Stimulated Raman Scattering of Intense Laser Radiation in a Nuclear-Disturbed Space Plasma

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November 8, 1988

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Interim

1988 November 8

19 Stimulated Raman scattering of intense laser radiation propagating in a nuclear-disturbed space plasma environment has been investigated. For parameters typical of a single high altitude nuclear explosion (HANE), we propagation due to Raman scattering, particularly for 10 μm radiation. 10 μm, respectively, and for beam power densities on the order of $10^5 \text{ W/cm}^2$. Here $\gamma$ is the growth rate for simulated Raman scattering. For the multiple HANE case, approximate growth times $\gamma^{-1} \approx 10^{-3} - 10^{-2}$ sec can be achieved for laser wavelengths 1 μm and 10 μm with beam power densities of $10^6 \text{ W/cm}^2$. As a result, a single burst HANE is not likely, due to stimulated Raman scattering, to effect the propagation of laser radiation with wavelengths of 10 μm and 1 μm and power densities on the order of $10^5 \text{ W/cm}^2$. However, the multiburst HANE environment may degrade laser propagation due to Raman scattering, particularly for 10 μm radiation.
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I. INTRODUCTION

A key component of proposed Strategic Defense Initiative (SDI) systems is high power coherent radiation sources, either ground or space-based. The propagation characteristics of such radiation beams in the ambient and nuclear-disturbed environment is of the utmost importance for the successful implementation of SDI goals and objectives.

Much work has been devoted to the study of laser propagation in the ambient atmosphere\(^1,2\). For low beam power densities, well known effects such as turbulence broadening of the beam, distortion of beam spatial coherence, and random refraction and wander of the beam have been studied both experimentally and theoretically. At higher beam power densities, nonlinear effects, e.g., thermal blooming, stimulated scattering, and optical breakdown can play an important role in beam propagation by enhancing beam absorption and scattering.

For the nuclear-disturbed environment, while many studies have been made to assess the impact of the high altitude nuclear explosion (HANE) environment on the propagation of radiation in the radio frequency range,\(^3\) very little work has been performed, particularly at high beam power densities, dealing with laser and optical propagation through the HANE environment.\(^4-6\) In this study we focus on plasma parametric instabilities driven by the radiation beam. These instabilities are dependent on the beam power density and can affect beam propagation by scattering beam radiation energy. The fastest growing plasma parametric instabilities will involve high frequency electron dynamics.\(^5\) From the results of our initial work\(^5\) we focus on stimulated Raman scattering (SRS) since this instability can be quite rapid and can grow on fast \(\omega_{pe}^{-1}\) time scales where \(\omega_{pe}\) is the electron plasma frequency. The outline of this report is as follows. In

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Section II we outline the theory and attendant assumptions in stimulated Raman scattering in nuclear-disturbed plasmas. In Section III we present our results giving growth rates of stimulated Raman scattering (SRS) for a typical single HANE. In addition we also compute growth rates for SRS for the multi-burst case. Finally, in Section IV we summarize and discuss our results.

II. THEORETICAL MODEL

The basic geometry of our model consists of a monochromatic electromagnetic wave with frequency $\omega_0$ and wavenumber $k_0$ propagating in a plasma imbedded in a magnetic field as shown in Fig. 1. Since we are considering frequencies $\omega_0 > \omega_{pe}$, $\Omega_e$ the effects of the ambient magnetic field on the electromagnetic wave will be small. Here $\omega_{pe}$ is the electron plasma frequency and $\Omega_e$ the electron gyrofrequency. In addition, since we will be investigating the scattering of high frequency modes with frequencies $|\omega| > \omega_{pe} > \Omega_e > \omega_{pi} > \Omega_i$, i.e., Langmuir waves, we take, as a first approximation, the electrons and ions to be unmagnetized. Here $\omega_{pi}$ is the ion plasma frequency and $\Omega_i$ the ion gyrofrequency. As a result, the general equilibrium implied by our model consists of electrons oscillating with high velocity $v_o = eE_o/m_e\omega_0$ in a stationary ion background where $e$ is the electron charge, $E_o$ the electric field associated with the incident electromagnetic wave, and $m_e$ is the electron mass.

If one perturbs this equilibrium with a density and electric field perturbation of the form exp $[i(k_1 \cdot x - \omega_1 t)]$ then beat oscillations will form with frequency $\omega_2 = \omega_1 \pm \omega_0$ and wave number $k_2 = k_1 \pm k_0$. These sidebands will in turn beat with $(\omega_0, k_0)$ and cause the growth or decay of the mode $(\omega_1, k_1)$ provided the Manley-Rowe relations
\[ \omega_0 = \omega_1 + \omega_2 \]  
(1a)

\[ k_0 = k_1 + k_2 \]  
(1b)

are satisfied. As a result, a Langmuir wave and a sideband electromagnetic wave can be parametrically driven to large amplitudes at the expense of the pump electromagnetic wave.

When \( \omega_1 = \omega \) and \( k_1 = k \) are Langmuir waves, the dispersion relation for stimulated Raman scattering can be found using the combined Vlasov-Maxwell equations and standard techniques to yield

\[\frac{1}{X_e} + \frac{1}{X_i} + 1 = \frac{2k^2v_e^2\sin^2\alpha \cos^2\theta}{\omega_0(\omega - \Delta \omega + i\gamma_d)} \]

where \( \alpha \) is the angle between the beat wave \( k - k_0 \) and \( v_o \) (see Fig. 2), \( \theta \) is the angle between \( k \) and \( k_0 \), \( \Delta \omega = (c^2/\omega_0)(k \cdot k_0 - k^2/2) \), \( \gamma_d \) is the damping rate of the free electromagnetic wave with \( \gamma_d = v_e\omega_e^2/2\omega_0^2 \), \( v_e \) is the electron collision frequency, and \( X_e (X_i) \) is the electron (ion) susceptibility given by

\[ X_e(\omega, k) = 2 (k\lambda_D)^{-2} \left[ 1 + \zeta_e Z(\zeta_e) \right] \left[ 1 + (i v_e/kv_e)Z(\zeta_e) \right]^{-1} \]

and
$$\chi_i(\omega, k) = 2(T_e/T_i)(k\lambda_D)^{-2}[1 + \zeta i Z(\zeta)]$$

with $\zeta = (\omega + iv_e)/kv_i$, $\zeta_i = \omega/kv_i$, $\lambda_D$ is the Debye length, $v_e(v_i)$ is the electron thermal velocity, $Z$ is the plasma dispersion function and $T_e(T_i)$ is the electron (ion) temperature. We note that the Manley-Rose relation requires $k = 2k_0\cos\theta$ in Eq. (2).

Eq. (2) has been solved for $\omega = \omega_r + iy$ in several limits. For example, if $k\lambda_D = 2k_0\cos\theta\lambda_D \ll 1$, so that the plasma wave is not heavily damped, it is found $^7,^8$ that $\omega_r = (\omega_{pe}^2 + k^2v_e^2)^{1/2}$, the Bohm-Gross frequency, and

$$\gamma = -\frac{1}{2}(\gamma_p + \gamma_d) \pm \frac{1}{2} \left[ (\gamma_p - \gamma_d)^2 + 4(\nu_o/c)^2 \sin^2\alpha \cos^2\theta \omega_o \omega_{pe} \right]^{1/2}$$

where $\gamma_p$ is the total damping (Landau and collisional) rate of the free plasma wave. The threshold beam power density is

$$\left(\frac{\nu_o}{c}\right)^2_{TH} = \sin^{-2}\alpha \cos^{-2}\theta (\gamma_p/\omega_{pe})(\gamma_d/\omega_o)$$

(4)

giving maximum growth rate for $\gamma_{\text{max}}$ far above threshold ($\gamma_p \ll \gamma \ll \omega_{pe}$)

$$\gamma_{\text{max}} = (\nu_o/c)|\sin\alpha|\cos\theta(\omega_o \omega_{pe})^{1/2}$$

(5)
In this case the growth rate assumes a linear dependence on $E_0$ or $v_o$ if $(v_o/c) > [\gamma_p] \sin \alpha \cos \theta (\omega \omega_p)^{1/2}$. On the other hand, for short wavelengths $k \lambda_D = 2k_o \cos \theta >> 1$, it can be shown\textsuperscript{7,8} that

$$\omega = \omega + 2(v_o/c)^2 \sin^2 \alpha \cos^2 \theta \omega_o \left[ \chi_e (\omega, 2k_o \cos \theta) / (1 + \chi_e (\omega, 2k_o \cos \theta)) \right] - i \gamma_d$$

(6)

giving a growth rate

$$\gamma = 2(v_o/c)^2 \sin^2 \alpha \cos^2 \theta \omega_o \text{Im} \left[ \chi_e (\omega, 2k_o \cos \theta) / (1 + \chi_e (\omega, 2k_o \cos \theta)) \right] - \gamma_d$$

(7)

If collisional damping of the electrostatic wave is neglected, Eq. (6) and (7) give $\omega = kv_e$ and

$$\gamma = (\omega_o/2) (v_o/c)^2 (\pi/2)^{1/2} \sin^2 \alpha \exp(-1/2) (k_o \lambda_d)^{-2} - \gamma_d$$

(8)

with threshold

$$(v_o/c)_{TH}^2 = (8/\pi)^{1/2} (\gamma_d / \omega_o) \exp(1/2) (k_o \lambda_D)^{-2} \sin^{-2} \alpha$$

(9)

and maximum growth rate

$$\gamma_{\text{max}} = (\omega_o/2) (v_o/c)^2 (\pi/2)^{1/2} \sin^2 \alpha \exp(-1/2) (k_o \lambda_D)^{-2}$$

(10)

For the nuclear environment the quantity $k_o \lambda_d$ can be of order unity with the result that Eq. (2) must be solved numerically.
III. RESULTS

We now proceed to solve Eq. (2) using parameters typical of HANE plasmas. For a CW laser with $10^8 \text{W}$ peak power with a 5-10 m beam diameter, we find beam power densities $I = 10^2 \text{W/cm}^2$ and resulting quiver velocities $v_o = 25.6 \left[ I(\text{W/cm}^2) \right]^{1/2} \lambda_L(\mu\text{m}) \text{ cm/sec} = 2.5 \times 10^3 \text{ cm/sec}$ where $\lambda_L$ is the laser wavelength. This gives nonrelativistic quiver velocities $v_o/c = 10^{-7}$. For the pulsed mode with $10^6 \text{J}$ of energy with repetition rate of 5μ sec, we find $v_o/c = 10^{-5}$.

Fig. 3(a)-(b) gives the growth rate $\gamma$ for stimulated Raman scattering as a function of $v_o/c$ for both the pulsed and CW modes using parameters typical of the later time ($t \geq 30 \text{ min}$) evolution of a single high altitude nuclear burst. At late times, the HANE plasma can extend several thousands (hundreds) of kilometers parallel (perpendicular) to the geomagnetic field and, as a result, provide a large plasma volume for scattering to occur. We take $n_e = 10^7 \text{ cm}^{-3}$, $T_e = T_i = 0.2 \text{ eV}$, and consider both 1 μm ($k_o\lambda_D = 6.2 \times 10^3$) and 10 μm ($k_o\lambda_D = 6.2 \times 10^2$) laser wavelengths. We find the shortest growth times $\gamma^{-1} = 1-10 \text{ sec}$ for the 10 μm case in the pulsed mode.

Fig. 4(a)-(b) displays the growth rate for stimulated Raman scattering as a function of $v_o/c$ again for both the pulsed and CW cases but using parameters typical of computer simulations [R. Dana, private communication] of a multiple high altitude nuclear burst scenario. Here we take $n_e = 2 \times 10^{11} \text{ cm}^{-3}$, $T_e = 2 \text{ eV}$, and consider both the 10 μm ($k_o\lambda_D = 10$) and 1 μm ($k_o\lambda_D = 100$) cases. Here we find much larger growth rates with the fastest occurring on time scales $\gamma^{-1} = 10^{-3} - 10^{-2} \text{ sec}$ for the pulsed mode. The growth rates $\gamma$ and corresponding growth times for the CW case are smaller due to the reduction in beam power density.
IV. SUMMARY AND DISCUSSION

We have computed the growth rates $\gamma$ of stimulated Raman scattering of both 10 $\mu$m and 1 $\mu$m laser radiation using plasma parameters typical of a single and multiple high altitude nuclear explosion. We have considered both CW and pulsed modes of laser operation using parameters representative of proposed SDI systems.

For the single burst case, we find relatively long e-folding growth times $\gamma^{-1} = 1-10$ sec in the late time regimes for both the 10 $\mu$m and 1 $\mu$m cases in the pulsed mode. The decreased power densities in the CW case result in much smaller growth rates and longer growth times.

On the other hand, for the multiple burst scenario, where plasma densities are expected to be much higher than the single burst case, we find faster growth times $\gamma^{-1} \sim 10^{-2}$ sec. For the pulsed 10 $\mu$m case typical e-folding growth lengths $L_e = c\gamma^{-1}$ are on the order of 100 km. For nuclear plume dimensions on the order of several thousands of kilometers, one would expect many e-folding lengths over which stimulated Raman scattering can grow. Depending on the angle of arrival of the beam with respect to the HANE plasma, which is expected to extend several thousands of kilometers in altitude, Raman scattering of beam energy in the multiburst case is expected to be strong with subsequent deleterious beam attenuation, erosion, and degraded propagation.

In order to more fully assess the impact of plasma parametric instabilities on beam propagation, several remaining issues need to be addressed. We have made the assumption of a homogeneous plasma. In all probability, the HANE plasma will be highly structured or turbulent on scale sizes comparable to the beam radius and smaller. This density
structure will affect the growth and evolution of Langmuir waves driven unstable by stimulated Raman scattering. In addition, we have not discussed nonlinear saturation mechanisms for stimulated Raman scattering in a nuclear environment. Resolution of these problems will give definitive information on beam propagation in the HANE environment.

Acknowledgments

We thank Dr. J.D. Huba and Dr. J.A. Fedder for discussions. This work was supported by SDIO/IST under contract to the Naval Research Laboratory.
References:


Fig. 1 Basic geometry of electromagnetic wave with wavenumber $k_0$, wave electric field $E_0$, and wave magnetic field $B_0$, propagating in plasma embedded in magnetic field $B_{\text{EXT}}$. 
Fig. 2  Definition of angles $\alpha$ and $\theta$ used in Eq. (2).
Fig. 3 Plot of growth rates $\gamma/\omega_{pe}$ vs. $v_0/c$ for stimulated Raman scattering for $N_e = 10^7$ cm$^{-3}$, $T_e = 0.2$ eV, $v_e = 5 \times 10^3$ sec$^{-1}$ with (a) $10^{-5} < v_0/c < 10^{-4}$ and (b) $10^{-7} < v_0/c < 10^{-6}$.
Fig. 3. (Continued) Plot of growth rates $\gamma/\omega_{pe}$ vs. $v_0/c$ for stimulated Raman scattering for $N_e = 1 \times 10^7$ cm$^{-3}$, $T_e = 0.2$ eV, $v_e = 5 \times 10^3$ sec$^{-1}$ with (a) $10^{-5} < v_0/c < 10^{-4}$ and (b) $10^{-7} < v_0/c < 10^{-6}$. 
Fig. 4  Plot of growth rates $\gamma/\omega_{pe}$ vs. $v_0/c$ for Raman scattering for $N_e = 2 \times 10^{11}$ cm$^{-3}$, $T_e = 2$ eV, $v_e = 10^6$ sec$^{-1}$ with (a) $10^{-5} < v_0/c < 10^{-4}$ and (b) $10^{-7} < v_0/c < 10^{-6}$. 

$\text{RAMAN SCATTERING}$

$N_e = 2 \times 10^{11}$ cm$^{-3}$

$\text{PULSED}$

$A: \lambda_l = 1 \mu\text{m}$

$B: \lambda_l = 10 \mu\text{m}$
Fig. 4. (Continued) Plot of growth rates $\gamma/\omega_{pe}$ vs. $v_o/c$ for Raman scattering for $N_e = 2 \times 10^{11}$ cm$^{-3}$, $T_e = 2$ eV, $v_e = 10^6$ sec$^{-1}$ with (a) $10^{-5} < v_o/c < 10^{-4}$ and (b) $10^{-7} < v_o/c < 10^{-6}$. 

$N_e = 2 \times 10^{11}$ cm$^{-3}$

CW

A: $\lambda_L = 1\mu$m

B: $\lambda_L = 10\mu$m