CHARACTERIZATION OF ULTRA WIDEBAND MULTIPLE ACCESS PERFORMANCE USING TIME HOPPED-BIORTHOGONAL PULSE POSITION MODULATION

THESIS
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THESIS

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To paraphrase one of my heroes, I feel Neil Armstrong would sum it up by saying “This is one small step for eight enlisted, one giant leap for the enlisted force.”

Donald J. Clabaugh
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Abstract

The FCC’s release of its UWB First Report and Order in April 2002 spawned renewed interest in impulse signaling research. This work combines Time Hopped (TH) multiple access coding with 4-ary UWB biorthogonal Pulse Position Modulation (TH-BPPM). Multiple access performance is evaluated in a multipath environment for both synchronous and asynchronous networks. Fast time hopping is implemented by replicating and hopping each TH-BPPM symbol $N_H$ times. Bit error expressions are derived for biorthogonal TH-BPPM signaling and results compared with previous orthogonal TH-PPM work. Without fast time hopping ($N_H = 1$), the biorthogonal TH-BPPM technique provided gains equivalent to Gray-coded QPSK; improved BER at a given $E_b/N_0$ and an effective doubling of the data rate. A synchronized network containing up to $N_T = 15$ transmitters yields an average BER improvement (relative to an asynchronous network) of approximately $-6.30$ dB with orthogonal TH-PPM and approximately $-5.9$ dB with biorthogonal TH-BPPM. Simulation results indicate that doubling the number of multipath replications ($N_{MP}$) reduces BER by approximately $3.6$ dB. Network performance degrades as $N_T$ and $N_{MP}$ increase and synchronized network advantages apparent in the $N_{MP} = 0$ case diminish with multipath interference present. Fast time hopping ($N_H > 1$) improves BER performance whenever $N_{MP} < N_H$ while reducing effective data rate by $1/N_H$. Compared to the $N_H = 1$ synchronized network, TH-BPPM modulation using $N_H = 10$ provides approximately $-5.9$ dB improvement at $N_{MP} = 0$ and approximately $-3.6$ dB improvement at $N_{MP} = 5$. At $N_{MP} = 10$, the BER for the hopped and $N_H = 1$ cases are not statistically different; with $N_H = 10$ hops, BER improvement varies from approximately $-0.57$ to $0.14$ dB (minimal variation between synchronous and asynchronous network performance).
CHARACTERIZATION OF ULTRA WIDEBAND MULTIPLE ACCESS PERFORMANCE USING TIME HOPPED-BIORTHOGONAL PULSE POSITION MODULATION

I. Introduction

1.1 Ultrawideband-An old technology with a new twist

Although Ultrawideband (UWB) technology was first introduced in the mid-1960s, it wasn’t until the digital age of the late 1980s and 1990s that realistic implementation was possible. UWB gained a great deal of attention over the last decade as civilian and military research communities developed applications for the technology. Recent approval by the Federal Communications Commission (FCC) [1] opened the doorway to fielding particular applications. The UWB signal structure makes it well-suited for use in communications, vehicular radar, and ground penetrating radar. It has also gained a considerable following among the special operations and radar communities because of its low probability of intercept and detection, multipath immunity, high data throughput, and precision ranging and localization.

Prior to the FCC’s release of its First Report and Order [1], UWB communication systems research focused on two dominant modulation schemes, direct sequence-binary phase shift key (DS-BPSK) and time hopped-pulse position modulation (TH-PPM). This was due mainly to the limited market and FCC restrictions. Though introduced as a hybrid modulation scheme [2], very little research has been conducted on m-ary systems and even less on biorthogonal signaling. This work extends the body of knowledge in both these areas.
1.2 Beneficial Characteristics

The spectral characteristics inherent to a nanosecond burst (UWB pulse) are of keen interest to military researchers studying radar fading, radar cross section (RCS), and low probability of intercept/detection.

Narrowband detection of UWB signal fluctuates slowly without multiple peaks or deep nulls. Rapid multiple fades and radar scintillation typical of narrowband communication and radar systems are largely mitigated with UWB since the multiple lobes are effectively eliminated. Tracking multiple responses and applying rake processing is easier with UWB modulation due to reduced scintillation and fluctuation rates. For example, most synthetic aperture radar (SAR) images, contain speckle. Speckle is an interference pattern caused by multiple time shifted waves that are incoherently detected. UWB SAR images contain no speckle because the sum of single-cycle waveforms sliding in time with respect to one another never sum destructively to create multiple nulls or constructively to create peaks, unless they are exactly aligned [3].

For the RCS engineer, the multi-gigahertz frequency spectrum of UWB radars is advantageous when used to identify scattering mechanisms; the ratio of object physical size to electrical wavelength governs object scattering characteristics and return signal strength is typically proportional to the frequency. When the electrical wavelength is large compared to the object’s physical dimensions, the target’s RCS is determined more by the scatterer’s volume than by its shape; when the wavelength is small with respect to the target, i.e., the optical scattering region, target shape influences the RCS the greatest. In the resonant scattering region, the wavelength is comparable to the target dimensions [4]. These regions are important for radar and communications because as frequency decreases, scattering lobes become broader and objects scatter less or stop scattering. For the radar, this phenomenon reduces clutter. With respect to communication systems, this phenomenon reduces the den-
sity of multipath reflections and multipath variance due to the broader scattering
lobes [3].

The UWB transmission system’s large bandwidth is fundamentally a function of the generated pulse shape and duration. The system bandwidth relative to the information bandwidth allows UWB systems to operate with a low power spectral density. A low power spectral density would seem to indicate an inherent covertness of UWB given that the UWB signal may be near or below the noise floor of a hostile detection device [5]. Thus, UWB is highly useful for military applications requiring covert communication in hostile environments while the wide spectrum makes it relatively insensitive to intentional jamming. These characteristics alone warrant investigation of UWB as a next generation communication system for America’s warfighters.

1.3 Applications of UWB Technology

The Defense Advanced Research Projects Agency (DARPA) and the Office of the Secretary of Defense (OSD) funded a study panel to examine the potential performance benefits and limitations of UWB technology. DARPA contracted with Batelle to evaluate the use of UWB in radar, communications, electronic warfare, and radio frequency weaponization. The results [6] were published in 1990 and many of the findings drove research over the last decade. Although the panel recommended against Department of Defense (DoD) investment in certain applications, research continued. The 2002 release of [1] provided additional direction while providing a market for previously developed UWB applications. Commercial developers who were previously reluctant to invest in UWB research and hardware, quickly moved into the UWB fray. The following subsections are a small subset of applications that have garnered interest in the UWB community.
1.3.1 Vehicular Radar. Application of UWB in vehicular radar focuses primarily on collision detection and avoidance. The radar is used to trigger visual alerts to aid the driver and could also be used as another sensor input for airbag restraint and deployment. With the resolution provided by the higher frequencies, application engineers are even looking into distinguishing cars, people, animals, or poles on or near roadways. UWB radar has the capability to sense road conditions (e.g., potholes, dips, bumps, gravel vs. pavement) which in turn can be used to dynamically adjust suspension, braking, and other drive systems.

The Multispectral Corporation demonstrated the use of a C-band UWB backup sensor to detect human and vehicle targets, though not in the prescribed FCC vehicular radar band. Human and pickup truck targets were identified at ranges of 1-50 feet, and 1-200 feet, respectively, at extremely low false alarm rates.

1.3.2 Ground/Wall Penetration. Urban warfare and hardened underground bunkers are critical areas of concern for the DoD and the special operations community in particular. Creating a picture of the combatant’s environment is paramount to gaining an advantage over ones enemy. UWB techniques may provide the needed enhancements for tomorrow’s counterinsurgency operatives. UWB exploitation is not limited to military demands; geophysical surveying and subsurface mapping in mining, agriculture, highway and building construction, archeology, and ice field surveying are one of three development areas allowed by [1].

The penetration depth into a lossy material/media is proportional to wavelength, the longer the wavelength the deeper the penetration. Therefore, the lower frequency content of UWB transmissions would have greater penetration abilities to detect deeply buried bunkers. Similarly, radar detection or communication through walls and floors requires lower frequencies for optimal operation. Measurements show that attenuation through a concrete wall is roughly $10f_o dB/m$, where $f_o$ is the operating frequency in GHz [7]. Thus to penetrate, the lowest possible frequen-
cies are needed, but high resolution is required to resolve multipath reflections or image objects. Therefore, the optimum device to communicate or image through a concrete wall is one that operates at the lowest possible frequency, yet provides the best resolution at those low frequencies. This is one of the principal characteristics of the UWB waveform-ultrawide relative bandwidth [3].

1.3.3 Target Imaging and Discrimination. Since time and frequency resolution are inversely proportional, wider bandwidth produces finer time resolution. UWB waveforms provide optimal resolution at the lowest possible frequency and when combined with the other waveform characteristics, mitigate multipath by both resolving it and reducing it. Once resolved, RAKE processing is applied to UWB communication signals to mitigate multipath by phase correction and coherent addition to form the final received signal. This discrimination methodology gives UWB systems spatial diversity that can add reliability and reduce the power required to support a desired range and data rate [3].

1.3.4 Secure Communication. UWB signals can also provide secure communications. This is an important benefit that can be exploited for covert operations or preventing theft of service. As stated earlier, UWB devices produce LPI/LPD signals. Visually a signal’s detectability comes from how “spiked” it appears to the instrument used to interrogate it. That is, signals are hard to detect if they have low peak-to-average ratios in the domain of the interrogating instrument. For instance, UWB signals that are properly modulated appear smooth in the frequency domain and are therefore hard to detect on a spectrum analyzer [3]. From an implementation standpoint, UWB system are favored as well since they can be implemented without a modulating carrier thereby simplifying the transmitter and receiver design.

One of the most recent applications of UWB communications technology is to the development of highly mobile, multi-node, ad hoc wireless communications networks for the DoD. One tested system provided a secure, low probability of inter-
cept and detection, UWB ad hoc wireless network capability to support encrypted voice/data (up to 128 kb/s) and high-speed video (1.544 Mb/s) T1 transmissions [8].

1.3.5 **High Capacity Networks.** The UWB bandwidth generates substantial interest in communications and networking arenas since it has been shown that UWB can transfer data at ranges up to 30 feet and at throughput ranging from 100 to 500Mbps [9]. Industry experts expect to field intra-room wireless systems within the next two years.

With the high processing gain of a UWB system comes an implied large code space. A large code space allows for many low cross correlation codes as discussed in Section 2.3. The large number of good codes enables high connectivity, both in terms of simultaneous users and the pool of unique addresses. UWB systems can have orders of magnitude more simultaneous users in a cell, with the same data rate and multi-user interference level, when compared to a conventional spread spectrum system [3]. Simply stated, a UWB system is capable of supporting more users in a faster network.

1.4 **Problem Statement and Scope**

The increasing demand for portable, high data rate communications has focused much attention on wireless technology. Ultra Wideband (UWB) waveforms have the ability to deliver megabits of information while maintaining low average power consumption. In accordance with the April 2002 FCC First Report and Order, UWB systems are now allowed to operate in the unlicensed spectrum of 3.1 to 10.6 GHz [10]. The order has motivated renewed interest in the forty-year-old concept of impulse signaling as applied to the three categories of approved UWB devices: 1) imaging systems including Ground Penetrating Radars (GPRs), through-wall, surveillance, and medical imaging devices, 2) vehicular radar systems, and 3) communications and measurement systems.
Gaussian monocycles are a class of UWB waveforms offering large bandwidths and enabling multiple access (MA) capability through “spreading” techniques. Although both Time Hopping (TH) and Direct Sequence (DS) MA modulation techniques are available, only time hopping is considered in this research to provide a UWB MA capability.

This work extends previous UWB multiple access (MA) performance characterization by combining Gold coded, Time Hopped Pulse Position Modulation (TH-PPM) with 4-Ary biorthogonal communication signaling, referred to here as TH-BPPM MA signaling. It also evaluates communication performance using a “fast hopping” modulation technique using 1, 2, and 10 hops per symbol. Matlab® is used to simulate probability of bit error ($P_b^H$) under multiple access interference (MAI) and multipath interference (MPI) conditions for both synchronous and asynchronous networks containing up to 15 transmitters.

1.5 Methodology

Matlab® was used to simulated end-to-end UWB network communication performance. The network consisted of 1-15 transmitters, 1-15 direct signals and 40 multipath replications per transmitter, and a correlation receiver for the signal of interest. UWB symbol generation, transmission, detection and estimation were entirely software driven to permit control and variation of key parameters. The model is validated using theoretical models for antipodal and orthogonal signaling and subsequently extended to include simulated network performance with multipath, multiple access, and “spread spectrum” fast hopping schemes.

1.6 Equipment

Matlab® Versions 6.1.0.450 (Release 12.1) and 6.5.0.180913a (Release 13) were used for algorithm development and execution. The Matlab® programs resided on multiple personal computers; the typical configuration was a Dell Personal Computer
with an Intel® Pentium® 4 processor operating at 2.53 Gigahertz, 1.047 Gigabytes of random access memory, and Microsoft Windows 2000, (Service Pack 4) operating system.

1.7 Thesis Organization

This document is organized into five chapters. Chapter 1 introduces (UWB) communication concepts and lays out the structure of the thesis document. Chapter 2 provides UWB background information based on relevant literature and previously research efforts. Chapter 3 details the research methodology. Chapter 4 presents the model validation and simulated network performance results. Chapter 5 provides conclusions and potential research topics related to this thesis. The appendices contain the algorithm code and additional simulation results.
II. Background

2.1 History

Several terms have been used over time to reference UWB waveforms. Nonsinusoidal, base-band [11], impulse radio, and carrier free signals are just a few of the terms used in literature to describe UWB signals. The term “UWB” was not adopted until about 1989. Dr. Gerald F. Ross first demonstrated the feasibility of utilizing UWB waveforms for radar and communications applications in the late 1960s and early 1970s [11]. The key to actual realization of a physical system came with the development of the avalanche transistor and tunnel diode. Initially, a nanosecond rise time pulse could be generated but there wasn’t any test equipment with a fast enough response to actually capture the signal. This changed as sampling oscilloscopes entered the market to further aid system development. Throughout the 1970s, UWB research focused on enhanced resolution for radar systems which demanded wider bandwidth. Research was not limited to American scientists; Russian researchers Astanin, Kosylev, Fedotov, and Immoreev published detailed analysis of UWB in a multitude of applications. One of the principal American figures over the last decade has been Lieutenant Colonel (retired) James D. Taylor. Taylor was chief of Advanced Technology Planning at the Air Force Electronic Systems Division, when he organized the first American UWB radar symposium, promoted early research work on defense applications, and authored “Introduction to Ultra-wideband Radar Systems” (1995) [12] for CRC Press.

During the last decade, the military has begun to support initiatives for developing commercial applications. These commercial applications, and the evolution of increasingly faster digital circuits, have led to the development of inexpensive hardware. Additionally, the ability to produce low cost units and unlicensed use have recently boosted interest in UWB.
The FCC has been extremely cautious in allowing the use of UWB systems due to possible signal interference issues. Figure 2.1 shows the broad spectral region available to UWB transmissions and highlights the overlap with operational systems and standards.

The multitude of potentially affected systems has slowed Government approval to ensure that UWB devices do not negatively interfere with currently fielded electronic devices. In April 2002 the FCC published the First Report and Order [1] guiding UWB development and subsequent system approval. The order established different technical standards and operating restrictions for four types of UWB devices based on their potential to cause interference. These UWB devices were categorized as:
Table 2.1: FCC EIRP Emission Limits (dBm)

<table>
<thead>
<tr>
<th>Frequency (MHz)</th>
<th>Low Freq</th>
<th>Medium Freq</th>
<th>High Freq</th>
<th>Indoor Freq</th>
<th>Vehicle Radar Freq</th>
<th>Hand Held Freq</th>
</tr>
</thead>
<tbody>
<tr>
<td>Below 960</td>
<td>-</td>
<td>15.209 Limits</td>
<td>15.209 Limits</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>960-1610</td>
<td>-65.3</td>
<td>-53.3</td>
<td>-65.3</td>
<td>-75.3</td>
<td>-75.3</td>
<td>-75.3</td>
</tr>
<tr>
<td>1610-1690</td>
<td>-53.3</td>
<td>-51.3</td>
<td>-53.3</td>
<td>-53.3</td>
<td>-61.3</td>
<td>-63.3</td>
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<tr>
<td>1990-3100</td>
<td>-51.3</td>
<td>-41.3</td>
<td>-51.3</td>
<td>-51.3</td>
<td>-61.3</td>
<td>-61.3</td>
</tr>
<tr>
<td>3100-10600</td>
<td>-51.3</td>
<td>-41.3</td>
<td>-41.3</td>
<td>-41.3</td>
<td>-61.3</td>
<td>-41.3</td>
</tr>
<tr>
<td>10600-22000</td>
<td>-51.3</td>
<td>-51.3</td>
<td>-51.3</td>
<td>-51.3</td>
<td>-61.3</td>
<td>-61.3</td>
</tr>
<tr>
<td>22000-29000</td>
<td>-51.3</td>
<td>-51.3</td>
<td>-51.3</td>
<td>-51.3</td>
<td>-41.3</td>
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<td>29000-31000</td>
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<td>-51.3</td>
<td>-51.3</td>
<td>-61.3</td>
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<tr>
<td>Above 310000</td>
<td>-51.3</td>
<td>-51.3</td>
<td>-51.3</td>
<td>-51.3</td>
<td>-61.3</td>
<td>-61.3</td>
</tr>
</tbody>
</table>

1. Imaging Systems (Ground Penetrating Radars, through-wall, surveillance, and medical imaging devices)

2. Vehicular Radar Systems

3. Indoor UWB Systems

4. Hand Held Devices

The FCC adopted unwanted emission limits for UWB devices that are significantly more stringent than those imposed on other devices. The First Report and Order also contained emissions masks limiting the frequency band within which certain UWB products would be permitted to operate. The frequency band of operation is based on the 10 dB bandwidth of the UWB emission as shown in Fig. 2.2. Table 2.1 outlines the Effective Isotropic Radiated Power (EIRP) by frequency band for different systems. Figure 2.3 graphically illustrates the mask imposed on indoor and outdoor (hand held) UWB systems. The combination of technical standards and operational restrictions were established to promote development and to ensure that UWB devices could coexist with authorized radio services without the risk of harmful interference while gaining experience with this new technology [1].
Figure 2.2: UWB Fractional Bandwidth

Figure 2.3: Indoor and Outdoor (Hand Held) UWB Frequency Mask Imposed by FCC
2.2 UWB Waveform Modeling and Phenomenology

2.2.1 UWB Signals Defined. Analysis of UWB signals begins with a detailed characterization of the waveform and its spectrum. Signals are categorized into three main classes, narrowband (NB), wideband (WB), and ultrawideband (UWB) based on fractional bandwidths of less than 1.0, 1.0 to 25.0, and greater than 25%, respectively. Fractional bandwidth \( B_f \) is defined as [10]

\[
B_f = 2 \left( \frac{f_H - f_L}{f_H + f_L} \right)
\]  

(2.1)

where \( f_H \) and \( f_L \) are the upper and lower frequency emission points which are 10 dB below the peak responses as indicated in Fig. 2.2. The center frequency \( f_C \) of the transmission is defined as the average of the upper and lower 10 dB emission points, i.e., \( f_C = (f_H + f_L)/2 \). The low power and gigahertz (GHz) bandwidth are the characteristics currently being exploited by radar and communications engineers. The UWB signal effectively spreads energy over a large spectral region and has a low power spectral density (watts/hertz); such waveforms are commonly used for low probability of intercept or detection applications. Thus, UWB signaling is highly useful for military applications requiring covert communication in hostile environments.

2.2.2 The Gaussian Monopulse. Figure 2.4 depicts the time domain and frequency domain representations of a UWB Gaussian monopulse, a commonly modeled output of a UWB transmitter. In many practical applications, an individual data bit is comprised of multiple Gaussian monopulses. The spectrum generated by a uniformly spaced pulse train of Gaussian monopulses can wreak havoc in a multiple access environment. The pulse train creates multiple spectral lines that could lead to massive destructive collisions whenever several pulses from two signals are received simultaneously. The line spectra can be “smeared” by randomly shifting the pulses in time through dithering or time hopping. Figure 2.5 shows the effects of uniform
Figure 2.4: Temporal (left-hand plots) and spectral (right-hand plots) characteristics of Gaussian monopulse (top), uniformly spaced pulse train (middle), and fast time hopped pulse train (bottom).

spacing and fast time hopping on the spectral envelope. The changes in smoothness from the monopulse to the uniform pulse train, and the smoothing effects of the fast time hopped pulse train are apparent. The shape of the envelopes remains relatively constant though the instantaneous values differ significantly, especially in the case of the uniform pulses.

Figure 2.4 graphically shows temporal and spectral characteristics of a single monopulse, a uniformly spaced pulse train of Gaussian monopulses, and a fast time hopped pulse train of Gaussian monopulses. The uniform pulse train’s narrow line
2.2.3 Transmitted Waveform. The second derivative of a Gaussian monopulse is modeled as the received UWB pulse to maintain consistency with [2]. Accounting for wave shaping effects of the transmit and receive antennas, the second
derivative waveform is represented in the time domain by

\[ w(t) = \left[ 1 - 4\pi \left( \frac{t}{\tau_m} \right)^2 \right] \exp \left[ -2\pi \left( \frac{t}{\tau_m} \right)^2 \right] \]  

(2.2)

where the impulse width parameter \( \tau_m \) is approximately equal to 0.4 times the pulse width \( T_w \). Basic UWB Pulse Position Modulation (PPM) can be achieved with

\[ s_i(t) = w[t - (-1)^{a_i} \cdot \Delta] \]  

(2.3)

where \( i \) is the symbol number, \( a_i \) is the binary input data qualifying 1 or 0, and \( \Delta \) is the relative PPM offset. The resulting binary PPM waveforms of (2.3) with \( T_w = 0.2 \text{ nsec} \) (5 GHz operation) are shown in Fig. 2.6.

\[ \text{Figure 2.6: Binary Pulse Position Modulation Offset} \]

2.2.4 Symbol Generation. Biorthogonal signals, as defined in [13], are two sets of orthogonal signals such that each symbol in one set has an antipodal
symbol in the other set. Biorthogonal PPM (BPPM) is achieved by combining binary PPM with antipodal signaling. The resultant communication symbols using the fundamental UWB waveform of (2.2) are shown in Fig. 2.7 and can be analytically represented by [14,15]

\[ s_i(t) = (-1)^{a_{2i}} \cdot w \left[ t - (-1)^{[a_{2i} \oplus a_{2i-1}]} \cdot \Delta \right] \]  

(2.4)

for \( t_i \leq t \leq t_i + T_s \) where \( i \) is the symbol number, \( a_{2i} \) and \( a_{2i-1} \) are the binary input data equaling 1 or 0, \( \oplus \) represents modulo-2 addition, \( T_s \) is the symbol duration, and \( \Delta \) is the relative PPM offset.

Figure 2.7: 4-ary Biorthogonal UWB Waveforms Generated from (2.2) and (2.4) Using Bit Patterns of \((a_{2i-1}, a_{2i})\) as Indicated [14]
2.2.5 Multiple Access via Time Hopping. Time hopping UWB modulated
signals in accordance with preassigned coding, such as that presented in Section 2.3,
is one common technique for providing multiple access (MA) capability [16]. In the
TH-BPPM technique, the signal information contained in both relative pulse posi-
tion and amplitude characteristics is preserved upon implementing MA capability.
This information can be reliably recovered using temporal “spreading”, i.e., repeat-
ing communication symbols across time, in a manner paralleling the fast frequency
hopping technique commonly used for spectral spreading. The 4-ary biorthogo-
nal modulated signals described by (2.4) are used in conjunction with preassigned,
uniquely coded time hopping sequences to implement MA capability. The analytic
representation for the biorthogonal TH-BPPM MA technique follows directly from
the orthogonal TH-PPM MA technique commonly used in research [16,17], with the
$k^{th}$ user’s signal is given by

$$s^{(k)}(t) = \sqrt{P_k} \sum_{i=1}^{\infty} \sum_{j=(i-1)N_H}^{iN_H-1} s_i \left[ t - jT_o - c_j^{(k)}T_c \right]$$  (2.5)

where $P_k$ is the average power, $N_H$ is the number of hops per communication symbol,
$T_c$ is the chip interval (the time allotted for one M-ary symbol), $T_o$ is the symbol
repeat interval, $\{c_j\}$ is the chip offset sequence with period $N_c$, with $\{c_j\}$ equal to
$\{c_0, c_1, ..., c_{N_c-1}\}$, and $c_j \in \{1, 2, 3, ..., N_c\}$.

Each communication symbol of (2.4) repeats $N_H$ times and occurs once within
each $T_o$ at a position dictated by $c_j$ as shown in Fig. 2.8. As indicated in (2.5),
sequential $c_j$ values are used for the $N_H$ repetitions of the original symbols, i.e., $c_j$
values are not constant over $N_H$ repetitions; every symbol is offset by a sequential
$c_j$. 

2-10
2.3 Multiple Access Code Generation and Selection

Multiple access capability can be achieved for all $N_H \geq 1$ where a processing gain of $N_H$ is realized. In this case, signal discrimination for the $k^{th}$ user is obtained by applying chip offsets $c_j^{(k)}$ derived from pseudorandom sequences. For consistency with previous work [17], 31 length Gold codes are used to generate chip offset sequences. Gold coding is a reasonable choice given the large number of available codes and the well-defined periodic cross-correlation ($R_{XY}$) characteristics [18]. The coding provides the added benefit of time hopping the transmitted waveforms thereby mitigating the line spectra issues discussed in Section 2.2.2.

Carefully chosen pairs of maximal length sequences (m-sequences) can be used to generate a family of Gold code sequences. One key characteristic of Gold codes
is the cross correlation of any two codes in the family produces is three valued, which allows the receiver to distinguish the signal of interest in a multiple access environment. The three Gold code cross-correlation values are easily calculated using [19]

\[ R_{XY} \in \left\{ 1, \frac{-\beta(n)}{N}, \frac{\beta(n) - 2}{N} \right\} \]

where \( \beta(n) = 1 + 2^{\frac{n+2}{2}} \), \( N \) is equal to the code length, \( n = \log_2(N+1) \), and \( \lfloor a \rfloor \) denotes the greatest integer less than \( a \). Typical normalized Gold code autocorrelation and cross correlation responses are illustrated in Fig. 2.9.

![Typical Normalized autocorrelation (top) and cross correlation (bottom) responses for a Gold code (31-length Illustrated)](image)

Figure 2.9: Typical Normalized autocorrelation (top) and cross correlation (bottom) responses for a Gold code (31-length Illustrated)

Figure 2.10 demonstrates a mechanism for deriving chip offset sequences from Gold code sequences by mapping (binary-to-decimal conversion) Gold code elements to integer values using an \( r \)-element \((r = 5)\) wide sliding window and single code
element shifts. The choice of $r$ is significant because 1) it determines the maximum number of transmitters on any given network based on the number of unique codes available and 2) the number of offsets $2^r$ multiplied by the chip interval ($T_c$) sets the symbol repetition interval ($T_o$), all of which relate to data rate and network throughput. The $r$ should be maximized such that $2^r - 1$ equals the respective code length. Using a large $r$ maximizes the resulting code space and thereby minimizes possible collisions with multiple transmitters. For $l$-length Gold codes, the conversion process provides unique $l$-length user TH code set where $c_j \in [0, 1, ..., 2^r - 1]$ with periodicity $N_c = 2^r$ such that $c_j = c_{j+nN_c}$ for all $n$.

![Figure 2.10: Code Gold 31 Binary to Decimal Conversion](image)

2.4 Interference Factors

A communication system’s bit error performance is directly related to $E_b/N_o$ into the demodulator, where $E_b$ is the energy per bit and $N_o/2$ is the 2-sided noise spectral density. The $E_b/N_o$ is in turn directly related to the received signal’s signal-
to-noise ratio (SNR) by

\[
\frac{E_b}{N_0} = \frac{S T_s/k}{N 2/W} = \left( \frac{S}{N} \right) \frac{T_s}{k \Delta t/2} \tag{2.7}
\]

where \( T_s \) is the symbol duration, \( W = 1/\Delta t \) is the signal bandwidth, \( \Delta t \) is the sample spacing, and \( k \) is the number of bits per symbol (\( k = 2 \) for 4-ary modulation). Though \( E_b/N_0 \) provides an easy means for determining expected performance, the ratio of bit energy to noise power spectral density is not as easily visualized, or measured, as SNR. Given fixed transmitter strength, \( S \) can only decrease while propagating while total noise power \( N \) can be affected by numerous sources. In an extreme environment, transmitted signals are subject to a multitude of interferers including multiple transmitters (MA), multiple signal reflections (multipath), noise added in the transmission channel, and even intentional jammers. A simple model of received SNR \((SNR_r)\) can be viewed as

\[
SNR_r = \frac{Average \, Received \, Signal \, Power \, (S_r)}{Average \, Received \, Noise \, Power \, (N_r)} \\
\approx \frac{S_r}{MAI + MPI + AWGN + J} \tag{2.8}
\]

where \( MAI \) is the interference from multiple transmitters, \( MPI \) is multipath interference, \( AWGN \) is additive white Gaussian noise, and \( J \) is additional jammer interfering power.

Although UWB communication systems are a relatively new field of study, the body of work addressing channel modeling which takes into account each of the above effects is growing. In-depth studies on channel effects have been reported by [20–22]. A UWB receiver’s ability to resolve a large number of multipath sources has garnered interest. Numerous channel models have been examined for validating against fielded hardware. Rayleigh fading is commonly applied in communication path loss models but laboratory results of fielded systems show that log-normal may
be more appropriate for UWB systems [23]. Additionally, [21] proposes a Markov
($\Delta - K$) model to characterize arrival time of multipath signals which indicated
strong correlation between analytic and experimental results. A detailed examination
of multipath interference effects for indoor wireless channels can be found in [24].
In [25], researchers conducted a signal propagation experiment in a general office
environment to investigate multipath. They concluded rather succinctly that UWB
signaling does not suffer multipath fading.
III. Methodology

3.1 Problem Definition

The objective of this research is to develop an analytical model which accurately characterizes the expected communication performance of a UWB TH-BPPM transmission system. Fast time hopping is implemented to improve performance in a multiple access/multiuser interference environment (MAI). Additional interference in the form of Additive White Gaussian Noise (AWGN), and multipath (MPI), delayed versions of the original signals, for synchronous and asynchronous transmission modes complete the performance analysis. The model’s performance in a single user, zero multipath environment is validated against results reported in [2] and analytic equations for equivalent Gray-coded QPSK modulation.

A communication system’s bit error rate (a key performance metric) degrades in the presence of other interfering signals. Bit error rate is merely the ratio of bits received and estimated in error divided by the total number of transmitted bits. Each interference factor (AWGN, MAI, and MPI) are varied to determine the individual impact on system performance. Combined interference effects, culminating in a hostile environment comprised of all forms of interference, are then considered.

Signal-to-Noise ratio ($SNR$) is a common term to indicate the “strength” of a received signal. However, in digital communications, the available $E_b/N_o$ into a demodulator determines the receiver’s ability to properly estimate the received signal. The relationship between SNR and $E_b/N_o$ was shown in Section 2.4. Acceptable bit error performance is one design factor for the communication system design engineer. The results presented herein will allow direct comparison with previously published results of other UWB modulation schemes.
3.2 System Boundaries

Characterization of the UWB TH-BPPM system begins with the development of an analytical model using a Matlab® implementation scheme as outlined in Fig. 3.1. The UWB transmitter described by [2] is used as a baseline and modified for the 4-ary signal constellation and fast time hopping environment.

3.2.1 System Under Test. The system under test (SUT) consists of two active components, the UWB transmitter and UWB receiver, and a passive component, the transmission medium – free space. From a macro perspective, a pulse generator within the transmitter creates the desired UWB Gaussian waveform. The waveform passes into the modulator where, depending on the current $k$ data bits at the demodulator, it is converted to one of $M$ symbols using Pulse Position Modulation (PPM) and antipodal signaling. The waveform then enters the multiple access encoder which applies the Time Hopping (TH) code presented in Section 2.3 and Section 3.6.6.

To simulate real-world channel effects, MAI and MPI are added following MA signal generation [2]. AWGN is combined to establish a $SNR_r$ based upon the user defined $E_b/N_o$. As indicated above, multiple independent waveforms are generated and unique user codes are applied to provide MAI. MPI is inserted by randomly delaying superposed replicas copies of the desired signal, plus any MAI, waveform(s). Different realizations of AWGN are added to each of the waveforms and superposed to create the composite received waveform. Separate iterations are performed to assess performance in synchronous and asynchronous networks.

All despreading and demodulation is performed within the detection and estimation stage described in Section 3.7. For this research, the received signal of interest is assumed to be properly synchronized. All user codes and number of hops per symbol ($N_H$) are known a priori which allows the correlator to integrate over
one symbol interval \((T_S)\). The estimated data bits are compared bit-by-bit to the original input at the transmitter modulator to derive the bit error rate.

Figure 3.1: Simulation Flowchart
3.2.2 System Limitations. As with any simulation, real world effects cannot be fully implemented given the processing constraints. The following limitations were implemented to permit comparison with previously published data:

Channel Fading: No channel fading models, such as the Rayleigh, log-normal, or Markov-K were applied the generated waveforms. All multipath and direct signals contained equivalent signal strength contributions from the UWB pulses.

RAKE Receiver: It has been shown [20] that improved performance in a UWB environment can be achieved using a RAKE receiver. RAKE was not used in this study. The receiver is a four channel correlator/accumulator combination.

Pulse overlap: Symbol duration $T_S$ and PPM offset $\Delta$ were made sufficiently large enough to provide zero overlap of pulses within the set of four communication symbols. A relative PPM offset of $\Delta = T_s/4 = T_w/2 = 0.1 \text{ ns}$ was used (cf., Fig. 2.6) resulting in the 4-ary symbols (cf., Fig. 2.7).

Multipath: Multipath can be modeled multiple ways, i.e., a different delay could be applied to each pulse, to each message (comprised of $N_H$ pulses per symbol), or to each multipath link. The approach herein was to vary the multipath value message-to-message. Some studies have reported root mean square (RMS) delays of 25 to 50 nanoseconds. For comparison with [2], the value is set at 15.4 nanoseconds as reported in [24].

3.3 System Services

Effective communication is defined by the message received equalling the message transmitted. Put in simple terms, the ones and zeros (bits) out of a receiver should equal the ones and zeros into the transmission system and be in the same order. Unfortunately, degradation occurs in a wireless transmission when the original bits are converted to an analog form for propagation. The transmission through free space imparts losses and interference corrupts the electromagnetic waveform.
Thus a noisy, weaker signal is received by a less than perfect antenna for reconstruction by the receiver into a digital waveform. The ultimate service provided is data/message transfer and the “goodness” of the system is characterized by how often it reconstructs the signal correctly.

3.4 Performance Metrics

Data analysis consists of characterizing communication performance of the UWB TH-BPPM signal in various multiple access and multipath environments. The true figure of merit for any communication system is the probability of bit error ($P_b$) in a given transmission. The confidence and accuracy of the $P_b$ results can be quantified using network performance equations from [26] where the Confidence Interval (C.I.) is given by

$$C.I. = P_b \pm z_{(1-\alpha/2)} \cdot \sqrt{\frac{P_b \cdot (1-P_b)}{n}} \text{ for } n \cdot P_b \geq 10$$

(3.1)

where $P_b$ is equal to the number of bit errors divided by the total number of bits generated in the simulation ($n$), $\alpha$ is the significance level, and $z_{(1-\alpha/2)}$ is the $(1 - \alpha/2)$-quantile of a unit normal variant. The accuracy ($r$) is merely one-half the variance of the C.I. values and is given by

$$r = z_{(1-\alpha/2)} \cdot \sqrt{\frac{P_b \cdot (1-P_b)}{n}}$$

(3.2)

Simulation time can be significantly reduced by limiting the number of errors required to meet C.I. and accuracy requirements. Computer processor speeds allowed pilot simulations to accrue 300 errors before terminating. Subsequent simulations used the same 300 error minimum which assured the $n \cdot P_b \geq 10$ requirement of (3.1) was met. With 300 errors as a constant, the theoretical value of $n$ varied as a function of required $P_b$, i.e., a $10^{-6} = P_b = 300/n \Rightarrow n = 300 \cdot 10^6 \text{ bits}$. Therefore,
given the following parameters, the bounded C.I. accuracy can be calculated as

\[ P_b = 10^{-6} \]

**Bit errors** = 300

\[ n = 300 \cdot 10^6 \]

**C.I.** = 95%

\[ \alpha = 0.05 \]

\[ z_{(1-\frac{\alpha}{2})} = 1.96 \]

\[ r = 1.96 \cdot \sqrt{\frac{10^{-6} \cdot (1-10^{-6})}{300 \cdot 10^6}} \approx 1.13 \times 10^{-7} \]

**C.I.** = \( P_b \div r \)

**C.I.** \( \approx 10^{-6} \div 1.13 \times 10^{-7} \).

The \( r \) value only improves as \( P_b \) decreases; for \( P_b \) of \( 10^{-2} \) through \( 10^{-6} \), the accuracy improves from approximately \( 1.13 \times 10^{-3} \) to \( 1.13 \times 10^{-7} \). Though the accuracy may improve in terms of raw numbers, the percent error \( P_b/r \) remains nearly constant at approximately 10% for all results presented in Chapter 4.

### 3.5 Parameters

A communication system model is comprised of a multitude of possible parameters defining the particular system. Multiple access using a fast time hopping algorithm in a multipath environment provides the basis of this work. The basic waveform structure must remain constant to accurately compare performance levels. Table 3.1 identifies the principal parameters addressed in this research. Those with fixed values are associated with the basic waveform structure. The waveform structure is similar to that reported in [2]. In generating the waveform, pulse duration \( T \) and repetition interval \( T_o \) control the frequency range over which the system operates. For example, a pulse gated on every \( T_w = 0.2 \text{ nsec} \) is spectrally centered
at 5.0 GHz. Pulse duration must be closely controlled since the center frequency is inversely proportional. A small error in pulse width can move system operation outside the bandwidth of receiver filters. Chip time $T_c$ and the length of the Chip Offset Sequence $c_j$ control the Symbol Repeat Interval $T_o$. Therefore, $T_o$ is set to $N_c \times T_c$.

Table 3.1: Principal System Parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pulse duration</td>
<td>$T_w$</td>
<td>$0.2 \times 10^{-9}s$</td>
</tr>
<tr>
<td>Pulse width parameter</td>
<td>$\tau_m$</td>
<td>$0.4 \times T = 0.8 \times 10^{-10}s$</td>
</tr>
<tr>
<td>Pulse Repetition Interval (PRI)</td>
<td>$T_o$</td>
<td>$T_c \times 2^r = 12.8 \times 10^{-9}s$</td>
</tr>
<tr>
<td>A/D sampling resolution</td>
<td>$dt$</td>
<td>$8.0 \times 10^{-12}s$</td>
</tr>
<tr>
<td>Chip duration</td>
<td>$T_c$</td>
<td>$2 \times T = 0.4 \times 10^{-9}s$</td>
</tr>
<tr>
<td>PPM Offset</td>
<td>$\Delta$</td>
<td>$T_w/2 = 0.1 \times 10^{-9}s$</td>
</tr>
<tr>
<td>User Code</td>
<td>$c_j$</td>
<td>Defined in Section 3.6.6</td>
</tr>
<tr>
<td>Sliding window width</td>
<td>$r$</td>
<td>5</td>
</tr>
<tr>
<td>Number of multipath</td>
<td>$N_{MP}$</td>
<td>${0, 5, 10, 20, 40}$</td>
</tr>
<tr>
<td>Number of transmitters</td>
<td>$N_T$</td>
<td>${1, 2, 3, \ldots, 15}$</td>
</tr>
<tr>
<td>Number of hops per symbol</td>
<td>$N_H$</td>
<td>${1, 2, 10}$</td>
</tr>
<tr>
<td>Signal energy</td>
<td>$E_b/N_o$</td>
<td>Based on $N_H$ and required BER</td>
</tr>
<tr>
<td>Asynchronous Offset</td>
<td>$Async$</td>
<td>Random $[0 : T_c]$</td>
</tr>
</tbody>
</table>

Variations in the parameters of Table 3.1 dictate the achievable data rates. Although it has been shown that biorthogonal TH-BPPM effectively doubles the data rate relative to the orthogonal TH-PPM [14], the inclusion of fast time hopping into the algorithm offsets this advantage. The data rates $R_D$ for each $N_H$ can be calculated using

$$R_D = \frac{k}{N_H \times T_o} \quad (3.3)$$

where $k = log_2$(number of symbols$M$). For $N_H = 1, 2$ and $10$, the associated data rates are 156.25, 78.125 and 15.625 Mbps, respectively.
The simulation workload is directly influenced by the total number of pulses transmitted (i.e., bits generated), the SNR (which determines $E_b/N_o$), the number of system transmitters ($N_T$), the number of multipath replications ($N_{MP}$) and the number of time hops per symbol ($N_H$). The total number of bits generated is not a predetermined simulation parameter; simulations continue until a C.I. of 95% is achieved with $\pm 10\%$ accuracy, i.e., until 300 errors accrue for given factors. The number of bits generated is used in calculations but does not influence the model. As $E_b/N_o$ increases, the probability of a bit error decreases. This requires more iterations of the loops shown in Fig. 3.1 and increases system workload. The variations in system workload have no bearing on simulation outcomes.

3.6 Factors

For all simulations, the composite UWB signal is specified by a combination of signal power, multiple access, multipath, hops per communication symbol, network synchronization and user code.

3.6.1 Signal Power. The model is first validated against analytical results obtained from (3.5) over fixed average power $E_b/N_o$ levels 0 to $+10$ dB in increments of 1.0 dB. These values provide estimated performance levels typically found in communication networks and are sufficient to characterize the biorthogonal TH-BPPM system performance with varying levels of $N_H$. The effects of multiple transmitters and multipath levels are studied using a fixed $E_b/N_o$ that provides a $P_b^H$ of $10^{-3}$. This value is chosen to permit performance comparison with previously published results for orthogonal TH-PPM [27]. The $E_b/N_o$ required at the demodulator input to meet the $P_b^H = 10^{-3}$ specification is dependent on $N_H$ (processing gain). The $E_b/N_o$ values (vertical dashed lines in Fig. 3.2) used for $N_H = 1, 2$, and 10 were 6.789, 3.7792 and -3.2105 dB, respectively. For all simulation results, the received power of all undesired interfering multiple access signals is identical to the received power of the desired signal.
3.6.2 Multiple Access. Using the $E_b/N_o$ values established in Section 3.6.1, network communication performance is evaluated for $N_T$ equal 1 to 15 transmitters (one desired and up to 14 multiple access interferers). As the number of transmitters increases, more collisions occur and destructive interference increases, increasing the expected BER. Simulation results will quantify BER changes due to added transmitters.

3.6.3 Multipath. Multipath interference (MPI) effects are characterized using an RMS time delay of 15.4 $ns$ for each user’s replicated signal [20]. The multipath remains constant over $N_H$ pulses. In this manner, each message will observe the same realization of multipath. Data is generated at an $E_b/N_o$ levels
for each $N_H$ providing a BER of $10^{-3}$ as defined in Section 3.6.1 for five levels of multipath replication including $N_{MP} = 0, 5, 10, 20$ and $40$ multipath replications per user. The two scenarios considered include: 1) a single transmit/receive link ($N_T = 1$) and 2) a network containing up to $N_T = 15$ transmitters.

3.6.4 Network Synchronization. For the communication link being evaluated, the transmitter of interest and receiver are perfectly synchronized. All other MA network signals arrive at the receiver either synchronously or asynchronously relative to the link being evaluated. For the asynchronous TH-BPPM cases considered, all interfering direct path MA signals are randomly time offset (delayed) in the range of $[0 : T_c]$. The asynchronous value remains constant for all direct and multipath signals from a given transmitter for the duration of the simulation. New realizations of the asynchronous offset are applied for each trial.

3.6.5 Fast Time Hopping. A fast time hopping technique is implemented whereby each symbol is replicated $N_H$ times prior to coding and transmission. Fast time hopping effectively reduces the data rate by a factor of $N_H$. However, a processing gain of $N_H$ is realized and BER improves due to the coherent detection process described in Section 3.7. The processing gains associated with large $N_H$ values significantly impact simulation run time due to the number of symbols that would be generated to validate system performance. Therefore, $N_H = 1, 2, 10$ were used to generate varying workloads and represent low-level and high-level processing gains.

3.6.6 Code selection. System performance is highly dependent upon code choice since the success of the correlation receiver depends upon both the cross-correlation and auto-correlation characteristics of the codes used. In other words, the probability of bit error is affected by the number of signal collisions causing the receiver to incorrectly estimate a modulated signal. Since the various codes are used
to control pulse position and phase alignment, the choice of uniquely assigned user codes is a significant factor in MA and multipath communication performance.

Gold codes were chosen to implement multiple access coding to permit direct comparison with [2]. Gold codes are generated from 31-length m-sequences resulting in a family of 33, 31-length codes. The two “preferred pair” sequences originally used to develop the family of codes are discarded. The remaining 29 codes are reordered to select the particular user of interest and activation sequence for interfering transmitters. The reordering is based upon the “zero-phase” cross correlation statistics of the m-sequences. “Zero-phase” refers to the fact that each code is cross correlated against all other codes just once. For a full characterization, the code of interest must be cross correlated against all other codes, shifted one bit and correlated again. This is repeated until each code of interest, in all phases, had been cross correlated against all other codes which makes it rather impractical.

The transmitter activation sequence used in all simulations (where the transmitter number relates to the row number of the original Gold code matrix) is

\[ [21 \ 1 \ 7 \ 13 \ 19 \ 4 \ 5 \ 12 \ 15 \ 29 \ 9 \ 23 \ 11 \ 22 \ 24 \ 25 \ 28 \ 2 \ 10 \ 20 \ 27 \ 3 \ 14 \ 18 \ 17 \ 6 \ 8 \ 26 \ 16] \]

The particular coding \( \{c_j\} \) sequence for the individual transmitter is calculated using the sliding window described in Section 2.3. Table 3.2 illustrates transmitter 21’s Gold code sequence to chip offset sequence \( \{c_j\} \) conversion using a sliding window of \( r = 5 \).

Table 3.2: Gold code sequence (top row) to chip offset sequence \( c_j \) (bottom row) conversion using a sliding window of \( r = 5 \) (Transmitter 21 illustrated)

| 1 1 1 1 1 1 0 0 1 1 0 0 0 1 1 0 0 1 1 0 0 1 1 | 31 31 31 30 28 25 19 07 14 28 25 18 04 09 19 06 12 25 19 07 14 29 27 23 15 30 28 25 19 07 15 |
Figure 3.3: M-ary correlation receiver for maximum likelihood estimation of time hopped UWB waveforms

3.7 Evaluation Technique

UWB communication systems are in their infancy and have not yet proliferated to the extent where experimentation is easily done. Additionally, the TH-BPPM signaling evaluated in this study has not been fielded and is purely theoretical. Thus, simulation is the only practical means to investigate the biorthogonal TH-BPPM UWB communication technique. Additionally, simulation allows for quick modification of parameters to gather necessary data. Analysis is also greatly simplified.

Since the communication service involves properly transmitting data from one location to another, it is prudent to evaluate systems on their communication performance. The system modeled is a “fast time hopping” communication system whereby each symbol is generated, fast hopped/replicated \( N_H \) times, time hopped by applying the \( c_j \) code offset and transmitted. Using the multichannel correlation receiver of Fig. 3.3 under perfect “dehopping” conditions, coherent detection is achieved using a collection of cumulative decision variables, or test statistics \( \{ z_i \} \), as generated by accumulating \( N_H \) correlator outputs for each possible communication symbol \( s_i(t) \) [28]. Assuming the signals are equally probable, maximum likelihood
(ML) estimation is achieved by estimating the symbol which corresponds to the Max \( \{ z_i \} \). It can be shown that the two processes used to generate test statistics in Fig. 3.4 are equivalent.

\[
\int_0^{T_s} r(t) dt \quad \sum_{n=0}^{NH} \int_0^{N_H T_s} r(t) dt \quad z_1(T_s) = z_2(T_s)
\]

\[
S_{ref} = \sum_{n=0}^{NH} S_i(t-nT_0)
\]

Figure 3.4: Detection stage correlator comparison

Performance optimization associated with binary antipodal signaling, i.e., maximum distance properties, directly translates to the biorthogonal symbol set. The biorthogonal symbol set generated by (2.4), as illustrated in Fig. 2.7, is equivalent to Gray coded quadrature PSK (QPSK) modulation where the theoretical bit error probability is given by

\[
P_b = Q\left(\sqrt{\frac{2E_b}{N_o}}\right) \quad (3.4)
\]

where \( Q \) is the complementary error function, \( E_b \) is the average received energy per bit, and \( N_o/2 \) is the two-sided noise power spectral density [28].

The generation of cumulative test statistics and selection of Max \( \{ z_i \} \) as shown in Fig. 3.3 provides equivalent estimation performance as a single channel system using \( NH \) times the received energy [28]. Therefore, the improvement in communication performance as a result of hopping QPSK communication symbols \( NH \) times, and coherently detecting at the receiver, results in theoretical bit error probability
\[ P_b^H = Q\left(\sqrt{\frac{N_H \cdot 2E_b}{N_o}}\right). \] (3.5)

For \( N_H = 1 \), the result is that expected of normal QPSK communication systems.

Equation 3.5 is analyzed to validate model results for the single user scenario and the results plotted against the analytical results shown in Fig. 3.2. Once the single user model is validated, the model is applied to multiple transmitters. Experimentation proceeds under the model’s assumptions of AWGN with non-selective channel fading.

### 3.8 Workload

The simulation workload SNR and number of transmitters \( N_T \) allows direct comparison with [2]. These factors affect operation throughout the system. The total number of pulses generated, the noise through the channel, and the ability of the receiver to detect and estimate data symbols are all directly impacted. Providing the simulation with 10 SNR values and then 15 transmitter levels, 5 values for multipath replications, and 2 synchronization scenarios is consistent with published literature and reasonable given the memory and CPU speed of the computers available.

By using a fixed \( E_b/N_o \) as described in Section 3.6.1 and varying the four parameters \( N_T, N_{MP}, N_H \) and synchronization, a full factorial (4500 of 4500 potential workloads) is used to span the range of biorthogonal TH-BPPM UWB signals.

Table 3.3 outlines the multiple workloads submitted to the simulation with \( N_H \in \{1, 2, 10\}, N_{MP} \in \{0, 5, 10, 20, 40\}, N_T = 1 \) or 1 through 15, for both synchronous and asynchronous networks.
Table 3.3: Simulation Configurations

<table>
<thead>
<tr>
<th>Number of Multipath ($N_{MP}$)</th>
<th>Number of Hops ($N_H$)</th>
<th>1</th>
<th>2</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1</td>
<td>1-15</td>
<td>1-15</td>
<td>1-15</td>
</tr>
<tr>
<td>0</td>
<td>Sync</td>
<td>X</td>
<td>X</td>
<td>X</td>
</tr>
<tr>
<td></td>
<td>Async</td>
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<td>X</td>
<td>X</td>
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<tr>
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<td>X</td>
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<td>X</td>
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<td></td>
<td>Async</td>
<td>X</td>
<td>X</td>
<td>X</td>
</tr>
</tbody>
</table>

3.9 Experimental Design

The research is conducted using simulation in two phases. Initial results are used to validate the simulation model and verify values to be used in subsequent simulations. The second phase conducts the experiments.

This research characterizes bit error performance ($P_b$) of TH-BPPM multiple access schemes for UWB communications by first validating communication performance. This is done by varying the $E_b/N_o$, energy per bit divided by Additive White Gaussian Noise (AWGN) power spectral density, which proportionally maps to Signal-to-Noise Ratio (SNR). The ratio of incorrectly estimated bits to total number of bits received is used to calculate $P_b^H$. The simulated results are compared to analytic expectations obtained from (3.5). The number of hops per communication symbol ($N_H$) is fixed at one to validate the model against expected QPSK modulation results. Communication performance under interference conditions of Multiple Access Interference (MAI), Multipath Interference (MPI), and varied levels of $N_H$.
are simulated to study the robustness of UWB communication systems operating in a network of users with realistic propagation delays.

Analysis of TH-BPPM begins with development of components used in a UWB communication system. The system is tested by introducing AWGN into the channel to validate the model. Various noise power values are used to test the multiple access TH method. Finally, a specific $E_b/N_o$ is chosen to validate against previous results and serve as an appropriate power level for digital communications. Biorthogonal TH-BPPM communication performance, in terms of BER, is reported for increasing levels. MAI, MPI, and $N_H$ are introduced into each scheme and performance results analyzed for both synchronous and asynchronous network operation.

This research assesses the performance characteristics of a UWB communication system operating at a center frequency of 5.0 GHz. Though the trends reported should hold for any operating frequency, the parameters are fixed as described in Section 3.5 to indicate simulated performance in the unlicensed spectrum as authorized by the FCC for UWB systems.

Experimentation occurs in several phases. Initially, the benchmark of 300 bit errors is reduced to develop the code and gain a coarse understanding of the effect SNR has on the results. Once the code is fully developed, the model is validated. SNR is varied over 10 values, mapping to $E_b/N_o$ values between 0 and 10 dB, in increments of 1.0 dB. Following validation of $N_H = 1$ results with expected theoretical performance described by (3.4), experimentation proceeds to incorporate multiple transmitters.

The number of total transmitters (including the transmitted signal of interest plus all interfering transmitters) is varied from $N_T = 1$ to 15 transmitters. The SNR is fixed at $E_b/N_o$ levels of Section 3.6.1. All trials are recorded for a synchronous network of users. These trials are repeated for users transmitting asynchronously.
MPI is added by creating $N_{MP} = 0, 2, 5, 10$ and 40 multipath reflections per user and recording the synchronous and asynchronous results for a fixed SNR.

Fast time hopping is implemented by replicating each symbol $N_H$ times, encoding and transmitting with various levels of MAI and MPI for synchronous and asynchronous networks.

Figure 3.1 flow charts the logic behind the Matlab® algorithm. An $N_T \times 200$ matrix of random data streams is generated to insure independence among transmitters. The time hopping is easily implemented by replicating every $k$-bits of every user/transmitter; in this manner each $k$-bits are undergo the same modulation and TH coding processes prior to “transmission”. The 4-ary UWB modulator merely maps $k$-bits to one of four discretely sampled and stored UWB TH-BPPM waveforms. The asynchronous values represent the random activation of the transmitters. Once activated, the transmitter remains activated for the duration of the simulation and the $(0 : T_C)$ pulse offset value unique to each transmitter remains constant and is applied to every pulse from that transmitter.

Additive white gaussian noise (AWGN) is applied to each pulse. The noise realizations for $N_T \cdot (N_{MP} + 1)$ discrete waveforms are generated once per iteration of the 200-bit loop to maintain independence among individual transmitters, yet preserve the small time correlation among pulses from a single transmitter. The stored noise values are retrieved and applied as required for a given user, symbol, multipath link. The composite signal (signal of interest + interferers) is applied to the input of the 4-channel correlator. The correlator creates test statistics $Z_i$ that are accumulated $N_H$ times. The accumulator sums the test statistics and sends the values to the maximum likelihood estimator. The largest summed $Z_i$ value is chosen and mapped to the appropriate data bits. Once all data bits for a given iteration are collected, they are compared to the original data bits. The number of errors are accumulated and the entire process is repeated until 300 errors are generated to provide the confidence interval described in Section 3.4.
3.10 Analyze and Interpret Results

Successful results must support the goals of this research to determine, for particular error levels, the $E_b/N_0$ required and multiple access interference experienced when using spreading codes for fast time hopping. $P_b$ is plotted versus $E_b/N_0$ for various multiple access codes. Fixing the value of $E_b/N_0$, $P_b$ is plotted versus the number of transmitters given the levels of multipath and number of hops per symbol. Results are anticipated to follow a logarithmic scale between 0.5 and $10^{-6}$ for $P_b$ over the range of $E_b/N_0$ values. Similar results are expected when $P_b$ is plotted over the range of user levels. The values of $P_b$ are distinguishable at various factor levels so that only visual tests are needed to determine uniqueness, avoiding the need for a $t$-test [26] to determine statistically unique values. Previous analysis of variance (ANOVA) [2] quantified the real-time impact of code, number of transmitters, and multipath levels on system performance in terms of impact on the $P_b$. From the ANOVA results in [2], the significant factors affecting the output value $P_b$ are determined to be equivalent given the similarity in signal structure.

Similar to the BER Improvement in [17] for code improvements, the significant factor effects are quantified by determining the average BER Improvement (over 15 transmitters) for increasing $N_H$ values relative to a $N_H = 1$ baseline. Since a ratio can be determined for the $P_b$ value of one $N_H$ relative to that of another code, a decibel value is used to report the BER improvement. The average ratio of $P_b$ values is calculated for the 15 transmitters. From this improvement factor, the performance of each hopping level can be assessed.

3.11 Summary of Experimental Setup

This chapter outlines the methodology used to assess the performance of a “fast time hopping,” multiple access, UWB communication system using TH-BPPM modulation. The transmitter, receiver, channel, and multiple interferers are modeled to provide assess communication performance with specific emphasis on the multiple
access and modulation components. Since the system’s service is transmitting data bits, the metrics used to characterize system performance are probability of bit error versus $E_b/N_o$ and size of the network in terms of transmitters.

A two stage simulation process provides the basis for the research. Initial simulations are validated against accepted analytical performance equations. Once the model is verified, the parameters are adjusted for the actual experimentation.

Analysis of the results compares the relative effects of $E_b/N_o$, number of transmitters, number of multipaths, number of time hops per symbol, and network synchronization. Results are expected to provide accurate indicators of how the factors affect communication performance using the TH-BPPM modulation scheme. Additional insight into the trade-offs between time-hopping, data rate, and fast time hopping should be extracted.
IV. Results and Analysis

4.1 Single Channel Communication Performance

A single communication link TH-BPPM model with \(N_H = 1\) was validated against analytic bit error given by (3.5). Figure 4.1 compares the simulation results against the analytic bit error curve and previously reported orthogonal TH-PPM performance [2]. For the \(N_H = 1\) case, the biorthogonal TH-BPPM provided performance gains equivalent to that of Gray-coded QPSK; improved performance at a given \(E_b/N_o\) and an effective doubling of the data rate.

![Graph showing single channel communication performance](image)

Figure 4.1: Single Channel Communication Performance: orthogonal TH-PPM and biorthogonal TH-BPPM with no hopping \((N_H = 1)\)

Once validated for \(N_H = 1\), the model was extended to \(N_H = 2, 3,\) and 4 cases where simulated \(P_b^H\) results shown in Fig. 4.2 remain consistent with analytic
results of (3.5) and Fig. 3.2. As a single communication channel, the TH coding does not have any effect on measured performance. For each simulation, a random binary data stream was produced and \( k \) bits mapped to a communication symbol. Each symbol is then hopped \( N_H \) times (time modulated), transmitted, and received. Symbols were detected using a 4-channel correlator which sums \( N_H \) test statistics \( \hat{Z}_i \) to estimate each symbol \( \hat{S}_i \). The \( \hat{S}_i \) are mapped back to bits and the estimated data bits are compared to the original data bits and the total number of errors recorded. Using the 300 bit error criteria, data in Fig. 4.3 produces median values for mean squared error and standard deviation between simulated and analytic results of \( 3.7 \times 10^6 \) and \( 1.4 \times 10^3 \), respectively. The impact of fast time hopping each communication symbol is inherent processing gain in BER performance is evident. Improved bit error rates are achievable at lower \( E_b/N_o \) levels. As shown in Fig. 4.2, for a given bit error rate \( (P_b) \) there is a reduction in required \( E_b/N_o \) to achieve that \( P_b \) as \( N_H \) increases. Alternately stated, for a given \( E_b/N_o \) value, \( P_b \) decreases (improves) as \( N_H \) increases; the trade off for this improved performance is a \( 1/N_H \) reduction in effective data rate.

4.2 Network Communication Performance, \( N_H = 1 \)

Network performance for biorthogonal TH-BPPM was first compared to that of orthogonal TH-PPM. Using fixed average power to achieve desired communication performance of \( P_b = 10^{-3} \), i.e., \( E_b/N_o \approx 9.78 \) dB for orthogonal TH-PPM and \( E_b/N_o = 6.789 \) dB for biorthogonal TH-BPPM, network communication performance is evaluated for 1 to 15 transmitting users (one desired and up to 14 multiple access interferers). For all simulation results, the received power of all undesired interfering multiple access signals is identical to the received power of the desired signal.

4.2.1 Multiple Access Interference Effects. Initial MA performance characterization was done using \( N_H = 1 \) to isolate code selection and assignment effects in the absence of fast time hopping processing gain present. Using fixed average power
Figure 4.2: Single Channel Communication Performance: Biorthogonal TH-BPPM using $N_H = 1, 2, 3$ and 4 hops per communication symbol to achieve desired communication performance of $P_b = 10^{-3}$, i.e., $E_b/N_o = 6.789$ dB for biorthogonal TH-BPPM, multiple access performance is evaluated using $N_H = 1$ for a network containing up to $N_T = 15$ transmitters. In this case, the receiver under test receives one desired signal and $(N_T - 1)$ undesired, direct path multiple access interferers. For all simulation results, the received power of all undesired interfering multiple access signals is identical to the received power of the desired signal. The receiver under test is perfectly synchronized to the transmitter of interest while all other signals are received either synchronously or asynchronously. For the asynchronous network, all multiple access interferers are randomly offset (delayed) in time over $[0, T_c]$. 

4-3
Network multiple access results for biorthogonal TH-BPPM were generated for comparison with orthogonal TH-PPM results of [27]. Simulation results are shown in Fig. 4.3 for the synchronous (filled symbols) and asynchronous (unfilled symbols) networks. This filled and unfilled symbol convention is maintained throughout the document.

Figure 4.3: Multiple Access Performance: Asynchronous and Synchronous Networks using Orthogonal TH-PPM [15] and Biorthogonal TH-BPPM with Gold Coding

As in previous orthogonal TH-PPM work [17], the synchronous biorthogonal TH-BPPM network experiences minimal symbol collisions with Gold code assignment and bit error performance is virtually unaffected by variation in $N_T$. The “jump” occurring in both TH-BPPM asynchronous networks when the eighth transmitter joins the network is not due to premature termination of the Monte Carlo
simulation process. Rather, the “jump” is due to specific Gold code assignment and ordering. The particular collection of Gold codes used for generating Fig. 4.3 results (15 of 31 possible codes are assigned to transmitters) is such that the cross-correlation response between the joining eighth transmitter and previous seven transmitters destructively interferes (degrades $P_b$). Reassigning this particular collection of codes, or randomly reassigning a new collection of 15 codes from the original 31, yields results consistent with those in Fig. 4.3 but with the anomalous “jump” occurring at a different $N_T$ value. Figure 4.4 shows the effect of altering the transmitter activation sequence (reassignment of the original collection) and how the “jump” now occurs when the fifth transmitter joins the network. To permit comparison with subsequent results, the original Gold code collection and assignment used for generating Fig. 4.3 results is maintained throughout all simulations.

![Network Multiple Access Performance: Synchronous TH-BPPM “jump” shift due to Gold code sequence assignment](image)

Figure 4.4: Network Multiple Access Performance: Synchronous TH-BPPM “jump” shift due to Gold code sequence assignment
Using a BER improvement metric, i.e., the average ratio (over all 15 transmitters) of synchronous $P_b$ performance to asynchronous $P_b$ performance, results in Fig. 4.5 indicate a synchronized network containing up to $N_T = 15$ transmitters yields an average BER improvement of approximately $-6.30$ dB with orthogonal TH-PPM and approximately $-5.9$ dB with biorthogonal TH-BPPM; nearly equivalent performance is indicated for both techniques.

![Figure 4.5](image_url)

**Figure 4.5**: Single channel communication performance with $N_{MP}$ multipath replications present

### 4.2.2 Multipath Interference Effects

Figure 4.5 shows multipath interference effects on a single channel communication system for $N_{MP} = 0, 5, 10,$ and $20$ multipath replications. The degradation of BER is evident throughout the range of $E_b/N_o$ considered. At lower $E_b/N_o$ levels, thermal/channel noise dominates and
determines performance. As the $E_b/N_o$ increases the multipath interference dominates and overshadows noise effects in establishing system performance. The trends in Fig. 4.5 indicate that doubling $N_{MP}$ reduces BER by approximately 3.6 dB. For $E_b/N_o = 10$, the simulated performance/analytic results for $N_{MP} = 5, 10, 20$ is approximately $-29.4, -33.01, -33.76$ dB, respectively.

For the remainder of the simulated results presented in this chapter, Fig. 4.6 through Fig. 4.11, the labeling convention of Table 4.1 is used.

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<tr>
<th>Time Hopping</th>
<th>Network Synchronization</th>
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<td>Asynchronous (Unfilled)</td>
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<td>$N_H = 10$</td>
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</tbody>
</table>

Figure 4.6 provides performance results for $N_H = 1$ synchronous and asynchronous networks with $N_{MP} = 0, 5, 10, 20, 40$. For all multipath levels, the composite received waveform consists of $N_T \times (N_{MP} + 1)$ total signals, including one direct desired signal, $(N_T - 1)$ direct multiple access interfering signals and $N_T \times N_{MP}$ delayed multipath interfering signals. Whenever multipath is present ($N_{MP} > 0$), statistically equivalent results are achieved under simulated multipath conditions independent of synchronization. The results exhibit the expected performance degradation as $N_T$ and $N_{MP}$ increase; most notably, synchronized network advantages which are apparent in the $N_{MP} = 0$ case quickly diminish when multipath interference is introduced.

4.3 Network Communication Performance, $N_H > 1$

4.3.1 Time Hopped MA Performance. Network MA performance was characterized with processing gain present using symbol repeat values of $N_H = 2$ and 10. In these cases, the average received symbol power was fixed to achieve desired theoretical communication performance of $P_b = 10^{-3}$. For the $N_H = 2$ and 10
Figure 4.6: Network multipath interference effects for $N_H = 1$ using $N_{MP} = 0, 5, 10, 20$ and 40 replications (indicated in parenthesis)

cases, the received $E_b/N_o = 6.789$ ($N_H = 1 E_b/N_o value) - 10 \log_2(N_H)$ dB which is approximately 3.78 and -3.21 dB, respectively. Multiple access performance was evaluated for a network containing up to $N_T = 15$ transmitters. As in the $N_H = 1$ case, the receiver under test receives one desired signal and $(N_T - 1)$ undesired, di-
rect path multiple access interferers. The received power of all undesired interfering multiple access signals was set equal to the desired signal power and perfect synchronization is assumed for the signal of interest. All other signals are received either synchronously or asynchronously. Results presented in Fig. 4.7 show network performance improvement due to processing gain, a function of the repeating symbols. As indicated, symbol hopping has minimal impact on synchronous network performance because of the unique code assignments. For the asynchronous network all multiple access interferers are randomly offset (delayed) in time over $[0, T_c]$. As expected, network performance degrades as transmitters are added to the network and the number of collisions between symbols increases. However, for the asynchronous network a 6-fold and 8-fold $P_b^H$ improvement is indicated for $N_T = 15$ using $N_H = 2$ and $N_H = 10$, respectively.

4.3.2 Time Hopped MA Performance with Multipath Present. Multipath interference (MPI) effects were characterized using an RMS time delay value of 15.4 $\text{ns}$ for each transmitter’s replicated signal [20]. Data was generated using $E_b/N_o$ values as defined in Section 4.3.1 for various multipath replications ($N_{MP}$), including $N_{MP} = 0, 5, 10, 20$ and 40 reflections per transmitter. Figures 4.8, 4.9, and 4.10 show network communication performance for $N_T = 1$ to 15 transmitters with $N_{MP} = 5, 10, 20$, respectively. Figure 4.11 is a composite of all multipath results. Fast time hopping improves bit error performance for all cases where $N_{MP} < N_H$. As implemented in the algorithm, all benefits of time hopping are diminished once the level of multipath equals or exceeds the number of hops. For example, the performance improvement for $N_H = 10$ shown in Figure 4.8 is no longer present in Fig. 4.9. Similar results have been obtained for $N_H = 20$. 

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Figure 4.7: Network multiple access performance with processing gain of $N_H = 1, 2, 10$ and no multipath present ($N_{MP} = 0$)
Figure 4.8: Network Communication Performance with Time Hopping 
($N_{MP} = 5$ multipath replications per transmitter present)
Figure 4.9: Network Communication Performance with Time Hopping ($N_{MP} = 10$ multipath replications per transmitter present)
Figure 4.10: Network Communication Performance with Time Hopping ($N_{MP} = 20$ multipath replications per transmitter present)
Figure 4.11: Network Communication Performance with Time Hopping ($N_{MP} = 0, 5, 10, \text{ and } 20$ multipath replications per transmitter present)
Table 4.2 shows average BER improvement provided by fast time hopping as compared to the $N_H = 1$ case. In this case, the BER improvement is given by

$$BER\ Improvement = 10 \times \log_{10}\left(\frac{Average\ BER\ of\ N_T = 1\ to\ 15}{Average\ BER\ of\ N_H = 1}\right)$$  \ (4.1)$$

where the average BER performance of $N_H = 1$ synchronous or asynchronous is designated as the baseline performance, as appropriate. The more negative the decibel number reported, the greater the improvement provided by fast time hopping relative to $N_H = 1$ for the multipath level reported. For example, in a synchronized network containing up to 15 transmitters, TH-BPPM modulation with $N_H = 10$ provides approximately -5.9 dB at $N_{MP} = 0$ and approximately -3.6 dB at $N_{MP} = 5$. At $N_{MP} = 10$ the BER rates for the hopped and $N_H = 1$ cases are not statistically different.

The BER improvement numbers in Table 4.2 and Table 4.3 indicate how time hopping advantages diminish as $N_{MP}$ becomes greater than $N_H$.

Table 4.2: Time Hopping BER Improvement (dB) of (4.1)

<table>
<thead>
<tr>
<th>$N_{MP}$</th>
<th>$N_H = 2$</th>
<th>$N_H = 10$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Sync</td>
<td>Async</td>
</tr>
<tr>
<td>0</td>
<td>-0.162162</td>
<td>-3.537399</td>
</tr>
<tr>
<td>5</td>
<td>-0.53014</td>
<td>-0.583243</td>
</tr>
<tr>
<td>10</td>
<td>0.084626</td>
<td>0.171558</td>
</tr>
<tr>
<td>20</td>
<td>-0.078261</td>
<td>0.0852</td>
</tr>
<tr>
<td>40</td>
<td>-0.099825</td>
<td>-0.053802</td>
</tr>
</tbody>
</table>

Table 4.3 reports the BER improvement between synchronous and asynchronous performance for fast time hopping at various $N_{MP}$ levels. The BER improvement in this case is the ratio of synchronous performance to asynchronous perfor-
mance for each $N_H$ value and is given by

$$BER\text{ Improvement}(x) = 10 \times \log_{10} \left( \frac{BER_{Sync}, N_T = 1 \text{ to } 15, N_H = x}{BER_{Async}, N_T = 1 \text{ to } 15, N_H = x} \right)$$  \hspace{1cm} (4.2)$$

where the average asynchronous BER performance ($BER_{Async}$) of the particular $N_H$ level is designated as the baseline performance. Again, the more negative the decibel number reported, the greater the synchronized performance is relative to the asynchronous network for a given $N_H$ value. For example, in a network containing up to 15 transmitters, the BER improvement factor for TH-BPPM modulation with $N_H = 10$ varies from approximately -0.57 to 0.14 which indicates minimal variation between synchronous and asynchronous network performance. At $N_{MP} = 10$ the BER rates for the hopped and $N_H = 1$ cases are not statistically different. As expected, the $N_H = 1$ case has a greater variation but as multipath is added any benefits from synchronous operation are lost.

Table 4.3: Synchronous BER Improvement (dB) of (4.2)

<table>
<thead>
<tr>
<th>$N_{MP}$</th>
<th>$N_H = 1$</th>
<th>$N_H = 2$</th>
<th>$N_H = 10$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>-6.713958</td>
<td>-3.049962</td>
<td>-0.572538</td>
</tr>
<tr>
<td>5</td>
<td>-0.284994</td>
<td>-0.205711</td>
<td>-0.155646</td>
</tr>
<tr>
<td>10</td>
<td>0.019582</td>
<td>-0.034833</td>
<td>-0.036261</td>
</tr>
<tr>
<td>20</td>
<td>0.070459</td>
<td>-0.031231</td>
<td>-0.017065</td>
</tr>
<tr>
<td>40</td>
<td>-0.101052</td>
<td>-0.094326</td>
<td>0.139463</td>
</tr>
</tbody>
</table>
V. Conclusions

5.1 Research Contributions

Multiple access performance is characterized for UWB waveforms using biorthogonal TH-BPPM with pseudorandom coding. Fast time hopping is introduced and bit error expressions derived for biorthogonal TH-BPPM signaling. Results expand upon the binary TH-PPM work of [27] regarding Gold code time hopping sequences. TH-BPPM multiple access network performance is compared head-to-head with published results for an orthogonal TH-PPM technique. Contributions to the UWB research knowledge base include UWB communication, multiple access interference (MAI), multipath interference (MPI), and fast time hopping performance characterization using 31-length Gold codes over both synchronous and asynchronous networks.

5.2 Summary of Findings

5.2.1 Findings Without Fast Time Hopping ($N_H = 1$). A single communication channel using biorthogonal TH-BPPM model produced median values for mean squared error and standard deviation between simulated and analytic results of $3.7 \times 10^6$ and $1.4 \times 10^3$, respectively. For the $N_H = 1$ case, the biorthogonal TH-BPPM provided performance gains equivalent to that of Gray-coded QPSK; improved bit error performance at a given $E_b/N_o$ and an effective doubling of the data rate. Using fixed average power to achieve desired communication performance, the synchronous biorthogonal TH-BPPM network experiences minimal symbol collisions with Gold code assignment and bit error performance is virtually unaffected by variation in $N_T$. A BER improvement metric is introduced to quantify performance gains relative to the $N_H = 1$ asynchronous results. Results indicate a synchronized network containing up to $N_T = 15$ transmitters yields an average BER improvement of approximately $-6.30$ dB with orthogonal TH-PPM and approximately

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-5.9 dB with biorthogonal TH-BPPM; nearly equivalent performance is indicated for both techniques. Multipath interference on a single communication channel degrades BER throughout the range of $E_b/N_o$ considered. At lower $E_b/N_o$ levels, thermal/channel noise dominates and determines performance. As $E_b/N_o$ increases the multipath interference dominates and overshadows noise effects in establishing system performance. The observed trends indicate that doubling $N_{MP}$ reduces BER by approximately 3.6 dB. For $E_b/N_o = 10$ dB, the simulated performance-to-analytic results ratio for $N_{MP} = 5, 10, 20$ replications is approximately $-29.4, -33.01$, and $-33.76$ dB, respectively. In a multiple access environment containing multipath, performance results that are not statistically different are achieved under simulated multipath conditions independent of synchronization. The results exhibit the expected performance degradation as $N_T$ and $N_{MP}$ increase; most notably, synchronized network advantages which are apparent in the $N_{MP} = 0$ case quickly diminish when multipath interference is introduced.

5.2.2 Findings With Fast Time Hopping. Fast time hopping each communication symbol improves BER performance. For a given $E_b/N_o$ value, bit error rate $P_b$ decreases (improves) as $N_H$ increases; the trade-off for this improved performance is a $1/N_H$ reduction in effective data rate. Fast time hopping, i.e., $N_H = 2$ and 10 cases, show network performance improvement due to processing gain. Fast time hopping symbols has minimal impact on synchronous network performance because of the unique code assignments. However, for the asynchronous network a 6-fold and 8-fold $P_b^H$ improvement is indicated for $N_T = 15$ using $N_H = 2$ and $N_H = 10$, respectively. Fast time hopping improves bit error performance for all cases where $N_{MP} < N_H$. Average BER improvement provided by fast time hopping is compared to the $N_H = 1$ case. In a synchronized network containing up to $N_T = 15$ transmitters, TH-BPPM modulation using $N_H = 10$ provides approximately -5.9 dB improvement at $N_{MP} = 0$ and approximately -3.6 dB improvement at $N_{MP} = 5$. At $N_{MP} = 10$, the BER rates for the hopped and $N_H = 1$ cases are not statistically
different. BER improvement between synchronous and asynchronous performance for fast time hopping is shown for various $N_{MP}$ levels. In a network containing up to $N_T = 15$ transmitters, the BER improvement factor for TH-BPPM modulation with $N_H = 10$ hops varies from approximately -0.57 to 0.14 (minimal variation between synchronous and asynchronous network performance). At $N_{MP} = 10$ the BER rates for the hopped and $N_H = 1$ cases are not statistically different. As expected, the $N_H = 1$ case has a greater variation but as multipath is added any benefits from synchronous operation are lost. The BER improvement statistics show time hopping advantages diminish as $N_{MP}$ becomes greater than $N_H$.

5.3 Future Research

5.3.1 Error Correction with M-Ary Signaling. The fast time hopping scheme implemented provides results consistent with coherent pulse integration techniques without potential advantages of error correction capabilities. The hop encoding process could be thought of as a $(N_H, 1)$ block encoder operating at the symbol level. A mapping sequence for the received signals could be developed and implemented in the estimation stage. Simulation results could be validated against known block encoder message error and bit error expressions of [28] given as

$$P_M = \sum_{j=t+1}^{N_H} \binom{n}{k} \left( P_{b}^{H} \right)^{j} \left( 1 - P_{b}^{H} \right)^{N_H-j}, \quad \text{and} \quad (5.1)$$

$$P_{b} = \frac{1}{N_{H}} \sum_{j=t+1}^{N_H} j \binom{n}{k} \left( P_{b}^{H} \right)^{j} \left( 1 - P_{b}^{H} \right)^{N_H-j} \quad (5.2)$$

where $t$ is equal to the error correcting capability of the code.

5.3.2 Code Selection. Thirty-one length Gold codes were used to provide multiple access capability while minimizing collisions between users. The processing gain inherent in fast time hopping showed significant gains and should be evaluated against other codes of varying lengths, such as the random and Gold-127 reported
in [2] to characterize code type effects. The degradation responses reported in [17] may be lessened by employing fast time hopping.

5.3.3 Channel Models. The UWB model provided equal energy signals for all multiple users and multipath replications in a AWGN channel. Although this is a worst case analysis, it may not necessarily reflect real-world phenomenology. The model may be improved by considering the TH-PPM multiuser characterization research of [29]. No fading channel effects were implemented and all multipath signals were received with equal power. Rayleigh, log-normal, or Markov($\Delta - k$) could be applied to the waveforms to more accurately predict system performance.

5.3.4 Pulse Repetition Modifications. Fixed symbol rates were used for all simulations. Pulse generation schemes that allow overlapping pulses, i.e., chip intervals less than two times the symbol duration, would increase the overall throughput. The simulation data rates were fixed, but varying the data rate based on symbol overlap conditions may impact communication performance. An effort could be undertaken to determine optimal pulse spacing and chip interval to maximize efficiency and avoid overspreading effects described in [2]. The time hopping code development algorithm could be tested to determine optimal register size and resultant time hop $c_j$ values.

5.3.5 Interference Testing. Potential interference issues are commonplace in UWB discussions given the UWB signal characteristics described in Section 1.2. Characterization of UWB waveform interference effects on military applications, e.g., Global Positioning System, radar systems, aircraft avionics, and wireless communications should be undertaken. Facilities and resources exist within the military test community to efficiently and effectively conduct susceptibility modeling, simulation and testing.
5.3.6 *UWB Hardware Evaluation.* The TH-BPPM modulation scheme has not yet been fielded. Investigation into possible implementation techniques may be warranted given the performance gains demonstrated via modeling and simulation.
Bibliography


BIB-2


# CHARACTERIZATION OF ULTRA WIDE BAND MULTIPLE ACCESS PERFORMANCE USING TIME HOPPED-BIORTHOGONAL PULSE POSITION MODULATION

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## ABSTRACT
The FCC's release of its UWB First Report and Order in April 2002 spawned renewed interest in impulse signaling research. This work combines Time Hopped (TH) multiple access coding with 4-ary UWB Biorthogonal Pulse Position Modulation (TH-BPPM). Multiple access performance is evaluated in a multipath environment for both synchronous and asynchronous networks. Fast time hopping is implemented by replicating and hopping each TH-BPPM symbol \( N_H \) times. Bit error expressions are derived for biorthogonal TH-BPPM signaling and results compared with previous orthogonal TH-PPM work.

Without fast time hopping (\( N_H = 1 \)), the biorthogonal TH-BPPM technique provided gains equivalent to Gray-coded QPSK; improved BER at a given \( E_b/N_0 \) and an effective doubling of the data rate. A synchronized network containing up to \( N_T = 15 \) transmitters yields an average BER improvement (relative to an asynchronous network) of approximately -6.30 dB with orthogonal TH-PPM and approximately -5.9 dB with biorthogonal TH-BPPM. Simulation results indicate that doubling the number of multipath replications (\( N_{MP} \)) reduces BER by approximately 3.6 dB. Network performance degrades as \( N_T \) and \( N_{MP} \) increase and synchronized network advantages apparent in the \( N_{MP} = 0 \) case diminish with multipath interference present. With fast time hopping (\( N_H > 1 \)) improves BER performance whenever \( N_{MP} < N_H \) while reducing effective data rate by \( 1/N_H \). Compared to the \( N_H = 1 \) synchronized network, TH-BPPM modulation using \( N_H = 10 \) provides approximately -5.9 dB improvement at \( N_{MP} = 0 \) and approximately -3.6 dB improvement at \( N_{MP} = 5 \). At \( N_{MP} = 10 \), the BER for the hopped and \( N_H = 1 \) cases are not statistically different; with \( N_H = 10 \) hops, BER improvement varies from approximately -0.57 to 0.14 dB (minimal variation between synchronous and asynchronous network performance).

## SUBJECT TERMS
Ultra Wideband, UWB, TH-BPPM, Biorthogonal, Pulse Position Modulation, Multiple Access, Interference, Multipath Transmission, Fast Time Hopping