**Title:** NMR Imaging Development for the study of Solids

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**Key Words:**
- NMR Imaging Solids
- Non-destructive evaluation (NDE)
- Defects in solids
- Non-invasive measurements

**Abstract:**
The Techniques of NMR imaging are developed for simple inorganic solids and applied to the study of mechanically induced defects in NaCl. The feasibility of the technique is demonstrated for defect (dislocation) densities greater than $10^7$/cm$^2$ with a resolution of better than 1mm.
ABSTRACT: The techniques of NMR imaging are developed for simple inorganic solids and applied to the study of mechanically induced defects in NaCl. The feasibility of the technique is demonstrated for defect (dislocation) densities greater than $10^7$/cm$^2$ with a resolution of better than 1 mm.

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Problem Studied

This grant covered, in part, the cost of one graduate student working on the NMR imaging of solids in conjunction with research sponsored by the US ONR under grants N00014-86-K-0149 and N00014-86-C-0724 subcontract SK60D782OF from Lockheed corporation.

The goal of the research was to:

i) Improve the quality of NMR images obtained from simple inorganic solids so they are useful non-destructive, non-invasive tools to study mechanically induced defects in solids.

ii) Use the techniques on mechanically damaged materials to establish the utility of the technique to study mechanically damaged materials.

Summary of Most Important Results

The quality of images using the $^{23}$Na signal from NaCl in a propellant simulant has improved as a function of time, as is illustrated in figure 1. The image labeled "1989" is, in fact, of high enough resolution that the use of contour plots is misleading. The images are normally viewed on the computer screen however a simple cost-effective means of reproducing these images has not been found. The major improvements to the equipment are the increase in gradient strength used to form the image and some improvements in the software data processing. The details of these improvements has been previously reported (see semi-annual progress reports, this grant).

The contents of the propellant simulant are shown in table I. The improvements in our instrumentation were sufficient that we were able to obtain a usable image using the Aluminum signal from the metal particles in the simulant. This image is shown in figure 2. The aluminum NMR signal is several times broader than the Na signal making images that much more difficult to obtain. To the best of our knowledge, no one has obtained a better image using aluminum with any technique. Attempts at Lockheed corporation to use sophisticated multiple pulse techniques did not yield an improved resolution due to significant distortions from off resonance signals.

The utility of the NMR imaging technique to study damaged materials was demonstrated and is contained in the reprint which is appendix A of this report. It is important to note that the line narrowing techniques commonly used for solids work cannot be used to study quadrupole broadened NMR signals to study defects. The line narrowing techniques reduce or remove the effects of the defects on the NMR signal. Our work so far has concentrated on the non-destructive measurement of defect densities in mechanically damaged NaCl using the NMR signal from the Na nucleus. The results demonstrate the utility of the technique to study mechanically damaged materials using the non-invasive NMR imaging technique.
Publications (this grant)


Participating Scientific Personnel

B. H. Suits (PI)
J. L. Lutz, MS 1989 (through summer 1989)
D. E. Wilken, (starting summer 1989 on this grant, MS 1988)
Resolution versus Time
PBAN propellant simulant

NMR IMAGES
as contour plots

SAMPLE GEOMETRY

1987

1988

1989

Note: New sample with more detail

$^{23}$Na from solid NaCl

(Actual resolution is very dependent on the particular situation studied and care must be used when comparing these results to other results on different materials)
Figure 2

$^{27}$Al signal

NMR IMAGES

Sample Dimensions

1989

PBAN Propellant Simulant
(contains Al Particles)
**PBAN Propellant Simulant**

<table>
<thead>
<tr>
<th>Component</th>
<th>weight %</th>
</tr>
</thead>
<tbody>
<tr>
<td>PBAN</td>
<td>14</td>
</tr>
<tr>
<td>Al (powder)</td>
<td>16</td>
</tr>
<tr>
<td>NaCl</td>
<td>49</td>
</tr>
<tr>
<td>((\text{NH}_4)_2\text{SO}_4)</td>
<td>21</td>
</tr>
</tbody>
</table>
Nuclear magnetic resonance imaging as a tool to characterize defect densities in solids

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(Received 23 September 1988; accepted for publication 13 January 1989)

Nuclear magnetic resonance imaging methods demonstrate the spatial variation of $^{23}$Na signal intensity in NaCl which results from an impact-induced inhomogeneous defect distribution.

Nuclear magnetic resonance (NMR) imaging of solids is a relatively new, nondestructive, noninvasive measurement technique which has been shown to be useful in monitoring inhomogeneities of chemical species, and for identifying cracks in materials. The work presented here demonstrates the utility of the technique to study the spatial distributions of other types of material defects as well, in particular, dislocations in solids containing a nucleus with a nonzero quadrupole moment.

The use of NMR to study mechanically induced defects is not new. A comprehensive review of the effects on the quadrupole interaction due to point defects and dislocations in cubic systems has been presented by Kanert and Mehring. What is new here is the application of these ideas in a spatially resolved mode.

This discussion is limited to the use of the electric quadrupole interaction, though other interactions which are modified in the presence of defects may prove useful as well. Thus, the discussion is limited to nuclei with spin, $I > 1/2$.

The electric quadrupole interaction is due to the presence of an electric field gradient (efg) at the nucleus under isolated dislocation, will be presented here. The features which these strain fields have an impact on the NMR signal may prove useful as well. The distance over which these strain fields have an impact on the NMR signal may be quite large.

For simplicity, the details of only one type of defect, an isolated dislocation, will be presented here. The features which emerge for others are qualitatively similar.

It is quite difficult to treat nuclei which are very close to the defect, but outside this "core" region elastic theory can be used. Estimates of the size of the core region show that it is only a few lattice constants in radius.

In the region where the elastic theory applies the atoms will be displaced only a small amount relative to their neighbors and hence one can assume that the changes in the quadrupole interaction will be linearly related to the local strain, $e$, or stress, $\sigma$. With this assumption one can write

$$V_{ij} = V_{ij}^0 + \sum_{\alpha x} C_{\alpha ij} e_{\alpha x}.$$  \hspace{1cm} (5)

The coefficients $C_{\alpha ij}$ are measured quantities and values for many cubic systems are tabulated in Ref. 5.

A dislocation is characterized by a line through the material and a slip plane. If the dislocation line defines the $z^*$ axis and the slip plane lies in the $x^* - z^*$ plane, then the stress tensor for a screw dislocation is

$$\sigma^* = \frac{G b}{2\pi r} \begin{pmatrix} 0 & 0 & -\sin \theta \\ 0 & 0 & \cos \theta \\ -\sin \theta & \cos \theta & 0 \end{pmatrix}.$$  \hspace{1cm} (6)

and for the edge dislocation

$$V_{\alpha} = V_{\alpha \epsilon} \cos^2 \theta + V_{\alpha \phi} \sin^2 \theta \cos^2 \theta + V_{\alpha \phi} \sin^2 \theta \sin^2 \phi,$$  \hspace{1cm} (3)

where $\theta$ and $\phi$ are the Euler angles relating the primed to the unprimed coordinates. This yields magnetic dipole transition frequencies $\omega_m$ between the states characterized by $m$ and $m + 1$, $m = -I, -I + 1, \ldots, +I$,

$$\omega_m = \gamma H + [3eQ/8I(2I - 1)h] (2m + 1) V_{\alpha}.$$  \hspace{1cm} (4)

Note that the transition from $m = -\frac{I}{2}$ to $m = +\frac{I}{2}$ (present for nuclei with half-integer spin) is not sensitive in first order to the presence of the quadrupole interaction, while other transitions can be strongly affected.

There are many types of defects in materials. Associated with any defect is a strain field, the nature of which depends on the particular type of defect. The distance over which these strain fields have an impact on the NMR signal may be quite large.

APPENDIX A

Nuclear magnetic resonance imaging as a tool to characterize defect densities in solids

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This discussion is limited to the use of the electric quadrupole interaction, though other interactions which are modified in the presence of defects may prove useful as well. Thus, the discussion is limited to nuclei with spin, $I > 1/2$.

The electric quadrupole interaction is due to the presence of an electric field gradient (efg) at the nucleus under study which couples to the nuclear electric quadrupole moment (eQ). The quadrupole interaction is discussed in detail elsewhere.

For NMR measurements in a high magnetic field, it is often the case that the Zeeman interaction is very small compared to the quadrupole interaction, $\mathcal{H}_Q$. If the convention is used that the $\mathcal{H}_Q$ axis of the lab frame define a crystal reference axis and the slip plane lies in the $(x,y,z)$ plane, then the stress tensor for a screw dislocation is

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\[
\sigma'' = \frac{D}{r} \begin{pmatrix}
\cos \theta \cos 2\theta & \cos \theta \cos 2\theta & 0 \\
-\sin \theta (2 + \cos 2\theta) & \cos \theta \cos 2\theta & 0 \\
0 & 0 & 2\nu \sin \theta
\end{pmatrix}
\]  
(7)

where \(G\) is the shear modulus, \(b\) is the magnitude of the Burgers vectors, \(D = Gb/[2\pi(1 - \nu)]\) where \(\nu\) is the Poisson ratio and the \(r\) and \(\theta\) are the positions in the sample relative to the dislocation in the dislocation's reference frame. Thus, the efg in the lab reference frame can be calculated as

\[
V = T^{-1}U^{-1}(V^0 + \Sigma \) UT,
\]  
(8)

where \(U\) transforms the interaction from the double prime to prime coordinates and \(T\) into the laboratory frame.

It can be seen that both types of dislocations yield an angularly dependent response. In some cases this angular dependence can be used as a means of characterizing the defects which are present.

Due to the cubic symmetry at the \(^{23}\)Na site in NaCl the efg tensor in the undistorted lattice, \(V^0\), is zero and all the transitions occur at the same frequency, \(\gamma H/\hbar\). As an explicit example, the screw dislocation in NaCl [(110) (110) slip system] gives

\[
V_{zz} = (GbC_1/2\pi r) f(\theta, T, U).
\]

The function \(f(\theta, T, U)\) (see Ref. 5) describes the angular dependence and in this case has the property that it is zero if the magnetic field is along or perpendicular to the dislocation. Putting in numbers one has an additional splitting of the \(J = \pm \frac{1}{2} \) to \(\pm \frac{3}{2}\) transition given approximately by

\[
\Delta \nu = \pm (2.4 \text{ MHz}/r) f(\theta, T, U),
\]  
(9)

where \(r\) is the distance from the dislocation line in angstroms. Figure 1 illustrates the effects of the dislocation on the NMR signal. Curves of constant frequency shift of the \(\pm \frac{1}{2}\) to \(\pm \frac{3}{2}\) satellite transition appear as lobes about the dislocation.

In the core region one does not know the efg but the number of nuclei involved is quite small and this region can be ignored. Outside the core region is a region where the quadrupole shift moves the satellites outside the bandwidth of the spectrometer (in our case roughly 0.3 MHz). The signal from these regions will be reduced in two ways: (1) the \(\pm \frac{1}{2}\) to \(\pm \frac{3}{2}\) transitions will be missing and (2) the \(-\frac{1}{2}\) to \(+\frac{1}{2}\) transition will be decreased in magnitude due to the fact that it must be treated in the effective spin \(\frac{1}{2}\) approximation. Outside this region is a region labeled "in baseline." From a simple point of view one regards the satellite transition frequencies from this region to be spread out over such a wide range that the total response within the spectrometer bandwidth is effectively flat. These signals are observed in a rigorous sense but if the baseline is corrected before or during image processing, they are removed. All that is observed then is the \(-\frac{1}{2}\) to \(\frac{1}{2}\) transition.

Outside all these regions the shift is small compared to the NMR linewidth (in this case roughly 3 kHz) and hence the effects of the dislocation are obscured and the full intensity is observed.

Of course, the dividing lines between the regions are not sharp and there is some change in the central lineshape used to create the image. The changes in lineshape are not overwhelming and this simple picture reflects the essence of the behavior.

The sensitivity of the NMR technique is quite good. Using the estimated 100 nm as the maximum range of the effects of the dislocation then in a cross section one has rough-

![FIG. 1. A schematic diagram of the spatial dependence of the contribution to the NMR signal from the \(\pm \frac{1}{2}\) to \(\pm \frac{3}{2}\) satellite transitions near a dislocation. The figure is scaled appropriately for the \(^{23}\)Na signal from NaCl with the magnetic field along (100).](image)

![FIG. 2. NMR images showing the spatial distribution of the NMR intensity (a) before and (b) after extensive damage to part of the crystal by impact. The difference (percent) between (a) and (b) is shown in (c). The change in signal intensity is due to the presence of defects which alter the NMR response. The sample is \(1 \times 0.54 \text{ cm}^2\) and 0.2 cm thick. The view is through the thickness of the sample.](image)
ly $1.6 \times 10^{-11}$ cm$^3$ which is unobserved for each dislocation. Thus, dislocation densities larger than about $10^6$ or $10^7$/cm$^2$ should be observable in NaCl using this technique for measurements with a good signal to noise ratio.

Figure 2 shows images for a crystal which has been damaged by impact using a drop hammer (495 g from 9 cm high). These images are two-dimensional projections through the thickness of the sample with the strike along the direction of view. Part of the sample (the right-most quarter in Fig. 2) was outside the region of the strike. The damage is clearly evident as a large decrease in intensity in the region that was hit. Plastic deformation of the damaged region is roughly 5% (there was no measureable loss of mass).

Figure 3 shows cross sections through the center for two orientations of the damaged crystal with respect to the applied magnetic field. The view of the sample is the same in both cases. There is a significant difference which is not uniform from one side of the sample to the other. That is, the defect distribution as seen by the $^{23}$Na nuclei does not have the cubic symmetry of the host lattice and the degree to which the symmetry is broken varies across the sample. One way the symmetry can be broken is if there are more dislocations along one direction than another equivalent direction. In cases where the defect density is high and a nucleus can "see" more than one at a time (for NaCl a local density of roughly $10^{10}$/cm or greater), a difference in the microscopies of the distribution for different directions may also give rise to this effect. As a simple example, if in one direction the dislocations occur in bunches, whereas in another they are spread out uniformly, one can expect this phenomena. It should be noted that the original sample, which was cleaved from a larger melt-grown block, also showed a lack of cubic symmetry for the NMR response, however, in this case the change in signal intensity upon rotation of the magnetic field was uniform across the sample. The observed lack of cubic symmetry in the undamaged sample is not unexpected based on previous results for NaCl.

The NMR data presented in this paper was obtained using a "homemade" microcomputer controlled NMR spectrometer with a magnetic field of approximately 85 kG ($360$ MHz for protons, $95$ MHz for $^{23}$Na). The projection reconstruction (convolution backprojection) algorithm described in Ref. 1 was used to create images from Fourier transformed free induction decays. The gradient strength used for images was approximately 15 G/cm. In all of these images, the linear resolution is limited by the NMR linewidth to about 1 mm.

The imaging method used so far in these studies has been the bare minimum. With improvements in the technique one can hope to improve the sensitivity and resolution of the images and to streamline the analysis of the defects present.

These results show that NMR imaging can be used to measure, and to some extent characterize, defect distribu-

![FIG. 3. Cross sections through images of the heavily damaged crystal for two orthogonal orientations of the magnetic field; magnetic field (a) perpendicular and (b) parallel to the sample face. The defect distribution does not have the cubic symmetry of the NaCl lattice and hence destroys the cubic symmetry of the NMR response.](image)

2. For example, see G. C. Chingas, J. B. Miller, and A. N. Garroway, J. Magn. Reson. 66, 530 (1986), and references therein.