EVALUATION OF DATA ERRORS INTRODUCED BY NOISE, SAMPLING RATES AND COMPOSITE WAVEFORMS

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Final Report

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**Evaluation of Data Errors Introduced by Noise, Sampling Rates and Composite Waveforms**

The limitations of automatic data processing of transient signals are studied. Errors resulting from noise, sampling, and forming composite records are evaluated by considering analytical waveforms. The applications of digital filtering and trend removal are also considered.

Various norms of time-domain signals are computed with the resulting errors identified for certain waveforms generic to nuclear electromagnetic pulse (NEMP) test data.
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1.0 INTRODUCTION

In obtaining recordings of fast transient signals, such as occur in nuclear electromagnetic pulse (NEMP) testing, the data system is configured typically as shown in Fig. 1. Because of the bandwidth and high-frequency spectral content, the handling of the data provides unique problems for the analyst. Typical error sources include:

Limited accuracy of the digitizer word
Extraneous electrical noise from the environmental excitation of the instrumentation system
Internal noise of the data system
Offset errors in the sampling device
Distortion from the nonlinearities of the data system
Excessive noise level resulting from the dynamic range limitation and low signal levels
Gain errors in the sampling device
Aperture errors in the sampling device
Monotonicity errors
Jitter in the digitizer
Dropdown in the digitizer
Operator errors
Aliasing errors

Quantitatively, characterizing the cumulative effects of all of the noise sources is necessary in order to have complete confidence in the results. There are techniques for quantitating the random noise level in data (Ref. 1). However, it is virtually impossible to obtain even reasonable estimates for some of the noise sources. Aliasing noise is one of those.

The phenomenon of aliasing occurs when the sampled signal is not band limited or when it is undersampled; i.e., the sampling rate is below the Nyquist rate for a band-limited signal, where the Nyquist rate, \( S_N \), is defined as
Here $f_{\text{max}}$ is the highest frequency of a band-limited signal. Consequently, aliasing occurs whenever the sampling rate, $S$, is below the Nyquist rate; i.e.,

$$S_N = \frac{1}{T} < \frac{1}{2} S_N$$

where $T$ is the sampling interval.

It is readily shown that a finite duration signal is not band limited and also that representing a transient by a finite length digitized record will always have aliasing error. Specifically, aliasing is the effect of a high frequency component in a signal taking on the identity of a lower frequency component.

Generally, an aliasing error is not significant if the frequency content of the digitized signal is small for frequencies near and above the sampling rate. Undersampling is significant when it is manifested in the time domain by a signal variation that is too rapid for the sampling rate to capture it. It can be detected at times by an apparent clipping of signal peaks. In the frequency domain, the aliasing error is manifested by anomalous high frequencies near the Nyquist folding frequency ($F_N$).

$$F_N = \frac{1}{2} S$$

The effects of aliasing are exacerbated by the presence of wide band noise, especially random noise. However, aliasing effects can be minimized by filtering the data with a low pass filter having a cutoff frequency equal to the Nyquist folding frequency prior to digitizing. This may not be desirable since the filter itself will affect the frequency content below $F_N$ and may disguise the presence of an important high frequency content.

In order to examine the cumulative effects of random noise, aliasing, and digital filtering, several NEMP-like signals (analytic representations) are considered. By successively adding noise and varying sampling rates, it is
possible to establish general behavior resulting from these effects and to quantify the results. Digital filtering is also introduced and general techniques for trend removal are discussed.

When broadband frequency signals are sampled at a rate fast enough to capture the high-frequency content, the limitation on the number of samples generally does not provide a sufficient record length to capture the low-frequency content of the signal. Consequently, multiple digitizers are used with sequenced triggering and different sampling rates. Typically, for NEMP test data, digitizers based on cathod-ray tube (CRT) scan converter technology are used where each unit obtains only 512 time samples. These records are combined to form a composite waveform. A uniformly sampled record is constructed via decimation and interpolation. Generally, the errors resulting from this procedure are not known. This topic is reserved for future study.

In order to categorize the characteristics of NEMP-induced signals that are important in invoking system responses, certain norms have been proposed (Ref. 2). The effects of sampling rates, random noise, digital filtering, and data trends on the norms are studied by using the analytical representations of typical data and introducing simulated noise and data trends. Results are obtained for various sampling rates and digital filtering schemes.
Several problems arise in collecting digitized response data from NEMP tests. Each of these problems are studied beginning with sampling.

2.1 SAMPLING

Typically, the voltage and current transients that result from NEMP excitation have substantial frequency content over the frequency range from 500 kHz to 100 MHz. Thus, the sampling of the data must faithfully capture that information. This introduces constraints on the sampling rate and the record length.

The upper bound on the frequency range of sampled data is determined by aliasing. A detailed explanation of aliasing is given by R. K. Otnes and L. Enochson in Ref. 3. It is not possible to determine precisely the least upper frequency bound. However, it is less than the Nyquist folding frequency given by Eq. 1. Ideally, the frequency content near the Nyquist frequency should be substantially below the peak frequency. If the frequency peaks near the Nyquist folding frequency, then the spectrum of the digitized data will be contaminated by aliasing for frequencies substantially below the Nyquist folding frequency.

The lower bound on the frequency range of the digitized data depends upon the record length and the total time duration of the sampling. A fundamental computational concept is that of an effective resolution bandwidth \( B_e \), which is defined as

\[
B_e = \frac{1}{NT}
\]  

(4)

where \( N \) is the number of time samples accumulated during a given signal time interval, \( T \). Any variations in the spectrum of the signal being digitized that occur over a bandwidth less than \( B_e \) will be substantially distorted by the digitizing. Consequently, the spectrum of the digitized signal will not be accurate for frequencies below \( f_L \) where
Moreover, it should be noted that resonant peaks that are narrower than $B_e$ will not be correctly preserved in the digitized signal.

In general, the instrumentation (sensors, data link, etc.) limits the frequency band of accurate data. Typically, the upper limit on frequency for NEMP testing is about 100 MHz. Therefore, a sampling rate of $200 \times 10^6$/s (or a sampling interval of 2 ns) is sufficient, providing that the spectral content is negligible above 100 MHz so that aliasing does not corrupt the spectrum below 100 MHz. One means of reducing this corruption is to use a low-pass filter. This is discussed in the next section.

2.2 DIGITAL FILTERING

Recent advances in digital filter development have made available a variety of filters that can be applied directly to digitized time-domain data. For example, filtering can be used to limit the bandwidth of the data and to interpolate between sampling points to eliminate dropout errors. However, care must be exercised in using digital filters since they can increase the noise level, introduce distortion, and become unstable in some applications.

Digital filtering may be used to reduce the aliasing in data, but requires a multistep process. First, the data are oversampled; i.e., they are sampled at a higher rate than is needed. Second, the data are then passed through a low-pass digital filter with the cutoff frequency equal to the Nyquist folding frequency for the sampling rate desired. Third, the filtered data are decimated to achieve the desired sampling rate. Of course, an alternative procedure could utilize a hard-wired low-pass filter and direct sampling at the desired rate.

Choosing a digital filter involves consideration of the memory required, computational speed, accuracy, distortion and stability. There is no perfect rule to follow. However, cascading lower-order filters should be used rather than higher-order filters. This generally results in a filter that is more stable and freer of noise and distortion. But the cascade implementation is computationally less efficient than the combined higher-order filter.
If the response signal is smooth, then the spectral density at the lower frequencies must exceed the spectral density in the high frequency regime. Generally, this does occur for NEMP test data. In fact, it is often this property of the data that is used to determine the quality of the data. Since the spectrum of random noise is flat, the response signal spectrum becomes noise dominated at higher frequencies. By passing the data through a low-pass filter whose cutoff frequency equals the signal/noise crossover frequency, it is possible to reduce the noise and improve the signal-to-noise ratio \( \text{SNR} \). This crossover frequency often can be obtained by visually inspecting the Fourier transform of the measured data (for example, see Fig. 2).

Recently a technique was developed to automatically determine the signal/noise crossover frequency and apply an ideal low pass filter to improve the SNR (Ref. 4). As a result of this process, the response signal is approximated by a band-limited signal. Then the discrete frequency Fourier transform pair is directly relatable to the continuous Fourier transform pair without approximations.

2.3 **NOISE**

There are a number of noise sources contributing to NEMP data. Many of these sources can be controlled by good measurement techniques. First, noise is picked up from the environment by the measurement instrumentation responding to the NEMP. Second, there is the inherent noise of the measurement system. Third, there is noise from the sampling device. Obviously, these noise sources do not produce totally random noise. However, for most practical purposes, the noise can be considered to be random.

2.4 **DATA TRENDS**

Slowly varying trends in NEMP data are common. These normally arise from integrated data where an error in the zero baseline when integrated produces a ramp function. Another source of data trends is the amplification of low frequency noise by an integrator. This type of trend is manifested in a slowly varying random behavior, and is somewhat dependent upon the sampling rate. The varying trend is best removed by a high-pass filter with the cutoff frequency set equal to \( f_L \).
The ramp trend is easily recognized to be spurious. It is an example of a polynomial trend and can be removed by using least squares techniques (Ref. 3). If it is only required to remove the direct current (dc) bias and the ramp trends, then Eq. 6 is used.

\[
\hat{x}(n) = x(n) - [C_o + (nT)C_I] \quad n = 0, 1, \ldots, N - 1
\]  

(6)

where \(\hat{x}(n)\) is the detrended data, \(x(n)\) is the raw data and

\[
C_o = [2(2N - 1)] \sum_{n=0}^{N-1} x(n) - 6 \sum_{n=0}^{N-1} nx(n)]/N(N + 1)
\]

(7)

\[
C_I = 12 \left[ \sum_{n=0}^{N-1} nx(n) - 0.5(N - 1) \sum_{n=0}^{N-1} x(n) \right]/TN(N^2 - 1)
\]

(8)

Generally, the foregoing treatments of data should be applied, if possible, to the processed data; i.e., the data that have been corrected for sensor response and the system transfer function. Some NEMP test data require integration, such as, the electric and magnetic free-field sensor data. Usually, this is accomplished by hardware. However, software implementation is possible provided detrending procedures are used. If Fourier transforms of the data are required, then the detrending of the data should be performed before a transform algorithm is implemented.

2.5 NORMS

Time-domain responses to NEMP illumination are varied and are, in general, quite complex. In an attempt to identify a minimum set of system response parameters, certain norms have been suggested (Ref. 5). These include the following norms for each system's time response:

\[
|x(t)|_{max.\over all \ t} \quad \text{PEAK VALUE}
\]

(9)
It is clear that the norms will be sensitive to sampling, filtering, noise, and data trends. These topics are investigated by considering certain NEMP-like response data with additive White-Gaussian noise combined with different sampling intervals.

2.6 COMPOSITE WAVEFORMS

For the fast transient signals induced by NEMP testing, digitizers based on CRT scan converter technology have been used. These devices provide a record length of only 512 samples. Consequently, the sampling rate required to capture the high frequency content does not provide sufficient resolution bandwidth (Refs. 2 and 4). In order to compensate for this lack of resolution, more than one digitizer is used with time delay in triggering to record the waveform. Typically, three digitizers are used in a sequenced triggering scheme with some overlapping in the recorded signals and with different

*The action integral is not truly a norm according to the mathematical definition of norms.
sampling rates. A composite signal is formed by using an interpolation scheme such as spline interpolation to tie the signals from the individual recorders. Testing algorithms have been developed to evaluate the veracity of the results (Ref. 6).

Recently, a digitizer was developed that uses a demultiplexing scheme and arrays of charged-coupled devices (CCD) to achieve very high sampling rates (≤1,348 gigasamples/s) and a long record length (10,240 samples) with a resolution of 8 bits (Ref. 7). This device would obviate the need for using composite waveforms for most applications. However, they have not been available for enough time to be employed extensively.

Since the existing NEMP test data have been collected in composite records, there is a need for quantitating the effects of forming composite records. This may be accomplished by simulating the process of forming composite records while using general analytical data with added White-Gaussian noise. This study is currently underway.
3.0 NUMERICAL RESULTS

The study of the accuracy and limitations of digitizing test transient data is conducted by considering three analytically derived generic time-domain waveforms. In general, the system response data for NEMP illumination can be expressed as superposition of damped sinusoids; i.e.,

\[ x(t) = \sum_{\alpha=1}^{N_p} C_{\alpha} e^{s_{\alpha}t} + \text{complex conjugates} \]

\[ = 2 \sum_{\alpha=1}^{N_p} |C_{\alpha}| e^{s_{\alpha}t} \cos(j\omega_{\alpha}t + \phi_{\alpha}) \]  \hspace{1cm} (15)

where

- \( x(t) \) = sample of response as a function of time
- \( N_p \) = number of complex poles
- \( C_{\alpha} \) = complex residues
- \( S_{\alpha} \) = complex poles
- \( t \) = time
- \( |C_{\alpha}| \) = absolute value of the complex residues
- \( e \) = 2.71828
- \( s_{\alpha} \) = attenuation constant
- \( \omega_{\alpha} \) = resonant radian frequency
- \( j = \sqrt{-1} \)
- \( \phi_{\alpha} \) = phase

Consequently, the three generic data sets, A, B, and C are expressed in terms of poles and residues in Tables 1, 2, and 3, respectively.
TABLE 1. Data set A, simulating data for small aircraft system.

| \( \alpha \) | \( |C_\alpha| \) | \( \phi_\alpha \) | \( \sigma_\alpha \) | \( \omega_\alpha/2\pi \) |
|---|---|---|---|---|
| 1 | 240 | 18° | -9.9 \times 10^6 | 8.7 \times 10^6 |
| 2 | 38 | 216° | -19 \times 10^6 | 27 \times 10^6 |
| 3 | 19 | 48° | -25 \times 10^6 | 45 \times 10^6 |

TABLE 2. Data set B, simulating data for a medium aircraft system.

| \( \alpha \) | \( |C_\alpha| \) | \( \phi_\alpha \) | \( \sigma_\alpha \) | \( \omega_\alpha/2\pi \) |
|---|---|---|---|---|
| 1 | 240 | 71° | -4.0 \times 10^6 | 3.5 \times 10^6 |
| 2 | 38 | -126° | -7.5 \times 10^6 | 11 \times 10^6 |
| 3 | 19 | 42° | -9.9 \times 10^6 | 1.8 \times 10^6 |

TABLE 3. Data set C, simulating data for a large aircraft system.

| \( \alpha \) | \( |C_\alpha| \) | \( \phi_\alpha \) | \( \sigma_\alpha \) | \( \omega_\alpha/2\pi \) |
|---|---|---|---|---|
| 1 | 0.27 | -90° | -0.65 \times 10^6 | 2.0 \times 10^6 |
| 2 | 0.31 | -90° | -1.7 \times 10^6 | 3.6 \times 10^6 |
| 3 | 0.63 | -90° | -1.1 \times 10^6 | 5.5 \times 10^6 |
| 4 | 0.79 | -90° | -1.6 \times 10^6 | 8.9 \times 10^6 |

NOTE:

| \( |C_\alpha| \) | Absolute value of the complex residues (amplitude) |
| \( \phi_\alpha \) | Phase |
| \( \sigma_\alpha \) | Damping coefficient |
| \( \omega_\alpha/2\pi \) | Frequency |
White-Gaussian noise with a zero mean value is added to the data. The resulting SNR is defined:

\[
\text{SNR} = \frac{\text{peak signal}}{\text{standard deviation of noise}}
\]  

(16)

In Figs. 3 through 7, two noise levels are considered with the generic data sets and the resulting Fourier transforms are exhibited. These data are followed by Figs. 8 through 13 where the effects of sampling rates are presented. And finally, Figs. 14 through 19 present the combined effects of noise and sampling. The selections of noise levels and sampling rates were made to coincide with those of recent NEMP tests. The transformed data are plotted up to the Nyquist folding frequency for the respective sampling rates. Clearly, the minimum requirements for accurate data from 500 kHz to 100 MHz require that:

\[
\text{SNR} > 30 \text{ dB}
\]  

(17)

\[
T < 2 \text{ ns}
\]  

(18)

\[
NT > 2 \mu\text{s}
\]  

(19)

where

- \(T\) = sampling interval
- \(N\) = total number of data samples

This is also seen in Figs. 20 through 27 where corresponding time-domain results are exhibited.

Treatment of data with digital filtering and detrending can improve their quality. This is shown in Figs. 20 through 39. A ramp trend is introduced into each of these data set and the turnon time is set a zero. The time-domain graphs (Figs. 28 through 33) clearly exhibit the ramp trend before and after detrending. However, caution is needed in using the detrending procedure on signals where the record length is less than the signal duration. Severe signal distortion may occur in this situation.
The spectral effects of trends are shown in Figs. 34 through 39. Two prominent effects are easily seen. First, the trend introduces an anomalous low frequency spectral content; and second, the termination of the ramp at the end of the record introduces a spurious high frequency spectrum. However, with the trend removed, the spectrum becomes more accurate. A comparison of the detrended signal in Fig. 34 with the original signal spectrum in Fig. 3 shows some differences. This results from the use of an extremely low frequency signal component added to the data to introduce the trend; whereas, the trend was removed by using a least-squares fit to a straight-line trend.

Norm data are best presented in tabular form. Tables 4 and 5 present typical results for norm calculations from noisy and undersampled data. As might be expected, with a moderate noise level, SNR ≥ 20 dB, little error was introduced into the peak value. The impulse and action integral norms exhibit moderate errors. However, the peak rate-of-rise and rectified impulse norms exhibit substantial errors (up to 666 percent). Also, the noise tended to increase the norm values. For severe noise levels; i.e., SNR < 10 dB, very large errors are observed. These errors are sufficiently large that the norm calculations are not valid. It also appears that the norm errors are sensitive to the waveshape. The peak norm appears to be least affected by the errors.

The undersampling of data tended to provide substantial errors in the rate-of-rise norms. However, the other norms were not affected as much. In general, undersampling resulted in reduced norm values.
TABLE 4. Small aircraft external response norm errors (%).

<table>
<thead>
<tr>
<th>SAMPLE INTERVAL/SNR</th>
<th>PEAK</th>
<th>PEAK RATE OF RISE</th>
<th>IMPULSE</th>
<th>RECTIFIED IMPULSE</th>
<th>ACTION INTEGRAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 ns/30 dB</td>
<td>1.9</td>
<td>7.6</td>
<td>34.0</td>
<td>63.0</td>
<td>4.5</td>
</tr>
<tr>
<td>2 ns/20 dB</td>
<td>12.7</td>
<td>23.6</td>
<td>87.7</td>
<td>201.9</td>
<td>30.4</td>
</tr>
<tr>
<td>5 ns/∞</td>
<td>1.4</td>
<td>60.6</td>
<td>26.9</td>
<td>2.5</td>
<td>3.0</td>
</tr>
<tr>
<td>5 ns/30 dB</td>
<td>1.9</td>
<td>57.7</td>
<td>34.9</td>
<td>180.1</td>
<td>11.1</td>
</tr>
<tr>
<td>5 ns/20 dB</td>
<td>2.8</td>
<td>51.9</td>
<td>38.2</td>
<td>93.6</td>
<td>61.8</td>
</tr>
<tr>
<td>10 ns/∞</td>
<td>1.4</td>
<td>80.3</td>
<td>33.3</td>
<td>1.2</td>
<td>1.8</td>
</tr>
<tr>
<td>10 ns/20 dB</td>
<td>10.8</td>
<td>78.5</td>
<td>152.7</td>
<td>88.0</td>
<td>102.3</td>
</tr>
</tbody>
</table>

TABLE 5. Large aircraft internal response norm errors (%).

<table>
<thead>
<tr>
<th>SAMPLE INTERVAL/SNR</th>
<th>PEAK</th>
<th>PEAK RATE OF RISE</th>
<th>IMPULSE</th>
<th>RECTIFIED IMPULSE</th>
<th>ACTION INTEGRAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>2 ns/30 dB</td>
<td>2.5</td>
<td>142.1</td>
<td>6.5</td>
<td>5.0</td>
<td>1.7</td>
</tr>
<tr>
<td>2 ns/20 dB</td>
<td>8.9</td>
<td>665.8</td>
<td>20.5</td>
<td>28.1</td>
<td>11.6</td>
</tr>
<tr>
<td>5 ns/∞</td>
<td>0.0</td>
<td>1.2</td>
<td>1.3</td>
<td>17.4</td>
<td>0.8</td>
</tr>
<tr>
<td>5 ns/30 dB</td>
<td>0.0</td>
<td>1.2</td>
<td>11.5</td>
<td>36.2</td>
<td>1.7</td>
</tr>
<tr>
<td>5 ns/20 dB</td>
<td>13.9</td>
<td>185.5</td>
<td>39.6</td>
<td>115.6</td>
<td>22.3</td>
</tr>
<tr>
<td>10 ns/20 dB</td>
<td>3.4</td>
<td>9.2</td>
<td>64.8</td>
<td>275.3</td>
<td>47.3</td>
</tr>
</tbody>
</table>
Figure 1. Typical system configuration for recording transient signals in NEMP testing.
Figure 2. Small aircraft external response for a 2 ns sampling interval and 10 dB SNR.
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Figure 4. Large aircraft internal response for a 2 ns sampling interval and 10 dB SNR.
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Figure 6. Large aircraft external response for 2 ns sampling interval and 30 dB SNR.
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Figure 23. Large aircraft interior time domain response for 2 and 30 ns sampling intervals and 10 dB SNR.
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Figure 39. Large aircraft internal response for (1) 10 ns sampling interval and 20 dB SNR trend and (2) detrended sample.
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