ABSTRACT

The objective of this program has been to work towards development of spin based quantum dots for optically driven quantum information processing. Using a combination of ultrahigh resolution laser spectroscopy to study the physics of the dots and ultrafast laser technology to coherently control the spins, we made several advances. Our main achievements include working with a model system based on the exciton optical Bloch vector where we demonstrated the first solid state quantum logic device and made the first demonstration of quantum state tomography in a solid. We also were successful in taking the new quantum dot structures produced by our collaborator, Dan Gammon at NRL that contained one electron, and demonstrated optically induced and detected quantum spin coherence and coherent optical control of the spin state. Our high resolution measurements also provided a measurement of the spin relaxation rate. The funding level in this program was primarily to support one graduate student and purchase equipment. The remaining support for the work comes from ARO, NSA (formerly ARDA), AFOSR, NSF.
**REPORT DOCUMENTATION PAGE**

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### 1. REPORT DATE
5/15/06

### 2. REPORT TYPE
FINAL TECHNICAL REPORT

### 3. DATES COVERED (From - To)
August 30, 2002 - December 31, 2005

### 4. TITLE AND SUBTITLE
Optically Controlled Quantum Dot Spins for Scaleable Quantum Computing

### 5a. CONTRACT NUMBER
N00014-02-1-0981

### 5b. GRANT NUMBER

### 5c. PROGRAM ELEMENT NUMBER

### 5d. PROJECT NUMBER

### 5e. TASK NUMBER

### 5f. WORK UNIT NUMBER

### 6. AUTHOR(S)
Duncan G. Steel

### 7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)
University of Michigan, EECS Department
1301 Beal Avenue, 1106 EECS Bldg.
Ann Arbor, MI 48109-2122

### 8. PERFORMING ORGANIZATION REPORT NUMBER

### 9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)
Defense Advanced Research Projects Agency

### 10. SPONSOR/MONITOR'S ACRONYM(S)
DARPA

### 11. SPONSOR/MONITOR'S REPORT NUMBER(S)

### 12. DISTRIBUTION/AVAILABILITY STATEMENT
Approved for public release; distribution unlimited

### 13. SUPPLEMENTARY NOTES

### 14. ABSTRACT
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### 15. SUBJECT TERMS

### 16. SECURITY CLASSIFICATION OF:
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### 17. LIMITATION OF ABSTRACT
UU

### 18. NUMBER OF PAGES
9

### 19a. NAME OF RESPONSIBLE PERSON
Duncan G. Steel

### 19b. TELEPHONE NUMBER (Include area code)
734-764-4469

*Standard Form 298 (Rev. 8/98)*

Prescribed by ANSI Std. 239.18
FINAL REPORT TO DARPA

Optically Controlled Quantum Dot Spins for Scaleable Quantum Computing

Contract Period: 8/30/02-7/31/05  NCTX 12/31/05
Grant No.: N00014-02-1-0981
Principle Investigator: Duncan G. Steel
The University of Michigan
Ann Arbor, MI 48109
734-764-4469
dst@umich.edu

Publications that reference this grant for support

Refereed Journal Articles
M.V. Gurudev Dutt, Yanwen Wu, Xiaoqin Li, D.G. Steel, D. Gammon, L.J. Sham, “Semiconductor quantum dots for quantum information processing : An


Invited Presentations


D.G. Steel, “Coherent Optical Control of Single Quantum Dots: A Step Towards


D.G. Steel, "Optical control in semiconductor dots for quantum operations", ICPS-27 (2004), Flagstaff, AZ.


Conference Papers


Jun Cheng, Xiaodong Xu, and D. G. Steel, A. S. Bracker and D. Gammon, L. J.


### Technical Summary of the Progress

Most of the progress in this program has been summarized in the annual reports we have submitted. In this Final Report, we summarize the major achievements of the program, providing illustrative data where appropriate. Note that the funding level in this program was primarily to support one graduate student and purchase equipment. The remaining support for the work comes from ARO, NSA (formerly ARDA), AFOSR, NSF.

### Technical Objectives

The objective of this program is to work in collaboration with the group at NRL directed by Dan Gammon to develop spin based quantum dots for optically driven quantum information processing. Our approach is based on using quantum dots fabricated in MBE grown III-V based materials. Our initial experiments are based on the dots produced by controlled interface fluctuations. However, long-term architectures are based on patterned self-assembled structures. Ultimately, we are working to demonstrate quantum entanglement and gate operations involving 3 distinct quantum dots that are located near each other which will demonstrate full scalability.

### Technical Approach

The quantum bit in this approach is the electron spin in a doped quantum dot and our approach is to coherently control the state of the single electron spin via a stimulated Raman transition involving the trion (electron-exciton). The exciton transition represents the first optical step in a two step optical process necessary to coherently control the state of qubit rotation and then ultimately to entangle two-spins in separate dots through a transient interaction between the dots.

The ideal quantum computing architecture we envision is a two dimensional array of quantum dots, each containing an electron. In its lowest orbital state, the two spin states of the electron form a qubit. The vertical dimension of a dot is about 2-3 nm and the lateral dimension of the dot in the plane of the dots is 10-30 nm in each direction. The interdot distance between two centers of the dots is about twice the lateral dot dimension. The spin-spin interaction between dots in the absence of laser radiation is negligible and any required interaction is induced by optical excitation of excitons which overlap two nearest neighbors. All electron spin rotations are controlled optically. A laser spot at the current level of optical technology covers about 10 dots. Within this optical field, we shape the pulse to control either single spin rotation or the conditional dynamics between two spins. Since each operation
involves only a small number of qubits and a quantum algorithm provides an exponential saving, then the overhead of the physical resources required by the pulse-shaping can be limited to preserve the exponential saving. Hence, with current MBE and III-V processing technology under development and by positioning optical fields and shaping pulses as required, we have the essence of a scalable quantum computer.

**Demonstration of an all optical quantum dot NOT-Gate**

Prior to the start of this program, we had demonstrated that the exciton spin represented by the optical Bloch vector was an excellent model for testing the viability for optical manipulation of quantum states in semiconductor quantum dots. We had demonstrated Rabi oscillations, quantum entanglement of the two exciton spins and coherent control over all four possible spin states of the two spin-state system.

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**Quantum State Tomography of an Optically Controlled Quantum Dot**

A key step along the way of building a quantum computer is to fully characterize the quantum state of a qubit. The means mapping out the 4 values for the corresponding density matrix.

Our first challenge was to develop an optical means to calibrate the system so that we could accurately determine the probabilities (diagonal terms) for occupation of the zero (ground) and one (excited) state of a single qubit system. We then applied the techniques developed in NMR to rotate the Bloch vector of the spin so that we could measure either the real or the imaginary parts of the off-diagonal density matrix terms on to the diagonal elements which we can then measure using our calibrated technique. The results are shown in Fig. 2 for a qubit exited by a π/2 pulse. The experimental results differ from the ideal results because of decay in the system. A complete calculation of the state and measurement include finite pulselength effects and measured decay rates (i.e., no adjustable parameters) shows complete agreement. The result is published in *Phys. Rev. Lett.* 2006.

![Figure 1](image1.png)

**Figure 1.** The figure shows the experimental demonstration of an optically controlled NOT-gate using two coupled exciton spins. The upper panel shows the schematic representation of the controlled NOT-gate where "a" is the control bit and "b" is the target bit. The middle panel shows the ideal truth table for the 4 different possible initial states of the system. The lower panel shows the experimentally determined truth table. All differences between the experimental and ideal truth table are fully accounted for by finite pulselength effects and state decay.

![Figure 2](image2.png)

**Figure 2.** Using the exciton spin vector as a model spin system in a semiconductor, we demonstrated that optical methods could be used to perform a complete determination of the quantum state of the system. The left panel shows the ideal values for the four terms of the density matrix for a
system initial excited by a $\pi/2$ pulse. The right panel shows the experimentally determined values. A complete calculation of the system including the effects of measured decay and decoherence rates and finite pulsewidth effects gives a diagram identical to the panel on the right, demonstrating that we have complete knowledge of this system.

**Optically Induced and Detected Electronic Spin Coherence in a Quantum Dot: Discovery of Spontaneously Generated Coherence**

Adding a single electron to the quantum dot enables us to move from using the exciton spin as the qubit to optically controlling the quantum state of individual electron spins. The clear motivation for this is that exciton spin coherence times are limited by recombination (<1 nsec) while electron spin coherence times are now expected to be longer than a microsecond. We note that this also changes the electronic structure of the system to a system generally characterized as a 3-level lambda system of the type also important for electromagnetic induced transparency (EIT).

Figure 3 shows the first demonstration of optically induced and detected electronic spin coherence using the doped quantum dots produced by our collaborator Dan Gammon at NRL. The electron spin states are controlled optically by using impulsive stimulated Raman excitation, where the trion (charged exciton) serves as the resonant intermediate state. In the usual pump/probe configuration, Fig.3 (upper panel) shows the quantum beats of a single spin and ensemble. The measurements show a dephasing time limited by inhomogeneous broadening ($T_2^*$) of order 10 nsec.

An unexpected result is shown in the lower panel of Fig. 3. The theory for impulsive Raman in this 3-level lambda system has been established for many years. It has been well known that neither the phase of the oscillations or the amplitude depend on the Zeeman splitting. However, contrary to this expectation, we clearly see that both parameters depend on the splitting. A complete theory for this system worked out by our theory collaborators, Lu Sham and his group at UC-SD, shows that in this system, symmetry breaking destroys the distinctness of the spontaneous emission decay from the trion state to the two spin states as long as the spin splitting is small compared to the natural radiative line width. In this case, the trion state can radiatively decay to both spin states with identical optical polarization, giving rise to spin coherence. This is forbidden in typical atomic systems because parity is a good quantum number. The solid lines are the theoretical predictions which are in good agreement. The results were published in *Phys. Rev. Lett.* (2005).
simultaneously with identical polarization to either of the two spin states.

**Demonstration of Optical Electron Spin Initialization and Control**

Initialization and coherent control of the spin state is an essential step towards quantum computing and are part of the DiVincenzo criteria for establishing a viable quantum computer. In this program, we have successfully demonstrated these essential features for the electron spin qubit in a charged quantum dot.

**Measurement of Spin Relaxation Time**

Ultrahigh resolution spectral hole burning measurements (data not shown) revealed various relaxation channels present in both the trion relaxation as well as the spin relaxation. The measurements showed a spin decoherence time in agreement with the coherent transient data (not shown) with the decoherence dominated by various aspects of inhomogeneous broadening. Interestingly, the relationship \( T_2 = 2T_1 \), held only at zero magnetic field. \( T_2 = T_2^* \) increased with increasing magnetic field, while the state relaxation rate, \( T_1 \), remained constant, independent of magnetic field. This suggested the measured state relaxation rate was not the slowest rate in the system, but rather was associated with a scattering rate leading possibly to spectral diffusion. This coupled with the fact that the measured rate was much faster than expected from theory for spin flip relaxation suggested there was a much longer relaxation process still to be observed. However, strong scattering by the sample lead to strong overwhelming noise in the megahertz region of the data, prohibiting higher resolution data by this means.

To obtain measurements in this frequency range, we developed a new kind of high resolution coherent spectroscopy based on amplitude modulation induced phase shifts. Details will be presented in a manuscript which is in preparation. However, the basic idea is that measurements are made using differential transmission using two cw optical fields (a
pump and a probe). The pump field is amplitude modulated, as usual. However, the pump modulation frequency is changed and the phase of the coherent nonlinear optical response is then measured using phase sensitive detection.

![Figure 5](image-url)

Figure 5. Measurement of the spin relaxation based on a new kind of coherent nonlinear optical spectroscopy (see text for discussion). In this approach, (upper panel) the cw pump field is amplitude modulated and the phase of the signal field is measured as a function of amplitude modulation frequency. Lower panel. The measured spin relaxation rate varies as the magnetic field to the fourth power as predicted in this field regime due to state mixing.

The upper panel of Fig. 5 shows the tangent of the angle as a function of pump modulation frequency. Using the density matrix equations and our model for the nonlinear optical response, we have extracted the relaxation rate (the phase determined by modulation frequency relative to the relaxation rate) as a function of magnetic field shown in the lower panel of Fig. 5. The solid curve varies as the magnetic field to the forth power, a result consistent with the theory of Khaetskii and Nazarov [PRB 64, 125316 (2001)]. The spin relaxation rate at zero-magnetic field was determined to be 27 μsec. This is the first measurement of the spin relaxation rate in the large area fluctuation dots, and when scaled for dot size, is in good agreement with the relaxation rate measured in the much smaller self-assembled quantum dot. Physically, the relaxation mechanism in this field and temperature region is dominated by state mixing of the spin states.

**Conclusion**

In summary considerable progress was made during this research period on development of methods for optical control of qubits in semiconductor quantum dots. The measurements also included a number of fundamental physics measurements of intrinsic phenomena on these systems. The support enabled a number of critical publications in this area as well as support of students working towards their doctoral degree.