PROPER-MOTION STUDY OF THE MAGELLANIC CLOUDS USING SPM MATERIAL

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ABSTRACT

Absolute proper motions are determined for stars and galaxies to \( V = 17.5 \) over a 450 deg\(^2 \) area that encloses both Magellanic Clouds. The proper motions are based on photographic and CCD observations of the Yale/San Juan Southern Proper Motion program, which span a baseline of 40 years. Multiple, local relative proper-motion measures are combined in an overlap solution using photometrically selected Galactic disk stars to define a global relative system that is then transformed to absolute using external galaxies and \textit{Hipparcos} stars to tie into the ICRS. The resulting catalog of 1.4 million objects is used to derive the mean absolute proper motions of the Large Magellanic Cloud (LMC) and the Small Magellanic Cloud (SMC); \( \mu_\alpha \cos \delta, \mu_\delta \) \textit{LMC} = \( (1.89, +0.39) \pm (0.27, 0.27) \) mas yr\(^{-1} \) and \( \mu_\alpha \cos \delta, \mu_\delta \) \textit{SMC} = \( (0.98, -1.01) \pm (0.30, 0.29) \) mas yr\(^{-1} \). These mean motions are based on best-measured samples of 3822 LMC stars and 964 SMC stars. A dominant portion (0.25 mas yr\(^{-1} \)) of the formal errors is due to the estimated uncertainty in the inertial system of the \textit{Hipparcos} Catalog stars used to anchor the bright end of our proper motion measures. A more precise determination can be made for the proper motion of the SMC relative to the LMC; \( \mu_\alpha \cos \delta, \mu_\delta \) \textit{SMC-LMC} = \( (-0.91, -1.49) \pm (0.16, 0.15) \) mas yr\(^{-1} \). This differential value is combined with measurements of the proper motion of the LMC taken from the literature to produce new absolute proper-motion determinations for the SMC, as well as an estimate of the total velocity difference of the two clouds to within \( \pm 54 \) km s\(^{-1} \). The absolute proper-motion results are consistent with the Clouds' orbits being marginally bound to the Milky Way, albeit on an elongated orbit. The inferred relative velocity between the Clouds places them near their binding energy limit and, thus, no definitive conclusion can be made as to whether or not the Clouds are bound to one another.

Key words: astrometry – catalogs – Magellanic Clouds – proper motions

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1. INTRODUCTION

The Magellanic Clouds have provided astronomers with a wide variety of information, from the small to the large hierarchy of objects in the universe. They are the first step in the cosmic-distance ladder, as well as a proxy for the low-metal gas-rich galaxies assembled in the early universe, they have zones of recent massive star formation, young 1–3 Gyr globular clusters, and a variety of old pulsating stars and planetary nebulae. They contain substantial amounts of gas and dust in a violent interstellar medium, harbor the closest supernova in recent years, and are being used as a testbed for dark matter searches.

The Magellanic Clouds are also the prime example of a galaxy–galaxy interaction, based on several lines of evidence, close enough to be studied in detail: an apparently starless Magellanic Stream trails the Clouds (Mathewson et al. 1974; Penston 1982); a bridge of gas and stars connects the Clouds (Hindman et al. 1963; Irwin et al. 1985); a gaseous Leading Arm precedes the clouds (Putman et al. 1998); an H\textsc{I} envelope surrounds the whole system and a collection of high-velocity clouds seems to be “raining” over the Galaxy (Olano 2004). Despite such convenient observational circumstances, on the theoretical side, no dynamical model has been able to reproduce all these phenomena simultaneously.

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It is widely accepted that the complexity and intricacies of the Magellanic Clouds’ external and internal features, have been largely determined by the orbit they have followed in the past few Gigayears. Due to their large distance, about 50 and 60 kpc to the Large Magellanic Cloud (LMC) and the Small Magellanic Cloud (SMC), respectively, only radial velocities were precise enough to provide some assessment of their spatial velocity. In fact, line-of-sight measurements of the Clouds began about a hundred years ago (Wilson 1915), while proper-motion measurements of a useful accuracy were possible only in the 1990s.

The first proper-motion results (Jones et al. 1989; Tucholke & Hiesgen 1991; Bastian et al. 1993; Lin 1993; Kroupa et al. 1994; Jones et al. 1994; Irwin et al. 1996; Kroupa & Bastian 1997a, 1997b, 1997c; Anguita 1999) based on plate and/or CCD data, were compatible with a picture in which the Magellanic Clouds were bound to each other and to the Milky Way. Such scenario relied heavily on the fact that the Galactic gravitational potential used (isothermal sphere) yields such results by default, and proper-motion errors were not small enough to refine the tangential velocities.

Absolute proper motions are determined for stars and galaxies to $V = 17.5$ over a 450 deg$^2$ area that encloses both Magellanic Clouds. The proper motions are based on photographic and CCD observations of the Yale/San Juan Southern Proper Motion program, which span a baseline of 40 years. Multiple, local relative proper-motion measures are combined in an overlap solution using photometrically selected Galactic disk stars to define a global relative system that is then transformed to absolute using external galaxies and Hipparcos stars to tie into the ICRS. The resulting catalog of 1.4 million objects is used to derive the mean absolute proper motions of the Large Magellanic Cloud (LMC) and the Small Magellanic Cloud (SMC); $\mu_{\alpha,\cos \delta}$ and $\mu_{\delta}$ LMC = $(1.89, +0.39) \pm (0.27, 0.27)$ mas yr$^{-1}$ and $(0.98, -1.01) \pm (0.30, 0.29)$ mas yr$^{-1}$. These mean motions are based on best-measured samples of 3822 LMC stars and 964 SMC stars. A dominant portion $(0.25 \text{ mas yr}^{-1})$ of the formal errors is due to the estimated uncertainty in the inertial system of the Hipparcos Catalog stars used to anchor the bright end of our proper motion measures. A more precise determination can be made for the proper motion of the SMC relative to the LMC; $(\mu_{\alpha,\cos \delta}, \mu_{\delta}) \text{SMC-LMC} = (-0.91, -1.49) \pm (0.16, 0.15)$ mas yr$^{-1}$. This differential value is combined with measurements of the proper motion of the LMC taken from the literature to produce new absolute proper-motion determinations for the SMC, as well as an estimate of the total velocity difference of the two clouds to within $\pm54$ km s$^{-1}$. The absolute proper-motion results are consistent with the Clouds’ orbits being marginally bound to the Milky Way, albeit on an elongated orbit. The inferred relative velocity between the Clouds places them near their binding energy limit and, thus, no definitive conclusion can be made as to whether or not the Clouds are bound to one another.
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2000; Momany & Zaggia 2005) were found to have unknown or important systematic errors. More interestingly, Hubble Space Telescope (HST)-based results (Kalivayalil et al. 2005, 2006a, 2006b, 2009; Platais et al. 2008) coupled to more modern and cosmologically inspired dark matter Halo models, suggest that the Clouds are not bound to the Galaxy, opposite to the long-held paradigm.

Twenty years have passed since the very first proper-motion measurements of the Clouds, and it is only now with the Yale-San Juan Southern Proper Motion (SPM) program—briefly explained in Section 2—that for the first time a wide-field astrometric proper motion survey of the Magellanic System is finally completed. All the first-epoch (early 1970s) and part of the second-epoch (early 1990s) SPM material used in this work are photographic plates. Their processing is briefly summarized in Section 3, but a more detailed explanation can be found in T. M. Girard et al. (2010, in preparation).7 A substantial part of our second-epoch data comes from SPM CCD observations. A short explanation of the data acquisition, quality control, and processing is explained in Section 4. To supplement our second-epoch plate data with CCD-quality positions, we have included more positions at Julian epoch 2000.0 from the UCAC2 catalog (Zacharias et al. 2004). Section 5 explains how these data were selected and included in this investigation.

In contrast to other SPM reductions, as explained in Section 6, relative proper motions measured in CCD-size fields of view were combined into a single common extended and accurately defined global system. Although our zero point accuracy, i.e., how well our reference frame is linked to the International Celestial Reference System (ICRS), is ultimately limited by Hipparcos accuracy, our very precise relative proper motions over the whole field of view (FOV), enabled us to measure the proper motion of the SMC with respect to the LMC, at a precision comparable to the quoted errors of space-based proper motions.

It is this capability that we exploit to obtain new measurements of the proper motion of the SMC based on previously published LMC proper motions. Section 7 contains the main results of this paper regarding the proper motion of the Clouds, absolute and relative. Section 8 has a discussion of the implications of our results on the current understanding of the dynamics of the Magellanic System. Finally, Section 9 states the conclusions of this paper, and future plans already in consideration to improve the current results.

2. THE SPM PROGRAM

This investigation is part of the SPM program, a joint venture of Yale University and Universidad Nacional de San Juan in Argentina. The SPM program was initiated in the early 1960s by D. Brower and J. Schlitt as a joint enterprise of the Yale and Columbia Universities (Wesselink 1974). The goal of the SPM program is to provide absolute proper motions, positions, and BV photometry for the Southern sky to a limiting magnitude of V ~ 18.

The SPM program makes use of the Yale Southern Observatory’s double astrograph at Cesco Observatory in the foothills of the Andes mountains in El Leoncito, Argentina. This telescope consists of two 51 cm reflectors, designed for photography in the blue and yellow bands, respectively. The first-epoch survey, taken between 1965 and 1974 was made on glass photographic plates, exposed simultaneously in blue–yellow pairs and always centered on the meridian. The plates’ FOV extends over an area of 6°3 × 6°3. The sky south of δ = −17° was observed in the first-epoch period.

Second-epoch SPM plate observations were begun in 1988. By the mid 1990’s, with only a third of the second-epoch survey completed, Kodak discontinued the production of the photographic plates. In 2000, with funding from the NSF, a CCD camera system was installed on the double astrograph to replace the photographic plate holders. A PixieVision 4K × 4K CCD camera (0°94 × 0°94 FOV) was placed in the yellow lens focal plane, and an Apogee Ap-8 1K × 1K (0°37 × 0°37 FOV) was fitted in the blue focal plane. In 2004, the Apogee 1K camera was upgraded to an Apogee Alta E42 2K × 2K (0°42 × 0°42 FOV) with funds from the Argentine CONICET. In order to achieve a limiting magnitude similar to the first-epoch plate material, the CCD survey consists of 2 minute exposures in both cameras.

In the past decade, catalogs of the SPM program covering various parts of the sky have been published, as the second-epoch material became available for its astrometric reduction. Catalogs SPM1 (Platais et al. 1998), SPM2 (van Altena et al. 1999), and SPM3 (Girard et al. 2004) are based on photographic plates only, in both first and second epochs. The plates were scanned either with the Yale PDS (using input lists of selected objects) or the USNO Precision Measuring Machine (PMM) for the whole plate. Also, two different centering algorithms have been used to measure the image centers in the scans, the Yale two-dimensional Gaussian fit from Lee & van Altena (1983), or the USNO circular fit from Monet et al. (2003).

Since 2004, regular CCD observations have been carried out to finish the second-epoch survey of the SPM program. By 2008 December, the survey was effectively completed for the sky south of δ = −20°. Subsequently, the SPM4 catalog, based on all available plate and CCD data, was completed in late 2009 and is currently available, (T. M. Girard et al. 2010, in preparation). SPM4 includes ~100 million objects south of δ = −20°, brighter than V ~ 18. Many of the data-processing procedures, software, and protocols developed in this investigation were also used in the construction of the SPM4 catalog.

3. THE PLATE DATA

3.1. Observations

The SPM survey fields are on 5° centers in declination and a maximum of 5° separation in right ascension, providing at least a full degree overlap between adjacent plates. Each 17 inch × 17 inch plate covers an area of 6°3 × 6°3 (55''1 mm−1 plate scale) and consists of a 2 hr and a 2 minute offset exposure. All observations were made with a wire grating over the objectives, producing measurable diffraction images out to third order. The grating constant is 3.8 mag, thus, along with the offset, very short exposure, effectively increasing the dynamic range of each plate allowing measurement of external galaxies and bright Hipparcos stars. Fields were observed simultaneously in blue and yellow passbands, and there are some fields with repeated blue and/or yellow plates from the same epoch. See Girard et al. (2004) for a more complete description of the SPM plate material.

Table 1 lists the SPM plates used in this investigation. During the course of this research, it was found that some plates yielded unusually deviant results. A visual examination of the suspect plates revealed that the stellar images suffered from significant defects, possibly caused by poor guiding, polar misalignment,
or poor focus. These plates, 0750B, 0751B, 1371B, 1357Y, and 1373Y, were therefore discarded for the research presented here. Coverage in these areas was not affected, since only one of the two plates at a given epoch per field affected was discarded. Figure 1 shows the distribution on the sky of the plates used in this work. Twenty-two (22) SPM regions were studied, of which seven (7) have second-epoch plates. For the areas with second-epoch plate data, no second-epoch CCD observations were made.

3.2. Astrometric Reduction and Photometric Calibration

The SPM plates used in this investigation were scanned with the PMM of the USNO Flagstaff Station. For more details about the PMM setup and operations, see Monet et al. (2003). In a collaboration between the USNO-Washington and the Yale Astronomy Group, the StarScan reduction pipeline (Zacharias et al. 2008) was modified to analyze the PMM pixel data of the SPM plates to produce a list of detections, image centers and photometric indices. The astrometric and photometric reductions then proceeded as follows: (1) cross-identification of detections to an input catalog, including (2) recognition and identification of central and higher grating orders, (3) photometric calibration to obtain $B V$, (4) correction for atmospheric refraction, (5) correction for Magnitude Equation, which also combines grating-order systems, (6) transformation of short-exposure positions into the long-exposure system, and (7) astrometric solution into Tycho-2 to obtain $(\alpha, \delta)$. The input catalog referenced in step (1) is a compilation of the following external catalogs: Hipparcos (Perryman & ESA 1997), Tycho-2 (Hogg et al. 2000), UCAC2 (Zacharias et al. 2004), 2MASS point-source and extended-source (Skrutskie et al. 2006), LEDA galaxies with DENIS measurements (Paturel et al. 2005), and the QSO catalog of Véron-Cetty & Véron (2006). In order for an object to be included in our study, it must appear in one or more of these listed catalogs. A thorough explanation of all these procedures can be found in T. M. Girard et al. (2010, in preparation). After the above processing, one has positions $(x, y)$ properly calibrated into a common system within each plate, with computed positional errors and astronomical coordinates $(\alpha, \delta)$ on the ICRS, as realized by Tycho-2.
3.3. Evaluation of the Plate Data

Well measured stars on the plates in all of the orders have positional errors between 0.9 μm and 1.6 μm (50 mas and 90 mas). These errors, which only assess measurement uncertainties, are consistent with the precision expected for a good centering procedure, based on previous experience with the SPM plates.

A single final position (x, y) per star per plate is obtained, from the positional-error-weighted-average of the available measurements. As expected, the error of the final position and magnitude will depend on the number of grating orders contributing to their calculation. If average measurements from different plates were later averaged to obtain a final number, then other errors, random and systematic, would come into play, and contributing to their calculation. If average measurements from the positional-error-weighted-average of the available measurements are consistent with the precision expected for a comparison with the evaluated in a CeD-size field in sources of uncertainty.

As with earlier SPM catalogs, an approximate estimate of the relative completeness between the plate data and Two Micron All Sky Survey (2MASS), can be made. Figure 2 shows the V magnitude distribution of all stars detected on a yellow plate, compared to the VJK magnitude distribution of all 2MASS point source stars in the same field. VJK = J + 2.79(J - K) is an approximate empirical transformation from 2MASS JHK to V determined by Girard et al. (2004) and found to be valid for a relatively wide range of spectral types. It can be seen that the SPM plates have a completeness similar to that of 2MASS up to V = 17.5 and a falloff after that.

In general, compared to previous SPM processing, these plate data have significantly fewer false detections, and a better correction of systematics in the detected positions associated with the scanning process.

3.4. SPM Second-epoch Plate Data

As explained in Subsection 3.1, seven SPM fields have second-epoch plates. For this reason, no second-epoch CCD observations were made at these locations. In order to facilitate the managing of files and software, the second-epoch plates were divided in CCD-size fields, to emulate the overlap scheme of the second-epoch CCD frames (see Section 4.2). This way, all the second-epoch material, regardless of its type, would have a uniform format and structure, for programming purposes. From the about 90 CCD pointings that usually cover one SPM field, half were used to divide the blue plate and the other half to divide the yellow plate, in such way that these yellow and blue fields overlap in a similar way as do the real CCD frames.

4. THE CCD DATA

4.1. CCD Cameras

The CCD system consists of four cameras, one each for the blue- and yellow-optimized lenses and two focus-sensor cameras, again, one for each lens. The CCD camera for the yellow telescope is a PixelVision camera with a Cryotiger Chiller cooled (−85 °C) 4K × 4K Loral chip with 15 μm pixels, which translates into a pixel size of 0.93 and a total area of 0.94 x 0.94 degrees. The pixel size is well matched to the YSO site where the seeing conditions usually yield an image FWHM of 2–3′, corresponding to 3–4 pixels per FWHM. This is optimal sampling for the derivation of astrometric image centers, based on SPM experience with digital image centering. The unthinned and front-illuminated Loral chip is fitted with a fixed custom scientific V-band filter.

The blue telescope was first fitted with an Apogee AP-8 camera that utilized a thermoelectrically cooled (−40 °C) and back-illuminated 1K × 1K Site chip with 24 μm pixels, which translated into a pixel size of 1.32 and a total area of 22.57 x 22.57. In 2005 May, an upgrade was made by replacing this camera with a new Apogee Alta E42 back-illuminated 2 K × 2 K chip, with 15.5 μm pixels, which correspond to a pixel size of 0.74 and a total area of 24.8 x 24.8. Centered on the same field as the larger PV yellow camera, the purpose of the blue CCD camera is to provide B-band CCD photometry for the stars that fall into its FOV.

Data from the yellow PV camera were used for both astrometry and photometry, while the blue Apogee and Alta cameras observations were used only for the photometric calibration of the blue plates.

4.2. Observations

As a norm for the SPM, CCD observations are done always within 1°30' of the meridian, in 2 minute exposures, with the wire grating placed so that the diffraction pattern is at about 45° from the E–W line. Normally, an E–W orientation is ideal to avoid differential color refraction effects within the diffraction pattern, but in this case, a diagonal orientation prevents the saturated central-order image of a bright star from spoiling its grating images by either row or column bleeding. The CCD pointings conform to a two-fold overlap coverage scheme for the PV camera, as shown in Figure 1. About 90 PV CCD frames cover one single SPM field. Only targets that did not have second-epoch plate data were observed with the CCD, except for a few special targets.

A total of 1310 CCD pointings were observed for this investigation. Each pointing was planned to be observed only once, except for 90 of them extending over a 6° × 6° field at (α, δ) = (3°44′33″, −71°40′18″), within the area delimited by the bold black line in Figure 1. This area corresponds to the non-SPM field for the variable stars in the Magellanic Clouds (VMC) study done from 1965 to 1968 by A. J. Wesselink, and comprises seventy 60 minute exposure blue plates without the wire objective grating, reaching a limiting magnitude of about 18. Numerous repeated CCD observations were performed on this area to provide suitable second-epoch observations for this material. The VMC plates were not used for this work because...
they require their own special reduction, different from the one used in normal SPM plates, but the repeated CCD observations were indeed used for this investigation. The VMC CCD targets have at least 13 good observations each, with some of them having up to 20 good observations.

The criteria used to qualify an observed frame as acceptable are: FWHM $\leq 3.5$, limiting magnitude $V_{\text{lim}} \geq 17$, and standard error $\leq 120$ mas from an astrometric solution into the UCAC2. If a frame fails any of these limits then it was taken again until it passed all of them. Nonetheless, all frames regardless of quality are saved and processed, and only later in the astrometric reduction are discarded, if they prove to be too bad for any use. In total, 5422 CCD frames were processed for this investigation.

4.3. Astrometric Reduction and Photometric Calibration

Data from all the CCD cameras went through the usual processing to calibrate the flux detected by the electronics, for the zero charge of the chip (bias), accumulated signal from the electronics dark current (dark) and different response to light from each pixel (flat). Details of these procedures can be found in T. M. Girard et al. (2010, in preparation).

Image detection on the processed CCD frames is done using SExtractor Version 2.4.4 (Bertin & Arnouts 1996), from which a preliminary centroid and an aperture instrumental magnitude are read. SExtractor centroids are then used as input positions to compute more precise centers, based on the Yale two-dimensional Gaussian centering algorithm (Lee & van Altena 1983). Typically, more than 90% of SExtractor detections are centered. A significant reduction in the rms of the positions for repeated observations of the PV frames was found when using the Yale-based centers as compared to the SExtractor-based centroids.

The process of transforming the Yale-based centers $((x,y))$ and SExtractor-based instrumental-magnitudes $m_{\text{rot}}$ into calibrated $(\alpha, \delta)$ and $BV$, for the CCD frames, follows a procedure similar to that of the plates (Section 3.2), with the exception that the external catalog used for the astrometric reduction of the CCDs is UCAC2 (T. M. Girard et al. 2010, in preparation). As a result of these procedures, all the detected positions $(x, y)$ are properly calibrated within each CCD frame, with computed positional errors and equatorial coordinates $(\alpha, \delta)$ in the ICRS, as realized by UCAC2.

4.4. Evaluation of the CCD Data

The single-image centering precision for well measured stars $(V < 15)$ in the CCD frames is 0.5 $\mu$m (25 mas), worsening for the faintest stars where it reaches about 2 $\mu$m (100 mas). A single final position $(x, y)$ and magnitude per star per CCD is obtained, from the positional-error-weighted-average of the available measurements. The final positional and photometric errors will depend on the various image orders contributing to the final value. At this point, each star in each CCD frame has a master ID identification, a position $(x, y)$ with errors, a calibrated $B$ or $V$ magnitude and a UCAC2-based $(\alpha, \delta)$. Because stars were identified in the CCD frames in the same way as in the plates, similar characteristics regarding completeness were expected when compared to 2MASS (see Figure 2). The CCD data show in general a completeness magnitude of about $V = 18$.

5. UCAC2 CCD-POSITIONS AS SUPPLEMENT FOR THE 2ND-EPOCH PLATE DATA

As seen in Figure 1, some fields on and adjacent to the Magellanic Clouds have only photographic plates as second-epoch material. Given the lower quality of plate images compared to CCD observations, the measured proper motions in these plate-only fields, will have significantly larger errors than those coming from the combination of plate and CCD data. In an attempt to counter this and achieve a more homogeneous quality in the final measurements, we decided to supplement the second-epoch plate measures with epoch 2000 positions from the UCAC2 Catalog (Zacharias et al. 2004). These are mostly based on CCD observations $^8$ with the USNO 8 inch (0.2 m) Twin Astrograph from Cerro Tololo International Observatory in Chile. The UCAC2 data were collected in such way that it mimics our second-epoch fields. The precision of the positions is 15 to 70 mas, depending on magnitude, with claimed estimated systematic errors of 10 mas or below. UCAC2 provides only crude magnitudes in a single nonstandard bandpass $R_{\text{UCAC}}$ between $V$ and $R$, and its limiting magnitude is about $R \approx 16$.

A significant number of faint stars in our second-epoch SPM plates do not have a counterpart in the UCAC2 catalog. This means we are only sampling stars about $V < 16$ for these SPM fields when using UCAC2 positions. UCAC2 completeness compared to 2MASS and SPM data, can be seen in Figure 2.

6. OBTAINING THE PROPER MOTIONS

Given that a substantial part of the second-epoch SPM material used in this work comes from CCD frames, previous SPM procedures for obtaining proper motions (used on first- and second-epoch plates), could not be straightforwardly applied. Since the CCD's FOV is about 40 times smaller than the plate's FOV, the number of reference stars available to measure relative proper motions in each field is proportionally smaller. A simple cut in magnitude, as in past SPM reductions, would result in too few reference objects per CCD frame; in particular, the extragalactic objects needed to transform relative proper motions into absolute ones.

However, if we select reference stars belonging to some specific population of the Galaxy, it is reasonable to assume that they have a mean absolute motion along an extended area on the sky$^9$ that can be parameterized as a smooth function of $(\alpha, \delta)$. Moreover, within a CCD FOV, their mean motion has a very small gradient, if any. It then becomes a matter of precisely quantifying, over the whole FOV, the measured mean relative proper motion of all known extragalactic objects, which is simply the reflex of the mean absolute proper motion of the reference stars. Applying such a function to the measured relative proper motions converts them to absolute.

The layout of the CCD fields, where substantial overlap exists (20% to 50%), contains a wealth of information that can provide linkage of the reference system across the observed region of the Clouds that is limited only by measurement errors. A key point

$^8$ Strictly speaking, the supplemental UCAC2 epoch-2000 positions we use include up to a few years' worth of UCAC2 proper motions. For the areas of sky in this study, the UCAC2 CCD observations were made around 1998. Thus the positions we employ as supplements are practically those of the UCAC CCD program.

$^9$ Stars behave like a collisionless system, all moving under the influence of the same general background gravitational field, therefore we can expect them to have a global smooth distribution in their velocities, with some scatter around a mean value at any given location.
of this investigation is therefore to find a procedure to utilize this large overlap to produce a precise global reference system.

6.1. Relative Proper Motions in the Small CCD FOVs

After all the plate and CCD data processing described above, the following data are ready for the measurement of proper motions.

1. First-epoch positions on the plates, which have been corrected for systematics, as much as Tycho-2 precision and number of stars allows.

2. Second-epoch positions on SPM CCD frames, SPM plates, or from UCAC2. CCD positions are mostly free of systematic errors. Plate positions have been corrected for systematics, as much as Tycho-2 stars precision and number of stars allows.

Henceforth, we will refer to each of the second-epoch CCD-size frames as a brick, regardless of the source of its data (SPM plate, SPM CCD or UCAC2). For each second-epoch brick, the corresponding first-epoch plate area was reprojected onto a tangential plane centered on the brick. Then a quadratic solution was computed to transform the reprojected first-epoch plate’s \((x, y)\) into the second-epoch brick’s \((x, \gamma)\), forcing the chosen reference stars to have zero mean proper motion. The quadratic terms in the solution were meant to model systematic errors, either from the plate (uncorrected Optical Field Angle Distortion) or from Tycho-2 proper-motion systematics\(^{10}\) unavoidably propagated backwards in time into the computed first-epoch \((x, \gamma)\). These solutions yield measured relative proper motions in each brick. The vast majority of the solutions only needed linear terms and the typical standard error of the solutions varied from about 5 to 8 mas yr\(^{-1}\), which is dominated by the intrinsic proper-motion dispersion of the reference stars.

The reference stars were chosen with the following criteria: \(1 < V - J < 1.5, 0.25 < J - K_s < 0.65\) and \(13 < K_s < 15\), which according to Nikolaev & Weinberg (2000) isolates mostly G-M dwarfs in the Galaxy disk, located between 0.4 to 1.6 kpc from us, with an estimated mean distance of \(\approx650\) pc. Their distribution in \(V\) magnitude ranges mostly from \(V = 15\) to \(V = 16.5\). In general there are between 200 and 500 reference stars per field, depending on the galactic latitude (our fields extend from \(b \approx -50^\circ\) to \(b \approx -20^\circ\)). The intrinsic proper-motion dispersion of the Galactic disk reference stars was seen to increase with \(|b|\), reflecting the changing kinematics of the Galaxy along it.

Despite the photometric cuts to select the reference stars, contamination by LMC and SMC stars could not be avoided in the densest parts of the Clouds. This forced us for the time being to restrict our investigation to those fields in which we trust the relative proper motions, as being measured with respect to bona fide Galactic foreground stars. These areas were defined as shown in Figure 3. Although a substantial number of Magellanic Clouds stars were lost in this selection, on the other hand, confusion due to image crowding at these locations render these fields useless anyway, due to the risk of misidentifications.

From the initial 13880 bricks available, 12180 are in the non-contaminated areas. After rejecting bricks from the discarded plates (Section 3.1), 10900 are left to build the catalog of proper motions, mostly outside the Magellanic Clouds. In order to increase the number of LMC and SMC stars measured at the end, contaminated fields that overlap with this non-contaminated catalog were later on directly tied into it, and common stars had their proper motions averaged.

6.2. Combining the Proper Motions

Once relative proper motions with respect to the Galactic foreground stars had been measured in the non-contaminated area, different approaches were tried to combine them into a single global well-defined reference frame. Reference stars were chosen hoping that their mean motion along the sky could be described by a smooth function. This goal was indeed attained as confirmed by the fact that the measured relative proper motion of all known extragalactic objects were very precisely fit by a quadratic polynomial in \((\alpha, \delta)\).

At this point, applying this polynomial to the relative proper motions to convert them to absolute, and then averaging all measurements, is a way to combine all the information available.
per star. But this would yield a catalog with a rather noisy zero point as one moves along the sky, mostly due to the real intrinsic proper motion dispersion of the reference stars and the fact that two overlapping frames may not have the same reference stars. Given two frames with about 50% overlap between them, means that both have 50% of the reference stars in common, while the other 50% are different. Given two samples with \( N \) data points each, both with the same dispersion \( \sigma \) and both having 50% of their points in common, it can be easily shown that their individual mean values typically differ by \( \sqrt{\frac{2}{N}} \sigma \). In other words, we can expect that two overlapping frames typically differ in their relative proper-motion systems by 50%, for \( N = 220 \) and \( \sigma = 6.5 \text{ mas yr}^{-1} \). This is too large for the level of precision that we want to obtain.

A variant of the so-called block adjustment solutions (Eichhorn 1960, 1988; Jeffreys 1979; Stock 1981; Taft 1988) was considered to link every frame’s relative system into a global one. Each frame, containing a sample of the whole population of reference stars, realizes a local system that could deviate from the global system, due to statistical, measurement and/or systematic errors. A linear function per frame was considered sufficient to describe the difference between the frame and the global system. Therefore three parameters per frame, per proper-motion component (\( \mu_x, \cos \delta \) and \( \mu_y \)) are solved separately need to be determined. The coefficients of the quadratic polynomial that globally describes the mean motion of the reference stars are determined as well. To simultaneously solve several thousands frames, we would need to invert an approximately 40,000 \( \times \) 40,000 matrix to get the parameters values and their errors. For this project, such a scheme was deemed impractical at this time. Nonetheless, ideas about using this approach over smaller areas first, like the SPM fields, and then performing another block adjustment solution to join these regions, are being adopted for future work.

A more practical approach was considered to bring each individual frame’s reference system closer to the global one. A single frame’s reference system is statistically more deviant from the global system than is the system defined by all stars, since the proper-motion reference stars are only a subset of all stars. Using all stars in common between overlapping frames, we can adjust each frame’s proper motions to agree with the average of the surrounding fields. This adjustment also helps to correct residual distortions, as they are statistically smoothed out in the average frame. To avoid frames drifting away from the global system as they are being aligned to one another, all reference stars in the field are explicitly assigned a relative proper motion of zero. Once the adjustments are applied, new averages can be computed, and the whole process is iterated until the adjustments converge to zero.

Before making these adjustments, we first checked to see if systematic differences existed as a function of the magnitude. A non-negligible number of frames exhibited systematic trends with magnitude when compared to the average frame (see Figure 4). In general, a linear function of the coordinates in the field would take care of the geometrical distortion, but the magnitude equation required a smoothed-localized median, which can trace the general trend better than any parameterized fit. Therefore, each frame is first corrected for its differential magnitude equation with respect to the average frame, and then we proceed to correct for the distortion, following the iterative procedure explained above. Each frame has typically about 1500 to 2000 stars, with some of them having up to 5000 stars, to compute the adjustments.

With these improved relative proper motions, the quadratic polynomial that describes the mean reflex proper motion of the extragalactic objects was computed and used to transform the relative proper motions into absolute ones. Polynomials for \( \mu_x \cos \delta \) and \( \mu_y \) as functions of \( \alpha \) and \( \delta \) were calculated separately, using proper-motion-error-weighted least squares. A total of 5351 external galaxies were used across the 450 sq-degree area and the formal errors of the polynomials, computed at the center of LMC and SMC, based on the full covariance matrix, amount to 0.03 mas yr\(^{-1}\) and 0.06 mas yr\(^{-1}\), respectively.

At this stage, a final absolute proper motion and its corresponding error are obtained per star, from the error-weighted average of all the individual absolute proper motions obtained for it. A total of 1,337,050 objects in the non-contaminated fields had final proper motions, including a good number of LMC and SMC stars located in the outskirts of these galaxies. For such reason, it is named the outside catalog.

In order to increase the number of LMC and SMC stars with measured absolute proper motions, contaminated fields that overlapped with the outside catalog just obtained, were directly tied into it by computing a linear solution to correct their relative proper motions and put them into its absolute system. A total of 678 additional fields were added with this procedure, eventually increasing the number of LMC and SMC stars by about 30% and 50%, respectively.

6.3. Zero-point Global Correction of the Absolute Proper Motions

Since we are now theoretically on the absolute reference frame defined by the external galaxies, our catalog should be
within measurement errors in the same reference frame system of other known catalogs of absolute proper motion. When we checked our measures ($\mu_\alpha \cos \beta$, $\mu_\beta$) of 1356 $Hipparcos$ stars against the $Hipparcos$ Catalog, we found a significant difference between the two that amounts to

$$\mu_\alpha \cos \beta, Hipparcos - \mu_\alpha \cos \beta, This\ work = -0.49 \pm 0.07 \text{ mas yr}^{-1}$$

(1)

and

$$\mu_\beta, Hipparcos - \mu_\beta, This\ work = -1.21 \pm 0.07 \text{ mas yr}^{-1}.$$  

The source of this systematic difference could be indeed in any (or both) of the two catalogs. Although $Hipparcos$ is the most accurate optical astrometric catalog published so far, it has significant correlations between the astrometric parameters (position, proper motion, and parallax) of different stars, when they are less than about 5° apart on the sky, and also between the astrometric parameters for a given star, due to the special measurement principle of $Hipparcos$ (Perryman & ESA 1997). In fact, a new reduction by van Leeuwen (2007) was performed to correct some systematic correlations in the data. However, no significant difference was found between the old reference frame (used in this investigation) and the new one.

On the other hand, our plate measurements of the galaxies are not error-free. Tests were run to compare the final absolute proper motions if only galaxies with second-epoch CCD data, or all of them, were used to compute the quadratic polynomials to transform relative proper motions into absolute. The polynomial for $\mu_\alpha \cos \beta$ exhibited noticeable differences around the SMC. This was not completely unexpected given that at that location, four SPM fields have plate-only data, but in any case it points to the fact that galaxies in the second-epoch plates may introduce problems. Hence, galaxies in the first-epoch plates may do the same.

As determined by Girard et al. (1998), the SPM plate material exhibits magnitude equation for galaxies and for stars that differ in functional form. However, the two could be brought into approximate agreement by adding an offset of $-0.7$ to the magnitudes of galaxy images before calculating the magnitude-equation correction as derived from stellar images. In the present study, we have applied the same $-0.7$ mag offset to galaxy images for the purpose of magnitude-equation correction only.

A comparison of the $V$ magnitudes for the galaxies in our work, showed that plate photometry returned significantly fainter magnitudes than in CCD calibrations. Not surprisingly, this may have affected the magnitude equation correction in the plates, since it was the calibrated plate photographic magnitude that was used for such purpose. More surprising though, was to find that Equation (1) showed a linear trend versus $\alpha$ with a slope of about 0.15 mas yr$^{-1}$ per degree (a bit smaller when using only galaxies with CCD data). The LMC and SMC center of mass positions are separated by about 20°, for which the trend above indicates a zero point shift of 0.3 mas yr$^{-1}$, that could in principle be related to $Hipparcos$' systematics. On the other hand, systematics in Equation (2) versus $\delta$ were also seen, that look to be related to the plates location and layout.

The investigation of the SPM plates magnitude equation done by Girard et al. (1998) found that magnitude equation terms$^{11}$ varied more or less uniformly from first to second-epoch plates, so we can expect more or less uniform offsets with $Hipparcos$ proper motions, if any residual uncorrected magnitude equation were still present in the data. Consequently, Equations (1) and (2) were applied to all the absolute proper motions, putting our catalog on the system of the ICRS via $Hipparcos$. The inaccuracy of its zero point is dominated mostly by $Hipparcos$' systematic error of 0.25 mas yr$^{-1}$, since the quadratic polynomial, as defined by the external galaxies, was in general very accurate, being within 0.1 mas yr$^{-1}$ of error for most of the 450 deg$^2$ area studied.

6.4. Final Catalog of Proper Motions—Evaluation of Errors

The final catalog of absolute proper motions at this point has 1,448,438 objects, with the following data listed: $\alpha, \delta, V, V - J, J - K_s, H - K_s$ when available; absolute proper motions $\mu_\alpha \cos \beta, \mu_\beta$ and their formal errors $\epsilon_\mu_\alpha \cos \beta, \epsilon_\mu_\beta$ in mas yr$^{-1}$, number of data points used, number of data points rejected (outliers were rejected based on their normalized errors), a flag to indicate $Hipparcos$, Tycho-2, 2MASS extended sources, confirmed LEDA Galaxies and QSOs, a flag to indicate if the object is or is not a reference star, and the 2MASS ID when available. The overall distribution of the stars in the catalog can be seen in Figure 5.

In the final catalog of proper motions, stars with $V < 12$ have formal proper motion errors of about 0.5 mas yr$^{-1}$, and well-measured stars with $12 < V < 15.5$, have values that range from 0.5 to 1.3 mas yr$^{-1}$. These only reflect measurement errors, as they are based on the positional errors and the epoch difference. When proper motions for the same star measured in different bricks are averaged together, statistical and systematic deviations between the bricks must be added to get the true error. The iterative method applied in Section 6.2 was designed to reduce those deviations, but cannot make them zero.

A better way to determine the real proper motion uncertainties, is to compute the standard deviation of the final error-weighted average proper motions. Figure 6 shows these scatter-based proper motion errors, for a random sample of about 5% the size of the whole catalog. These errors can still be an underestimate of the real proper motion uncertainty, because in the error-weighted average the data points are not independent, two overlapping bricks reduced into the same plate can produce (positively) correlated proper motions. In this case, the true uncertainty is larger than the measured one.

The most reliable assessment of the proper motion errors is obtained from a comparison with external catalogs. The scatter observed in the differences between our proper motions and those from $Hipparcos$, is the combined result of both catalogs' proper motion errors. Given that $Hipparcos$ errors are about 1 mas yr$^{-1}$, the measured dispersion indicates that our real proper motion uncertainties are about 2.3 mas yr$^{-1}$, for stars brighter than $V = 10$. This coincides well with the scatter-based errors in Figure 6, at the bright end.

The scatter in the proper motion of the LMC and SMC samples can be used to estimate the proper motion uncertainties, at the mean magnitude of the Clouds, since their intrinsic internal velocity dispersion$^{12}$ makes a very minor contribution to the observed scatter. Results indicate that our real proper motion uncertainties are about 3.8 mas yr$^{-1}$ for stars around $V = 16.4$, entirely consistent with the scatter-based uncertainties in Figure 6.

$^{11}$ A polynomial in $(X, Y, m)$ is used to describe the magnitude equation correction.

$^{12}$ 30 km s$^{-1}$ (0.13 mas yr$^{-1}$ at 50 kpc distance) or less in each (Westerlund 1997).
7. PROPER MOTION OF THE MAGELLANIC CLOUDS

7.1. Selection of LMC and SMC Dominated Samples

A photometric selection was made to choose bona fide red giant LMC and SMC stars, based on the analysis of the 2MASS LMC infrared color magnitude diagram (CMD) of Nikolaev & Weinberg (2000) (their sample “J”). The photometric cuts applied, as seen in Figure 7, are

LMC: \[1.1 \leq J - K_s \leq 1.3\] and \[9.5 \leq K_s \leq 12\]

SMC: \[1.0 \leq J - K_s \leq 1.2\] and \[10 \leq K_s \leq 12.5\]

Only stars with CCD second-epoch data were selected, as stars whose proper motions were based on plate data only showed a significantly higher dispersion and some visible systematics. We were also forced to discard an area of high stellar density, at \(71^\circ \leq \alpha \leq 76^\circ\) and \(-68^\circ \leq \delta \leq -71^\circ\), with CCD data close to the LMC center, which consistently showed deviant results probably caused by misidentifications.

We selected 3822 LMC and 964 SMC stars, as seen in Figure 8, to measure the mean absolute proper motion of the Clouds. Bluer sequences of the CMDs in Figure 7 containing LMC/SMC stars have significant contribution from Milky Way stars and therefore were not considered. The redder sequences of LMC/SMC asymptotic giant branch stars have very faint \(V \approx 17.5\) mag. Consequently, the proper motion errors are too large to be useful. Also, given the magnitude-related problems in the plates, it is desirable to have the smallest possible difference in brightness between the reference stars and the Clouds' stars, and indeed, the chosen samples overlap sufficiently in magnitude (see Figure 9).

7.2. Absolute Proper Motion of the LMC and SMC

Probability plots (Hamaker 1978) of the chosen samples yielded the mean and dispersion values for the LMC and SMC proper motion listed in Table 2. The errors quoted include: the formal error of the mean value \((\sigma/\sqrt{N_{\text{obs}}})\), the error of the quadratic polynomial at the LMC and SMC centers, transformation to Hipparcos errors (Equations (1) and (2)), and the estimated Hipparcos systematic error (0.25 mas yr\(^{-1}\)). As
7.2.1. Center-of-mass Proper Motion

The large extent of the Clouds and their non-negligible depth means that all previous investigations, which measured proper motions on scattered small fields, had to convert their measured values into a center-of-mass proper motion. That is because a given space velocity at a fixed distance projects differently on radial velocity and proper motion at different locations in the sky, following the same principle of the moving cluster method and the solar motion.\footnote{One of the first attempts to estimate the proper motion of the Magellanic Clouds was done by measuring gradients in the radial velocity along them (Feitzinger et al. 1977; Weatheringham et al. 1988).} Besides, proper motion obviously scales with distance.

7.2.2. Tangential Velocities

Table 3 and Figures 10 and 11 summarize how our results compare with recent measurements of the proper motion of the Magellanic Clouds. The error bars hinder a more precise conclusion about the individual tangential velocities of the Clouds based on our data. Nonetheless, the methodology used to measure the stellar proper motions in our catalog permits us to make a rather precise measurement of the proper motion of the SMC with respect to the LMC, as explained in more detail in Section 7.3.
rotation curve is obtained from radial velocities of Carbon (2006b); et al. in gray while ours is plotted in black. yield widely accepted values of VCLMC = 50-60 km s⁻¹. Nonetheless, Piatek et al. (2008) estimates its own VCLMC = 120 km s⁻¹, based on the gradient of their measured proper motions along the radius in the LMC disk, and use such value for the rotation correction. Given such discrepant values, Costa et al. (2009) actually obtains two final results for the LMC, Costa et al. (2009)-(1) refers to their final proper motion when using VCLMC = 50 km s⁻¹, while Costa et al. (2009)-(2) does so for VCLMC = 120 km s⁻¹. For the latter, it must be noted that μ₁, cos δ deviates noticeably from the other determinations in Table 3.

Altogether, the typical correction for perspective effect for the LMC from both methods is about ± 0.2 mas yr⁻¹ and may rise to about ± 0.5 mas yr⁻¹ for locations farther than 5° from the LMC center, running more or less in opposite directions at opposite locations on the Cloud. Rotation effects for the LMC are usually less than 0.1 mas yr⁻¹. Perspective effects for SMC...
are much smaller. For previous studies, these corrections are necessary and in some cases yield quite different values for the same fields, but in our work, given the spatial extent and symmetry of the data, the net effect on the mean motion of the Clouds is very close to zero, and no correction is done.

7.3. Relative Proper Motion of the SMC with Respect to the LMC

As explained in Section 6.2, we measured the mean motion of our reference stars precisely all over our FOV, in particular at the location of LMC and SMC within 0.03 and 0.06 mas yr⁻¹, respectively. Combined with the relative proper motion of LMC and SMC stars with respect to these reference stars, we can indeed measure the proper motion of the SMC with respect to that of the LMC, with a higher precision, limited by the error just quoted plus the formal error of the mean coming from the number of stars and their measured scatter.

From Table 2 and taking the errors quoted above into account, it is straightforward to obtain the relative proper motion of the SMC with respect to the LMC:

\[ \Delta \mu_{\cos \delta}^{\text{SMC-LMC}} = -0.91 \pm 0.16 \text{ mas yr}^{-1} \]  

\[ \Delta \mu_{\delta}^{\text{SMC-LMC}} = -1.49 \pm 0.15 \text{ mas yr}^{-1}. \]

These values cannot be transformed directly into a measurement of the relative velocity between the Clouds. Being at different locations in the sky means that the planes of their tangential velocities are different as well, and the necessary rotation and projections to measure the SMC velocity on the LMC reference frame does not allow us to obtain the relative space velocity as merely a function of the relative proper motion between the Clouds.

Table 4

<table>
<thead>
<tr>
<th>Using the LMC</th>
</tr>
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<tbody>
<tr>
<td>Proper Motion of</td>
</tr>
<tr>
<td>( \mu_{\cos \delta} )</td>
</tr>
<tr>
<td>( \mu_{\delta} )</td>
</tr>
<tr>
<td>( \text{mas yr}^{-1} )</td>
</tr>
<tr>
<td>( \text{mas yr}^{-1} )</td>
</tr>
<tr>
<td>----------------</td>
</tr>
<tr>
<td>Jones et al. (1994)</td>
</tr>
<tr>
<td>Kroupa &amp; Bastian (1997c)</td>
</tr>
<tr>
<td>Pedreros et al. (2006a)</td>
</tr>
<tr>
<td>Kallivayalil et al. (2006b)</td>
</tr>
<tr>
<td>Piatek et al. (2008)</td>
</tr>
<tr>
<td>Costa et al. (2009)(1)</td>
</tr>
<tr>
<td>Costa et al. (2009)(2)</td>
</tr>
</tbody>
</table>

Notes. Results (1) and (2) from Costa et al. (2009) are obtained assuming two different rotational velocities for the LMC, as explained in detail in Section 7.3. Compare with the direct determinations of the proper motion of the SMC in Table 3. Quoted errors include the contribution from our measured relative proper motion.

But, we can use these values to obtain new independent measurements of the SMC’s absolute proper motion, based on existing measurements of the LMC’s absolute proper motion plus our precise relative proper motion from above. Moreover, since all authors that directly measured the proper motion of the SMC had previously measured the LMC’s proper motion as well, we can verify if their original SMC results are consistent with our relative measure. Figure 12 shows the absolute proper-motion determination for the SMC from Table 4 (made by combining our relative LMC–SMC motion with absolute LMC motions from the literature), compared to the direct determinations of the absolute proper motion of the SMC from Table 3.

Except for Piatek et al. (2008) and Costa et al. (2009)-(2), all published measurements of the SMC proper motions are consistent with our new ones. These two works are the only ones that use \( V_{\text{rel},\text{LMC}} = 120 \text{ km s}^{-1} \). It is worth noting that field L11 in the LMC from Piatek et al. (2008) is also in Costa et al. (2009), but their measured proper motions are significantly different, beyond the quoted errors. All this makes us suspect that the rather small quoted proper motion errors in Piatek et al. (2008) underestimate their real uncertainties.

In summary, although our proper motions for the LMC and the SMC separately are in agreement—within error bars—with Kallivayalil et al. (2006b, 2006a), Piatek et al. (2008), and Costa et al. (2009), our relative proper motion of SMC with respect to LMC is consistent only with Kallivayalil et al. (2006a, 2006b) and Costa et al. (2009)-(1).

7.4. The Space Motion of the Clouds

The individual as well as relative space velocities of the Clouds, as derived from our LMC and SMC proper motions, are given in Table 5. The escape velocity at the distance of the LMC is estimated to be 300–350 km s⁻¹, depending on the Galactic potential model used (either a simple isothermal sphere or a more elaborate cosmologically inspired) Navarro–Frank–White (NFW) dark matter profile (Gardiner & Noguchi 1996; Klypin et al. 2002; Xue et al. 2008). Taken at face value, the galactocentric velocities in Table 5 indicate that the LMC is traveling at a speed that is very close to the escape velocity, while the SMC is still below the escape velocity of the Galaxy. Unfortunately, the uncertainties hinder a more definitive conclusion regarding their binding status.

From our proper motion measures, we determine that the SMC is moving at \( 89 \pm 54 \text{ km s}^{-1} \) with respect to LMC. Our error bars do not allow us to determine whether or not the Clouds are bound to each other, given that the escape velocity from the
Table 6. For comparison, this table also lists the relative velocity at the precise LMC proper motions available in the literature, and the point-mass geometry, a mass for the LMC of $2 \times 10^6 M_\odot$.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit</th>
<th>LMC</th>
<th>SMC</th>
</tr>
</thead>
<tbody>
<tr>
<td>$(\alpha, \delta)$</td>
<td>deg</td>
<td>$(81.90, -69.87)$</td>
<td>$(13.20, -72.50)$</td>
</tr>
<tr>
<td>$(\ell, b)$</td>
<td>deg</td>
<td>$(290.56, -32.57)$</td>
<td>$(203.78, -44.62)$</td>
</tr>
<tr>
<td>Distance</td>
<td>kpc</td>
<td>$50.1 \pm 2.3$</td>
<td>$62.8 \pm 2.6$</td>
</tr>
<tr>
<td>Radial velocity</td>
<td>km s$^{-1}$</td>
<td>$262.1 \pm 3.4$</td>
<td>$146.0 \pm 0.6$</td>
</tr>
<tr>
<td>$(\mu_\alpha \cos \delta, \mu_\delta)$</td>
<td>mas yr$^{-1}$</td>
<td>$(1.89, 0.39)$</td>
<td>$(0.98, -1.10)$</td>
</tr>
<tr>
<td>$(U, V, W)_{\odot, LSR}$</td>
<td>km s$^{-1}$</td>
<td>$(10.00, 5.25, 7.17)$</td>
<td>$(0, 220, 0)$</td>
</tr>
</tbody>
</table>

### Derived Quantities

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$(X, Y, Z)$</td>
<td>kpc</td>
<td>$(0.3, -41.5, -26.9)$</td>
</tr>
<tr>
<td>$R_{gc}$</td>
<td>kpc</td>
<td>41.5</td>
</tr>
<tr>
<td>$(U, V, W)_{gc}$</td>
<td>km s$^{-1}$</td>
<td>$(71.8, -468.1, 226.1)$</td>
</tr>
<tr>
<td>$(U, V, W)_{gc}$</td>
<td>km s$^{-1}$</td>
<td>$(71.8, -248.1, 226.1)$</td>
</tr>
<tr>
<td>$</td>
<td></td>
<td>(U, V, W)_{gc}</td>
</tr>
<tr>
<td>$</td>
<td></td>
<td>(U, V, W)_{SMC-LMC}</td>
</tr>
</tbody>
</table>

### Notes.

$(\alpha, \delta)$ from van der Marel et al. (2002) (LMC) and Stanimirović et al. (2004) (SMC). $(\ell, b)$ are transformed from $(\alpha, \delta)$. Distance from Freedman et al. (2001) (LMC) and Cioni et al. (2000) (SMC). Radial velocity from van der Marel et al. (2002) (LMC) and Harris & Zaritsky (2006) (SMC). Solar motion $(U, V, W)_{\odot, LSR}$ and galactocentric velocity of the Local Standard of Rest $(U, V, W)_{LSR, gc}$ from Dehnen & Binney (1998). $R_0 = 8$ kpc was adopted. $R_{gc}$ is the Galactocentric distance. $(U, V, W)_{gc}$ and $(U, V, W)_{gc}$ are the heliocentric and galactocentric space velocities of the Clouds. $|| (U, V, W)_{SMC-LMC} ||$ is the relative velocity of SMC with respect to LMC.

Table 6. Relative Velocity between LMC and SMC

| Reference | $|| (U, V, W)_{SMC-LMC} ||$ km s$^{-1}$ |
|-----------|----------------------------------|
| Originally quoted by reference |
| Kallivayalil et al. (2005a) | $105 \pm 42$ |
| Platek et al. (2006) | $142 \pm 19$ |
| Costa et al. (2009)-(1) | $84 \pm 50$ |
| Costa et al. (2009)-(2) | $62 \pm 63$ |
| New value using our $f_{SMC-LMC}$ |
| Kallivayalil et al. (2005a) | $125 \pm 61$ |
| Platek et al. (2008) | $106 \pm 51$ |
| Costa et al. (2009)-(1) | $85 \pm 52$ |
| Costa et al. (2009)-(2) | $152 \pm 63$ |
| This work | $89 \pm 54$ |

Notes. Results (1) and (2) from (Costa et al. 2009) are obtained assuming two different rotational velocities for LMC, as explained in detail in Section 7.3.

LMC at the SMC location is about $90$ km s$^{-1}$ (assuming a simple point-mass geometry, a mass for the LMC of $2 \times 10^6 M_\odot$ and 23 kpc for the distance between the Clouds). Yet, we can use our new SMC proper motions to obtain additional determinations of the relative velocity between the Clouds, using the more precise LMC proper motions available in the literature, and the other needed input parameters listed in Table 5. Then we obtain more estimates of $|| (U, V, W)_{SMC-LMC} ||$, which are listed in Table 6. For comparison, this table also lists the relative velocity originally quoted by the references used. It is important to be aware of how sensitive $|| (U, V, W)_{SMC-LMC} ||$ is for different values of the LMC proper motion (see Figure 13). It is clear that even the smallest proper motion errors quoted translate into a substantial relative velocity error between the Clouds. On top of that, the measured values are close enough to the escape velocity of the SMC with respect to the LMC, such that any conclusion regarding the binarity of the Clouds is still far from decided. The same situation applies to the individual space velocities of the Clouds, the binding status of the Clouds to the Milky Way is also extremely sensitive to the individual proper motions.

Thus, although our individual absolute proper motions for the Clouds cannot tell us much about their orbits, our measured relative proper motion between LMC and SMC allowed us to identify the best self-consistent measurements of the proper motion of both clouds, from those authors that had measured both galaxies with claimed very good accuracies. Our measured space velocity has also helped to check which results were more consistent with that value, since it is quite sensitive to the proper motions used.

8. IMPLICATIONS OF OUR RESULTS TO THE DYNAMICS OF THE MAGELLANIC SYSTEM

The most prevalent scenario for the orbit of the Magellanic Clouds, before the HST proper motion results, favored them as a binary system in a bound orbit around the Milky Way. Dynamical simulations were performed under the presumption that the Clouds were bound to each other, due to the existence of the common H I envelope surrounding them (Hindman et al. 1963). Crude timing estimates suggested that for its creation and survival, a long time of shared orbits was needed. The extent of the Magellanic Stream implied that the Clouds had undergone multiple orbits gravitationally bound to the Milky Way and to each other.
The orbits of the Clouds are naturally a key ingredient in such dynamical modeling. Once an orbit is chosen, then a full simulation of the Clouds themselves is run. The main goal has been to reproduce as much as possible the position and radial velocity of the Magellanic Stream, though significant validation is obtained if the Leading Arm, the Magellanic Bridge, and the distorted structure of the Clouds, are also replicated. Another "condition" imposed is that the Clouds share the same orbital plane with the Magellanic Stream, since the latter runs more or less on a great circle on the sky.

Depending on the particular questions under study, Cloud model investigators use different approaches. Either one or both Clouds are considered, using collisionless (stars) and/or collisional (gas) particles. The Cloud(s) is(are) made of one or many particles, which can be massless test particles under a given potential, or a conglomerate of self-gravitating particles or even "sticky" self-gravitating particles (to model hydrodynamic processes).

Overall, two competing scenarios have been systematically studied and have had some degree of success in the modeling of the mentioned structures: the tidal model and the ram pressure model. In the first scenario, the Galaxy extracted a tidal plume from the LMC and/or the SMC, which gave origin to the Magellanic Stream, in a previous close encounter of the three bodies about 1.5 Gyr ago. A most recent encounter 200 Myr ago created the Magellanic Bridge. The second scenario proposes that the Stream and the Leading Arm consist of material that has been ram pressure stripped from the LMC (and SMC), during its last passage through the extended ionized Halo of the Galaxy, about 500 Myr ago.

A complementary scenario to extract substantial amounts of gas and no stars from the Clouds, the blowout model, has been proposed by Nidever et al. (2008). The main hypothesis is that star formation outflow in the leading edge of the LMC has been blowing out or puffing up the gas over the past 2 Gyr; making it easier for ram pressure and tidal forces to strip it off.

The first dynamical simulation of the Magellanic System (Murai & Fujimoto 1980) was done knowing only the radial velocity of the Clouds, and very little about the mass of the Milky Way at the Clouds' distances. Some dynamically permissible parameters were assumed in order to have all the input parameters necessary to compute an orbit. Their models required the inclusion of a massive halo (an idea that was just starting to being accepted then) in order to reproduce the highly negative radial velocities observed in the tip of the Magellanic Stream. Conversely, assuming that the LMC was in a bound orbit provided estimates consistent with a massive Galactic halo.

In general, all the simulations for the Magellanic Clouds (Lin & Lynden-Bell 1982; Gardiner et al. 1994; Moore & Davis 1994; Heller & Rohlfis 1994; Lin et al. 1995; Gardiner & Noguchi 1996; Yoshizawa & Noguchi 2003; Mastropietro et al. 2005; Bekki & Chiba 2005; Connors et al. 2006; Beba et al. 2007) are based on the backwards integration of the equations of motion, first applied by Murali & Fujimoto (1980). Most papers consider an isothermal sphere with a given constant rotational velocity at a large galactocentric distance, while three of the most recent calculations use NFW dark matter halo profiles. Not surprisingly, the mass (profile and amount) of the Galaxy is an important source of uncertainty in the orbital models. The masses of the Clouds are as well another source of error, their current distorted state makes any dynamical estimate of the mass a difficult task.

Given the large mass of the Clouds, dynamical friction can significantly reduce their perigalacticon distance as they move through the Galactic halo. N-body simulations of self-gravitating particles naturally consider it by default, while in other cases, it is accounted for by using an analytical expression given by Binney & Tremaine (1987). Recent studies (Hashimoto et al. 2003; Just & Pefarrubia 2005) have found though, that the latter tends to circularize orbits to excess when compared to equivalent N-body simulations, thus some simulations have scaled down its effects.

The important point to consider here is that a high orbital eccentricity, or equivalently a high transverse motion with respect to the Galaxy, is needed to lead to the formation of the high-velocity Magellanic Stream. Therefore, the initial conditions of the Clouds' orbits must be such that even after the effects of dynamical friction, orbital eccentricity is high enough for the Stream to be formed. Interestingly enough, Lin et al. (1995) had pointed out that a hyperbolic encounter of the Clouds with the Galaxy, in which they are passing by for the first (and only) time, could lead to the tidal stripping of gas segments that would later infall and trail rapidly behind. Such a model was discarded then, on the basis that the Clouds were presumed bound to the Galaxy.

Another source of dynamical friction, the LMC dark matter halo, is considered as well in the calculations of the Magellanic orbits (Bekki & Chiba 2005). Its effects are quite important on the bimarity of the galaxy pair, exerting a significant frictional drag on the SMC when it penetrates the LMC halo. If they...
get close enough, they would merge quickly, and since this has not occurred yet, it implies either that this force is negligible or that the Clouds became bound to each other relatively recently (Gardiner et al. 1994). Bekki & Chiba (2005) also found that under these conditions, the Clouds cannot keep their binary status for more than \( \approx 5 \) Gyr in the past. This opens the possibility of the Clouds being coupled only recently.

Curiously, the very first dynamical model of the Magellanic System (Murai & Fujimoto 1980) had to make an extensive search for the binary state that could produce the Magellanic Stream. The choice of tangential velocities for SMC had to be so specific, that they could—thereoretically—predict it within \( \pm 5 \) km s\(^{-1}\). This prompted them and others to make the first inferred estimates of the proper motion of the Clouds. This early model though, did not include a dark matter halo for the LMC.

A similar situation was faced later on by Heller & Rohlfis (1994), who explain that if the perturbing forces acting on the LMC and/or SMC have to be small enough to leave the binary system intact while simultaneously producing long streams similar in shape to the Stream, then the evolution time of these streams has to be rather long and very special, and properly chosen initial conditions for the test particles in the simulations have to be adopted.

One point in which all orbital models agree, is that the Clouds had a recent encounter, sometime between 200 to 500 Myr ago. In fact, several models also found that the binarity of the Clouds, regardless of how long it has been in place, was most probably broken at this last collision, which happened very close to their perigalactic distance. In other words, the Milky Way’s powerful gravitational tide has disrupted the pair.

In general, searching for the appropriate binary-bound orbits for the Clouds that can later be used to reproduce the Magellanic System, has been a difficult fine tuning task. The challenge is now even harder, since the most recent \( HST \) measurements of the LMC and SMC proper motion (Kallivayalil et al. 2006b; Piasek et al. 2008) seem to indicate that the Clouds are traveling too fast to have ever been bound to the Milky Way.

Numerical simulations of the LMC orbit by Besla et al. (2007), based on these new numbers, suggest that the Large Cloud is “plunging” in a highly eccentric parabolic orbit, on its first passage about the Milky Way. At such speed, dynamical friction is negligible, but the choice of the Galactic potential (isothermal sphere versus NFW) introduces dramatic changes in the orbital history of the LMC. In an isothermal sphere, the LMC has indeed a bound orbit, although with an increased period and apogalacticon distance compared to previous models. In an NFW profile, the “best case scenario” of a bound orbit has a period of about a Hubble time, and reaches an apogalacticon distance of \( \approx 250 \) kpc.

Despite such three-dimensional differences, their projected orbits on the sky were in good agreement, so their predicted location compared to the Magellanic Stream’s great circle, could not be used to distinguish Milky Way mass profile models. More importantly though, in both cases the projected orbit did not trace the Magellanic Stream, deviating from it by about 10° on the sky. Adding the SMC into the calculations did not reduce the disagreement, nor using the weighted average of all pre-\( HST \) proper motions. Besla et al. (2007) argue then that the usual criteria to validate a dynamical model of the Magellanic System, its ability to match an orbit with the Stream, is no longer acceptable.

The conclusion of Besla et al. (2007), that the Clouds are on their first passage relies heavily on the large value for \( \mu_\alpha \cos \delta \) that was measured with \( HST \) for the LMC. Lin et al. (1995) and others have in fact argued that it is hard to explain how a bound LMC could have maintained a high angular momentum perpendicular to the Galaxy’s rotation axis for so long. Raychaudhury & Lynden-Bell (1989), Shuter (1992) and Byrd et al. (1994) have suggested that an early interaction with M31 could be the source of such a high tangential velocity. In any case, such a condition is easier to understand with an LMC not bound to the Milky Way. In addition, the Clouds are the only gas-rich dwarf galaxies at small galacto-centric distances (van den Bergh 2005), different from the rest in the Local Group. All these reasons are used by Besla et al. (2007) to support the case of an unbound LMC.

Notably, all LMC proper motion results after Kallivayalil et al. (2006b), including this work, have produced lower values of \( \mu_\alpha \cos \delta \). Therefore, a bound orbit with a long period and a large apogalacticon distance is still a scenario compatible with the most recent results. As for the binarity of the Clouds, a recent period of joint orbits could be enough to explain the common features between the Clouds, that is the H\textsc{i} envelope, the Bridge and even the Stream, and can account for the different star formation history and chemical evolution in each Cloud, that point to a separate origin and place of birth.

To conclude, the search for a realistic orbit of the Magellanic Clouds is far from over. The space velocities obtained in this investigation are supportive of a scenario in which the Magellanic Clouds are possibly currently unbound from each other, with the LMC traveling at a velocity that is high enough to make it nearly unbound to the Galaxy. But having nowadays a much more precise measurement of the proper motion of the Clouds, has not facilitated our understanding of their dynamics and has instead opened new questions and placed all the constructed models in doubt.

9. CONCLUSIONS AND FUTURE WORK

A catalog of absolute proper motions containing 1,448,438 objects has been obtained from SPM material, supplemented with UCAC2 data. The catalog covers an estimated area of 450 deg\(^2\) except for the inner regions of LMC, SMC, and 47 Tucanae, where the high stellar density made it impossible to obtain accurate cross-identification of the stars.

Samples of 3822 LMC stars and 964 stars were selected from the catalog to measure the mean proper motion of the Magellanic Clouds. The results obtained are

\[
(\mu_\alpha \cos \delta, \mu_\delta)_{\text{LMC}} = (+1.89, +0.39) \pm (0.27, 0.27) \, \text{mas yr}^{-1}
\]

and

\[
(\mu_\alpha \cos \delta, \mu_\delta)_{\text{SMC}} = (+0.98, -1.01) \pm (0.30, 0.29) \, \text{mas yr}^{-1}.
\]

Our much more precise relative proper motions with respect to the photometrically selected Galactic Disk dwarf stars, enabled us to obtain the proper motion of the SMC with respect to the LMC, with significantly smaller uncertainties:

\[
(\mu_\alpha \cos \delta, \mu_\delta)_{\text{SMC-LMC}} = (-0.91, -1.49) \pm (0.16, 0.15) \, \text{mas yr}^{-1}.
\]

This was used to obtain new independent and more precise proper motions for the SMC, based on the more accurate LMC proper motions of other authors. It was also used to confirm if their separate measurements of the SMC proper motion were consistent or not with our results.

After a comparison in an absolute and relative sense with previous proper motion results, followed by a discussion of the
orbital models of the Magellanic Clouds based on those results, we conclude that our proper motions are compatible with the LMC and SMC being born and formed as separate entities, which later joined in a temporary binary state for the past few Gigayears, being recently disrupted by the Milky Way in their most recent perigalacticon passage about 200 Myr ago. The Clouds orbits are marginally bound to the Milky Way, possibly following a very elongated but still periodic orbit around the Galaxy.

The search for a realistic orbit of the Magellanic Clouds is far from over. Having (formally) very accurate and precise LMC and Magellanic Stream parameters in the orbital calculation. But we are getting closer.

9.1. Future Work

From the very beginning, this investigation of the proper motion of the Magellanic Clouds was known to be restricted by the conditions and characteristics of the SPM material. We have proven that even under those constraints, these data are able to produce independent significant results on the proper motion of nearby dwarf galaxies. Thus, there is certainly room for improvement.

Second epoch CCD data over the whole field are needed, especially in the inner areas of the Clouds. Since the definition of an adequate uncontaminated relative reference frame in those areas is difficult, it is also necessary to devise an adequate proper motion reduction method, to precisely link these fields into the global relative reference frame. A scaled-down version of the block adjustment method could be put in place here, in which plate-size fields of view are assembled first, and then another solution is run to paste those into the larger global system.

Since the dominant limiting factor in terms of precision is the plate measurement errors, additional improvement can be achieved by re-scanning the first-epoch plates used in this work with the Yale PDS, which yields two times more precise positions than the currently measured ones. As PDS scanning of a full plate is very time consuming, a subset of properly pre-selected objects should be measured.

Although additional HST follow up observations are already planned to improve the space-based proper motions, and other research teams are still working on additional ground-based measurements, these studies are still limited since they must correct their observed proper motions into a center-of-mass value. Therefore, it is still worth trying to improve the results, since they offer a wide field extended coverage of the Magellanic Clouds.

Another future work being considered, is to search in the intercloud region for coherent structures in the relative proper motion space, to identify stars whose motion is directed towards the LMC. This will require us to find what possibly is a small number of stars spread over an extended area that share systematic proper motions.

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