The Electron Content and Its Variations at Natal, Brazil

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The Faraday rotation and amplitude data for the period September 1978 through August 1979, recorded from the geostationary satellite SMS 1 (90°W) at Natal (5.9°S, 35.2°W), have been utilized to study the behavior of total electron content (TEC). Apart from diurnal and seasonal behavior of TEC, two characteristic features of the nighttime ionosphere are discussed: (1) a postsunset enhancement in TEC which lasts for several hours following the rapid sunset decrease and (2) the sharp, isolated changes in TEC. In particular, relating to phenomenon 2, the depletions in TEC are usually accompanied by a simultaneous increase in fading rate, scintillation index, and amplitude level, while the enhancements are accompanied by a simultaneous decrease in fading rate, scintillation index, and amplitude level. The statistics of their occurrence and nature are described. The average behavior of the signal amplitude after propagating through either a depleted or an enhanced ionosphere is modeled theoretically and shown to be in agreement with the observed experimental behavior.

Behavior of Total Electron Content (TEC) at Natal

Diurnal and Seasonal Variation in TEC

Natal is an equatorial station (latitude 5.9°S, dip -9.6°). A rotation of $\pi$ rad on the 136.379-MHz signal received from the geostationary satellite SMS 1 (90°W) is equivalent to $1.89 \times 10^{17}$ el/m$^2$ in total electron content for a mean field height of 350 km. To study the general behavior of TEC in different seasons, 10-12 days of uninterrupted data were selected from the periods September-October 1978, December 1978 to January 1979, March-April 1979, and June-July 1979. The hourly median values of TEC are plotted in Figure 1. It may be pointed out here that no claims are made regarding the absolute value of the TEC, especially for individual cases near the diurnal minimum values, for want of independent calibration. It is, however, felt that the error in the median values is only a small fraction of $\pi$ and that no $\pi \pi$ ambiguity is involved, though it may sometimes be present in individual day-to-day values.

Diurnally, the minimum occur around 0500 hours LMT in all the seasons, while the maximum occurs around 1500 LMT in the June solstice (winter), 1200 LMT in the December solstice (summer), 1330 LMT in the spring equinox, and 1430 LMT in the fall equinox. The electron content increases rapidly following sunrise. The rate of increase is very fast during spring, fall, and the December solstice but very slow during the June solstice. The average diurnal minimum and maximum values of TEC for spring, fall, winter, and summer are $1.33 \times 10^{17}$, $9.07 \times 10^{17}$, $1.11 \times 10^{17}$, and $11.47 \times 10^{17}$, $0.67 \times 10^{17}$, and $5.70 \times 10^{17}$, and $1.00 \times 10^{17}$ and $7.94 \times 10^{17}$ m$^{-2}$ respectively, giving a diurnal ratio of TEC of 6.8, 10.5, 8.8, and 7.9. It may be noted that, in general, the decay rate of the TEC after sunset is greater than the buildup rate at sunrise.

Post-sunset Enhancement in TEC

Following the dramatic drop in Faraday rotation angle for an hour or so after sunset, it may then either settle down to a gradual decay, finally reaching a minimum just before the following sunrise, or sometimes, and at different seasons, a substantial increase in TEC occurs for a duration of 3-4 hours centered around 2300 LMT. This phenomenon is much more pronounced during equinoxes and hence is very visible even in median curves, while only a trace increase is noticeable in solstices. On the evening of November 25, 1978, as shown in Figure 2, the increase at 2200 LMT is approximately $1.61 \pi$ rad or $3.12 \times 10^{17}$ el/m$^2$, which is nearly one half of the diurnal variation, while on the night of November 15, 1978, the increase at 2330 LMT is $3.8 \pi$ radians or $7.18 \times 10^{17}$ el/m$^2$, which is about 90% of the diurnal maximum and about 4% more than the diurnal change in TEC (Figure 3). This nocturnal increase, in varying degrees, has been observed both on days of no scintillation as well as on days of strong scintillation. Therefore it is not likely to be connected with the irregularity-producing mechanism.

The large post-sunset enhancements in equatorial zone have been reported by various workers e.g., Hunter, 1969; Koster, 1972; Koster and Beer, 1972; Yehoh-Amankwa and Koster, 1972; Donatelli et al., 1981. It was suggested that the $F$ region dynamo theory (Rishbeth, 1971, 1977) may offer the most plausible explanation for this effect. Rishbeth [1971, 1977] suggested that the neutral winds in the $F$ region produce polarization fields that short-circuit through the $E$ region.
Fig. 1. Diurnal and seasonal variation of TEC over Natal, Brazil, for the period September 1978 through August 1979.

Fig. 2. Typical Faraday rotation variation showing postsunset enhancement as observed on November 23, 1978. This day is marked by the absence of scintillation even though scintillations are usually very active in November.

Fig. 3. Typical Faraday rotation variation showing sharp, isolated depletions superposed over the enhancements in the period 2100-2330 as well as the normal decaying nighttime ionosphere after local midnight.

at 13° dip latitude, and even less in the Ascension Island observations [Donatelli et al., 1981] at 15° dip latitude. These observations are consistent with the Defense Meteorological Satellite Program measurements in the postsunset (1930 LT) sector at 840 km which showed smooth density depletions in the immediate vicinity of the magnetic equator with enhancements in the ±10°-20° magnetic latitude range. The subsequent increase around local midnight in TEC, however, is more pronounced in the present and in Hunter's observations.

We note that the above arguments [cf. Koster, 1972] clearly explain the dramatic decrease in TEC after sunset at the magnetic equator and the relative increase in electron density in the 10°-20° magnetic latitude range, but the very large enhancements in TEC around 2200-2300 LT in the equatorial ionosphere as reported in this paper are not explicitly explained. Lanzerotti et al. [1976] reported, discussed, and related the occurrence of nighttime ledges in TEC measurements at Arecibo, via a model calculation, to the rise and fall of the height of the F2 peak around midnight. They concluded that the characteristics of the nighttime ledge observed at Arecibo could be directly related to the meridional component of nighttime thermospheric winds. Anderson and Roble [1974] studied the behavior of the nighttime ionosphere near the geomagnetic equator and showed that the E × B vertical drifts can cause perturbations in the neutral winds and temperatures. Recently, Bittencourt and Sahai [1979], using a tropical ionospheric F region model described by Bittencourt and Tinsley [1976], investigated the effect of E × B drift velocity on the local time dependence of NmF2, hmF2, and 6300-Å emission at the magnetic equator. They concluded that the times of NmF2 enhancements during the night are closely related to the time history of the vertical E × B drift, its magnitude, and time of reversal. When the postsunset enhancement in upward drift is well developed and downward drift commences after 2000 LT, then NmF2 enhancement occurs around 0200 LT. When upward drift is less pronounced and downward drift occurs at 1900 LT, the enhancement occurs around 2230 LT [cf. Bittencourt and Sahai, 1979; Anderson and Rusch, 1980]. This clearly explains the variability of TEC enhancements during the nighttime at equatorial stations.
Isolated Depletions and Enhancements in TEC

The recent measurements at the magnetic equator have helped to reach some understanding about the nature of one kind of ionospheric perturbation occurring at night. Such perturbations are described variously as ionization depletions, bubbles, plumes, and some type of irregularity patches, or equatorial spread $F$ irregularities. On the experimental side the radar backscatter maps [Woodman and LaHoz, 1976] show dramatically the plumelike structures when they are viewed vertically upward as a function of time at a fixed location. In situ measurements, large depletions of ionization are observed as the satellite passes nearly horizontally [McClure et al., 1977] or as the rocket traverses nearly vertically [Kelley et al., 1976] through these bubbles. On the basis of propagation measurements the occurrence of these bubbles has been shown to be correlated with the onset of scintillation on satellite radio signals [Aarons, 1977; Basu and Basu, 1976]. These have also been found to be responsible for backscattering in transequatorial propagation [Röttger, 1976]. On the theoretical side, early investigations have shown that the bottomside ionosphere is subject to Rayleigh-Taylor instabilities [Liu and Yeh, 1966a, b]. Recent numerical simulations have shown that as the depletion increases, the nonlinear polarization $E \times B$ forces in the equatorial geometry can drive the depleted region upward through the ionization peak to the topside ionosphere [Ossakow et al., 1979].

Yeh et al. [1979a, b] reported observations of ionospheric bubbles utilizing the 136-MHz Faraday rotation records from Natal, and Wernik [1979] presented a simple model of an equatorial bubble. Looking again at Figure 3, it may be noted...
Fig. 5. Original record for November 12, 1978, from Natal using SMS I transmissions showing both enhancements and depletions in Faraday rotation. Note the characteristic behavior that the depletions are accompanied by increases in fading rate, scintillation index, and amplitude level, while the enhancements are accompanied by decreases in fading rate, scintillation index, and amplitude level.
that there are several sharp structures superposed over the background TEC variation. The first sharp depletion occurred at 1920 LMT, shortly after the onset of scintillations. There are also other depletions, but those occurring before local midnight are not as isolated and distinct as those occurring near or after midnight. For example, the bubble occurring at 0040 LMT on November 16, 1978, appeared in the original record as shown in Figure 4. Note the coincident increase in scintillation index as well as scintillation rate and the average amplitude level with the appearance of the bubble. This suggests that the isolated rapid scintillation rate can be used as a possible indicator of a bubble. It may be mentioned here that these isolated bubbles should not be taken as traveling ionospheric disturbances (TID), which generally have quasi-periodic and wavelike structure. It is very clear from Figure 3 that the five sharp depletions occurring successively a few hours around local midnight do not possess the usual TID appearance.

Another example is shown in Figure 5. The amplitude channel at the bottom shows rapid fluctuations at three times: near 0015, 0025, and 0030 LMT. Coincidentally, the depletions in Faraday rotation angle can be clearly identified for the latter two times but not so clearly for the former time. Every time the average amplitude level also shows an increase. In addition to sudden increases in scintillation rate, there are also times when scintillation rate is reduced momentarily and the average amplitude level is simultaneously decreased, coinciding with the increase in Faraday rotation angle. Two such cases can be identified in Figure 5, at 0010 and 0038 LMT. The labeling of Faraday rotation enhancement cases may look subjective, especially when they occur along with depletions as in Figure 5. Such doubts may be further reinforced from the fact that the in situ data have clearly shown the presence of isolated depletions in electron density, but no enhancement cases have been reported so far. However, the decrease in scintillation rate and scintillation index below the normal level at the time of enhancement and the rare example of isolated enhancement like the one shown in Figure 6 make us believe that both depletions and enhancements do occur, though their relative occurrence may be affected by the subjective approach. Consequently, the typical behavior of these events is as follows: The depletions in TEC are usually accompanied by simultaneous increases in fading rate, scintillation index, and the average amplitude level, while the enhancements in TEC are accompanied by simultaneous decreases in fading rate, scintillation index, and the average amplitude level. During the 1-year period from September 1978 through August 1979 a total of 990 cases consisting of 710 isolated depletions and 280 enhancements have been identified. Thus the cases of enhancements were only about 28% of the total cases. The statistics of these cases follows.

Figure 7 is a histogram showing the occurrence of isolated depletions and enhancements during different months for the period September 1978 to August 1979. It is clear that the occurrence of both depletions and enhancements is a maximum in the month of October and a minimum in August. It is noted that 67% of depletions occur during October–December and 80% during the period September–February, while 83% of enhancements occur during September–December. Furthermore, only 2% of depletions and 4% of enhancements occur during the May–August period. Figure 8 shows
Fig. 7. Histogram showing occurrence of isolated depletions and enhancements during different months for the 1-year period from September 1978 to August 1979.

A histogram depicting the diurnal variation of the occurrence of such cases. It is clear that these depletions/enhancements occur mostly at night, between 1900 and 0300 LT, with a maximum between 2000 and 2300 LT.

A histogram depicting the duration of the ionization depletions/enhancements is given in Figure 9. Most of these cases last less than 20 min, with a large number of depletion cases (165) having a duration between 8 and 10 min, but there are also a number of depletions/enhancements lasting longer than half an hour. These depletions/enhancements have a distribution shown in Figure 10. Most of the cases have a decrease/increase in equivalent vertical electron content of less than $4 \times 10^{16}$ el/m$^2$, but depletions as large as $1.2 \times 10^{17}$ el/m$^2$ have also been observed, which is about 11-17% of the total diurnal change in TEC for the period October-December, when most of the cases occur.

Modeling of the Ionospheric Bubble

In an attempt to simulate a bubble by a model a Gaussian lateral distribution of electron density has been used. Assuming that the lateral distribution and the height distribution enter in a multiplicative manner, the two-dimensional electron density can be expressed as

$$N(x, h) = f(h) \cdot [1 - \alpha \exp \left( -\left| x - x_0 \right| \right)]^2$$  \hspace{1cm} (1)

where

- $h$ height;
- $x$ lateral distance;
- $\alpha$ constant, usually smaller than unity;
- $l$ half width of the bubble;
- $f(h)$ height distribution of the electron density of the background ionosphere.

Equation (1) gives an electron density model which represents a depletion when the constant $\alpha$ is positive and an enhancement when $\alpha$ is negative. In each case the maximum deviation occurs when $x = x_0$. When ray bending is ignored, the optical path $\psi$ can be evaluated by the integration

$$\psi = \int n \, dh = \psi_0 - \frac{40.3}{f^2} \cdot N_{TB} \cdot [1 - \alpha \exp \left( -\left| x - x_0 \right| \right)]^2$$  \hspace{1cm} (2)

where

- $n$ refractive index;
- $\psi_0$ reference phase;
- $N_{TB}$ background TEC, equal to $\int f(h) \, dh$.

According to ray theory the phase variation (2) along the wave front will develop into an amplitude variation after propagating a distance. This amplitude variation as observed on the ground can be shown to be proportional to the integral [Yeh and Liu, 1972]

$$\exp \left( -\frac{1}{2} \int_0^L \frac{d^2 \psi}{dx^2} \, dx \right) = \exp \left[ \frac{40.3 \alpha N_{TB} S}{f^2} \cdot \left( 1 - \frac{2(x - x_0)^2}{l^2} \cdot \exp \left( -\left| x - x_0 \right| \right) \right) \right]$$  \hspace{1cm} (3)

Equation (3) gives the amplitude variation on the ground. If the amplitude is measured in decibels, its variation is then
depletion and enhancement cases as observed during the period September 1978 to August 1979.

The parameters deduced from Figure 4 and used to calculate an amplitude pattern on the ground by using (3) are as follows:

\[ \alpha = 0.163 \]
\[ f = 136 \text{ MHz} \]
\[ N_f = 3.5 \times 10^{17} \text{ el/m}^2 \]
\[ l = 18.5 \text{ km} \]

The bottom of the layer was assumed to be at a height of 300 km. Since the elevation angle is 28°, the path S turns out to be 640 km.

The calculated amplitude pattern on the ground is depicted in Figure 11. The similarity of the calculated and the experimentally observed average amplitude pattern is obvious. The maximum amplitude is dependent on the width of the bubble when the other parameters are fixed. In our case the best fit was achieved at \( f = 37 \text{ km} \).

The minimum points of amplitude can be determined quite accurately from the observed amplitude variation (Figure 4). The time difference between the minima of the calculated amplitude variation is approximately 450 s. The corresponding length in the calculated amplitude variation (Figure 10) is about 44 km, giving a drift velocity of about 98 m/s, which agrees well with drift velocities measured independently by other means [Yeh et al., 1981].

As was pointed out previously, the amplitude pattern of enhancement can be computed simply by changing the sign of \( \alpha \) in (1). On a logarithmic scale the curve will be the same shape as in the case of depletion, but turned upside down, because in (3), \( \alpha \) is in the exponent. On a linear scale the nature of the curve will be different.

It is obvious that the suggested Gaussian model is not perfect. However, it describes quite well the main features of the average amplitude variation caused by the ionospheric bubble. The present model does not explain the change in fading rate and scintillation index caused by a bubble as described in the present work. This is because, in addition to a general depletion of electron density inside the bubble as modeled in (1), there are also sharp fingerlike wedges which are not contained in (1). Computations by Wernik et al. [1980] show that regions of sharp wedges can be sources of intense scintillations. The model constructed by them is based on in situ measurements [McClure et al., 1977] and shows these highly complex structures, with steep gradients in the center of the bubble. The horizontal gradients gradually decrease toward the edge of the bubble, as also revealed by in-situ measurements. The computed pattern indicates an increase of the scintillation rate with increase of bubble thickness and shows a change in the scintillation rate with increase of bubble thickness and shows a change in the scintillation rate from slow, close to the edges of the bubble, to fast, at its center [Wernik et al., 1980]. This is in complete agreement with our experimental results.

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2532


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