

# Kronecker-FFT Algorithms for Multidimensional SAR PSF Processing

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## **Work Areas:**

Embedded Computing for Global Sensors and Information Dominance

Algorithm Mapping to High Performance Architectures

Reconfigurable Computing for Embedded Systems

## **Abstract**

This work presents new variants of FFT algorithms (not necessarily power of two lengths), in a computational Kronecker-core array algebra setting, tailored to the efficient point spread function (PSF) processing in multidimensional synthetic aperture radar (SAR) systems. The tailoring of the algorithms is performed through a targeted study of group theoretic properties of input/output data indexing sets and associated groups of stride permutations. The advantage of these new FFT variants over conventional formulations is that additive group theoretic properties of multidimensional input/output indexing sets are used for their mathematical formulations, establishing mapping identifications between computing structures and mathematical expressions identified as factored compositions of functional primitives, reducing in this manner their computational complexity and improving their implementation performance.

There exist many formulations of fast algorithms for computing the multidimensional discrete Fourier transform (DFT). In this work, computational Kronecker-core array (CKA) algebra, a branch of finite dimensional multi-linear algebra, is used as a language to identify similarities and differences among various FFT algorithm variants as well as for the creation of new variants. Each multidimensional DFT computation is expressed in matrix form. The multidimensional DFT matrix, in turn, is decomposed into a set of factors, called functional primitives, which are individually identified with an underlying software/hardware computational constructs. It is in this identification process where the language of CKA algebra becomes instrumental. For a given hardware computational structure and multidimensional DFT matrix, there are many FFT algorithm variants which can map to this target machine. The language of CKA algebra aids the application developer in the mapping effort of identifying the more computational efficient FFT variants and thus reducing the computational effort.

This work is partially supported by NSF Grant 99-77071

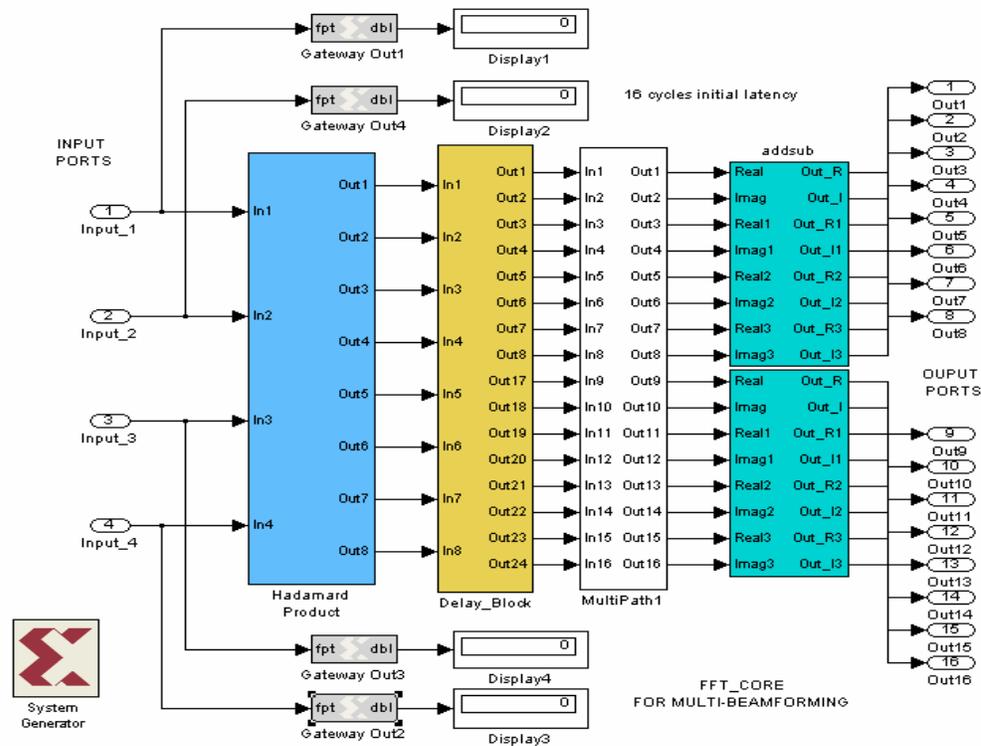
# Report Documentation Page

*Form Approved  
OMB No. 0704-0188*

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1. REPORT DATE <b>01 FEB 2005</b>	2. REPORT TYPE <b>N/A</b>	3. DATES COVERED <b>-</b>	
4. TITLE AND SUBTITLE <b>Kronecker-FFT Algorithms for Multidimensional SAR PSF Processing</b>		5a. CONTRACT NUMBER	
		5b. GRANT NUMBER	
		5c. PROGRAM ELEMENT NUMBER	
6. AUTHOR(S)		5d. PROJECT NUMBER	
		5e. TASK NUMBER	
		5f. WORK UNIT NUMBER	
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) <b>Research and Development Center of UPRM University of Puerto Rico at Mayaguez Road 108, Km. 1.0, B. Miradero Mayaguez PR 00680</b>		8. PERFORMING ORGANIZATION REPORT NUMBER	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)		10. SPONSOR/MONITOR'S ACRONYM(S)	
		11. SPONSOR/MONITOR'S REPORT NUMBER(S)	
12. DISTRIBUTION/AVAILABILITY STATEMENT <b>Approved for public release, distribution unlimited</b>			
13. SUPPLEMENTARY NOTES <b>See also ADM001742, HPEC-7 Volume 1, Proceedings of the Eighth Annual High Performance Embedded Computing (HPEC) Workshops, 28-30 September 2004. , The original document contains color images.</b>			
14. ABSTRACT			
15. SUBJECT TERMS			
16. SECURITY CLASSIFICATION OF:			17. LIMITATION OF ABSTRACT
a. REPORT <b>unclassified</b>	b. ABSTRACT <b>unclassified</b>	c. THIS PAGE <b>unclassified</b>	<b>UU</b>
			18. NUMBER OF PAGES <b>2</b>
			19a. NAME OF RESPONSIBLE PERSON

The FFT computing methods presented are currently being placed in a Weyl-Heisenberg computational framework setting for the study of real-time adaptive computation of linear arrays of cross-ambiguity functions, formulated as point surface response functions for coded and/or linearly FM modulated, time-frequency collocated, synthetic aperture radar (SAR) transmitted signals and received signals for applications in signal detection, information extraction, and clutters and jammers suppression operations. The **Figure One** below depicts a basic FFT-core functional primitive developed in MATLAB's Simulink for multi-FPGA implementation of multidimensional FFTs.



**Figure One: Basic Core-FFT Simulation**

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This work is partially supported by NSF Grant 99-77071