Theoretical Prediction of Ripple-Load Effect on Stress-Corrosion Cracking

G. R. Yoder, P. S. Pao, and R. A. Bayles

Mechanics of Materials Branch
Materials Science and Technology Division

May 31, 1988
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Yoder, George R., Pao, Peter S. and Bayles, R. A.

19. ABSTRACT (Continue on reverse if necessary and identify by block number)

The ripple-load effect (RLE) is a perplexing phenomenon in which the threshold stress-intensity factor (K_{isc}) for stress-corrosion cracking (SCC) appears to be severely degraded — at least in some cases, if the constant load condition characteristic of SCC is perturbed by superposition of a small-amplitude cyclic load. In this study, a theoretical framework has been developed to predict the conditions required for a material to exhibit a RLE in a marine environment — and the extent of such degradation. Insofar as a framework for the RLE necessarily involves the interface between SCC and corrosion fatigue (CF), the model presented herein derives from concepts and descriptors used in SCC and CF characterization. Thus, analysis begins with consideration of the relationship between the small amplitude stress-intensity range associated with ripple loading, ΔK, the high stress-ratio conditions, R > 0.90, the threshold for CF crack growth, AK_{th}, the maximum stress-intensity factor in the loading cycle, K_{max}, and...
19. ABSTRACT (Continued)

and $K_{isc}$. The results are expressed in terms of critical conditions required for the RLE to occur, as well as the predictive equation for the maximum degradation that would be anticipated — or, alternatively, the threshold level of stress-intensity factor below which ripple-load cracking would not occur. Moreover, through numerical integration of CF crack growth rate data, it is shown that the time-to-failure curves associated with ripple-load degradation can be predicted for a specific combination of material/structure and loading conditions.
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INTRODUCTION

For a structural material which contains a crack or crack-like defect, the resistance to stress-corrosion cracking is normally evaluated in terms of the fracture mechanics parameter, $K_{\text{isc}}$, the threshold stress-intensity factor below which fracture will not occur. The measurement of $K_{\text{isc}}$ and its application to design of structures for the marine environment commonly presume sustained or constant load conditions. However, recent work\(^{(1-6)}\) has demonstrated that with the superposition of a very small amplitude cyclic load (or "ripple load"), fracture can occur in some cases at stress-intensity levels much less than $K_{\text{isc}}$. An extensive literature survey on such ripple-load effects was recently prepared, which cited several examples from both ferrous and nonferrous alloy systems\(^{(7)}\). Applications in the real world --- including many in the Navy --- rarely involve an absolutely constant load condition, but are far more apt to involve the superposition of relatively small amplitude load perturbations. Thus, the implications of the ripple-load effect (RLE) may be quite serious. Indeed, ripple-load cracking has been reported to occur at stress-intensity levels as much as 60 per cent below $K_{\text{isc}}$, as in the case of a 5Ni-Cr-Mo-V steel\(^{(6)}\), as illustrated in Fig. 1a. On the other hand, it does not appear from the literature that all ferrous alloys exhibit similar levels of ripple-load degradation. In fact, wide disparities have been reported --- to the point of complete absence of a RLE in some cases, as in the case of an AISI 4340 steel\(^{(6)}\), cf. Fig. 1b --- for reasons which have remained obscure. The origin of the RLE is even more confused by recent evidence that an increase in time-to-failure may be caused by ripple loading, in the case of a 3Ni-Cr-Mo-V steel\(^{(6)}\).

The purpose of this work is to develop the theoretical framework required for prediction of the RLE. First of all, definition is sought of the critical conditions required for a material to exhibit a RLE in the marine environment. Secondly, quantitative prediction is desired of the maximum extent of degradation by the RLE, relative to $K_{\text{isc}}$ --- i.e. a threshold below which ripple-load cracking will not occur. And finally, the quantitative
prediction of time-to-failure curves associated with ripple-load cracking is sought, for a given combination of material/structure and loading conditions. The desired framework necessarily involves the interface between SCC and corrosion-fatigue (CF) behavior. Ripple-load cracking has been approached as an extreme case of CF crack growth behavior. Thus, the analysis begins with consideration of the relationship between the small amplitude stress-intensity range associated with ripple loading, $\Delta K$, the high stress-ratio conditions, $R \geq 0.90$, the threshold for CF crack growth, $\Delta K_{th}$, the maximum stress-intensity factor in the loading cycle, $K_{max}$, and $K_{l_{sc}}$.

ANALYSIS OF RIPPLE-LOAD EFFECT (RLE)

A. Critical Conditions (for susceptibility)

To define the critical conditions required for a material to exhibit a RLE in marine environment, consider first of all the nature of the interface between stress-corrosion cracking and corrosion fatigue, as represented in the schematics of Fig. 2. In Fig. 2a, the SCC resistance is indicated by the "static" loading curve, wherein the level of $K$ represents the initial value of stress-intensity factor associated with a precracked specimen (structure) which is subjected to a constant load. Here, $K_{l_{sc}}$ represents a threshold level below which fracture will not occur. However, if this constant load is superposed with a "ripple" or small-amplitude cyclic load --- as in the schematic of Fig. 2b, then for a material exhibiting susceptibility to the RLE, cracking resistance appears to be degraded to levels significantly below $K_{l_{sc}}$, as in Fig. 2a. There, the $K$-level plotted for the "ripple" curve is actually $K_{max}^{RL}$, the maximum level of $K$ in the ripple-load cycle, cf. Fig. 2b. If the RLE is defined as degradation relative to the "static" $K_{l_{sc}}$ threshold, then the first condition for the RLE can be expressed as:

$$K_{max}^{RL} \leq K_{l_{sc}}$$

With the treatment of ripple-load cracking as an extreme case of very high stress ratio*, CF crack growth, then with reference to Fig. 2b, this

*In the context of a "ripple" or small amplitude cyclic load, the stress ratio is generally presumed to be $R \geq 0.90$, although such a stipulation does not affect the generality of the treatment offered herein. With regard to notation, the superscript "RL" will be used to denote ripple loading, and the subscript "th" to denote threshold.
condition can be represented in terms of stress-intensity range,

\[ \Delta K_{RL}^{R} \leq (1-R) * K_{Iscc} \]  

(1a)

where \( R \) is the stress ratio \( (K_{min}:K_{max}) \) and \( \Delta K = K_{max} - K_{min}. \) Now the resistance of a material to CF crack growth is normally reported in terms of fatigue crack growth rate \( \left( \frac{dA}{dN} \right) \) as a function of \( \Delta K, \) as shown in Fig. 2c. The lower limit of the \( \Delta K \) spectrum is defined by \( \Delta K_{th}, \) the threshold level below which cracks will not propagate (while the upper bound is controlled by the fracture toughness). Consequently, cracks cannot propagate to failure under ripple-loading for any material unless this second condition is also met:

\[ \Delta K_{RL}^{R} \leq \Delta K_{th} \]  

(2)

Or, equivalently, the threshold level of \( K \) below which ripple-load cracking will not occur, is given by:

\[ K_{RL}^{\max} \bigg|_{th} = \frac{\Delta K_{th}}{1-R} \]  

(2a)

Consequently, if conditions (1) and (2) are combined, it can be stated that a material will exhibit a susceptibility to the RLE if and only if:

\[ \Delta K_{th} \leq \Delta K_{RL} \leq K_{Iscc} \]  

(3)

Or, equivalently,

\[ \Delta K_{th} \leq \Delta K_{RL} \leq (1-R) * K_{Iscc} \]  

(3a)

B. Maximum Extent of Degradation

Relation (3) thus defines a "window" for which the RLE would be anticipated --- as sketched in Fig. 3a. If one considers the differential
between the threshold for ripple-load cracking \(K_{max|th}^{RL}\) and \(K_{isc}\), then the maximum amount of degradation attributable to the RLE is given by:

\[
\% \text{ degradation}_{RL} = \left[1 - \frac{\Delta K_{th}}{K_{isc}(1-R)}\right] \times 100
\]  

(4)

On the other hand, if conditions of relation (3) are not met, a material will not exhibit susceptibility to the RLE --- as illustrated in Fig. 3b, since**

\[
\frac{\Delta K_{th}}{1-R} > K_{isc}
\]  

(5)

C. Quantitative Prediction of Time-to-failure (\(t_f\)) Curves

Though the typical logarithmic CF crack-growth rate curve may well exhibit a more complex shape than shown in the schematic of Fig. 2c, nevertheless, it can be approximated in piecewise fashion with power-law segments,

\[
\frac{da}{dN} = C_j \left(\Delta K\right)^{m_j}
\]  

(6)

Or,

\[
dN = \frac{da}{C_j \left(\Delta K\right)^{m_j}}
\]  

(6a)

Thus, the total number of cycles to propagate a crack can be estimated

**This statement and the preceding are contingent, of course, upon definition of the RLE as degradation relative to the \(K_{isc}\) threshold. If, however, attention were to be focused on cracking behavior above \(K_{isc}\), then it is important to recognize that for levels of \(K_{max}\) in excess of \(K_{isc}\) in the "susceptible" case --- or in excess of \(K_{max|th}^{RL}\) in the "nonsusceptible" case, "ripple" or cyclic loading at \(R \geq 0.90\) will definitely affect the time-to-failure \(t_f\). For a given geometry, reductions in \(t_f\) would be anticipitated from levels associated with "static" loading, in accord with the superposition model of CF(8). These reduced levels of \(t_f\) can still be computed using the framework described in the following section.
from the piecewise integration (over \( j \) segments) as:

\[
N_p = \sum_j \int_{(a_i)_j}^{(a_f)_j} \frac{da}{C_j [(1-R)P_{\text{max}} f(a,Q)]^{m_j}}
\]  \( (7) \)

where \((a_i)_j\) and \((a_f)_j\) are initial and final crack sizes relative to the \( j \)th segment. Of course, for the initial segment of the integration, \(a_i\) is the starting flaw (crack) size in the actual specimen or structure. On the other hand, for the final segment, \(a_f\) is the flaw (crack) size at failure. Thus, \(a_f\) can be obtained from knowledge of the fracture toughness --- \(K_{IC}\) in the case of plane strain crack tip constraint. (However, if the point of general yielding is attained prior to fracture instability, then the integration should be truncated with an \(a_f\) associated with such point.) Since stress-intensity factor can be expressed in general as:

\[
K = P \times f(a,Q)
\]  \( (8) \)

where \(P\) is load and \(f(a,Q)\) is a function of crack length \(a\) and structural geometry \(Q\), then equation (7) can be rewritten as:

\[
N_p = \sum_j \int_{(a_i)_j}^{(a_f)_j} \frac{da}{C_j [(1-R)P_{\text{max}} f(a,Q)]^{m_j}}
\]  \( (7a) \)

Now time-to-failure is simply given by:

\[
t_f = \frac{N_p}{\nu}
\]  \( (9) \)

where \(\nu\) is the cyclic frequency. Thus, finally, \(t_f\) can be estimated as:

\[
t_f = \frac{1}{\nu} \sum_j \int_{(a_i)_j}^{(a_f)_j} \frac{da}{C_j [(1-R)P_{\text{max}} f(a,Q)]^{m_j}}
\]  \( (10) \)

Though in certain cases equation (8) is sufficiently simple to permit direct integration of equation (10) --- such as in the case of a center-cracked
tension panel, in general, a numerical integration of equation (10) will facilitate computation.

DISCUSSION

It is useful to elaborate somewhat on a number of points related to the predictive methodology offered in this paper. First of all, it is appropriate to ask the question: what material properties tend to promote the high levels of $K_{I_{SCC}}$ and low levels of $\Delta K_{th}$ which promote the ripple-load degradation indicated by relations (3) or (4)? In general, higher levels of $K_{I_{SCC}}$ tend to be associated with lower yield strength, higher toughness materials. On the other hand, there is evidence that the lower levels of $\Delta K_{th}$ are related to smaller grain size or microstructural mean free path dimension --- and higher yield strength. Thus, interestingly, it would appear that strength level may play competing roles relative to ripple-load degradation.

Secondly, it is useful to focus further on the parameter, $K_{RL_{max}}$, and its relation to $K_{I_{SCC}}$ --- since susceptibility or nonsusceptibility of a material to the RLE depends on whether the level of $K_{I_{SCC}}$ exceeds the term, $\Delta K_{th}/(1-R)$, or not (cf. relation (3) or (5)). Even though the numerator ($\Delta K_{th}$) is a parameter that normally decreases with an increase in $R$, it is clear that the denominator is a quite potent function of $R$ at the high levels of stress ratio concerned with ripple loading ($R \geq 0.90$). Thus if the term, $\Delta K_{th}/(1-R)$, increases significantly with increased $R$, it may have the potential to rise from levels less than $K_{I_{SCC}}$ to levels in excess. In this way, theoretically at least, a material may be capable of exhibiting both susceptibility and nonsusceptibility to the RLE, depending on the particular value of $R$. Thus, it appears that susceptibility to the RLE is not necessarily a material characteristic.

A few words are also in order regarding the time-to-failure curves. It is significant to note that the corrosion-fatigue data required for their prediction, via equation (10), are readily obtained via automated test methods. The framework offered herein thus permits the saving of much greater time and expense associated with experimental determination of such time-to-failure curves, which are geometry dependent. Furthermore, the CF crack growth rate data employed in the predictive framework have the anticipated virtue of geometry independence --- if plane strain crack-tip constraint prevails.
If, however, predictive $t_f$ curves are desired for structures (geometries) exhibiting crack-tip constraint relaxed from the plane strain level, then it would be most appropriate to develop corrosion-fatigue crack-growth rate data for the particular section size of concern. It should be pointed out, though, that geometry-independent CF crack growth rate data (for plane strain) would still offer a useful, conservative estimate of $t_f$ for cases where the constraint is relaxed.

The $t_f$ curves, as indicated by equation (10), are not only geometry dependent, but also frequency dependent. Insofar as some alloys exhibit unusual frequency dependence in their CF crack growth behavior\(^{(12)}\), frequency has the potential to be a significant variable relative to estimates of $t_f$.

CONCLUSIONS

- A predictive model for the ripple-load effect (RLE) has been developed from concepts and descriptors used in stress-corrosion cracking (SCC) and corrosion-fatigue (CF) characterization.
- Definition has been made of the critical conditions required for the appearance of a RLE.
- A mathematical expression has been developed to describe the maximum extent of RLE degradation, for a specific combination of material/structure and loading conditions.
- Susceptibility to the RLE does not appear to be a material characteristic; rather, if an appropriate value of $K_{\text{ISC}}$ is presumed --- together with a reasonable dependence of $\Delta K_{\text{th}}$ on $R$, then a material may theoretically exhibit both susceptibility and nonsusceptibility, depending on the particular level of $R$.

ACKNOWLEDGMENTS

The support of this work by the Office of Naval Research is gratefully acknowledged (ONR Work Unit No. 4315195). Special thanks are extended to Dr. A. J. Sedriks, ONR Scientific Officer (Corrosion Science), for his continual encouragement.
REFERENCES


Fig. 1. Susceptibility to ripple-load degradation versus nonsusceptibility in two ferrous alloys cycled at R=0.90 in 3.5% NaCl solution. (a) susceptibility in a 5Ni-Cr-Mo-V steel; (b) nonsusceptibility in an AISI 4340 steel.
Fig. 2. Schematics on analysis of RLE. (a) "ripple"-load degradation analyzed via $K_{\text{max}}$ parameter versus "static" $K_{\text{isc}}$ threshold; cf. text. (b) "ripple" or small amplitude cyclic load superposed on much larger sustained load; stress ratio, $R > 0.90$. (c) piecewise analysis of corrosion-fatigue crack growth rate curve via power-law approximation to $j$th segment.
A. SUSCEPTIBLE CASE

\[ K_{\text{max}} = K_{\text{Iscc}} \]

RIPPLE-LOAD EFFECT

\[ K_{\text{RL max, th}} = \frac{\Delta K_{\text{th}}}{1 - R} \]

TIME-TO-FAILURE (log t_f)

B. NONSUSCEPTIBLE CASE

\[ K_{\text{max}} = K_{\text{Iscc}} \]

TIME-TO-FAILURE (log t_f)

Fig. 3. Illustration of predictions from relation (3); cf. text. (a) susceptibility to RLE. (b) non-susceptibility to ripple-load degradation.