Automated Consistency Checking of Requirements Specifications

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This article describes a formal analysis technique, called consistency checking, for automatic detection of errors, such as type errors, nondeterminism, missing cases, and circular definitions, in requirements specifications. The technique is designed to analyze requirements specifications expressed in the SCR (Software Cost Reduction) tabular notation. As background, the SCR approach to specifying requirements is reviewed. To provide a formal semantics for the SCR notation and a foundation for consistency checking, a formal requirements model is introduced; the model represents a software system as a finite-state automaton, which produces externally visible outputs in response to changes in monitored environmental quantities. Results of two experiments are presented which evaluated the utility and scalability of our technique for consistency checking in a real-world avionics application. The role of consistency checking during the requirements phase of software development is discussed.

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General Terms: Documentation, Languages, Verification

Additional Key Words and Phrases: Application-independent properties, consistency checking, formal requirements modeling, Software Cost Reduction (SCR) methodology, tabular notations

1. INTRODUCTION

Errors in requirements are pervasive, dangerous, and costly [Faulk 1995]. It is well known that the majority of software errors are introduced during the requirements phase [GAO 1992]. There is also growing evidence that

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requirements errors can lead to serious accidents. For example, a 1992 study found that the major source of safety-related software errors in NASA’s Voyager and Galileo spacecraft were errors in functional and interface requirements [Lutz 1993]. Unfortunately, fixing requirements errors can be extremely costly, especially if the errors are detected late in the software lifecycle. It is estimated that correcting requirements errors late (e.g., during maintenance) can cost up to 200 times as much as correcting the errors during the requirements phase [Boehm 1981; Fairley 1985]. Given the high frequency of requirements errors, the serious accidents they can cause, and the high cost of correcting them late, techniques for improving the quality of requirements documents and for early detection of requirements errors are crucial.

One promising approach to reducing requirements errors is to apply formal methods during the requirements phase of software development. By a formal method, we mean a development method based on some formalism, such as a formal specification notation or a formal analysis technique. A formal requirements specification can reduce errors by reducing ambiguity and imprecision and by making some instances of inconsistency and incompleteness obvious. Formal analysis can detect many classes of errors in requirements specifications, some of them automatically.

The SCR (Software Cost Reduction) requirements method was introduced more than a decade ago to specify the software requirements of real-time embedded systems unambiguously and concisely [Heninger 1980; Heninger et al. 1978]. Recently, the method has been extended to describe system, rather than simply software, requirements and to incorporate both functional requirements (the values the system assigns to outputs) and non-functional (e.g., timing and accuracy) requirements [Parnas and Madey 1995; van Schouwen 1990; van Schouwen et al. 1993]. Recent work has also strengthened the method’s formal underpinnings [Faulk 1989; Parnas and Madey 1995; van Schouwen 1990].

Designed for use by engineers, the SCR method has been successfully applied to a variety of practical systems, including avionics systems, such as the A-7 Operational Flight Program [Alspaugh et al. 1992; Heninger et al. 1978], a submarine communications system [Heitmeyer and McLean 1983], and safety-critical components of the Darlington nuclear power plant in Canada [van Schouwen et al. 1993]. More recently, a version of the SCR method called CoRE [Faulk et al. 1992] was used to document requirements of Lockheed’s C-130J Operational Flight Program (OFP) [Faulk et al. 1994]. The OFP consists of more than 100K lines of Ada code, thus demonstrating the scalability of the SCR method.

While the above applications of SCR rely mostly on manual techniques, effective use of the method in industrial settings will require powerful and robust tool support. A significant barrier to industrial use of formal methods to date has been the weakness of the methods associated with given formalisms. Although much attention has been focused on the formal aspects of formal methods, too little effort has been devoted to the supporting methods. To be useful in developing practical systems, not only must
formal methods provide rigor, in addition they must be supported by robust, well-engineered tools. In many practical cases, a large amount of detail is required to apply a formal method. This detail is difficult to manage without some automation.

To provide automated support for the SCR requirements method, we are developing a suite of prototype tools for constructing and analyzing formal requirements specifications [Heitmeyer et al. 1995a]. The tools include a specification editor for creating and modifying the specifications, a simulator for symbolically executing the system based on the specifications, and formal analysis tools for checking the specifications for selected properties.

One analysis tool, called a consistency checker, checks a requirements specification for properties defined by our formal requirements model [Heitmeyer et al. 1996]. Because the requirements model describes properties that all SCR requirements specifications must satisfy, the properties checked by the consistency checker are independent of a particular application. A second analysis tool, called a verifier, checks the specification for critical application properties, such as timing properties [Heitmeyer and Mandrioli 1996] and security properties [Landwehr et al. 1984]. Because verification of application properties depends on a consistent requirements specification, analysis using a verifier logically follows analysis with a consistency checker.

Checking the consistency of an SCR requirements specification is usually quite simple. For example, given a specification that includes a total function $F$, the consistency checker analyzes $F$ to make sure it is total (i.e., defined everywhere in $F$’s domain). Although checking such properties is usually straightforward, the number of times the properties need to be checked in practical requirements specifications can become very large, and thus reviewers must spend considerable time and effort verifying that the specifications have the properties. In fact, in the certification of the Darlington plant, Parnas [1993] has observed that the “reviewers spent too much of their time and energy checking for simple, application-independent properties” (such as the ones we describe in this article) which distracted them from the “more difficult, safety-relevant issues.” Tools that automatically perform such checks can save reviewers considerable time and effort, liberating them to do more creative work.

An industrial-strength formal method should be usable by engineers, scalable, and cost effective. Automated consistency checking as described in this article is an important step in developing such a method for requirements specification. It is easy to use: after developing a requirements specification in the SCR notation, a developer invokes the consistency checker to find inconsistencies automatically. It scales up to handle practical applications: in two experiments, our automated consistency checker found significant errors (that is, missing cases and nondeterminism) in the requirements specification of a medium-size Navy application. These errors were detected even though the specification had previously undergone systematic, comprehensive checks by two independent review teams. These results and the high cost (several million dollars) of the Darlington certifi-
cation effort, where such checks were done by hand, suggest that automated consistency checking is more cost effective than manual techniques.

After reviewing the SCR method for specifying requirements, this article introduces our formal requirements model, describes consistency checks based on the model, presents the results of experiments we conducted to determine the utility of automated consistency checking, and discusses the role of consistency checking in the software development process. The contributions of this article include (1) formal definition and application of a class of analysis, which we call consistency checking, for detecting domain-independent errors in requirements specifications and (2) evidence that software tools for automated consistency checking are usable, scalable, and cost effective.

2. REVIEW OF THE SCR METHOD

2.1 Background

The purpose of a requirements document is to describe all acceptable system implementations [Heitmeyer and McLean 1983]. The software requirements document for the A-7 aircraft’s Operational Flight Program was published in 1979 to demonstrate a systematic approach to producing such a document. The A-7 document introduces many features associated with the SCR requirements method—the tabular notation, the underlying finite-state machine model, and special constructs for specifying requirements, such as conditions and events, input and output data items, mode classes, and terms. Recently, a number of researchers, including Faulk [Faulk 1989; Faulk et al. 1992; 1994], van Schouwen [van Schouwen 1990; van Schouwen et al. 1993], and Parnas [Parnas and Madey 1995], have extended and refined the original SCR method and strengthened its formal foundations.

Faulk [1989] provided formal definitions for parts of the A-7 model. In particular, condition tables, a special class of tables in SCR requirements documents, are described as total functions and mode classes as finite-state machines defined over events. Using mode classes to partition the state space is a form of abstraction that not only makes analysis of the specifications more efficient, it also reduces redundancy and makes the specifications easier to understand. A deficiency in the original A-7 requirements document, however, is that a mode class may be undefined in certain states; for example, if no weapon is allocated, the Weapons mode class is undefined. Faulk’s model defines a mode class in every state; for example, when no weapon is allocated, the Weapons mode class is in mode None.

Using the original A-7 requirements document as a model, van Schouwen [1990] published a system-level requirements specification for the Water Level Monitoring System (WLMS), part of the shutdown system for a nuclear power plant. The WLMS specification extends the SCR method
from software requirements to system requirements and demonstrates the use of the method to describe a system's accuracy and timing requirements as well as its functional requirements. The Four-Variable Model of Parnas and Madey [1995] provides a formal framework for the SCR method.

2.2 Four-Variable Model

The Four-Variable Model, illustrated in Figure 1, describes the required system behavior, including the required timing and accuracy, as a set of mathematical relations on four sets of variables—monitored and controlled variables and input and output data items. A monitored variable represents an environmental quantity that influences system behavior, a controlled variable an environmental quantity that the system controls. A black-box specification of required behavior is given as two relations, REQ and NAT, from the monitored to the controlled quantities. NAT, which defines the set of possible values, describes the natural constraints on the system behavior, such as constraints imposed by physical laws and the system environment. REQ defines additional constraints on the system to be built as relations the system must maintain between the monitored and the controlled quantities.

In the Four-Variable Model, input devices (e.g., sensors) measure the monitored quantities, and output devices set the controlled quantities; input and output data items represent the values that the devices read and write. The relation IN defines the mapping from the monitored quantities to the input data items. The relation OUT defines the mapping from the output data items (e.g., actuators) to the controlled quantities. The use of monitored and controlled quantities to define the required behavior (rather than input and output data items) keeps the specification in the problem domain and allows a simpler specification.

Like the Four-Variable Model, our requirements model can be used to describe both system requirements and software requirements. Our model defines the system requirements by describing REQ, the required relation between the monitored and controlled variables, and the software requirements by describing SOFT, the required relation between the input and output data items. Below, the term input variable (output variable) represents a monitored variable (a controlled variable) when REQ is being defined and an input data item (an output data item) when SOFT is being defined.
The next section reviews the constructs and tabular notation used in SCR requirements specifications in terms of the Four-Variable Model. Because our initial requirements model emphasizes the system's functions, the discussion focuses on aspects of the Four-Variable Model that describe functional behavior.

2.3 SCR Constructs

To specify the relations of the Four-Variable Model in a practical and concise manner, four other constructs, each introduced in the A-7 requirements document [Heninger et al. 1978], are useful. These are modes, terms, conditions, and events. A **mode class** is a state machine, defined on the monitored variables, whose states are called **system modes** (or simply **modes**) and whose transitions are triggered by events. Complex systems are defined by several mode classes operating in parallel. Mode classes reduce redundancy in the specifications by assigning a name (i.e., a mode) to a logical expression used many times in the specifications and using the name rather than repeating the logical expression. A **term** is an auxiliary function defined on input variables, modes, or other terms that helps make the specification concise. A **condition** is a predicate defined on one or more system entities (a system entity is an input or output variable, mode, or term) at some point in time. An **event** occurs when any system entity changes value. A special event, called an **input event**, occurs when an input variable changes value. A **conditioned event** occurs if an event occurs when a specified condition is true.

To illustrate the SCR constructs, we consider a simplified version of the control system for safety injection described by Courtois and Parnas [1993]. The system uses three sensors to monitor water pressure and adds coolant to the reactor core when the pressure falls below some threshold. The system operator blocks safety injection by turning on a “Block” switch and resets the system after blockage by turning on a “Reset” switch. Figure 2 shows how SCR constructs are used to specify the requirements of the control system within the framework of the Four-Variable Model. Water pressure and the “Block” and “Reset” switches are represented as monitored variables, WaterPres, Block, and Reset; safety injection as a controlled variable, SafetyInjection; each sensor as an input data item; and the
hardware interface between the control system software and the safety injection system as an output data item.\(^1\)

The specification for the control system includes a mode class Pressure, a term Overridden, and several conditions and events. The mode class Pressure, an abstract model of the monitored variable WaterPres, contains three modes, TooLow, Permitted, and High. At any given time, the system must be in one of these modes. A drop in water pressure below a constant Low causes the system to enter mode TooLow; an increase in pressure above a larger constant Permit causes the system to enter mode High. The term Overridden describes situations in which safety injection is blocked. An example of a condition in the specification is “WaterPres < Low.” Events are denoted by the notation “@T.” Two examples of events are the input event @T(Block=On) (the operator turns Block from Off to On) and the conditioned event @T(Block=On) WHEN WaterPres < Low (the operator turns Block to On when water pressure is below Low).

### 2.4 SCR Tables

The tabular notation used in SCR specifications facilitates industrial application of the method. Not only do engineers find tabular specifications of requirements easy to understand and to develop; in addition, tables can describe large quantities of requirements information concisely. Among the tables in SCR specifications are condition tables, event tables, and mode transition tables. Each table defines a mathematical function. A condition table describes an output variable or term as a function of a mode and a condition; an event table describes an output variable or term as a function of a mode and an event. A mode transition table describes a mode as a function of a mode and an event.

Tables I–III are part of REQ, the system requirements specification for the control system. Table I is a mode transition table describing the mode class Pressure as a function of the current mode and the monitored variable WaterPres. The table defines all events that change the value of the mode class Pressure. For example, the first row of Table I states, “If Pressure is TooLow, and WaterPres rises to Low, then Pressure changes to Permitted.” Events that do not change the value of the mode class are omitted from the

\(^1\)The example omits the SCR bracketing notation, e.g., *\ldots* for a mode, /\ldots/ for an input data item, !\ldots! for a term, $\ldots$ for an enumerated value, etc.

<table>
<thead>
<tr>
<th>Old Mode</th>
<th>Event</th>
<th>New Mode</th>
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<tbody>
<tr>
<td>TooLow</td>
<td>@T(WaterPres ≥ Low)</td>
<td>Permitted</td>
</tr>
<tr>
<td>Permitted</td>
<td>@T(WaterPres ≥ Permit)</td>
<td>High</td>
</tr>
<tr>
<td>Permitted</td>
<td>@T(WaterPres &lt; Low)</td>
<td>TooLow</td>
</tr>
<tr>
<td>High</td>
<td>@T(WaterPres &lt; Permit)</td>
<td>Permitted</td>
</tr>
</tbody>
</table>

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1 The example omits the SCR bracketing notation, e.g., *\ldots* for a mode, /\ldots/ for an input data item, !\ldots! for a term, $\ldots$ for an enumerated value, etc.
Table II. Event Table for Overridden

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<tr>
<td>High</td>
<td>False</td>
</tr>
<tr>
<td>TooLow, Permitted</td>
<td>@T(Block=On) WHEN Reset=Off</td>
</tr>
<tr>
<td></td>
<td>@T(Inmode) OR @T(Reset=On)</td>
</tr>
<tr>
<td>Overridden</td>
<td>True</td>
</tr>
<tr>
<td></td>
<td>False</td>
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Table III. Condition Table for SafetyInjection

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<td></td>
<td>False</td>
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<td>TooLow</td>
<td>Overridden</td>
</tr>
<tr>
<td></td>
<td>NOT Overridden</td>
</tr>
<tr>
<td>Safety Injection</td>
<td>Off</td>
</tr>
<tr>
<td></td>
<td>On</td>
</tr>
</tbody>
</table>

table. For example, if Pressure is TooLow, and WaterPres changes, but does not reach Low, then Pressure is still TooLow after the event.

Table II is an event table describing the term Overridden as a function of Pressure, Block, and Reset. Like mode transition tables, event tables make explicit only those events that cause the variable defined by the table to change. For example, the middle entry in the second row states, “If Pressure is TooLow, and Block becomes On when Reset is Off, then Overridden becomes true.” In contrast, if the mode class is High, and either Block or Reset changes (from Off to On or vice versa), then the value of Overridden does not change because the first row does not specify events involving either Block or Reset. The entry “False” in an event table means that no event can cause the variable defined by the table to assume the value in the same column as the entry; thus, the entry “False” in row 1 of Table II means that when the mode class is High no event can cause Overridden to become true. The notation “@T(Inmode)” in a row of an event table describes system entry into the group of modes in that row; for example, “@T(Inmode)” in the second row of Table II means, “If the system enters TooLow or Permitted, then Overridden becomes false.”

Table III is a condition table describing the controlled variable SafetyInjection as a function of Pressure and Overridden. Table III states, “If Pressure is High or Permitted, or if Pressure is TooLow and Overridden is true, then SafetyInjection is Off; if Pressure is TooLow, and Overridden is false, then SafetyInjection is On.” The entry “False” in the first row means that SafetyInjection is never On when Pressure is High or Permitted.

While condition tables define total functions, event tables and mode transition tables may define partial functions. This is partly because some events cannot occur when certain conditions are true. For example, in the control system introduced above, the event @T(Pressure=High) WHEN Pressure=TooLow cannot occur, because starting from TooLow, the system can only enter Permitted when a state transition occurs. In other cases and as illustrated by the examples above, an event may occur that does not
change the value of a variable defined by an event table or a mode transition table. In our formal requirements model (see below), we make the functions defined by event tables and mode transition tables total by assigning a variable its old value whenever the table does not explicitly define the variable’s value.

3. FORMAL REQUIREMENTS MODEL

Although earlier requirements models—namely, Faulk’s automaton model [Faulk 1989], the model underlying van Schouwen’s specification [van Schouwen 1990; van Schouwen et al. 1993], and the Four-Variable Model—define some aspects of the SCR requirements method, these models are too abstract to provide a formal basis for our tools. To provide a precise and detailed semantics for the SCR method, our model represents the system to be built as a finite-state automaton and describes the input and output variables, conditions, events, and other constructs that make up an SCR specification in terms of that automaton. Our automaton model, a special case of the Four-Variable Model, describes all monitored and controlled quantities, even those which are naturally continuous, as discrete variables. Moreover, because our model abstracts away timing and imprecision, it describes the “ideal” system behavior. The system requirements are easier to specify and to reason about if the ideal behavior is defined first. Then, the required precision and timing can be specified separately. Heitmeyer [1996] describes how our model can be extended to include continuous variables and to describe timing and accuracy requirements.

Our requirements model, inspired by the formal security model presented by Landwehr et al. [1984], defines sets of modes, entity names, values, and data types and a special function TY, which maps an entity to its legal values. The model defines system state in terms of the entities, a condition as a predicate on the system state, and an input event as a change in an input variable which triggers a new system state. It also describes how a set of functions, called table functions, can be derived from the SCR tables. These table functions define the transform $T$, a special case of REQ (or SOFT), which maps the current state and an input event to a new state. Below, we present excerpts from our requirements model [Heitmeyer et al. 1996] along with examples taken from the system requirements specification for the simple control system introduced above. To clarify the presen-
3.1 System State

We assume the existence of the following sets.

- $MS$ is the union of $N$ nonempty, pairwise disjoint sets, namely, $M_1, M_2, \ldots, M_N$, called mode classes. Each member of a mode class is called a mode.
- $TS$ is a union of data types, where each type is a nonempty set of values.
- $VS = MS \cup TS$ is the set of entity values.
- $RF$ is a set of entity names. $RF$ is partitioned into four subsets: $MR$, the set of mode class names; $IR$, the set of input variable names; $GR$, the set of term names; and $OR$, the set of output variable names. For all $r \in RF$, $TY(r) \subseteq VS$ is the type (i.e., the set of possible values) of the entity named $r$. For all $r \in MR$, there exists $i$ such that $TY(r) = M_i$; we say that $r$ is the mode class name corresponding to $M_i$.

A system state $s$ is a function that maps each entity name $r$ in $RF$ to a value. More precisely, for all $r \in RF$: $s(r) = v$, where $v \in TY(r)$. Thus, by assumption, in any state $s$, the system is in exactly one mode from each mode class, and each entity has a unique value.

**Example.** In the sample system, the set of entity names $RF$ is defined by

$$RF = \{ \text{Block, Reset, WaterPres, Pressure, SafetyInjection, Overridden} \}.$$ 

The type definitions include

- $TY(\text{Pressure}) = \{ \text{TooLow, Permitted, High} \}$
- $TY(\text{WaterPres}) = \{ 0, 1, 2, \ldots, 2000 \}$
- $TY(\text{Overridden}) = \{ \text{true, false} \}$
- $TY(\text{Block}) = \{ \text{On, Off} \}$

3.2 Conditions

Conditions are defined on the values of entities in $RF$. A simple condition is $true$, $false$, or a logical statement $r \odot v$, where $r \in RF$ is an entity name; $\odot \in \{ =, \neq, >, <, \geq, \leq \}$ is a relational operator; and $v \in TY(r)$ is a constant value. A condition is a logical statement composed of simple conditions connected in the standard way by the logical connectives $\land$, $\lor$, and $\neg$.

3.3 Events

The “@T” notation denotes various events. A primitive event is denoted $@T(r = v)$, where $r$ is an entity in $RF$, and $v \in TY(r)$. An input event is a primitive event $@T(r = v)$, where $r \in IR$ is an input variable. A basic event

---

2 Here, $v$ is defined as a constant to keep the notation simple. Our formal model generalizes this definition, so that $v$ may be any function defined on entities whose range is $TY(r)$. 

is denoted \( \text{T}(c) \), where \( c \) is any simple condition. A *simple conditioned event* is denoted \( \text{T}(c) \) WHEN \( d \), where \( \text{T}(c) \) is a basic event, and \( d \) is a simple condition or a conjunction of simple conditions. Any basic event \( \text{T}(c) \) can be expressed as the simple conditioned event \( \text{T}(c) \) WHEN true. A *conditioned event* \( e \) is composed of simple conditioned events connected by the logical connectors \( \land \) and \( \lor \).

A simple conditioned event represents the logical expression defined by

\[
\text{T}(c) \text{ WHEN } d = \neg c \land c' \land d,
\]

where the unprimed version of condition \( c \) denotes \( c \) in the old state, and the primed version denotes \( c \) in the new state. Given \( c = r \odot v \), we define \( c' \) as \( c' = (r \odot v)' = r' \odot v \). Based on these definitions and the standard predicate calculus, any conditioned event can be expressed as a logical statement. An event occurs if the logical statement that the event represents evaluates to true for a given old state and a given new state.

**Example.** Applying the definition in (1), the conditioned event \( \text{T}(\text{Block}=\text{On}) \) WHEN \( \text{Reset}=\text{Off} \) can be rewritten as \( \text{Block} \neq \text{On} \land \text{Block}'=\text{On} \land \text{Reset}=\text{Off} \). This event occurs if both Block and Reset are Off in the old state and if Block is switched On in the new state.

### 3.4 System (Software System)

A *system* (software system) is a 4-tuple, \( (E^m, S, s_0, T) \), where

- \( E^m \) is a set of input events,
- \( S \) is the set of possible system states,
- \( s_0 \) is a special state called the initial state, and
- \( T \), the system transform, is a partial function\(^3\) from \( E^m \times S \) into \( S \).

A basic assumption, called the One-Input Assumption, is that exactly one input event occurs at each state transition.\(^4\)

### 3.5 Ordering the Entities

To compute an entity’s value in the new state, the transform function may use the values of entities in both the old state and the new state. To describe the entities needed in the new state, each entity \( r \) is associated with a subset of \( RF \) called the *new state dependencies set*. For each input variable, the new state dependencies set is empty. For each entity defined by a condition table, the set contains the entity naming the associated

---

\(^3\) \( T \) is a partial function because not all input events can occur in a given state. For example, in the control system, \( \text{Block} \) cannot change to \( \text{On} \) if \( \text{Block} \) is already \( \text{On} \).

\(^4\) Atlee and Gannon [1993] present an alternate definition of a conditioned event, namely, \( \text{T}(c) \) WHEN \( d = \neg c \land c' \land d \land d' \). When \( c \) and \( d \) define independent input variables, Definition (1) and the One-Input Assumption imply this alternative definition. Although we prefer Definition (1) because the alternate definition makes the expression of certain conditioned events overly complex, we see advantages in making two WHEN operators available to specifiers, namely, WHEN \( d \equiv d \) and WHEN \( d \equiv d \land d' \).
mode class and all entities appearing in conditions in the table’s body. For each entity defined by an event table or a mode transition table, the set contains all entities appearing in the table as part of a basic event and, if \( @T(\text{Inmode}) \) appears in the table, the associated mode class. These new state dependencies impose a partial ordering on the set \( RF \). Using these sets, the entities in \( RF \) can be ordered as a sequence \( R \), where for all \( i \) and \( j \) such that \( r_i \) and \( r_j \) belong to \( R \), \( r_i \) depends directly on \( r_j \) implies that \( r_i \) follows \( r_j \) in \( R \) (that is, \( i > j \)).

**Example.** The condition table in Table III shows that the controlled variable SafetyInjection depends on two entities in the new state, the mode class Pressure and the term Overridden. Hence, the new state dependencies set for SafetyInjection is the set \{Pressure, Overridden\}. The partial ordering of the entities based on the new state dependencies is determined as follows: the three monitored variables are first because they only depend on changes in the environment. Next is the mode class Pressure, which depends on WaterPres. Next is the term Overridden, which depends on Pressure and two monitored variables, Block and Reset. The last entity in the partial ordering is SafetyInjection. A sequence \( R \) satisfying this partial ordering is

\[
R = \langle \text{WaterPres}, \text{Block}, \text{Reset}, \text{Pressure}, \text{Overridden}, \text{SafetyInjection} \rangle.
\]

In sequence \( R \), \( r_1 = \text{WaterPres}, r_2 = \text{Block}, \ldots \), and \( r_6 = \text{SafetyInjection} \).

### 3.6 Table Functions

Each SCR table describes a *table function*, called \( F_i \), which defines an output variable, a term, or a mode class \( r_i \). Each entity \( r_i \) defined by a table is associated with exactly one mode class, \( M_j \), \( 1 \leq j \leq N \). To represent the relation between an entity and a mode class, we define a function \( \mu \), where \( \mu(i) = j \) if and only if entity \( r_i \) is associated with mode class \( M_j \). Using this notation, \( M_{\mu(i)} \) denotes the mode class associated with entity \( r_i \).

**Example.** The single mode class in this specification is Pressure. Hence, \( N = 1 \), and \( M_1 = \text{TY(Pressure)} = \{\text{TooLow}, \text{Permitted}, \text{High}\} \). Because all three entities defined by tables, namely, \( r_4 = \text{Pressure}, r_5 = \text{Overridden}, \) and \( r_6 = \text{SafetyInjection} \), are functions of Pressure, we have \( \mu(4) = \mu(5) = \mu(6) = 1 \).
Presented below for condition, event, and mode transition tables is a typical format and a description of how the table function is derived from a given table.

3.7 Condition Tables

Table IV shows a typical format for a condition table with \( n + 1 \) rows and \( p + 1 \) columns. Each condition table describes an output variable or term \( r_i \) as a relation \( r_i \) defined on modes, conditions, and values. More precisely, \( r_i = \{(m_j, c_j,k, v_k) \in M_{\mu(i)} \times C_i \times TY(r_i), \} \), where \( C_i \) is a set of conditions defined on entities in \( RF \). The relation \( r_i \) must satisfy the following four properties:

1. The \( m_j \) and the \( v_k \) are unique.
2. \( \bigcup_{j=1}^{n} m_j = M_{\mu(i)} \) (all modes in the associated mode class are included).
3. For all \( j: v_k = c_j,k = true \) (Coverage: the disjunction of the conditions in each row of the table is true).
4. For all \( j, k, l, k \neq l; c_j,k \land c_j,l = false \) (Disjointness: the pairwise conjunction of conditions in a row of the table is always false).

To make explicit entity \( r_i \)'s dependencies on other entities, we consider an alternate form \( F_i \) of the relation \( r_i \). The four properties above ensure that \( F_i \) is a total function. Properties (1) and (4) ensure that \( F_i \) is a function, while Properties (2) and (3) guarantee totality. To define \( F_i \), we require the new state dependencies set, \( \{y_{i,1}, y_{i,2}, \ldots, y_{i,n_i}\} \), where \( y_{i,1} \), is the entity name for the associated mode class, and \( y_{i,2}, \ldots, y_{i,n_i} \) are entities that appear in some condition \( c \) in \( C_i \). Based on this set and \( \rho_i \), we define \( r_i \) as a function \( F_i \) as follows:

\[
r_i = F_i(y_{i,1}, \ldots, y_{i,n_i}) = \begin{cases} v_1 & \text{if } \lor_{j=1}^{n} (y_{i,1} = m_j \land c_j,1) \\ v_2 & \text{if } \lor_{j=1}^{n} (y_{i,1} = m_j \land c_j,2) \\ \vdots \\ v_p & \text{if } \lor_{j=1}^{n} (y_{i,1} = m_j \land c_j,p) \end{cases}
\]

The function \( F_i \) is called a condition table function.

Example. Based on the new state dependencies set \( \{\text{Pressure, Overridden}\} \) and Table III, the condition table function for SafetyInjection, denoted \( F_6 \), is defined by

<table>
<thead>
<tr>
<th>Modes</th>
<th>Events</th>
</tr>
</thead>
<tbody>
<tr>
<td>( m_1 )</td>
<td>( e_{1,1} )</td>
</tr>
<tr>
<td>( m_2 )</td>
<td>( e_{2,1} )</td>
</tr>
<tr>
<td>( \ldots )</td>
<td>( \ldots )</td>
</tr>
<tr>
<td>( m_n )</td>
<td>( e_{n,1} )</td>
</tr>
<tr>
<td>( r_i )</td>
<td>( v_1 )</td>
</tr>
</tbody>
</table>
SafetyInjection =

\[ F_6(\text{Pressure}, \text{Overridden}) = \begin{cases} 
\text{Off} & \text{if } \text{Pressure} = \text{High} \lor \text{Pressure} = \text{Permitted} \lor \\
(\text{Pressure} = \text{TooLow} \land \text{Overridden} = \text{true}) & \text{if } \text{Pressure} \text{TooLow} \land \text{Overridden} = \text{false} \\
\text{On} & \text{if } \text{Pressure} = \text{TooLow} \land \text{Overridden} = \text{false} 
\end{cases} \]

3.8 Event Tables

Table V illustrates a typical format for an event table with \( n + 1 \) rows and \( p + 1 \) columns. Each event table describes an output variable or term \( r_i \) as a relation \( \rho_i \) between modes, conditioned events, and values, i.e., \( \rho_i = \{(m_j, e_{j,k}, v_k) \in M_{\mu(i)} \times E_i \times TY(r_i)\} \), where \( E_i \) is a set of conditioned events defined on entities in \( RF \). The relation \( \rho_i \) must satisfy the following two properties:

1. The \( m_j \) and the \( v_k \) are unique.
2. For all \( j, k, l \neq l \); \( e_{j,k} \land e_{j,l} = \text{false} \) (Disjointness: the pairwise conjunction of events in a row of the table is always false).

As with condition tables, we make explicit \( r_i \)'s dependency on other entities by extending the relation \( \rho_i \) to an alternate form \( F_i \). The One-Input Assumption and the two properties above ensure that \( F_i \) is a function. The “no change” part of \( F_i \)'s definition (see below) guarantees totality.

To define \( F_i \), we require both the new state dependencies set \( \{y_{i,1}, \ldots, y_{i,n}\} \) and an old state dependencies set \( \{x_{i,1}, x_{i,2}, \ldots, x_{i,m}\} \), which contains the associated mode class \( x_{i,1} \) along with all entities appearing in some \( e_{i,k} \) in the associated table. Based on the old state dependencies, the new state dependencies, and \( \rho_i \), \( F_i \) is defined by

\[ r'_i = F_i(x_{i,1}, \ldots, x_{i,m}, y'_{i,1}, \ldots, y'_{i,n}) = \begin{cases} 
v_1 & \text{if } \bigvee_{j=1}^{n} (x_{i,1} = m_j \land e_{j,1}) \\
v_2 & \text{if } \bigvee_{j=1}^{n} (x_{i,1} = m_j \land e_{j,2}) \\
\vdots & \\
v_p & \text{if } \bigvee_{j=1}^{n} (x_{i,1} = m_j \land e_{j,p}) \\
r_i & \text{otherwise (i.e., no change)}
\end{cases} \]

The function \( F_i \) is called an event table function. Note that if none of the \( e_{j,k} \) occurs, then the entity \( r_i \) defined by \( F_i \) retains its value in the old state.

Example. Both the old state dependencies set and the new state dependencies set for Overridden, \{Block, Reset, Pressure, Overridden\} and \{Block, Reset, Pressure\}, can be derived from Table II. Based on these sets and Table II, the event table function for Overridden is defined by
3.9 Mode Transition Tables

Table VI shows a typical format for a mode transition table for an entity \( r_i \) that names a mode class \( M_{\mu(i)} \). The table describes \( r_i \) as a relation 
\[
\rho_i = \{(m_j, e_{j,k}, m_{j,k}) \in M_{\mu(i)} \times E_i \times M_{\mu(i)} \}
\]
where \( E_i \) is a set of conditioned events defined on entities in \( RF \). The relation \( \rho_i \) must satisfy the following four properties:

1. The \( m_j \) are unique.
2. For all \( k \neq l, m_{j,k} \neq m_{j,l}, \) and for all \( j \) and for all \( k, m_j \neq m_{j,k}, \)
3. For all \( j, k, l, k \neq l; e_{j,k} \land e_{j,l} = false \) (Disjointness: the pairwise conjunction of conditioned events in a row of the table is always false).
4. Let \( m_0 \) be the initial mode. Then, \( M_{\mu(i)} \subseteq \{m \mid Q^*(m_0, m)\} \), where \( Q(m_1, m_2) \) if and only if \( \rho_i(m_1, e, m_2) \) for some \( e \) and \( Q^* \) is the reflexive and transitive closure of \( Q \) (Reachability: each mode must be reachable from the initial mode).

It is easy to show that a mode transition table with the format in Table VI can be expressed in the format shown in Table V for an event table. Hence, a mode transition table can be expressed as an event table function.

Example. Based on Table I, the old and new dependencies sets for the mode class Pressure are \{WaterPres, Pressure\} and \{WaterPres\}. Given these sets and Table I, the table function for Pressure is defined by

\[
\begin{align*}
\text{Pressure} & \quad \text{Pressure} = \text{Permitted} \land \text{WaterPres'} < \text{Low} \land \\
\text{TooLow} & \quad \text{Pressure} = \text{Permitted} \land \text{WaterPres'} < \text{Low} \land \\
\text{High} & \quad \text{Pressure} = \text{Permitted} \land \text{WaterPres'} \geq \text{Permit} \land \\
\text{Permitted} & \quad (\text{Pressure} = \text{TooLow} \land \text{WaterPres'} \geq \text{Low} \land \\
\text{Pressure} & \quad \text{Pressure} = \text{Permitted} \land \text{WaterPres'} < \text{Permit} \land \text{WaterPres} \neq \text{Permit}
\end{align*}
\]

Otherwise.

4. AUTOMATED CONSISTENCY CHECKING

Listed below are consistency checks derived from our formal requirements model. These checks, which determine whether the specifications are well formed, are independent of a particular system state. Because they can be performed without executing the system (or the specification), these checks are a form of static analysis.

— **Proper Syntax.** Each component of the specification has proper syntax. For example, each condition and event is well formed.

— **Type Correctness.** Each variable has a defined type, and all type definitions are satisfied. For example, given any expression of the form \( r = v \), where \( r \) is an entity and \( v \) a value, \( v \in TY(r) \) must hold.

— **Completeness of Variable and Mode Class Definitions.** The value of each controlled variable, term, and mode class is defined. (Most variables will be defined by tables, but standard mathematical definitions may be given for some controlled variables and terms.)

— **Initial Values.** Initial values are defined for all mode classes, input variables, terms, and output variables. Initial values are not required for entities defined by condition tables, since they can be derived from the tables.

— **Reachability.** Every mode in a mode class is statically reachable from the initial mode of the mode class. This is a check of Property (4) for Mode Transition Tables.

— **Disjointness.** To make the specifications deterministic, each condition, event, and mode transition table must satisfy the Disjointness property. That is, in a given state, each controlled variable, mode class, and term is defined uniquely.

— **Coverage.** Each condition table satisfies the Coverage property. That is, each variable described by a condition table is defined everywhere in its domain.

— **Lack of Circularity.** No circularities exist among the new dependencies sets. This property checks that the entities are partially ordered.
Clearly, some checks must precede others. For example, checks for proper syntax must precede type checking, and type checking should precede checking for the Coverage property.

4.1 Checking for Disjointness and Coverage

The most computationally expensive checks are checks for Disjointness and Coverage. To check these properties, the consistency checker determines whether a logical expression is a tautology. For example, to check two entries $c_1$ and $c_2$ in a row of a condition table for Disjointness, the consistency checker evaluates the logical expression $c_1 \land c_2 = false$. To check the entries $c_1, c_2, \ldots, c_n$ in a row of a condition table for Coverage, the tool evaluates the logical expression $c_1 \lor c_2 \lor \cdots \lor c_n = true$. To determine whether these logical expressions are tautologies, our tool applies a tableaux-based decision procedure that encodes the algorithm in Smullyan [1968].

Examples. Checking the consistency of Table VII, a modification of the condition table in Table III, reveals four errors. The third row has two type errors: SafetyInjection has the values Off and On, not False and True. The second row violates two properties of condition tables—namely, Coverage ($\text{Overridden} \lor \text{Overridden} = \text{Overridden} \neq true$) and Disjointness ($\text{Overridden} \land \text{Overridden} = \text{Overridden} \neq false$).

Disjointness, the second property required of event tables, is violated if events in two different columns, say $e_1$ and $e_2$, overlap, i.e., $e_1 \land e_2 \neq false$. Table VIII is a variation of the event table in Table II. Running the consistency checker detects a Disjointness error in the second row of Table VIII. In checking for Disjointness, the consistency checker evaluates the expression, 

$$\lnot (T(Block=On) \land \lnot (T(Reset=Off) \lor \lnot T(Block=On) \lor \lnot T(Reset=On))) = false$$

Below, we show that this expression is not a tautology.

Table VII. Modified Table for Safety Injection

<table>
<thead>
<tr>
<th>Mode</th>
<th>Conditions</th>
</tr>
</thead>
<tbody>
<tr>
<td>High, Permitted</td>
<td>True</td>
</tr>
<tr>
<td>TooLow</td>
<td>Overridden</td>
</tr>
<tr>
<td>Safety Injection</td>
<td>False</td>
</tr>
</tbody>
</table>

Table VIII. Modified Table for Overridden

<table>
<thead>
<tr>
<th>Mode</th>
<th>Events</th>
</tr>
</thead>
<tbody>
<tr>
<td>High</td>
<td>False</td>
</tr>
<tr>
<td>TooLow, Permitted</td>
<td>@T(Block=On) WHEN Reset=Off</td>
</tr>
<tr>
<td>Overridden</td>
<td>True</td>
</tr>
</tbody>
</table>
Because the expression does not evaluate to false, the specified behavior is nondeterministic, i.e., there is at least one pair of states \((s, s')\), where the event expression evaluates to true. In particular, if in TooLow or Permitted mode the operator turns Block on when Reset is off, the system may nondeterministically change Overridden to true or to false.

Some checks, such as syntax and type checking, are straightforward. More complex are checks that depend on definitions, other than type definitions, in different parts of the specification or checks that require deductive reasoning. Consider, for example, checking the mode table in Table I for nondeterminism. Nondeterminism can occur only if events in the second and third rows overlap. These rows overlap if the expression 

\[ \negT{\text{WaterPres}} \land \negT{\text{Permit}} \lor \negT{\text{WaterPres}} \land \text{Low} \lor \negT{\text{WaterPres}} \land \text{High} \lor \negT{\text{WaterPres}} \land \text{Low} \land \negT{\text{WaterPres}} \land \text{High} \]

By assumptions on the constants, Permit > Low. This assumption and WaterPres’ ≥ Permit imply WaterPres’ ≥ Low, a contradiction. Hence, the expression is always false and the defined behavior deterministic.

We have provided a semantic framework to reason formally about assumptions, such as Permit > Low, that underlie a specification. Because, in general, mechanical evaluation of such expressions is undecidable, we are devising algorithms to identify and evaluate decidable subsets of these expressions under a set of assumptions (see Bharadwaj [1996] for details). For the general case, the tool may need user feedback to complete certain checks.

4.2 Efficiency of Our Technique

The analysis performed by our consistency checker is quite efficient because it is based on static checks of components of an SCR requirements specification rather than some form of reachability analysis. As noted above, some checks, such as checks for proper syntax, type correctness, and the completeness of definitions, are easy. Moreover, mode reachability can be computed using standard search techniques in time linear in the number of transitions in the mode class. Similarly, checking for lack of
circularity requires time linear in the number of arcs in the new state dependencies graph.

Our definition of the transform function \( T \) simplifies checking that \( T \) is complete (for each input event that may occur, at least one new system state is completely defined) and deterministic (at most one new system state is defined). Determinism and completeness are guaranteed if the following properties are satisfied for each input event that occurs (see Heitmeyer et al. [1996] for details):

—Lack of circularity,
—Properties (1)–(4) for condition tables,
—Properties (1)–(2) for event tables, and
—Properties (1)–(3) for mode transition tables.

As we indicate above, checking for Disjointness and Coverage amounts to checking that logical formulas on conditions or events are tautologies. Although tautology checking may have worst-case behavior that is exponential in the size of the expression [Garey and Johnson 1979], we expect this not to occur in practice. In particular, the use of modes to partition the system state means that Disjointness and Coverage checking is decomposed into small, independent subproblems. Thus Coverage checking for condition tables can be performed independently for each row (rather than checking all rows together for missing cases). Similarly, each condition table, event table, and mode transition table can be checked for Disjointness by analyzing each pair of cells in a row (rather than checking two columns at a time). Another benefit of using modes arises in analyzing Coverage errors: in our consistency checker, the same analysis that detects an error also identifies the specific cause of the error (i.e., the missing cases) and its precise location in the table. Section 6 compares our approach to Disjointness and Coverage checking with other approaches.

Our experience with consistency checking is that the number of subproblems and the size of each subproblem grow rather slowly. In contrast, using state reachability techniques, such as model checking, to check for Disjointness and Coverage would be more expensive, because the cost of reachability analysis increases exponentially with the size of the specification. Thus we expect that our techniques would not suffer the state explosion problem that plagues techniques such as model checking. Section 5 demonstrates that our technique for consistency checking scales to industrial-strength systems. Because consistency checking is cheap, it makes sense to perform consistency checking early and to postpone more expensive checks, such as model checking, until later on.

4.3 Prototype Consistency Checker

A prototype consistency checker that performs all of the above checks has been implemented [Heitmeyer et al. 1995a]. The tool is coded in C++ and runs on X-Windows with Motif widgets to support its user interface. In a typical session with the consistency checker, the user edits a specification...
and then runs the consistency checker to test for selected properties. The tool runs the selected checks, listing any errors it finds. The user may select one of the listed errors to display the parts of the specification that produced the error (e.g., the specific rows or entries of the relevant table). In the case of a Coverage or a Disjointness error, the tool also displays a counterexample. Once the user has made corrections, he or she can rerun the consistency checker to ensure that (1) the error has been properly corrected and (2) no new errors have been introduced.

5. APPLYING CONSISTENCY CHECKS

To evaluate the utility of checking requirements specifications for consistency, we conducted two experiments. In the experiments, our consistency checker was used to analyze both the condition tables and the mode transition tables in a revised version [Alspaugh et al. 1992] of the requirements specification for the A-7’s Operational Flight Program (OFP). The OFP contains more than 16K lines of tight assembly code. The revised version corrects several errors in the original specification [Heninger et al. 1978] and uses a new tabular format to specify mode transitions [Faulk 1989; Meyer and White 1983].

The results of these two experiments demonstrate the efficiency of our techniques. Running on a Sun SPARCstation 20, our consistency checker checked all of the condition tables in the A-7 requirements specification for both Disjointness and Coverage and all of the mode transition tables in the specification for Disjointness. The tool required a total computation time of 245 seconds to perform the entire analysis. This time includes a time of 45 seconds to check the syntax and type correctness of the tables and only 200 seconds for all of the Disjointness and Coverage checks, 30 seconds for the condition tables, and 170 seconds for the mode transition tables.

Below, we briefly describe the two experiments. Because each mode transition table is much larger than any of the condition tables and thus more complex to analyze, we describe the analysis of the mode transition tables in somewhat more detail.

5.1 Checks on Condition Tables

In the first experiment, our tool checked 36 condition tables, a total of 98 rows, for both Coverage and Disjointness. The tool found 19 errors. Seventeen of these, distributed over 11 tables, proved to be legitimate errors. Determining that the remaining two “errors” were correct required knowledge that our simple tool lacked. Both cases involved three values describing combined settings of two input devices. We confirmed by hand that the two rows containing these values satisfy the two properties.

Table IX describes the detected errors. Interestingly, all 17 are Coverage errors. In this example, the reason why inspection is more likely to detect Disjointness errors than Coverage errors is that all the information needed to detect Disjointness errors is in the table, whereas the information needed to detect Coverage errors is not. Finding Coverage errors requires
knowledge of all values a variable can take on. In Alspaugh et al. [1992],
some type information is provided, not in the table, but elsewhere in the
requirements document; in several cases, it is omitted entirely. (Omission
of type information is a consequence of the semiformal nature of the A-7
requirements document. Using our tool, which enforces the type definitions
of our requirements model, helps eliminate such errors. The tool checks
that each entity in the specification has a corresponding type definition and
that each logical expression in the specification satisfies the type defini-
tions.)

5.2 Checks on Mode Transition Tables

In a second experiment, our tool checked all three mode transition tables in
the A-7 requirements specification for Disjointness. The three mode
classes contain a total of 48 different modes (18 modes in the first mode
class, 7 modes in the second, and 23 modes in the third). The mode
transition tables together contain a total of 700 rows, each row a simple
conditioned event of the form described below. In analyzing the tables, our
tool found 57 Disjointness errors. Although many of the 57 instances of
Disjointness violations that the tool detected are undoubtedly errors, a few
probably are not, since some detected events may be impossible. (As noted
above, some events cannot occur when certain conditions are true.) Of the
57 errors, 54 occurred in the mode transition table for the Weapons mode
class and the remaining three in the mode transition table for the Align-
ment, Navigation, and Test mode class. Many of the Disjointness errors in
the table for the Weapons mode class were instances of nondeterminism
present in the prose requirements documents from which the A-7 require-

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5 The authors learned recently of an experiment, reported in 1983, which also detected
Disjointness errors in mode transition tables [Meyer and White 1983]. However, our algorithm
is more general than the algorithm of Meyer and White.

6 Heitmeyer et al. [1995b] describe a similar experiment which used an early version of the
consistency checker and detected fewer errors. Although the early tool used the same
algorithm, it only looked for one Disjointness error for every pair of disjunctions it analyzed.
The current tool is designed to find all Disjointness errors and thus detected additional errors.
ments specification [Alspaugh et al. 1992; Heninger et al. 1978] was partially derived.

Table X, an excerpt from the revised A-7 specification, shows a small part of the mode transition table for the Alignment, Navigation, and Test mode class. (In Alspaugh et al. [1992], the complete table is more than 14 pages long.) This table has the same formal definition as Table I, but a more structured format. In contrast to Table I, headings in the middle column are simple conditions defined on input variables and terms. Each row of the middle column of Table X must contain a simple conditioned event. Consecutive rows of Table X that are not separated by a dashed line (e.g., rows 2 through 5) represent the disjunction of the simple conditioned events in the rows. In Table X, the notation “@T” (“@F”) denotes the event occurring when the corresponding condition becomes true (false); “t” (“f”) means that the corresponding condition is true (false); and “—” means that the corresponding condition may be either true or false. To clarify the relationship between the two formats for mode transition tables, Table XI translates the first five rows of Table X into the alternate format. (Except for the asterisks denoting mode names, Table XI omits the special SCR brackets.)

Table X. Error Detected in the Mode Transition Table for the Alignment, Navigation, and Test Mode Class [Alspaugh et al. 1992].

<table>
<thead>
<tr>
<th>Current Mode</th>
<th>New Mode</th>
</tr>
</thead>
<tbody>
<tr>
<td><em>Ain</em></td>
<td><em>Landahl</em></td>
</tr>
<tr>
<td><em>Dig</em></td>
<td></td>
</tr>
<tr>
<td><em>Di</em></td>
<td></td>
</tr>
<tr>
<td><em>OlB</em></td>
<td><em>Mag sl</em></td>
</tr>
<tr>
<td><em>Grid</em></td>
<td><em>IMS fail</em></td>
</tr>
<tr>
<td><em>Polar</em></td>
<td></td>
</tr>
</tbody>
</table>
Table X illustrates a Disjointness error detected by our consistency checker. Because the two conditioned events marked by arrows are mapped to different new modes, they should not overlap. That they do overlap is an error. Overlap in these two events allows the system to transfer nondeterministically from the mode Inertial (*I*) to either the mode Airborne Alignment (*Airaln*) or the mode Doppler Inertial (*DI*). An event that triggers either transition is

\[
\@T(\text{Doppler up}) \text{ WHEN } \neg (\text{CA stage complete}) \land \text{IMSMODE} = \text{Gndal} \land \text{latitude} > 70 \deg \land \text{latitude} \geq 80 \deg \land \neg (\text{present position entered}).
\]

Table XI. Mode Transition Table in Table X Expressed in the Alternate Format

<table>
<thead>
<tr>
<th>Current Mode</th>
<th>Event</th>
<th>New Mode</th>
</tr>
</thead>
<tbody>
<tr>
<td><em>I</em></td>
<td>@F(ACAIRB = Yes) WHEN NOT(Data23 = Sea) \land \text{IMSMODE} = \text{Gndal}</td>
<td><em>Landln</em></td>
</tr>
<tr>
<td><em>I</em></td>
<td>@T(Doppler up) WHEN NOT(CA stage complete) \land \text{IMSMODE} = \text{Gndal} \lor @T(Doppler up) WHEN NOT(CA stage complete) \land \text{IMSMODE} = \text{Norm} \lor @T(\text{IMSMODE} = \text{Gndal}) WHEN NOT(CA stage complete) \land \text{Doppler up} \lor @T(\text{IMSMODE} = \text{Norm}) WHEN NOT(CA stage complete) \land \text{Doppler up}</td>
<td><em>Airaln</em></td>
</tr>
</tbody>
</table>

Table X illustrates a Disjointness error detected by our consistency checker. Because the two conditioned events marked by arrows are mapped to different new modes, they should not overlap. That they do overlap is an error. Overlap in these two events allows the system to transfer nondeterministically from the mode Inertial (*I*) to either the mode Airborne Alignment (*Airaln*) or the mode Doppler Inertial (*DI*). An event that triggers either transition is

\[
\@T(\text{Doppler up}) \text{ WHEN } \neg (\text{CA stage complete}) \land \text{IMSMODE} = \text{Gndal} \land \text{latitude} > 70 \deg \land \text{latitude} \geq 80 \deg \land \neg (\text{present position entered}).
\]

In its analysis, the consistency checker examined 4319 conjunctions. Each conjunction was of the form \( e_1 \land e_2 \), where \( e_1 \) and \( e_2 \) are simple conditioned events from two different rows of a mode transition table in the format shown in Table X. The two rows have the same current mode but different new modes. The arrow in Table X indicates two such rows. In the analysis, the maximum number of \( @T, @F, t, \) or \( f \) entries in the analyzed conjunctions (that is, entries not marked “.”) was 18. The average number of \( @T, @F, t, \) or \( f \) entries in the analyzed conjunctions was 5.7. Of the 4319 conjunctions, 1691 required analysis by the tautology checker, while the remainder were analyzed separately because they were trivial. Our experience is that the relatively small sized logical expressions analyzed in our experiments do not require sophisticated algorithms, such as BDDs [Bryant 1986].

5.3 Manual vs. Automated Checks

Prior to its publication, the revised A-7 requirements document was carefully reviewed by two teams, one made up of NRL computer scientists (including the third author), the other composed of engineers at the Naval Air Warfare Center who maintained the OFP. As noted above, our tools detected many significant errors that the reviewers missed.
That errors were detected should not diminish the credit due the reviewers, who did very well given the large volume and complexity of the requirements data. Tools, such as ours, can complement the efforts of software developers. Human effort is crucial to acquiring the requirements information and expressing it precisely. Further, after errors are detected in the specification, human intervention is needed to correct them. However, once the developers have a reasonable draft of the requirements specifications, software tools provide a quick, effective means of checking the specification for properties, such as those described in Section 4. Not only are tools more effective than people for checking these properties; in addition, they can significantly reduce a labor-intensive task that humans find tedious and boring.

Another important feature of our tool is its low cost. In the Darlington certification effort, which cost over U.S. $40M, reviewers checked the requirements specifications for application-independent properties, such as Disjointness and Coverage. In addition, they searched for discrepancies between the requirements specifications and the code specifications. A tool that compares the specifications with a refinement will be more complex than our consistency checker. However, this does not diminish the value of our tool. Parnas [1993] has observed that the “majority of the theorems that arose in the documentation and inspection of the Darlington Nuclear Plant Shutdown Systems” were simple properties and that the reviewers analyzed trivial tables for such properties in documents weighing 40 kilograms. Using tools to do this analysis should cost far less than using people.

6. RELATED WORK

A number of industrial organizations, including Bell Laboratories [Hester et al. 1981], Grumman [Meyer and White 1983], Ontario Hydro [Parnas et al. 1991], and the Software Productivity Consortium [Faulk et al. 1992; 1994], have adapted the SCR method to specify the requirements of practical systems. Additionally, Parnas [1992] and Janicki [1995] have developed formal semantics for many classes of tables. The condition tables and event tables defined formally in Section 3 are special cases of their Inverted Tables. For another class of tables defined by Parnas [1994] called Program Tables, a tool has been developed which checks for Disjointness and Coverage errors before proceeding with additional analyses [Dai and Scott 1995]. Below, we briefly describe other related work: two other automated techniques for analyzing tabular specifications for consistency and three other approaches for detecting errors in SCR requirements specifications.

6.1 Decision Table Processors

Decision tables [Hurley 1983; Metzner and Barnes 1977], an early tabular notation, have been used for many years to specify software requirements because tables are easier to read than expressions in predicate logic.
Typically, decision tables associate each system input with one or more actions. A general difference between SCR and methods based on decision tables is that, unlike SCR, which associates a separate table with each output, term, and mode class in the specification, methods based on decision tables do not usually decompose a specification into smaller, more manageable pieces. A notable exception is an early specification technique, called Systematics [Grindley 1968], which decomposes decision tables into smaller tables similar to SCR's condition tables.

Various techniques have been developed to process decision tables. Although most techniques focus on code generation, a few have been designed to do consistency checking. DETRAN (DEcision TRANslator) is an early example of a technique that checks decision tables for both Disjointness and Coverage. It can also translate the contents of a given table to either Fortran or Cobol [Hughes et al. 1968].

6.2 Tablewise
Tablewise [Hoover and Chen 1995], a recent technique for processing decision tables, checks a table for both Disjointness (called “consistency”) and Coverage (called “completeness”). Tablewise improves on earlier techniques based on decision tables in that it supports nonboolean variables. The format of the tables analyzed by Tablewise is similar to the format of Table X, except conditions label rows (rather than columns), and each column is associated with an action. A significant difference between the tables processed by Tablewise and SCR tables is that the former do not use modes.

6.3 RSML
The Requirements State Machine Language (RSML) [Heimdahl and Leveson 1995; Jaffe et al. 1991; Leveson et al. 1994], which was developed to describe real-time process control systems, uses a combination of graphical and tabular notations. RSML's graphical notation (e.g., its superstates and AND-decomposition) is largely borrowed from Statecharts [Harel 1987]. Additional features of RSML include directed one-to-one communication among high-level state machines and the introduction of AND/OR tables to describe the guards on state transitions. Each table in RSML describes the conditions under which a given state machine can make a transition from one state to a second state under a specific input event. An output event may be associated with each table. The format of RSML tables resembles the format of Table X, except (as in Tablewise) conditions label the rows of the table rather than the columns. Also, in contrast to Table X, different conditions need not be disjoint; events do not appear as table entries; and modes (that is, modes defined explicitly as functions of input variables) are not used.

A prototype tool has been developed for checking RSML specifications for “completeness” (i.e., every possible input event and the system's response to the event must be stated explicitly) and “consistency” (i.e., no input
event can cause a transition to two different system states). The tool, which has been applied to large portions of the requirements specification of TCAS II, a collision avoidance system for commercial aircraft, detected errors not caught by an extensive manual review.

6.4 Consistency Checking in Tablewise, RSML, and SCR
RSML and SCR each support next-state semantics that simplify checking for completeness and determinism. In either case, these checks may be performed by decomposing the problem into smaller subproblems and avoiding the state explosion inherent in reachability techniques. However, a comparison of these two requirements languages and of the analysis required to perform Disjointness and Coverage checks is made difficult by the major differences in the RSML and SCR semantics. Further investigation is required for a quantitative comparison of these two methods on realistic systems.

Because decision table processors, such as Tablewise, do not structure a specification using mode classes, they cannot exploit the reduced analysis for Coverage and Disjointness errors that mode classes make possible. In addition to reducing the analysis needed to check certain properties, our use of modes also makes it easy to determine the specific cause of an error. When Tablewise detects a Coverage error, additional analysis, called a “structural analysis,” must be performed to determine the missing cases [Hoover and Chen 1995]. This additional analysis is unnecessary for our consistency checker: As noted above, the specific cases that have been omitted as well as the precise row of the table in which the missing case was detected are byproducts of the analysis our tool does in checking for coverage errors.

6.5 Mechanical Proof Systems
Parnas [1993] describes 10 small theorems that must be true of sample specifications expressed in his tabular notation (similar to other SCR notation) and challenges the developers of automated proof systems to prove the theorems. Two of the theorems, the Domain Coverage Theorem and the Disjoint Domains Theorem, are slight variations of our Coverage and Disjointness properties. SRI researchers accepted Parnas’ challenge. In a recent paper [Rushby and Srivas 1993], they describe the mechanical proof of nine of Parnas’ theorems using the “tcc-strategy” (tcc’s are type correctness conditions) of SRI’s proof system PVS [Crow et al. 1995]. That PVS can prove such theorems easily is not too surprising, since the proofs are based on very simple logic. What is noteworthy about the PVS experiment is that the theorems were proven automatically.

6.6 Model Checking
Atlee and Gannon [1993] have demonstrated the utility of model checking [Clarke et al. 1986] for detecting application-dependent errors in SCR requirements specifications. However, where our consistency checker tests
all tables and other definitions (e.g., definitions of types, constants, etc.) in an SCR specification, their tool analyzes properties of the mode transition tables only.

6.7 Detecting Errors by Inspection
A recent experiment [Porter and Votta 1994] compares the effectiveness of three different inspection methods for detecting errors in SCR requirements specifications. Many of the errors of interest in the experiment can be automatically detected by our consistency checker. Using a tool like ours in conjunction with inspection is likely to detect more errors than either alone.

7. REQUIREMENTS PROCESS
We envision the following process for developing requirements specifications. Although such a process is an idealization of a real-world process [Parnas and Clements 1986], it shows how tools such as our consistency checker can be used to produce high-quality requirements specifications.

(1) A formal notation, such as the SCR notation, is used to specify the requirements.

(2) An automated consistency checker is used to check the specification for syntax and type correctness, coverage, determinism, and other application-independent properties.

(3) The specification is executed symbolically using a simulator to ensure that it captures the customers' intent.

(4) In the later stages of the requirements phase, mechanical support is used to analyze the specification for application properties. Initially, a small subset with fixed parameters and only a few states is extracted from the specification, and a tool, such as a model checker, is used to detect violations of the properties. This may be repeated, each time with a different or larger subset. Once there is sufficient confidence in the specification, a mechanical proof system may be used to verify the complete requirements specification or, more likely, safety-critical components.7

8. CONCLUDING REMARKS
Based on our experience with automated consistency checking to date, we have four conclusions:

—Tools for consistency checking can be highly effective for detecting errors in requirements specifications. Not only can such tools find errors people miss; they can liberate people from the tedious and error-prone task of checking specifications for consistency.

7 A similar approach that combines model checking and mechanical theorem proving is suggested in Lincoln and Rushby [1993].
—Using properly designed tools for consistency checking is significantly cheaper than using people.

—Computer-based analysis requires an explicit formal semantics, such as that provided by our requirements model. This semantics provides the basis for algorithms that do the analysis.

—The formal method on which our tools are based scales up. The method detected a significant number of errors in a medium-size real-world specification. The structuring of the specifications using modes contributes significantly to the efficiency with which consistency checks, especially Disjointness and Coverage checks, can be performed on large requirements specifications.

In addition to the consistency checker described in this article, our current toolset includes a specification editor and a simulator. We are also developing a verifier that checks SCR requirements specifications for application properties. An option being considered is to link the toolset with a mechanical proof system to support both automated consistency checking and computer-assisted verification. This would relieve us of the difficult and error-prone task of encoding our own proof engine.

We expect our requirements model to provide a solid foundation for a suite of analysis tools. We also expect the process outlined above, which uses formal notation to specify requirements and computer-supported formal analysis to detect errors, to produce high-quality requirements specifications. Such specifications should produce systems that are more likely to perform as required and less likely to lead to accidents. They should also lead to significant reductions in software development costs.

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Consistency Checking of Requirements Specifications


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