Comparing ADA and FORTRAN Lines of Code: Some Experimental Results

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This paper presents the results of an experiment in rewriting four FORTRAN programs in the Ada computer language. We counted and compared the numbers of lines of code in both languages. We found Ada programs to be larger than their functionally equivalent FORTRAN counterparts. However, we observed that the overhead for Ada diminishes as the program size is increased. Our limited data suggested that there may even be a cross-over point beyond which the size of an Ada program is smaller than a functionally equivalent FORTRAN program.
COMPARING ADA AND FORTRAN LINES OF CODE:
SOME EXPERIMENTAL RESULTS

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PREFACE

This paper was prepared by the Institute for Defense Analyses (IDA) under the IDA Independent Research Program. The objective of the research was to compare the relative sizes of functionally equivalent programs written in the Ada and FORTRAN computer languages.

This paper was reviewed by Bruce N. Angier and D. Graham McBryde.
I. INTRODUCTION

A. BACKGROUND

The introduction of the Ada computer programming language in the early 1980s has been cited as one of the major weapons in the fight to reduce the proliferation of computer languages and to control the cost of software in the Department of Defense (DoD). The features of the Ada language were carefully chosen to enable good engineering practices and structure to be imposed during the development and maintenance of computer software. However, the use of these structural and engineering features presents new problems for the cost analysts responsible for estimating either the size or the cost of software systems to be developed in Ada.

Most software cost-estimating models in use today assume that the cost of developing a computer program is a function of the size of the program (plus other representations or measures of the complexity of the program), the skills and experience of the programmers, and other factors that affect cost. Typically, these cost models use lines of code as a representation of the size of a software program or project. For example, Reference [1] employs the following relationship between effort to develop software and the size of the code

\[ E = \alpha (KLOC)^\beta \prod_i m_i, \]

where \( E \) is defined to be the staff-months of development effort, \( \alpha \) and \( \beta \) are the parameters that have been previously estimated, \( KLOC \) is defined as thousands of source lines of delivered code, and \( m_i \) are multipliers or cost drivers that account for differences in software product attributes, computer attributes, personnel attributes and project attributes.

The use of a line of code as a unit of measure is appropriate and effective when dealing with line-oriented languages such as FORTRAN or assembly languages. However, several problems arise when applying a FORTRAN-specific or line-oriented cost model to software being developed in Ada.

First, instead of being line-oriented, Ada is block-oriented, which means its statements and declarations can span several lines or be nested within one another. This
implies that, instead of simply counting carriage returns, a special Ada-specific way of counting the effective number of lines in an Ada program is needed. Further, even given a way of measuring the size of an Ada program by some method of line counting, there is no assurance that a line of Ada by this definition will capture the same amount of function as a line of FORTRAN. This means that two functionally equivalent programs in the two languages might be considerably different in size, as measured by lines of code. Finally, there is no assurance that the cost to develop a line of Ada by this definition will be the same as the cost to develop a line of FORTRAN.

B. OBJECTIVE

This paper addresses the functional size issues but not the programming effort issues raised when comparing the sizes of Ada and FORTRAN programs. However, there are currently no standard rules for normalizing the sizes of Ada developments and FORTRAN developments with respect to the functionality delivered.

Information about the relative sizes of functionally equivalent programs is needed by any organization that is considering a transition to the use of Ada in application areas in which they have previous experience in FORTRAN. The reasoning is that such an organization would be able to estimate the size of a programming job if it were developed in FORTRAN. However, it would have no way of knowing whether an Ada solution would be more or fewer lines of code. What is needed is the added knowledge about how large an Ada solution to a problem will be, given an estimate of size for a FORTRAN solution. This knowledge will allow FORTRAN organizations to “bootstrap” their software cost-estimating capabilities to include developments in the Ada language. Eventually, the need for this stop-gap technique will be eliminated by first-hand experience with Ada.

The focus of this study can be expressed in algebraic terms. The relationship between effort and size in line-oriented languages such as FORTRAN has been studied extensively by software engineers and cost analysts [3] and can be represented by equation (2),

\[ E_r = \alpha(KLOC_r)^\rho \prod_i m_i, \]

---

1 The programming effort issues can be addressed by observing the cost required to develop Ada programs of various sizes. There are several databases containing observations of productivity on Ada projects. One of the best examples is the work done at the MITRE Corporation and reported in Reference [2].
where the subscript $F$ denotes FORTRAN. Researchers are learning about the relationship between effort and size in block-oriented languages such as Ada as represented by equation (3),

$$E_A = \delta(KLOC_A)^r \prod_i m_i,$$

where the subscript $A$ denotes Ada.

What is less known is the relationship between the size of an Ada program and a functionally equivalent FORTRAN program, or

$$KLOC_A = f(KLOC_F).$$

We focus on FORTRAN because the impetus for this research stems from the Institute for Defense Analyses’ work for the Strategic Defense Initiative Organization (SDIO). Space systems have historically employed FORTRAN for both the ground segment software and the software embedded in the spacecraft or satellite itself. Cost-estimating relationships using FORTRAN lines of code have been the rule. However, the SDIO plans to field space systems software that will be predominately written in Ada. By determining the differences in size between functionally equivalent FORTRAN and Ada programs, this study will further our understanding of how traditional FORTRAN cost- and size-estimating models will have to be adjusted to handle the Ada language. In addition, by understanding the differences in size between functionally equivalent FORTRAN and Ada programs, we can estimate the error incurred by cost analysts when they simply use Ada and FORTRAN lines-of-code counts interchangeably.
II. APPROACH

In order to compare the sizes of functionally equivalent Ada and FORTRAN programs, we devised a simple experimental procedure. The procedure involved rewriting standard FORTRAN programs and routines using the Ada language. First, we developed an Ada solution for each program using the features of Ada as appropriate, such as packages and user-defined types. Because programming style can affect program size, we also wrote both terse and verbose versions of each of the FORTRAN and Ada programs. This yielded six functionally equivalent versions of each algorithm studied—three in FORTRAN and three in Ada. We then selected two established definitions for an Ada line of code and compared the number of Ada lines of code in these new programs to the number of lines in the original FORTRAN programs.

This chapter describes the test programs we selected and the formatting and code-counting conventions we employed.

A. TEST PROGRAMS

A total of four FORTRAN routines were used in the experiment. Three FORTRAN routines and their drivers were taken from *Numerical Recipes in FORTRAN* [4]. The National Aeronautics and Space Administration (NASA) Software Engineering Library (SEL) supplied the fourth FORTRAN program [5], along with an Ada translation, which we adapted for our basic Ada version of the program. Terse versions of the FORTRAN routines were devised by taking “shortcuts,” such as allowing implicit declarations and eliminating certain unnecessary statements, such as format statements and continue statements. Verbose versions were devised by separately declaring variables, adding explicit format statements, and adding other optional statements to improve clarity. The terse versions of the Ada routines were devised by allowing multiple variables to appear in a single declaration and by using only positional parameter associations. The verbose versions were devised by separately declaring all variables and by using named parameter associations. By having a terse, normal, and verbose version of each algorithm in each language, we were able to obtain a useful picture of how the range of possible program sizes for a given function would differ in the two languages.
The three routines selected from *Numerical Recipes* were:

- **Quicksort**—a sorting routine that uses a “partition-exchange” sorting method.
- **Fast Fourier Transform (FFT)**—a computational algorithm that relates physical processes defined either in the time domain or frequency domain.
- **Moments of a Distribution**—a statistical routine that computes the moments (e.g., mean, variance, kurtosis) of a given distribution.

A fourth routine, an orbit propagator provided by the NASA/SEL, computes the orbital position of an earth satellite. These four were selected because they cover a range of computational applications likely to be used in space systems, and the algorithms involved are well known and widely used.

### B. ADA AND FORTRAN FORMATTING AND STYLE

For comparisons we used two methods to measure the size of each of the Ada and FORTRAN subprograms and their drivers. Method 1 involves adopting a specific style for the formatting of the code and then simply counting the number of non-comment, non-blank lines in the file containing the code. The most complete definition we found for Ada formatting and style was “Ada Quality and Style: Guidelines for Professional Programmers” [6]. Except when deliberately employing either a verbose or a terse format, we adopted those rules of style for the examples of Ada used in this report. For the style of the FORTRAN examples, we followed the conventions detailed in *American National Standard Programming Language FORTRAN* (ANSI FORTRAN) [7]. This standard was adopted by the DoD in 1978.

Method 2 is a count of the number of source statements that appear in the code. Because this method measures the number of logical statements it is not sensitive to the number of physical lines a statement occupies. It is therefore not sensitive to formatting, comments or blank lines. Because of the multiple declaration option in Ada, this method is still somewhat sensitive to programming style, however. The specific declaration and statement counting rules we followed for both methods are described in “Code Counting Rules and Category Definitions/Relationships” [8]. To be consistent with the terms used in that report, we call Method 1 the physical source statement count, or the PSS count, and Method 2 the logical source statement count, or the LSS count.²

² The definitions of PSS and LSS are identical to the definitions in [9].
Although Reference [8] also discusses how to count comments in each language, we chose to ignore all comments and blank lines when measuring the sizes of our examples for this study. Also, we adopted the definition for a source statement to mean any programming instruction. In other words, all Ada declarations, statements, and pragmas are counted as source statements. In FORTRAN a source statement can be an executable statement, a data declaration, or a compiler directive.

C. CODE-COUNTING CONVENTIONS: SIZING ISSUES

The two selected methods for measuring program size are each compromises between the amount of the information captured by a size measure and the complexity of taking the measurement. The PSS method requires the program to be first formatted according to a set of rules and then simply counts the number of carriage returns in the code, excluding blank lines and comments. This approach either requires that a particular style be followed by the code developers or that a formatter (or "pretty printer") be used before any line counting is done. The LSS method defines a method for counting syntactic units rather than counting lines at all, so that the formatting of the code is immaterial. This LSS approach can be useful when reporting size outside of an individual development organization where styles and formatting rules may differ. However, it requires the additional complexity of processing or parsing the code in order to obtain the size count automatically.

Each statement, declaration, or pragma in Ada terminates with a semicolon (";"). Semicolons are also used to separate formal subprogram and entry parameters. Computing LSS means counting the semicolons except when they appear in (1) comments, (2) character literals, and (3) string literals. We decided to count the semicolons in formal parameter lists because formal parameters are, in effect, declarations. Although this count always misses the last parameter, we felt that correcting for this small effect was not worth the added complexity. A logical source statement in FORTRAN can be computed by counting only those lines that have the blank character in column 1 and either a blank or a zero in column 6. This follows from the convention that comments in FORTRAN are identified as those lines with the character "C" or "*" in column 1, while continuation lines have any character except a blank or a zero in column 6. This rule, therefore, counts only non-comment, non-continuation lines. In structured FORTRAN (such as that used in our examples) the statement "end if" is not counted as a logical source statement but it is included in the count of physical source statements.
The difference between the PSS and LSS methods and how they apply to counting code in Ada and FORTRAN can best be illustrated through a simple example. Table II-1 shows a portion of the FORTRAN and Ada code found in the Fourier analysis subroutine.

**Table II-1. Comparison of Ada and FORTRAN “if...then” Statements**

<table>
<thead>
<tr>
<th>FORTRAN</th>
<th>LSS</th>
<th>Ada</th>
<th>LSS</th>
</tr>
</thead>
<tbody>
<tr>
<td>if (j.g.l.l)then</td>
<td>✓</td>
<td>if J &gt; I then</td>
<td>✓</td>
</tr>
<tr>
<td>temp= data(j)</td>
<td>✓</td>
<td>Temp := Data (J);</td>
<td>✓</td>
</tr>
<tr>
<td>temp+i=data(i+1)</td>
<td>✓</td>
<td>Data (J) := Data (I);</td>
<td>✓</td>
</tr>
<tr>
<td>data(i)=data(i)</td>
<td>✓</td>
<td>Data (I) := Temp;</td>
<td>✓</td>
</tr>
<tr>
<td>data(i+1)=data(i+1)</td>
<td>✓</td>
<td>end if;</td>
<td>✓</td>
</tr>
<tr>
<td>data(i)=temp</td>
<td>✓</td>
<td></td>
<td></td>
</tr>
<tr>
<td>data(i+1)=temp+i</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>end if</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The portion of the subroutine is an “if...then” statement written in the styles according to the references noted above. (Capitalization is not significant in either language. The lower-case convention used in the FORTRAN example is adopted from [4].) The Ada PSS count is five and the FORTRAN PSS count is eight. The Ada LSS count is four and the FORTRAN LSS count is seven. There are four semicolons in the Ada code. The “end if” in the FORTRAN code is not counted as a logical statement since it is required by and part of the “if” statement.
III. RESULTS

In this chapter we examine the results of applying the code and style conventions discussed in the preceding chapter to the four test programs. We examine some of the differences between Ada and FORTRAN that might explain the results, and we discuss the notion that the Ada language exhibits scale economies (i.e., as the size of the program grows the number of Ada lines grows slower than the size of an equivalent FORTRAN program). Finally, we discuss the effect of our results on the practice of software cost estimating.

A. PSS AND LSS COUNTS

The results of applying the code-counting methods to the FORTRAN and Ada examples using the conventional programming style examples are summarized in Table III-1.

<table>
<thead>
<tr>
<th>Program</th>
<th>FORTRAN PSS</th>
<th>FORTRAN LSS</th>
<th>Ada PSS</th>
<th>Ada LSS</th>
<th>Ada/FORTRAN PSS</th>
<th>Ada/FORTRAN LSS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Quicksort</td>
<td>92</td>
<td>79</td>
<td>141</td>
<td>106</td>
<td>1.53</td>
<td>1.34</td>
</tr>
<tr>
<td>Moments</td>
<td>68</td>
<td>61</td>
<td>124</td>
<td>109</td>
<td>1.82</td>
<td>1.78</td>
</tr>
<tr>
<td>Fourier</td>
<td>133</td>
<td>115</td>
<td>189</td>
<td>147</td>
<td>1.42</td>
<td>1.27</td>
</tr>
<tr>
<td>Orbit</td>
<td>1,101</td>
<td>803</td>
<td>1,382</td>
<td>1,065</td>
<td>1.25</td>
<td>1.32</td>
</tr>
</tbody>
</table>

There are several interesting aspects to the results. The PSS count is always greater than the LSS count. The Ada code count is in every case greater than the FORTRAN code count. The Ada code count is, on average, 50-percent greater than the FORTRAN count when measured by PSS. The Ada code count is, on average, 40-percent greater than the FORTRAN count when measured by LSS. McGarry and Agresti, in an experiment of parallel development of flight dynamics systems by two teams of programmers, one team using FORTRAN and the other team using Ada, reported the Ada product was significantly larger (measured by PSS) than the FORTRAN product by a factor of almost three [10]. McGarry and Agresti posit three reasons for the large difference in the counts. First, the characteristics of the Ada language itself (about which more will be said in the next
sections). Second, additional functionality was built into the Ada version (the Ada team developed a more contemporary screen-oriented user interface). Third, the Ada version was not driven by tight schedules and funds as was the FORTRAN version; thus, there was a tendency to continually add capability to the Ada version. Our experiment controlled for the latter two factors. Our results also indicate that as the size of the program grows, the difference between the FORTRAN and Ada counts falls. This result suggests that Ada exhibits economies of scale relative to FORTRAN.

In order to determine if the observed differences between the Ada and FORTRAN code counts are statistically significant, we conducted a nonparametric test. We would expect Ada to be greater than FORTRAN half of the time and less than FORTRAN half the time. As noted, the Ada program code counts were always greater than the FORTRAN counts. Obviously, we would reject the null hypothesis that the Ada and FORTRAN counts were the same. One might wonder whether the same results would be observed if the programs were decomposed into their smaller constituencies. We decomposed the four programs into 17 corresponding modules. In only one out the 17 components was the Ada component not larger than the equivalent FORTRAN component. Here again we would reject the null hypothesis that the Ada and FORTRAN counts were the same.

In carrying out this experiment, we observed that FORTRAN, like Ada, has optional variations in style that can change the number of lines in a subroutine depending on the formatting used. We also observed that certain kinds of statements, such as input and output statements, were more verbose in Ada than in FORTRAN, while other kinds of statements, such as assignments to structured data, could be expressed more efficiently in Ada. The affect of these variations in style are discussed in detail in the next two sections.

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3 The nonparametric test that we conducted was the sign test. To test the hypothesis that Ada code counts are greater than FORTRAN code counts, we needed to determine whether the null hypothesis (code counts are the same) could be rejected at a specific level of significance $\alpha$. The null hypothesis can be rejected if $x \geq k_a$, where $x$ is the number of positive differences (i.e., Ada code count is greater than FORTRAN code count) and $k_a$ is the smallest integer that satisfies

$$P(x \geq k_a) = \sum_{x = k_a}^{n} \binom{n}{x} \left( \frac{1}{2} \right)^x \left( \frac{1}{2} \right)^{n-x} \leq \alpha,$$

where $n$ is the sample size. When the sign test was performed on the four programs, the null hypothesis could not be rejected at the 5-percent level of significance. However, at the 10-percent level, we rejected the null hypothesis and concluded that the Ada code counts are greater than FORTRAN. We then conducted the sign test on the 17 components and rejected the null hypothesis at the 5-percent level.
B. DECLARATIONS

This section discusses specific issues with respect to how declarations can be counted in both Ada and FORTRAN and why we chose to write and count them as we did.

FORTRAN allows the implicit declaration of variables, where the data type is implied by the first letter of the name (beginning a symbolic name with the letters "I" through "N" implies an integer while any other letter implies a real number). In spite of this allowance, most programming practices now dictate explicit declaration as a way of avoiding certain kinds of errors. Nevertheless, it is common in FORTRAN to use a single statement to declare all the variables of a certain type rather than to place each declaration on a separate line. Conversely, most of the guides about Ada style recommend using a separate line for each declaration. This allows the initialization of variables during the elaboration of their declarations, and also improves the maintainability of the code, though it tends to inflate both the LSS and the PSS for Ada when compared with FORTRAN. As discussed earlier, in order to understand the variability in program size due to the observance of these and other conventions, we wrote and compared both terse and verbose versions of each routine in each language.

Another stylistic issue that tends to increase the size of a program written in Ada over a similar one written in FORTRAN is the use of descriptive names. Since FORTRAN symbolic names are limited in length to six characters [7, section 2.2] it is often easier to fit a long expression that contains several names on a single line. In several of our examples, multiple editor lines were required to write an expression in Ada that took only one line in FORTRAN. One might argue that the descriptive choice of names in Ada might reduce the need for in-line commentary as compared with a corresponding FORTRAN program, meaning that the effect on the size of a fully commented program may be counterbalanced. However, since we did not study the effects of commenting on program size, we did not attempt to investigate this possibility. Further, this issue only affects the physical source statements (PSS) and not the count of statements and declarations (LSS).

In Ada, formal parameters are declared along with the name of a subprogram, rather than in a subsequent declarative area, as is the case with FORTRAN. The effect of this on size is often canceled out, depending on the counting method used, because this practice makes the program unit declaration longer in Ada, but it eliminates the need to repeat the parameter names in a later declaration.

Ada allows, but does not require, the declaration of a library-level subprogram (i.e., a procedure or function) to be compiled separately from its executable body. If this
separation is not done, the number of lines needed to write a given program will be reduced. However, most style guides recommend the addition of these lines because it can greatly reduce the recompilation effort required if a subprogram body is modified. A separate subprogram declaration can also be used within a declarative area, usually to allow mutual visibility between two locally-declared subprograms. In the case of subprograms exported from a package declaration, the subprogram declarations are always separated from their bodies, which appear in the package body. In all these cases, however, the extra programming effort required to provide a separate subprogram declaration is negligible because it is simply a verbatim repetition of the specification part of the subprogram body. In fact, some Ada development environments automatically complete the repeated syntax so that no additional typing or editing is required of the programmer. (It might be argued that maintenance is made more complicated by this syntactic duplication in the language since both copies have to be modified in the case of a change. However, the more likely maintenance situation is a change to the unique code in a subprogram body rather than the redundant interface code in the specification.) For these reasons, one might argue that separate subprogram declarations should not be included in the size of a program. However, we deemed it not worth the added complexity of defining counting rules to compensate for this.

Since FORTRAN does not allow the definition of structured data types, arrays are often used for various logical data structures. This simplifies the declaration of such structures, because it requires only a dimension statement, but at the possible expense of more elaborate processing later in the program. To assign an array value to an array object in FORTRAN, it is necessary to use a loop that explicitly assigns each component. In comparison, Ada array objects contain implicit information about their own size and bounds, which allows the array objects to be assigned to one another with single assignment statements.

The manipulation of arrays that represent nested data structures can require even more complexity. For example, the FORTRAN version of the fast Fourier transform used in one of our examples uses an array of real numbers to represent an array of complex numbers. The odd-indexed values are the real parts and the even-indexed values are the imaginary parts. This practice required the “do” loops to use an increment of two rather than one each time the complex numbers were processed. When we initially translated the programs into Ada, extra statements were required to implement these loops because Ada does not allow “for” loops that skip values in the loop range. When the algorithms were
written in a more appropriate Ada style using structured data, however, the loops were reduced to half the number of statements required by their FORTRAN equivalents.

C. STATEMENTS

This section presents issues with respect to how statements can be written and counted in both Ada and FORTRAN.

One of the most noticeable differences in program size between Ada and FORTRAN programs was in the statement areas used for input and output. Because Ada allows only a single value to be either input or output with each statement, the translation into Ada of a formatted FORTRAN input/output statement often resulted in considerable expansion. This effect can be clearly observed by comparing the driver routines in Ada and FORTRAN for the example engineering algorithms. For example, the three “write” statements in the driver for the Fourier transform routine required five statements, while the same output in Ada required 27 statements.

One of the stylistic issues that allows a single FORTRAN program to be written with different numbers of lines is the use of separate “format” statements when specifying input and output columns rather than including this information directly in the “read” or “write” statements. Our FORTRAN program examples, which were originally written without “format” statements, were re-styled to conform to the conventions found in [7] in order to make them representative of industry programming standards. Note that the verbose and terse versions of the FORTRAN programs show the different ways to effect input and output formatting.

We noticed several minor differences between the syntactic conventions used in the two languages when applying the counting rules chosen. One minor difference between the languages is that Ada always implicitly declares loop variables. This is to ensure that the availability of that variable is limited to the scope of its loop. It also has the effect of reducing the size of the program by one declaration. Another minor difference is the implicit “return” statement at the end of an Ada subprogram. A “return” statement is still required if processing is to stop at any other point, but most Ada subprograms are written to return after their last statement. In a FORTRAN routine, the last line must be an “end” statement. It has the same effect as a “return” statement, which is to return control to the referencing program unit. Nevertheless, it is common to see both a “return” and an “end” statement in a FORTRAN subprogram. A third minor difference is the lack of a need for a “continue” statement in Ada. Although a “continue” statement is rarely required in FORTRAN, it is common practice to use one at the end of a loop to avoid confusing the
last statement in the loop with the statements that follow the loop. In comparison, Ada loops require an "end loop"; however, this increases the number of physical lines (PSS) only, not the number of statements (LSS).

It should be noted that an inconsistency between the LSS methods for Ada and FORTRAN existed. In FORTRAN the "else" statement is counted as a logical source statement, but it is considered part of the same logical statement as its containing "if" statement in Ada. Thus, it was not counted as an additional logical source statement in Ada [8].

D. ECONOMIES OF SCALE IN THE ADA LANGUAGE

As previously noted, the relative difference between the FORTRAN and Ada counts fell as the size of the four programs in the experiment grew. An interesting question concerning this observed scale effect is: At what program size would the Ada code count fall below the FORTRAN code count? A graphical representation of this cross-over or break-even point is presented in Figure III-1.

![Graph](image)

**Figure III-1. Break-Even Size**

The Ada and FORTRAN lines of code (measured in thousands) are represented on the Y and the X axis, respectively. The ray that passes through the origin at 45 degrees represents points where the number of Ada and FORTRAN lines of code are equal. The curved line represents a hypothetical relationship between Ada and FORTRAN. If economies of scale exist, we would expect this relationship to exhibit a curvilinear form similar to that depicted in Figure III-1. This form suggests that as the size of the program grows, the number of Ada lines required to perform the function grows, more slowly than...
does the corresponding FORTRAN program. The point where the two lines intersect represents the break-even point. The interpretation of this point is that any program of size greater than B could be written with fewer lines in Ada than in FORTRAN.

What is the actual shape of the curvilinear line? We estimated a regression curve of the form:

\[ \text{KLOC}_A = \alpha \text{KLOC}_F \beta \mu, \]

where \( \alpha \) and \( \beta \) are the coefficients to be estimated, and \( \mu \) is a stochastic disturbance term.

The results of estimating the coefficients using the four test programs were:

\[ \text{KLOC}_A = 1.26 \text{KLOC}_F^{.937} \]

\[ (1.27) \quad (11.1) \]

\[ R = .97 \quad \text{SEE} = .16 \]

The numbers in parentheses are the t-scores of the FORTRAN coefficient and intercept term. If there were a scale effect, we would expect the coefficient on the FORTRAN variable to be less than one. In this case, the value of coefficient is 0.937. Using these regression results the break-even point was computed to be around 40,000 lines of code.

Note that we have estimated the point where functionally equivalent programs in Ada and FORTRAN would be the same size. However, this is the break-even size only from the perspective of development effort if the cost to develop a line of code in either language is the same. To compute the break-even cost, we must drop the implicit assumption that the cost to develop a line of code is the same for both languages. The cross-over point would depend on the values of the parameters used in the FORTRAN and Ada cost or effort estimating equations.

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4 From the regression we found:

\[ \text{KLOC}_A = 1.26 \text{KLOC}_F^{.937}. \]

If there were no difference between Ada and FORTRAN, then the relationship would simply be \( A = F \). Setting these two relationships equal to each other, we have

\[ 1.26 \text{KLOC}_F^{.937} = \text{KLOC}_F, \]

and solving for the break-even point, we find:

\[ \text{KLOC}_F = \frac{1}{.937 \sqrt[.937]{1.26}} \]

\[ = 39,190. \]

5 As an example, assume that the effort estimating equation for a FORTRAN development is taken to be

\[ E_F = 3.0 \text{KLOC}_F^{1.12}. \]
A word of caution about the interpretation of these results is in order. The results are based on only four relatively small programs, all of which are smaller than the projected break-even point. However, there is at least some anecdotal evidence from NASA/SEL and others that suggests that the magnitude of our estimate is consistent with their findings in this area [5].

The question remains as to why we should observe this scale effect with the Ada language. Several especially noticeable differences between the two languages may contribute to the effect. One difference was the fact that as program size increased, the executable portions increased slower in Ada than in FORTRAN. Although the declarative portions increased more in Ada than in FORTRAN, they contributed less to overall size. In our largest example, the executable portion was smaller in Ada than in FORTRAN even though the overall size was greater in Ada. Table III-2 presents a view of the four test programs separated into their executable and declarative portions.

<table>
<thead>
<tr>
<th>Program</th>
<th>FORTRAN LOC</th>
<th>Ada LOC</th>
<th>Ada/FORTRAN</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Executable</td>
<td>Declarative</td>
<td>Executable</td>
</tr>
<tr>
<td>Quicksort</td>
<td>72</td>
<td>7</td>
<td>81</td>
</tr>
<tr>
<td>FFT</td>
<td>104</td>
<td>11</td>
<td>110</td>
</tr>
<tr>
<td>Moment</td>
<td>52</td>
<td>9</td>
<td>71</td>
</tr>
<tr>
<td>Orbit</td>
<td>738</td>
<td>65</td>
<td>701</td>
</tr>
</tbody>
</table>

An example from the FFT test program illustrates this tradeoff between the number of executable and declarative statements. Table III-3 presents functionally equivalent Ada and FORTRAN code taken from the FFT program.

If our results that indicate significant differences in size between functionally equivalent FORTRAN and Ada programs are correct, then the practice of cost analysts to

and the effort estimating equation for an Ada development is assumed to be

\[ E_A = 5.8KLOC_A^{1.04} \]

Setting these two equations equal to each other and substituting in our estimated relationship between Ada and FORTRAN, we get:

\[ 5.8[1.26KLOC_F^{0.97}]^{1.04} = 3.0KLOC_F^{1.12}. \]

Solving for \( F \), we find the point of equal effort for Ada and FORTRAN developments is about 485,000 lines of code.
use Ada and FORTRAN lines-of-code counts interchangeably will induce errors in the subsequent cost estimates.

<table>
<thead>
<tr>
<th>Table III-3. Declarations Versus Statements</th>
</tr>
</thead>
<tbody>
<tr>
<td>FORTRAN</td>
</tr>
<tr>
<td>REAL Data (2*on)</td>
</tr>
<tr>
<td>REAL temp, temp2</td>
</tr>
<tr>
<td>REAL wi, wr</td>
</tr>
<tr>
<td>REAL Dat(2*+) type Complex is record</td>
</tr>
<tr>
<td>REAL mpn wt Rea Fl (type Complex)</td>
</tr>
<tr>
<td>REAL wi, wr Imaginy Float</td>
</tr>
<tr>
<td>Type Complex is record:</td>
</tr>
<tr>
<td>end record:</td>
</tr>
<tr>
<td>type Complex_Array:</td>
</tr>
<tr>
<td>function &quot;+&quot; (Left,Right:Complex) return Complex;</td>
</tr>
<tr>
<td>function &quot;+&quot; (Left,Right:Complex) return Complex;</td>
</tr>
<tr>
<td>function &quot;-&quot; (Left,Right:Complex) return Complex;</td>
</tr>
<tr>
<td>Data : Complex_Array (1..N);</td>
</tr>
<tr>
<td>W, Temp : Complex;</td>
</tr>
<tr>
<td>temp := wr * Data(j) - wi * Data(j+1)</td>
</tr>
<tr>
<td>temp := wr * Data(j+1) - wi * Data(j)</td>
</tr>
<tr>
<td>Data := Data(j) - temp</td>
</tr>
<tr>
<td>Data := Data(j+1) - temp</td>
</tr>
<tr>
<td>Data := Data(j) + temp</td>
</tr>
<tr>
<td>Data := Data(j+1) + temp</td>
</tr>
</tbody>
</table>

How large these potential errors can be is seen in Table III-4. The table’s first column is the number of lines of FORTRAN code. The second column is the estimate of the effort (measured in staff-months) to develop the appropriate FORTRAN lines of code using an equation taken from [1]. The third column is the estimate of the effort required to develop Ada code using the FORTRAN code count as the explanatory variable value rather than the appropriate Ada code count value. In this case, the parameter values were taken from [2]. The fourth column shows our algorithm that converts FORTRAN lines to the equivalent Ada lines of code count. The last column shows the effort-estimates that result from using the Ada code count from column four in the Ada effort-estimating equation.

<table>
<thead>
<tr>
<th>Table III-4. Estimates of Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>LOC in FORTRAN</td>
</tr>
<tr>
<td>1,000</td>
</tr>
<tr>
<td>5,000</td>
</tr>
<tr>
<td>10,000</td>
</tr>
<tr>
<td>20,000</td>
</tr>
<tr>
<td>40,000</td>
</tr>
<tr>
<td>100,000</td>
</tr>
<tr>
<td>500,000</td>
</tr>
</tbody>
</table>

III-9
The difference between the effort estimates in column three (which simulate the practice of using Ada and FORTRAN lines of code counts interchangeably) and those in the last column (which represent the "correct" estimate) is the error. We note that for small programs the relative error is large (e.g., 27 percent for 1,000 lines of code), then gets smaller as it approaches the cross-over point at around 40,000 lines, then grows larger again, but at a very slow rate (at 100,000 lines, the error is approximately 5 percent). Obviously, the results are sensitive to the effort-estimating equation used. Again, our FORTRAN-to-Ada equation is based on a small sample and should be used with caution. However, the point is that significant error can result from the practice of indiscriminately interchanging code-counting units.
IV. CONCLUSIONS AND FUTURE RESEARCH

The main objective of this research was to fill a gap in the knowledge needed by experienced FORTRAN size and cost estimators when estimating Ada developments for the first time. Although there are published models for the cost of developing Ada programs based on their expected size, there has been no standard way of estimating the size of an Ada development based on the expected size of an equivalent FORTRAN development. This work has shown that the sizes of functionally equivalent programs in Ada and FORTRAN are different. It would therefore be a mistake to assume that either a FORTRAN effort estimate or the expected number of FORTRAN lines of code would be sufficient in an Ada estimating equation. One such Ada equation was shown in this study; however, the magnitude of the error will depend on the exact estimating equations used. With the added knowledge of how the sizes of functionally equivalent programs in Ada and FORTRAN compare, a cost estimator can first adjust the expected number of lines of FORTRAN code to complete a job to a more accurate estimate of the expected number of lines of Ada code. Then, an Ada effort-estimating equation may be properly applied.

This study should be viewed mainly as a model for further investigation, although we believe our limited results are still of interest. In particular, we suspect that the tendency we observed for small Ada programs to be larger than their functionally equivalent FORTRAN counterparts is reasonable, as is our further observation that the overhead for Ada diminishes as the program size is increased. Our limited data suggested that there may even be a cross-over point beyond which the size of an Ada program is smaller than a functionally equivalent FORTRAN program. Although the number of observations was small and all were below this projected cross-over point, one of the strongest pieces of evidence that such a point exists, beyond the regression analysis, is that the number of executable lines of Ada in our largest example was smaller than the equivalent number of executable lines in FORTRAN. After an inspection of language features, we believed this to be a reasonable occurrence, because Ada has richer declarative power and, in return, can take advantage of simpler algorithmic processing.

Because the relationship between the sizes of functionally equivalent Ada and FORTRAN programs is probably not linear, more observations are needed, and in particular, observations are needed that are at least an order of magnitude greater than the
largest of our examples. The only published comparison of the sizes of a pair of large Ada and FORTRAN programs developed from the same set of requirements was too confounded to be useful for this purpose [10]. The only other evidence we found about the way larger Ada and FORTRAN programs compare was anecdotal, although the opinions reported to us tended to agree with our observations [5].

A final observation not previously mentioned stems from our interest in examining the possible variations of program size due to programming style. Although we used what we considered to be a conventional style of formatting for the programs in our analyses, we additionally wrote both terse and verbose styles for each example. The most interesting result we observed was that the possible variation in size for an Ada program is much greater than the possible variation for a FORTRAN program. This means that the comparison of Ada size, effort, and productivity results across organizations (which may not be observing the same style standards) is more prone to error than are similar comparisons using FORTRAN results. Although we used well-defined counting rules for both languages to maximize the portability of our results, we were not able to similarly well-define a programming style. In order to assure comparability of Ada size, effort, and productivity results across organizations, more study is needed into how the size of an Ada program might be normalized for any implemented functionality.
APPENDIX A

ADA AND FORTRAN CODE FOR EXAMPLE PROGRAMS
APPENDIX A

ADA AND FORTRAN CODE FOR EXAMPLE PROGRAMS

This appendix contains the code for three of the four programs discussed in the report. The three programs are Quicksort, Fast Fourier Transform, and Moments of a Distribution. The code for the Orbit program was not included because of its length. A copy of the code is available from the authors.

QUICKSORT

FORTRAN

PROGRAM xsort
C driver for routine sort
INTEGER i,j
REAL a(100)
open(7,file='TARRAY1.DAT',status='OLD')
open(8,file='sortprog.out',status='NEW')
read(7,*) (a(i),i=1,100)
close(7)
C print original array
write(8,*) 'Original array:'
do 11 i=1,10
  write(8,15) (a(10*(i-1)+j),j=1,10)
11 continue
15 format(1x,10f7.2)
C sort array
call sort(100,a)
C print sorted array
write(8,*) 'Sorted array:'
do 12 iff1,10
  write(8,15) (a(10*(i-1)+j),j=1,10)
12 continue
close(8)
END

SUBROUTINE sort(n,arr)
INTEGER n,M,NSTACK
REAL arr(n)
PARAMETER (M=7,NSTACK=50)
INTEGER i,ir,j,istack,k,l,istack(NSTACK)
REAL a,temp
jstack=0
i=1
ir=n
1 if(ir-l.lt.M)then
do 12 j=l+1,ir
   a=arr(j)
do 11 i=j-1,1,-1
   if(arr(i).le.a)goto 2
   arr(i+1)=arr(i)
11 continue
   i=0
2 arr(i+1)=a
12 continue
if(jstack.eq.0)return
ir=istack(jstack)
l=istack(jstack-1)
jstack=jstack-2
else
   k=(l+ir)/2
   temp=arr(k)
   arr(k)=arr(l+1)
   arr(l+1)=temp
   if(arr(l+1).gt.arr(ir))then
      temp=arr(l+1)
      arr(l+1)=arr(ir)
      arr(ir)=temp
   endif
   if(arr(l).gt.arr(ir))then
      temp=arr(l)
      arr(l)=arr(ir)
      arr(ir)=temp
   endif
   if(arr(l+1).gt.arr(l))then
      temp=arr(l+1)
      arr(l+1)=arr(l)
      arr(l)=temp
   endif
   i=l+1
   j=ir
   a=arr(l)
3 continue
   i=i+1
   if(arr(i).lt.a)goto 3
4 continue
   j=j-1
   if(arr(j).gt.a)goto 4
   if(j.lt.i)goto 5
   temp=arr(i)
   arr(i)=arr(j)
   arr(j)=temp
   goto 3
5 arr(l)=arr(j)
   arr(j)=a
   jstack=jstack+2
if(jstack.gt.NSTACK) pause 'NSTACK too small in sort'
if(ir-i+1.ge.j-l)then
   istack(jstack)=ir
   istack(jstack-1)=i
   ir=j-1
else
   istack(jstack)=j-1
   istack(jstack-1)=l
   l=i
endif
endif
goto 1
END

ADA

Quicksort Routine

with Text_1o;
procedure Quicksort_Generic (Arr : in out Element_Array) is
   Temp_Slip : array (1..Max_Size) of Integer,
   Stack_Ptr : Integer := 0;
   L : Integer := 1;
   IR : Integer := Arr.Length;
   A : Element;
   I : Integer;
   J : Integer;
   IQ : Integer;
   Found : Boolean;

   function "<" (Left, Right : Element) return Boolean is
      begin
         if Left = Right then
            return False;
         end if;
         return Left <= Right;
      end "<";

   function ">" (Left, Right : Element) return Boolean is
      begin
         return not "<=" (Left, Right);
      end ">";

      begin
         loop
            if IR - L < Subarray_Size then
               for JJ in L + 1 .. IR loop
                  A := Arr (JJ);
                  Found := False;
                  for II in reverse 1 .. JJ - 1 loop
                     if Arr (II) <= A then
                        Found := True;
                        Arr (II + 1) := A;
                        exit;
                     end if;
                  end loop;
               end loop;
            else
                istack(jstack)=IR
                istack(jstack-1)=L
                IR:=l
                istack(jstack-1)=i
                ir=L
            endif
         end loop;
      end loop;
      return Found;
end Quicksort_Generic;
else
    Arr (II + 1) := Arr (II);
end if;
end loop;
if not Found then
    Arr (I) := A;
end if;
end loop;
if Stack_Ptr = 0 then
    return;
end if;
IR := Temp_Stack (Stack_Ptr);
L := Temp_Stack (Stack_Ptr - 1);
Stack_Ptr := Stack_Ptr - 2;
else
    I := L;
    J := IR;
    IQ := (L + IR) / 2;
    A := Arr (IQ);
    Arr (IQ) := Arr (L);
    loop
        while J > 0 loop
            if A < Arr (J) then
                J := J - 1;
            else
                exit;
            end if;
        end loop;
        if J <= I then
            Arr (I) := A;
            exit;
        end if;
        Arr (I) := Arr (J);
        I := I + 1;
    while I <= Arr Length loop
        if A > Arr (I) then
            I := I + 1;
        else
            exit;
        end if;
    end loop;
    if J <= I then
        Arr (J) := A;
        I := J;
        exit;
    end if;
    Arr (J) := Arr (I);
    J := J - 1;
end loop;
Stack_Ptr := Stack_Ptr + 2;
if Stack_Ptr > Max_Size then
    Text_IO.Put_Line ('Max_Size must be made larger.');
    raise Constraint_Error;
end if;
if IR - I >= I - L then
    Temp_Seq (Stack_Ptr) := IR;
    Temp_Seq (Stack_Ptr - 1) := I + 1;
    IR := I - 1;
else
    Temp_Seq (Stack_Ptr) := I - 1;
    Temp_Seq (Stack_Ptr - 1) := L;
    L := I + 1;
end if;
end if;
end loop;
end Quicksort_Generic;

Specification for Quicksort
generic
    type Element is private;
    type Element_Array is array (Positive range <>) of Element;
    with function "<" (Left, Right : Element) return Boolean;
    Max_Size : Natural := 50;
    Subarray_Size : Positive := 7;
procedure Quicksort_Generic (Arr : in out Element_Array);

Driver for Quicksort
with Quicksort_Generic;
with Text Io;
procedure Xquicksort_Generic is
    package Floatio is new Text Io.FloatIo (Float);
    Size : constant := 100;
    type Float_Array is array (Positive range <>) of Float;
    procedure Sort is new Quicksort.Generic (Float, Float_Array, "<=");
    A : Float_Array (1 .. Size);
    File : Text Io.File_Type;
    Output : Text Io.File_Type;
begin
    Text Io.Open (File, Text Io.In_File, "Tarray.Dat");
    for I in 1 .. Size loop
        FloatIo.Get (File, A (I));
    end loop;
    Text Io.Close (File);
    --print original array
    Text Io.Create (Output, Text Io.Out_File, "Output.Lis");
    Text Io.Set_Output (Output);
    Text Io.Put_Line ("Original array:");
    for I in 1 .. 10 loop
        for J in 1 .. 10 loop
            FloatIo.Put (A (10 * (I-1) + J), 4, 2, 0);
        end loop;
        Text Io.New_Line;
    end loop;
    --sort array
    Sort (A);
    --print sorted array
    Text Io.Put_Line ("Sorted array:");
    for I in 1 .. 10 loop
for J in 1 .. 10 loop
    Float_Lo.Put (A (10 * (I-1) + J), 4, 2, 0);
end loop;
Text_Lo.New_Li ne;
end loop;
Text_Lo. Ci ose (Output);
end Xquicksort_Generic;

MOMENTS OF A DISTRIBUTION

FORTRAN

PROGRAM xmoment

C driver for routine moment

REAL PI

INTEGER Nbin,Ndat,Npts

PARAMETER(PI=3.14159265,Npts=10000,Nbin=100,Ndat=Npts+Nbin)

INTEGER i,j,k,nlim

REAL adev,ave,curt,data(Ndat),sdev,skew,var,x

i=1

do 12 j=1,Nbin
    x=PI*j/Nbin
    nlim=nint(sin(x)*PI/2.0*Npts/Nbin)
    do 11 k=1,nlim
        data(i)=x
        i=i+1
    end do
11 continue

12 continue

open(9,file='statsprog.out',status='NEW')

write(9,15) 'Moments of a sinusoidal distribution'

write(9,15) call moment(data,ave,adev,sdev,skew,curt)

write(9,16) 'Calculated','Expected'
write(9,17) 'Mean :',ave
write(9,17) 'Average Deviation :',adev
write(9,17) 'Standard Deviation :',sdev
write(9,17) 'Variance :',var
write(9,17) 'Skewness :',skew
write(9,17) 'Kurtosis :',curt

15 format(1x,a/)
16 format(1x,t29,a,t42,a/)
17 format(1x,a,t25,2f15.4)

close(9)

END

SUBROUTINE moment(data,n,ave,adev,sdev,skew,curt)

INTEGER n

REAL adev,ave,curt,sdev,skew,var,data(n)

INTEGER j

REAL p,s,ep

if(n.le.1)pause 'n must be at least 2 in moment'
n=0.

do 11 j=1,n

A-6
s = s + data(j)
11 continue
ave = s/n
addev = 0.
var = 0.
skew = 0.
curt = 0.
ep = 0.
do 12 j = 1, n
s = data(j) - ave
ep = ep + s
addev = addev + abs(s)
p = s*s
var = var + p
p = p*s
skew = skew + p
p = p*s
curt = curt + p
12 continue
addev = addev / n
var = (var - ep**2/n)/(n-1)
sdev = sqrt(var)
if(var.ne.0.) then
  skew = skew / (n*sdev**3)
curt = curt / (n*var**2) - 3.
else
  pause 'no skew or kurtosis when zero variance in moment'
endif
return
END

ADA
Moment Subroutine
with Text_1o;
procedure Moment_Generic (Data: Data_Array;
  Ave : in out Real;
  Adev : in out Real;
  Sdev : in out Real;
  Var : in out Real;
  Skew : in out Real;
  Curt : in out Real) is
  Powers : Real;
  Sum : Real;
  Deviation : Real;
  Sum_Devs : Real := 0.0;
  N : constant Integer := DataLength;
begin
  if N <= 1 then
    Text_1o.Put_Line ("Must be at least 2 in moment.");
  else
    Sum := 0.0;
    for J in Data'Range loop
      Sum := Sum + Data(J);
end loop;
Ave := Sum / Real (N);
Adev := 0.0;
Var := 0.0;
Skew := 0.0;
Curt := 0.0;
for J in Data'Range loop
  Deviation := Data (J) - Ave;
  Sum_Devs := Sum_Devs + Deviation;
  Adev := Adev + abs (Deviation);
  Powers := Deviation * Deviation;
  Var := Var + Powers;
  Powers := Powers * Deviation;
  Skew := Skew + Powers;
  Curt := Curt + Powers;
end loop;
Adev := Adev / Real (N);
Var := (Var - Sum_Devs ** 2 / Real (N)) / Real (N - 1);
Sdev := Sqrt (Var);
if Var /= 0.0 then
  Skew := Skew / (Real (N) * Sdev * Sdev * Sdev);
  Curt := Curt / (Real (N) * Var ** 2) - 3.0;
else
  Text_Io.Put_Line ("No skew or kurtosis when zero variance in moment");
end if;
end if;
end Moment_Generic;

Procedure Specification for Moment Routine
generic
  type Real is digits <>;
  type Data_Array is array (Positive range <>) of Real;
with function Sqrt (Number : Real) return Real;
procedure Moment_Generic (Data : Data_Array;
  Ave : in out Real;
  Adev : in out Real;
  Sdev : in out Real;
  Var : in out Real;
  Skew : in out Real;
  Curt : in out Real);

Driver for Moment Routine
with Text_Io;
with Moment_Generic;
with Math_Lib;
procedure Xmoment_Generic is
  Ave, Adev, Sdev, Var, Skew, Curt, X : Float;
  Pi : constant Float := 3.14159265;
  Nbin : constant Natural := 100;
  Npts : constant Natural := 10000;
  Ndat : constant Natural := Npts + Nbin;
  Nlim : Integer;
  I : Integer := 1;
type Float_Array is array (Positive range <> ) of Float;  
Data : Float_Array (1 .. Ndat);  
package Int_Lo is new Text_Lo_Integer_Io (Integer);  
package Float_Lo is new Text_Lo_Float_Io (Float);  
package Math is new Math_Lib (Float);  
procedure Moment is new Moment_Generic (Float,
Float_Array,
Math.Sqrt);  

begin  
for J in 1 .. Nbin loop  
X := Pi * Float (J) / Float (Nbin);
Nlim := Integer (Math.Sin(X) * Pi/2.0 * Float (Npts/Nbin));
for K in 1 .. Nlim loop  
Data (I) := X;
I:=I+1;
end loop;
end loop;
Text_Lo.Put_Line ("Moments of a sinusoidal distribution");
Moment (Data (1 .. I-1), Ave, Adev, Sdev, Var, Skew, Curt);
Text_Lo.Set_Col (29);
Text_Lo.Put ("Calculated");
Text_Lo.Set_Col (42);
Text_Lo.Put_Line ("Expected");
Text_Lo.Put ("Mean :");
Text_Lo.Set_Col (25);
Float_Lo.Put (Ave, 6, 5, 0);
Float_Lo.Put (Pi / 2.0, 7, 5, 0);
Text_Lo.New_Line;
Text_Lo.Put ("Average Deviation :");
Text_Lo.Set_Col (25);
Float_Lo.Put (Adev, 6, 5, 0);
Float_Lo.Put (0.570796, 7, 5, 0);
Text_Lo.New_Line;
Text_Lo.Put ("Standard Deviation : ");
Text_Lo.Set_Col (25);
Float_Lo.Put (Sdev, 6, 5, 0);
Float_Lo.Put (0.683667, 7, 5, 0);
Text_Lo.New_Line;
Text_Lo.Put ("Variance :");
Text_Lo.Set_Col (25);
Float_Lo.Put (Var, 6, 5, 0);
Float_Lo.Put (0.467401, 7, 5, 0);
Text_Lo.New_Line;
Text_Lo.Put ("Skewness :");
Text_Lo.Set_Col (25);
Float_Lo.Put (Skew, 6, 5, 0);
Float_Lo.Put (0.0, 7, 5, 0);
Text_Lo.New_Line;
Text_Lo.Put ("Kurtosis :");
Text_Lo.Set_Col (25);
Float_Lo.Put (Curt, 6, 5, 0);
Float_Lo.Put (-0.806249, 7, 5, 0);
Text_Lo.New_Line;
end Xmoment_Generic;
FAST FOURIER TRANSFORM

FORTRAN

PROGRAM xfour1
C driver for routine four1
INTEGER NN,NN2
PARAMETER (NN=32,NN2=2*NN)
REAL data(NN2),dcmp(NN2)
INTEGER i,isign,j
open(8,file='four1 prog.out',status='NEW')
write(8,'(a45)') 'h(t)=real-valued even-function'
write(8,'(a)') 'H(n)=H(N-n) and real?
do 11 i=1,2*NN-1,2
   data(i)=1.0/(((i-NN-1.0)/NN)**2+1.0)
data(i+1)=0.0
11 continue
isign=1
call four1(data,NN,isign)
call prntft(data,NN2)
write(8,'(a45)') 'h(t)=imaginary-valued even-function'
write(8,'(a)') 'H(n)=H(N-n) and imaginary?
!j=1,2*NN-1,2
   data(i+1)=1.0/(((i-NN-1.0)/NN)**2+1.0)
data(i)=0.0
12 continue
isign=1
call four1(data,NN,isign)
call prntft(data,NN2)
write(8,'(a45)') 'h(t)=real-valued odd-function'
write(8,'(a)') 'H(n)=-H(N-n) and real?
!j=1,2*NN-1,2
   data(i+(i-NN-1.0)/NN)/(((i-NN-1.0)/NN)**2+1.0)
data(i)=0.0
13 continue
data(1)=0.0
isign=1
!j=1,2*NN-1,2
   data(i+(i-NN-1.0)/NN)/(((i-NN-1.0)/NN)**2+1.0)
data(i)=0.0
14 continue
data(2)=0.0
isign=1
!j=1,2*NN-1,2
   data(i+(i-NN-1.0)/NN)/(((i-NN-1.0)/NN)**2+1.0)
data(i)=0.0
15 continue
C transform, inverse-transform test
!j=1,2*NN-1,2
   data(i)=1.0/((0.5*(i-NN-1)/NN)**2+1.0)
dcmp(i)=data(i)

A-10
data(i+1) = (0.25*(i-NN-1)/NN)*
* exp(-(0.5*(i-NN-1.0)/NN)**2)
dcmp(i+1) = data(i+1)

continue
isign=1
    call fourl(data,NN,isign)
    isign=-1
    call fourl(data,NN,isign)
write(8,20) 'Original Data:','Double Fourier Transform:
20 format(/lx,10x,t44,a)
    write(8,21) 'k','Real h(k)','Imag h(k)','Real h(k)','Imag h(k)'
21 format(/lx,t5,a,t11,a,t24,a,t41,a,t53,a)
do 16 i=1,NN,2
    j=(i+1)/2
    write(8,22) j,dcmp(i),dcmp(i+1),data(i)/NN,data(i+1)/NN
22 format(/lx,i4,2x,2f12.6,5x,2f12.6)
continue
close(8)

SUBROUTINE prntft(data,nn2)
INTEGER n,nn2,m,mm
REAL data(nn2)
write(8,30) 'n','Real H(n)','Imag H(n)','Real H(N-n)','
* 'Imag H(N-n)'
30 format(/lx,t5,a,t11,a,t23,a,t39,a,t51,a)
write(8,31) ,data(1),data(2),data(1),data(2)
do 31 n=3,(nn2/2)+1,2
    m=(n-1)/2
    mm=nn2+2-n
    write(8,32) m,data(n),data(n+1),data(mm),data(mm+1)
31 continue
return
END

SUBROUTINE fourl(data,nn,isign)
INTEGER isign,nn
REAL data(2*nn)
INTEGER i,i1,j,j1,m,mmax,n
REAL tempi,temps
DOUBLE PRECISION theta,wi,wpi,wpr,wr,wtemp
n=2*nn
j=1
do 11 i=1,n,2
    if(i.gt.j) then
        tempi=data(j)
        temps=data(j+1)
data(j)=data(i)
data(j+1)=data(i+1)
data(i)=temps
data(i+1)=tempi
4 endif
11 continue
m=n/2
if (Qnmgc.2).and.(.gt.an)) then
   j=j-m
   m=m/2
   goto 1
endif
j=j+m
continue
mmax=2
if (n.gt.mmax) then
   istep=2*mmax
   theta=6.28318530717959d0/(isign*mmax)
   wpr=-2.0d0*sin(0.5d0*theta)**2
   wpi=sin(theta)
   wr=1.0d0
   wi=0.d0
   do 13 m=1,mmax,2
      do 12 i=mn,istep
         j=i+mmax
         temp=sngl(wr)*data(j)-sngl(wi)*data(j+1)
         temp1=sngl(wr)*data(j+1)+sngl(wi)*data(j)
         data(j)=data(i)-temp
         data(j+1)=data(i+1)-temp1
         data(i)=data(i)+temp
         data(i+1)=data(i+1)+temp1
      12 continue
      wtemp=wr
      wr=wr*wpr-wi*wpi+wr
      wi=wi*wpr+wtemp*wpi+wi
   13 continue
   mmax=istep
   goto 2
endif
return
END

ADA

Fast Fourier Routine
procedure Fourier_Generic (Data :in out Complex_Array;
    Positive :in Boolean := True) is
   Istep :Integer;
   J :Integer := 1;
   I :Integer;
   M :Integer;
   Mmax :Integer;
   Temp, W, Wp :Complex_Type;
   Theta :Real;
   Pi :constant := 3.1415926535897932;
   Sign :Integer := 1;
begin
   if not Positive then
      Sign := -1;
   end if;
   for I in Data'Range loop
if J > I then
    Temp := Data (J);
    Data (J) := Data (I);
    Data (I) := Temp;
end if;
M := DataLength / 2;
while M >= 1 and J > M loop
    J := J - M;
    M := M / 2;
end loop;
J := J + M;
end loop;
Mmax := 1;
while DataLength > Mmax loop
    Istep := 2 * Mmax;
    Theta := Pi / Real (Sign * Mmax);
    Wp := Make (-2.0 * (Sin (0.5 * Theta)) ** 2, Sin (Theta));
    W := Make (1.0, 0.0);
    for M in 1 .. Mmax loop
        for Iteration in 0 .. (DataLength - M) / Istep loop
            I := Iteration * Istep + M;
            J := I + Mmax;
            Temp := W * Data (J);
            Data (J) := Data (I) - Temp;
            Data (I) := Data (I) + Temp;
        end loop;
        W := W * Wp + W;
    end loop;
    Mmax := Istep;
end loop;
end Fourier_Generic;

Specification for Fast Fourier Routine
generic
    type Real is digits < >;
    with function Sin (Angle : Real) return Real;
    type Complex_Type is private;
    type Complex_Array is array (Positive range < >) of Complex_Type;
    with function Make (Left, Right : Real) return Complex_Type;
    with function " (Left, Right : Complex_Type) return Complex_Type;
    with function "+" (Left, Right : Complex_Type) return Complex_Type;
    with function "-" (Left, Right : Complex_Type) return Complex_Type;
procedure Fourier_Generic (Data : in out Complex_Array;
    Positive : in Boolean := True);

Driver for Fast Fourier Routine
with Fourier_Generic;
with Complex_Generic;
with Math_Lib;
with Text_Jo;
procedure Xfourier_Generic is -- Good Ada driver for routine Fourier_Generic
    package Math is new Math_Lib (Float);
    package Complex is new Complex_Generic (Float);
type Complex_Array is array (Positive range < >) of Complex.Complex_Type;
procedure Four1 is new Fourier_Generic (Float, 
  Math.Sin, 
  Complex.Complex_Type, 
  Complex_Array, 
  Complex.Make, 
  Complex."*", 
  Complex."+", 
  Complex."-"); 

package Int_Io is new Text_Io.Integer_Io (integer); 
package Float_Io is new Text_Io.Float_Io (Float); 
Size : constant integer := 32; 
Half_Size : constant Integer := Size / 2; 
Complex_Data, Dcmp : Complex_Array (1 .. Size); 
Outfile : Text_Io.File_Type; 

procedure Prntt (Data : Complex_Array) is 
  Length : Integer := Data'Last - Data'First + 1; 
  Line : Integer := 0; 
  Rev_Ptr : Integer; 
begin 
  Text_Io.New_Line; 
  Text_Io.Set_Col (4); 
  Text_Io.Put ("n"); 
  Text_Io.Set_Col (10); 
  Text_Io.Put ("Real H(n)"); 
  Text_Io.Set_Col (22); 
  Text_Io.Put ("Imag H(n)"); 
  Text_Io.Set_Col (38); 
  Text_Io.Put ("Real H(N-n)"); 
  Text_Io.Set_Col (51); 
  Text_Io.Put_Line ("Imag H(N-n)"); 
  Int_Io.Put (Line, 4); 
  Text_Io.Put (" "); 
  Float_Io.Put (Complex.Real_Of (Data (1)), 5, 6, 0); 
  Float_Io.Put (Complex.Imaginary_Of (Data (1)), 5, 6, 0); 
  Text_Io.Put (" "); 
  Float_Io.Put (Complex.Real_Of (Data (1)), 5, 6, 0); 
  Float_Io.Put (Complex.Imaginary_Of (Data (1)), 5, 6, 0); 
  Text_Io.New_Line; 
for I in Data'First + 1 .. Data'Last / 2 + 1 loop 
  Line := I - 1; 
  Rev_Ptr := Length + 2 - I; 
  Int_Io.Put (Line, 4); 
  Text_Io.Put (" "); 
  Float_Io.Put (Complex.Real_Of (Data (I)), 5, 6, 0); 
  Float_Io.Put (Complex.Imaginary_Of (Data (I)), 5, 6, 0); 
  Text_Io.Put (" "); 
  Float_Io.Put (Complex.Real_Of (Data (Rev_Ptr)), 5, 6, 0); 
  Float_Io.Put (Complex.Imaginary_Of (Data (Rev_Ptr)), 5, 6, 0); 
  Text_Io.New_Line; 
end loop; 
end Prntt;
begin
  Text_Io.Create (Outfile, Text_Io.Out_File, "Output.Lis");
  Text_Io.Set_Output (Outfile);
  Text_Io.Put_Line ("h(t)=real-valued even-function");
  Text_Io.Put_Line ("H(n)=H(N-n) and real?";
  for I in Complex_Data'Range loop
    Complex_Data (I) := Complex.Make
      (1.0 / ((Float (I - Half_Size - 1) / Float (Half_Size)) ** 2 + 1.0),
       0.0);
  end loop;
  Four1 (Complex_Data);
  Pntft (Complex_Data);
  Text_Io.Put_Line ("h(t)=imaginary-valued even-function");
  Text_Io.Put_Line ("H(n)=H(N-n) and imaginary?";
  for I in Complex_Data'Range loop
    Complex_Data (I) := Complex.Make
      (0.0,
       1.0 / ((Float (I - Half_Size - 1) / Float (Half_Size)) ** 2 + 1.0));
  end loop;
  Four1 (Complex_Data);
  Pntft (Complex_Data);
  Text_Io.Put_Line ("h(t)=real-valued odd-function");
  Text_Io.Put_Line ("H(n)=H(N-n) and imaginary?";
  for I in Complex_Data'Range loop
    Complex_Data (I) := Complex.Make
      ((Float (I - Half_Size) - 1.0) / Float (Half_Size) /
       ((Float (I - Half_Size) - 1.0) / Float (Half_Size)) ** 2 + 1.0),
       0.0);
  end loop;
  Complex_Data (1) := Complex.Make (0.0, 0.0);
  Four1 (Complex_Data);
  Pntft (Complex_Data);
  Text_Io.Put_Line ("h(t)=imaginary-valued odd-function");
  Text_Io.Put_Line ("H(n)=H(N-n) and real?";
  for I in Complex_Data'Range loop
    Complex_Data (I) := Complex.Make
      (0.0,
       (Float (I - Half_Size) - 1.0) / Float (Half_Size) /
       ((Float (I - Half_Size) - 1.0) / Float (Half_Size)) ** 2 + 1.0));
  end loop;
  Complex_Data (1) := Complex.Make (0.0, 0.0);
  Four1 (Complex_Data);
  Pntft (Complex_Data);
  transform, inverse-transform test
  for I in Complex_Data'Range loop
    Complex_Data (I) := Complex.Make
      (1.0/(0.5 * Float (I - Half_Size - 1) / Float (Half_Size)) ** 2 + 1.0),
       (0.25 * Float (I - Half_Size - 1) / Float (Half_Size)) *
       Math.ExP (-((0.5 * Float (I - Half_Size - 1) / Float (Half_Size))**2));
    Dcmp (I) := Complex_Data (I);
  end loop;
  Four1 (Complex_Data);
  Four1 (Complex_Data, False);
  Text_Io.New_Line;
end
Text_Io.Put(" Original Data:");
Text_Io.Set_Col (44);
Text_Io.Put_Line("Double Fourier Transform:");
Text_Io.New_Line;
Text_Io.Put(" k Real h(k) Imag h(k)");
Text_Io.Set_Col (41);
Text_Io.Put_Line(" Real h(k) Imag h(k)");
Text_Io.New_Line;
for I in Complex_Data’First .. Complex_Data’Last / 2 loop
  Int_Io.Put (1, 4);
  Float_Io.Put (Complex.Real_Of (Dcmp (1)), 7, 6, 0);
  Float_Io.Put (Complex.Imaginary_Of (Dcmp (1)), 5, 6, 0);
  Float_Io.Put (Complex.Real_Of (Complex_Data (I)) / Float (Size), 10, 6, 0);
  Float_Io.Put (Complex.Imaginary_Of (Complex_Data(I)) / 
    Float (Size), 5, 6, 0);
  Text_Io.New_Line;
end loop;
Text_Io.Close (Outfile);
end Xfourier_Generic;
REFERENCES
REFERENCES


ABBREVIATIONS
### ABBREVIATIONS

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Description</th>
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<tbody>
<tr>
<td>DoD</td>
<td>Department of Defense</td>
</tr>
<tr>
<td>FFT</td>
<td>Fast Fourier Transform</td>
</tr>
<tr>
<td>FORTRAN</td>
<td>Formula Translation</td>
</tr>
<tr>
<td>IDA</td>
<td>Institute for Defense Analyses</td>
</tr>
<tr>
<td>KLOC</td>
<td>thousand lines of code</td>
</tr>
<tr>
<td>LSS</td>
<td>logical source statement</td>
</tr>
<tr>
<td>NASA</td>
<td>National Aeronautics and Space Administration</td>
</tr>
<tr>
<td>PSS</td>
<td>physical source statement</td>
</tr>
<tr>
<td>SDIO</td>
<td>Strategic Defense Initiative Organization</td>
</tr>
<tr>
<td>SEL</td>
<td>Software Engineering Library</td>
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