RELATIVISTIC CALCULATIONS AND MEASUREMENTS OF ENERGIES, AUGER RATES AND LIFETIMES

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Deep atomic hole states constitute a regime that has only recently become amenable to detailed investigation. The physics of atomic inner shells are peculiar in several respects: (i) The energies are high; for example the 1s binding energy reaches 100 keV at Z=87. Consequently, strong relativistic and quantum electrodynamic effects arise. (ii) Transitions are mostly radiationless, proceed through many channels, and are often very strong; hole-state lifetimes thus become as short as attoseconds, with widths measured in tens of electron volts. The dynamics of inner-shell transitions consequently exhibit unusual features. This research program has explored these peculiar properties of energetic inner-shell processes. Attention has been paid to relativistic and quantum-electrodynamic effects and large-scale state-of-the-art computations of hole-state energies and transition rates have been made. In the course of this work, there has been developed the first general computer code for the relativistic calculation of Auger rates.

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15 February 1985
Deep atomic hole states constitute a regime that has only recently become amenable to detailed investigation, thanks to large-scale computers and such energetic probes as synchrotron radiation and accelerated ion beams. The physics of atomic inner shells is peculiar in several respects: (i) The energies are high, e.g., the $1s$ binding energy reaches 100 keV at $Z=87$. Consequently, strong relativistic and quantum electrodynamic effects arise. (ii) Transitions are mostly radiationless, proceed through many channels, and are often very strong; hole-state lifetimes thus become as short as attoseconds, with widths measured in tens of electron volts. The dynamics of inner-shell transitions consequently exhibit unusual features.

The central purpose of our research program is to explore these peculiar properties of energetic inner-shell processes. We have, in the past, paid particular attention to relativistic and quantum-electrodynamic effects and have performed large-scale state-of-the-art computations of hole-state energies and transition rates. In the course of this work, we have developed the first general computer code for the relativistic calculation of Auger rates.

At the present time, our primary aim is to gain a better understanding of the dynamics of inner-shell processes, particularly under threshold excitation. It has been known for some years that here the traditional two-step model breaks down, i.e., one cannot treat the decay of a deep inner-shell hole state as separate from its production. The concept breaks down that there is a relaxation phase during which the electrons in the excited atom adjust themselves to the new potential and "forget" how the state was produced. Instead, threshold excitation and decay take place in a single second-order transition, which in essence can be thought of as the inelastic analog of resonance fluorescence. A few years ago, we were able to demonstrate the single-step nature of inner-shell excitation and radiationless deexcitation, dubbed the "resonant Auger Raman effect." This effect results in resonant emission of sub-natural linewidth radiation.

With the single-step nature of threshold excitation-deexcitation established, and the two-step model long proved valid in the asymptotic limit, the pressing fundamental question is: how does nature link these seemingly contradictory regimes? We have devoted several years to an investigation of this question, and to a search for a unified description that would encompass the entire range of excitation energies.

Related questions with which we have been concerned are (i) the extent and nature of many-body processes associated with atomic inner-shell excitation, (ii) a correct relativistic description of inner-shell ionization by slow charged particles, and of subsequent x-ray emission, and (iii) a search for an explana-
tion why theory almost invariably predicts much too short a lifetime for certain atomic hole states, such as [2s].

We have pursued an integrated theoretical and experimental approach. The theoretical aspect has a strong numerical component. Major computations are being performed at the NASA Ames Research Center, which has a CRAY 1 computer. A professional programmer works half-time for us at NASA ARC. The experimental work is primarily conducted in the Stanford Synchrotron Radiation Laboratory (SSRL), where we operate an on-line gas-phase electron spectrometry system. Data are transferred by magnetic tape to Oregon for analysis on campus.

The major result of the year is the successful outcome of our investigation of the dynamics of inner-shell photoionization and radiationless deexcitation (see Sec. 2.1). Detailed measurements of the Auger resonant Raman effect in the L_2 subshell of xenon and of post-collision interaction (PCI) shifts of the L_2-M_4-M_5 (2G_4) Auger line were completed and successfully explained in the framework of resonant scattering theory. For this purpose, the first fully quantum-mechanical theory of post-collision interaction was constructed. The result is a consistent, unified description of excitation/deexcitation of deep hole states, that incorporates the resonant Raman effect at threshold and asymptotically turns into the two-step model, with PCI providing the link between the two extremes. This result culminates five years of intensive work. Crucial contributors were Teijo Åberg of the Helsinki University of Technology, who spent the fall quarter in our group as a visiting professor and developed the resonant scattering formulation, and Mau Hsiung Chen of the Lawrence Livermore Laboratory, who solved the extremely difficult two-electron continuum wave-function problem.

A related important result of this year's work concerns a many-body effect in inner-shell ionization. A synchrotron-radiation study of double photoionization, through measurements of Auger satellites, permitted us to demonstrate for the first time the theoretically predicted difference between the dependence of shakeup and shakeoff probabilities on the photon energy near threshold (cf. Sec. 2.2).

We have utilized the large computing power of the NASA ARC facility in order to construct tables of K- and L-shell crosssections for ionization under impact by slow protons, on the basis of a fully relativistic theory that we developed previously (Sec. 2.3).

Progress was achieved in a protracted theoretical study designed to understand why calculated lifetimes of certain inner-shell hole states (e.g., in the 2s subshell) tend to be very much shorter (by a factor of 2 or 3) than measured. This problem is perplexing because calculations of other lifetimes (or widths) tend to come out well; it is important because the results of such calculations enter into the design of schemes for short-wavelength lasers. Added to previous studies of the effects of
relaxation and intermediate coupling.\textsuperscript{5,6} we have now calculated the effects of final-state channel mixing. The interchannel interaction is found to have a major influence on transition rates (Sec. 2.4).

A calculation of x-ray emission rates for transitions to atomic M-shell vacancies has been completed, with particular emphasis on the results of the choice of gauge.\textsuperscript{7} This is the first systematic relativistic calculation of such rates employing a nonlocal potential (Sec. 2.5).

Our results on dynamical and many-body aspects of inner-shell transitions urgently call for extension of these studies. We plan to carry out further calculations of post-collision interaction to encompass other experimental data obtained recently, and to perform new high-resolution measurements in the threshold region where additional data can provide critical tests of the resonant scattering theory. For this purpose, we hope to gain access to the new 54-pole wiggler line at SSRL, which provides substantially enhanced x-ray flux. Theoretical results on inner-shell transition rates and ionization cross sections also invite significant extensions, building on the recently attained insights.


2. Research Results

2.1 Dynamics of atomic inner-shell processes

In threshold excitation of short-lived, deep atomic inner-shell hole states, ionization and decay cannot be treated as distinct processes. Directly at threshold, photoionization and radiationless deexcitation occur in a single process, the resonant Raman effect.\textsuperscript{1} Above threshold, excitation and deexcitation are still linked by post-collision interaction (PCI), in which the Auger decay takes place under the influence of the Coulomb field of the receding photoelectron and some of the photoelectron's energy is transferred to the Auger electron. Measurements of the Auger spectrum excited near threshold can therefore probe
the dynamics of inner-shell transitions and provide a stringent
test of the semiclassical PCI theory which has been shown to be
valid in the limit of long hole-state lifetimes. The first fully
quantum-mechanical calculation of PCI becomes possible, based on
resonant scattering theory, since the intermediate-state sum-
mations can be restricted to states associated with the initial
inner-shell hole.

We have performed an investigation in which highly monochro-
matized, hard synchrotron radiation was tuned through the L\textsubscript{3}
threshold of Xe and the L\textsubscript{2}-M\textsubscript{4}M\textsubscript{5} (1\textsuperscript{G}\textsubscript{4}) Auger decay including the
nd (n\geq5) spectator-electron satellite distribution was observed.
The peak positions and widths of the n=5 and n=6 spectator lines
were measured as functions of photon energy. The evolution of the
M\textsubscript{4}M\textsubscript{5} double photoionization peak into the Auger diagram line was
found to be strongly blended with the n\geq6 spectator satellites in
the excitation-energy range from E\textsubscript{exc}=-0.5 eV to +5 eV with
reference to the ionization threshold, producing a large apparent
PCI shift (-3 eV). We compare this result with predictions from
the resonant scattering theory at E\textsubscript{exc}=+3 eV. Above E\textsubscript{exc}=+5 eV,
the PCI shift is solely due to distortion of the diagram-line
shape, so that comparison with both the resonant scattering and
semiclassical theories becomes possible.

In the experiment, performed in the Stanford Synchrotron
Radiation Laboratory, x rays from an 8-pole wiggler operating at
14 kG were focussed onto a Xe jet by a Pt-coated doubly-curved
toroidal mirror. A narrow energy band (-0.6 eV) was selected with
a tunable Si (111) (1,-1) double-crystal monochromator. The energy
spectrum of electrons emitted from the Xe target was measured
with a double-pass cylindrical-mirror analyzer. We take the
asymptotic Auger diagram-line energy E\textsubscript{A}\textsuperscript{0}=3.365.9\pm0.2 eV as refe-
rence for the PCI shift. Typical Auger spectra excited at E\textsubscript{exc}=+2
eV and +1.5 eV are shown in Fig. 1.

In the resonant scattering theory of the PCI effect, a
consistent treatment of threshold phenomena is achieved by inter-
preting the Auger transition \([n_1l_1]\to[n_ell, n_ell, l_ell]\) as a resonance
in the double electron photoionization of the \(n_ell\) and \(n_ell\) subshells. As the incident-photon energy approaches the ioniza-
tion energy \(I_1\) of the \(n_1l_1\) threshold, spectator transitions of the type \([n_1l_1]nl\to[n_ell, n_ell, l_ell]nl\) start to appear owing to \(n_1l_1\)
\(nl\) excitations. At the threshold, the spectator lines blend into
the rapidly increasing double-ionization peak, for which the cross
section at large excitation energies E\textsubscript{exc}=\omega-I\textsubscript{1} becomes
the product of the \(n_1l_1\to\ell l\) single-electron photoionization cross
section and the Auger decay probability \(P(\ell l)\) for the \([n_1l_1]\)
\([n_ell, n_ell, l_ell]\) \(2S+1L\) transitions with energy \(E\textsubscript{A}\). Close to thresh-
hold, the Auger decay cannot be treated as an independent process
because the emission of the Auger electron is affected by transi-
FIG. 1. Xenon $L_3-M_4M_5$ ($^{1}G_4$) Auger-electron spectrum, excited with synchrotron-radiation photons of energy 2.0 eV below the Xe $L_3$ binding energy (top) and 1.5 eV above the Xe $L_3$ binding energy (bottom). Feature A consists primarily of nd ($n \geq 6$) satellites, with a slight admixture of the PCI-shifted diagram line; feature B is the 5d spectator satellite, and feature C consists of the PCI-shifted diagram line, with an admixture of nd ($n \geq 6$) satellites.

tions from the single- to double-hole n($\xi$)l states. The double photoionization cross section is

$$
\frac{d^2\sigma}{d\varepsilon d\varepsilon_A} = \frac{4\pi^2 \omega_0}{3} \Gamma(\xi_A^0) \int_0^{\infty} \int_0^{\infty} N(\omega - \omega_0) \frac{d\omega}{2(\omega - \varepsilon - \xi_A - I_{eff})} d\omega',
$$

where $N(\omega - \omega_0)$ is the distribution function of the incident photons (normalized to unity), $\xi_A$ is the Auger-electron energy, and $I_{eff}$ is the ionization energy of the final double-hole state. We have placed the slowly varying factor $\omega_0 \Gamma(\xi_A^0)$ outside the integral. If the continuum wave function $|\xi\rangle$ is replaced by the discrete-state wave function $|n\rangle$ in the overlap matrix element $<\xi | n\rangle$, the double-ionization cross section reduces to the cross section $d\sigma/d\varepsilon_A$ for emitting an Auger electron and placing a spectator electron in the excited state nl. In Eq. (1), we have

$$
|n\rangle = \sum_{n' \in \{n\}} \sum_{m' \in \{n\}} \left( \frac{m'!}{m!} \right) \frac{1}{E_{n'\epsilon} + \Gamma_n + i \Gamma_n / 2} \left( \frac{m'}{m} \right) + \int_0^{\infty} \frac{d\varepsilon}{E_{n'\epsilon} + \varepsilon + i \Gamma_n / 2},
$$

where each $|T(n')\rangle$ must be evaluated in the field of the singly ionized atom with an $n_1l_1$ hole, in contrast to the final $|\xi(n)\rangle$ double-hole states. In Eq. (2), $\Gamma_n$ is the total decay width of the $[n_1l_1]$ hole state, and $<\xi(n')|n\rangle$ is the reduced radial dipole matrix element.

Close to threshold, the Auger-electron emission intensity as a function of $\xi_A$ is a measure of the cross section
\[ \frac{d\sigma}{dE_A} = \sum_{n=1}^{\infty} \frac{d\rho_n}{dE_A} + \int_{\rho}^{\infty} \frac{d^2\sigma}{dE_A dE_c} \, dE_c, \] (3)

which must be convoluted with the spectrometer window function for comparison with the experimental data. If the final double-hole-state lifetime \( \Gamma_f^{-1} \) is taken into account, the Dirac delta function in Eq. (1) is replaced by the normalized density function \( \frac{\Gamma_f}{2\pi} (\omega - \epsilon_f - \epsilon_A - i \Gamma_f/2)^{-1} \). It follows from Eqs. (1) and (2) that for \( E_{\text{exc}} > 0 \) the discrete part of the cross section (3) rapidly vanishes compared with the continuum part \( \frac{d\sigma_c}{d\epsilon_A} \).

In the \( \Gamma_f > 0 \) limit, the corresponding overlap integral \( \langle \xi | \Xi \rangle \) can be approximated by taking the overlap between two WKB wave functions, corresponding to \( \xi_k^2 = E_{\text{exc}} - i \Gamma_f/2 + V_f(R) \) and \( \xi_{k_f}^2 = E_{\text{exc}} - i \Gamma_f/2 + V_f(R) \), respectively. We have \( V_f = 2V_i = R^{-\frac{1}{2}} \), where the angular-momentum exchange between the photoelectron and the Auger electron is neglected. All semiclassical models of PCI seem to be variants of the WKB approximation, limited to the very-high-\( n \) and continuous-\( \epsilon \) region. Qualitatively, both Eqs. (1)-(3) and the semiclassical approach lead to a transfer of intensity from the low-energy to the high-energy flank of the Auger-electron peak, compared with a Lorentzian shape, resulting in a positive PCI shift. However, whereas in the semiclassical approach the \( \epsilon_A \rightarrow -\epsilon_A^0 \) regime is approached by analytic continuation, the quantum-mechanical theory leads to a spectator-line structure, important in practice for \( E_{\text{exc}} < 2\Gamma_f \).

The derivation of Eq. (1) from the general transition matrix formula is based on a number of approximations. The most severe of these is probably the factorization of the many-electron Hamiltonian matrix element that involves the final two-electron scattering wave function into the one-electron overlap element \( \langle \xi | \Xi \rangle \) and the Auger-electron probability amplitude.

The cross section (3) was calculated for the \( L_3-M_4M_5 \) \( (1^G_4) \) transition with the use of Hartree-Fock (HF) wave functions. Calculation of the continuous part of the function (2) required, for each \( E_{\text{exc}} \) (3, 10, and 20 eV), 2,000 continuum wave functions \( |\xi_d\rangle \) in steps of 0.1 eV. These wave functions, as well as the final-state continuum wave functions \( |\xi_f\rangle \), were generated in the configuration-average frozen HF core, with the exchange interaction taken into account. The summation over the discrete intermediate states was found to be negligible in all three cases.

The -2.3-eV width of the spectrometer window allows us to resolve only the 5d spectator line in the range \(-8eV < E_{\text{exc}} < +5eV\), at \( \Delta(5d) = E_{\text{exc}} + 10.5 \) eV, from the rest of the structure which appears as a single peak at \( \Delta\Delta(5d) \). Up to \( E_{\text{exc}} = 0 \) eV, \( \Delta \) appears to follow a linear dispersion law, \( \Delta = E_{\text{exc}} + 4.0 \) eV, which indicates that it is mostly 6d. The linear dependence of \( \Delta(5d) \) and \( \Delta(6d) \) on \( E_{\text{exc}} \) is plotted in Fig. 2: the resonance energies are indicated at which the spectator lines gain maximum intensity. According to Eqs. (1)-(3), these resonances occur at \( E_{\text{exc}} = \)
The measured energies $\zeta_n$ agree well with relaxed HF calculations for $n=5$ and 6.

FIG. 2. Xenon $L_3-M_4M_5\ (^1G_4)$ Auger-electron-peak energies, as functions of excitation energy. Experimental data are indicated by solid circles. Diamonds represent the quantum-mechanical shift $\Delta$ of the diagram line, while the solid curve indicates the semiclassical shift.

The measured width of the 5d and 6d spectator lines is 4.0±0.5 eV, independently of $E_{\text{exc}}$. This is clearly narrower than the natural width of the $L_3-M_4M_5\ (^1G_4)$ line ($\Gamma_1^{\text{t}}+\Gamma_2^{\text{t}}\approx 4.2$ eV), convoluted with the 2.3-eV wide spectrometer window, i.e., 5.3 eV. This resonance narrowing is in accordance with Eqs. (1)-(3) which, in analogy with the x-ray resonant Raman case, predict $d\sigma_n/d\varepsilon_n \propto N(\omega-\omega_0)$, where $N(\omega-\omega_0)$ is 0.6 eV wide in our experiment.

With the sum rule $\int |<\xi'\zeta'\rangle|^2 d\varepsilon = <\zeta'\zeta>$, where summation over discrete states is included, it is possible to estimate how much of the low-energy structure represented by peak C in Fig. 1 is due to spectator states. The result, in agreement with the gradual, slow disappearance of the 5d spectator line, is that for $E_{\text{exc}}=2^{\text{t}}\Gamma_1$, the contribution from the discrete final states cannot be neglected. Hence $E_{\text{exc}}=3$ eV represents an intermediate case, in which there is an apparent shift due to the spectators. Experimentally we find $\Delta=3.0\pm 0.5$ eV, whereas theory predicts $\Delta=2.8$ eV after convoluting with the final-state density and the spectrometer window function.
In the calculation of $d\sigma_n/d\omega$, the discrete portion of complete-set HF computations was approximated by quantum defect theory for both $n'$ (intermediate) and $n$ (final) states $\geq 8$. The summation over intermediate continuum states was found to be important, indicating that there is appreciable recapture of the photoelectron into Rydberg states.

For $E_{\text{exc}} = 5$ eV, the quantum-mechanical shape of the Auger diagram line agrees closely with that obtained from the semiclassical Niehaus theory through numerical integration. After convoluting the theoretical shapes, we find the shifts $\Delta_{\text{theory}} = 2.0$ eV, $\Delta_{\text{expt}} = 2.5 \pm 0.5$ eV for $E_{\text{exc}} = 10$ eV, and $\Delta_{\text{theory}} = 1.6$ eV, $\Delta_{\text{expt}} = 1.9 \pm 0.7$ eV for $E_{\text{exc}} = 20$ eV. It remains to be shown analytically why the Niehaus theory, if the stationary-phase approximation is not invoked, leads to almost identically the same results as the quantum-mechanical approach. In Fig. 2, the solid curve for the diagram-line energy represents the function $\Delta = \Delta(E_{\text{exc}})$, obtained from the Niehaus theory and convoluted.

Similar measurements as here described have been performed on other wide inner-shell hole states. Computations are in progress to apply the resonant scattering theory to these cases as well. A preliminary report on this work has been submitted for publication (cf. Sec. 3, Item 12 of this Report).

6. We follow the convention of denoting hole states by square brackets, and use atomic units throughout.
7. The width $\Gamma_z = 2.82$ eV was taken from M. H. Chen, B. Crasemann, and H. Mark, Phys. Rev. A 24, 177 (1981); $\Gamma_z$ = 1.4 eV was estimated from the Xe 3d photoelectron linewidth as given by U. Gélius, J. Elec. Spect. Rel. Phenom. 5, 985 (1974).
8. This approximation has recently been discussed by A. Russek and W. Mehlhorn (submitted for publication in J. Phys. B).
2.2 Threshold double photoionization of argon with synchrotron radiation.

In atomic inner-shell photoionization, multiple excitation processes occur with significant probability. The resulting final states are approximately described by configurations formed by removal of a core electron and excitation of additional electrons to higher bound states (shakeup) or to the continuum (shakeoff).\textsuperscript{1-3} Such multiple excitation processes result in satellites in the photoelectron spectra\textsuperscript{1,4-6} and in the Auger and x-ray spectra from transitions through which the photoexcited states decay.\textsuperscript{2,7,8} The study of these multiple excitation processes is important because they epitomize the breakdown of the independent-particle model and can provide important clues for the understanding of electron correlation and of excitation dynamics.\textsuperscript{3,5,9,10} The energy dependence of the cross sections for double excitation is particularly informative near threshold; the observation of Auger satellites makes it possible to measure this dependence. We have performed an investigation in which highly monochromatized, hard synchrotron radiation was tuned through the thresholds for various multiple excitation processes during ionization of Ar, and the probabilities of accompanying 3s and 3p excitation were traced by measuring the intensities of pertinent Auger satellites. Results were compared with theory.\textsuperscript{3,10}

In the experiment, x rays from an 8-pole wiggler, operating at 14 kG, were focused onto an Ar jet by a Pt-coated doubly curved toroidal mirror. The x-ray bandwidth from a Ge (111) double-crystal Bragg monochromator was 0.9 eV at \( h\nu = 3200 \text{ eV} \); the flux on target was \( 10^{12} \) photons/s with 60 mA of 3-GeV electrons in the SPEAR storage ring. Electron spectra were measured with a computerized double cylindrical-mirror analyzer; with a pass energy of 82.5 eV, the electron-spectrometer resolution was 1.6 eV.

We take the 2,660-eV Ar \( K_{\eta}L_{\gamma}L_{\zeta}^{3/2}D_{2} \) Auger-electron line as reference. The K-LL Auger yield\textsuperscript{1-2} of Ar is affected only minutely by excitation of one or two M-shell electrons. The intensity of satellites of the \( 1D \) Auger line relative to that of the "diagram" line is therefore a measure of the probability of the multiple photoexcitation processes studied in this work.

To interpret the \( 1D \) Auger satellite spectrum it was necessary to calculate the radiationless transition energies and rates in the presence of one or two open M subshells. The initial states can be limited to those which in the sudden approximation are expected to be significantly populated.\textsuperscript{1} These are the \([1s3l](l=0,1)\) shakeoff states and the \([1s3l]n1(n=4 \text{ and } 5 \text{ for } l=1, n=4 \text{ for } l=0)\) shakeup states, where square brackets indicate hole states. In the limited \(3s(2S)ns^{1,3}S_{1/2}S^{2}S\) and \(3p(2P)np^{1,3}S_{1/2}S^{2}S\) basis, the eigenstates are linear superpositions of \(1S\) and \(3S\) states. The initial shakeup states can be identified as states with dominant \(1S\) component because the monopole selection rules
prevent transitions to the triplet state. According to our Hartree-Fock (HF) calculations, the initial [1s3p]4p state has almost pure 1S character, whereas in the other shakeup cases the mixture is more uniform.

### FIG. 3. Calculated energies of Auger satellites caused by 3s- and 3p-electron excitation accompanying 1s ionization, with reference to an Ar K-L_2,L_3 Auger spectrum photoexcited 2,000 eV above the 1s ionization threshold. Estimates of relative satellite intensities within each multiplet are indicated by the heights of the bars.

Calculated Auger satellite energies are indicated schematically in Fig. 3. The satellites arising from 3s and 3p shakeoff accompanying 1s ionization are seen to fall into the peak around -2,643 eV, while most 3s and 3p shakeup processes cause Auger satellites that fall within the 2,650-eV peak, unresolved from the K-L_2,L_3 1S_0 diagram line. The measured intensity of the 1S line, excited below the threshold for any [1sn1] double processes, is 11.0±0.6% of the 1D-line intensity, in excellent agreement with the prediction (11.12%) from a relativistic intermediate-coupling calculation that includes configuration interaction. The predicted positions of the Auger lines are only slightly affected by configuration mixing in the initial states and by relativity.

In Fig. 4(a), the relative intensity of the 2,650-eV shakeup satellite peak including the 1S_0 diagram line is plotted. The satellite peak that arises at photon energy E=3.225 eV is tentatively ascribed to the [1s3p]4p^2 bound-bound resonance, in accordance with the interpretation of the Ar K absorption spectrum which shows a peak at 3,224 eV. In accord with observations of Kobrin et al., the [1s3p]4p shakeup satellite appears to have approximately half its asymptotic intensity at 5 eV above threshold. Saturation of [1s3p]4p plus opening of the [1s3s]4s channel lead to a small gradual increase which levels off to a constant shakeup satellite intensity -60 eV above the [1s3p]4p threshold.

If we assume in accordance with Fig. 4(a) that the shakeup ratio is practically constant as a function of E, then it can be concluded that the experimental shakeoff curve levels off at high E at 19±2% (after subtracting the threshold value of 5%). The shape of the curve is well predicted by our calculations using HF
wave functions for both the $[1s3p]$ core and continuum states [Fig. 4(b)]. In the calculation of the continuum wave functions the Lagrangian multipliers were neglected, but a Schmidt orthog-

![Image](https://example.com/image.png)

FIG. 4. (a) Intensity of the 2,650-eV feature in the photoexcited Ar K-L$_2$,3L$_2$,3 Auger spectrum, with reference to the $^1D$-line intensity, as a function of x-ray energy. The dashed line at 11.1% indicates the $^1S$ diagram-line contribution. Energy thresholds for 1s ionization and for 3p→4p and 3s→4s shakeup accompanying 1s ionization are indicated by vertical arrows. The normalized theoretical prediction for the near-threshold energy dependence of these relative shakeup probabilities is represented by the solid curve. (b) Photoexcitation-energy dependence of the 2,643-eV Auger satellite-group intensity. Thresholds for 1s ionization alone and accompanied by 3p and 3s ionization are indicated by vertical arrows. The normalized theoretical relative shakeoff probability is indicated by the solid curve. Circles and triangles pertain to data from separate experiments.

[Image]

normalization was carried out afterwards. As seen in Fig. 4(b), the measured cross-section curve is only slightly affected by the opening of the $[1s3s]$ shakeoff channel. Our calculations predict an asymptotic shakeoff probability of 25% at high E.

We can draw the following conclusions. (1) The difference in the photon-energy dependence of shakeup vs. shakeoff close to threshold has been shown experimentally, for the first time, to be as predicted by theory. (2) The measurements indicate more shakeoff than shakeup at high photon energy, in contrast to the predictions of Ref. 10 but in accord with Ref. 1. (3) The measured shakeup probabilities agree well with the predictions of Ref. 10, but the shakeoff probabilities do not. (4) The measured total shake probabilities are bracketed by the sudden-approximation values calculated by the HF (DF) method for a double-hole $[1s31]$ and a single-hole $[1s]$ field. Within the restricted HF (DF) method, both procedures are somewhat inconsistent with respect to fulfilling the closure relation. This inconsistency could
be removed if many-electron wave functions were used to obtain the

\[ \langle \Phi_1|1s3l|n(l)1\rangle^2S|\Phi_{\text{frozen}}(1s)\rangle^2S \]

shakeup and shakeoff amplitudes, since the \( \Phi \) functions are eigenfunctions of the same projected (N-1)-electron Hamiltonian PH(N-1)P, where P=|1s><1s|.

This work was submitted for publication during the period covered by the present Report (cf. Sec. 3, Item 7) and has since been published [Phys. Rev. Lett. 54, 182 (1985)].

11. and 442 (1980).

2.3 Ionization by charged particles

Atomic inner-shell ionization by charged-particle impact has been studied intensively during recent years. The theory has progressed beyond the plane-wave Born approximation, through incorporation of binding and Coulomb-deflection effects.1,2 For low-energy collisions, it has been found quite important to include relativity and to employ more realistic wave functions than hydrogenic ones.3-10

Previously tabulated cross sections for atomic inner-shell ionization by charged-particle impact were based on plane-wave Born-approximation (PWBA) calculations with hydrogenic wave functions.11-12 No systematic calculations of inner-shell ionization cross sections have hitherto been published that take into ac-
count the effects of realistic wave functions and that consistently incorporate relativity.

We have drawn upon our previous work on the subject\textsuperscript{4,7,8} and invested a substantial amount of computing time on the NASA Ames Research Center CRAY 1 to prepare tables of relativistic ionization cross sections for K and L shells of 27 elements with atomic numbers 22≤Z≤92, for proton impact with incident energies from 0.15 to 3 MeV. These cross sections were calculated with Dirac-Hartree-Slater wave functions and include binding, polarization, and Coulomb-deflection corrections.

The work has been accepted for publication in Atomic Data and Nuclear Data Tables (cf. Sec. 3, Item 10).


2.4 Lifetimes of deep hole states

Atomic inner-shell vacancy states decay predominantly by radiationless processes and, to a minor extent, by radiative transitions. The coupling between radiative and radiationless channels has usually been neglected\textsuperscript{1} The electrostatic coupling between the final K-LL Auger channels in Ne was considered by Howat et al.\textsuperscript{2,3} and for K-LL, K-LM, and K-MM transitions in Mg by Howat.\textsuperscript{4} These authors found that interchannel coupling substantially alters the spectral distribution of the K Auger electrons which are emitted with kinetic energies of several hundred electron volts. It is tempting, therefore, to investigate similar effects in the case of Coster-Kronig processes which are extremely intense, compared with Auger processes, and in which the outgoing electrons' kinetic energy is at least an order of magnitude less than in Auger transitions.
One inviting case for theoretical investigation is that of L-shell Coster-Kronig transitions in Ar, for which perplexing discrepancies have existed between experimental results and theoretical predictions. Hartree, Hartree-Fock-Slater, and Hartree-Fock single-configuration calculations have been found to overestimate experimental Ar L_1-L_23M_1 Coster-Kronig rates by factors of ~4, the L_1-L_23M_1 to L_1-L_23M_2 intensity ratio by a factor of ~2, and the ratio of L_1-L_23M_1 (^3P_1) to L_1-L_23M_1 (^3P_1) transition rates by a factor of ~120!

Possible reasons for these striking discrepancies in theoretical predictions include (i) many-body interactions in the initial and final atomic systems, (ii) effects of relaxation in the final ionic state, and (iii) effects of the exchange interaction between the continuum electron and the final bound-state electrons. These possibilities have been investigated in recent calculations.

Mehlhorn has recently reevaluated his experimental data, leading to a 13% decrease in the L_1-L_23M_1/M_23 intensity ratio. This revised experimental ratio agrees better with theoretical predictions, but the discrepancies remain large in comparison with other atomic transition-rate calculations in which theory tends to come within 10-20% of measured rates.

In an effort to resolve this perplexing situation, we have investigated the effects of continuum interaction in the outgoing channels on the total and relative term intensities of Ar L-shell Coster-Kronig transitions. The rates were calculated through a formulation which includes the effects of final-state channel mixing. The interchannel interaction was found to change individual transition rates by as much as 84%. The relative term intensities from this calculation agree better with experiment than computations which do not take account of channel mixing. The discrepancies previously found between calculated and measured total Coster-Kronig rates and between ^1P/^3P ratios are largely removed when channel coupling is taken into consideration.

A description of this research has been accepted for publication in Physical Review A (cf. Sec. 3, Item 11); earlier work on this subject has been published in the course of the report year (Sec. 3, Items 2, 4, 6).

1. Interference between radiative and radiationless channels has been considered by L. Armstrong, Jr., C. E. Theodosiou, and M. J. Wall, Phys. Rev. A 18, 2538 (1978); V. L. Jacobs (private communication).

2.5 X-ray emission from the M shell

Most of the existing calculations of x-ray emission rates deal with transitions to K- and L-shell vacancies. Only one calculation has been performed for M x-ray emission rates, based on relativistic Hartree-Slater wave functions and covering 6 elements with atomic numbers between 48 and 93. We have now performed Dirac-Fock calculations of M x-ray emission rates, both in the Coulomb and length gauges, for 10 elements with atomic numbers between 48 and 92. We have studied the gauge dependence of the M x-ray rates, which is due to the effect of the nonlocal potential. We have explored the effects of relativity on these rates, which are caused by changes in transition energies, shifts in the wave functions, and the role played by higher multipoles. Typical results are illustrated in Fig. 5. This research has been published (Section 3, Item 3.)

FIG. 5. Total probabilities (in atomic units) of radiative transitions to an M_3 vacancy, as functions of atomic number Z. Results from relativistic Dirac-Fock calculations in the length gauge (DF-L) and in the Coulomb gauge (DF-C) are compared with rates from relativistic local-potential Dirac-Hartree-Slater (DHS) and nonrelativistic Hartree-Slater (HS) calculations.
3. Publications

Published Papers


In Press and Submitted


10. Mau Hsiung Chen and Bernd Crasemann: "Relativistic Cross Sections for Atomic K- and L-Shell Ionization by Protons, Calculated from a Dirac-Hartree-Slater Model." At. Data Nucl. Data Tables, in press.


In Preparation


Abstracts


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