

# **The Calculation of Stability of Tunnel under Effects of Seismic Wave of Explosion**

**Li Zheng**

**Huang Hong**

Engineering Design and Research Institute

Ministry of Machinery and Electronic Industry

P.O. Box 55 Beijing 100053 P. C. China

## **Abstract**

With a lot of experiments on explosion, the dynamic stability of grotto and sprayed anchor strutted grotto were studied under effects of seismic wave of explosion, and a formula was put out for calculating the stability. The results of calculation fitted results of testing well.

## **1. Introduction**

It is usually needed to evaluated the stability of tunnels and galleries in structures of mines, railroads and hydro-electric engineerings under effects of dynamic loading, and the safety distance needed to be determined. The dynamic loads result mainly from explosion work and accidents. When the stability of tunnels and galleries are evaluated under effects of seismic wave of explosion, it should be considered the dynamic loads from explosion as well as static loads from rocky soil. The quantities of dynamic loads are related to amplitude and lasting period of seismic wave of explosion propagated among ground.

## **2. The dynamic strength of rocks**

It is well known that under effects of dynamic loads, the limit range of rock strength increases with the increasing of loading rate. The increased value of strength relates to the nature of rocks and loading rate. The values of granite and marble are listed in table 1.

# Report Documentation Page

Form Approved  
OMB No. 0704-0188

Public reporting burden for the collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington VA 22202-4302. Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to a penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number.

1. REPORT DATE <b>AUG 1994</b>		2. REPORT TYPE		3. DATES COVERED <b>00-00-1994 to 00-00-1994</b>	
4. TITLE AND SUBTITLE <b>The Calculation of Stability of Tunnel under Effects of Seismic Wave of Explosion</b>				5a. CONTRACT NUMBER	
				5b. GRANT NUMBER	
				5c. PROGRAM ELEMENT NUMBER	
6. AUTHOR(S)				5d. PROJECT NUMBER	
				5e. TASK NUMBER	
				5f. WORK UNIT NUMBER	
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) <b>Engineering Design and Research Institute, Ministry of Machinery and Electronic Industry, P.O. Box 55, Beijing 100053 P. C. China,</b>				8. PERFORMING ORGANIZATION REPORT NUMBER	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)				10. SPONSOR/MONITOR'S ACRONYM(S)	
				11. SPONSOR/MONITOR'S REPORT NUMBER(S)	
12. DISTRIBUTION/AVAILABILITY STATEMENT <b>Approved for public release; distribution unlimited</b>					
13. SUPPLEMENTARY NOTES <b>See also ADM000767. Proceedings of the Twenty-Sixth DoD Explosives Safety Seminar Held in Miami, FL on 16-18 August 1994.</b>					
14. ABSTRACT <b>see report</b>					
15. SUBJECT TERMS					
16. SECURITY CLASSIFICATION OF:			17. LIMITATION OF ABSTRACT <b>Same as Report (SAR)</b>	18. NUMBER OF PAGES <b>13</b>	19a. NAME OF RESPONSIBLE PERSON
a. REPORT <b>unclassified</b>	b. ABSTRACT <b>unclassified</b>	c. THIS PAGE <b>unclassified</b>			

Table 1. The variations of compressive strength of rocks with loading rate

Rock	Loading rate	Com. strength		Loading rate	Com. strength		$\sigma_2/\sigma_1$
	$V_1$ kg/cm <sup>2</sup> /sec	$\sigma_1$ kg/cm <sup>2</sup>		$V_2$ kg/cm <sup>2</sup> /sec	$\sigma_2$ kg/cm <sup>2</sup>		
Granite	5	1220		20	2000		1.64
Marble	5	500		30000	980		1.98

**Table 1. The variations of compressive strength of rocks with loading rate**

All of compressive strength of rocks increase with increasing of loading rate, but increased value is different for each rock. The compressive and flexural strength and elasticity modules of rock increase with a logarithmic function of loading rate.

### 3. The dynamic strength of rock mass

Because cracks and cleavages exist, the strength of rock mass is lower than that of rock. The discount factor is about 0.80~0.90. When the loading rate is  $10^2\sim 10^4$ kg/cm<sup>2</sup>/sec, the compressive strength of rock increases by 1.16~1.43 times and flexural strength increases by 1.24~1.48 times. Because the damage of rock mass of tunnel is controlled by tensile strength, the dynamic strength of rock is taken as 1.30~1.40 times of static strength. So, the formula for calculating the dynamic strength of rock mass is:

$$\sigma_D = K_D \sigma_P \quad (1)$$

Where:  $\sigma_D$  is dynamic tensile strength of rock mass (kg/cm<sup>2</sup>);  $\sigma_P$  is ultimate static tensile strength of rock (kg/cm<sup>2</sup>);  $K_D$  is increasing factor of dynamic strength of rock mass.

If the surface rocks of grotto are stable, the surface are usually sprayed with 5cm thickness concrete and  $K$  is among 1.04~1.26. If the surface rocks of grotto are unstable, the surface are usually strutted by rollbolts and then sprayed with 5cm thickness concrete and  $K$  is among 1.30~1.40.

### 4. The calculation of stability of tunnels under effect of seismic wave of explosion

#### 4.1. Concentrated factors of dynamic and static stress of tunnel without lining

Under effect of plane wave of explosion, the concentrated factors of dynamic and static stress of tunnel without lining are listed in table 2.

Table 2. Concentrated factors of dynamic and static stress of tunnel without lining\*

Pattern of tunnel	Position	Concentrated factor of dynamic stress		Concentrated factor of static stress
		Analytical $D/\lambda=0.12\sim 0.15$	Numerical $D/\lambda=0.50$	
Straight wall and round arch	Arch	3.25~2.25	3.00	3.25
	Wall	2.00~1.65	1.80	1.50

\*D is diameter of tunnel;  $\lambda$  is wave length

**Table 2.**  
**Concentrated factors of dynamic and static stress of tunnel without lining\***

#### 4.2. The calculation of stability of tunnel under effects of seismic wave of explosion

Under effects of seismic wave of explosion, the stable condition of rock mass of tunnel without lining is that the sum of static stress of mountain and dynamic stress of seismic wave of explosion is smaller than or equals to the dynamic strength of rock mass; that is:

$$\sigma = \sigma_{CT} + \sigma_{DT} < [\sigma_D] \quad (2)$$

Where:  $\sigma$  is the total stress among rock mass ( $\text{kg/cm}^2$ );  $[\sigma_D]$  is allowable dynamic strength of dynamic strength of rock mass calculated from equation (1) ( $\text{kg/cm}^2$ );  $\sigma_{DT}$  is dynamic stress of rock mass under effect of seismic wave of explosion, ( $\text{kg/cm}^2$ ).

$$\sigma_{DT} = (1/K_0)(K_G \gamma/g) C_e V \times 10^{-3} \quad (3)$$

Where:  $\gamma$  is unit weight of rock ( $\text{kg/cm}^2$ );  $V$  is vibrating velocity of rock particles in periphery of tunnel under effects of seismic wave of explosion ( $\text{cm/sec}$ );  $C_e$  is elastic velocity of longitudinal wave;  $g$  is acceleration of gravity  $g=9.81 \text{ m/sec}^2$ ;  $K_0$  is reflection factor. Tested results showed that if the tunnel is acted by incident seismic wave of explosion, the factor is  $K_0=2$ ; if the tunnel is acted by reflected seismic wave of explosion, the factor is  $K_0=2$ .

#### 4.3. The calculation of critical vibrating velocity of rock particles

From equation (2), the critical vibrating velocity of rock particle is:

$$V_e = K_0(K_D \sigma_P - \sigma_{CT}) / (K_G \gamma C_e) \times 10^{-3} \quad (4)$$

Where:  $V_e$  is critical vibrating velocity of rock particle. When the critical vibrating velocity of rock particle is calculated to rock mass in elasticity zone, the elastic velocity of longitudinal wave  $C_e$  is taken; when the critical vibrating velocity of rock particle is calculated to rock mass with cracks, the elasto-plastic velocity of longitudinal wave  $C_p$  is taken, and it is taken  $C_p=C_e/2$  if there is no tested data of  $C_p$ .

#### 4.4. The calculation of critical vibrating velocity of rock particle for collapsed rock mass

The tested results showed that when the properties of tunnel structure change to plasticity, cracks appear in arch and in boundaries between arch bottom and side wall. With the continuous effect of explosion wave, the deformations of arch and side wall increase, but the stress in rocks doesn't increase and the tunnel appears a unloading effect. Under effect of a normal big explosion, the self-vibrating frequency of rock is 10~15 Hz and the seismic wave of explosion lasts 0.4~0.6 sec. If the tunnel is taken as a structure, the unloading factor of tunnel in plasticity zone is solved from theory calculation, thus the critical vibrating velocity of rock particles in collapsed rock mass is:

$$V_p = K_0(K_D \sigma_P + \sigma_{CT}) g / (K_G \gamma C_p) \cdot (1/K_2) \times 10^{-3} \quad (5)$$

With tested data of deformation of tunnel caused by effect of seismic wave of explosion, the unloading factor  $K_z$  is solved theoretically. If unloading factories  $K_z=0.80\sim 0.65$ , rock mass appears partial collapsing and the collapsed volume is usually smaller than  $1m^3$ . If unloading factor is  $K_z = 0.50\sim 0.35$ , the rock mass appears large area collapsing.

#### 4.5. Comparison between results of calculation and practical tests

Known a round arch and straight wall tunnel without lining, rollbolt and sprayed concrete. The span is  $L=3m$ , height is  $H=3m$ . The rock is granite with macro crystalline (weathering). The properties of rock are tested as: Pope's factor  $f=4\sim 6$ ; unit weight  $\gamma = 2.64t/m$ ; elastic velocity of longitudinal wave  $C_e=2060m/sec$ ; dynamic elastic modulus  $E=0.928 \times 10^5 kg/cm^2$ ; Poisson ratio  $\mu = 0.30$ ; internal friction angle  $\phi = 41^\circ 06'$ ; static ultimate tensile strength  $\sigma_p = 23.60kg/cm^2$ .

Chosen  $f=5$ ,  $C_e=2060m/sec$ ,  $C_p=1030ni/sec$ ,  $K_p=1.15$ ,  $K_o=2$ ,  $K_z=0.65$  for partial collapsing and  $K_z=0.35$  for large area collapsing, the results of calculation is listed in table 3.

Table 3. A comparison of critical vibrating velocity of rock particles from calculation and from practical tests cm/sec

	No damage [V1]	Slight cracking [V2]	Partial collapsing [V3]	Large area collapsing [V4]
Tested	30	30~50	50~100	100~200
Calculated	30.36	30.36~60.73	60.73~93.42	93.42~173.48

**Table 3. A comparison of critical vibrating velocity of rock particles from calculation and from practical tests cm/sec**

The calculated results fit the tested results well and the maximum error is smaller than 20%.

## 5. Applications in engineering

### 5.1. Land form

If the thickness of rock mass at minimum resistant line of grotto is smaller than 50 times of explosive diameter, the rock mass is called gentle slop; if the thickness of rock mass is bigger than 50 times of explosive diameter, the rock mass is called steep slop.

When a explosive in grotto explosion, a projection of rock over the grotto takes place if the

grotto is in a gentle slop and projection doesn't take place if the grotto in a steep slop.

## 5.2. Geology

The classification of rock is made according to features of structure and is listed in table 4.

Table 4. Classification of structure of rock mass

Classification	Structure features	Comp. strength of rock kg/cm	Elastic velocity of longitudinal wave m/sec	n
Concordant structure	Rock mass is a whole or a giant layer, extramly undeveloped joints, no dominate structure plane Bo*=1~2, M<0.5	>300	>4000	>0.85
Massive structure	Rock mass is a massive or thick layer structure, undeveloped joints most of structure planes are joint plane and closed (such as psephyte) Bo=2~3, M=0.5~2	>200	3000~4000	0.85~0.6
Fragment structure	Rock mass is a less thick layer or massive structure, developed joint, most of structure planes are joint planes. Bo=3~4. M=2~5	>100	2000~3500	0.6~0.3

\*Bo is joint data; M is number of joints in one meter;  $n=(C_v/C_e)^2$ ;  $C_v$  is longitudinal wave velocity of rock mass m/sec.  $C_e$  is longitudinal wave velocity of rock m/sec.

**Table 4. Classification of structure of rock mass**

### 5.3. The critical vibrating velocity of wall rock with different degree of damage

The velocity are listed in table 5.

Table 5. Critical vibrating velocity of wall rock of grotto [V1], [V2], [V3], [V4]

Rocks	Unit weight (t/m <sup>3</sup> )	Comp. strength (kg/cm <sup>2</sup> )	Tens. strength (kg/cm <sup>2</sup> )	No damage (cm/sec)	Slight damage (cm/sec)	Intermediate damage (cm/sec)	Serious damage (cm/sec)
Hard rock	2.60~2.70	750~1100	21~34	27	54	82	153
	2.70~2.90	1100~1800	34~51	31	62	96	178
	2.70~2.90	1800~2000	51~57	36	72	111	209
Soft rock	2.00~2.50	400~1000	11~31	29	58	90	167
	2.00~2.50	1000~1600	34~45	35	70	107	199

Note: 1. The data in this table are applicable for grottoes in gentle slop; if grottoes in steep slop, the data needed to be multiplied by 2.

2. If the hole of explosives is parallel or oblique or perpendicular to a grotto, the critical vibrating velocity of wall rock [V1], [V2], [V3] and [V4] need to be multiplied by 1.0, 1.2 and 1.4, respectively.

3. The data in the table are applicable for rocks with concordant structure and the data need to be multiplied by 0.9 or 0.8 for rocks with massive structure and fragment structure, respectively.

Table 5. Critical vibrating velocity of wall rock of grotto [V1], [V2], [V3], [V4]

#### 5.4. The determination of support pattern of wall rock

According to the relation between perpendicular vibrating velocity of seismic wave of explosion and critical vibrating velocities of wall rock of no damage[V1], slight damage[V2], intermediate damage[V3] and serious damage[V4], the support pattern of wall rock is determined:

A. if  $V_v < [V1]$ , sprayed with #200 plain concrete of thickness 50 cm;

B. if  $[V1] < V_v < [V2]$ , sprayed with #200 plain concrete of thickness 80 cm;

C. if  $[V2] < V_v < [V3]$ , net and concrete; a 250x250 mm net made of 8mm steel is placed on the surface of wall rock and then sprayed with #200 plain concrete of thickness 80~100mm;

D. if  $[V3] < V_v < [V4]$ , net, concrete and rollbolt; a 250x250 mm net is placed on surface and sprayed with ~200 plain concrete of thickness 80~100 mm, and ~16x2000 mm rollbolts are installed. The rollbolts are made of mortar and arranged with a distance of 2000x2000 mm to each other.

## **6. The calculation of perpendicular vibrating velocity of seismic wave of explosion**

Based on analysis of tested data from explosion on ground, mine explosion including standing shot, long hole volley firing, long hole short-delay blasting, directional explosion and internal explosion of tunnel, empirical formulae for calculating the perpendicular vibrating velocity of rocks in various geological conditions are listed in table 6 and drawn in fig. 1 and 2.

Table 6. Empirical formulae of perpendicular vibrating velocity of rock particles under effects of seismic wave of explosion

No	Pattern of explosion	Explosion conditions and explosive quantity	Grological condition	$V_v=k(Q^{1/3}/R)^\alpha$			
				k	$\alpha$		
1	ground explosion	Central charged Q=1, 3, 5, 10, 15, 14,100t	Granite	98.76	1.37		
2	Unsheltd big explosion	A. once delayed blasting Q=9320t	Diabase	804	2.24		
			Disbase	630	2.80		
		①Standing shot	B. Vollery blasting Q=1000t	Diabase	206	1.81	
				Metamorphic rock	180	1.47	
				Metamorphic rock	79	1.39	
				Phyllite	82.5	1.32	
				Mica-quartz schist	152	1.56	
				Phyllite	156	1.93	
				Diabase	718	2.40	
				Granite and marble	150	2.00	
	②Long-hole vollery blasting	Q=200t Q=103t Q=8~14t	Marble	77.6	2.33		
			Quartz	624	2.41		
			Limestone	125.7	1.63		
			Limestone	130	1.80		
			Limestone	140	1.80		
			Limestone	200	1.80		
			Limestone	340	1.80		
			③Long-hole shoet ddelay blasting	A. 6 pieces Q=45.9 B. 10 pieces Q=4.23t C. 10 pieces Q=4.74t D. 10 pieces	Gneiss	180	1.83
					Gnciss	116.2	1.73
					Marble	378	1.60
Marble	107	1.50					
Primary	130	1.70					
Quartz	142	1.61					
④Directional blasting	A. Total Q=13394t B. Total Q=503t	Sandstone	240	2.00			
		Diabase	115	2.00			
3	Internal explosion of tunnel	Linear charge Q=8~15t	Granite	99.6	1.72		
			Granite	111.2	1.92		
			Granite	591.4	2.30		
			Granite	90.8	1.82		

Note:  $V_v$  is perpendicular vibratting velocity of seismic wave of explosion (cm/sec);  
Q is total quantity of explosion; R is distance between centre of explosion and testing point (m).

Table 6. Empirical formulae of perpendicular vibrating velocity of rock particles under effects of seismic wave of explosion

**Fig. 1.**  
**Distribution of perpendicular vibrating velocity of seismic wave of explosion**

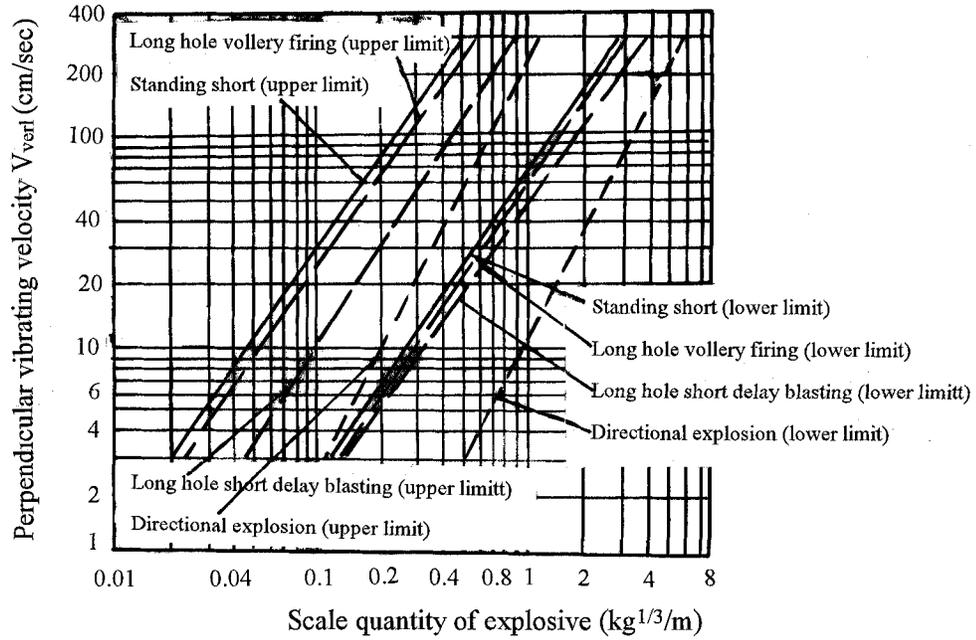


Fig.1. Distribution of perpendicular vibrating velocity of seismic wave of explosion

**Fig.2. Distribution of velocity of seismic wave of internal explosion of tunnel**

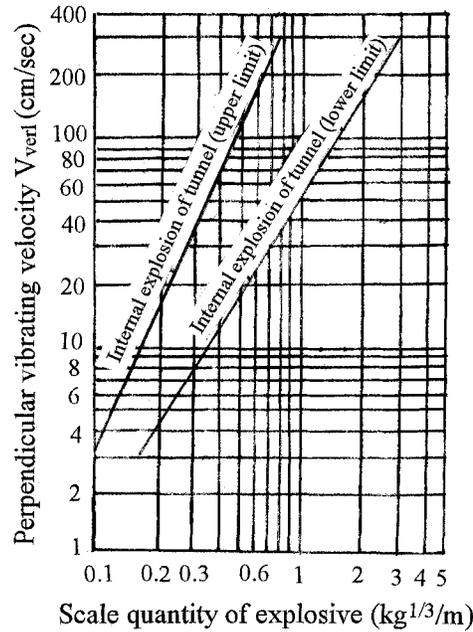


Fig.2. Distribution of velocity of seismic wave of internal explosion of tunnel

Fig. 1 and fig.2 show relations between perpendicular velocity of rocks and scale quantity of explosive  $Q^{1/3}/R$  under various conditions of explosion.

### 7. Safety distance of tunnel without lining under effect of seismic wave of explosion

With the empirical formulae and tested data in table 6, the calculating formula of safety distance is derived:

$$R = 1/([V]/k)^{(1/\alpha)} Q^{1/3} \quad (6)$$

Where: R is safety distance (m) of tunnel without lining under effects of seismic wave of explosion;  $\alpha$ , K are factors determined from tested data in table 6 or in fig. 1~2.; Q is calculated explosive quantities: total quantities of standing shot, the maximum quantity among each delay explosion and the maximum quantity in each period of short-delay blasting; [V] is critical vibrating velocity of rock particles (cm/sec) and calculated with equation (4), (5) or with formulae in table 5.

## **8. Conclusions**

1. On basis of balance between dynamic strength of rock and the sum of dynamic and static stress acted on tunnel, the formulae for calculating critical vibrating velocity of rocks are derived when tunnel without lining un elastic state appears cracking, partial collapsing and large area collapsing under effect of seismic wave of explosion. The results of calculating fit the tested results well.

2. With the critical vibrating velocity, the support pattern of rollbolt and sprayed concrete, and safety distance of stability of grotto are determined.