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WLF Dependence of the Dielectric Properties of DGEBA Epoxy Resins

by

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dipole loss, \( f_{\text{max}} \), and of the conductivity, \( \sigma \), obey the Williams-Landel-Ferry (WLF) equation. The WLF constants \( C_1 \) and \( C_2 \) were determined for both the \( f_{\text{max}} \) and \( \sigma \) data for each of the resins. In a given material, the WLF constants for \( \sigma \) and \( f_{\text{max}} \) differed, indicating that the temperature dependences of the mobilities of ionic impurities and permanent dipole moments differ quantitatively. As the EEW of the material increased, the \( C_1 \) constants for the conductivity remained constant, while the \( C_2 \) constants increased. The \( C_1 \) constants for \( f_{\text{max}} \) decreased with increasing resin EEW, approaching the \( C_1 \) values determined for the conductivity at high EEW's, while the corresponding \( C_2 \) constants decreased slightly. Free volume and entropic theories of the glass transition are used to interpret these results in terms of the underlying conduction and dipole relaxation processes.
Synopsis

The frequency and temperature dependence of the complex dielectric constant ($\varepsilon'$) of seven diglycidyl ether of bisphenol-A (DGEBA) epoxy resins having epoxide equivalent weights (EEW) in the range 175 to 1880 have been measured from $T_g - 30^\circ C$ to $T_g + 70^\circ C$ at frequencies between 0.1 and 10,000 Hz. In the vicinity of $T_g$, $\varepsilon'$ is dominated by dipole relaxation, while at higher temperatures ionic conductivity dominates. For all resins, the temperature dependences of the frequency of maximum dipole loss, $f_{max}$, and of the conductivity, $\sigma$, obey the Williams-Landel-Ferry (WLF) equation. The WLF constants $C_1$ and $C_2$ were determined for both the $f_{max}$ and $\sigma$ data for each of the resins. In a given material, the WLF constants for $\sigma$ and $f_{max}$ differed, indicating that the temperature dependences of the mobilities of ionic impurities and permanent dipole moments differ quantitatively. As the EEW of the material increased, the $C_1$ constants for the conductivity remained constant, while the $C_2$ constants increased. The $C_1$ constants for $f_{max}$ decreased with increasing resin EEW, approaching the $C_1$ values determined for the conductivity at high EEW's, while the corresponding $C_2$ constants decreased slightly. Free volume and entropic theories of the glass transition are used to interpret these results in terms of the underlying conduction and dipole relaxation processes.
INTRODUCTION

The measurement of dielectric properties is widely used as a means of studying the cure of thermosetting polymers because it is one of the few methods that can follow the complete transformation from liquid resin to glassy solid. The dielectric properties of these materials depend on the mobilities of ionic impurities and of permanent dipole moments, both of which decrease by many orders of magnitude during cure. There is evidence in the literature of a correlation between viscosity and both mean dipole relaxation time \([1,2]\) and ionic conductivity \([3,4]\).

Recent studies of thermosets \([5,6,7]\) have attempted to model the temperature and cure dependence of the viscosity using a Williams-Landel-Ferry (WLF) equation \([8]\), but modified to include the dependence of the glass transition temperature, \(T_g\), on chemical conversion. While there is considerable evidence that the temperature dependence of the mean dipole relaxation time \([9]\) and ionic conductivity \([10-13]\) in polymers can be modeled using the WLF equation, this approach has not yet been used to model the dielectric properties during cure. However, given the relationship between the dielectric properties and the viscosity, such modeling should be successful.

The purpose of this work is to make a first step in the WLF modeling of dielectric properties of curing epoxy systems. The WLF approach would require measuring the temperature dependence of the quantity of interest at fixed chemical conversion. This paper reports a simpler study of the dielectric properties of a homologous series of DGEBA epoxy resins of varying molecular weights (without curing agent). The insights drawn from this study about the application of the WLF equation
to the dielectric properties during cure will be discussed in the conclusion.

EXPERIMENTAL

The epoxy resins used were seven commercial samples of diglycidyl ether of bisphenol-A (DGEBA) resins having epoxide equivalent weights ranging from 175 to 1880. The structural formula of DGEBA is illustrated in Figure 1. Table 1 presents epoxide equivalent weight, the value calculated from the EEW, and the measured at 10°C/min using DSC. Prior to use, the samples were heated under vacuum to remove water and other volatiles.

The dielectric measurements were performed using microdielectrometry [14,15], which utilizes a silicon integrated circuit sensor having a comb electrode pattern, amplifying circuitry, and a semiconductor diode for temperature measurement. The sample to be measured is placed on the surface of the sensor, in intimate contact with the comb electrode pattern. Utilizing additional amplifying circuitry and a Fourier transform signal source/correlator, the electrical admittance of the comb electrode pattern can be measured at frequencies ranging from 0.005 Hz to 10,000 Hz. The calibration of the sensor in terms of the complex permittivity is based on a numerical solution to Laplace's equation [16]. The maximum electric field is approximately 1000 V/cm.

The electrode area of the microdielectrometry sensor is 2 x 3.5 mm. Resin samples of less than 10 mg were applied to the sensors by heating the sensor on a hot plate and melting the resin over the comb electrode structure. The sensor was placed into a programmable sample chamber.
under nitrogen and the room temperature reading of the diode temperature indicator was calibrated against a thermocouple embedded in the sensor holder. The sample was then cooled or heated to the starting temperature and the temperature program and data acquisition, under computer control, was initiated. The temperature was increased from approximately $T_g - 30^\circ C$ to $T_g + 70^\circ C$ in discrete steps of $4^\circ C$. At each temperature, the dielectric permittivity and loss factor were measured at 26 frequencies in the range of 0.1 to 10,000 Hz.

**RESULTS AND DISCUSSION**

**Conductivity and Frequency of Maximum Dipole Loss**

Figure 2 illustrates the temperature dependence of the dielectric permittivity and loss factor for EPON 828 resin, which has a glass transition temperature of $-17^\circ C$. At temperatures well below $T_g$, the permittivity at all frequencies has a value of 4.2, and the loss factor is below 0.1. As the temperature approaches $T_g$, the dipoles gain sufficient mobility to orient partially during one cycle of the alternating field. The permittivity and loss factor at the lowest frequencies begin to increase first. With a further increase in temperature, the permittivity for a given frequency levels off, starts to decrease (a thermal effect [17,18]), and then abruptly increases again as a result of electrode polarization [19]. A dipole loss peak is observed in the loss factor, which then rises continuously with temperature due to an increasing ionic conductivity. The frequency at which the dipole loss peak occurs is proportional to the average dipole mobility. The ionic conductivity is proportional to the mobility of ionic impurities, pro-
vided the ion concentration remains fixed. This is a reasonable assumption since the ionic species are predominantly sodium and chloride remaining from the synthesis procedure [20,21], although there has been no explicit verification for the specific epoxy samples reported on here. Both the frequency of maximum loss, $f_{\text{max}}$, and the ionic conductivity increase by many orders of magnitude over a narrow temperature range, a characteristic of relaxation processes very close to the glass transition temperature.

The frequency dependence of the loss factor at fixed temperature, shown for three different temperatures in Figure 3, illustrates the mechanisms of ionic conductivity and dipole relaxation. At the highest temperature, $22^\circ \text{C}$, the loss factor is inversely proportional to frequency, with a slope on a log-log plot very near to $-1$. This behavior is characteristic of a frequency independent ionic conductivity, $\sigma$, which is related to the loss factor by the equation,

$$\sigma = \varepsilon'' \varepsilon_0 \omega$$

(1)

where $\varepsilon_0$ is the permittivity of free space and $\omega$ is the angular frequency. If electrode polarization effects were present in the loss factor data, the slope would decrease as the frequency decreased. Conductivity results presented here are taken from loss factor data where polarization effects are absent.

At the lowest temperature, $-12^\circ \text{C}$, there is a peak in the loss factor having a maximum value of about 2, characteristic of a dipole relaxation process. The asymmetric shape of this peak is well described by a Williams-Watts function [22]. This will be discussed in more detail in a separate communication. The present analysis is concerned
only with the average dipole mobility, characterized by the frequency of maximum loss. At an intermediate temperature, 5°C, the ionic conductivity is observed at low frequencies, while the onset of the dipole loss peak is seen at high frequencies.

The temperature dependent conductivities of all of the resin samples, determined at frequencies where the loss factor is inversely proportional to frequency, are shown plotted in Arrhenius fashion in Figure 4. There is significant curvature in this plot, indicating that the conduction process is not simply activated, and suggesting a process described by the WLF equation. The solid curves through the data points represent the fit to the WLF equation, to be discussed below.

The temperature dependence of the frequency of maximum loss for each resin sample was determined directly from the loss factor versus temperature data by identifying the dipole loss peak temperature for each frequency. An Arrhenius plot of the \( f_{\text{max}} \) data is presented in Figure 5. Although not as pronounced as the conductivity data, careful examination of the data reveals curvature characteristic of WLF rather than Arrhenius behavior. The smaller curvature is due to the fact that the dipole relaxation occurs at temperatures much closer to the glass transition and over a much narrower temperature range. The apparent activation energies calculated from the data are in the range 350-500 kJ/mol, extremely large for a thermally activated process. The solid curves represent the fit to the WLF equation, to be described below.
Williams-Landel-Ferry Equation

The Williams-Landel-Ferry (WLF) equation [8] is expressed as,

\[ \log (a_T) = \frac{-C_1 (T - T_g)}{C_2 + T - T_g} \]  \hspace{1cm} (2)

where \( a_T \) is the shift factor, originally defined as the ratio of the viscosity at temperature \( T \) to that at a reference temperature, \( T_g \). \( C_1 \) and \( C_2 \) are constants which depend on the reference temperature chosen and on the material. The constants were originally thought to be universal, having values of 17.44 and 51.6 when the reference temperature was taken as the dilatometric glass transition temperature. The universality of this equation was attributed to relaxation processes governed by free volume. By combining Doolittle's free volume theory of viscosity [23] with a free volume that increases linearly with temperature above the glass transition temperature, the constants \( C_1 \) and \( C_2 \) can be expressed in terms of \( f_g \), the free volume fraction of the glass, and a free volume thermal expansion coefficient, \( \Delta \alpha \), taken to be the difference in the thermal expansion coefficients above and below the glass transition temperature.

\[ C_1 = \frac{1}{2.3 f_g} \quad \quad C_2 = \frac{f_g}{\Delta \alpha} \]  \hspace{1cm} (3)

The proposal by Fox and Flory [24] that \( T_g \) is an iso-free-volume state \((f_g \text{ constant})\) and experimental evidence [8] showing that \( \Delta \alpha \) is approximately constant for a large number of polymers supported the argument that the WLF constants were universal.
To explain the subsequent observation that the constants $C_1$ and $C_2$ were not universal, Cohen and Turnbull [25] proposed a theory for transport based on free volume in which a critical free volume, $V^*$, resulting from redistribution of free volume without a change in energy, is required for a particle to diffuse. This theory leads to the WLF equation, with the constants equal to [10],

$$C_1 = \frac{\gamma f^*}{2.3 f_g} \quad C_2 = \frac{f_g}{\Delta u}$$  \(4\)

where $\gamma$ is a factor to account for the overlap of free volume [25], and $f^*$ is the critical free volume fraction. Since the critical free volume will depend on the particle or molecule diffusing, this theory helps account for the observed material dependence of the constants. When the theory is applied to dielectric relaxation of polymers, the critical free volume is interpreted as that volume necessary for the polar segment to relax. In recent work in which the ionic conductivity of polymers was interpreted in terms of WLF theory [10,11], the critical free volume has been interpreted as that volume required for ion transport.

Adam and Gibbs [26] proposed a theory for cooperative relaxation processes in polymers near $T_g$ based on Gibbs and Dimarzio's entropic theory for the glass transition [27]. The theory assumes a configurational entropy which goes to zero at a temperature $T_2$. A second order phase transition would occur at $T_2$ if the rate of molecular rearrangement, which depends on the configurational entropy, did not become infinitesimal. The glass transition is observed experimentally at a
temperature $T_g > T_2$, which is the temperature at which the time scale for molecular rearrangement becomes comparable to the time scale of the experiment.

The Adam and Gibbs theory relates the relaxational properties of polymers to the Gibbs and Dimarzio second order transition temperature, $T_2$. The basis of the theory is that the number of segments required for a cooperative relaxation increases as the temperature decreases, making the relaxation process more difficult. An average transition probability, $W(T)$, is derived,

$$W(T) = A \exp \left( -\frac{z^* \Delta \mu}{kT} \right)$$

where $z^*$ is the number of molecules or segments involved in the relaxation, and $\Delta \mu$ is the free energy barrier per molecule or segment. Assuming the cooperatively rearranging regions to be noninteracting subsystems, $z^*$ is expressed in terms of $s_c^*$, a critical entropy for rearrangement, and the configurational entropy per segment, equal to the molar configurational entropy of the sample, $S_c$, divided by Avogadro’s number, $N_{av}$:

$$z^* = \frac{N_{av} s_c^*}{S_c}$$

As the temperature is lowered and the molar configurational entropy, $S_c$, approaches zero, $z^*$ gets very large, and the average transition probability $W(T)$ gets very small. The temperature dependence of the entropy term $S_c$ is expressed in terms of the change in specific heat at the glass transition, $\Delta C_p$. 
recalling that the configurational entropy is zero at temperature \( T_2 \). Note that this equation does not include any ionic contribution to the entropy; nor are the ions presumed to participate in the initial partitioning of the system into segments in Eq. 6. This point will be addressed later as possibly affecting the difference between the \( f_{\text{max}} \) and conductivity \( C_2 \) constants.

The shift factor, \( a_T \), can be expressed as a ratio of transition probabilities at temperatures \( T \) and \( T_s \), and rearranged to yield an expression in the form of the WLF equation,

\[
\log (a_T) = \log \left( \frac{W(T_s)}{W(T)} \right) = \frac{-C_1 (T - T_s)}{C_2 + (T - T_s)}
\]

where the WLF constants \( C_1 \) and \( C_2 \) are approximately,

\[
C_1 = \frac{2.303 s \sigma}{k \Delta \mu} \quad C_2 = \frac{\frac{T_s}{1 + \ln \left( \frac{T_s}{T_2} \right)}}{k \Delta \mu} \]

The WLF constants can be expressed in terms of the "true" second order transition temperature \( T_2 \), and the energy barrier \( \Delta \mu \). Adam and Gibbs found "universal" values of \( T_s/T_2 = 1.3 \) and \( T_2 - T_s = 55^\circ \text{C} \), and estimated \( \Delta \mu \) to be comparable to molecular interaction energies [26].

**Interpretation of \( C_1 \) and \( C_2 \)**

The results presented in the Arrhenius plots of Figures 4 and 5 suggested that both the conductivity and the frequency of maximum loss
could be represented by the WLF equation. The substitution of \( \sigma \) or \( f_{\text{max}} \) for viscosity in the definition of the shift factor, \( a_T \), necessitated a sign change in Equation 2, because both \( \sigma \) and \( f_{\text{max}} \) increase with increasing temperature. To determine \( C_1 \) and \( C_2 \) for a given material, a variation of the standard WLF test plot procedure [8], shown in Figure 6, was used. Each of the data points was used as a trial reference temperature, and the resulting values of \( C_1 \) and \( C_2 \) were then normalized to a reference temperature equal to the glass transition temperature determined from the DSC. The set of normalized constants, which agreed to \( \pm 10\% \) for the conductivity data and \( \pm 20\% \) for the \( f_{\text{max}} \) data, were then averaged to obtain the "best fit" \( C_1 \) and \( C_2 \) values for that material. These values are presented in Table 2 for the conductivity and in Table 3 for the frequency of maximum loss. The constants in the Tables were used to draw the solid curves through the data in Figures 4 and 5.

The conductivity \( C_1 \) constant is independent of the EEW of the resin, while the \( f_{\text{max}} \) \( C_1 \) constant and the \( C_2 \) constants are EEW dependent. For the cases that are EEW dependent, note that the values for the two low molecular weight resins are similar to one another, as are those for the four high EEW resins, while the \( n=0.6 \) resin values are intermediate. The conductivity at \( T_g \) increases with increasing EEW of the resin, while \( f_{\text{max}}(T_g) \) is approximately constant. The variation in \( \sigma(T_g) \) for the different resins is too large to attribute to variations in ionic impurity concentration and, instead, is attributable to a basic difference between ion mobility and polymer chain mobility. This is discussed in detail below. The approximately constant value of \( f_{\text{max}}(T_g) \) indicates a correlation between the DSC glass transition temperature and
the dipole loss peak measured at a frequency of approximately 3 Hz. A similar correlation between the low frequency dipole loss peak and vitrification has been observed in curing systems [18].

Assuming that $T_8$ is an iso-free-volume state ($f_8$ constant) [24], and the overlap factor $\gamma$ is independent of EEW, Cohen and Turnbull's model described above predicts that the $C_1$ constants for conductivity and $f_{\text{max}}$ are proportional to critical volumes for ion transport, $V_1^0$, and for polar segmental motion, $V_2^0$, respectively. The $C_1$ behavior indicates that the critical volume for ion transport, $V_1^0$, is independent of EEW. This is not surprising because of the small size of the ionic impurities relative to the resin molecules; even the lowest EEW resin is large compared to the ion. The observed decrease in $V_2^0$, the critical volume for segmental motion, suggests the volume required to relax a typical dipolar segment decreases with increasing EEW. This result may not be due to the increased chain length, but to the changing chemical composition. Referring back to Figure 1, two types of polar segments can be identified: a glycidyl ether unit at the chain end and a hydroxyether segment in the backbone of the oligomers. As the molecular weight of the resin increases, there is a systematic increase in the fraction of hydroxyether segments. Assuming all of the DGEMA resins are linear molecules, and the polarities of the two types of segments are approximately the same, the fraction of hydroxyether segments in a sample of given EEW will be equal to $n/(2+n)$. If the critical volume for segmental relaxation can be expressed in terms of a number average of that for a hydroxyether segment (HE) and of a glycidyl ether segment (GE), then $C_1$ can be expressed as,
\[ C_1 = \frac{2}{(2+n)} C_{1,GE} + \frac{n}{(2+n)} C_{1,HE} \]  

This \( n \)-dependence can be illustrated as follows. Taking \( C_{1,HE} \) as equal to 10.5, the average value obtained from the ionic conductivity analysis, and taking \( C_{1,GE} \) as twice \( C_{1,HE} \) yields the solid line plotted in Figure 7. The agreement is qualitative at best, but supports the hypothesis that the \( C_1 \) value is related to the type of polar segment relaxing. A possible explanation for the difference in critical relaxation volumes for the two segments is that the hydroxyether may relax by a crankshaft mechanism with minimal involvement of neighboring molecules, whereas the relaxation of the glycidyl ether requires cooperative motion of neighboring molecules.

The free volume theory is unable to explain the behavior of the \( C_2 \) constants. Referring back to Equation 2, the \( C_2 \) constant depends only on \( f_g \), the free volume fraction at \( T_g \), and \( \Delta \alpha \), the difference in thermal expansion coefficients above and below \( T_g \). On this basis, the \( C_2 \) values should be the same for the \( f_{\text{max}} \) and the conductivity data, but the \( C_2 \) values determined from the conductivity data increase with increasing EEW, while those determined from the \( f_{\text{max}} \) data decrease slightly.

The Adam-Gibbs thermodynamic theory provides an expression for \( C_2 \) in terms of the second order transition temperature, \( T_2 \), which can be determined directly from \( C_2 \) using Equation 8. The results of this analysis for the \( f_{\text{max}} \) data are presented in Table 4. The \( T_2 \) values range from 175 K for the \( n=0.2 \) sample to 309 K for the \( n=12.1 \) sample, while the corresponding values of \( T_g \) are 257 K and 352 K, respectively. The average value of \( T_g - T_2 \) for the seven samples is 60°C ± 21% which is
consistent with the value of 55° ± 11% found by Adam and Gibbs for a wide variety of polymers [26]. The same analysis was repeated for the conductivity data and the results are presented in Table 5. The T2 values range from a low of 209 K for the n=2.3 sample to 259 K for the n=12.1 sample. These values are significantly different than those determined from the f_max data. This is emphasized in Figure 8, which is a plot of the T2 values versus the Tg of the resins. The f_max values scatter about a line with a slope of 1.2, while the conductivity T2 values are relatively independent of Tg.

The correlation of the T2's from the f_max data with Tg indicates that the temperature dependence of the configurational entropy function governing the heat capacity change at Tg measured by the DSC is similar to that governing the dipole relaxation. The constant values of f_max at the DSC Tg are a manifestation of this. The relative insensitivity of the conductivity T2 values to Tg indicates that cooperative molecular relaxation processes are only a part of the conduction process. The wide variation in σ(Tg) for the different resins is consistent with this interpretation. The application of the Adam-Gibbs theory to the ionic conductivity may require a reformulation or redefinition of the critical segment (Eq. 6) and/or the relevant configuration entropy term (Eq. 7), to account for the additional configurational states available to ions. Such a reformulation has not been carried out.

CONCLUSION

The temperature dependences of the conductivity and frequency of maximum loss in DGEBA epoxy resins near Tg are described by different
WLF equations, due to the differing natures of the conduction and dipole relaxation processes. The WLF $C_1$ constants reflect critical volumes for ion transport and dipolar segment motion. The critical volumes for ion transport are independent of resin EEW, because of the small size of ionic impurities relative to the resin molecules. The EEW dependence of the critical volumes for polar segmental motion correlates with the relative concentrations of glycidyl ether and hydroxyether segments, leading to speculation that the hydroxyether relaxes by a crankshaft mechanism with minimal involvement of neighboring molecules, while the glycidyl ether requires cooperative motion of neighbors.

The Adam-Gibbs entropic theory of the glass transition was used to determine the Gibbs-Dimarzio second order transition temperatures, $T_2$, from the WLF $C_2$ constants. For the $f_{\text{max}}$ data, $T_2$ values were about 60° below $T_g$. The $T_2$ values determined from the conductivity data were relatively independent of $T_g$, indicating that degrees of freedom in addition to the polymer chain configurations are required for the ionic conduction process, and that proper application of this theory to conduction will require reformulation to account for these additional degrees of freedom.

An important conclusion to be drawn from these results is that to first order, the parameters $C_1$ and $T_2$ describing the temperature dependence of the conductivity are both relatively independent of the detailed chemical structure of the sample. Therefore, in curing systems, if the constancy of $C_1$ and $T_2$ can be assumed, it should be possible to follow the change in $T_g$ during cure using the measured conductivity.
change and the WLF equation. Results supporting this idea will be presented in a separate communication.

ACKNOWLEDGEMENT

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REFERENCES


### Table 1 - Epoxy Resin Samples

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<sup>1</sup> Values from [20]

<sup>2</sup> Samples and EEW's by titration supplied by J. LeMay, Univ. of Akron

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### Table 2 - WLF Constants for σ

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<th>n</th>
<th>C&lt;sub&gt;1&lt;/sub&gt; ± C&lt;sub&gt;1&lt;/sub&gt;'</th>
<th>C&lt;sub&gt;2&lt;/sub&gt;(°C) ± C&lt;sub&gt;2&lt;/sub&gt;'</th>
<th>log[σ(T&lt;sub&gt;g&lt;/sub&gt;)]</th>
</tr>
</thead>
<tbody>
<tr>
<td>X22</td>
<td>0</td>
<td>10.2 ± 0.1</td>
<td>34 ± 3</td>
<td>-15.7</td>
</tr>
<tr>
<td>828</td>
<td>0.2</td>
<td>10.3 ± 0.1</td>
<td>30 ± 5</td>
<td>-16.1</td>
</tr>
<tr>
<td>834</td>
<td>0.6</td>
<td>10.1 ± 0.2</td>
<td>49 ± 6</td>
<td>-15.4</td>
</tr>
<tr>
<td>1001</td>
<td>2.3</td>
<td>11.5 ± 0.6</td>
<td>92 ± 10</td>
<td>-14.1</td>
</tr>
<tr>
<td>1002</td>
<td>3.4</td>
<td>10.1 ± 0.2</td>
<td>71 ± 5</td>
<td>-14.7</td>
</tr>
<tr>
<td>1004</td>
<td>5.1</td>
<td>11.3 ± 0.4</td>
<td>82 ± 9</td>
<td>-15.3</td>
</tr>
<tr>
<td>1007</td>
<td>12.1</td>
<td>10.3 ± 0.4</td>
<td>83 ± 11</td>
<td>-14.5</td>
</tr>
</tbody>
</table>
Table 3 - VLF Constants for $f_{\text{max}}$

<table>
<thead>
<tr>
<th>ID</th>
<th>n</th>
<th>$C_1$</th>
<th>$C_2 (^\circ\text{C})$</th>
<th>log[$f_{\text{max}}(T_g)$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>X22</td>
<td>0</td>
<td>21.4 ± 3.5</td>
<td>61 ± 12</td>
<td>-0.1</td>
</tr>
<tr>
<td>828</td>
<td>0.2</td>
<td>21.2 ± 3.5</td>
<td>71 ± 13</td>
<td>0.3</td>
</tr>
<tr>
<td>834</td>
<td>0.6</td>
<td>15.2 ± 2.7</td>
<td>48 ± 10</td>
<td>-0.2</td>
</tr>
<tr>
<td>1001</td>
<td>2.3</td>
<td>12.5 ± 1.0</td>
<td>51 ± 4</td>
<td>1.3</td>
</tr>
<tr>
<td>1002</td>
<td>3.4</td>
<td>12.7 ± 1.8</td>
<td>53 ± 8</td>
<td>0.8</td>
</tr>
<tr>
<td>1004</td>
<td>5.1</td>
<td>13.4 ± 1.4</td>
<td>55 ± 7</td>
<td>0.5</td>
</tr>
<tr>
<td>1007</td>
<td>12.1</td>
<td>11.6 ± 1.2</td>
<td>40 ± 6</td>
<td>0.1</td>
</tr>
</tbody>
</table>

Table 4 - Adam-Gibbs Analysis for $f_{\text{max}}$ data

<table>
<thead>
<tr>
<th>n</th>
<th>$C_2$</th>
<th>$T_g$</th>
<th>$T_2$</th>
<th>$T_g-T_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>61</td>
<td>254</td>
<td>185</td>
<td>69</td>
</tr>
<tr>
<td>0.2</td>
<td>71</td>
<td>257</td>
<td>175</td>
<td>82</td>
</tr>
<tr>
<td>0.6</td>
<td>47</td>
<td>269</td>
<td>217</td>
<td>52</td>
</tr>
<tr>
<td>2.3</td>
<td>51</td>
<td>315</td>
<td>259</td>
<td>56</td>
</tr>
<tr>
<td>3.4</td>
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<td>324</td>
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</tr>
<tr>
<td>5.1</td>
<td>55</td>
<td>334</td>
<td>274</td>
<td>60</td>
</tr>
<tr>
<td>12.1</td>
<td>40</td>
<td>352</td>
<td>309</td>
<td>43</td>
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</tbody>
</table>
Table 5 - Adam-Gibbs Analysis for conductivity data

<table>
<thead>
<tr>
<th>n</th>
<th>C₂</th>
<th>Tₙ</th>
<th>T₂</th>
<th>Tₙ-T₂</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>34</td>
<td>254</td>
<td>217</td>
<td>37</td>
</tr>
<tr>
<td>0.2</td>
<td>29</td>
<td>257</td>
<td>225</td>
<td>32</td>
</tr>
<tr>
<td>0.6</td>
<td>48</td>
<td>269</td>
<td>215</td>
<td>54</td>
</tr>
<tr>
<td>2.3</td>
<td>91</td>
<td>315</td>
<td>209</td>
<td>106</td>
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<tr>
<td>3.4</td>
<td>71</td>
<td>324</td>
<td>245</td>
<td>79</td>
</tr>
<tr>
<td>5.1</td>
<td>81</td>
<td>334</td>
<td>242</td>
<td>92</td>
</tr>
<tr>
<td>12.1</td>
<td>82</td>
<td>352</td>
<td>259</td>
<td>93</td>
</tr>
</tbody>
</table>
1. Structure of diglycidyl ether of bisphenol-A (DGEBA)
2. Permittivity, $\varepsilon'$, and loss factor, $\varepsilon''$, versus temperature for EPON 828 at frequencies of 0.1, 1, 10, 100, 1000 and 10,000 Hz.
3. Loss factor, $\varepsilon''$, versus frequency for EPON 828 at temperatures of -12°C, 5°C and 22°C.
4. Arrhenius plot of ionic conductivity, $\sigma$, of EPON resins.

- $a = 1007$, $b = 1004$, $c = 1002$, $d = 1001$, $e = 834$, $f = 828$, $g = 822$
5. Arrhenius plot of frequency of maximum dipole loss, $f_{\text{max}}$, of EPON resins.
   a - 1007, b - 1004, c - 1002, d - 1001, e - 834, f - 828, g - X22
6. Test plot of Williams-Landel-Ferry equation for EPON 828 ionic conductivity data, using a reference temperature of $-1.5^\circ C$. 
7. WLF constant $C_1$ versus mer index $n$ of DGEBA. Triangles - $\sigma$, circles - $f_{\text{max}}$
8. Gibbs-DiMarzio second order transition temperature, $T_2$, versus glass transition temperature of DGEBA.
triangles - $\sigma$, circles - $f_{\text{max}}$
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