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**Synthetic Aperture Sonar Performance and Randomly Varying Sound Speeds in the Water Column**

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Random sound speed fluctuations are prevalent in the ocean, even over distance scales of only a few meters (the so called "fine structure" and microstructure"). Since synthetic aperture sonar (SAS) measurements involve repeatedly "pinging" the target, these random sound speed fluctuations will cause the time of flight to the target to vary between pings. These time variations may produce significant phase errors in the array, degrading system performance. This paper intends to study the effect on SAS system performance of random sound speed fluctuations as evidenced in simulations.

The approach is to modify an existing Matlab simulation to include a ping-to-ping variation of the sound speed characterized by a Gaussian distribution, then compare results to the non-varying case.

stochastic, SAS (synthetic aperture sonar), sound speed fluctuations, and Matlab simulation

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Keywords—Stochastic, synthetic aperture sonar

I. INTRODUCTION

Random sound speed fluctuations are prevalent in the ocean, even over distance scales of only a few meters (the so called "fine structure" and "microstructure").\[1\]

Since synthetic aperture sonar (SAS) measurements involve repeatedly "pinging" the target, these random sound speed fluctuations will cause the time of flight to the target to vary between pings. These time variations may produce significant phase errors in the array, degrading system performance. This paper intends to study the effect on SAS system performance of random sound speed fluctuations as evidenced in simulations.

The approach is to modify an existing Matlab simulation to include a ping-to-ping variation of the sound speed characterized by a Gaussian distribution, then compare results to the non-varying case.

A. Matlab Simulation

The Matlab simulation used and modified for this paper is called sassin.m and was coded by José Fernandez at the Naval Coastal Systems Center in Panama City, FL. The program requires the frequency, the source and receiver array dimensions, the sound speed (assumed constant in time and space), the along-track velocity, the range to the target, the yaw angle and the steering angle. All inputs had default values which were used to describe a nominal environment during the simulations performed for this paper (see Section II).

The output of the simulation is a chart of the point response function of the SAS as a function of along-track position (normalized to the maximum response found).

The author modified the sassin.m program in order to investigate the effects of water column sound speed fluctuations on the simulated SAS response. The resulting program is called sassin1.m. One section of the original sassin.m modeled the source-to-target-to-receiver propagation in a loop over the number of pings required. This part of the code was modified so that for each ping, a sound speed was chosen from a Gaussian distribution whose mean and standard deviation were input by the user. The mean value of sound speed was used for all other processing.

Hence, the code modeled random ping-to-ping sound speed variations.

Specifying a standard deviation of 0.0 to the modified sassin1.m generated identical results as the original sassin.m.

II. SIMULATION RESULTS

The modified simulation was run with various frequencies and sound speed standard deviations. The remaining parameters are listed in Table I. The values of these parameters are the original program’s defaults.

<table>
<thead>
<tr>
<th>System Parameters Unchanged in the Simulations</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean sound speed</td>
</tr>
<tr>
<td>Receiver element spacing</td>
</tr>
<tr>
<td>Number of Receiver elements</td>
</tr>
<tr>
<td>Number of Source elements</td>
</tr>
<tr>
<td>Along-track source offset</td>
</tr>
<tr>
<td>Along-track velocity</td>
</tr>
<tr>
<td>Range to target</td>
</tr>
<tr>
<td>Array yaw angle</td>
</tr>
<tr>
<td>Steering angle</td>
</tr>
</tbody>
</table>

Figure 1 shows the change in the point response function as the sound speed is varied with a standard deviation $\sigma$ of just 0.005 m/s (out of a mean of 1500 m/s). The central peak at $x = 0$ is broadened substantially so that localization becomes significantly more difficult. The acoustic frequency used in this simulation was 180 kHz, the default for sassin.m.

A. Varying Sound Speed Distribution

Figure 2 shows how SAS performance depends upon the sound speed distribution. The figure plots "mean error" as a function of sound speed standard deviation. The mean error is defined according to

$$E(\sigma) = \left\langle \frac{s(\sigma) - s(0)}{s(0)} \right\rangle$$ (1)

where $\langle \rangle$ indicates the arithmetic mean, $s(\sigma)$ is the SAS response (in dB relative to the maximum value) for the simulation where the sound speed standard deviation is $\sigma$. While the actual value is not terribly significant, equation 1 gives us a way of comparing the SAS response in the presence of sound speed variations to the SAS response in the absence of these variations.
In fact, the value plotted in figure 2 is the mean value of \( E(\sigma) \) calculated over 100 trials for each data point, since the value of \( E(\sigma) \) for any given run can be influenced by the exact values of the sound speed chosen from the distribution. The standard error is reflected in the plot with error bars.

Figure 2 shows that the SAS performance degrades with increasing sound speed standard deviation, as one might expect. It is perhaps alarming that sound speed variations of only 5–10 cm/s are enough to seriously affect performance. These sorts of fluctuations are well within the range of variations observed in the ocean (see Section II-C below).

### B. Varying Frequency

Figure 3 shows how SAS performance with a randomly varying sound speed depends upon the acoustic frequency. The figure plots mean error as defined in equation 1 against frequency, again using the mean value of \( E(\sigma) \) over 100 trials.

Figure 3 shows that the SAS performance degrades with increasing frequency. One way of improving the performance of an SAS in a stochastic environment would therefore be to use the lowest frequency practical.

### C. Expectation of Performance Under Actual Conditions

In high frequency medium coherence experiments conducted off Panama City, FL in April, 1995, Stanic collected data on temporal variability of the ocean temperature \( \Delta T \) using thermistors with a response of 23 ms.[2] With an ambient ocean temperature of about 22.5°C, the corresponding variation in sound speed \( \Delta c \) can be calculated.[5] Table II gives the expected values of \( E(\sigma) \) (with associated standard errors) for these values of sound speed variances. In this table, the range to the target is 90 m, not 30 m as in figures 1–3.

<table>
<thead>
<tr>
<th>Date</th>
<th>( \Delta T )</th>
<th>( \Delta c )</th>
<th>Mean Error (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>°C</td>
<td>(m/s)</td>
<td>50 kHz</td>
</tr>
<tr>
<td>4/17 AM</td>
<td>0.017</td>
<td>0.043</td>
<td>16.15±0.04</td>
</tr>
<tr>
<td>4/17 PM</td>
<td>0.018</td>
<td>0.046</td>
<td>16.69±0.05</td>
</tr>
<tr>
<td>4/18 AM</td>
<td>0.021</td>
<td>0.054</td>
<td>18.10±0.05</td>
</tr>
<tr>
<td>4/18 AM</td>
<td>0.057</td>
<td>0.145</td>
<td>29.27±0.19</td>
</tr>
<tr>
<td>4/18 PM</td>
<td>0.143</td>
<td>0.365</td>
<td>35.64±0.15</td>
</tr>
</tbody>
</table>

### III. Conclusions

An independently produced simulation of SAS performance was modified to allow a ping-to-ping variation of the sound speed. The resulting SAS response was compared with no-variation responses to determine the impact that time-varying sound speeds would have on SAS performance.

It was found that small variations in sound speed, comparable to those found in experimental tests performed off Panama City, FL, can significantly degrade SAS performance, especially at high frequencies.

### IV. Acknowledgments

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REFERENCES