

# DTIC FILE COPY

MASTER COPY - FOR REPRODUCTION PURPOSES

UNCLASSIFIED

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

2

AD-A201 609

## REPORT DOCUMENTATION PAGE

READ INSTRUCTIONS  
BEFORE COMPLETING FORM

1. REPORT NUMBER

AR 21817.23-E6

2. GOVT ACCESSION NO.

N/A

3. RECIPIENT'S CATALOG NUMBER

N/A

4. TITLE (and Subtitle)

Sliding and Debonding Inclusions

5. TYPE OF REPORT & PERIOD COVERED

Final Report  
June 15, 1985 - June 30, 1988

6. PERFORMING ORG. REPORT NUMBER

7. AUTHOR(s)

T. Mura

8. CONTRACT OR GRANT NUMBER(s)

DAAG29-85-K-0134

9. PERFORMING ORGANIZATION NAME AND ADDRESS

Department of Civil Engineering  
Northwestern University  
Evanston, IL 60208

10. PROGRAM ELEMENT, PROJECT, TASK  
AREA & WORK UNIT NUMBERS

N/A

11. CONTROLLING OFFICE NAME AND ADDRESS

U. S. Army Research Office  
Post Office Box 12211  
Research Triangle Park, NC 27709

12. REPORT DATE

August 15, 1988

13. NUMBER OF PAGES

14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office)

15. SECURITY CLASS. (of this report)

Unclassified

15a. DECLASSIFICATION/DOWNGRADING  
SCHEDULE

16. DISTRIBUTION STATEMENT (of this Report)

Approved for public release; distribution unlimited.

17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)

NA

DTIC  
ELECTE  
OCT 20 1988  
S D  
CD  
D

18. SUPPLEMENTARY NOTES

The view, opinions, and/or findings contained in this report are those of the author(s) and should not be construed as an official Department of the Army position, policy, or decision, unless so designated by other documentation.

19. KEY WORDS (Continue on reverse side if necessary and identify by block number)

→ sliding inclusions, composite materials, DeBANDING, INCLUSIONS, shear STRESS, Linear Theory. (B)KE

20. ABSTRACT (Continue on reverse side if necessary and identify by block number)

Research results performed during this research contract are summarized in the following pages.

SLIDING AND DEBONDING INCLUSIONS

Final Report

T. Mura

August 15, 1988

U.S. Army Research Office

Grant Number DAAG29-85-K-0134

Department of Civil Engineering  
Northwestern University  
Evanston, Illinois 60208



Approved for Public Release  
Distribution Unlimited

Accession For	
NTIS CRA&I	<input checked="" type="checkbox"/>
DTIC TAB	<input type="checkbox"/>
Unannounced	<input type="checkbox"/>
Justification	
By _____	
Date _____	
Distribution/Classification	
A-1	

List of Publications Published under ARO Sponsorship during this period

1. R.R. Castles and T. Mura, The analysis of eigenstrains outside of an ellipsoidal inclusion, Journal of Elasticity, 15 (1985) 27-34.
2. T. Mura, General Theory of Inclusions, In Fundamentals of Deformation and Fracture, Eshelby Memorial Symposium, ed. by B.A. Bilby, K.J. Miller and J.R. Willis, Cambridge University Press, Cambridge (1985) 75-89.
3. T. Mura, Boundary Problems for Dislocations, In Dislocations in Solids, Yamada Conference IX, ed. by Hideji Suzuki, Toshiyuki Ninomiya, Koji Sumino and Shin Takeuchi, University of Tokyo Press (1985) 17-23.
4. T. Mura, Sliding Inclusions, In The Mechanics of Dislocations, International Symposium on Mechanics of Dislocations, ed. by Elias C. Aifantis and John P. Hirth, American Society of Metals (1985) 77-79.
5. T. Mura and M. Taya, Residual stresses in and around a short fiber in metal matrix composites due to temperature change, in Recent Advances in Composites in the United States and Japan, ed. J.R. Vinson and M. Taya, ASTM STP 864, (1985) 209-224.
6. Y. Hirose and T. Mura, Crack nucleation and propagation of corrosion fatigue in high-strength steel, in Engineering Fracture Mechanics, 22 (1985) 859-870.
7. T. Mura, A note on the crack opening displacement, in Mechanics of Materials, 4 (1985) 213-214.
8. T. Mura, I. Jasiuk, and B. Tsuchida, The stress field of sliding inclusion, Int. J. Solids and Structures, 21 (1985) 1165-1179.
9. T. Mura, A new NDT: Evaluation of plastic strains in bulk from displacements on surfaces, Mechanics Research Communications, 12 (1985) 243-248.
10. Y. Hirose and T. Mura, The effect of prior austenite grain size on the stress corrosion cracking susceptibility of AISI 4340 steel, in Predictive Capabilities Environmentally Assisted Cracking, ed. R. Rungta, ASME PVP 99 (1985) 245-257.
11. E. Tsuchida, T. Mura and J. Dundurs, The elastic field of an elliptic inclusion with a slipping interface, J. Appl. Mech., 53 (1986) 103-107.
12. N. Kinoshita and T. Mura, An ellipsoidal inclusion with polynomial eigenstrains, Quart. Appl. Math., 44 (1986) 195-199.

13. Y. Hirose, Z. Yajima, and T. Mura, X-ray fractography on fatigue fracture surfaces of AISI 4340 steel, in Advances in X-ray Analysis, eds. C.S. Barrett, J.B. Cohen, J. Faber, R. Jenkins, D.E. Leyden, J.C. Russ and P.K. Predecki, Plenum Pub. Co., 29 (1986) 63-70.
14. D.A. Kouris, E. Tsuchida, and T. Mura, An anomaly of sliding inclusions, J. Appl. Mech., 53 (1986) 724-726.
15. T. Mura, I.M. Jasiuk, D.A. Kouris, and R. Furuhashi, Recent results of the equivalent inclusion method applied to composite materials, in Composite '86 Recent Advances in Japan and the United States, eds. K. Kawata, S. Umekawa and A. Kobayashi, Proc. Japan-U.S., CCM-III, Tokyo (1986) 169-177.
16. E.N. Mastrojannis, L.M. Keer, and T. Mura, Thin circular plate under temperature loading in adhesive contact with an elastic half-space, J. Thermal Stresses, 10 (1987) 71-81.
17. D.A. Sotiropoulos and T. Mura, Torsion of an elasto-plastic bar via a dislocation method, J. Appl. Mech., 54 (1987) 226-227.
18. S.J. Chang and T. Mura, Inclined pileup of screw dislocations at the crack tip with a dislocation-free zone, Int. J. Engng. Science, 25 (1987) 561-576.
19. R.R. Castles and T. Mura, Theory and application of harmonic eigenstrains, O.J. Mech. Appl. Math., 40 (1987) 169-188.
20. T. Mura, The eigenstrains method applied to fracture and fatigue mechanics, Role of Fracture Mechanics in Modern Technology, eds. G.C. Sih, H. Nishitani and T. Ishihara, North-Holland, (1987) 145-152.
21. T. Mura, R. Furuhashi and T. Mori, Sliding ellipsoidal inhomogeneities under shear, in Advanced Composite Materials and Structures, eds. G.C. Sih and S.E. Hsu, VNU Science Press, The Netherlands, (1987) f113-122.
22. T. Mori and T. Mura, Blocking effect of inclusions on grain boundary sliding; spherical grain approximation, J. Mech. Phys. Solids, 35 (1987) 631-641.
23. I. Jasiuk, E. Tsuchida, and T. Mura, The sliding inclusion under shear, Int. J. Solids Structures, 23 (1987) 1373-1385.
24. T. Mura, Inclusion problems, Appl. Mech. Rev., 41 (1988) 15-20.
25. I. Jasiuk, T. Mura, and E. Tsuchida, Thermal stresses and thermal expansion coefficients of short fiber composites with sliding interfaces, J. Engng. Materials and Technology (Trans. ASME), 110 (1988) 96-100.

26. B.N. Cox, D.B. Marshall, D. Kouris, and T. Mura, Surface displacement analysis of the transformed zone in magnesia partially stabilized zirconia, J. Engng. Materials and Technology (Trans. ASME), 110 105-109.
27. M. Morinaga, N. Yukawa, H. Adachi, and T. Mura, Electronic state of interstitial atoms (C, N, O) in FCC Fe, J. Phys. F: Met. Phys., 18 (1988) 923-934.
28. T. Mura, Advancement of Micromechanics, Japan Soc. Precision Eng., 54 (1988) 1040-1045.
29. A. Sato, Y. Watanabe, and T. Mura, Octahedral defects in a b.c.c. lattice examined by lattice theory, J. Phys. Chem. Solids, 49 (1988) 529-540.
30. E.N. Mastrojannis, L.M. Keer and T. Mura, Axisymmetrically loaded thin circular plate in adhesive contact with an elastic half-space, Computational Mechanics, 3 (1988) 283-298.

#### Books

31. T. Mura, Micromechanics of Defects in Solids, second, revised edition, Martinus Nijhoff Publ., The Hague (1987).

Scientific Personnel Supported by this project:

I. Jasiuk (Ph.d. earned), D. Kouris (Ph.D. earned) Dr. E. Tsuchida, Dr. K. Saito, Dr. S.J. Chang, Z. Gao (Ph.D. earned), Dr. Y. Hirose, Dr. E. Tsuchida, Dr. N. Yamashita, Dr. R. Furuhashi, Dr. H. Sekine, K. King, A. Safadi, W. Yeih

Statements of Problems and Summary of Results:

It was found by Mura and Furuhashi, [J. App. Mech. 51 (1984) 308-310], when an ellipsoidal inclusion undergoes a uniform shear eigenstrain in the principal axis directions and the inclusion is free to slip along the interface, the stress field vanishes everywhere in the inclusion and the matrix. This finding is the main result of the ARO research grant DAAG29-81-K-0090.

The main objective of the present grant DAAG29-85-K-0134 is to give more theoretical investigation on this amazing finding and to find applications to composite materials.

This anomaly of sliding inclusions is based upon the fact that an ellipsoid is transformed into an identical ellipsoid by the uniform shear in the principal axis directions of the ellipsoid in the framework of linear theory as demonstrated by Mura [2,4].

When the ellipsoidal inhomogeneity embedded in an infinite medium is subjected to an applied shear stress at infinity in the directions of the principal axes of the ellipsoid, the inhomogeneity behaves like a void if the interface can slide freely. When the ellipsoid is degenerated into a spheroidal, the shear eigenstrains introduce the stress field and the spheroidal inhomogeneity does not behave like a void. The elastic solution of circular inhomogeneity under shear can not be obtained as a limiting case of the elliptical inhomogeneity [14].

When the eigenstrains inside the ellipsoidal inclusion are not of the shear type, non-zero stress fields are introduced. The associated solutions are completely different from Eshelby's solution. By using the Papkovitch-Neuber potentials, we obtained various solutions corresponding to the type of applied loads and of non-shear eigenstrains [8,11,23].

- 
1. The reference numbers in the List of Publications Published under ARO Sponsorship during the grant period.

These solutions are applied to investigate mechanical behavior of composite materials when constituents can slide [5,15,21,22,25,26].

Along the research of sliding inclusions, the perfectly bonded inclusions were also investigated for non-uniform eigenstrains [1,12,19]. These results are further extensions of Eshelby's inclusions.

Another research was conducted to investigate fracture and fatigue of alloys. The interest of the research is to evaluate the interaction between the dislocation pile-up and imperities (particles) [6,7,10,13,18,20]. More microscopic approach was employed by solving Schrödinger's equation in quantum mechanics to evaluate the eigenstrain (misfit strain) caused by a hydrogen atom in the iron lattice [20,27,29]. Series of experiments for the crack initiation time due to the stress corrosion and the corrosion fatigue were performed and compared with the theory of dislocation pile-up model [6,10]. The reasoning of the detached crack initiation at notch roots and the depending of the notch radii were explained with satisfaction when the result of quantum mechanics is used.

Finally, literature research was performed concerning publications on sliding and debonding inclusions. The work is summarized in [24,31].