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Unsteady Flow Computations of a Finned Body in Supersonic Flight

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This report describes a multidisciplinary computational study undertaken to compute the flight trajectories and simultaneously predict the unsteady free flight aerodynamics of a finned projectile at supersonic speeds with the use of an advanced unstructured time-accurate Navier-Stokes computational technique. Actual flight trajectories are computed with an advanced coupled computational fluid dynamics (CFD)-rigid body dynamics (RBD) technique. In addition, our goal is to be able to extract the aerodynamic coefficients from these fully coupled time-accurate CFD-RBD computations. Computed positions and orientations of the projectile have been compared with actual data measured from free flight tests and are found to be generally in good agreement. Unsteady numerical results obtained from the coupled method and unstructured grids show the flow field, the extracted aerodynamic forces and moments, and the flight trajectories of the projectile. Aerodynamic coefficients such as the dynamic derivatives have been obtained with a separate unsteady time-accurate CFD approach and have been compared with the extracted aerodynamic coefficients from the fully coupled dynamic simulations.
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1. Introduction

The prediction of aerodynamic coefficients for projectile configurations is essential in the assessment of the performance of new designs. Understanding the aerodynamics of projectiles, rockets, and missiles is critical to the design of stable configurations and contributes significantly to the overall performance of weapon systems (1 through 3). The prediction of aerodynamic coefficients for these weapon systems is essential in the assessment of the performance of new designs. Numerical simulations have the potential of greatly reducing design costs while providing a detailed understanding of the complex aerodynamics associated with each change. Recently, we have made progress in coupling computational fluid dynamics (CFD) and flight dynamics to perform required multidisciplinary simulations for moving body problems. This involves real-time multidisciplinary coupled CFD-rigid body dynamic (RBD) computations for the entire flight trajectory of a complex guided projectile system. This can lead to accurate determination of aerodynamics, critical to the low-cost development of new advanced guided projectiles, rockets, missiles, and smart munitions.

Improved computer technology and state-of-the-art numerical procedures now enable solutions to complex, three-dimensional (3-D) problems associated with projectile and missile aerodynamics. In particular, our recent focus has been directed at the development and application of advanced predictive capabilities to compute unsteady projectile aerodynamics, especially during and after control maneuvers. During these maneuvers (4, 5) very limited data are available, and there is a lack of knowledge and understanding of the detailed aerodynamics. Accurate numerical modeling of the unsteady aerodynamics has been found to be challenging and has required the use of time-accurate solutions techniques. The present work is focused on the coupling of CFD and RBD techniques for simultaneous prediction of the unsteady free-flight aerodynamics and the flight trajectory of projectiles. In addition, our goal in the future is to be able to perform time-accurate multidisciplinary coupled CFD-RBD computations for complex guided projectiles with control maneuvers using control surfaces such as fins and canards.

Multidisciplinary computations can provide detailed fluid dynamic understanding of the unsteady aerodynamic processes involving the maneuvering flight of modern guided weapon systems. The advanced CFD capability used here solves the unsteady Navier-Stokes equations (6 through 8), incorporates unsteady boundary conditions and a special coupling procedure. The present research allows “virtual fly-out” of projectiles on the supercomputers and allows numerical prediction of the actual flight paths of a projectile and all the associated unsteady free flight aerodynamics using coupled CFD-RBD techniques in an integrated manner. Sahu (9) has successfully applied such advanced coupled procedures to simultaneously determine the flight trajectory and the associated unsteady free-flight aerodynamics of a finned projectile at supersonic velocity using structured grids. This research work was further extended and applied to a spinning projectile at a subsonic
The present research two purposes: to use unstructured methodology to perform similar virtual fly-outs with the use of unstructured grids, and to develop and apply methods to extract the aerodynamic coefficients, including the dynamic pitch-damping and roll-damping derivatives, and to compare the results with those obtained from the fully coupled virtual fly-outs. The following sections describe the coupled numerical procedure and the computed results obtained for the finned body at supersonic speeds.

2. Solution Technique

At the U.S. Army Research Laboratory, research efforts are continuing to perform real-time multidisciplinary coupled CFD-RBD computations for the entire flight trajectory of a complex guided projectile system. A real-time accurate approach is used in the present work; however, the computations require much greater computer resources. The real-time accurate approach requires that the six-degrees-of-freedom (6-DOF) body dynamics be computed at each repetition of a flow solver. The CFD capability used here solves the Navier-Stokes equations and incorporates advanced boundary conditions and grid motion capabilities. The complete set of 3-D time-dependent Navier-Stokes equations is solved in a time-accurate manner for simulations of actual flights. A commercially available code, CFD++ (7, 8) is used for the time-accurate unsteady CFD simulations. The basic numerical framework in the code contains unified grid, unified physics, and unified computing features. The user is referred to these references for details of the basic numerical framework.

The 3-D, time-dependent Reynolds-averaged Navier-Stokes (RANS) equations are solved with the following finite volume method:

\[
\frac{\partial}{\partial t} \int_W dV + \int_{\partial V} \left[ F - G \right] dA = \int_H dV
\]

in which \( W \) is the vector of conservative variables, \( F \) and \( G \) are the inviscid and viscous flux vectors, respectively, \( H \) is the vector of source terms, \( V \) is the cell volume, and \( A \) is the surface area of the cell face.

The use of an implicit scheme circumvents the stringent stability limits encountered by their explicit counterparts, and successive relaxation allows cells to be revised as information becomes available and thus aids convergence. These features of the code have been extremely useful in the present numerical simulations at supersonic speeds. Second order discretization was used for the flow variables and the turbulent viscosity equation. The turbulence closure is based on topology-parameter-free formulations. Two-equation turbulence models (11, 12) were used for the computation of turbulent flows. These models are ideally suited to unstructured bookkeeping and
massively parallel processing because of their independence from constraints related to the placement of boundaries and/or zonal interfaces.

For time-accurate simulations of virtual fly-outs that are of interest here, dual time stepping as described next was used to achieve the desired time accuracy. The grid was actually moved to take into account the spinning motion of the projectile.

2.1 Dual Time Stepping

The “dual time-stepping mode” of the code was used to perform the transient flow simulations. The term “dual time step” implies the use of two time steps. The first is an “outer” or global (and physical) time step that corresponds to the time discretization of the physical time variation term. This time step can be chosen directly by the user and is typically set to a value to represent 1/100 of the period of oscillation expected or forced in the transient flow. It is also applied to every cell and is not spatially varying.

An artificial or “inner” or “local” time variation term is added to the basic physical equations. This time step and corresponding “inner iteration” strategy is chosen to help satisfy the physical transient equations to the desired degree. If the inner iterations converge, then the outer physical transient equations (or their discretization) are satisfied exactly; otherwise, they are satisfied approximately. For the inner iterations, the time step is allowed to vary spatially. Also, relaxation with multi-grid (algebraic) acceleration is employed to reduce the residues of the physical transient equations. It is found that an order of magnitude reduction in the residues is usually sufficient to produce a good transient iteration. This may require a few internal iterations (between 3 and 10) to achieve, depending on the magnitude of the outer time step, the nature of the problem, the nature of the boundary conditions, and the consistency of the mesh with respect to the physics at hand.

2.2 Grid Movement

Grid velocity is assigned to each mesh point. This general capability can be tailored for many specific situations. For example, the grid point velocities can be specified to correspond to a spinning projectile. In this case, the grid speeds are assigned as if the grid were attached to the projectile and spinning with it. Similarly, to account for RBD, the grid point velocities can be set as if the grid were attached to the rigid body with 6 DOF. As shown in figure 1, the 6 DOF includes the inertial position components of the projectile mass center (x,y,z) and the three standard Euler angles (φ, θ, ψ): roll angle, pitch angle, and yaw angle, respectively. For RBD, the coupling refers to the interaction between the aerodynamic forces and moments and the dynamic response of the projectile and body to these forces and moments. The forces and moments are computed every CFD time step and transferred to a 6-DOF module that computes the body’s response to the forces and moments. The response is converted into translational and rotational accelerations that are integrated to obtain translational and rotational velocities and integrated once more to obtain linear position and angular orientation. The 6-DOF RBD module uses quaternions to define the angular
orientations. However, these are easily translated into Euler angles. From the dynamic response, the grid point locations and grid point velocities are set.

Figure 1. Six-DOF schematic.

2.3 Six-Degrees-of-Freedom Coupling

In CFD++, two modes are available to help simulate RBD: an uncoupled mode and a coupled mode. The coupling refers to the interaction between the aerodynamic forces and moments and the dynamic response of the projectile or body to these forces and moments. In both modes, the forces and moments are computed every time step and reported to the user. In the coupled mode, the forces and moments are passed to a 6-DOF module which computes the body’s response to the forces and moments. The response is converted into translational and rotational accelerations which are integrated to result in translational and rotational velocities and integrated once more to result in linear position and angular orientation. The 6-DOF RBD module uses quaternions to define the angular orientations. However, these are easily translated into Euler angles. From the dynamic response, the grid point locations and grid point velocities are set. In the uncoupled mode, the forces and moments are not coupled with the RBD module. The motion of the projectile is kinematics only and depends on the initial linear and angular velocities prescribed.

The projectile state vector consists of the inertial position components of the projectile mass center \((x,y,z)\), the standard Euler angles \((\phi, \theta, \psi)\), the body frame components of the projectile mass center velocity \((u,v,w)\), and the body frame components of the projectile angular velocity vector \((p,q,r)\).
The entire state vector consisting of these 12 variables is required in the initial conditions before a virtual fly-out can be performed and a coupled dynamic solution can be obtained. Typically, we begin with a computation performed in “steady state mode” with the grid velocities prescribed to account only for the translational motion component of the complete set of initial conditions to be prescribed. At this stage, we also impose the angular orientations from the initial conditions. The complete set of initial conditions includes translational and rotational velocity components along with initial position and angular orientation. With a fixed translational velocity, we obtain the steady state solution. This becomes the initial condition for the next step which involves adding just the spin component of the projectile. With the addition of spin, time-accurate calculations are performed for a few cycles of spin until converged periodic forces and moments are obtained. A sufficient number of time steps are performed so that the angular orientation for the spin axis corresponds to the prescribed initial conditions. All this is performed in an uncoupled mode. The angular velocity initial conditions associated with the non-spin rotational modes are then added. The mesh is translated back to the desired initial position, the non-spin rotational velocity initial conditions are turned on, and computations are performed in the coupled mode.

As a special case, this procedure can also be run very easily in an uncoupled mode to model motions such as the pitching and rolling of a projectile. Such a time-accurate CFD procedure allows one to compute the dynamic derivatives of projectiles from the unsteady simulations. For determination of dynamic derivatives, all calculations are done only in the uncoupled mode. In addition, the translational velocity is fixed to zero. The spin component of the projectile or the angular velocity of the projectile is added to compute the rolling motion of the projectile. With the addition of spin, time-accurate calculations are performed for a few cycles of spin until converged periodic forces and moments are obtained. A sufficient number of time steps are similarly performed for the angular pitching motion case where the pitching motion (sinusoidal, for example) is imposed.

3. Results and Discussion

Time-accurate unsteady numerical computations were performed with Navier-Stokes and coupled 6-DOF methods to predict the flow field and aerodynamic coefficients and the flight paths of a fin-stabilized projectile at supersonic speed, $M = 3$. In all cases, full 3-D computations were performed, but no symmetry was used.

The supersonic projectile modeled in this study is an ogive-cylinder-finned configuration (see figure 2). The length of the projectile is 121 mm and the diameter is 13 mm. The ogive nose is 98.6 mm long and the afterbody has a 22.3-mm, 2.5-degree boattail. Four fins are situated on the back end of the projectile. Each fin is 22.3 mm long and 10.16 mm thick.
An unstructured computational mesh was generated for this projectile (see figure 3). In general, most of the grid points are clustered in the boundary layer as well as near the afterbody fin and the wake regions. The total number of grid points is about 6.5 million for the full grid. The first spacing away from the wall was selected to yield a $y^+$ value of 1.0. The projectile configuration has a base cavity and was included in the mesh generation process. The unstructured mesh also included the base cavity region and was generated with the use of the Multipurpose Intelligent Meshing Environment (MIME) grid-generation software recently developed by Metacomp Technologies.

![Figure 2. Finned configuration.](image)

Here, our primary interest is in the development and application of coupled CFD and RBD techniques for accurate simulation of the free flight aerodynamics and flight dynamics of the projectile in supersonic flight. The total aerodynamic forces and moments are used for the virtual
fly-outs of the projectiles. The first step was to obtain the steady state results for this projectile at a given initial supersonic velocity. Also imposed were the angular orientations at this stage. Corresponding converged steady state solution was then used as the starting condition along with the other initial conditions for the computation of coupled CFD-RBD runs. Numerical computations have been made for these cases at an initial velocity of 1034 m/s. The simulations were started a small distance away from the muzzle. The corresponding initial angle of attack was $\alpha = 4.9$ degrees and initial spin rate was 2500 rad/s. Figure 4 shows the computed pressure contours at a given time or at a given location in the trajectory. It clearly shows the orientation of the body at that instant in time and the resulting asymmetric flow field attributable to the body at angle of attack. The orientation of the projectile of course changes from one instant in time to another as the projectile flies down range. Figure 5 shows the variation of the Euler pitch angle with distance traveled. As seen in this figure, both the amplitude and frequency in the Euler angle variation are predicted very well by the computed results and match extremely well with the data from the flight tests. One can also clearly see that the amplitude damps as the projectile flies down range, i.e., with the increasing x-distance. As shown in figure 6, similar behavior is observed with the Euler yaw angle, and it damps with the increasing x-distance. Computed results again compare very well with the measured data from the flight tests.

Figure 4. Computed pressure contours.
Figure 5. Euler pitch angle versus x-distance.

Figure 6. Euler yaw angle versus x-distance.
The time histories of the pitch and yaw angles are often customarily presented as a motion plot where the pitch angle is plotted versus the yaw angle during the flight of the projectile. It represents the path traversed by the nose of the projectile during the flight trajectory (looking forward from the back of the projectile). Such motion plots are shown in figure 7. This figure shows the comparison of the motion plots obtained from the numerical simulations and the 6-DOF analysis of the flight results from ARFDAS (Aeroballistics Research Facility Data Analysis System) (13) software commonly used for this purpose. Computed results match very well with the experimental flight test results. The unsteady simulations took thousands of hours of central processing unit time on a Xeon PC cluster system running with 32 to 64 processors.

![Figure 7. Motion plot (a) computation, (b) flight test.](image)
The results produced by the virtual fly-out simulations provide the total aerodynamic forces and moments at every time step as the projectile flies down range. For a variety of reasons, one may want to extract the traditional aerodynamic force and moment coefficients from these coupled CFD-RBD simulations. For example, the aerodynamic coefficients are in many cases available from experiments and other databases and can be used for further verification and validation of the computed results obtained from the virtual fly-out simulations. Currently, work is in progress to look at a number of ways to achieve it. One way is to feed the CFD-RBD-generated data back into software such as ARFDAS and extract the aerodynamic coefficients with the same procedure used on the actual test data (14). Another approach is to perform a set of short time histories or virtual fly-outs at different Mach numbers and use a simple fitting procedure to estimate all aerodynamic force and moment coefficients (15).

Both approaches were used in this study to extract the aerodynamic force and moment coefficients for the finned projectile. In the first approach, the position (x,y,z) and the orientation (three Euler angles) of the projectile, obtained from the virtual fly-out simulations, were provided as input to ARFDAS. These are the six quantities that are actually measured in the free flight tests, a reduction procedure is performed, and the aerodynamics that best fit the data are obtained. The CFD-generated data were cast to resemble spark range data, and the same fitting procedure was applied. The aerodynamics that matched the CFD-supplied data were obtained and the aerodynamic coefficients were extracted (14). The second approach is currently being developed and the results, although somewhat preliminary, are included for comparison. The extracted aerodynamic coefficients are shown in table 1 and are compared with the same coefficients obtained with the actual test data. As shown in table 1, computed aerodynamic coefficients are generally in very good agreement with the data for the static aerodynamic coefficients such as the drag, normal force, and pitching moment coefficients. The table also includes a comparison of the dynamic derivatives such as the pitch-damping moment and the roll-damping derivatives. Dynamic derivatives extracted by the first approach seem to be in slightly better agreement with the data than those extracted by the second approach. As stated earlier, the second approach is still undergoing development, and its accuracy is expected to improve in the near future.

### Table 1. Comparison of extracted aerodynamic coefficients with test data.

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<th>Data Source</th>
<th>Mach No.</th>
<th>Zero Yaw Axial Force Coeff, C_{Xo}</th>
<th>Normal Force Coeff Deriv., C_{X_n}</th>
<th>Pitching Moment Coeff Deriv, C_{m_q}</th>
<th>Pitch Damping Moment Coeff, C_{m_q}</th>
<th>Roll Damping Moment Coeff, C_{l_p}</th>
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<td>Spark Range</td>
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<td>5.88</td>
<td>-12.46</td>
<td>-172</td>
<td>-3.24</td>
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<td>CFD (2)</td>
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<td>0.24</td>
<td>5.83</td>
<td>-12.36</td>
<td>-150</td>
<td>-3.40</td>
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Some of the results obtained from the fitting procedure with the first approach are shown figures 8 and 9. Figure 8 shows the total aerodynamic forces in all three coordinate directions as a function of the x-distance or the range. As shown in this figure, the ARFDAS fitting procedure produces aerodynamic forces that match well with the computed results from the virtual fly-out of the projectile. As seen here, the total axial force decreases with increasing range as the total angle
of attack decreases. Initially, the angle of attack is larger and it becomes smaller and smaller, i.e., the amplitude of oscillations becomes smaller with increasing x-distance. The total force in the y-direction, $F_y$, is initially larger and damps some until an x-distance of about 25 m. With increasing x-distance beyond 25 m, the amplitude of oscillation stays more or less the same. As expected, the force in the z-direction, $F_z$, follows a trend similar to that presented earlier with the Euler pitch angle (figure 5). As the pitch angle damps with increasing x-distance, so does the amplitude of oscillation in $F_z$. It decreases with the increase in the range. Figure 9 shows the variation of total aerodynamic moments with the distance downrange. All the moments are taken with respect to the center of gravity of the projectile. Again, the total aerodynamic moments ($M_x$, $M_y$, and $M_z$) produced by the ARFDAS fitting procedure match fairly well the computed results.

The actual flight model included a base cavity which is known to have an effect on the aerodynamic axial force. In the present computations with the unstructured grid, the base cavity was modeled and the flow field inside the base cavity was computed. Figure 10 shows the total aerodynamic forces in the three coordinate directions. This figure shows the comparison of these forces with and without the base cavity with the forces obtained from ARFDAS. As expected, the force in x-direction ($F_x$) is affected by the cavity. The predicted $F_x$ obtained with the base cavity matches with the ARFDAS result better than the $F_x$ predicted without it. The extracted zero yaw axial force coefficient for the projectile without the base cavity was found to be approximately 0.28 with both aerodynamic coefficient extraction approaches. As shown in table 1, it drops to 0.24 with the base cavity. The base cavity appears to have a negligible effect on the other aerodynamic forces.

Although the fitting technique in the first approach to extract the aerodynamic force and moment coefficients has been used over the years with the flight data, further validation of the force and moment coefficients derived from the virtual fly-out CFD data is required. Traditional steady and unsteady CFD procedures can be employed to compute the aerodynamic force and moment coefficients to determine the accuracy of the extraction methods. The predicted static aerodynamic coefficients such as the axial force, normal force, and the pitching moment coefficients compare very well with those extracted from the full dynamic coupled calculation. The accuracy of the extracted dynamic derivatives must be determined. The numerical framework described in section 2 can be easily modified to not allow translational motion. This separate unsteady CFD procedure can then be used to calculate the pitch-damping moment and the roll-damping dynamic derivatives for projectiles with sinusoidal pitching motion and spin, respectively.
Figure 8. Total aerodynamic forces (Fx, Fy, and Fz from top to bottom) versus x-distance, initial M = 3.0.
Figure 9. Total aerodynamic moments (Mx, My, and Mz from top to bottom) versus x-distance, initial $M = 3.0$. 
In the present work, emphasis is put on the numerical computation of the pitch-damping moment coefficient and its comparison with that extracted from the virtual fly-out simulations. Sinusoidal pitching motion is imposed and time-accurate CFD computations have been performed at various supersonic velocities. Figure 11 shows the time history of the pitching moment coefficient as a function of angle of attack at $M = 3$. Computed results shown here correspond to one full cycle of imposed pitching motion and include the pitch-up and pitch-down cycles. Also shown in this figure are the computed pitching moment coefficients for the first two complete pitch cycles. Other than the initial start-up differences, the computed results converge quite rapidly at this velocity. Results obtained for the third cycle (not shown here) were virtually identical to those of the second cycle. The static pitching moment coefficient can be easily obtained from this plot if we connect a line between the two end points in the $C_m$ curve corresponding to angles of attack of +1 and -1 degree and passing through the origin. The pitch-damping moment coefficient is related to the difference in the values of the pitching moment coefficients at 0-degree angle of attack in this case between the up and down portions of the imposed pitching motion.

Computed static pitching moment coefficients as well as computed dynamic pitch-damping moment coefficients were obtained from a series of time-accurate calculations at different supersonic velocities from $M = 1.6$ to $M = 3.4$ and are shown in figures 12 and 13, respectively. These computed results are compared with the data derived from free flight tests for the same projectile configuration with single and multiple fits. Figure 12 shows the variation of the computed pitching moment coefficient with Mach number. As shown in this figure, the static pitching moment coefficient increases with Mach number from $M = 1.6$ to $M = 3.4$ and the computed results match very well with the test results. Figure 13 shows the variation of the dynamic pitch-damping moment coeffi-
cient with Mach number. Again, computed pitch-damping moment coefficients have been compared to those obtained from the flight tests for the same configuration and the same supersonic velocities. The computed results are generally in good agreement with the data and they are within the accuracy of the experimental test results. As shown in figure 13, the pitch-damping moment coefficient predicted by the separate unsteady CFD procedure at $M = 3$ is -172.5, which is almost identical to that extracted by the first approach (see table 1) from the virtual fly-out CFD results. This result indicates that virtual fly-outs could be used to obtain the pitch-damping moment as accurately as the traditional unsteady CFD technique. Further work is needed and is currently in progress to determine the accuracy of the roll-damping coefficients and in looking at other techniques for extraction of the aerodynamic force and moment coefficients.

![Figure 11. Time history of the pitching moment coefficient with angle of attack in the pitch cycle, $M = 3.0$.](image)

![Figure 12. Pitching moment coefficient versus Mach number.](image)
4. Summary and Conclusions

This report describes a coupled CFD-RBD computational study undertaken to simultaneously determine the flight trajectory and the associated unsteady free-flight aerodynamics of a finned projectile with an unstructured grid. A 3-D unsteady unstructured Navier-Stokes solver is employed to compute the time-accurate flow fields for the finned projectile at supersonic velocities. Computed results have been obtained for the virtual fly-out case at an initial supersonic speed, $M = 3$ with time-accurate Navier-Stokes computational technique. Computed positions and orientations of the projectile have been compared with actual data measured from free flight tests and are found to be in good agreement. Aerodynamic force and moment coefficients have been extracted from the fully coupled CFD-RBD numerical solutions. Unsteady time-accurate CFD methods have been used separately to compute the dynamic pitch-damping moment derivatives and have been compared with those obtained from the fully coupled approach. Computed static pitching moment coefficients and dynamic pitch-damping moment derivatives have been obtained at various supersonic velocities between $M = 1.6$ and 3.4 and are found to compare well with the data obtained from free flight tests. Computed CFD results at $M = 3$ show that the pitch-damping moment derivative obtained from the virtual fly-out technique matches extremely well with that predicted by traditional unsteady CFD technique.

This work demonstrates a coupled method to accurately predict the time-accurate unsteady aerodynamics of a finned projectile at supersonic speed and provides for a new way to obtain the aerodynamic coefficients including the dynamic pitch-damping and roll-damping derivatives. The present CFD-RBD simulations clearly show the capability of the coupled approach and form the basis for future multidisciplinary, time-dependent computations of advanced maneuvering munitions.
5. References


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   ATTN AMSAM RD SS AT L AUMAN
   R W KRETZSHMAR
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1  DIRECTOR
   US ARMY RSCH LABORATORY
   ATTN AMSRD ARL CI OK (TECH LIB)
   BLDG 4600

18  DIR USARL
    AMSRD WM
       J SMITH
    AMSRD WM B
       M ZOLTOSKI
    AMSRD WM BA
       D LYON
    AMSRD WM BC
       P PLOSTINS
       I CELMINS
       M CHEN
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1 DSTL BEDFORD
   T BIRCH
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