha) \cdot R_H, \quad (3)$$

where α ($0 \leq \alpha \leq 1$) is the relative doping front position, which is the ratio of the doping front position over the total thickness of the TiO_2 device.



(a) TiO_2 Memristor Structure (b) Equivalent Circuit
Figure 1. TiO_2 thin-film memristor

3.2. The Memristor-based Logic Design

3.2.1 The Principle of Memristor-based Synapse. Rather than using a memristor crossbar array in a neuromorphic reconfigurable architecture, we proposed a memristor-based synapse design to mimic the biological structure. Figure 2 depicts the conceptual scheme, which simply consists of an NMOS transistor (Q) and a memristor. When the input V_{in} is low, the transistor Q is turned off. Thus, the output V_{out} is connected to ground through the memristor. Conversely, when V_{in} is high, turning Q on, the memristance M and the equivalent transistor resistance (R_Q) together determine V_{out} ,

$$V_{out} = f(V_{in} \cdot M), \quad (4)$$

where V_{out} is weighted by the memristance. This variable weight can be treated like a synapse.

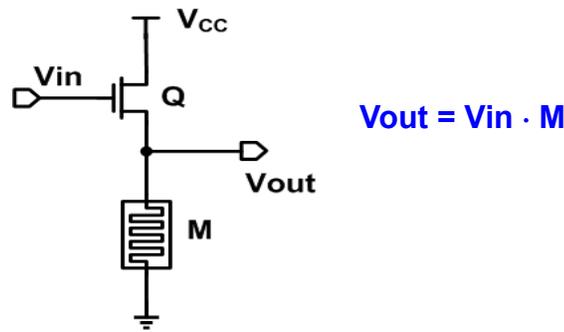


Figure 2: A memristor-based synapse design

Note that the response of the synapse design was dependent on the equivalent resistance (effectively, the size) of the Q transistor (R_Q). A larger Q would offer a wider range of V_{out} with poorer linearity. However, for a large Q , the increased range of V_{out} by further size increase would be marginal. The simulation results showing this can be found in Section 4.1.1.

To improve design stability, a buffer can be added at output of the synapse to increase the voltage swing. Furthermore, some circuit optimization techniques, such as asymmetry gates in other blocks, can be used to minimize the overall synapse-based system.

3.2.2 Synapse Training Circuit. Being self-adaptive to the environment is one of the most important properties of a biological synapse. To accomplish a similar functionality, a training block is needed in the memristor-based synapse to adjust its memristance.

The training circuit compares the generated result V_{out} and the expected result D_{train} to decide if training is needed or not. The corresponding V_{top} and V_{bot} are generated and

applied to the two terminals of a memristor. Figure 3 is the symbol of the synapse training circuit.



Figure 3: Synapse training circuit symbol

Figure 4 shows the diagram of a training circuit for a one synapse design based on logic analysis and simplification. It included two major components: a *training controller* and a *write driver*. By comparing the current synapse output V_{out} and the expected output D_{train} , the training controller generated the control signals. The write driver used these signals to control two pairs of NMOS and PMOS switches and supply the training voltage pair V_{top} and V_{bot} . The training pair was then applied to the two terminals of the memristor in the synapse design.

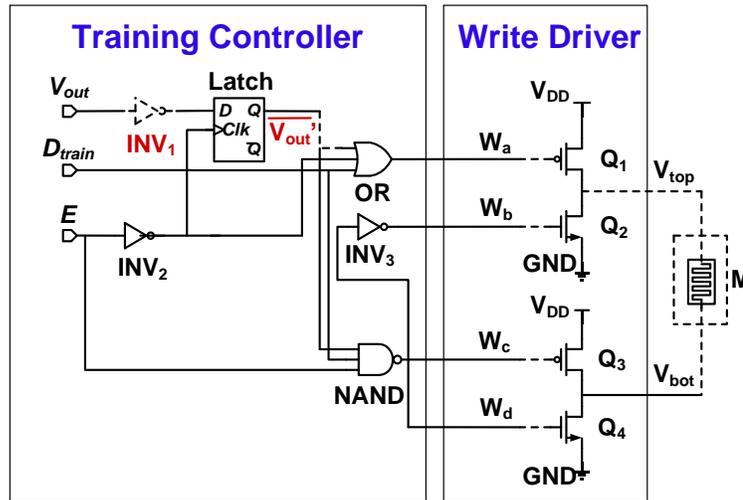


Figure 4. Synapse training circuit diagram

Table 1 summarizes the operation conditions of the proposed training circuit design. The training circuit can work under two modes determined by the training enable signal E .

Table 1. Training Circuit Operation Conditions

E	V_{out}	D_{train}	V_{top}	V_{bot}	V_{mem}	Status
0	X	X	Floating	0	X	Operating
1	1/0	1/0	0	0	0V	No training
1	1	0	1	0	1.8V	R_H to R_L
1	0	1	0	1	-1.8V	R_L to R_H

* ‘0’ – logic low; ‘1’ – logic high, and ‘X’ – unknown or don’t care.

- *Operating mode*: When $E = 0$, the synapse operated in the regular (read) mode; and the training circuit was disabled.
- *Training mode*: The training circuit was enabled when $E = 1$. By comparing the current synapse output V_{out} and the expected D_{train} , the training circuit generated V_{top} and the V_{bot} applied to the two terminals of the memristor to update or keep its memristance. We define $V_{mem} = V_{top} - V_{bot}$.

Figure 5 depicts the proposed memristor-based synapse integrated with training circuit. An extra NMOS transistor Q_2 was inserted in the synapse to isolate training operation from other voltage sources. When $E = 1$, Q_2 was turned off so that the two terminals of memristor were controlled only by the training circuit and not by V_{in} .

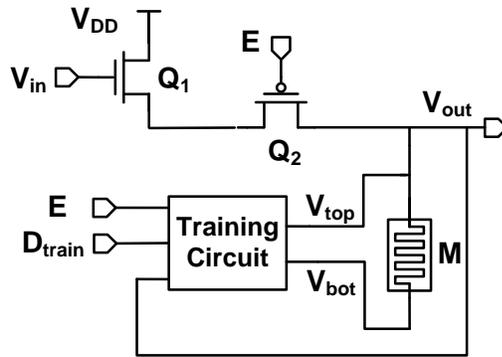


Figure 5. Synapse together with training circuit

3.2.3 Multi-synapse Training Scheme. Most of the neuron systems are constructed by multiple synapses. In this section, we discuss the corresponding training scheme for a 2-synapse neuron, of which Figure 6 is an example. Here, A_1 and A_2 were two synapse inputs received from other neurons. M_1 and M_2 are memristor-based weights for the two synapses S_1 and S_2 . N denoted a neuron with output V_{out} . The value of V_{out} depended upon the functionality of N as well as V_{out1} and V_{out2} from the two synapses. With the different combinations of M_1 and M_2 , the two-input neuron obtained different functionalities.

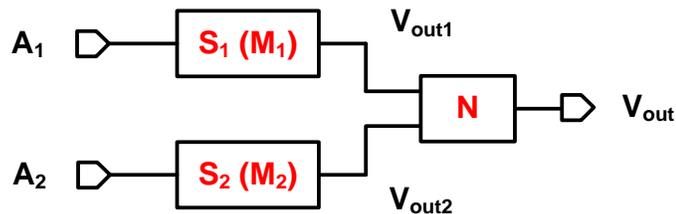


Figure 6. Two-input neuron structure

To save design cost, memristances of the 2-synapse can be trained separately and share one training circuit. Figure 7 shows a training sharing distribution circuit, which generated training signals to control M_1 and M_2 . The training sharing circuit operations under different conditions are shown in Table 2.

The two synapse inputs A_1 and A_2 can be used to determine which memristor, M_1 or M_2 , was in training. Table 3 lists the required A_1 and A_2 when the logic functionality of N was one of the following: OR/NOR, XOR/XNOR, AND/NAND.

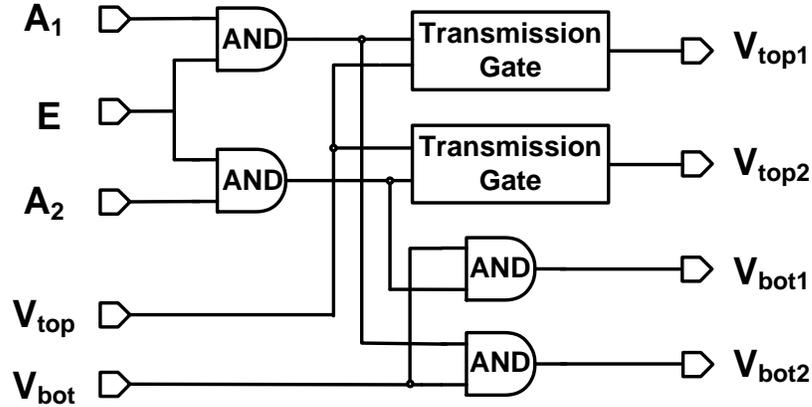


Figure 7. Training sharing distribution circuit

Table 2. Training Sharing Circuit Operation

Status	V_{top1}	V_{bot1}	V_{top2}	V_{bot2}
Training M_1	V_{top}	V_{bot}	Floating	0
Training M_2	Floating	0	V_{top}	V_{bot}

Table 3. Synapse Input Pairs for Different Logic Values

Functionality of N	Training M_1	Training M_2
OR/NOR	$A_1 = 1, A_2 = 0$	$A_1 = 0, A_2 = 1$
XOR/XNOR	$A_1 = 1, A_2 = 0$	$A_1 = 0, A_2 = 1$
AND/NAND	$A_1 = 1, A_2 = 1$	$A_1 = 1, A_2 = 1$

3.2.4 Training Block Sharing Scheme. Since the two memristors could be trained separately, it was possible to share a training circuit between two synapses. By doing this, we achieved the same functionality but with reduced design cost. The design diagram of the 2-synapse shared training circuit and the sharing distribution circuit are depicted in Figure 8.

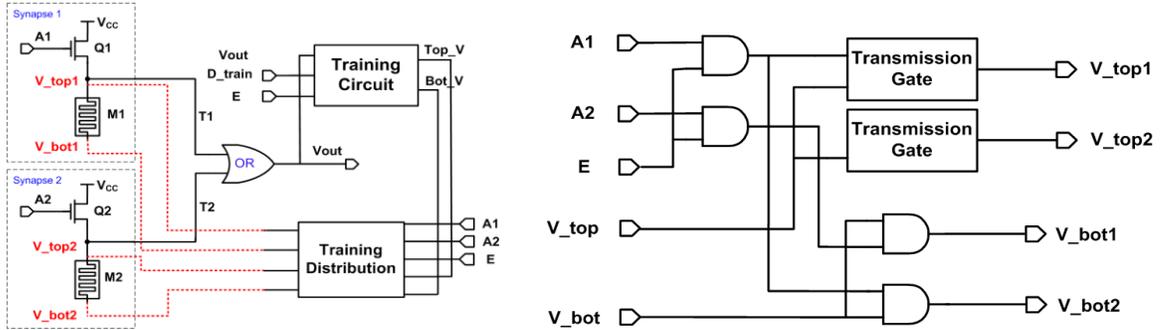


Figure 8. 2-synapse shared training circuit and sharing distribution circuit

3.2.5 Two-level OR Neuron Training Strategy. Expanding the synapse design to multiple levels can provide a more powerful reconfigurable design. For example, Figure 9 shows a 2-level OR neuron circuit built with the previous 2-synapse structure. Such a design can achieve 16 possible logics at output.

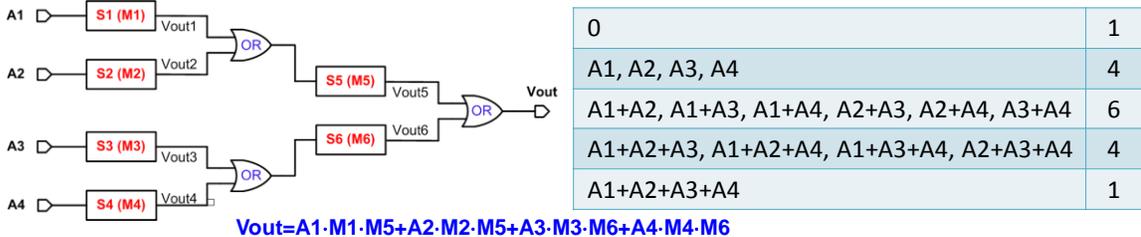


Figure 9. Two-level OR neuron circuit and possible logic values table

Detailed analysis showed that the memristances of $M5$ and $M6$ did not introduce more logic functionality. Training only $M1$ through $M4$ and keeping $M5$ and $M6$ all high achieved all 16 possible logic functions. Similar to 2-synapse training, we trained $M1 - M4$ separately by activating one synapse branch at a time. To do this, we applied ‘1’ to the input of the activated branch and ‘0’ to the inputs of all the other branches. For example, to train $M1$, we set $A1 = 1$ and $A2 = A3 = A4 = 0$.

Figure 10 illustrates the training steps. We used the same training case, where $M1$ through $M4$ were set high at the beginning, trained to low, and then finally trained back to high again.

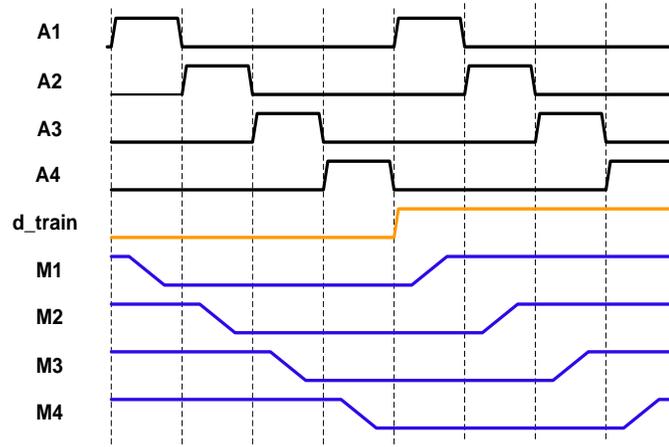


Figure 10. Two-synapse shared training strategy

3.2.6 Ten-synapse Circuit. Figure 11 gives an example of a 3-level design with ten synapses. Each sub-block was composed of two synapses with an OR gate as the neuron function. $M1 - M10$ were used to denote the weights of the ten synapses in the circuit. The functionality of this structure can be summarized as

$$V_{out} = A1 \cdot X1 + A2 \cdot X2. \quad (5)$$

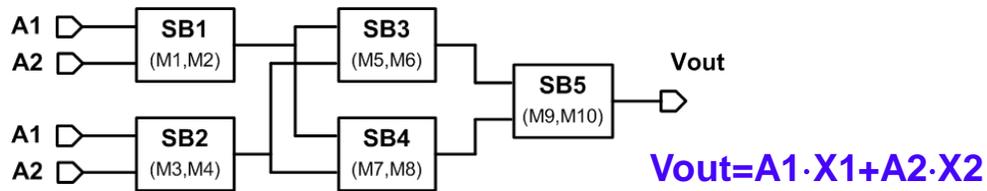


Figure 11. 10-synapse OR neuron circuit

$X1$ and $X2$ are simplified combinations of $M1 - M10$. Theoretically, this circuit had the same functionality as the 2-synapse structure OR neuron. However, the redundant design was more robust with a higher fault tolerance. Even if some devices were damaged, the structure could be self-healed and obtain the required logic. For example, when $M5$ and $M6$ were open and appeared as high memristance due to process damage, V_{out} could still execute the four logic combinations.

In this design, we kept $M5 - M10$ as high all the time and trained $M1 - M4$ only. Applying '1' to $A1$ and '0' to $A2$ trained $M1$ and $M3$ simultaneously. We then applied '0' to $A1$ and '1' to $A2$ to train $M2$ and $M4$ at the same time. Figure 12 illustrates this training scheme.

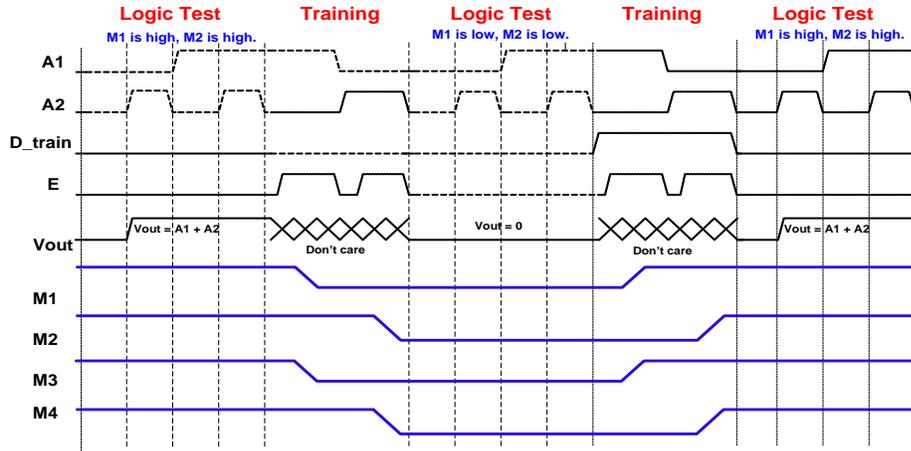


Figure 12. Timing diagram of 10-synapse circuit training

3.3. Case Study – Synapse-based ALU Design

We designed an 8-bit arbitrary logic unit (ALU) by using memristor-based synapses. The ALU can be used for addition, subtraction, and counting. In the project, we completed the circuit design, simulation, layout, and functionality verification. The design details are explained in the following section.

3.3.1 1-bit Adder-Subtractor Block. Figure 13 shows the schematic of the 1-bit adder-subtractor block built by synapses.

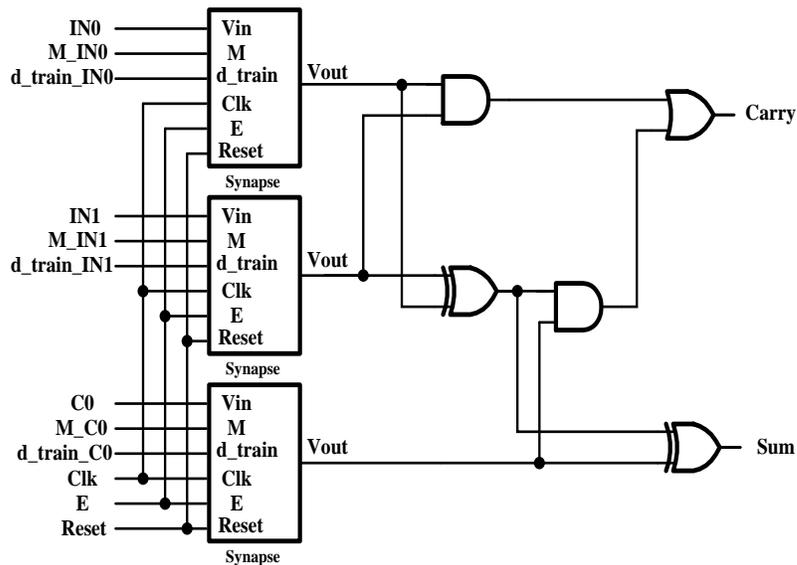


Figure 13. Schematic of 1-bit adder-subtractor block

The full adder had three inputs (IN_0 , IN_1 , and C_0) and two outputs (Sum and $Carry$) with the following relations:

$$\begin{aligned} Sum &= IN_0 \oplus IN_1 \oplus C_0 \\ Carry &= IN_0 \cdot IN_1 + C_0 \cdot (IN_0 \oplus IN_1) \end{aligned} \quad (6)$$

This full adder design could be used as an unsigned subtractor by inverting the subtrahend and setting $C_0 = 1$,

$$\begin{aligned} Sum &= IN_0 \oplus \overline{IN_1} \oplus C_0 \\ Carry &= IN_0 \cdot \overline{IN_1} + C_0 \cdot (IN_0 \oplus \overline{IN_1}) \end{aligned} \quad (7)$$

In the 1-bit adder-subtractor design, three synapse blocks bridged the input signals and activation functions. Based on the required functions, i.e., adding or subtracting, the weights in these synapses could be trained accordingly. For details of the synapse design, refer to Section 3.2.

3.3.2 Binary Counter. An m -bit binary counter used n digital bits to represent 2^m numbers. It incremented by 1 for every clock cycle and started over from 0 if all the digital bits were 1's. We assumed the outputs of an m -bit binary counter at n^{th} clock cycle and the $(n + 1)^{\text{th}}$ clock cycle were $Q^n = q_{m-1}^n \cdots q_0^n$ and $Q^{n+1} = q_{m-1}^{n+1} \cdots q_0^{n+1}$, respectively. Then we had

$$\begin{aligned} q_0^{n+1} &= \overline{q_0^n} \\ q_i^{n+1} &= q_i^n \oplus q_{i-1}^n \quad (i = 1 \dots m - 1) \end{aligned} \quad (8)$$

We used m -pieces of the above adder-subtractor blocks to build a binary counter. For example, Figure 14 shows a 4-bit counter based on the adder-subtractor blocks.

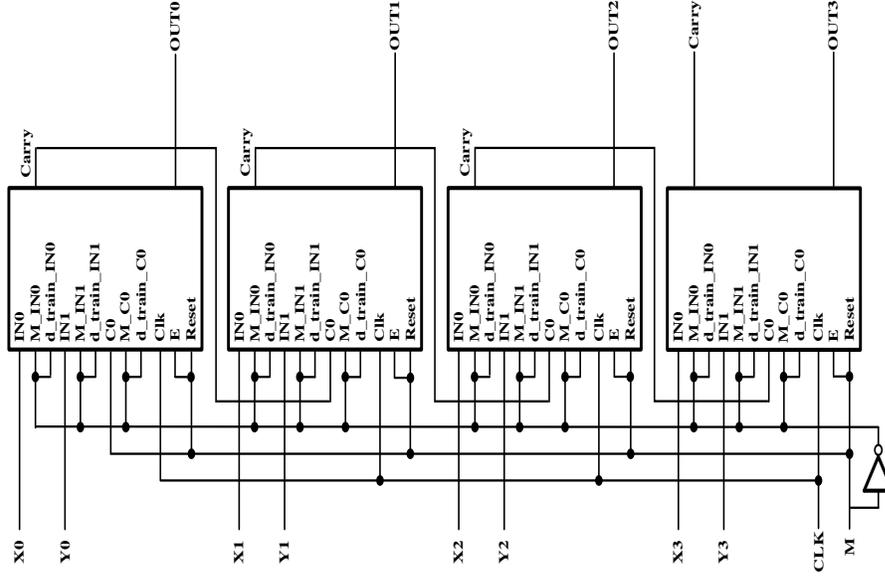


Figure 14. Schematic of 4-bit binary counter built with adder-subtractor blocks

3.3.3 Decade Counter. A decade counter has four output pins to represent decimal numbers 0 – 9. The corresponding binary outputs are from ‘0000’ to ‘1001’. On the rising edge of each clock cycle, the output increased 1 or reset back to ‘0000’ after it reached ‘1001’. By properly modifying the adder-subtractor block design, we also build up a decade counter.

We assumed that the outputs of a decade counter at n^{th} clock cycle and the $(n + 1)^{\text{th}}$ clock cycle were $Q^n = q_3^n q_2^n q_1^n q_0^n$ and $Q^{n+1} = q_3^{n+1} q_2^{n+1} q_1^{n+1} q_0^{n+1}$, respectively. Based on the Karnaugh map, we had

$$q_0^{n+1} = \overline{q_0^n}, \quad (9a)$$

$$q_1^{n+1} = q_1^n \cdot \overline{q_0^n} + \overline{q_3^n} \cdot q_0^n \cdot \overline{q_1^n}, \quad (9b)$$

$$q_2^{n+1} = q_2^n \cdot \overline{q_1^n} + q_2^n \cdot \overline{q_0^n} + \overline{q_2^n} \cdot q_1^n \cdot q_0^n, \quad (9c)$$

$$q_3^{n+1} = q_3^n \cdot \overline{q_0^n} + q_2^n \cdot q_1^n \cdot q_0^n. \quad (9d)$$

Eq. (9a) could be realized with a 1-bit adder by setting $IN_0 = 0$, $IN_1 = 1$, and $C_0 = q_0^n$. So $q_0^{n+1} = Sum = 0 \oplus 1 \oplus q_0^n = \overline{q_0^n}$.

Eq. (9b) could be transformed to $q_1^{n+1} = q_1^n \cdot \overline{q_0^n} \cdot (1 + \overline{q_3^n}) + \overline{q_3^n} \cdot q_0^n \cdot \overline{q_1^n} = q_1^n \cdot \overline{q_0^n} + \overline{q_3^n} \cdot (q_0^n \oplus q_1^n)$. This form had the similar shape as the Carry output in Eq. (7) and hence we could obtain Eq. (9b) by setting $IN_0 = q_0^n$, $IN_1 = q_1^n$, and $C_0 = \overline{q_3^n}$.

By using DeMorgan's Law, Eq. (9c) could be changed to $q_2^{n+1} = q_2^n \cdot (\overline{q_1^n} + \overline{q_0^n}) + \overline{q_2^n} \cdot q_1^n \cdot q_0^n = q_2^n \oplus (q_1^n \cdot q_0^n)$. By slightly modifying the adder-subtractor block as shown in Figure 15, one could realize Eq. (9c).

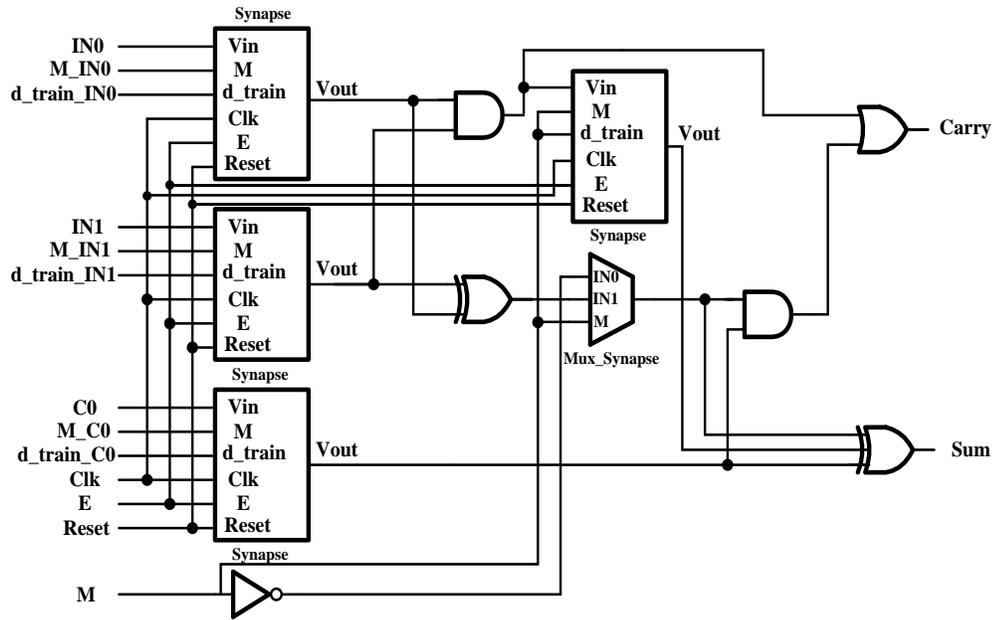


Figure 15. Schematic of the modified adder-subtractor block to realized Eq. (9c)

Similarly, we could add one inverter and two synapse blocks in the adder-subtractor block to realize Eq. (9d), as seen in Figure 16.

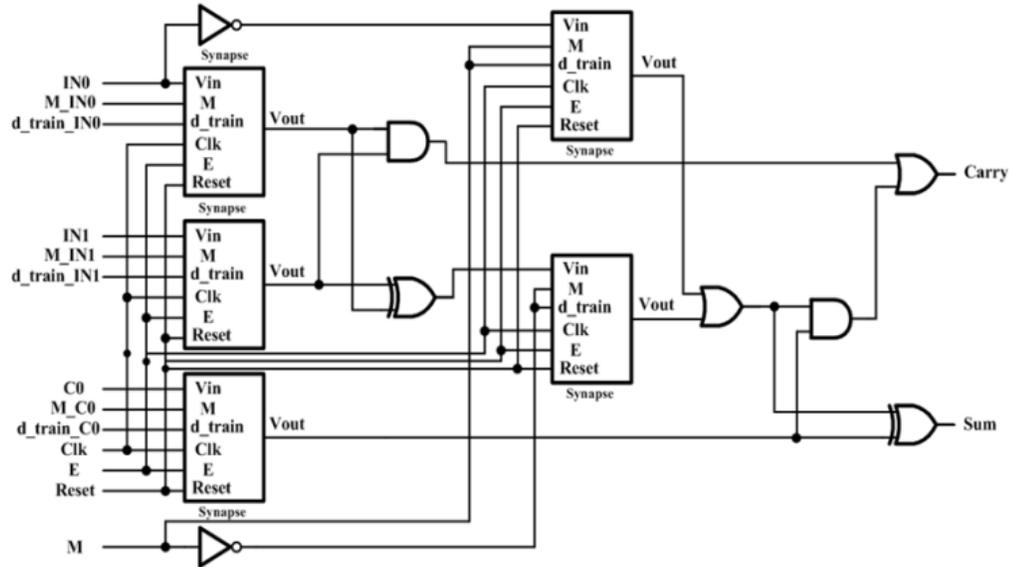


Figure 16. Schematic of the modified adder-subtractor block to realized Eq. (9d)

3.3.4 4-bit ALU as Adder, Subtractor, and Decade Counter. Figure 17 shows the schematic of a 4-bit ALU, which could add, subtract, and count decimal numbers.

3.3.5 8-bit ALU as Adder, Subtractor, and Decade Counter. We built an 8-bit ALU unit by using the basic block shown in Figure 18. It could conduct 8-bit addition, subtraction, or binary counting. The design contained ~100 synapses. In development, we adopted a CMOS-only design in order (a) to demonstrate the design concept and (b) to avoid the risks due to immature memristor fabrication process. Taiwan Semiconductor Manufacturing Co. (TSMC) 0.18 μm technology was used for cost reduction. The schematic and layout are shown in Figure 18 and Figure 19, respectively.

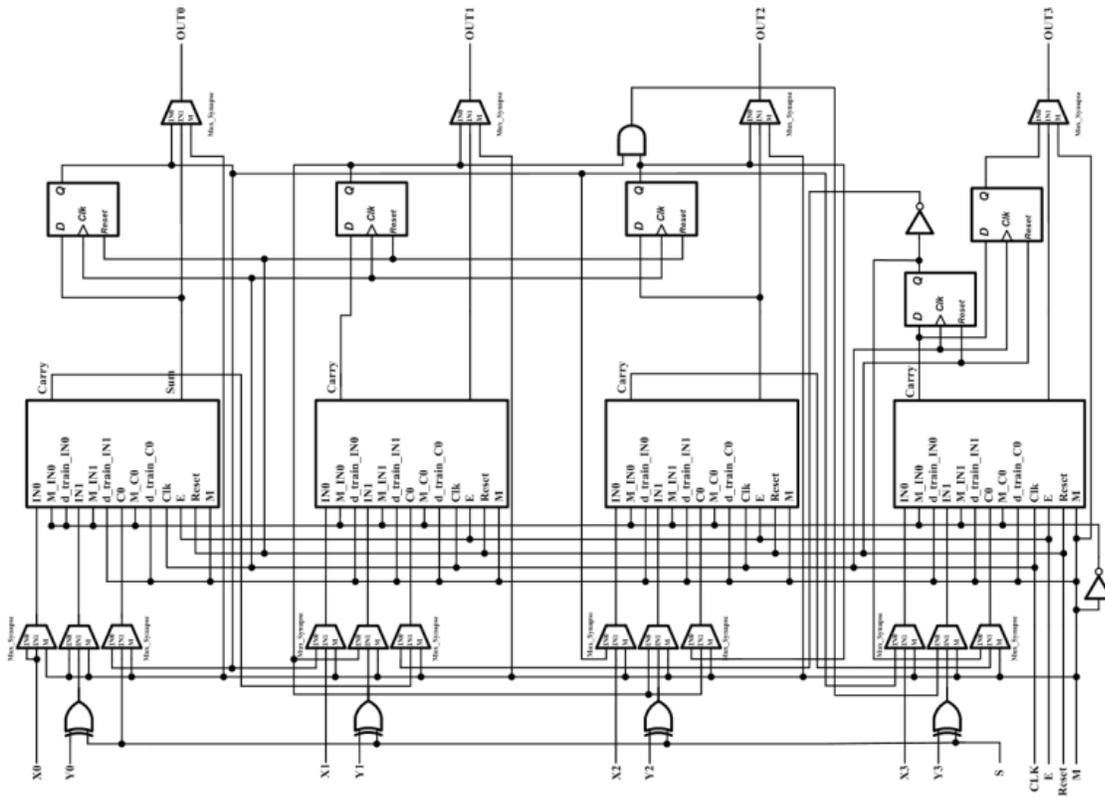


Figure 17. Schematic of a 4-bit ALU as adder, subtractor, and decade counter

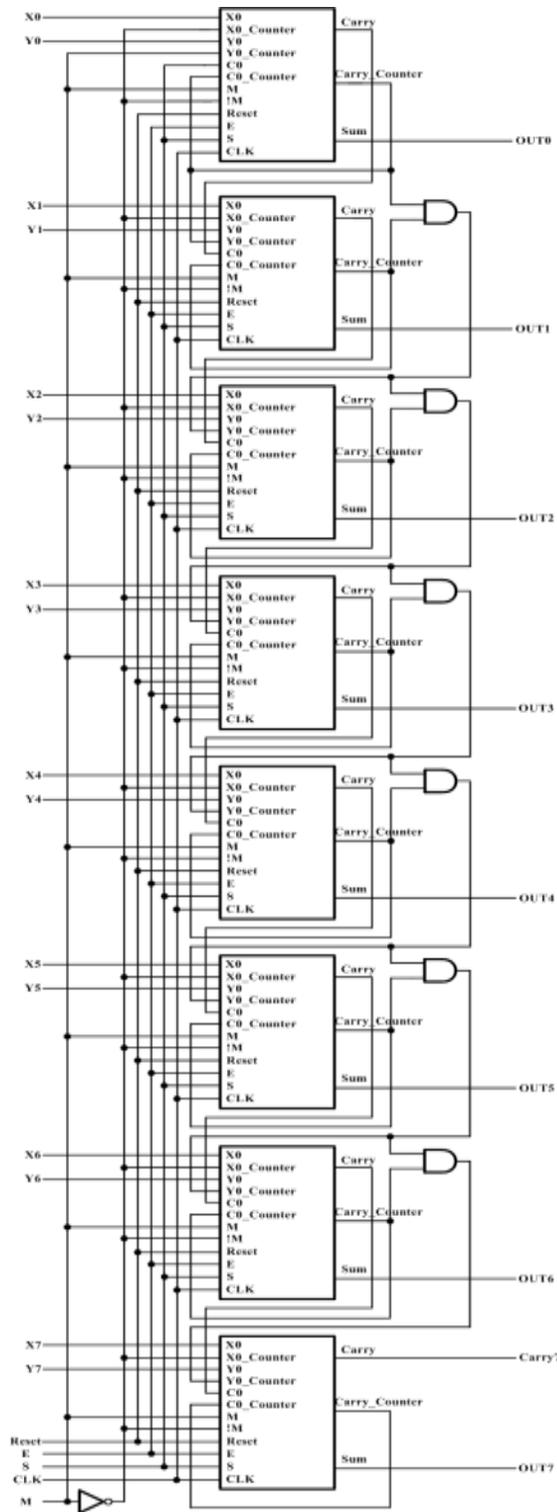


Figure 18. Schematic of a 8-bit ALU as adder, subtractor, and binary counter

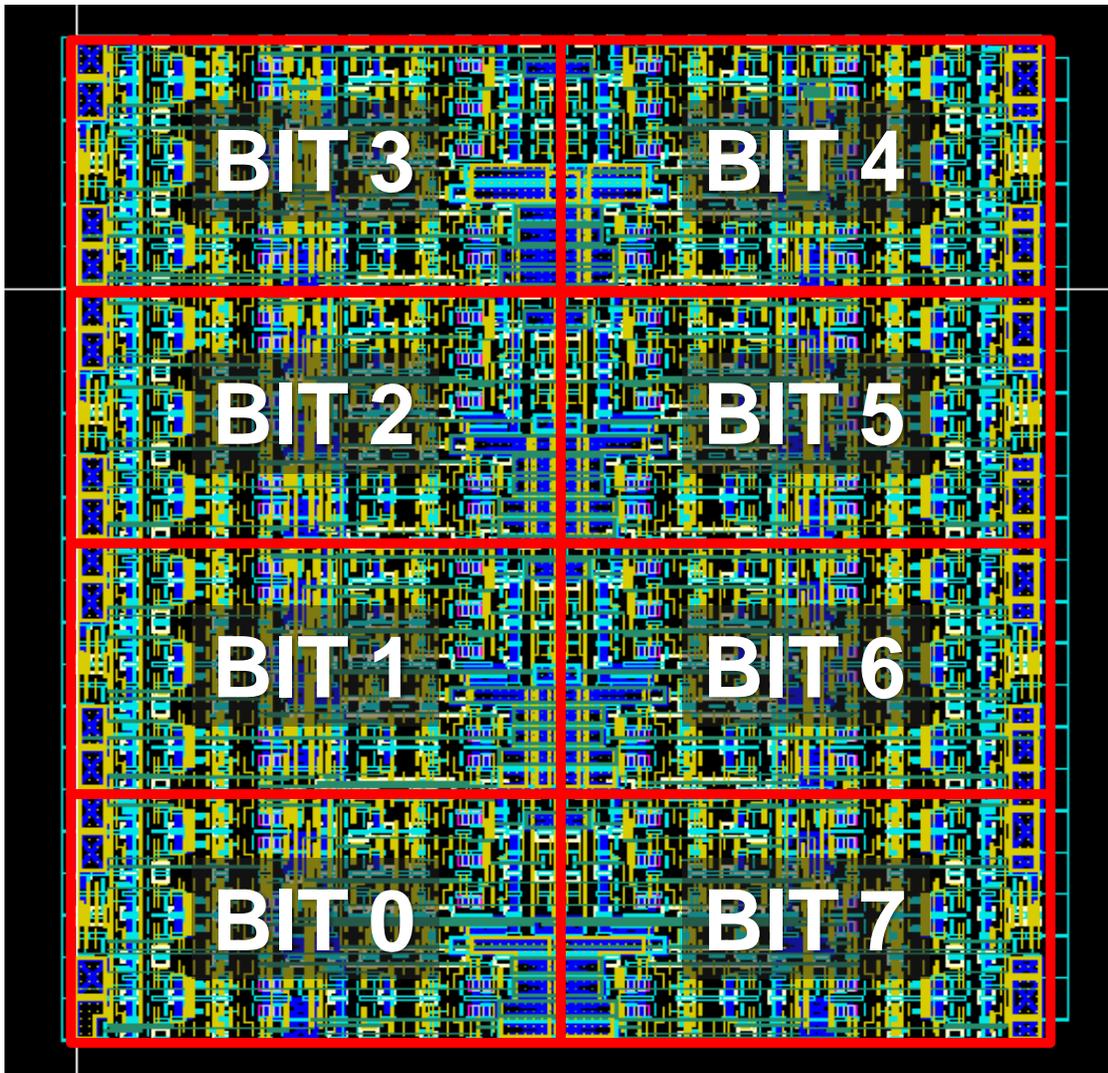


Figure 19. Layout of a 8-bit ALU as adder, subtractor, and binary counter

4.0 RESULTS AND DISCUSSION

In the section, we will show the corresponding simulation results to validate the effectiveness of the proposed memristor-based synapse based design. Also, the functionality of the ALU case study as an adder, subtractor, and binary counter will be verified.

4.1. Simulation Verification of Memristor-based Logic Design

4.1.1 The Memristor-based Synapse. Figure 20 shows the relation of the input and output signals of a memristor-based synapse proposed in Figure 2. Here, V_{in} was the input of the synapse design; and V_{out} represented its output signal. When V_{in} was low, V_{out} was connected to ground through the memristor and hence was low. When V_{in} rose high, V_{out} was at an intermediate value, which was determined by the memristance M together with the equivalent resistance of Q (R_Q).

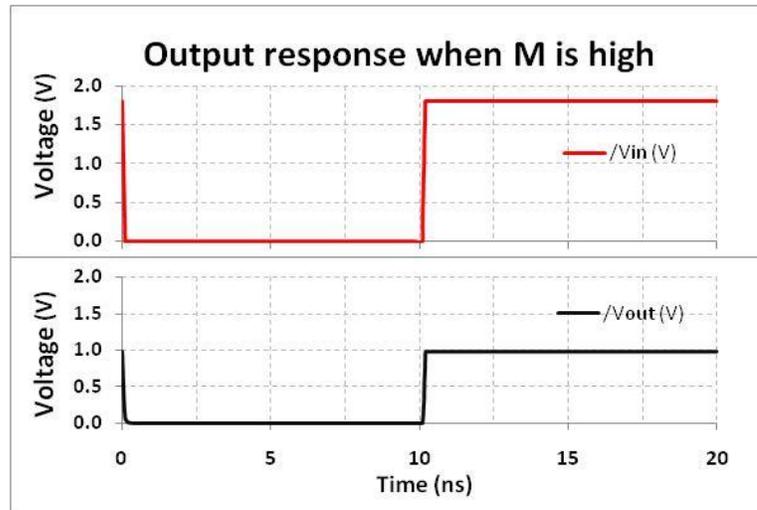


Figure 20. Output response of a synapse when memristor is at high resistance state

Figure 21 shows the response of V_{out} for changing memristance from $1\text{K}\Omega$ to $16\text{K}\Omega$. Here, CMOS devices used TSMC $0.18\mu\text{m}$ technology. In general, V_{out} increased as the memristance becomes higher. The response of the synapse design relied on the equivalent resistance of the transistor Q (R_Q), or the size of Q . This was demonstrated in Figure 21 by sweeping the width of Q from 220 nm to $4.4\ \mu\text{m}$ in 220 nm steps. The simulation showed that a larger Q can result in a wider range of V_{out} but with poorer linearity. However, for a large Q , the enhancement of V_{out} by further increasing its size was marginal.

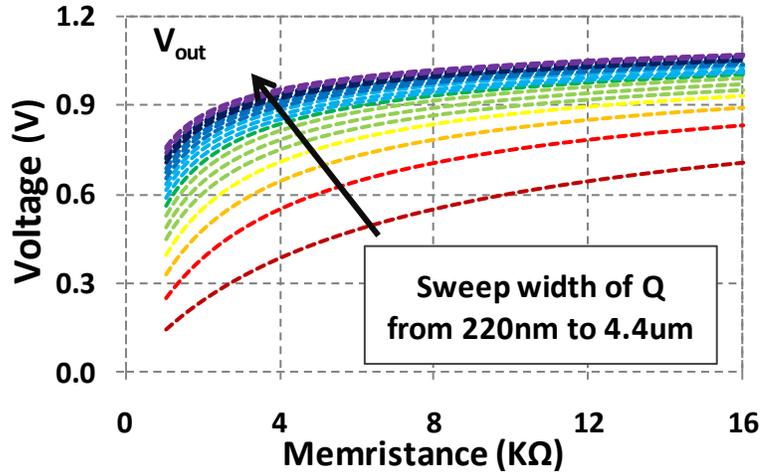


Figure 21. Output voltage of a memristor-based synapse vs. memristance

To improve design stability, a buffer can be added at the output of the synapse to increase the voltage swing. Furthermore, some circuit optimization techniques, such as an asymmetry gate in other blocks, could be used to minimize the overall synapse-based system.

4.1.2 Synapse Training Circuit. The timing diagram of training circuit is demonstrated Figure 22. Before a training procedure starts, a sensing step was required to detect the current V_{out} to be compared with D_{train} . In the sensing phase, accordingly, training enable signal E was set to low for a very short period of time, e.g., 4.5 ns, at the beginning of training. At the same time, $\overline{V_{out}}$ was sent to $Latch$, whose output $\overline{V_{out}}$ remained constant during one training period, as shown in Figure 4. In the training phase, E was set back to high for a much longer time, i.e., 51 ms, to change the memristance if needed.

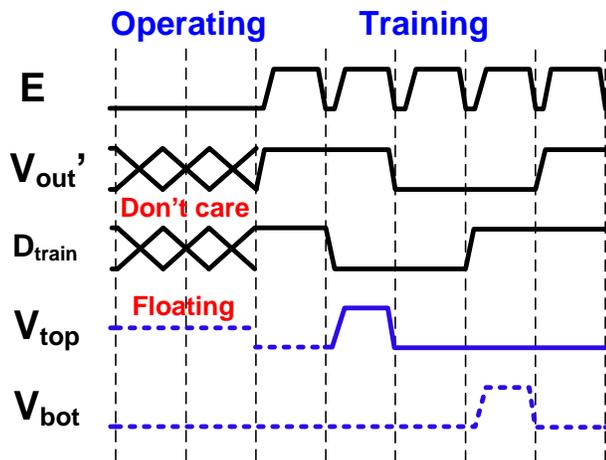


Figure 22. The timing diagram of training circuit

We tested the training procedure using the TiO_2 memristor model [4]. The training circuit was designed with TSMC 0.18 μm technology with $V_{DD} = 1.8 \text{ V}$. Changing the memristance from R_H to R_L or vice versa required about 51 ms. The simulation result is shown in Figure 23. Here, the memristance was initialized to $M = 16 \text{ K}\Omega$. Over the first 51 ms, the memristor was trained to $1 \text{ K}\Omega$ by setting $Dtrain$ to low. Then at $t = 51 \text{ ms}$, we set $Dtrain$ to high and trained the memristance back to R_H in the following 51 ms.

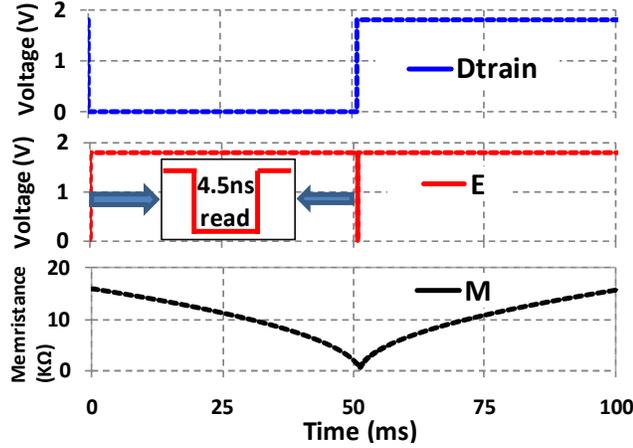


Figure 23. The simulation result of memristor training

4.1.3 Asymmetric Gate Design. Since the size of $Q1$ affects the range of V_{out} , the asymmetry gate design can be adopted to minimize the layout area of synapse design instead of adding a buffer or having a giant $Q1$ in the synapse. More specifically, we tuned the P-type/N-type transistor (P/N) ratio of $INV1$ of the training circuit in Figure 4. Table 4 summarized the required sizes of $INV1$ and $Q1$ under different combinations of successful training parameters. The result shows that the asymmetric design with P/N ratio = 0.5 can obtain the smallest area. The last option was used in the following synapse analysis.

Table 4. Sizing of $INV1$ and $Q1$

P/N Ratio	PMOS/NMOS in $INV1$	$Q1$
2	720 nm/ 360 nm	$18 \times 220 \text{ nm}$
	440 nm/ 220 nm	$16 \times 220 \text{ nm}$
1	360 nm/ 360 nm	$12 \times 220 \text{ nm}$
	220 nm/ 220 nm	$11 \times 220 \text{ nm}$
0.5	360 nm/ 360 nm	$9 \times 220 \text{ nm}$
	220 nm/ 440 nm	$9 \times 220 \text{ nm}$

4.1.4 2-Synapse Design with an OR Logic Neuron. To demonstrate the functionality of a circuit composed of multiple synapses, we used a 2-synapse circuit with an OR logic neuron. The functionality of this structure could be summarized as

$$V_{out} = A1 \cdot M1 + A2 \cdot M2. \quad (10)$$

Based on $M1$ and $M2$ combinations, the structure could be configured into four possible logics: 0, $A1$, $A2$, and $A1+A2$. Eq. (5) shows that $M1$ and $M2$ are independent to each other. We could also train each path separately. By applying ‘1’ to $A1$ and ‘0’ to $A2$ and comparing V_{out} and D_{train} , we can train the memristor $M1$. Similarly, the memristor $M2$ can be trained independently by applying ‘0’ to $A1$ and ‘1’ to $A2$.

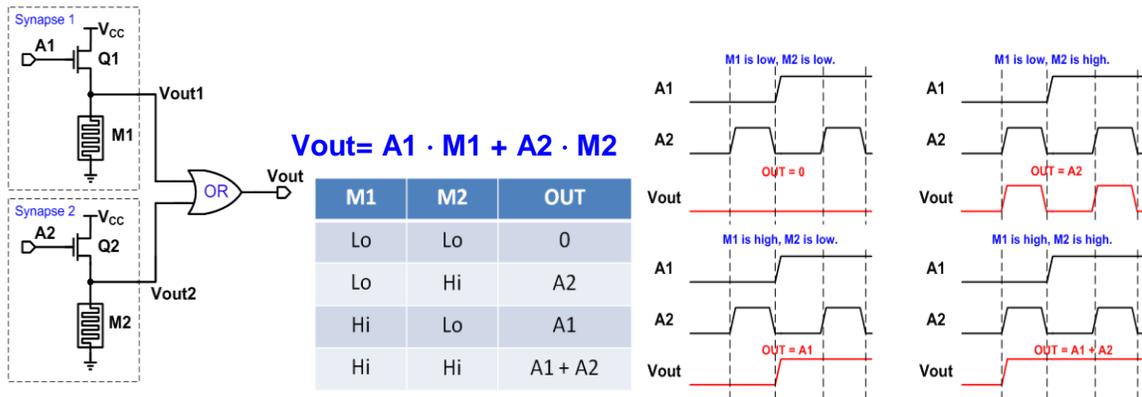


Figure 24. A design with two synapses and its four possible outputs

We could use two one-cell training block shown in Figure 4 to train $M1$ and $M2$ individually. Such a 2-synapse circuit with training blocks is shown in Figure 25. Here, we add $Q2$ and $Q4$ to help control the synapse training. When training enable E was low, both $Q2$ and $Q4$ were turned on to generate V_{out1} and V_{out2} , respectively. When E was high and the circuit was in training mode, either $Q2$ or $Q4$ was turned off to train $M1$ or $M2$, respectively. The two PMOS transistors $Q2$ and $Q4$ were used to control the access of two different memristor rail paths, i.e., *synapse 1* and *synapse 2*, when either reading or training.

The simulation result is also shown in Figure 25. This case study started with both $M1$ and $M2$ as high. First, we separately trained them to low and then changed them back to high again. To verify the training results, a logic test was conducted before and after a training. There are three logic tests in Figure 25(a). The logic test (nanoseconds) was much faster than the training process (milliseconds). Hence, we highlighted the inset of the logic tests at 0 s, 200 ms, and 400 ms, in Figure 25(b-d), respectively.

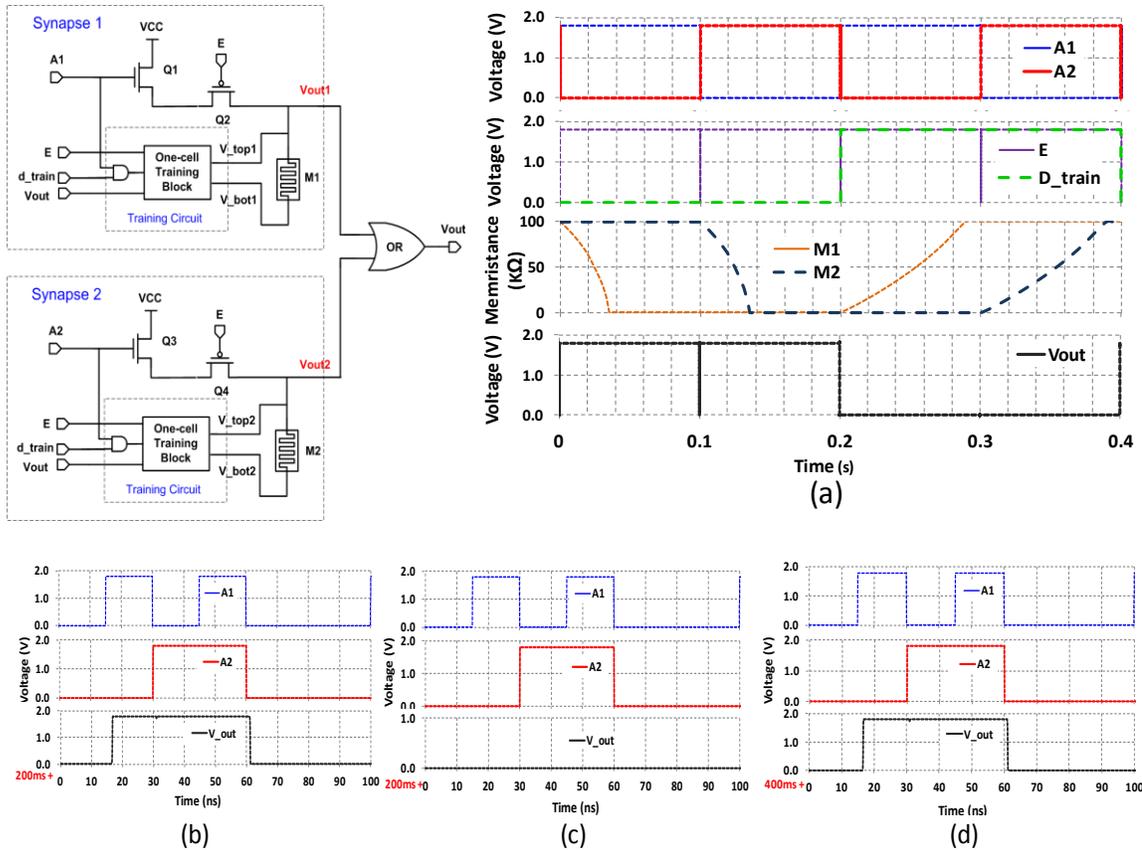


Figure 25. The 2-synapse training circuit and simulation results

At the beginning ($t = 0$ s), $M1 = M2 = 1$ and $V_{out} = A1 + A2$. After training ($t = 200$ ms), $M1$ and $M2$ were low, $M1 = M2 = 0$, and V_{out} remained at 0 without respect to any applied input. By $t = 400$ ms, both memristances were trained back to high, and $V_{out} = A1 + A2$. The timing diagram in Figure 26 graphically depicts our training strategy.

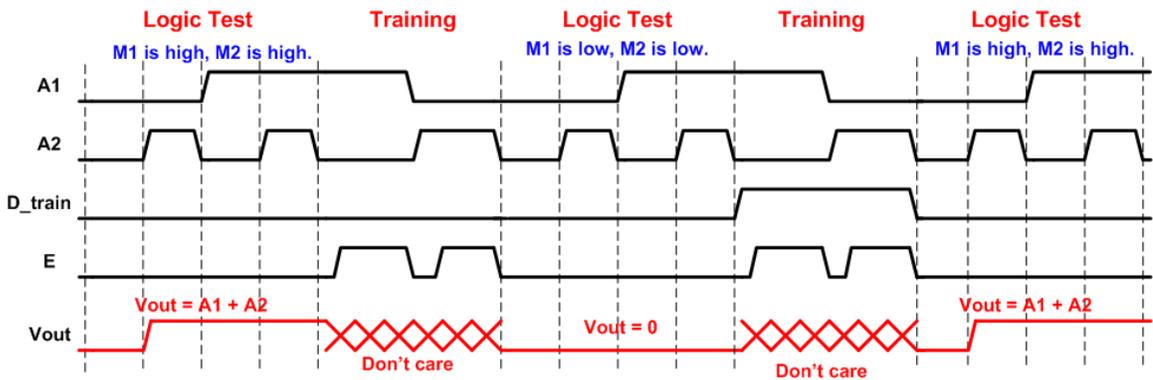


Figure 26. The timing diagram of a 2-synapse training procedure

4.1.5 Self-training mode. To improve the training time and reduce power consumption, we introduced the concept of self-training to our design. Rather than using a fixed long training period, i.e., 51 ms, the self-training mode automatically stopped programming the memristor whenever V_{out} and D_{train} became the same.

The proposed training circuit supported a self-training mode by dividing a long training period into multiple shorter periods and detecting V_{out} between the periods. The programming period needed to be carefully selected. If it was too short, the delay and energy overhead induced by V_{out} detection might overwhelm the benefit of self-training. On the contrary, a long programming period would not show significant improvement.

The simulation result in Figure 27 shows the memristance change over increasing programming periods from (5.1 to 51) ms in 10ms steps. Obviously, the self-training mode could significantly reduce the required training time. In theory, the proposed training circuit could train the memristance to any value between R_H and R_L . The training time in practice would be determined by the specific application and neuron functionality.

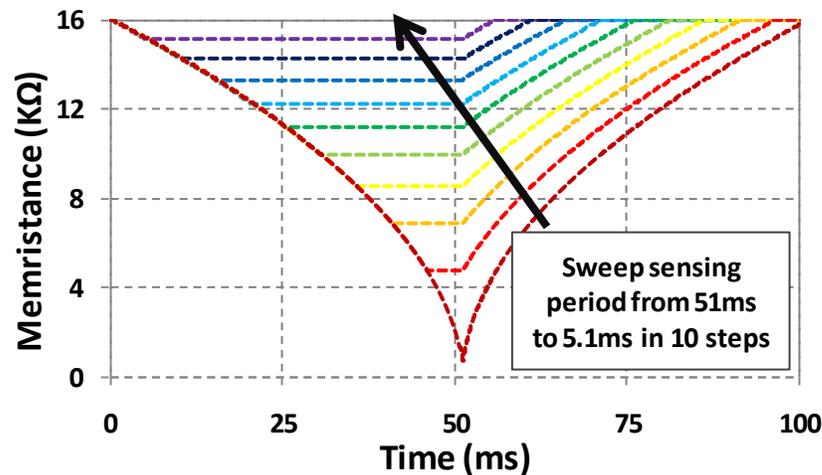


Figure 27. Self-training simulation

4.1.6 Power Analysis. The expected power consumption of reading and training operations are presented in Table 1. The energy value was obtained for a set read time and write time of 4.5 ns and 51 ms, respectively. Compared to the separated training circuit for each memristor, the shared scheme could reduce 26% of training circuit transistor count. More saving in cost and area can be obtained when utilizing this training sharing distribution scheme to multi-synapse structure with more inputs.

Table 5. Synapse Power Consumption Analysis

Operation		Power	Energy
Read	R_L	1.04 mW	4.68 pJ
	R_H	113.4 uW	0.51 pJ
Training	From R_H to R_L	216.7 uW	11.1 uJ
	From R_L to R_H	234 uW	11.9 uJ

4.2. The Functionality Verification of 8-bit ALU Design

In this section, we will demonstrate addition, subtraction, and counting functionalities of the proposed synapse-based ALU design. Though our simulations proved the functionality of the ALU design, it is impractical to graphically present all possible input combinations. Only a few representative input combinations are presented.

4.2.1 Addition. Figure 28 is the simulation result of the addition function. In the first testing period, we set the addend and summand to ‘10011001’ and ‘00010010’, respectively. After 16 ns, we change the summand to ‘00111011’. The first expected final result ‘10101011’ was achieved after 4.46 ns, and the second expected final result ‘11010100’ was achieved after 22.9 ns.

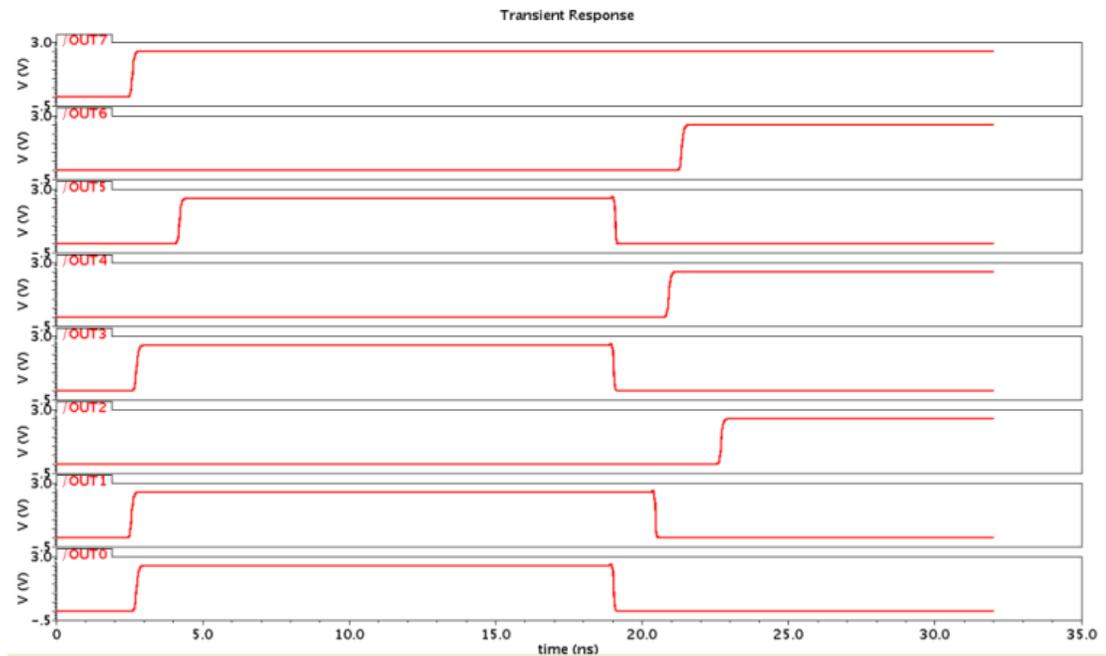


Figure 28. Simulation results of the 8-bit adder

4.2.2 Subtraction. Figure 29 is the simulation result of subtraction function. In the first testing period, we set the minuend and subtrahend as ‘10011001’ and ‘00010010’, respectively. After 16 ns, we changed the minuend and summand to ‘11011001’ and ‘00111000’, respectively. The first expected final result ‘01011110’ was achieved after 5.12 ns and the second expected final result ‘10100001’ was achieved after 27.15 ns.

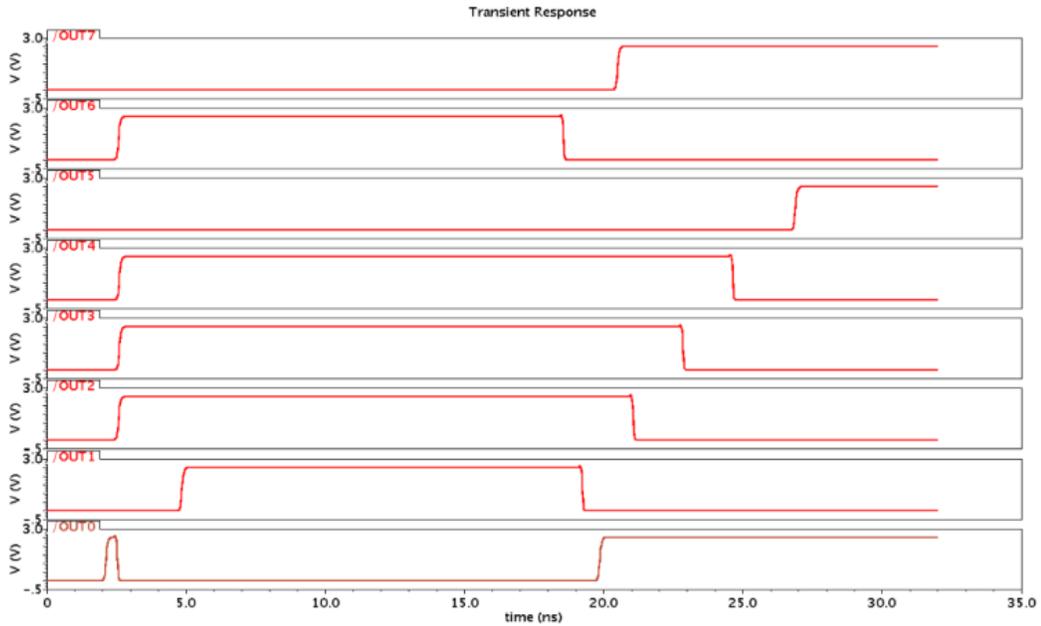


Figure 29. Simulation results of the 8-bit subtractor

4.2.3 Binary Counting. Figure 30 presents the simulation results for an 8 ns clock period applied to the 8-bit binary counter.

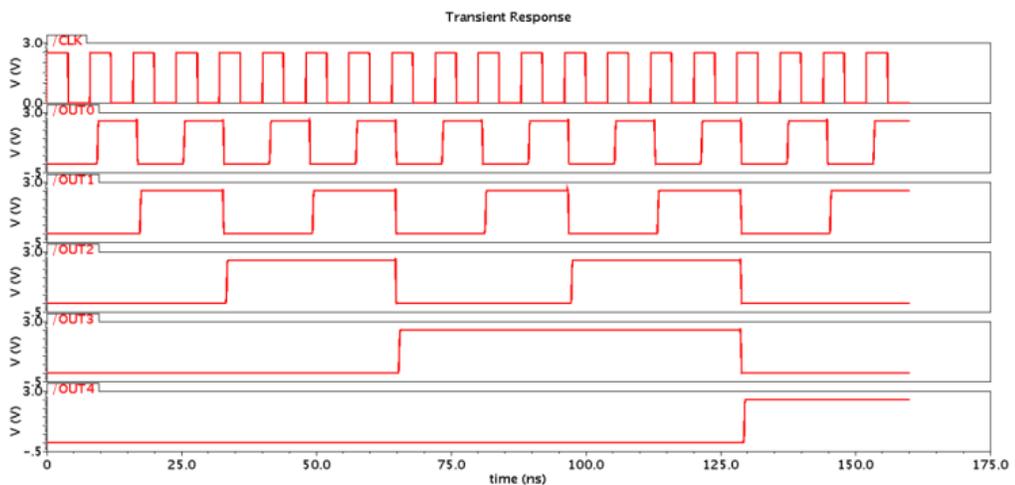


Figure 30. Simulation results of the 8-bit binary counter

5.0 CONCLUSIONS

In this project, we proposed a novel synapse design based on the emerging memristor technology. The corresponding logic design to enable the adaptive logic functionality including the synapse design scheme, training circuitry, multi-level synapses, and training strategy was investigated. The proposed synapse design can be used to construct reconfigurable systems. A two level synapse design was used to illustrate the design and training concept. Then an 8-bit ALU capable of realizing addition, subtraction, and binary counting functionality was designed and verified using TSMC 0.18 μ m technology. Layout for fabrication was completed for this design.

In the next stage of our project, we plan to extend our research of the memristor-based reconfigurable system design into a broader context, including developing the design automation design flow and the scalable design methodology of large-scale synapse circuits.

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APPENDIX A - Publications and Presentations

1. H. Li and R. E. Pino, Statistical Memristor Model and Its Applications in Neuromorphic Computing, a book chapter in *Advances in Neuromorphic Memristor Science and Applications*, edited by R. Kozma, R. E. Pino, and G. Paziienza, Springer, 2012.
2. Y.-C. Chen, H. Li, W. Zhang, and R. Pino, “3-Dimensional High-Density Interleaved Memory for Bipolar RRAM Design,” to appear in *IEEE Transaction on Nanotechnology*.
3. H. Li, R. Pino, Y. Chen, M. Hu, and B. Liu, “Statistical Memristor Modeling and Case Study in Neuromorphic Computing,” *Design Automation Conference (DAC)*, June 2012, pp. 585-590.
4. H. Wang, H. Li, and R. E. Pino, “Memristor-based Synapse Design and Training Scheme for Neuromorphic Computing Architecture,” *International Joint Conference on Neural Networks (IJCNN)*, June 2012.
5. X. Bi, C. Zhang, H. Li, Y. Chen, and R. Pino, “Spintronic Memristor Based Temperature Sensor De-sign with CMOS Current Reference,” *Design, Automation & Test in Europe (DATE)*, Dresden, Germany, March 2012, pp. 1301-1306.
6. M. Hu, H. Li, and R. E. Pino, “Statistical Model of TiO₂ Memristor and Applications,” *International Conference on Computer Aided Design (ICCAD)*, November 2011, pp. 345-352.
7. Y.C. Chen, H. Li, W. Zhang, and R. Pino, “3D-HIM: A 3-Dimensional High-Density Interleaved Memory for Bipolar RRAM Design,” *IEEE/ACM International Symposium on Nanoscale Architectures (NANOARCH)*, June 2011, pp. 59-64.
8. Y.C. Chen, H. Li, Y. Chen, and R. Pino, “3D-ICML: A 3D Bipolar ReRAM Design with Interleaved Complementary Memory,” *Design, Automation & Test in Europe Conference and Exhibition (DATE)*, March 2011, pp. 1-4.
9. M. Hu, H. Li, Y. Chen, X. Wang, and R. E. Pino, “Geometry Variations Analysis of TiO₂-based and Spintronic Memristors,” *the 16th Asia and South Pacific Design Automation Conference (ASPDAC)*, Jan. 2011, pp. 25-30. (**Best Paper Nomination, 1 out of 28 in track, 3.6%**)
10. M. Hu, H. Li, Y. Chen, and R. E. Pino, “Statistical Model of TiO₂ Memristor,” *the 48th Design Automation Conference (DAC)*, in WIP track, June 2011.

LIST OF ABBREVIATIONS AND ACRONYMS

ALU	arbitrary logic unit
P/N	P-type/N-type transistor
TSMC	Taiwan Semiconductor Manufacturing Co.