THE IMPORTANCE OF PHASE IN WORD RECOGNITION

by

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Phase Representation, Cepstral Processing, Homomorphic Processing, Hilbert Transform, Speech Recognition, Analytic Signal, Short-term Phase, Cepstrum

The use of phase-only representations of speech for isolated word recognition is explored. Until recently the ear was thought to be short-term phase insensitive. However, short-term phase-only reconstructed speech has been shown to retain much of the intelligibility of the original signal. Using cepstral and analytic-signal processing techniques, a
20. (Continued)

system for isolated word recognition is developed. The
results of tests for both the speaker-dependent and
speaker-independent case indicate that phase may be an
important feature to consider in the development of word
recognition systems.
ABSTRACT

The use of phase-only representations of speech for isolated word recognition is explored. Until recently the ear was thought to be short-term phase insensitive. However, short-term phase-only reconstructed speech has been shown to retain much of the intelligibility of the original signal. Using cepstral and analytic signal processing techniques, a system for isolated word recognition is developed. The results of tests for both the speaker-dependent and speaker-independent case indicate that phase may be an important feature to consider in the development of word recognition systems.
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I. INTRODUCTION

As the complexity of man's machines increases, so does the need for simple, efficient man-machine interfaces. Automatic speech recognition plays a major role in this man-machine communication because of the superiority of speech over other modes of human communication. Speech is the most familiar and most convenient way for humans to communicate. Voice input leaves the hands and eyes of the operator free to perform other tasks and allows speaker mobility.

Word recognition is one facet of the research conducted in the area of speech processing. Speech processing can be divided into three major categories. The speech analysis area includes word recognition, speaker identification, and speaker verification. The second category is speech synthesis. An example of synthesis is a data-retrieval system, where the computer responds verbally when its database is interrogated. Another example is when a child receives a verbal response from his toy informing him he has correctly answered a question. The third area is a combination of the first two, speech analysis followed by speech synthesis. This has application in secure voice transmission and speech data rate reduction. As an example of the latter, the telephone company requires 64K bits/sec
to transmit speech. The Department of Defense standard for data rate reduction is 2.4K bits/sec. The Air Force is experimenting with data rates as low as 150 bits/sec which provides intelligible speech.

The advent of the general purpose digital computer in the mid-1960s provided speech researchers with a powerful tool. Numerous speech processing algorithms using digital signal process techniques have been developed for both analysis and synthesis. From using dynamic programming to time-warp speech prior to processing, to algorithms for extracting parameters to be used for speech synthesis, speech processing is a billion dollar a year business.

Various speaker-dependent word recognition systems are commercially available. These systems generally perform some type of spectral analysis on the incoming speech signal. The recognition process involves classical pattern recognition techniques. These systems have a very high rate of successful recognition.

The success of these systems notwithstanding, the problem of constructing a speaker-independent recognition system remains unsolved. The solution to this problem involves determining what features of speech contain the information and hence are speaker independent. Before one can talk about extracting the information content from the
speech signal, a look at a model of how humans produce speech is in order.

A. FUNDAMENTALS OF SPEECH

Flanagan [Refs. 1 and 2] formulated a generally accepted model for human speech production. His model describes the vocal tract as a nonuniform acoustic tube connecting the vocal cords and the lips. In an adult male the vocal tract is approximately 17 cm. in length.

The vocal tract can be connected to an ancillary cavity called the nasal cavity. The coupling is accomplished through a trapdoor mechanism called the velum. The nasal cavity begins at the velum and terminates at the nostrils. In an adult it is about 12 cm. long. When non-nasal sounds are produced the velum closes, thereby sealing off the nasal cavity.

Humans are capable of producing two types of sounds, voiced and unvoiced. In the case of voiced sounds air moves over the vocal cords causing them to vibrate in a quasi-periodic fashion. Unvoiced sounds are generated by either forming a constriction in the tract and forcing the air through at high velocity or by allowing pressure to build up behind the closure and then releasing it suddenly. The name fricative is associated with the former while plosive is the name given to the latter.
Since the physical configuration of the vocal tract changes with time, Flanagan's model can be represented as a linear time-varying system as shown in Figure 1.1.

![Diagram of Speech Production Model](image)

Figure 1.1. Model of Speech Production

If it is assumed that the vocal tract changes slowly with time the output can be approximated by the short-term convolution of the excitation, \( x(t) \), and the vocal tract impulse response, \( v(t) \). For voiced sounds \( x(t) \) is quasiperiodic hence the output \( y(t) \) is also quasiperiodic. For the unvoiced case the excitation \( x(t) \) is random and is generally approximated by white noise.

If the vocal tract impulse response of an individual could be obtained, then using the time varying linear system model intelligible speech should be able to be generated. The excitation would either be periodic or random depending on whether voiced or unvoiced sounds are
desired. Figure 1.2 is a simplified speech synthesis machine where the vocal tract parameters are stored in the RAM and downloaded to the voice synthesis chip which is excited by either the periodic or the random signal. This

![Diagram of voice synthesis machine](image)

Figure 1.2. Voice Synthesis

type of speech synthesis arrangement is the basis for Texas Instruments' (TI) Speak and Spell toys. TI can custom manufacture a speech synthesis chip which will emulate anyone's voice for $15,000.
These voiced and unvoiced sounds are combined in a unique fashion to form phonemes, the basic building blocks of language. All languages can be reduced to a finite number of these distinguishable building blocks. Phonemes are of such fundamental importance that if one phoneme is exchanged for another the meaning of an utterance is completely altered.

Thus, in theory, if a machine could be designed to disassemble utterances into their phoneme components the speech recognition problem would be completely solved. Despite vast amounts of time, effort, and money expended, however, the phoneme disassembler is years away from becoming an appears to be reality.

B. SPEECH RECOGNITION MACHINES

While the phoneme disassembler does not exist, several types of speech recognition systems are commercially available. The majority of these systems are classified as isolated word recognizers. As the name implies the systems are designed to recognize isolated words. The vocabulary of these machines is usually limited to 100-300 words and these systems are extremely speaker dependent. Thus, a person desiring to use these machines must first train the machine to recognize his voice. During the training phase the speaker's utterances are processed and templates formed. The recognition process involves comparing the incoming
utterance with those templates stored in the machine's memory [Ref. 3]. Although these machines have a limited vocabulary and cannot recognize connected or conversational speech, they are extremely useful for inventory control, quality assurance control, or for a pilot to check the systems in a combat aircraft. In all these instances the vocabulary is limited, the speaker is known, and voice data entry frees the individual to perform other tasks.

ITT has developed a word recognition system for the Air Force's F-16 fighter. The system is capable of recognizing 300 words and allows the pilot to check the status of certain systems while he maintains two-hand control of the plane. This two-hand control is particularly important during low level, high speed attack runs. The pilots update their voice patterns monthly or if their voice changes due, say, to a cold. The patterns are stored in a bubble memory and inserted into the system prior to take-off. The microphone is located inside the pilot's oxygen mask and the system status is displayed on the cockpit's CRT. At a recent demonstration of this system it had a correct recognition rate of 99%.

The NPS Speech Processing Laboratory acquired an isolated word recognition system for experimentation purposes. The system is the VRM Voterm-2 manufactured by Interstate Electronics Corporation. The system, acquired in 1981,
weighs 10 lbs. and cost $2500. Today the same system has been reduced to a four chip set, for a cost of $1000.

The operation of the VRM is typical of the word recognition systems currently available [Ref. 4]. It allows the user to select the vocabulary size, decision threshold and number of training passes. It also allows for reference pattern transfer between itself and the host computer. The host computer serves only as a mass storage device and controller. All processing and recognition is performed real-time by the VRM.

The input speech signal is analyzed by a 16-filter analog spectrum analyzer and then passed through an A/D converter. This digitized speech data is then converted to a fixed-size (120 bit) pattern that preserves the information content of the utterance. During the training phase the VRM rejects utterances that do not sufficiently agree with previous training samples of the word. This rejection leads to a reduction of the number of 'ones' stored in the pattern. After seven training passes the pattern contains approximately one hundred 'zeroes'.

In 1980, NATO and the Rome Air Development Center (RADC) [Ref. 5] conducted a comparison test on three isolated word recognition systems. The vocabulary used consisted of the ten single digits of the respective languages of the speakers. The machines evaluated were the VRM system, the
Threshold Technology 8040 Preprocessor (cost $50,000) and the Nippon Electric DP-100 (cost $60,000).

Table 1.1 lists the results from the RADC test [Ref. 6]. Each speaker trained the machines by repeating each digit ten times. No attempt was made to introduce speakers who had not trained the machine. However, tests run at the Speech Processing Lab with the VRM with some non-trained speakers, using the ten digits and three sets of reference patterns the successful recognition rate for new speakers was less than 30%.

Thus, these systems work extremely well for what they were designed to accomplish. As previously stated, the basic question of what parameters of speech are speaker independent still remains unanswered. Numerous theories have been proposed and all have been unsuccessful. There is a lack of understanding of the human mechanisms used in understanding speech.
<table>
<thead>
<tr>
<th>Language Spoken</th>
<th>Native or Non-Native</th>
<th>#Speakers</th>
<th>VRM Rec%</th>
<th>Thresh Rec%</th>
<th>VRM Thresh #Utters</th>
<th>NEC Rec%</th>
<th>NEC #Utters</th>
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<td>Native</td>
<td>8</td>
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<td>5400</td>
<td>99.64</td>
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<tr>
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<td>100.00</td>
<td>3000</td>
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<td>1200</td>
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<td>5400</td>
<td>99.97</td>
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<td>99.86</td>
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<tr>
<td>All/Female</td>
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<td>96.60</td>
<td>98.70</td>
<td>3000</td>
<td>99.65</td>
<td>2000</td>
</tr>
</tbody>
</table>
II. MODELS OF THE EAR

For a long time people have been trying to understand how the human ear functions. In the first century B.C., the Roman poet, philosopher Lucretius postulated a model "involving little grains of sand in the inner ear responding too different tones" [Ref. 7]. The 18th century Italian violinist Tartini noted that the ear produced a third tone from two tones played simultaneously. Thus the long held belief that the ear was a linear device was demonstrated to be false. Today the ear is thought to be a nonlinear device even at power levels near the threshold of hearing.

The first concentrated research into the process of hearing did not begin until the mid-1800's. This was the time of Seebeck, Helmholtz, and Ohm. It was Ohm who postulated a now famous law on the relationship of speech and its phase angle. He stated that all the information content of speech is contained in its power spectrum and was independent of the phase angle of the components. Although Ohm's law has been modified in recent years, it remains as one of the fundamental laws of psychoacoustics.

The ear can be broken down into three physical areas; the outer, middle and inner ear. Sound waves impinge on the outer ear and are conducted down a canal until they reach
the middle ear. The middle ear contains three tiny bones. The alternate compressions and refractions of the speech wave cause the eardrum to strike the bones. In the inner ear the wave travels along a thin membrane whose frequency response varies between 100 Hz and 20 KHz. This provides for spectral analysis of the incoming signal.

The membrane of the inner ear is lined with tiny hairs. It is these hairs or more correctly groups of hairs that perform the spectral analysis. Recent studies at the California Institute of Technology [Ref. 8] have found that each tiny hair bundle consists of 30-150 thin, rod-shaped extensions called cilia. These hair bundles are attached to hair cells. The hair cells are very sensitive transducers which convert the movement of the hair bundle into an electrical signal which is sent to the brain. The hair bundle-hair cell combination form a sort of mechanical spectrum analyzer.

Manfred Schroeder [Ref. 9] describes an experiment in which the inner ear's sensitivity to phase was demonstrated. The experiment was as follows:

1) A 100 sec. sample of speech was Fourier transformed.

2) Random phase angles were assigned to the frequency components (assuming a uniform distribution 0 to 2π).

3) The inverse Fourier transform was taken.

The resultant signal sounded like white noise. Thus by randomizing the phase angles the signal was transformed from
intelligent speech to noise. This lent credence to the hypothesis that the inner ear was phase sensitive and that Ohm's law, if not wrong, was at least in need of modification. The experiment was repeated this time using a 50 msec. sample of speech. The resultant signal was non-intelligible noise. Ohm's law modified to say that only the short term amplitude spectrum contained the speech information appeared to be correct.

Ohm based his law on a model of the ear that said:

1) The ear has a tuned bandpass filter covering the audio range.
2) Only the output amplitude of each filter is sent to the brain.

Today the most likely candidate for the bandpass filter are the hair bundle-hair cell combinations that respond to only selected stimuli.

In 1947 an experiment was conducted [Ref. 10] in an effort to obtain a definite answer to the phase sensitive question. An AM signal at 2000 Hz was modulated by a 100 Hz signal. Thus three frequency components (1900 Hz, 2000 Hz, 2100 Hz) were present. One of the sidebands had its phase shifted by $180^\circ$. This phase shift resulted in what was termed a quasi-FM (QFM) signal. Upon listening to the signals there was a noticeable difference between the AM and QFM signal. Thus there was a revived interest in the ear's
capability to discern waveforms and not just their amplitude.

In a further effort to determine to what extent phase is important in discerning speech, Hall and Schroder [Ref. 11] conducted an experiment where the phase angle of one of two pure tones was changed. Specifically two tones one at 200 Hz and 0° and another at 400 Hz but with phase angles of 0°, 60°, 120°, 180°, 240°, and 300° were listened to, three signals at a time. The listeners' task was to determine which two signals sounded most alike and which two sounded least alike. The results showed that those harmonics of 400 Hz whose phase angle differed the least were judged to be the most similar consistently.

About twelve years prior to this experiment researchers at Bell Labs postulated that the phase dependency seen in experiments involving the inner ear could be traced to the phase dependence of the inner and middle ear distortion products. Due to the presence of these nonlinear distortion products a new spectrum, called the inner spectrum was formed in the inner ear. It is this spectrum that is analyzed by the hair bundles of the inner ear.

This theory certainly would explain what happened at Bell Labs during a 1958 experiment [Ref. 12]. When the phase of one of 31-equal amplitude harmonics all 0° phase was changed to a 180° a pure tone was heard. This tone was
not heard when the signal was put through a loud speaker. Thus using the inner spectrum theory changing the phase of one harmonic to 180° altered the amplitude of one of the distortion products. This altered the inner spectrum causing a bump in the spectrum where previously it had been flat.

In Germany, Terhardt and Fastl [Ref. 13] conducted experiments trying to connect frequency difference and phase angles. They formed a signal \( s(t) = a_1 \cos(2\pi f_1 t) + a_2 \cos(2\pi f_2 t - \phi_2) \) where \( f_1 = 200 \text{ Hz} \), \( f_2 = 400 \text{ Hz} \) and asked listeners to adjust the amplitude of each component so the 400 Hz tone was just audible. This was to be done while the phase angle, \( \phi_2 \), of the 400 Hz tone was changed. The results showed that when \( \phi_2 \) was changed from 0° to 180°, the amplitude of the 400 Hz signal had to be increased by 12 dB to remain audible.

Yet another theory on the functioning of the ear came out of this experiment. The researchers theorized that the hair cells of the ear were discerning the time between successive spikes in the waveform and passed this information to the brain. This appeared as a reasonable explanation as when \( \phi_2 = 0° \) the time between successive spikes was 2.5 msec. With \( \phi_2 = 180° \) the time between spikes was 5 msec., unless the amplitude of the 400 Hz tone was increased by considerable
amount. With the amplitude increased the small spikes at the 2.5 msec. mark would increase dramatically.

This theory is consistent with the physiology of the ear. All the electric pulses transmitted to the brain from the hair cells have approximately the same amplitude, thus the timing between the pulses is the information that they carry.

From the myriad of theories presented it is easy to conclude that a definitive model of the human ear is non-existent. The fact that phase contains some information content has been demonstrated. Whether phase alone is the speaker independent feature that researchers are looking for remains an unanswered question. Experiments conducted in the late 1970's and 1980's using phase-only representations of speech have given some creditability to the hypothesis that phase must be included as one of the speaker independent features of speech.
III. PHASE-ONLY REPRESENTATIONS OF SPEECH

Recapitulating, Ohm's law stated that all the information content of speech could be obtained from the short term power spectrum and that phase angle of the components was meaningless. Thus, in the short term the ear is phase deaf. Oppenheim [Ref. 14] sought to explore more fully the importance of phase in speech.

Given the Fourier transform of a speech signal

\[ F(\omega) = |F(\omega)| e^{j\theta(\omega)} \]  

(3.1)

and if the \(|F(\omega)|\) is set equal to one, the inverse transform of \(e^{j\theta(\omega)}\) is a phase only representation of the speech. This phase only representation retained total intelligibility, while exhibiting the characteristics of being high passed filtered and having white noise added. The magnitude only representation was speech-like in its appearance but was not intelligible.

Oppenheim concluded that transforming a signal to its phase only form was equivalent to passing it through a spectral whitening process with a filter whose response is \(H(x) = 1/|F(x)|\), where \(F(x)\) is the Fourier transform of the original signal. This spectral whitening did not destroy the intelligibility of the speech.

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Contrary to Ohm's law, Cox and Robinson [Ref. 15] conducted a series of four experiments which preserve the short term phase of a speech signal while either destroying or severely distorting the amplitude. These phase-only signals were found to retain many speech characteristics and were intelligible to the listeners. Hence under certain transformations short term phase may be one of the physical invariants of speech.

The experiments used a speech signal that was analog band limited to 8 KHz and sampled at a rate of 20 KHz with 12 bits A/D. Successive 25.6 msec windows, corresponding to 512 data points, were fast Fourier transformed. Nonlinear operations were applied to each data set, and the inverse fast Fourier transforms were taken yielding 25.6 msec of reconstructed speech signal. These signals were D/A converted at a rate of 20 KHz and passed through a 8 KHz low pass analog filter. Only rectangular windows were used and no attempt was made to fit the windows together since amplitude of the reconstructed signal was unimportant. The first two experiments are included for completeness only. The latter two are the concern of this thesis.

A. SHORT-TERM PHASE ONLY SIGNALS

This experiment basically repeated the previously mentioned work of Oppenheim, as the magnitude of the Fourier transform of the data sets was set equal to one. The phase
was unchanged. The reconstructed short-term phase only signal was found to retain many of the original waveform's features. Listeners could identify speaker dependent characteristics and the intelligibility, while not judged good, was likened to a signal containing a lot of noise. There was no attempt made by the researchers to clean up the signal. The results of this experiment clearly are contrary to Ohm's law and demonstrate that short-term phase only speech is intelligible.

B. ANALYTIC SIGNAL PROCESSING

The second experiment was a repeat of one carried out in the late 1940's. Here the representation is an infinitely clipped version of the original signal

\[ sc(t) := \text{Sgn} \{s(t)\} \]  

(3.2)

where \( s(t) \) is the original signal, and \( \text{Sgn} \) is defined to be the sign of \( s(t) \). Thus the continuous valued signal, \( s(t) \), was transformed into a discrete valued signal. The transformation retains only the real-zero information of \( s(t) \). That is, if \( s(t) \) was an analytic signal the real-zeros mark the time when the phase was changed by \( 180^\circ \). The intelligibility of such a signal was not commented on by the experimenters, however, they did say that large amounts of speech information were retained using this transform.

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C. DIRECT PHASE CEPSTRUM

The concept of cepstral analysis of speech was developed by Oppenheim [Ref. 16] and is an example of a broad class of nonlinear processing called homomorphic processing. These homomorphic systems obey generalized laws of superposition. If \( x_1(n) \) and \( x_2(n) \) are inputs to a homomorphic system and \( y_1(n), y_2(n) \) are corresponding outputs and \( k \) is any scalar then

\[
\begin{align*}
y_1(n) &= \#[x_1(n)] \\
y_2(n) &= \#[x_2(n)] \\
\#[x_1(n) \triangle x_2(n)] &= \#[x_1(n)] \square \#[x_2(n)] \\
\#[k \odot x_1(n)] &= k \ast y_1(n)
\end{align*}
\]

where \( \triangle, \square, \odot, \) and \( \ast \) are mathematical operations.

The importance of these homomorphic systems is that \( \# \) can be broken down into a cascade of operations as shown in Figure 3.1 where \( A_0, A_0^{-1} \) are inverses of each other and \( L \) is a simple linear filter.

Thus Oppenheim [Ref. 17] formulated a model for the production of speech as shown in Figure 3.2. The model is based on the assumption that the excitation and vocal tract parameters are independent. The source of excitation for the voiced sounds is the impulse generator whose period is
Figure 3.1. Homomorphic System

Pitch Period

Impulse Generator

Random Number Generator

Time Varying Digital Filter

Digital Filter Coefficient

Amplitude

Speech Samples

Figure 3.2. Model for Speech Production
controlled by the pitch-period signal. The impulse
generator produces an impulse once every \( N_0 \) samples, where
\( N_0 \) is the pitch-period and \( 1/N_0 \) is the pitch frequency. The
unvoiced excitation is from the random number generator and
simulates both fricative and plosive sounds. The digital
filter is assumed to be slowly varying with time and hence
changes its coefficients once every 10 msec. The amplitude
control simply adjusts the output level of the speech.

Using this model the output digitized speech waveform
consists of the convolution of

1. The train of impulses representing the pitch
2. The excitation pulse
3. The vocal tract impulse response.

If \( x(n) \) denotes the output signal, then

\[
x(n) = [p(n) \ast e(n) \ast u(n)] w(n)
\]  \hspace{1cm} (3.3)

where \( p(n) \) is the train of pitch pulses, \( e(n) \) is the
excitation pulse, \( u(n) \) the vocal tract impulse response, and
\( w(n) \) the window through which the speech is viewed. The
window \( w(n) \) is smooth, hence we can define

\[
\hat{p}(n) = p(n) w(n)
\]  \hspace{1cm} (3.4)
Then substituting this into equation (3.3) it is possible to approximate \( x(n) \) by

\[
x(n) = \hat{p}(n) \ast e(n) \ast u(n)
\]  

(3.5)

Examining equation (3.5) it is possible to convert the triple convolution into a triple sum by first taking the Fourier transform and then taking the logarithm. Processing of this signal can be accomplished by a linear system and recovery of the waveform can be made by passing the processed signal through an exponentator followed by inverse Fourier transformer. Thus a homomorphic system for processing speech has been developed, as shown in Figure 3.3 [Ref. 18].

![Homomorphic System for Processing Speech](image)

Figure 3.3. Homomorphic System for Processing Speech

Variations on this basic system have been developed to estimate parameters of both the vocal tract transmission
functions and the excitation functions. One of these variations involves making the assumption that the excitation is \( s(n) = \hat{p}(n) * e(n) \), then equation (3.5) can be written as

\[
x(n) = u(n) * s(n)
\]  

(3.6)

The system to process signals given by equation (3.6) is shown in Figure 3.4 [Ref. 19].

Referring to Figure 3.4, the signal at A is \( x(n) \) and the signal at D is called the cepstrum of \( x(n) \) and equals the cepstra of the excitation plus the cepstra of the vocal tract impulse response.

![Figure 3.4. Cepstral Processing of Speech](image)

An important feature of the cepstrum at D is that it separates the excitation from the vocal tract response. The excitation is a sequence of quasi-periodic pulses, thus its
Fourier transform, at point B, is a line spectra where the lines are spaced at harmonics of the fundamental frequency. The log magnitude operation does not effect the general shape of the spectra. The IDFT of the signal produces another quasi-periodic waveform with pulses spaced at the fundamental period. Thus the cepstrum of the excitation should consist of pulses around $n = 0, T, 2T, \ldots$, where $T$ is the pitch period.

The DFT of the vocal tract response is a slowly varying function of frequency. The log magnitude and IDFT yield a sequence that is negligible after a few samples. The cepstrum at D consists of two sequences, one which is negligible after a few samples and one that is periodic. Thus the cepstrum at D does differentiate the excitation from the vocal tract parameters. The use of the cepstral processing has been extended into many diverse fields [Ref. 20].

For their third experiment, Cox and Robinson [Ref. 21] modified Figure 3.4 by setting the magnitude of the signal at point C equal to one. Hence the cepstrum at point D is due only to the phase of the signal at A. What amount of information and intelligibility does this phase only cepstrum contain? Surprisingly the cepstrum was judged to be very intelligible by listeners and the noise level was reduced when compared with the short-term phase only speech (experiment number one).
D. INSTANTANEOUS PHASE OF THE ANALYTIC SIGNAL

The fourth experiment performed by Cox and Robinson [Ref. 22] was first performed in 1955 by Marcoui and Daguet who were looking for more efficient modulation techniques. They sought to use the analytic signal representation of a real signal $s(t)$. Given a real signal $s(t)$, which is Hilbert transformable, form a quadrature signal $s^*(t)$ and construct

$$m(t) = s(t) + j s^*(t)$$  \hspace{1cm} (3.7)

From equation (3.7) it is possible to recover the original signal as

$$s(t) = \text{RE}[m(t)] = |m(t)| \cos \theta(t)$$  \hspace{1cm} (3.8)

Equation 3.8 lets the real signal, $s(t)$, be represented by a magnitude and phase.

The concept of an analytic signal, which equation (3.7) is called, was meaningless for discrete-time signals, until Rabiner and Schafer [Ref. 23] developed a complex representation for real discrete-time bandpass signals.

Following the notation of Rabiner and Schafer, given a real sequence, $x(n)$, with Fourier transform $X(w)$, construct a complex sequence
\[ x(n) = x(n) + j \hat{x}(n) \]  \hspace{1cm} (3.9)

The Fourier transform of which is

\[ \tilde{X}(\omega) = 2X(\omega) \hspace{1cm} 0 \leq \omega < \pi \]  \hspace{1cm} (3.10)

\[ = 0 \hspace{1cm} \pi \leq \omega < 2\pi \]

From equation (3.9) the Fourier transform of \( x(n) \) is

\[ \tilde{X}(\omega) = X(\omega) + j \hat{X}(\omega) \]  \hspace{1cm} (3.11)

and from equation (3.10) it follows that

\[ X(\omega) + j \hat{X}(\omega) = 0 \hspace{1cm} \pi \leq \omega < 2\pi \]

and

\[ \tilde{X}(\omega) = 2X(\omega) \hspace{1cm} 0 \leq \omega < \pi \]

These requirements are satisfied if

\[ \hat{X}(\omega) = H_d(\omega) X(\omega) \]  \hspace{1cm} (3.12)

where

\[ H_d(\omega) = -j \hspace{1cm} 0 \leq \omega < \pi \]

\[ = + j \hspace{1cm} \pi \leq \omega < 2\pi \]  \hspace{1cm} (3.13)
Thus given any sequence $x(n)$, it is possible to obtain the sequence $\hat{x}(n)$ by linear filtering of $x(n)$ with a filter whose frequency response is given by equation (3.13). Such a filter is called an ideal Hilbert transformer and $\hat{x}(n)$ is the Hilbert transform of $x(n)$. The impulse response of the ideal Hilbert transformer is

$$h_d(n) = \frac{2}{\pi} \frac{\sin^2 \left( \frac{\pi n}{2} \right)}{n} \quad n \neq 0 \quad (3.14)$$

$$= 0 \quad n = 0$$

Examining equation (3.14), the impulse response is non-causal, of infinite duration, has odd symmetry, and all even-numbered samples are equal to zero (i.e., $h_d(2n) = 0$, $n = 0, \pm 1, \pm 2, \pm 3, \ldots$).

Since infinite length, non-causal impulse responses are not realizable an FIR approximation is required. Given a causal FIR system whose impulse response is $h(n)$, $0 \leq n \leq N-1$, its frequency response is given by

$$H(\omega) = \sum_{n=0}^{N-1} h(n)e^{-j\omega n} \quad (3.15)$$

Equation (3.13) says the desired frequency response, $H_d(\omega)$, is purely imaginary. Thus the real part of equation (3.15) must equal zero as $h(n)$ is real. In order for the real part of equation (3.15) to be zero $h(n)$ must satisfy the symmetry condition
If \( N \) is odd, \( h(n) \) has odd symmetry about \( n = (N-1)/2 \). If \( N \) is even, \( h(n) \) has odd symmetry about a point halfway between the samples at \( n = N/2 \) and \( n = (N/2) + 1 \). If equation (3.16) is satisfied, equation (3.15) can be written as

\[
H(\omega) = e^{-j\omega(N-1)/2} [jH^*(\omega)]
\]  

(3.17)

where \( H^*(\omega) \) is a real function of \( \omega \). If \( N \) is odd, \( H^*(\omega) \) can be written as

\[
H^*(\omega) = \sum_{n=1}^{(N-1)/2} a(n) \sin(\omega n)
\]  

(3.18)

where \( a(n) = 2h(\frac{N-1}{2} - n), n = 1, 2, ..., (\frac{N-1}{2}) \)  

(3.19)

Also for \( N \) odd,

\[
h(\frac{N-1}{2}) = 0
\]  

(3.20)

For \( N \) even, equation (3.18) becomes

\[
H^*(\omega) = \sum_{n=1}^{N/2} b(n) \sin[\omega(n - 1/2)]
\]  

(3.21)

where \( b(n) = 2h(\frac{N}{2} - n), n = 1, ..., N/2 \)
Examining equation (3.17) more closely, we find that the factor $e^{-j\omega(N-1)/2}$ is a delay of $(N-1)/2$ samples.

In finding an approximation to the ideal Hilbert transform, coefficients $a(n)$ and $b(n)$ were chosen in such a fashion that $jH^*(\omega)$ approximates the ideal frequency response given by equation (3.13). Thus $H^*(\omega)$ must approximate

$$D(\omega) = -1 \quad 2\pi F_L \leq \omega \leq 2\pi F_H$$

$$= +1 \quad 2\pi (1 - F_H) \leq \omega \leq 2\pi F_L$$

where $F_L$ and $F_H$ are the lower and upper cutoff frequencies represented as fractions of $2\pi$. From equation (3.18), $H^*(\omega)$ must equal zero at $\omega = 0$ and $\omega = \pi$ when $N$ is odd and must equal zero at $\omega = 0$ for the case when $N$ is even.

For the ideal transformer the impulse response was zero for all even numbered samples and the frequency response was imaginary, odd, periodic and

$$H_d(\omega) = H_d(\pi - \omega).$$

For the FIR approximation similar properties must be valid. If $N$ is odd and $F_L = 0.5 - F_H$ and assuming that

$$H^*(\omega) = H^*(\pi - \omega).$$

Then substituting into equation (3.18) yields,
\[
\sum_{n=1}^{(N-1)/2} a(n) \sin(n\omega) = \sum_{n=1}^{(N-1)/2} a(n) \sin[(\pi - \omega)n]
\]

\[
= \sum_{n=1}^{(N-1)/2} a(n) (-1)^{n+1} \sin(\omega n)
\]

rearranging terms

\[
\sum_{n=1}^{(N-1)/2} a(n) \sin[\omega n(1 - (-1)^{n+1})] = 0
\]

Thus \( a(n) = 0 \) \( n \) even

= unconstrained \( n \) odd.

Combining this result with equations (3.16), (3.19), and (3.20) have that for \((N-1)/2\) even, \( h(n) = 0 \), for \( n = 0, 2, \ldots \) and when \((N-1)/2\) is odd, \( h(n) = 0 \), for \( n = 1, 3, 5, \ldots \).

For the case of \( N \) even no relationship among the coefficients exist.

One important difference between even and odd length impulse responses can be seen in direct convolution. The convolution summation given by

\[
\hat{x}(n) = \sum_{k=0}^{N-1} h(k) x(n-k)
\]

involves only \((N+1)/4\) multiples per output sample for \( N \) odd and \( N/2 \) multiples for \( N \) even. The saving occurs because
alternate values of $h(n)$ are zero for $N$ odd. Because of this savings and for technical considerations only Hilbert transformers of odd length are used.

In determining the values of $h(n)$, Rabiner and Schafer [Ref. 24] used the Remez algorithm for the design of optimal FIR filters. The values of $h(n)$ were calculated to minimize the peak approximation error which is given by

$$G = \text{MAX} \ [D(\omega) - H^*(\omega)]$$

(3.24)

$$2\pi F_L \leq \omega \leq 2\pi F_H$$

The Remex algorithm gives a Chebyshev or equiripple approximation to the desired response. Hence the error function is equiripple over the range $2\pi F_L \leq \omega \leq 2\pi F_H$. Given an $N$, $F_L$ and $F_H$ the resulting approximation is best in the minimax sense.

Using this concept of an analytic signal representation for discrete-time signals, Cox and Robinson [Ref. 25] formed the analytic phase representation of a speech signal. Given a sampled speech signal, $s(n)$, they calculated the Hilbert transform, $s^*(n)$, by the use of a 79-weight Hilbert transformer. Thus having the analytic signal

$$m(n) = s(n) + j s^*(n)$$
the original signal $s(n)$ is given by

$$s(n) = |m(n)| \cos \theta(n).$$

The analytic phase representation is given by $\cos \theta(n)$. Thus by way of a mathematical artifice a real-valued sequence $s(n)$ is represented as having magnitude and phase with the phase only being retained. Contrary to common sense, perhaps, this analytic phase representation of speech was found to be intelligible. While these experiments by themselves do not prove that phase is a physical invariant of speech, they do indicate that more research is needed to determine to what role phase plays in speech intelligibility.

As was mentioned, a 79-weight Hilbert transformer was used in obtaining the analytic signal. Rabiner and Schafer [Ref. 26] calculated weights for three different values of peak approximation errors and cutoff frequencies. Table 3.1 lists these weights and Figures 3.5 through 3.7 are plots of the magnitude of the frequency response. Table 3.1 only lists even weights, since 79 is odd, all odd weights are zero and the weights have odd symmetry about $n = 39$. 
**TABLE 3.1**

**HILBERT TRANSFORMER WEIGHTS**

<table>
<thead>
<tr>
<th>$n$</th>
<th>$F_L = .01$</th>
<th>$F_L = .02$</th>
<th>$F_L = .05$</th>
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<td>-.6362830</td>
<td>-.6357869</td>
<td>-.6343000</td>
</tr>
</tbody>
</table>
Figure 3.5. Frequency Response of Hilbert Transformer
N = 79, $F_L = .01$, $G = .0388830$
Figure 3.6. Frequency Response of Hilbert Transformer
N = 79, $F_L = .02$, $G = .0024390$
Figure 3.7. Frequency Response of Hilbert Transformer
N = 79, F_L = .05, G = .0000010
IV. EXPERIMENTAL PROCEDURE

This thesis extends the work of Cox and Robinson to the isolated word recognition field. Specifically using the homomorphic and analytic signal processing techniques employed in experiments three and four an isolated word recognition system is developed.

A. DATA ACQUISITION

In order to form a data base for use by the system twenty volunteers were recruited to record the digits zero through nine. Each participant was given a questionnaire/instruction sheet like that contained in Appendix A. All speakers were males between the ages of 25 and 35 and all were native English speakers. Their places of birth varied from eastern Pennsylvania to southern Tennessee. Ten of these speakers were selected to form the data base or pattern base of the system. The other ten speakers were used to test the system.

The speech was recorded on an analog tape recorder with all recordings being done in the Speech Processing Laboratory. The recordings were done in the late afternoon or in the evening when the ambient noise level was at a minimum. The tape recorder used was the HP-3964A reel-to-reel instrumentation recorder running at 7.5 ips using AMPEX professional audio tape.
Before this analog speech could be digitized an appropriate bandwidth and sampling rate had to be determined. The power spectral density of each digit was computed and averaged over ten utterances of the digit. The majority of the power was found to be below 3 KHz except in the case of the number 'six' where nonnegligible power was found to frequencies up to 6 KHz. A cutoff frequency of 4 KHz was chosen, which is exactly half the bandwidth that Cox and Robinson used. As will be explained later, once the bandwidth is fixed the sampling rate is also fixed. In this case the sampling rate is fixed at 10 KHz.

The machine used to digitize the speech was the GENRAD 2505 Signal Analysis System [Ref. 27]. The system is a narrowband (0 - 25 KHz) signal analysis system originally designed for vibrational analysis studies. The system uses a DEC PDP 11/34A as the host computer and supports two channels of A/D conversion.

The heart of the system, softwarewise, is GENRAD's Time Series Language (TSL) which allows the operator to control the A/D converter. TSL is an interpretive language which uses commands similar to BASIC. The TSL program 'ANADSK' is the routine that provides analog input to disk storage. Given a bandwidth the 'ANADSK' routine sets the sampling rate at 2.56 times the highest frequency component to prevent aliasing. The system provides for high-speed
continuous sampling and writes the digitized data to the system's Winchester disks in 2048 byte blocks.

The two-channel A/D converter has two 6-pole Chebychev filters in cascade each with 96 dB/octave rolloff above cutoff per channel as anti-aliasing filters. The A/D converter is a 2 µsec converter with a 12 bit output.

Once the speech was digitized a time window for the sampled data had to be determined. Referring again to the utterances whose power spectral densities were computed, the average length of the utterances was 740 msec. In order for the mathematics to work out nicely a 750-msec window was chosen.

Using TSL library routines 'RTIO' and 'XDISPL' a routine was written that displayed the digitized data on the system's CRT. The program graphically displayed 1024 samples at a time and allowed the operator to select any 256 samples for transfer to the W. R. Church Computer Center's IBM 3033 for processing. This transfer was via a 1200 baud modem. With the capability to view the data prior to transfer, the start of the utterance could be selected to within 128 samples. Since the time window was selected to be 750 msec and the speech was sampled at 10,240 samples/sec, 7680 points needed to be transferred. Thus thirty blocks of 256 samples each were transferred per utterance.
The transfer/interface program between the Speech Lab's PDP 11/34A and the IBM 3033 was written by LT Jay H. Benson. A copy of his program, 'CATCH', is included in Appendix B. The transfer of data via the modem was very time consuming as for technical reasons each sample which occupied two bytes on the PDP 11/34A was made into a four byte number for transfer. The sixteen most significant bits were then masked off prior to storage on the IBM system. In order to minimize the amount of disk storage required, the data was written to the disk using an unformatted FORTRAN write statement, using Integer * 2 numbers. Even using this scheme to maximize storage efficiency 24 cylinders plus magnetic tape backup were required to store the data.

B. DATA PROCESSING

The decision to use the IBM system to process the data was based on the availability of library routines (e.g., IMSL, NONIMSL), the DISSPLA graphics package, and the full screen text editor. All programs in Appendix B were written in FORTRAN H.

The first task was to compute an average waveform for the speaker. In order to accomplish this, three of the four utterances of each of 10 speakers were averaged together. The program 'MEANS' was used to compute this average. The technique is very simple and straightforward as the ensemble mean was computed. This agrees with the
work done by the Air Force [Ref. 28] where they assumed that
the samples are statistically independent, identically
distributed Gaussian random variables. This is an over
simplification as it is known that the vocal tract is slowly
varying with the tract parameters changing only every 10
msec.

The short-term cepstral representation of the averaged
waveform was computed using the program 'CEP'. In keeping
with Cox and Robinson the waveform was segmented into
25 msec parts and each part was processed in sequence.

Finally the analytic signal representation of the
waveform was computed using a FIR Hilbert transformer with
79 weights, and a lower cutoff frequency of .05. The
frequency response of this filter is shown in Figure 3.3.
This particular filter was chosen over the other two 79
weight filters because of its very small approximation
error. The small approximation error does imply that the
transition band of this filter is larger than the other two
filters, however, this was deemed less important than the
peak approximation error.

Examples of these three representations of the same
utterances can be found in Figures 4.1 thru 4.30. These
examples are of a male 30 years old, born and raised in
eastern Pennsylvania, and a Naval cryptologic officer. In
order to display all 7680 points on one graph the waveform
was first normalized, then divided into four 1920 point parts. Each part was biased by \((N-1) \times 2\), where \(N = 1, 2, 3, 4\), to permit graphing by the four segments on one page. The graphs should be read from left to right, top to bottom.

C. DECISION ALGORITHM

Once the speech had been processed a decision algorithm had to be formulated to classify utterances based on the patterns collected. All of the isolated word recognizers use a form of classical pattern recognition to classify utterances. The VRM system uses a nearest neighbor algorithm with a variable threshold. If no utterance is within the distance specified by the threshold, an unable to classify message is issued.

The nearest neighbor rule is an example of the pooled form of the nearest neighbor rule [Ref. 29]. For the two class case, a hemisphere is formed around the vector \(y\) to include \(k\) total samples regardless of their class. Thus \(k_1 + k_2 = k\), where \(k_i\) equals the number of vectors belonging to class \(i\). The quotient \(k_1/k_2\) is formed and compared to one. If \(k_1/k_2 > 1\), then this implies there are more class one vectors in the hemisphere around \(y\) and the vector \(y\) is said to belong to class one. If the converse of the inequality is true, \(k_1/k_2 < 1\), then \(y\) is said to belong to class two. The probability of error for the case \(k=1\) is less than twice the minimum probability of error for any decision rule.
The nearest neighbor rule was employed to classify the utterances. Using the program 'DEC', the Euclidean distance between a test vector and the stored patterns was computed. The results of this pattern matching are discussed in the next chapter.
Figure 4.1. Sampled Waveform, Zero
Figure 4.2. Analytic Representation of Zero
Figure 4.3. Cepstral Representation of Zero
Figure 4.4. Sampled Waveform, One
Figure 4.5. Analytic Representation of One
Figure 4.6. Cepstral Representation of One
Figure 4.7. Sampled Waveform, Two
Figure 4.8. Analytic Representation of Two
Figure 4.9. Cepstral Representation of Two
Figure 4.10. Sampled Waveform, Three
Figure 4.11. Analytic Representation of Three
Figure 4.12. Cepstral Representation of Three
Figure 4.13. Sampled Waveform, Four
Figure 4.14. Analytic Representation of Four
Figure 4.15. Cepstral Representation of Four
Figure 4.16. Sampled Waveform, Five
Figure 4.17. Analytic Representation of Five
Figure 4.18. Cepstral Representation of Five
Figure 4.19. Sampled Waveform, Six
Figure 4.20. Analytic Representation of Six
Figure 4.21. Cepstral Representation of Six
Figure 4.22. Sampled Waveform, Seven
Figure 4.23. Analytic Representation of Seven
Figure 4.24. Cepstral Representation of Seven
Figure 4.25. Sampled Waveform, Eight
Figure 4.26. Analytic Representation of Eight
Figure 4.27. Cepstral Representation of Eight
Figure 4.28. Sampled Waveform, Nine
Figure 4.29. Analytic Representation of Nine
Figure 4.30. Cepstral Representation of Nine
V. RESULTS AND CONCLUSIONS

Ten speakers were selected to form the data base for the system. Their utterances were processed to obtain both their cepstral and analytic phase representations. The system was then tested using two groups of speakers. The first group, denoted Group A, consisted of speakers whose utterances were used to form the data base. Each speaker repeated the digits four times, and only three of these utterances were used to compute the average waveform and hence the cepstral and analytic phase representations. Group A can be thought of as having trained the system. The second group, Group B, consists of the other ten speakers.

The system was tested using ten utterances per digit from each of the two groups of speakers. The reference pattern space was varied, using three different spaces each containing 100 patterns. The cepstral and analytic representations formed two of the reference spaces, while the unprocessed signals formed the third space. Tables 5.1 and 5.2 contain the results of the test.

The results for Group A, in all categories, are below the results attainable with the VRM system. For three training passes the VRM system has a 97% recognition rate. The high percentage of recognition for the unprocessed
waveforms was to be expected since the speakers trained the system and the pattern space did consist of the average of each speaker's utterances. The distances between the pattern vectors and the test vector were of the same magnitude for the unprocessed waveforms, regardless of whether the utterance was correctly identified or not. In the case of the short-term phase representations when the system correctly identified an utterance, the distance between the test vector and its nearest neighbor was an order of magnitude less than all the other distances. When the system incorrectly identified an utterance all distances were of the same magnitude.

The success demonstrated in the speaker-dependent case is not without cost. As compared to the VRM system, which has at most 120 bits/pattern, this system has 122.8K bits/pattern (7680 two byte numbers). There was an extensive amount of manual editing involved to obtain these patterns, on the order of ten minutes per utterance. However, it was shown that short-term phase-only speech can be used to construct a speaker-dependent isolated word recognizer.

The results for Group B appear to be abysmal, however, several things must be considered. First, there was no pre-processing of the signals to time-wrap them. Second, no features were extracted, only the entire waveforms were
used. Third, the decision algorithm may have to be tailored to fit the data, rather than using a general purpose decision rule. Last, but certainly not least, no system exists today that is completely speaker independent.

One final observation concerning Group B. When the decision algorithm incorrectly identified any utterance it did so with a great deal of bias. In 30% of the cases where an utterance was incorrectly identified the number 'one' was picked to be the nearest neighbor.

This thesis was not an attempt to definitively answer the question, "is phase a physical invariant of speech?". Its purpose was to show that phase should be considered when constructing a word recognition system. This was accomplished. The next step is to use the information obtained from the phase in conjunction with other word recognition systems to possibly improve these systems with the long range goal of solving the speaker-independent word recognition problem.
TABLE 5.1

GROUP A RECOGNITION RESULTS
BASED ON TEN UTTERANCES PER DIGIT

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<tr>
<th>Digits</th>
<th>Unprocessed Waveforms</th>
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<th>Analytic Representation</th>
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### TABLE 5.2

GROUP B RECOGNITION RESULTS
BASED ON TEN UTTERANCES PER DIGIT

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APPENDIX A

INSTRUCTION SHEET

Thank you for participating in the Speech Processing Lab's effort to collect speech samples. This exercise will require about 10 minutes of your time to complete.

I. Biographical Data

A. Name:
B. Age:
C. Sex:
D. Place of Birth:
E. Occupation:

II. Speech Sampling

A. Repeat each word on the list four times, pausing approximately 5 sec. between utterances. (For example: the first word on the list is 'zero', therefore you would say: 'zero' (pause) 'zero' (pause) 'zero' (pause) 'zero' (pause) 'one' (pause) ......)

zero       six
one        seven
two        eight
three      nine
four
five

B. Repeat the following exercise 3 times:

Read the entire list of numbers at your natural speaking rate pauseing approx. 5 secs. before repeating the list. Do not pause unnaturally between the numbers. We are looking for continuous speech such as in a conversation.

zero-one-two-three-four-five-six-seven-eight-nine (pause/repeat)
APPENDIX B

COMPUTER PROGRAMS

All programs were written in IBM FORTRAN H to run on the W. R. Church Computer Center's IBM 3033. The programs access routines from the ISML library. The graphics programs interact with the DISSPLA graphics package.
SUBROUTINE PATTIN(FNI, FMI, Y)
(C) EY LT. JEFF PFIEFFER, JUNE 1983

ALGORITHM REACTS IN A PATTERN FOR USE WITH THE DECISION
ALGORITHM

IMPLICIT REAL*8(A-G), INTEGER(H-M), REAL(L-Z)
REAL Y(1680)
INTEGER*2 ICATA(32)

START THE PROGRAM

CALL FRICMNS ('FI', '83', 'DISK', 'FMI', 'CAT', 'FMI')
REWIND 83
DC 2010 I=1,7680,32
REAL (83, END=2030) IDATA
DO 2020 J=1,32
  K=I+J-1
  IF (K < GT, 768C) GO TO 2020
  Y(K) = IDATA(J)

2020 CONTINUE
2010 CONTINUE
2003 CONTINUE
RETURN
END
ALGORITHM ANALYTIC
(C) BY LT JEFF PFEIFFER JULY 1983

COMPUTES THE ANALYTIC SIGNAL REPRESENTATION OF A SPEECH SIGNAL
VIA THE USE OF A 79 WEIGHT HILBERT TRANSFORM

IMPLICIT INTEGER (A-Z)
INTEGER LA, LB, [1K(10]
REAL A(1024), B(512), Y(7680), RES(7680), H(75), ANAL(7680)
REAL AMAX, ATIEMF
COMPLEX CA(512), CB(256), RESLT(7680)
EQUIVALENCE (A(1), CA(1)), (B(1), CB(1))
INTEGER*2 ANDATA(32)
REAL*8 FA, FT, FM

 INITIALIZE THE DATA

LA=256
LB=75

READ IN THE WEIGHTS OF THE FILTER

WRITE(6,90C)
900 FORMAT('READING IN THE FILTER WTS, ASSUMING FA=FIR7905, FT=CAT*)
WRITE(6,90C)
910 FORMAT('ENTER THE FILEMODE')
READ(5,920,END=930)FM
920 FORMAT(A8)
930 REMIND 5
CALL FRTCMS ('FI', '85', 'DISK', 'FIR7905', 'DAT
1', 'FM)
REMIND 85
DC 950 [I=1,79
REAL(85, 760)H(I)
960 FORMAT(11C, F10.7)
950 CCATINLE

READ IN THE VECTOR

CALL INPART(1, Y)

SEGMENT THE VECTOR INTO 25 MSEC SEGMENTS

DC 2000 K=1,30
DO 10 I=1,1024
A(I) = 0.
10 CONTINUE
     DO 20 I = 1, 512
        BI(J) = 0.
     CONTINUE
20...

DO 100 I = 1, 256
     J = I + (K - 1) * 256
     A(I) = Y(J)
100 CONTINUE

DO 200 J = 1, 79
     B(I) = * (J)
200 CONTINUE

CALL IAML ROUTINE 'VCNV0' TO CONVOLVE THE VECTORS
CALL VCNAVO(CA, CB, LA, LB, IWK)

OBTAIN THE OUTPUT NOTING THAT ONLY 256 PTS OF VECTOR WERE USED
DO 300 I = 1, 256
     J = I + (K - 1) * 256
     RES(J) = A(I)
300 CONTINUE

300 CONTINUE

FORM THE ANALYTIC SIGNAL AND THE PHASE REPRESENTATION:

DC 400 I = 1, 17680
     RESL(I) = CABS(CMPLX(Y(I), RES(I)))
     ANAL(I) = (V(I) / RESL(I))
400 CONTINUE

AEXP = 0.
DC 410 I = 1, 17680
     ATEMP = AEXP(ANAL(I))
     IF (ATEMP .GT. AMAX) AMAX = ATEMP
410 CONTINUE

CONVERT TO I*2 FORMAT
CC 450 I = 1, 17680
     ANDATA(I) = ANAL(I)) / AMAX)* 10000.
450 CONTINUE

OUTPUT THE DATA
CALL OPART(ANDATA)
C .... QUERY THE OPERATOR IF ANOTHER RUN IS DESIRED

50C FORMAT(1X, A) READ(5, 55C) ANS

550 FORMAT(11)

600C CONTINUE

STOP

END
PROGRAM COMPUTES THE EUCLIDEAN DISTANCE BETWEEN A TEST VECTOR AND THE VECTORS IN THE PATTERN SPACE

IMPLICIT INTEGER(I-N), REAL(C-Z), REAL*8 (F-G)
REAL VECIN(768), E(7680), PAT(7680)

REAL IN THE VECTOR TO BE CLASSIFIED

WRITE(6,100)
100 FORMAT('ENTER THE DIGIT U WISH TO CLASSIFY')
READ(5,110,END=120)
110 FORMAT(I2)
120 REWIND 5
CALL IMPART(1, VECIN)

READ IN PATTERN VECTORS FROM ARRAY FORMED BY USING LISTFILE CMD
ASSUMING THAT THIS ARRAY HAS FILENAME = PAT, FILETYPE = CAT.

WRITE(6,130)
130 FORMAT('ENTER FILENAME OF PATTERN FILE')
READ(5,140,END=150)
140 FORMAT(A8)
150 REWIND 5
CALL FRCMS(*FI '82 'DISK *PAT *DAT
200 FM)
REWIND 82
CC 200 I=1,100
READ(82,210)FIN,FMI
210 FORMAT(I8,A8,T24,A8)
CALL PATMIN(FINI,FMI,PAT)

COMPUTE THE EUCLIDEAN DISTANCE

SUM = 0.
DO 24 J=1,768
24 SUM = SUM + (PAT(J) - VECIN(J)) ** 2
CONTINUE
SUM = SQRT(SUM)

OUTPUT THE RESULTANT VECTOR

WRITE(6,300)
300 FORMAT('FILENAME OF RESULTANT VECTOR')
READ(5,31C,END=32C)FNR
210 FORMAT(AB)
220 REIND 5
230 WRITE(6,33C)
240 FORMAT('OFIEMODE OF RESULTANT VECTOR')
READ(5,310,END=340)FNR
250 REIND 5
260 CALL FRICMS('F1 ',80 ',DISK ',FNR,'DEC ',FMR)
270 REIND 80
280 WRITE(80,45C)
290 FORMAT('I')
300 WRITE(80,56C)
310 FORMAT(T15,'NUMBER TO BE CLASSIFIED IS ',I2)
CC 510 I=1,100
320 WRITE(8C,520I1S(I))
330 FORMAT(15,I12,T15,E14.7)
340 CONTINUE
C --------- QUERY OPERATOR FOR ANOTHER RUN
C ---------
350 WRITE(6,64C)
360 FORMAT('ANOTHER RUN? Y(1), N(2)')
READ(5,55C)ANS
380 FORMAT(I1)
390 GC TO (1,2CC0),NAAS
400 CONTINUE
410 STEP
420 END
ALGORITHM: FREQUENCY RESPONSE
(C) MAY 1983 J. I. PFEIFFER

THIS IS A DOUBLE PRECISION ALGORITHM TO COMPUTE THE FREQUENCY RESPONSE OF A F.I.R. HILBERT TRANSFORM WITH CAD SYMMETRY ABOUT THE POINT (N-1)/2. THE RESPONSE IS CALCULATED FOR THE FREQUENCIES FROM 0 TO PI RADIANS. THE CUTFIL FILTER USES THE DISCRETE ROUTINE AND USES AS THE ABSCISSA THE NORMALIZED FREQUENCY (I.E. FRACTION OF 2 PI)

** * * ** FILEDEF'S USED ** ** ** **
10 - TERMINAL
85 - INPUT WEIGHTS

** * * ** VARIABLES DEFINED ** ** ** **
N - NUMBER OF WEIGHTS, INTEGER
H - VECTOR OF WEIGHTS, REAL
M - (N-1)/2, INTEGER
HSTAR - VALUE OF THE REAL PART OF THE RESPONSE, REAL
E - REAL PART OF RESPONSE, REAL
F - IMAGINARY PART OF RESPONSE, REAL
C - COMPLEX VECTOR (E,F),COMPLEX
X - ABSCISSA FOR PLOTTING, REAL
Y - ORDINATE FOR PLOTTING, REAL
D - INCREMENT IN FREQUENCY, REAL
DEL - PEAK APPROX ERROR, REAL
FL - LOWER CUTOFF FREQ, REAL

** * * ** DECLARE VARIABLES ** ** ** **

IMPLICIT Complex(A-C),Integer(I-P),Real(C-Z)
REAL*8 PI,ESTAR,ERRCR,0,D,H
DIMENSION F(900),X(900),Y(900),C(900),ERRCR(900)
INTEGER SWITCH,I1,I2,CC
REAL XCM,YCM,XPG,YPG,GR,HT,F,E,I1,XX(900),FH,FL,DELM,KK,DEL

** * * ** INITIALIZE VARIABLES ** ** ** **

PI = (3.14159265)

** * * ** BEGIN ALGORITHM ** ** ** **

** * REAL IN SPECIFICATIONS FOR THE FILTER ** **

WRITE(10,1CC)
100 FORMAT(ENTER NUMBER OF WEIGHTS TO BE USED, IN 12 FORMAT*)
READ(5,110)
110 FORMAT(12)
WRITE(10,112)  
FORMAT('ENTER THE VALUE OF THE PEAK APPROX ERROR,D, IN F4.2 FORMAT')

READ(5,114)DEL  
READ(5,114)FL  
READ(5,114)FH  
READ(5,114)N  
READ(5,116)I   
WRITE(10,117)  
FORMAT('ENTER THE LOWER CUTOFF FREQ FL IN F4.2 FORMAT')  
WRITE(10,117)  
FORMAT('ENTER THE NUMBER OF PAIRS OF POINTS TO FLOT, IN I3 FORMAT')  
WRITE(10,117)

* * * * * READ IN VALUES OF WEIGHTS * * * * * * * * *
CC 10 I=1,N  
READ(85,120)H(I)  
FORMAT(I11,F10.7)  
CC CONTINUE

* * * * * COMPUTE THE VALUE OF THE IMPULSE RESPONSE * * *
G = FLCAT(F)  
P = P+1  
N = (N-1)/2  
HSTAR = 0.  
D = FLAT(I-1)*(PI/G)  
X(I) = FLAT(I-1)/(2.*G)  
CONTINUE  
E = HSTAR*DSIN(M*E)  
F = HSTAR*UCOS(M*E)  
CONTINUE

* * * COMPUTE MAGNITUDE OF THE FREQUENCY RESPONSE * * *
CC 40 I = 1,C  
Y(I) = CAES(C(I))  
CONTINUE

* * * COMPUTE THE ERROR OVER THE RANGE (FL,FH) * * *
DEL = -DEL  
II = 2.*G*FL + 1.
III = INT(II)
FF = 5. - FL
KK = 2. * GST + 1.
K = INT(KK)
DC 50 I = III, K
ZZ = I + 1 - III
ERRC(ZZ) = (Y(I) - 1.)
XX(ZZ) = X(I)
50 CONTINUE
CC = K - III + 1

** * * * * * * * * PLOT OUTPUT * * * * * * * * * * *

** * * * PARAMETERS FOR DISPLAY * * * * * * * * *

WRITE(10, 3CC)
300 FORMAT('ENTER 1 IF TEK 610 IS USED, ENTER 2 IF OTHER DEVICE')
READ(5, 310) SWI\CH
310 FORMAT(III)
WRITE(10, 3CC)
320 FORMAT('ENTER X-DIM FOR PAGE,F4.1')
READ(5, 330) DIM
330 FORMAT(F4.1)
WRITE(10, 34CC)
340 FORMAT('ENTER Y-DIM FOR PAGE,F4.1')
READ(5, 350) YDIM
350 FORMAT(F4.1)
WRITE(10, 36CC)
360 FORMAT('ENTER X-DIM FOR SUBPLOT AREA,F4.1')
READ(5, 370) XP\G
370 FORMAT(F4.1)
WRITE(10, 38CC)
380 FORMAT('ENTER Y-DIM FOR SUBPLOT AREA,F4.1')
READ(5, 390) Y\PG
390 FORMAT(F4.1)
WRITE(10, 40CC)
400 FORMAT('ENTER GRACE MARGIN,F3.1')
READ(5, 410) GR
410 FORMAT(F3.1)
WRITE(10, 42CC)
420 FORMAT('ENTER CHARACTER HEIGHT SPEC,F3.1')
READ(5, 430) FT
430 FORMAT(F3.1)

** * * * SET LP LARGE BUFFER * * * * * * * * *

CALL LR\GBUF
* * * * * * CALL DEVICE TO BE USED * * * * * *

CALL TO (50C, 600), SWITCH

50C  CALL TEEKIE
600  CALL PIEKAL
62C  CONTINUE

* * * * * * SET UP PAGE * * * * * * * * * *

CALL HEIGHT(HI)
CALL PAGE(XCIM, YDIM)
CALL NBROF
CALL GRACE (GR)

* * * * * * CALL SETUP FOR SUBPLOT AREA * * * * * *

CALL AREA2([XPG, YPG])

* * * * * * NAME THE X & Y AXSES * * * * * *

CALL XNAME('FREQUENCY AGRMAZED TO 2 PI*', 100)
CALL YNAME('MAGNITUDE', 100)
CALL YAXAN(0.)

* * * * * * SET UP HEADING FOR THE GRAPH * * * * *

CALL HEAD1N('FREQ RESPONSE OF HILBERT TRANSFORM WITH 79 WEIGHTS', 100)
CALL HEAD1N('PEAK ERROR = 0.03888301', 10, 1..3)
CALL HEAD1N('LOWER CLT OFF FREQ = 0.01*', 10, 1..3)

* * * * * * SET UP THE GRAPH SPECS * * * * * *

CALL GRAP(0., 25, .5, C,, .05, L, .05)

* * * * * * * * DRAI THE GRAPH * * * * * * * * *

CALL CURVE(X, Y, 0, 0)

CALL ENDPL(C)

* * * * * * START FOR THE SECOND GRAPf * * * * * *

WRITE(10, 72C)

72C  FORMAT('ENTER X-DIM FOR PAGE', F4.1)

READ(5, 730)DIM

730  FORMAT(F4.1)

WRITE(10, 74C)
FCMAT(ENTER Y-DIM FOR PAGE,F4.1*)
READ(5,72C)YDIM
WRITE(10,72C)
FCMAT(ENTER X-DIM FGR SUBPLCT AREA,F4.1*)
READ(5,77C)XPG
WRITE(10,77C)
FCMAT(ENTER Y-DIM FOR SUBPLOT AREA,F4.1*)
READ(5,790)YPG
WRITE(10,790)
FCMAT(ENTER GRACE MARGIN,F3.1*)
READ(5,910)GR
WRITE(10,910)
FCMAT(ENTER CHAR HEIGH SPEC,F3.1*)
READ(5,930)FT
FCMAT(F3.1)
CALL HEIGHT(HT)
CALL PAGE(XLIN,YDIM)
CALL NCBROF
CALL GRACE(GR)
CALL AREA2C(XPG,YPG)
CALL NAME(1CC)
CALL NAME(100)
CALL YAXANG(0.)
CALL HEADIN('ERROR CF HILBERT TRANSFORM WITH 79 WEIGHTS',1CC)
CALL HEADIN('PEAK APPROX ERROR = 0.0388830',1CC)
CALL HEADIN('LOWER CUTFREQ FREQ = 0.015',1CC)
CALL GRAF(FL,'SCALE',FH,DELN,'SCALE',DEL)
CALL GRAF(FL,'SCALE',FH,DELN,'SCALE',DEL)
CALL CURVE(XX,ERRCR,CG,O)

     ***** ENG THE PLOT*****

CALL ENDP(L(C)
CALL DCNEPL
STOP
END
ALGORITHM GRAPH

THIS PROGRAM IS A MODIFICATION OF A GRAPHICS ROUTINE "GRAFI." WRITTEN BY LT JAY H. BENSON IN MAY 1983. MODIFICATION WAS DONE BY LT JEFFREY T. PFEIFFER IN JULY 1983.

PROGRAM PLots 1680 samples of speech data.

IMPLICIT INTEGER (A-V), REAL (X-Z)

INTEGER*2 ICATA(32)
LOGICAL READ1(25)
LOGICAL LTRDOL, LTRBLK
REAL X(7680), Y(7680)
REAL Y(1920), Y2(1920), Y3(1920), Y4(1920), Y5(1920)

CALL LTRDOL/*6, LTRBLK/1*

CALL FRTCHMS ('EXEC *,"GR")
READ (5,901,END=8000) IANS

IF (IANS.NE.0) GOTC 8000

READ IN THE WAVEFORM TO BE PLOTTED

REWIND 1
DE 1010 I = 1,7680+32
READ (1,ENC=1030) IDATA
CC 102C J = 1,32
K = I + J -1
IF (K.GT.7680) GOTG 1020
Y(K) = IDATA(J)

CONTINUE
CONTINUE
CONTINUE
CONTINUE

NORMALIZE THE DATA TO BE PLOTTED

IMAX = 0
CC 2000 I = 1,7680
TEMP = ABS(Y(I))
2000 IF (TEMP.GT.IMAX) IMAX = TEMP
CC 2010 I = 1,7680
X(I) = 1
2C10  Y(I) = Y(I) / IMAX

C----- QUERY THE OPERATOR FOR GRAPHICS PARAMETERS

C----- WRITE 6,16C
160  FORMAT('OPTEKAL(1),TEK618(2)?')
   REWIND 5
   READ (5,17C,END=40C) DEV
170  FORMAT(1I)
40C  CCNTINE
180  FORMAT(1OC,PPRS(1),NC(2)?)
   REWIND 5
   READ (5,190,END=405) CNUM
190  FORMAT(1I)
405  CCNTINE
200  FORMAT(4,2OC)
   REWIND 5
   READ (5,210,END=410) XFACT
210  FORMAT(F3.1)
410  CCNTINE
   IF (DEVI .LE. 1) CALL PTEKAL
   IF (DEVI .LE. 2) CALL TEK618
   IF (CNUM .LE. 1) CALL COMPRES

C----- CLEARY OPERATOR AS TC THIRD LINE OF HEADING

DC 21OC I = 1.24
   READ(1) = LTRBLK
2100  CCNTINE
   READ(135) = LTRDOL
   WRITE (6,91C)
910  FORMAT('CENTER SUBHEADING LINE 3 UF 3 (ENG WITH $ TO CENTER):')
   REWIND 5
   READ (5,911,END=211C) (HEAD1(I),I=1,24)
911  FORMAT (24A1)
2110  CCNTINE

C----- SETUP THE PLOTTING AREA

XPAGE  = 11.0
YPAGE  = 8.5
   CALL PAGE (XPAGE,YPAGE)
   CALL NCBRD
   XAXIS  = 8.0
   YAXIS  = 5.0
   CALL AREAZ (XAXIS, YAXIS)
CALL BLOWUP(XFACT)

CALL XNAME (*SAMPLE NUMBERS(K)$$,100)
CALL YNAME (*NORMALIZED VOLTAGES$$,100)
CALL HEAD1 (*SAMPLED SPEECH WAVEFORM$$,100,1.3,3)
CALL HEAD1 (*UTTERANCE IS$$,100,1.1,3)
CALL HEAD1 (HEAD1,100,1.1,3)

DEFINE THE AXISES

XCRIG = 0.0
XSTP = 320.0
XMAX = 1920.0
YCRIG = -1.0
YSTP = 1.0
YMAX = 1.0
CALL YNONUP
CALL GRAF (XORIG,XSTF,XMAX,YORIG,YSTP,YMAX)
CALL GRID (C,1)

SEGMENT THE WAVE INTO 4 PARTS ON 1920 POINTS EACH. GRAPH ALL THE SEGMENTS ON ONE PHYSICAL PAGE BEGINING WITH SEGMENT 1 BLADING THE SEGMENTS AS FOLLOWS:

SEGMENT 1 BY+6.0
SEGMENT 2 BY+4.0
SEGMENT 3 BY+2.0
SEGMENT 4 BY+C.

DC 300C I = 1,1920
3CCG Y[I] = Y[I] + 6.0
CC 3010 I = 1921,384C
3C1C Y[I] = Y[I] + 4.0
DC 302C I = 3841,576C
3C2C Y[I] = Y[I] + 2.0

DRAW THE FIVE CURVE SEGMENTS

NPNTS = 192C
I MARK = 0
CALL CURVE (X,Y1,NPNTS,IMARK)
CALL CURVE (X,Y2,NPNTS,IMARK)
CALL CURVE (X,Y3,NPNTS,IMARK)
CALL CURVE (X,Y4,NPNTS,IMARK)
CALL CURVE (X,Y5,NPNTS,IMARK)

TERMINATE THIS FLCT
C --- CALL ENOPL (0)
C
C LCOP BACK FOR ANOTHER PLOT, IF DESIRED
GOTO 1000
C
C NCRMAL EXIT
CC CONTINUE
CALL DEPEPL
RETURN
END
LIST OF REFERENCES


6. Ibid., p. 12.


10. Ibid., p. 1345.

11. Ibid., p. 1346.

12. Ibid., p. 1347.

13. Ibid., p. 1348.


17. Ibid., p. 663.

18. Ibid., p. 688.

19. Ibid., p. 689.


22. Ibid., p. 152.


24. Ibid., p. 372.


27. GENRAD, 2500-Series System, 1981.


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<td>Commander</td>
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<td>Naval Electronics Systems Command</td>
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