New Cirrus Models for MODTRAN4

I: Models Derived from the Standard and Subvisual Models

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1. Introduction

The purpose of this report is to set forth a new set of cirrus cloud models for use with the MODTRAN4 atmospheric transmission model and to provide a wider range of cirrus models with which to investigate future remote sensing techniques that may have to observe through cirrus. The cirrus cloud models were derived by selecting mode particle sizes between and beyond the two existing cirrus cloud models in MODTRAN4: Standard (mode particle radius 64 μm) and subvisual (mode 4 μm). The new set of models consists of 70 models whose mode particle radius range from between 0.1 and 64 μm. The format of the models meets the input requirements for MODTRAN4 and consist of files containing the input information on card 2E2. All the model calculations are based on spherical particles. A plan is included for extending the models to more realistic ones that use nonspherical particles.

The Moderate Resolution Transmittance (MODTRAN) code developed by the Air Force Research Lab (AFRL) calculates atmospheric transmittance and radiance for frequencies from 0 to 50,000 cm$^{-1}$ at moderate spectral resolution, primarily 2 cm$^{-1}$ (20 cm$^{-1}$ in the UV) (Berk et al. 1989). The development of the MODTRAN model was motivated by the need for higher spectral resolution than was available in the Low Resolution Transmittance (LOWTRAN) (Kneizys et al. 1986). MODTRAN’s capabilities include spherical refractive geometry, solar and lunar source functions, scattering (Rayleigh, Mie, single and multiple), and default atmosphere profiles (gases, aerosols, clouds, fogs, and rain). MODTRAN, version 4, release 1 was used for these calculations, and is the most current release.

The Cirrus cloud models in MODTRAN, and its predecessor LOWTRAN, were calculated by Shettle et al. (1988) using the optical constants for water ice measured by Warren (1984). These are known as the “Standard” and “Subvisual” Cirrus cloud models. The shape of the ice crystals was approximated using spherical particles, allowing the use of Mie theory to calculate the absorption and extinction (Bohren 1983, van de Hulst 1957). Shettle et al. assumed a particle size distribution given by the log-normal distribution function:

$$dN/d\sigma = n(\sigma) = a\sigma \exp(-b\sigma),$$

where $\sigma$ is the particle radius, and $a$ and $b$ are constants. Figure 1 shows the particle size distributions used to compute $K_E$ for the standard and subvisual models. The mean (mode) particle radius for the standard and subvisual models is 64 μm and 4 μm, respectively, and the calculations were done under the assumption that all the particles are spherical. The particles were treated individually between 0.05 μm and 1000 μm with 799 interspaced sizes.

The term “cirrus” is used to describe a number of clouds with similar characteristics (Lynch and Sassen 2001), the main difference within the cirrus category being particle size. In a previous study,
Figure 1. The particle size distribution for the subvisual model contains more particles \( \text{cm}^{-3} \), and they are on average much smaller \( (d_{\text{mode}} = 4 \, \mu\text{m}) \) than for the standard model \( (d_{\text{mode}} = 64 \, \mu\text{m}) \).

Lynch and Mazuk (2000) discussed how the particle size distribution has a strong influence on the absorption and emission spectra for a particle cloud. The paper by Fu (1996) summarizes 25 distinct particle size distributions that have been experimentally measured in cirrus clouds. Fu also notes that the particle size distributions are difficult to measure experimentally. Small ice particles are particularly difficult to measure, and in some experiments, the distribution functions were extrapolated to small sizes from measurements of larger particles.
2. Derivation of the New Models

The new cirrus models fill in the mode particle sizes between the two existing cirrus models and extend the subvisual cirrus model to smaller particle sizes than have previously been available. The same modeling methods used by Shettle et al. (1988) were used here. The Mie scattering code of Shettle et al. was used along with the optical constants of Warren (1984) to generate a set of extinction coefficient ($K_E$, $\text{km}^{-1}$), absorption coefficient ($K_A$, $\text{km}^{-1}$), and asymmetry parameter ($g$), all as a function of wavelength between 0.4 and 14.7 $\mu$m.
3. The New Models

The new cirrus cloud models consist of a large amount of numerical tabulations of extinction, absorption, and asymmetry coefficients. Therefore, we show them here in graphical form in Figures 2–15. The actual numerical models will be in the form of MODTRAN card 2E2 (See below) and will be transferred electronically. In each of Figures 2–9, the standard cirrus model corresponds to the far edge of the plot ($\sigma_{\text{MODE}} = 64 \, \mu\text{m}$), and the subvisual cirrus model corresponds to the near edge ($\sigma_{\text{M}} = 4 \, \mu\text{m}$). In each of Figures 10–17, the subvisual cirrus model corresponds to the far edge of the plot ($\sigma_{\text{M}} = 4 \, \mu\text{m}$).

Figure 2 shows a surface plot of the extinction coefficient $K_E$ over the wavelength range of 0.4 to 14.7 \, \mu\text{m}. This is normalized to unity at 0.55 \, \mu\text{m} for all mode particle sizes, but can be rescaled according to the user’s selection of optical depth. Note that $K_E$ is relatively flat and unstructured except in the foreground where the small particle effects become evident. The two obvious valleys correspond to the vibrational structure of ice at 3.16 \, \mu\text{m} and the broader rotational structure around 10.5 \, \mu\text{m}.

Figure 3 shows a surface plot of the absorption coefficient $K_A$ over the wavelength range of 0.5 to 14 \, \mu\text{m}. Here, there is considerably more structure in both wavelength and mode particle size space, and as in Figure 2, the structure increases with decreasing particle size.

Figure 2 is relatively flat because the extinction is dominated by scattering, and scattering efficiency is not strongly dependent on particle size or wavelength. In fact, it depends on the scattering size parameter $X = 2\pi a / \lambda$, which is generally greater than unity for most of the situations shown in the figure. The ample structure in Figure 3, on the other hand, is the result of numerous variations in the optical constants of ice. These are embodied in the absorption size parameter $\Omega = 4\pi k a / \lambda$ (Lynch and Mazuk 1998), where $k$ is the imaginary part of the index of refraction. In this situation, $\Omega << 1$, and, therefore, the variations in $k$ become dominant.

The asymmetry parameter $g$ results are shown in Figure 4, showing similar structure. There is considerable structure, but unlike the values in Figure 3, $g$'s dynamic range is fairly small, generally falling in the range of 0.8 to 1.0. As $\sigma_{\text{M}}$ decreases, the particles become small compared to the wavelength, and the $X$ drops below unity. When this happens, the particles become more like “Rayleigh” particles, and $g$ approaches zero.

Figures 5, 6, and 7 are expanded version of Figure 2, 3, and 4. These figures show the extinction, absorption, and asymmetry parameters between 1 and 1.5 \, \mu\text{m}. In Figure 5, the extinction, $K_E$, is relatively flat, although some size- and wavelength-dependent “warpage” is present. Figure 6 shows virtually no variation in the absorption $K_A$, but Figure 7 shows significant variation in $g$ as a function of mode radius $\sigma_{\text{M}}$. 

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Figure 2. Extinction coefficient (K_E km^{-1}): \lambda = 0.5 to 14 \mu m, and \sigma_M = 4 to 64 \mu m.

Figure 3. Absorption coefficient (K_A km^{-1}): \lambda = 0.5 to 14 \mu m, and \sigma_M = 4 to 64 \mu m.
Figure 4. Asymmetry parameter (g, unitless): $\lambda = 0.5$ to 14 $\mu$m, and $a_M = 4$ to 64 $\mu$m.

Figure 5. Extinction coefficient ($K_E$ km$^{-1}$): $\lambda = 1.0$ to 1.5 $\mu$m, and $a_M = 4$ to 64 $\mu$m.
Figure 6. Absorption coefficient ($K_A \text{ km}^{-1}$): $\lambda = 1.0$ to $1.5 \mu m$, and $\sigma_M = 4$ to $64 \mu m$.

Figure 7. Asymmetry parameter (g, unitless): $\lambda = 1.0$ to $1.5 \mu m$, and $\sigma_M = 4$ to $64 \mu m$. 
Figures 8 and 9 show the scattering coefficient $K_S$, which is defined as $K_E - K_A$. They are included for completeness.

It is clear from all of the above results that changes in the mean particle size (i.e., changes in $\bar{a}_M$) have the greatest influence for small particles. This sensitivity is well known and has been discussed in the context of cirrus clouds by Takano et al. (1992). Therefore, we extended the range of values for $\bar{a}_M$ downward to between 0.1 and 4.0 $\mu$m and calculated $K_E$, $K_A$ and $g$. The results are shown in Figures 10–17, and correspond to Figures 2–9, except they are for smaller particles. In each of Figures 10–17, the subvisual cirrus model corresponds to the far edge of the plot ($\bar{a}_M = 4 \mu$m).

![Graph showing scattering coefficient $(K_E \text{ km}^{-1})$: $\lambda = 0.5$ to $14 \mu$m, and $\bar{a}_M = 4$ to $64 \mu$m.](image)

Figure 8. Scattering coefficient $(K_E \text{ km}^{-1})$: $\lambda = 0.5$ to $14 \mu$m, and $\bar{a}_M = 4$ to $64 \mu$m.
Figure 9. Scattering coefficient ($K_E \text{ km}^{-1}$): $\lambda = 1.0$ to 1.5 $\mu$m, and $\delta_M = 4$ to 64 $\mu$m.

Figure 10. Extinction coefficient ($K_E \text{ km}^{-1}$): $\lambda = 0.5$ to 14 $\mu$m, and $\delta_M = 0.1$ to 4 $\mu$m.
Figure 11. Absorption coefficient ($K_a \text{ km}^{-1}$): $\lambda = 0.5$ to 14 $\mu$m, and $\sigma_M = 0.1$ to 4 $\mu$m.

Figure 12. Asymmetry parameter (g, unitless): $\lambda = 0.5$ to 14 $\mu$m, and $\sigma_M = 0.1$ to 4 $\mu$m.
Figure 13. Extinction coefficient \( (K_E \text{ km}^{-1}) \): \( \lambda = 1.0 \) to 1.5 \( \mu \text{m} \), and \( \sigma_M = 0.1 \) to 4 \( \mu \text{m} \).

Figure 14. Absorption coefficient \( (K_A \text{ km}^{-1}) \): \( \lambda = 1.0 \) to 1.5 \( \mu \text{m} \), and \( \sigma_M = 0.1 \) to 4 \( \mu \text{m} \).
Figure 15. Asymmetry parameter (g, unitless): $\lambda = 1.0$ to 1.5 $\mu$m, and $\sigma_M = 0.1$ to 4 $\mu$m.

Figure 16. Scattering coefficient ($K_F \text{ km}^{-1}$): $\lambda = 0.5$ to 14 $\mu$m, and $\sigma_M = 0.1$ to 4 $\mu$m.
Figure 17. Scattering coefficient ($K_F$ km$^{-1}$): $\lambda = 1.0$ to 1.5 $\mu$m, and $\delta M = 0.1$ to 4 $\mu$m.
4. Using the New Models in MODTRAN4

The new cirrus cloud models were developed for use with the MODTRAN4 atmospheric transmission model. MODTRAN4 allows for the insertion of a cloud model, which is then used in conjunction with model (or measured) atmospheric data in the calculation of transmission and radiance. Inputs to MODTRAN4 consist of lines of formatted ASCII text, and are referred to as "cards" in reference to IBM punch cards formerly used as computer inputs.

The cloud and aerosol specification begins on Card 2. Here, we commonly set the parameter IHAZE = 1 for a rural aerosol model with 23 km visibility. We also set ICLD = 1 to select a cumulus cloud. Remaining values are set to zero, but the user can make further selections depending on the characteristics of a particular analysis.

Card 2A (alternate form used if ICLD = 1 through 10) defines the parameters for the cloud model chosen on Card 2, and is used for clouds other than cirrus. Entries on this card trigger the reading of cards 2E1 and 2E2. The simplest way to define a cirrus cloud is to specify its base height and thickness (both in km) and its extinction coefficient, $K_E$, from the calculated models. In this mode, however, the thickness must be chosen so as to give the proper optical depth at 0.55 μm. The optical depth, $\tau$, and $K_E$ are simply related through the cloud thickness,

$$\tau = K_E L,$$

where $L$ is the cloud thickness in km. The user also sets the number of layer boundaries used to define the cloud structure on card 2E1, and the number of wavelengths to be input for cloud extinction and absorption values on card 2E2. The cloud column water density is set to zero. Finally, the user specifies the model asymmetry values rather than defaulting to Henyey-Greenstein values.

Card 2E1 defines the cloud layer's ice and liquid water densities in g/m$^3$. As it happens, the value of densities are not used directly; so as long as they are greater than zero, the code will work. For cirrus clouds only, the user must zero out the water density and the rain rate as well.

Card 2E2 defines the extinction, absorption, and asymmetry of water and ice for each wavelength (Table 1). Here, the user must input negative values for the water, which causes the cloud model to use the default extinction, absorption, and asymmetry values for the cloud we specified in Card 2 (here a cumulus cloud). But recall that the user previously zeroed out the water content of the cloud, so there is no contribution here. So the only values that should be active are the ones input for the ice based on the models presented here.
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<td>Extinction coefficient</td>
<td>(km⁻¹)</td>
<td>for water (negative suppresses water cloud)</td>
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<tr>
<td>-9</td>
<td>Absorption coefficient</td>
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<td>for water (negative suppresses water cloud)</td>
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<td>Asymmetry parameter</td>
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<td>Asymmetry parameter</td>
<td>(unitless)</td>
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5. Limitations of the Models

The models presented here are based on Shettle et al.'s cirrus cloud models. They give reasonable results and reproduce the basic properties of cirrus clouds, i.e., absorption peaks at the appropriate places, representative transmission, scattering cross sections that behave as expected, etc. To the extent to which the two models in MODTRAN4 are useful, the models presented here extend this utility to intermediate size regimes and, perhaps more importantly, to smaller sizes that are associated with subvisual cirrus. For most applications, they are about as good as can be achieved within the computational limitations of MODTRAN.

All the new cirrus cloud models, as well as the built-in cirrus cloud models, suffer from one major limitation: they are calculated assuming that the clouds are composed of spherical particles. The ice particles comprising cirrus clouds are unquestionably non-spherical, often highly so. The impact of the spherical particle assumption is that the scattering of light is not accurately calculated over all angles; i.e., the bi-directional reflectance distribution function (BRDF) is not well modeled. However, the current release of the MODTRAN4 model does not allow insertion of a BRDF for any cloud model; only ground surface BRDFs can be inserted, so this solution is not available. The alternative is to parameterize the effects of non-spherical particles within the limitations of the MODTRAN inputs. This approach will be explored in the next phase of our modeling efforts.
6. Conclusions

We have produced a new set of cirrus cloud models for use with the MODTRAN atmospheric transmission code. These models extend the range of mean particle sizes beyond the limits of the existing models included in MODTRAN, covering the broader range of cloud composition seen in nature. These models can be used in conjunction with MODTRAN to investigate the effects of cirrus clouds on future remote sensing techniques that may have to observe through cirrus.
References


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