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**ABSTRACT** (Maximum 200 words)

Based on findings indicating that both the Zeldovich and N$_2$O mechanisms are important in the formation and decomposition of NO in direct injection (Dl) Diesel engines, a skeletal mechanism consisting of seven elementary reactions is used to develop a two-zone model for NOx emissions from Dl Diesel engines. Characteristic chemical kinetic times for NO formation in zone 1 and NO decomposition in zone 2 are formulated from the law of mass action applied separately to each zone, and the relative importance of NO decomposition in four Dl Diesel engines is examined. Preliminary fluid mechanic mixing times for NO formation are developed by the combination of fluid relations characteristic of each of the many mixing processes occurring in a Dl Diesel engine. These results are empirical, but future fluid mechanic mixing times applicable to all Dl Diesel engines may be found. Similarly, a two-zone soot CTM accounting for both soot formation and oxidation is outlined. The NOx/soot tradeoff for low loads is also proven using the preliminary models for soot and NOx, thereby showing that when complete the models will predict the correct trends.

**SUBJECT TERMS**
Dl Diesel emission models, combustion processes, skeletal mechanisms, NOx, and soot.
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NOMENCLATURE

bmep  Brake mean effective pressure (kPa)
bsfc  Brake specific fuel consumption (g/kW-hr)
CTM   Characteristic time model
Da    Damköhler number
d_{noz} Nozzle hole diameter (m)
E     Activation energy (cal/gmol)
EGR   Exhaust gas recirculation
Kc    Equilibrium constant based on concentration
k_{if} Forward rate coefficient of the i\textsuperscript{th} reaction
k_{ir} Reverse rate coefficient of the i\textsuperscript{th} reaction
l_{imp} Fuel jet impingement distance (m)
M_{NO2} Molecular weight of NO\textsubscript{2}
m  Model constant incorporating various conversion constants
m_{f} Mass of fuel per cycle (g)
m_{sf} Model constant for soot formation process
m_{so} Model constant for soot oxidation process
m'  Scale factor
N    Engine speed (rpm)
NO\textsubscript{x}EI Oxides of nitrogen emissions index (g NO\textsubscript{x} as NO\textsubscript{2}/kg fuel)
P_{2} Cylinder pressure at start of combustion (atm)
P_{3} Maximum cylinder pressure (atm)
PSR   Perfectly stirred reactor
R    Universal gas constant (1.986 cal/gmol·K or 82.06 atm L/kmol·K); correlation coefficient
Re  Reynolds number
Ri  ith reaction in a mechanism
rc  Compression ratio
SootEI  Soot emissions index (g soot/kg fuel)
T2  Cylinder temperature at start of combustion (K)
T3b  Burned gas temperature at the end of combustion (K)
T_{50\%}  50% fuel recovery temperature (K)
T\phi+1  Stoichiometric, adiabatic flame temperature (K)
T\phi+3  Temperature at a equivalence ratio of 3 (K)
V_{3b}  Cylinder volume at the end of combustion (cm$^3$)
We  Weber number
AP  Pressure drop across fuel injection nozzle (MPa)
\varepsilon_{NO}  Fractional extent of reaction for NO formed per eddy in a given zone
f  Fuel-air equivalence ratio
\rho_a  Density of air
\rho_d  Power density
\tau_{fl,NO}  Eddy lifetime in NO formation zone
\tau_{id}  Characteristic time for ignition delay
\tau_{imp}  Characteristic time for fuel impingement on cylinder bowl wall (based on the penetration correlation of Arai and Hiroyasu (1990)
\tau_{no}  Characteristic kinetic time for NO formation (s or ms)
\tau_{no,3b}  Characteristic kinetic time for NO decomposition (s or ms)
\tau_{sf}  Characteristic kinetic time for soot formation (s or ms)
\tau_{sl,3b}  Eddy lifetime in NO decomposition zone
\tau_{sl,sf}  Eddy lifetime in soot formation zone
\[ \tau_{sl,so} \quad \text{Eddy lifetime in soot oxidation zone} \]

\[ \tau_{so} \quad \text{Characteristic kinetic time for soot oxidation (s or ms)} \]

\[ \nu_{\text{fuel}} \quad \text{Kinematic viscosity of fuel} \]

Subscripts:

\( \text{eq} \quad \text{Equilibrium} \)

\( f \quad \text{Forward reaction} \)

\( \text{no} \quad \text{Nitric oxide} \)

\( \text{ov} \quad \text{Overall equivalence ratio} \)

\( r \quad \text{Reverse reaction} \)

\( \text{sf} \quad \text{Soot formation} \)

\( \text{so} \quad \text{Soot oxidation} \)

\( \phi = 1 \quad \text{Stoichiometric} \)

\( \infty \quad \text{High-pressure limit} \)

\( 0 \quad \text{Low-pressure limit} \)

\( 1 \quad \text{Zone 1 conditions} \)

\( 1' \quad \text{Zone 1' conditions} \)

\( 2 \quad \text{Zone 2 conditions} \)

\( 3b \quad \text{End of combustion} \)
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1-1. The two-zone model for NO formation and decomposition in a DI Diesel combustion chamber as postulated by Mellor et al. (1998). Zone 1' is intermediate and based on the zone 1 pressure and flame temperature but the zone 2 stoichiometry, φow, for the engine.

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1.0 CHARACTERISTIC TIME MODEL

1.1 STATEMENT OF THE PROBLEM STUDIED

The goal of this work has been to develop characteristic time models (CTMs) for the prediction of engine-out NO\textsubscript{x} and soot emissions from direct injection (DI) Diesel engines. The CTM approach to emission prediction involves identifying the characteristic times of the dominant chemical and fluid mechanic subprocesses in the combustion phenomenon and, based on these times, develop a correlation between the appropriate model and pollutant. From a computational standpoint, this type of semi-empirical correlation is relatively simple. Consequently, the model is useful as a preliminary design tool, which may be used by Diesel engineers to reduce the cycle time required to design, develop and test new engines. The computational simplicity of the model also makes it amenable to incorporation into a CFD code or a phenomenological cycle simulation code to improve the emissions prediction. Still another perceived end use is for real-time engine emissions control.

In previous work done to model NO\textsubscript{x} emissions in Diesel engines, Ahmad and Plee (1983) showed that NO kinetics are described by a single global activation temperature. The global activation temperature suggested by these investigators for DI Diesels was 34,300 K, significantly less than the global activation temperature that is typically associated with NO formation through the extended Zeldovich kinetics in conventional gas turbine combustors (68,479 K, Sawyer et al., 1973; 67,976 K, Tuttle et al., 1977). Ahmad and Plee (1983) attribute this difference to NO decomposition within the engine. Thus, the model of Ahmad and Plee (1983) implies that the importance of NO decomposition relative to formation in Diesel combustion is approximately constant.
More recent analysis by Duffy et al. (1996), however, suggests that a single global activation temperature does not model NO$_x$ emissions from modern DI Diesel engines. Consequently, the one-step global model of Ahmad and Plee (1983), though adequate for the engines analyzed in that investigation, is not generally applicable to DI Diesel engines.

The work of Plee and coworkers (Plee et al., 1981; Ahmad and Plee, 1983) also used a single global activation temperature to describe the kinetics of particulate emissions. The obtained activation temperature represented the contributions of both soot oxidation and formation, and varied from engine to engine. The variations of the activation temperature was attributed to differences in mixing and thus combustion chamber geometry. The increased mixing causes the formation of soot to be reduced along with better recirculation of soot particles through the reaction zone, enhancing soot oxidation (Ahmad and Plee, 1983). Although both chemical processes involved in soot emissions are important, it was concluded that the oxidation process is dominant and affected more by flame temperature changes.

In this work, the one-step global approach to modeling NO kinetics in Diesels is replaced by a skeletal mechanism, which contains the NO chemistry relevant to high pressure and temperature combustion typical of DI Diesels. Additionally, based on the work done under this program as well as laser-sheet imaging results from Dec (1997), a zonal model of the physics of the NO formation and decomposition processes in Diesels is postulated. From these kinetic and physical models for NO emissions, a characteristic time model for NO$_x$ emissions from Diesel engines is derived. From kinetic times for NO formation and decomposition, derived here from first principles, the factors affecting
the importance of NO decomposition are evaluated. Preliminary empirical analysis to define a fluid mechanic time for NO formation has also been performed under this program.

For the soot emissions model, the global activation temperature approach still applies, but the contribution of both soot formation and oxidation will be represented by individual chemical kinetic and mixing times. Also based on the work of Dec (1997), a two zone model is postulated for soot with the importance of each chemical process dependent on the spatial location.

1.2 SKELETAL MECHANISM FOR NO CHEMISTRY

NO\textsubscript{x} chemistry can proceed through the extended Zeldovich mechanism (Lavoie et al., 1970), the prompt mechanism (Fenimore, 1971), the N\textsubscript{2}O mechanism (Malte and Pratt, 1974), and NO formation from fuel-bound nitrogen. The last pathway is negligible for modern Diesel fuels, which contain low amounts of organic nitrogen.

To formulate a skeletal mechanism for NO\textsubscript{x} emissions in Diesel engines, it is necessary to consider the different pathways of NO formation and decomposition and, through kinetic analysis, determine those pathways that are significant at the operating conditions of interest. Mellor et al. (1998) present a review of such kinetic analyses. From this review it is concluded that, at conditions typical of Diesel combustion (i.e., stoichiometric and lean flame temperatures and high pressures), the significant paths for NO chemistry are the extended Zeldovich (Lavoie et al., 1970) and nitrous oxide (Malte and Pratt, 1974) mechanisms.

Based on the review discussed above, Mellor et al. (1998) postulate a skeletal mechanism for NO chemistry in DI Diesel engines. This mechanism is expressed as
where reactions (R1), (R2), (R3), and (R6) are from the extended Zeldovich mechanism and (R4), (R5), and (R7) are from the N\textsubscript{2}O mechanism.

Along with the kinetic studies reviewed by Mellor et al. (1998), the present exclusion of the prompt mechanism at Diesel conditions is further supported by Dec (1997). Using laser-sheet imaging, he shows that premixed combustion in DI Diesels is not conducive to NO formation through the prompt mechanism since $\phi \approx 4$. Dec (1997) does argue that prompt NO may form in the diffusion portion of the Diesel burning process; nevertheless, given the temperature of Diesel combustion, NO formation through this pathway is likely to be negligible compared to the alternatives.

It is also important to note that (R5) is a three-body reaction and is thus pressure sensitive. In the following section, it will be shown that this pressure sensitivity changes the relative contribution of the N\textsubscript{2}O pathway to NO formation in Diesel engines.

1.3 TWO-ZONE MODEL FOR DIESEL COMBUSTION

Based on recent laser sheet imaging results of Dec (1997) and the earlier findings of Ahmad and Plee (1983), Mellor et al. (1998) have postulated a two-zone model for NO formation and decomposition in DI Diesel engines as illustrated in Fig. 1-1. In the figure,
Figure 1-1. The two-zone model for NO formation and decomposition in a DI Diesel combustion chamber as postulated by Mellor et al. (1998). Zone 1' is intermediate and based on the zone 1 pressure and flame temperature but the zone 2 stoichiometry, $\phi_{zo}$, for the engine.
Zone 1 is a near stoichiometric region (ϕ ≈ 1) where [NO] is small and in which NO formation occurs through forward reactions (R1) through (R5), equilibrium (R6), and forward reaction (R7). Following the results of Dec (1997), this zone is shown as a thin layer surrounding the periphery of the fuel plume. Between zone 1 and zone 2, there is a transition in which the concentrations of the products in zone 1 are adjusted to the overall engine stoichiometry (zone 1'). Zone 2 is a region in which hot, burned gases are present at the overall equivalence ratio. In this zone, NO decomposition occurs through the reverse of the mechanism given above.

The adiabatic stoichiometric flame temperature $T_{4-1}$ for zones 1 and 1' is computed following Plee et al. (1980), that is, with start of combustion (SOC) conditions, the stoichiometric amount of fuel, and assuming constant pressure burning. Stoichiometric temperatures vary from 2200 K to 2700 K with the lower values resulting from EGR or water injection. The representative temperature in zone 2 is the end of combustion temperature, $T_{3b}$ and is calculated following Mellor et al. (1998). Typical values for $T_{3b}$ are in the range of 1300 to 2200 K depending upon overall equivalence ratio, inlet manifold conditions, and so forth.

In the zonal model just described, it is assumed that concentration and temperature gradients can be ignored within a given zone. Thus, Mellor et al. (1998) model the chemistry in each zone using a perfectly stirred reactor (PSR) simulation (Bowman et al., 1995) with adiabaticity assumed. The GRI MECH 2.11 methane-air kinetic mechanism (Bowman et al., 1995) is used to provide heat release and, in this sense, model stoichiometric and lean Diesel fuel combustion.
The relatively constant concentrations of N-atom and N$_2$O in each zone provide a basis for the steady-state approximation to be made in the following section. Also, the PSR simulation of Mellor et al. (1998) shows that [NO]$_{eq}$ is largest in zone 1' where $\phi = \phi_{ov}$ and the reactor temperature and pressure remain at the stoichiometric zone conditions. This fact will be used in the definition of the characteristic times derived below.

1.4 NO FORMATION AND DECOMPOSITION TIMES

1.4.1 Characteristic Time For NO Formation

Writing the law of mass action for the rate of NO formation in zone 1 gives

$$\frac{d[NO]}{dt} = k_{1f}[O][N_2] + k_{2f}[N][O_2] + k_{3f}[N][OH] + 2k_{4f}[N_2O][O] + 2k_{7f}[N_2O][H]$$  \hspace{1cm} (1)

Invoking the N-atom and N$_2$O steady state assumptions as discussed above, Eq. (1) becomes

$$\frac{d[NO]}{dt} = 2[O][N_2](k_{1f} + k_{5f})$$  \hspace{1cm} (2)

The NO-forming eddies, to which Eq. (2) applies, originate just inside zone 1 and are convected outward through zone 1' to zone 2.

Mellor et al. (1998) let $\varepsilon_{NO}$ represent the fractional extent of reaction of NO such that $\varepsilon_{NO} = [NO]/[NO]_{eq}'$, where $0 < \varepsilon_{NO} < 1$ and [NO]$_{eq}'$ is the equilibrium NO concentration from the zone 1 stoichiometric flame temperature calculation adjusted to the overall engine stoichiometry. As shown by Mellor et al. (1998), [NO]$_{eq}'$ is the proper choice as a normalizing factor to constrain $\varepsilon_{NO}$ between the limits of zero and one since it is the largest value among the various zones.

Substituting this definition into Eq. (2) gives

$$d\varepsilon_{NO}/dt = (1/[NO]_{eq}')d[NO]/dt = 2[O][N_2](k_{1f} + k_{5f})/[NO]_{eq}'$$  \hspace{1cm} (3)

The inverse of this equation is the characteristic time for NO formation.
\[ \tau_{no} = \frac{[\text{NO}]_{eq1'}}{2[\text{O}]_{eq1}[\text{N}_2]_{eq1} (k_{1f} + k_{5f})} \]  

(4)

where \([\text{O}]_{eq1}, [\text{N}_2]_{eq1},\) and the rate coefficients are evaluated at the zone 1 burned gas conditions (i.e., the output from the stoichiometric equilibrium calculation based on motored engine conditions at start of combustion).

Also, Mellor et al. (1998) define Zeldovich and N\(_2\)O mechanism formation times as follows:

\[ \tau_{no,1f} = \frac{[\text{NO}]_{eq1'}}{2k_{1f}[\text{O}]_{eq1}[\text{N}_2]_{eq1}} \]  

(5)

\[ \tau_{no,5f} = \frac{[\text{NO}]_{eq1'}}{2k_{5f}[\text{O}]_{eq1}[\text{N}_2]_{eq1}} \]  

(6)

The activation temperatures for \(\tau_{no,5f}\) and \(\tau_{no,1f}\) are 36120 K and 62184 K, respectively. The latter value is typical of the values obtained for NO\(_x\) emissions from conventional gas turbine combustors (see the discussion above).

Recall that \(k_{1f}\) in Eq. (4) and (5), represents the extended Zeldovich mechanism, (R1) through (R3), while the \(k_{5f}\) term in Eq. (4) and (6) is the third-body component, thus sensitive to pressure, originating in the N\(_2\)O mechanism, (R4), (R5), and (R7). In Fig. 1-2 each contribution in Eq. (2) is evaluated in Arrhenius format for typical engine conditions using the kinetic information presented in Mellor et al. (1998).

The figure shows that at low pressures, 1 or 10 atm, NO formation will follow extended Zeldovich kinetics (\(k_{1f}\) exceeds \(k_{5f}\)) over most of the temperature range shown. However, at 10 atm and the lower stoichiometric flame temperatures, obtained with inert injection for example, the N\(_2\)O mechanism will be predominant (\(k_{5f}\) exceeds \(k_{1f}\)). The crossover temperature moves to somewhat higher values as the pressure is increased, and for 60 atm (representative of motored TDC Diesel conditions), the N\(_2\)O mechanism dominates at many stoichiometric temperatures of interest (approximately 2200 to 2460
Figure 1-2. The contribution of the Zeldovich and \( \text{N}_2\text{O} \) mechanisms to the NO formation rate as postulated by Mellor et al. (1998). The information in this figure is presented in Arrhenius format for typical engine conditions. Logarithms are presented as functions of inverse stoichiometric flame temperature in the approximate range from 2200 to 2900 K, so that midrange values correspond to stoichiometric values, with pressure as a parameter.
K). The contribution of this mechanism at higher values of stoichiometric temperature cannot be ignored.

1.4.2 Characteristic Time for NO Decomposition

The characteristic time for NO decomposition is defined in a manner analogous to the characteristic time for NO formation. Writing the law of mass action for the rate of NO decomposition in zone 2 gives (for reasons given by Mellor et al. (1998), the reverse of (R7) is ignored for the present analysis)

\[
\frac{d[NO]}{dt} = - k_{1r}[NO][N] - k_{2r}[NO][O] - k_{3r}[NO][H] - 2k_{4r}[NO]^2 \quad (7)
\]

Expressed in terms of the fractional extent of reaction, and again assuming steady-state N-atom, this equation becomes

\[
\frac{d\varepsilon_{NO}}{dt} = \frac{1}{[NO]_{eq1}} \cdot \left( \frac{d[NO]}{dt} \right) = \frac{- 2k_{1r}[NO][N] - 2k_{4r}[NO]^2}{[NO]_{eq1}} \quad (8)
\]

The inverse of this expression is the characteristic time for NO decomposition

\[
\tau_{no,3b} = \frac{1}{\varepsilon_{NO} \left( 2k_{1r}[N]_{eq2} + 2k_{4r}[NO]_{eq1}\epsilon_{NO} \right)} \quad (9)
\]

The form of this equation demonstrates that NO decomposition is a function of both the reverse Zeldovich mechanism \((2k_{1r}[N]_{eq2})\) and the reverse \(N_2O\) mechanism \((2k_{4r}[NO]_{eq1}\epsilon_{NO})\). Individual decomposition times for the extended Zeldovich and \(N_2O\) mechanisms are respectively expressed as

\[
\tau_{3b,1r} = \frac{1}{2k_{1r}[N]_{eq2}} \quad (10)
\]

\[
\tau_{3b,4r} = \frac{1}{2k_{4r}[NO]_{eq1}} \quad (11)
\]

In an Arrhenius plot similar to Fig. 1-2, Mellor et al. (1998) show that NO decomposition through the reverse \(N_2O\) mechanism is dominant over a range of typical DI Diesel operating conditions \((p = 60 \text{ atm} \text{ and } T_{3b} = 1300 \text{ K to } 2200 \text{ K})\).
1.5 CHARACTERISTIC TIME MODEL FOR NO\textsubscript{X} FROM DIESEL ENGINES

Using the kinetic times defined above, expressions for the engine-out NO\textsubscript{x} emissions are obtained by integrating the laws of mass action over the fluid or residence times available in zones 1-1’ and 2. For NO formation in zones 1-1’, Eq. (3) and (4) are combined such that

\[
\frac{d\varepsilon_{\text{NO}}}{dt} = \frac{1}{\tau_{\text{no}}}
\]  

(11)

where [O] and [N\textsubscript{2}] in \(\tau_{\text{no}}\) are evaluated at constant equilibrium zone 1 conditions.

Equation (11) can be integrated over the eddy lifetime in zone 1-1’, \(\tau_{\text{f1, no}}\), to obtain

\[
\varepsilon_{\text{NO1'}} = m'(\tau_{\text{f1, no}} / \tau_{\text{no}}) = m'D_{\text{a, no}}
\]  

(12)

In Eq. (12), \(\varepsilon_{\text{NO1'}}\) is the fractional extent of reaction for NO formed in zone 1-1’ per stoichiometric eddy, \(m'\) is a scale factor introduced because the magnitude of the characteristic time ratio is unknown at this point, and \(D_{\text{a, no}}\) is the Damköhler number for NO formation in zone 1-1’.

If a portion of the NO formed in zone 1-1’ decomposes in zone 2, then as Mellor et al. (1998) have shown in detail, Eq. (8), (10), and (11) can be used to obtain engine-out emissions such that

\[
\text{NO}_x\text{EI} = \frac{mV_{3b}D_{\text{a, no}}[\text{NO}]_{\text{eq1'}}e^{-D_{3b,1r}}}{m_f\frac{k_{4r}[\text{NO}]_{\text{eq1'}}(1 - e^{-D_{3b,1r}})}{k_{1r}[N]_{\text{eq2}}}}
\]  

(13)

where \(m\) is a model constant incorporating the scaling factor \(m'\) and other conversion constants, \(D_{3b,1r}\) is a Damköhler number based on the eddy lifetime in zone 2 (\(\tau_{d,3b}\)) and the reverse Zeldovich mechanism for zone 2 (\(D_{3b} \equiv \tau_{d,3b}/\tau_{3b,1r}\)), \(m_f\) is the fuel supplied.
per cycle in g, and \( V_{3b} \) is the volume in the cylinder at the end of combustion in cm\(^3\).

Mellor et al. (1998) show that Eq. (13) can be simplified for various limiting cases. In particular, if the eddy lifetime in zone 2 is inadequate so that NO decomposition is negligible (i.e., \( \tau_{3b,3b} \) and \( D_{3b,1r} \) approach zero), then

\[
\text{NO}_x \text{EI} = \frac{V_{3b}}{m_f} D_{3b} \text{Da}_{3b,4r} [\text{NO}]_{\text{eq},t} \tag{14}
\]

Another limiting case of interest consists of adequate time for zone 2 decomposition with dominant \( N_2O \) kinetics (\( k_{1r} \to 0 \)), the most likely case for decomposition as shown by Mellor et al. (1998). For this situation, Eq. (13) reduces to

\[
\text{NO}_x \text{EI} = \frac{V_{3b}}{m_f} D_{3b,4r}^{-1} [\text{NO}]_{\text{eq},t} \tag{15}
\]

where the kinetic time in \( D_{3b,4r} \) is evaluated at \( T_{3b} \).

1.6 APPLICATION OF NO\(_x\) KINETIC MODEL TO DI DIESELS

1.6.1 Determining Significance of NO Decomposition in Diesel Engines

The ratio of the characteristic times for NO decomposition and formation, \( \tau_{3b,\text{no}}/\tau_{\text{no}} \), provides a method to evaluate the importance of the former in any engine situation. This ratio is developed and verified in Mellor et al. (1998). The advantages of using this ratio are its ease of calculation and that it depends only on the fuel and engine operating parameters: engine load, pressure at SOC (\( P_2 \)), temperature at SOC (\( T_2 \)), compression ratio (\( r_c \)), and maximum cylinder pressure (\( P_3 \)).

The effect of various engine operating parameters on the decomposition to formation time ratio is investigated by conducting an equilibrium analysis of various representative engine operating conditions for four DI Diesel engines. The engines examined (three heavy duty and one light duty) are relatively new engines, some of
which are equipped with state-of-the-art NO\textsubscript{x} control systems (EGR and water injection). Configurations with turbocharging and inter/aftercooling as well as naturally aspirated are available. A complete table of engine descriptions is given in Mellor et al. (1998). The variety of engine setups gives a wide range of operating conditions from which to examine the results of the study.

Results of this investigation lead to the following conclusions about the effects of engine operating conditions on $\tau_{3b,\text{no}}/\tau_{\text{no}}$. By far the most important engine operating parameter affecting NO decomposition is load. The higher cylinder temperatures and pressures associated with higher loads increase the rate of decomposition. SOC and peak pressures, injection timing, and fuel properties have negligible effects. Start-of-combustion temperature and compression ratio have small influences masked by changes in load. Inert injection results can be interpreted in terms of their effect on equilibrium concentrations and characteristic temperatures in each zone.

1.6.2 Fluid Mechanic Mixing Times

The CTM equation for the prediction of engine-out NO\textsubscript{x,EI} is given in Eq. (13). In order to use this equation values for the fluid mechanic mixing times $\tau_{\text{fi, no}}$ and $\tau_{3b,3b}$ must be known. A characteristic mixing time can be defined as the time an eddy resides in a characteristic zone before its temperature is lowered to the point that the chemistry of interest is quenched by dilution or expansion. A primary assumption of the model construction done thus far has been that NO forms primarily in zone one and decomposes in zone two. Therefore, the characteristic fluid mechanic mixing time for NO formation ($\tau_{\text{fi, no}}$) is defined as the residence time of a stoichiometric eddy in zone 1. Likewise, the
characteristic mixing time for NO decomposition \( (\tau_{sl,3b}) \) is defined as the residence time of an eddy in zone 2.

Equation (13) includes both formation and decomposition reactions. Of the three unknowns in the equation, two are mixing times and one is a model constant. The model constant is equal to the slope of the linear best-fit line formed by graphing engine-out NO\(_x\)EI versus the appropriate model parameter. Thus, the constant can be solved for once the other two unknowns have been determined and is therefore ignored in the following analysis. The characteristic mixing time for NO decomposition is eliminated from the equation by utilization of low load engine data for which NO decomposition is thought to be negligible \( (\tau_{no,3b} \gg \tau_{no}) \), thereby simplifying the equation to Eq. (14) with only \( \tau_{fi,no} \) unknown.

Engine C data are used for the \( \tau_{fi,no} \) study because these data contain a wide range of operating conditions at low load \( (\tau_{no,3b} \gg \tau_{no}) \). Engine C is a HSDI Diesel with a displacement of 0.55 L/Cyl and is equipped with a turbocharger and intercooler. Mellor et al. (1998) give a full description of the engine. Analysis of Engine C data indicates that NO decomposition can be assumed negligible for loads of 600 kPa and below as discussed in Mellor et al. (1998).

An ongoing literature review gives insight as to which engine parameters should be included in the mixing time. Some of the topics being studied along with key references are listed in Table 1-1. This list is by no means thorough, but does give an idea of the mixing processes examined in the study.

Knowledge gained from the literature review about in-cylinder mixing is used to compile a list of mixing processes important to fuel-air mixing in the cylinder and the
characteristic terms by which they are modeled. Some such terms are: \( \text{We}_{\text{air}} \) – secondary breakup, \( \text{Re}_{\text{air}} \) – turbulence in air, etc. Using this list as a starting point, different

\textbf{Table 1-1. Fluid Mechanic Research Topics}

<table>
<thead>
<tr>
<th>Research Topics</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Effects of cylinder gas density on spray penetration</td>
<td>Nabers and Siebers (1996), Arai and Hiroyasu (1990)</td>
</tr>
<tr>
<td>and dispersion</td>
<td></td>
</tr>
<tr>
<td>Fuel film formation and wall interaction</td>
<td>Stanton and Rutland (1996)</td>
</tr>
<tr>
<td>Engine speed</td>
<td>Uludogan et al. (1996)</td>
</tr>
<tr>
<td>Sauter mean diameter</td>
<td>Hiroyasu et al. (1989)</td>
</tr>
<tr>
<td>Secondary breakup</td>
<td>Arcoumanis et al. (1997)</td>
</tr>
<tr>
<td>Effects of swirl</td>
<td>Timoney and Smith (1996)</td>
</tr>
<tr>
<td>Overall combustion and/or mixing sources</td>
<td>Arcoumanis et al. (1997), Heywood (1988), Ferguson (1986)</td>
</tr>
</tbody>
</table>

definitions of the mixing time are tested to establish the best correlation between engine-out \( \text{NO}_x \text{EI} \) and the CTM model parameter.

A single \( \tau_{\text{f, no}} \) for all Engine C data, assuming NO decomposition negligible, has not yet been obtained. Instead, the data are correlated for the present using two separate empirical mixing times for NO formation. The first applies to cases in which fuel impinges on the cylinder bowl before SOC (wall jet), and the second to cases in which fuel impinges after SOC or not at all (free jet). The mixing times contain identical terms that are related to spray breakup, impingement time, and ignition delay time, but the significance (i.e. exponent) of each term is different for the two cases. The mixing time for the wall jet case is defined as

\[
\tau_{\text{f, no}} = \frac{\text{We}_{\text{air}}^{1.6} \cdot \text{l}_{\text{imp}} \cdot \text{d}_{\text{noz}} \cdot \text{Re}_{\text{fuel}}^{0.5} \cdot \text{u}_{\text{fuel}}}{\text{Re}_{\text{air}}^{1.8} \cdot \text{Re}_{\text{fuel}}^{0.5} \cdot \text{u}_{\text{fuel}} \cdot \text{\tau}_{\text{id}}^{-0.5}} \quad (16)
\]

and the mixing time for the free jet case is found to be
\[ \tau_{n,0} = \frac{We_{\text{air}}^2 l_{\text{imp}} d_{\text{noz}}}{Re_{\text{air}}^{1.6} Re_{\text{fuel}}^{0.8} \rho_{\text{air}}^{0.6}} \]  

(17)

Graphs of NO\textsubscript{x}EI versus the right hand side of Eq. (14) can be found in Fig. 1-3 and 1-4. These graphs use data that meet the criteria of negligible decomposition (load \( \leq 600\text{kPa} \)) and SOC = 0. The linear best-fit lines give correlation coefficient, R, values of 0.9793 and 0.9704 for the impingement before SOC and impingement after SOC cases, respectively. A problem arises with these linear fits in that as \( \tau_{n,0} \) goes to infinity the engine-out NO\textsubscript{x} is expected to go to zero, but for both cases the y-intercept is relatively large. We are evaluating the method of defining \( \tau_{n,0} \) at this time. The lowest engine-out NO\textsubscript{x} datum points seem to indicate the expected y-intercept of zero, however. The graphs presented are preliminary and appropriate fits will be determined after further research.

Currently, our efforts are directed toward improving the empirical mixing times for NO formation. We are hopeful that a single mixing time for NO formation can be found that is valid for start of combustion prior to and following wall impingement. Once a correctly defined mixing time for NO formation is developed for engine C, it will be validated for other engines. With a satisfactory definition of the mixing time for NO formation, work will begin on the mixing time for NO decomposition. When both mixing times have been defined the CTM will be capable of predicting NO\textsubscript{x}EI for any DI Diesel operating condition.

1.7 CHARACTERISTIC TIME MODEL FOR SOOT FROM DIESEL ENGINES

Although the model for soot emissions is in the early stages of development, it is postulated that a two-zone model representing the formation and oxidation of soot will
Figure 1-3. Engine-out NO\textsubscript{X} emissions index versus model parameter (Eq. (14)) for wall jet datum points with SOC = 0. The legend has the format: engine speed (RPM)/load (kPa)/injection pressure (MPa). Each set of data is obtained via an EGR sweep.
Figure 1-4. Engine-out NO\textsubscript{x} emissions index versus model parameter (Eq. (14)) for free jet datum points with SOC = 0. The legend has the format: engine speed (RPM)/load (kPa)/injection pressure (MPa). Each set of data is obtained via an EGR sweep.
properly model this exhaust emission. Figure 1-5, based on past laser sheet images (see Dec, 1997), shows a schematic of a Diesel spray plume with the pertinent zones where soot is forming and oxidizing. Dec (1997) postulates that during the diffusion flame (mixing controlled) combustion, a thin premixed flame will form at the liquid/vapor fuel interface, and initiation of soot occurs just downstream of this flame in the products of rich combustion. Soot will then continue to form in the vapor fuel core, where a hypothetical homogeneous mixture with $\phi \approx 3$ exists, until it reaches the diffusion flame front. Thus, soot formation is assumed to occur spatially in the vapor core of the spray, labeled zone 1 in Fig. 1-5. For the oxidation of soot, Dec (1997) shows that due to the large concentrations of hydroxyl (OH) radicals in the diffusion flame, the majority of soot oxidation will occur in this location. This assumption is further supported through the work of Dec and Coy (1996) and Kosaka et al. (1995). For modeling purposes, it will be assumed that soot oxidation is initiated at the stoichiometric contour of the fuel spray and continues out into the periphery of the flame (see Fig. 1-5).

The representative temperature of zone 1, $T_{sf}$, is defined as an average of 2 limiting temperatures, namely the 50% fuel recovery temperature, $T_{50\%}$, and the $\phi = 3$ flame temperature, $T_{\phi = 3}$, where $T_{\phi = 3}$ is calculated using TDC cylinder conditions as done for $T_{\phi = 1}$. The temperature indicative of zone 2, $T_{50}$, is defined as the average of the stoichiometric and end of combustion temperatures, $T_{\phi = 1}$ and $T_{3b}$.

Assuming the presence of soot formation and oxidation, the emissions model for soot was developed following the approach used by Mellor et al. (1998) to derive the NO$_x$ CTM, except that global reactions for soot formation and oxidation will be used instead of a skeletal mechanism because of the complex chemistry involved in the
Figure 1-5. Schematic of a DI Diesel spray plume with regions of soot formation and oxidation labeled.
formation and oxidation of soot. This is consistent with the work of others to model soot emissions from Diesel engines (see for example, Nishida and Hiroyasu, 1989).

Following the methodology used in developing the NO\textsubscript{x} CTM, the overall reactions used to model soot formation and oxidation are as follows:

\[ \text{Fuel} \rightarrow \text{Soot} \]  \hspace{1cm} (18)

\[ \text{Soot} + \text{OH} \rightarrow \text{CO}_2 \]  \hspace{1cm} (19)

Applying the law of mass action to Eqs. (18) and (19) gives

\[ \frac{d[\text{soot}]}{dt} \bigg|_{\text{form}} = k_{sf} [\text{fuel}] \]  \hspace{1cm} (20)

\[ \frac{d[\text{soot}]}{dt} \bigg|_{\text{oxid}} = -k_{so} [\text{soot}] \cdot [\text{OH}] \]  \hspace{1cm} (21)

In Eq. (20) it is assumed that soot has a first order of dependence on fuel. Now integrating Eqs. (20) and (21) over the lifetime that eddies spend in the soot formation and oxidation zones, \( \tau_{sf} \) and \( \tau_{so} \), respectively, yields

\[ \frac{[\text{soot}]}{[\text{fuel}]} = m_{sf} \frac{\tau_{sf}}{\tau_{sl, sf}} = m_{sf} \cdot D_{sf} \]  \hspace{1cm} (22)

\[ \frac{[\text{soot}]}{[\text{soot}]} = e^{-m_{so} \frac{\tau_{so}}{\tau_{sl, so}}} = e^{-m_{so} D_{so}} \]  \hspace{1cm} (23)

where \( \tau_{sf} = 1/k_{sf} \), \( \tau_{so} = 1/k_{so} [\text{OH}] \), and \( m_{sf} \) and \( m_{so} \) are model constants. For Eq. (23) it is assumed that [OH] is in steady state, which is based on the work of Tuttle et al. (1977) for the CO CTM. However, further development of this model by Connors et al. (1996) incorporates a first order dependence of [OH]. The concentrations \([\text{soot}]_1\) and \([\text{soot}]_2\) in Eq. (23) represent the amount of soot formed in zone 1 and the total soot remaining after
oxidation in zone 2 has ceased, where the amount \([\text{soot}]_2\) is dependent on the soot formed in zone 1.

The kinetic times associated with each of the chemical processes will be represented as inverse Arrhenius expressions:

$$\tau_x \sim \exp\left(\frac{E_x}{RT_x}\right)$$

with \(E_x\) and \(T_x\) the global activation energy and representative temperature, respectively, for each process.

The engine-out soot, in units of emissions index of soot, is obtained by combining Eqs. (22) and (23):

$$\text{SootEI} \propto \frac{[\text{soot}]_2}{[\text{fuel}]} = m_\text{af} Da_{af} \cdot e^{-m_\text{af} D_{af}}$$

(25)

The soot model, Eq. (25), includes the competition between soot formation and oxidation with each process represented by the Damköhler numbers \(Da_{af}\) and \(D_{so}\), respectively.

Tuttle et al. (1977) showed the exponential term in the CO CTM, similar to that in Eq. (25), can be approximated by a series expansion of \(\tau_{so}/\tau_{sl,so}\):

$$e^{-m_\text{af} \tau_{sl,so}/\tau_{so}} \approx a_0 + a_1 \frac{\tau_{so}}{\tau_{sl,so}} + a_2 \left(\frac{\tau_{so}}{\tau_{sl,so}}\right)^2 + \ldots$$

(26)

where the coefficients \(a_0, a_1, a_2 \ldots\) are determined through best fitting. Furthermore, Tuttle et al. (1977) found that neglecting the squared and higher terms for their measurements results in errors of less than one percent. If the same holds true for soot data, then the exponential term in Eq. (25) can be represented by the two term expansion resulting in the following:

$$\text{SootEI} \propto m_\text{af} Da_{af} \left( a_0 + a_1 \frac{\tau_{so}}{\tau_{sl,so}} \right)$$

(27)
Equation (27) represents the final soot model, where the coefficient $m_{sf}$ is determined from the best-fit slope of experimental data of SootEI plotted versus $Da_{af}$ times the bracketed term. Although Eq. (27) is preliminary, a point of departure would be to assure that the combination of both the NO$_x$ and soot models is capable of predicting the trends existing between these exhaust emissions under various engine operating conditions.

1.8 NO$_x$ – SOOT EMISSION TRENDS

1.8.1 Diesel Engine Performance

Since the Diesel engine is used in a number of applications, from large, heavy-duty (HD) engines for the military in combat vehicles to the smaller light-duty (LD) Diesels in small trucks and automobiles, performance requirements demand engine operation over wide load and speed cycles. The transient conditions under which commercial vehicles operate require Diesel engines to typically run at three quarter to full load (see Mori, 1997), while military vehicles spend the majority of time at low load conditions. These different load cycles result in different engine performance requirements which in turn lead to changes in the trends existing between NO$_x$ and soot emissions.

Since any emissions model must be capable of predicting the changes in trends of exhaust emissions with varying engine operating conditions, examination of a performance map for DI Diesel engines is beneficial. Figure 1-6, a typical performance map, describes the effects of load and speed variations on bsfc (Heywood, 1988). The performance map shows that at approximately 50% load and speed, the best fuel economy of the engine is obtained. Note for the engine of Fig. 1-6, the maximum attainable load is limited to about 800 kPa bmep due to the smoke limit of the engine.
Figure 1-6. Performance map for a naturally aspirated DI Diesel engine (Heywood, 1988).
The Blue Ribbon Committee Report (BRC, 1995) shows the tradeoff between load (bmep) and bsfc through the relationship to the power density of a Diesel engine ($\rho_d$), defined as the engine output divided by the volume of the engine plus accessories (i.e., turbocharger, air filter, etc.):

$$\rho_d \propto \text{bmep} \propto (\rho_a)(\phi)(1/\text{bsfc}) \tag{28}$$

where $\rho_a$ is the cylinder inlet air density and $\phi$ the equivalence ratio. From Eq. (28), the highest $\rho_d$ would be obtained by a turbocharged (increased $\rho_a$) engine operating under rich conditions with low bsfc; however, rich operating conditions will result in higher particulate and bsfc (BRC, 1995). The tradeoff in Eq. (28) between bmep and bsfc translates into different trends existing between NO$_x$ and soot.

The work of Wilson et al. (1973) and Murayama et al. (1978) clearly exhibits the effects that increasing load has on bsfc and emissions of soot and NO$_x$ for a constant speed. As the load (or $\phi$) is increased, NO$_x$ and soot emissions simultaneously increase until a maximum value of NO$_x$ is reached, after which a further increase in load yields a decrease in NO$_x$ and a continued increase in soot. The initial increase in NO$_x$ with load corresponds to the decrease in bsfc; once the minimum in bsfc is obtained, roughly coinciding with the maximum NO$_x$, any further increase in load results in a decrease in NO$_x$ that is caused not only by the increase in bsfc, but also extended burning into the expansion stroke causing reductions in peak gas temperature and increased heat losses so the production rate of NO is reduced, according to Wilson et al. (1973). As discussed in the previous sections, an alternative interpretation of the results involves increased decomposition of NO as load is increased.
The above discussion suggests that there are two different trends present between NO\textsubscript{x} and soot emissions with varying load: 1) low load cases (≤ 50% load) show an increase in NO\textsubscript{x} and soot with increasing load and 2) higher load cases (≥50%) where the typical NO\textsubscript{x}/soot tradeoff exists. Algebraic expressions are derived below from the NO\textsubscript{x} and soot CTMs to prove that the overall model will properly predict the trends of NO\textsubscript{x} and soot emissions, regardless of operating conditions.

1.8.2 Derivation of NO\textsubscript{x}-Soot Trends Using the CTM

To derive the NO\textsubscript{x}/soot emissions equations for Diesel engines, a relationship between the NO\textsubscript{x} and soot CTM is needed. The link in the derivation is the mixing times involved in the models for NO\textsubscript{x} and soot emissions. The zonal assumptions of the NO\textsubscript{x} and soot CTMs indicate that NO is forming at the diffusion flame front, which as noted previously is the same spatial region for soot oxidation initiation. Therefore, a possible relationship between these two mixing times may exist and could be used in the derivation of the NO\textsubscript{x}/soot tradeoff equations.

Analysis of the Engine C data leads to an expression for the mixing time associated with NO formation, \( \tau_{fi,NO} \), where NO\textsubscript{x} has a first order dependence with pressure drop, \( \Delta P \), across the injection nozzle, and a \(-1.6\) order of dependence with engine speed (Eq. 17). A similar analysis for Engine C soot data was performed to determine the dependency of soot with each of the above operating parameters; however, the chemical kinetics for the soot model are not yet fully developed, so engine conditions must be such that only the engine parameter of interest (i.e., \( \Delta P \) or \( N \)) is varying. For

\[ \text{Analysis only includes data where NO decomposition is negligible (200-600 bmep range) and the injected fuel ignites prior to impinging on the piston bowl wall (free jet).} \]
example, soot data for constant load, EGR and injection pressure were used to determine
the order of dependence of soot with engine speed. The results show that soot has an
approximate third order dependence with engine speed, which is twice the inverse of that
found for NO\textsubscript{x} and slightly higher than the value used by Plee et al. (1981). There is no
single order dependence of soot on ΔP; instead the magnitude of dependence varies with
EGR (i.e., increasing EGR decreases the order dependence). However, in general the
analysis did reveal that soot emissions will have an inverse dependency on ΔP, opposite
the dependency found for NO\textsubscript{x}, which is expected.

Several major issues arose during the above analysis of the soot emissions from
Engine C. The first problem was that the yet-to-be-determined chemical kinetics for soot
formation and oxidation act as a constraint and eliminate many datum points since only
ΔP or N variations can be considered, while load, EGR, and SOC are constant. Thus,
more datum sets with only ΔP or N changing are needed in order to ensure that the
obtained dependencies of soot with ΔP and N are well understood. Another issue
concerning the available data is the lack of high load run conditions. These higher load
data are required to test and ensure that the CTM will properly predict soot over the entire
load cycle, not just at low loads.

Although there exist some questions about the data available for analysis, the
overall trends of soot emissions with ΔP and speed are consistent with those reported by
Plee et al. (1981); therefore, the NO\textsubscript{x}/soot proportionality can be derived for these data.
In general, it has been shown that soot has an inverse and perhaps a higher order of
dependence on ΔP and N than found for NO\textsubscript{x}. These results would suggest the mixing
times associated with soot oxidation and NO formation are inversely proportional.

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By solving for \( \tau_{fi,so} \) and \( \tau_{sl,so} \) in Eqs. (14) and (27), respectively, and substituting these new expressions into Eq. (29), the following NO\(_x\)/soot equation is obtained:

\[
\tau_{fi,so} \propto \frac{1}{\tau_{sl,so}}
\]  

(29)

Equation (30) shows that the NO\(_x\) and soot emissions are directly proportional for the lower load data, which is consistent with the trends shown by Wilson et al. (1973) and Murayama et al. (1978). Higher load data will be required to determine the relationship existing between the mixing times associated with NO\(_x\) and soot emissions. The higher load data are expected to exhibit the NO\(_x\)/soot tradeoff obtained through “normal” vehicle operation.
2.0 PUBLICATIONS AND TECHNICAL REPORTS


Various Internal Ford Reports, Ford Motor Company, Dearborn, MI.
3.0 PARTICIPATING PERSONNEL

Mellor, A.M., Centennial Professor, Mechanical Engineering Department, Vanderbilt University, Nashville, TN.

Plee, S.L., Director, Systems Engineering, Motorola, Inc., Dearborn, MI.

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Duffy, K.P., Ph.D. Candidate.

Gurtner, D., M.S.

Mello, J.P., M.S. Candidate.

Easley, W.L., M.S. Candidate.

Psota, M.A., M.S. Candidate.

A number of undergraduate students participated throughout the program as well.
4.0 REPORT OF INVENTIONS

No inventions were made under the sponsorship of the grant.
5.0 REFERENCES


Murayama, T., Morishima, Y., Tsukahara, M. and Miyamoto, N. (1978), "Experimental reduction of NO\textsubscript{x}, smoke, and BSFC in a Diesel engine using uniquely produced water (0 – 80%) to fuel emulsion," SAE Paper 780224.


Plee, S. L., Ahmad, T. and Myers, J. P. (1981), "Flame temperature correlation for the effects of exhaust gas recirculation on Diesel particulate and NO\textsubscript{x} emissions," SAE Paper 811195.


