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by

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ON THE CALCULATION OF ACOUSTIC INTENSITY FLUCTUATIONS CAUSED BY OCEAN  
CURRENTS

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ABSTRACT

Ocean currents can cause significant and interesting effects on the intensity of underwater sound transmissions. We study this phenomenon via the parabolic approximation, beginning with conservation laws, and derive a family of equations, each of which is valid for different magnitudes of current speed, current gradient, and sound-speed variation. Numerical results indicate that some current structures can cause large variations in received intensity, and that substantial differences can occur in reciprocal transmissions. Current effects on intensity may be quite sensitive to the sound-speed distribution.

INTRODUCTION

Ocean currents cause interesting and significant effects on underwater sound. For example, in a time-independent ocean environment, currents cause reciprocity relations to fail. Based on ray theory, work has been done by the authors and others to model the influences of currents on acoustic transmissions. It has been shown, for instance, that certain current structures can cause large fluctuations in total-field intensity and per ray phase. These results are limited to high-frequency sound transmissions. To estimate current-induced effects for lower frequencies, a full-wave model should be used. One computational model is the parabolic approximation, which has been implemented using several algorithms, and is a particularly attractive method for efficiently generating transmission-loss calculations.

MODEL FORMULATION

In a complicated medium such as a moving ocean, it is not obvious how known parabolic equations should be modified to include current effects. For this reason, we systematically reformulated the governing time-dependent wave equation, starting from the conservation laws and state relations governing the ocean medium, and including medium motion (Robertson et al., 1985). If the current is assumed steady but non-uniform, additional terms occur in the wave equation. These terms depend on the current gradient and, as will be discussed below, can be significant in subsequent approximations.

We then assume that the sound source is time-harmonic and that the propagating wave is outgoing, thereby obtaining a reduced wave equation. After transforming coordinate systems, we invoke the far-field approximation, and proceed to generate a family of parabolic equations. Each of these equations depends on the relative sizes of three dimensionless parameters: a Mach number, the sound-speed deviation, and a shear number. The last parameter indicates the magnitude of current gradient, and also depends on source frequency. For example, a parabolic approximation appropriate for an isospeed sound channel, through which flows a steady depth-dependent current, is

$$2i\kappa_0\psi_r + \psi_{zz} - 2\kappa_0^2 \left(\frac{u}{c_0}\right)\psi + \left(\frac{2}{c_0}\right)\left(\frac{du}{dz}\right)\psi_z = 0, \quad (1)$$

where  $\kappa_0$  is a wave number,  $u$  is current speed, and  $\psi$  is an envelope of acoustic pressure in the far field. The reference sound speed  $c_0$  in this isospeed case is equal to the sound speed  $c$ . Depth is indicated by  $z$  and range by  $r$ . It can be shown that range-dependent sound-speed profiles can be incorporated into these approximations in a straightforward way, provided that the horizontal gradient of sound speed is not large, which is often the case in many important ocean regions. For example, for a sound channel in which the sound-speed deviation is of the same order of magnitude as the Mach number, the appropriate equation is

$$2i\kappa_0\psi_r + \psi_{zz} + \kappa_0^2 (n^2-1)\psi - 2\kappa_0^2 \left(\frac{u}{c_0}\right)\psi + \left(\frac{2}{c_0}\right)\left(\frac{du}{dz}\right)\psi_z = 0, \quad (2)$$

where  $n(r,z) = c_0/c$  is the index of refraction.

In Eqs. (1) and (2), the term which depends on the first derivative of current may or may not be retained, depending upon the size of the shear-number parameter. In the event that it is kept, the parabolic approximations are not in a "standard form"; that is, they cannot be solved directly with existing numerical implementations. However, it is possible to transform this family into related parabolic equations which are in a standard form. The transformed version of Eq. (2) is, for example:

$$2i\kappa_0\phi_r + \phi_{zz} + \kappa_0^2 (n^2-1)\phi - 2\kappa_0^2 \left(\frac{u}{c_0}\right)\phi - \frac{1}{c_0}\left(\frac{d^2u}{dz^2}\right)\phi - \frac{1}{c_0^2}\left(\frac{du}{dz}\right)^2\phi = 0, \quad (3)$$

where

$$\psi(z,r) = e^{-Mu(z)}\phi(z,r). \quad (4)$$

Note the appearance of two new terms in Eq. (3) which depend on the square of the derivative of current and the second derivative of current. The structure of Eq. (3) and other such equations suggests the use of an effective sound-speed profile (ESSP), which includes all sound-speed and current-related effects, and is used as the "actual" sound speed for numerical solution of the equations. For example, the ESSP corresponding to Eq. (3) is

$$\tilde{c} = c + u + \frac{1}{2\kappa_0^2 c_0} \left(\frac{du}{dz}\right)^2 + \frac{1}{2\kappa_0^2} \left(\frac{d^2u}{dz^2}\right). \quad (5)$$

## NUMERICAL RESULTS

To solve any of our parabolic equations numerically, we elect to use the IFD model developed by Lee and Botseas (1982). In the discussion below, we consider several sound-speed profiles, together with current profiles, as

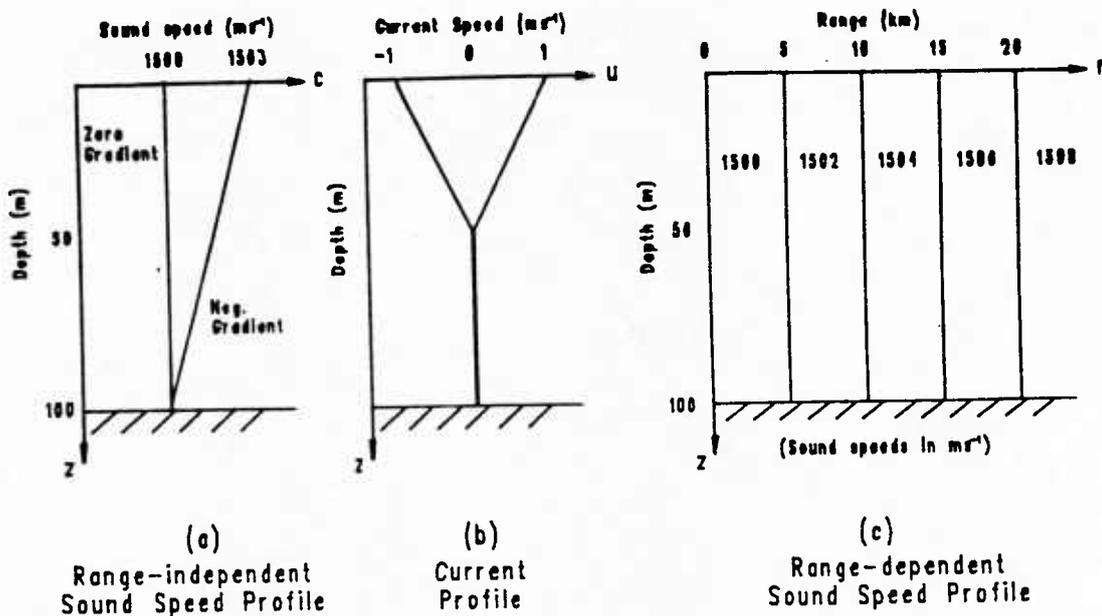


Fig. 1. Profiles of (a) range-independent sound speed, (b) current, and (c) range-dependent sound speed.

shown in Fig. 1. The zero-gradient and negative-gradient sound-speed profiles are sometimes range-independent as in Fig. 1(a), as are the current profiles in Fig. 1(b). The surface current may be either plus or minus 1 m/s. At other times, we employ a simple range-dependent sound-speed profile, Fig. 1(c), for which the horizontal gradient is both constant and small. Here, isopleths are vertical lines. We consider first the result of one calculation done in the isospeed channel, with surface current of magnitude 1 m/s. The source frequency is 200 Hz, for which it can be shown that current-gradient effects are negligible. The source and receiver depths are 25 m. In Figs. 2-6, the bottom acoustical properties are the same as in Robertson et al. (1985). Figure 2 shows a relative intensity in decibels versus range for three cases: no current present, a positive current in the source-receiver direction, and a negative current in the opposite direction. Several important current-related effects can be seen in the figure. When compared to the solid curve, representing intensity in the absence of any current, we see that a current with either direction can induce substantial variations in intensity. For example, with a positive current present, variations can exceed 10 dB over certain range intervals, such as those between 13 and 14 km. Similar behavior is seen for negative current. Current effects in both cases tend to increase with increasing range.

Intensity variations are highlighted in Fig. 3, which illustrates difference in relative intensity versus range for three cases: no current and positive current, no current and negative current, and positive and negative currents. Because source and receiver are at the same depth, this figure also illustrates one type of effect which may be seen in reciprocal transmissions (RTs). The intensity difference between positive and negative currents, indicated in Fig. 3 by the long-dashed curve, suggests that measurements of intensity variation between reciprocal source-receiver pairs may be very large. Near ranges 14 and 19 km, this difference attains a magnitude of nearly 20 dB. At other range intervals the difference is smaller, but significant. For example, between 10 and 12 km, the intensity difference is seen to generally be well over 4 dB. RT differences can also be significant in range-dependent channels. Using the sound-speed profile in Fig. 1(c), and the same source frequency, source-receiver depths, and current structure as above, the computed intensity difference between a source-receiver pair is shown in Fig. 4. Note that one effect of the range

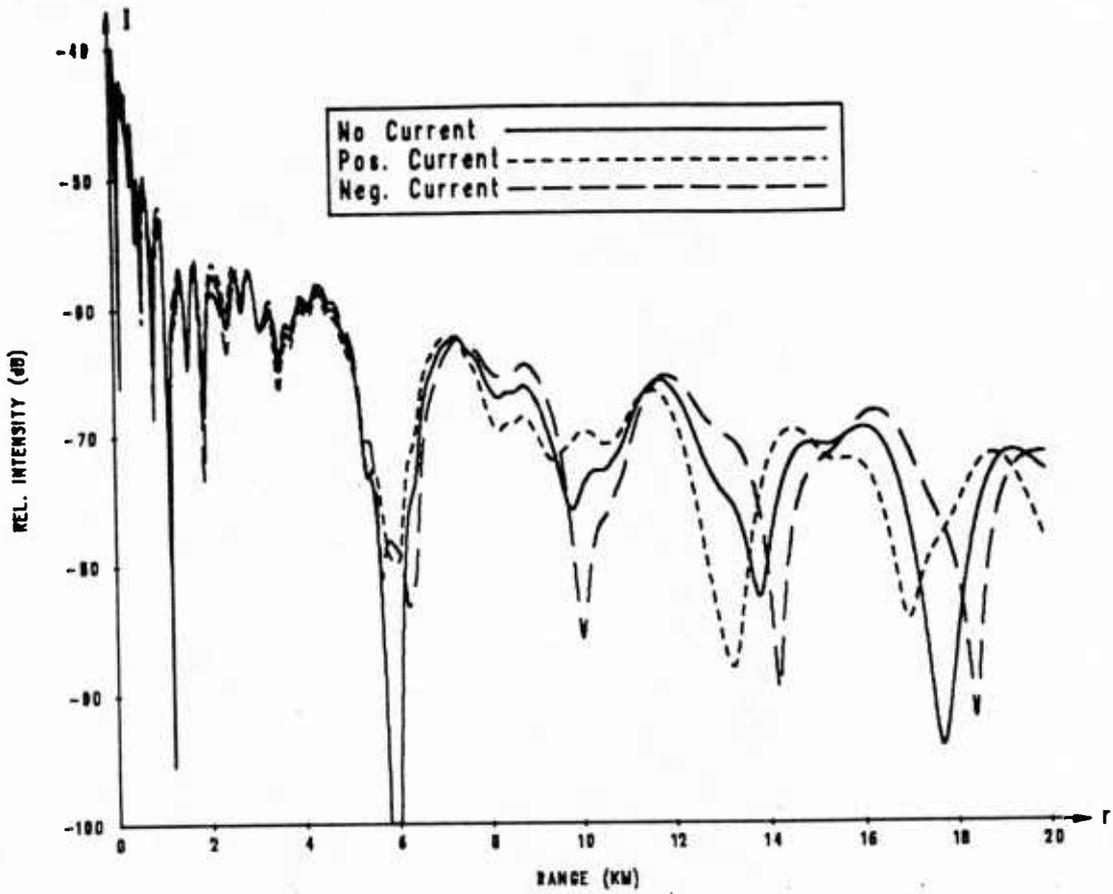


Fig. 2. Relative intensity versus range for three currents in an isospeed channel.

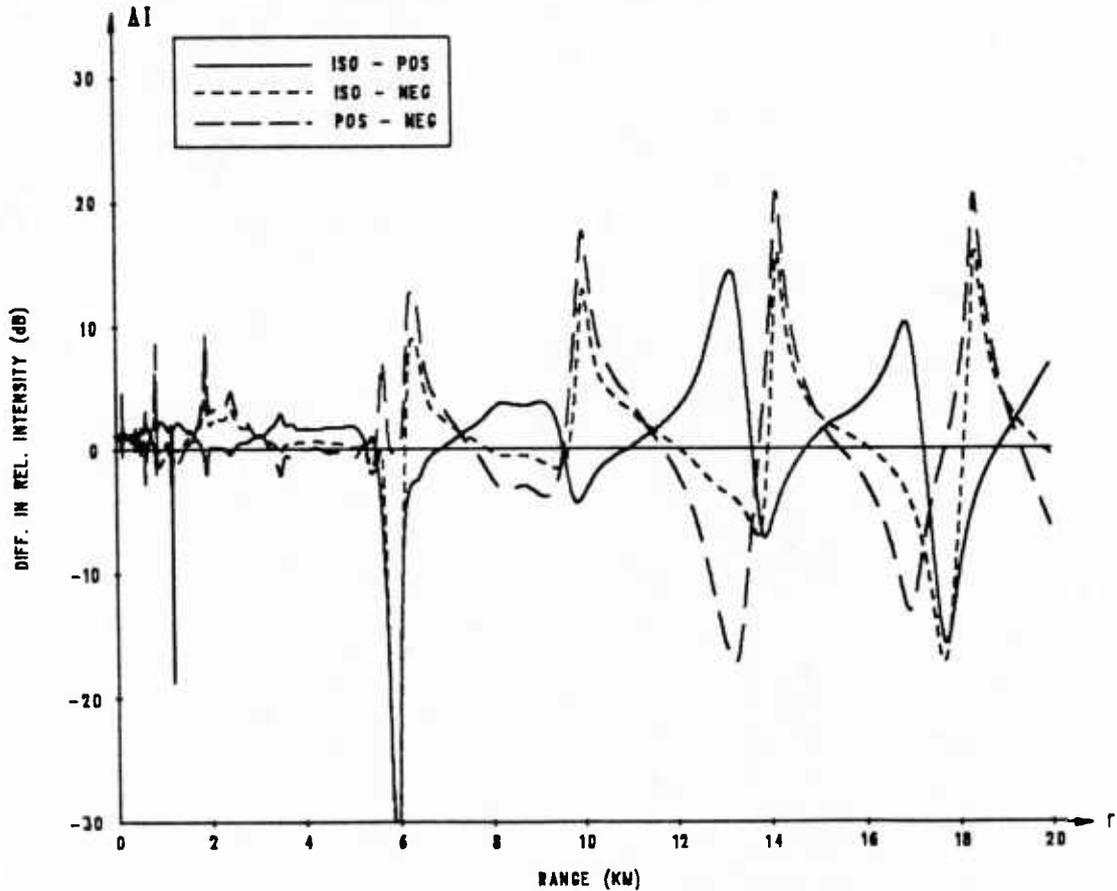


Fig. 3. Difference in relative intensity versus range, from Fig. 2. Oppositely-signed current effects are readily compared (long-dashed curve).

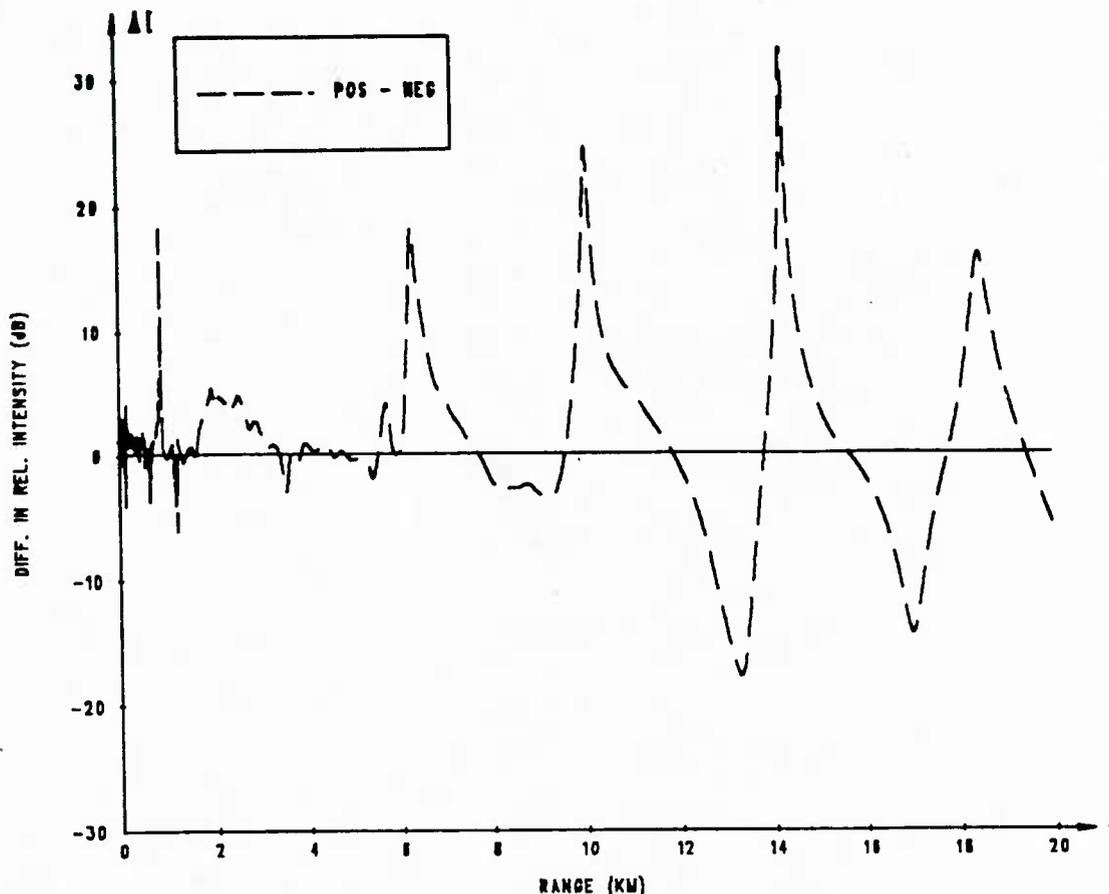


Fig. 4. Difference in relative intensity versus range, for current reversal. Reciprocal-transmission difference is shown for a range-dependent sound-speed profile.

variation in sound speed is to cause the relative intensity curve to shift toward the source, when compared to the analogous curve in Fig. 3. Maximum intensity values have been altered, also. For example, at a range 14 km, the peak difference is over 30 dB.

Another way to visualize the effects of reversing current direction is shown in Fig. 5. Here, differences in the two intensity functions are plotted as level curves in a portion of the depth-range plane. The difference is intensity for a positive current (in the source-receiver direction) minus intensity for a negative current, as in Fig. 1(b). The source frequency and source depth are again 200 Hz and 25 m, respectively. Contour intervals are 5 dB, with negative differences denoted by dotted curves. This figure illustrates the intensity differences that might be observed in a channel with tidal effects. At ranges larger than about 7 km, bottom attenuation has stripped away most higher modes, leaving a well-defined pattern of alternating intensity differences. Regions of large positive difference occur in finger-like patterns which alternately emanate from the channel surface and bottom. Similar structures are also seen for negative differences. In this example, a zone of very small differences extends in range across most of the channel at roughly mid-depth. Regions of maximum difference occur regularly above and below this zone. In contrast, the intensity-difference pattern in a negative gradient channel is noticeably different. Figure 6 shows the analogous level curves for the negative gradient profile of Fig. 1(a). The finger-like structures apparent in Fig. 5 have in some cases blended together in Fig. 6, leaving regions of high intensity difference located at many mid-depth points. The overall pattern is more complicated than the one present in the isospeed channel. Consequently, the intensity-difference pattern resulting from oppositely-signed currents

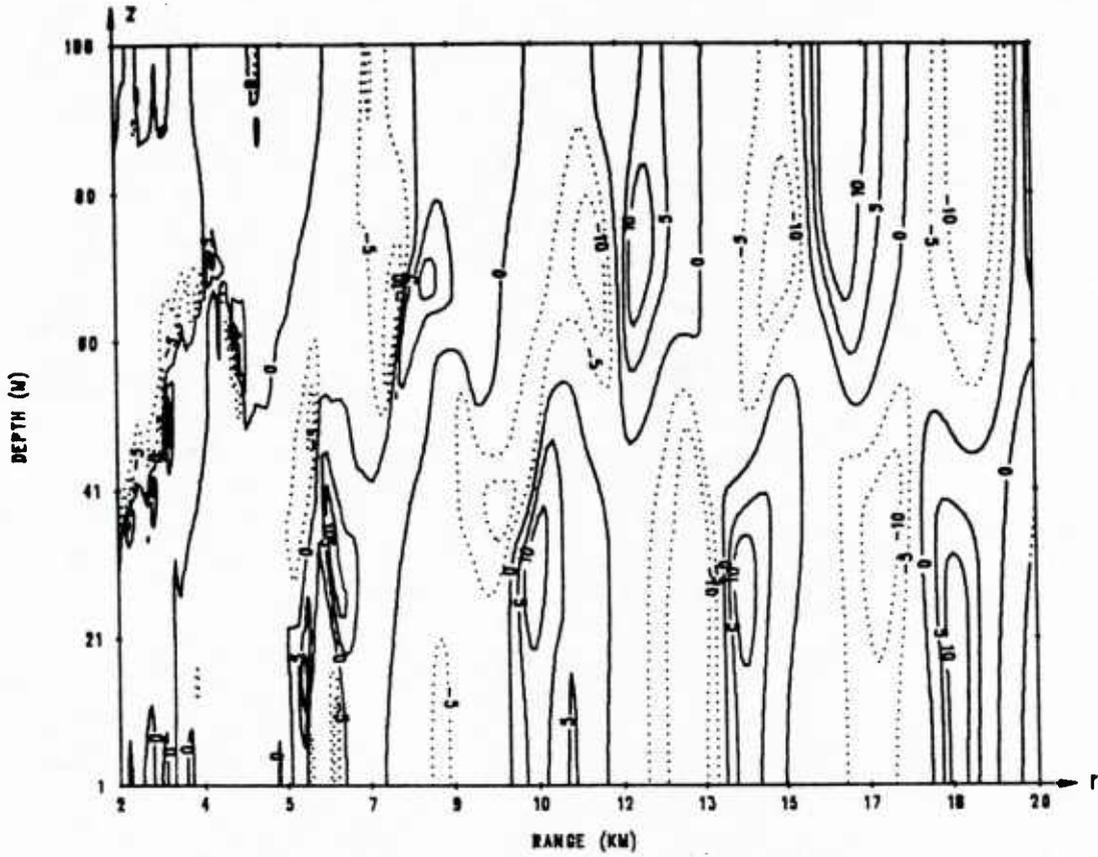


Fig. 5. Level curves of intensity difference in an isospeed channel, with current reversal.

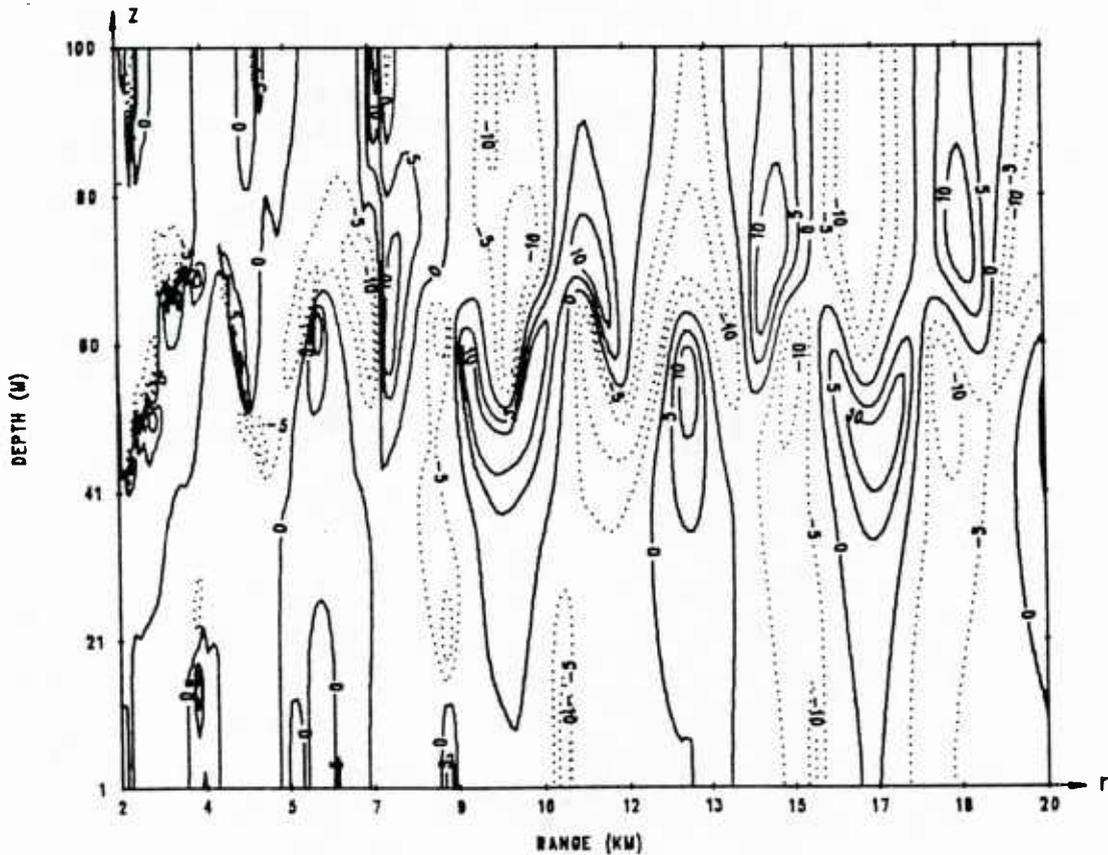


Fig. 6. Level curves of intensity difference for a negative gradient channel (see Fig. 1(a)), with current reversal.

appears to be very sensitive to these types of changes in the sound-speed profile. 7

For some current structures and lower source frequencies, the appropriate transformed parabolic equation will include new terms which depend on current concavity and (possibly) the square of current gradient. One type of current structure which may require additional terms is shown in Fig. 7(a). At the surface, the current speed is 1 m/s, and it decays to zero at the bottom. Note the appearance of several strong shear layers, particularly those at depths 35 and 60 m. The vertical shear structure seen here can be acoustically significant for sufficiently low source frequencies. For example, when the source frequency is 30 Hz, the ESSP is similar to that given by Eq. (5) and is depicted in Fig. 7(b). In this example, concavity effects are significant, but shear effects can be neglected. Note that current concavity dominates the behavior of the ESSP. The current shear structure has introduced large rapid variations, one of which, at the depth 60 m, approaches 20 m/s in Fig. 7(b). For higher source frequencies, the magnitude of the variations decreases, yet may still be significant. We anticipate that this current structure can cause interesting acoustical effects.

In Fig. 8, we see one result of computations done with the current structure shown in Fig. 7(a). In order to observe concavity (or second derivative) effects, we solved the relevant parabolic equation, first with concavity included and then with concavity omitted. The root-mean-square difference of the intensities in the two cases, called  $J$ , was then calculated with a range averaging. Source and receiver depths are 25 m, and the source frequency is 100 Hz. The results for three different bottom types are shown. The rigid bottom is perfectly reflecting, while beneath the water column for the hard and soft bottoms is a second fluid layer with different sound speed and density. The hard bottom has larger discontinuities in these quantities than the soft bottom. For both hard and soft bottoms, a small amount of volume attenuation was introduced. As the bottom changes

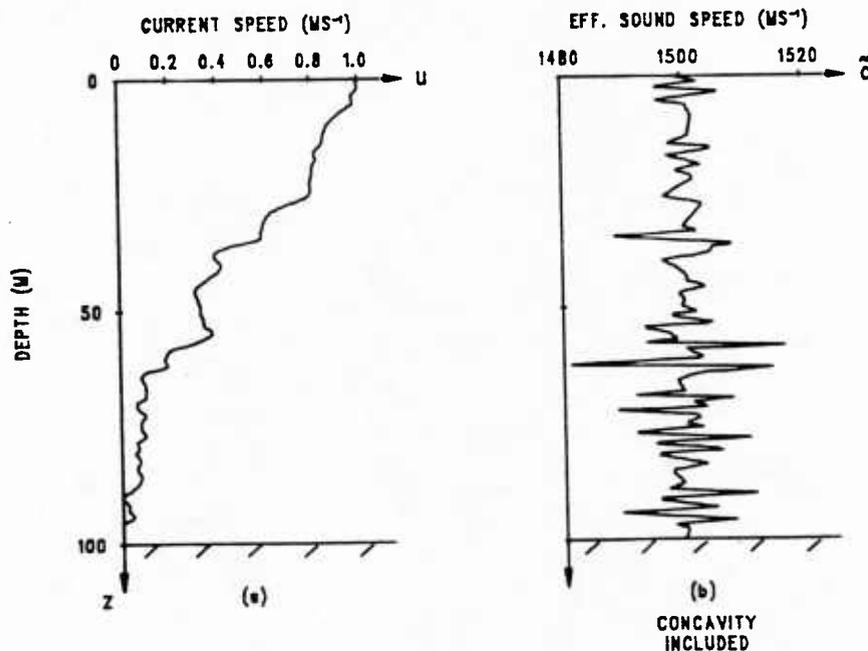


Fig. 7. Profiles of (a) a current with high shear, and (b) the effective sound speed.

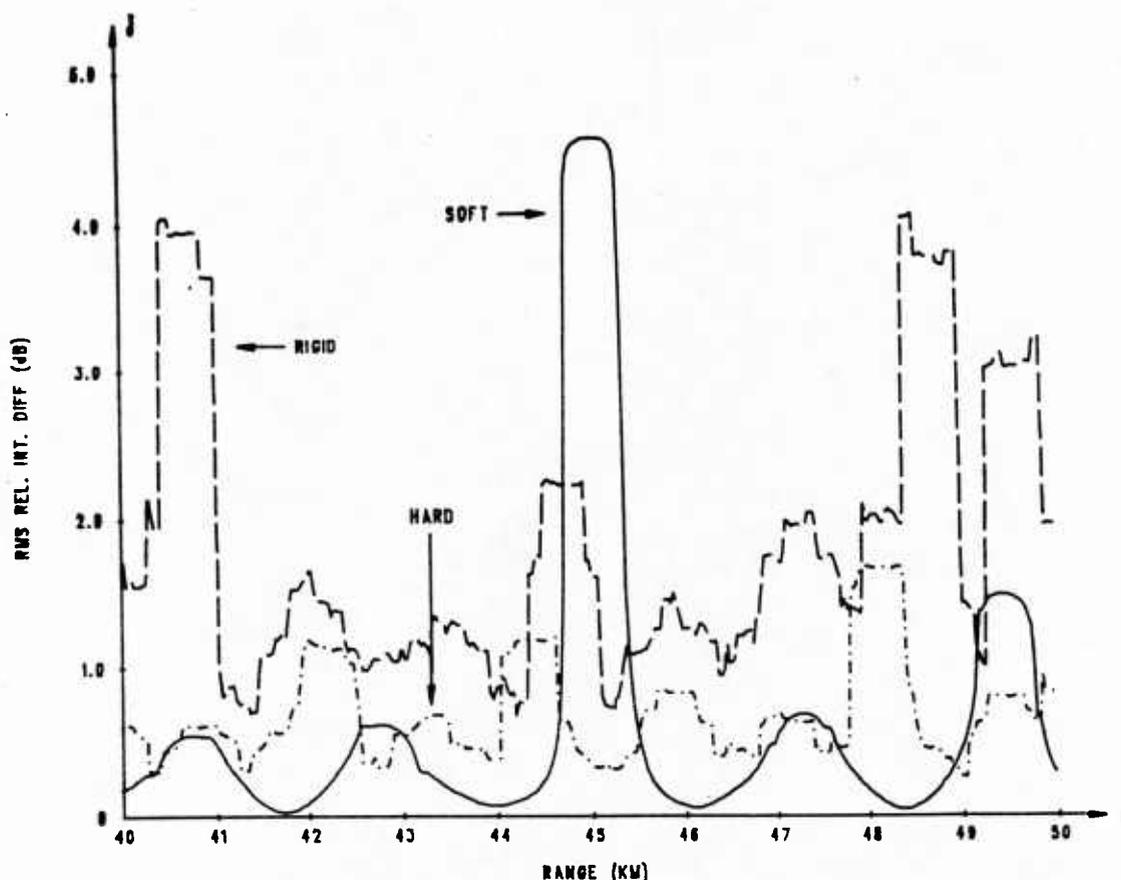


Fig. 8. RMS difference in intensity versus range for the current of Fig. 7(a) and for three bottom types.

from rigid to hard to soft, note that the overall values of  $J$  tend to decrease. However, the peak values may actually increase substantially. For example, at 45 km the soft bottom has a peak which is about 4 dB larger than its overall value. Furthermore, the curves are smoother for both the hard and soft bottoms, since they attenuate higher modes more rapidly than the rigid bottom. These observations illustrate the strong dependence of concavity effects on bottom influences in underwater sound transmissions.

#### SUMMARY

We discuss a family of parabolic approximations, valid for depth- and range-dependent sound-speed profiles, which include effects caused by steady depth-dependent currents. These approximations permit examination of intensity effects caused by currents for frequencies and environments where other models may not be valid or convenient. Using a standard numerical implementation, we present the results of computations for several current and sound-speed structures. They suggest that currents can cause significant intensity variations, principally by altering the effective sound-speed profile. Intensity differences arising from reciprocal transmissions are shown to be especially large. Also, current effects on intensity can be very sensitive to small changes in sound speed. Finally, the presence of current fine structure can introduce additional fluctuations in intensity predictions.

Lee, D., and Botseas, G., 1982, IFD: An implicit finite difference computer model for solving the parabolic equation, New London Lab., NUSC, New London, CT, TR 6659.

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