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# THEORY OF GYROTRON AMPLIFIERS IN A DISK OR A HELIX LOADED WAVEGUIDE

BY JOON Y. CHOE,  
HAN S. UHM

RESEARCH AND TECHNOLOGY DEPARTMENT

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helix mode can be very broad in its bandwidth. Moreover, the hybrid mode operation, using the helix mode as a carrier, shows possibility of fast wave wide band amplification by contouring waveguide.

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## FOREWORD

The gyrotron amplifiers in two slow wave structures, the disk and the helix loaded waveguides, are investigated for wide band applications. For each structure, properties of the vacuum waveguide mode are examined in connection with the gyrotron application, and the gyrotron dispersion relation is obtained. For the disk loaded gyrotron, it is found that the group velocity of the waveguide mode can be easily varied by the disk parameters, and the gain and the bandwidth are at least comparable to those of the ordinary gyrotron. In the helix waveguide configuration, the gyrotron utilizing the helix mode can be very broad in its bandwidth. Moreover, the hybrid mode operation, using the helix mode as a carrier, shows possibility of fast wave wide band amplification by contouring waveguide.

Approved by:

A handwritten signature in cursive script that reads "Ira M. Blatstein".

IRA M. BLATSTEIN, Head  
Radiation Division

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## I. INTRODUCTION

The gyrotron (Flyagin et al 1977, Hirschfield and Granatstein 1977) is a high power microwave tube that utilizes the fast wave coupling of the waveguide mode with the cyclotron frequency upshifted beam mode. One of the shortcomings of the gyrotron, however, is its narrow bandwidth, primarily due to the fast variation of the group velocity of the waveguide mode in a smooth wall configuration. Therefore, it is necessary to slow down the wave in order to broaden the bandwidth. In this regard, we have to re-examine various slow wave structures that have been widely used in conventional traveling wave tubes (Pierce 1950), in the context of the fast wave interaction of the gyrotron. In this paper we will examine the gyrotron in two of such slow wave structures; the periodic disk loaded gyrotron and the sheath helix loaded gyrotron. Another slow wave structure, the dielectric loaded gyrotron, has been exhaustively investigated already (Choe et al 1981).

Previous analyses of these two configurations exist (Chu and Hansen 1947, Walkinshaw 1948, Pierce 1950, Hutter 1950, Sensiper 1955), but these are limited to the slow wave applications to the TWT. In the periodic disk configuration the transverse magnetic (TM) mode is analyzed, and for the sheath helix waveguide most of them have ignored important role of the outer conducting wall. Here we will investigate the transverse electric (TE) mode suitable for the gyrotron interaction for the periodic disk geometry, and include the conducting wall in our analysis for the helix geometry to utilize the location of the wall as a useful parameter. The periodic disk loaded gyrotron will be discussed in Sec. II, and the sheath helix loaded gyrotron in Sec. III.

In view of the role that the vacuum waveguide mode plays in performance of the tubes, we will first examine the dispersion characteristics of the beam-free waveguide mode for each structure (in Subsection A). This will be followed by the

derivation of the gyrotron dispersion relation with the electron beam in Subsection B. For each structure, the Subsection B will include some numerical examples of the gyrotron gain. We emphasize that the objective of this paper is to examine the dispersion characteristics of the waveguide and to derive the gyrotron dispersion relation for two slow wave structures. Therefore, the detailed parametric optimization with respect to the gain and the bandwidth will be deferred for later works, only giving few typical examples.

## II. DISK LOADED GYROTRON

We consider a cylindrical waveguide loaded with periodic disks as shown in Fig. 1. The thin disks extend radially from the outer conductor at  $r = b$  to  $r = a$  as shown, with the axial period given by  $L$ . The cylindrical coordinates  $(r, \theta, z)$  are employed.

This configuration has been studied before in the context of the slow wave TWT interaction (Chu and Hansen 1947, Walkinshaw 1948). Thus these analyses have been limited to the TM modes. In order to utilize the same configuration for the fast wave interaction of the gyrotron, therefore, we must examine the TE modes. Otherwise the present analysis is similar to the previous ones. Emphases are, hence, on the differences between TM and TE modes. In Subsection A, the TE dispersion relation for the vacuum waveguide mode is obtained and discussed. The gyrotron dispersion relation with the electron beam is derived and an example of the gyrotron gain from this dispersion relation will be given in Subsection B.

## A. Vacuum Waveguide Dispersion Relation

In this subsection we will derive and discuss the vacuum waveguide dispersion relation for the periodic disks shown in Fig. 1. We limit our attention to the azimuthally symmetric (i.e.  $\partial/\partial\theta = 0$ ,  $\ell = 0$ ) TE modes. Moreover, we will employ an approximate scheme in order to obtain an analytical result.

The procedure to obtain the approximate dispersion relation is given elsewhere (Choe and Uhm 1982), and only the outline will be given here. First, the domain is divided into two separate regions (I for  $r \leq a$ , II for  $a \leq r \leq b$ , see Fig. 1), and the electromagnetic fields for TE mode are expressed in the separate eigenfunction expansion for each region. The eigenfunctions are determined by the boundary conditions on the metallic boundaries and the axial periodic conditions (i.e. Floquet theorem, Slater 1950). Then, the dispersion relation results in by matching the fields at the mouth of the disks (i.e. at  $r = a$ ), where an approximate method is used to simplify the dispersion relation.

The fields for each region (I and II) can be expressed as the sum of the space harmonic ( $n$ ) waves in region I, and of the standing waves with the nodal number  $m$  for region II. Namely,

$$B_z^I(r, z) = \sum_{n=-\infty}^{\infty} C_n J_0(p_n r) \exp(ik_n z), \quad (1)$$

$$B_z^{II}(r, z) = \sum_{m=1}^{\infty} D_m \left[ N_1(q_m b) J_0(q_m r) - J_1(q_m b) N_0(q_m r) \right] \\ \times \sin(\kappa_m z), \quad (1)'$$

where

$$k_n \equiv k + 2n\pi/L, \quad p_n^2 \equiv \omega^2/c^2 - k_n^2, \quad (2)$$

$$\kappa_m \equiv m\pi/L, \quad q_m^2 \equiv \omega^2/c^2 - \kappa_m^2. \quad (2)'$$

Here  $\omega$  and  $k$  refer to the frequency and the axial wavenumber, respectively, and  $J_\ell$  and  $N_\ell$  to the first and second kind of Bessel functions of order  $\ell$ . Other TE components ( $E_\theta$ ,  $B_r$ ) are given in terms of  $B_z$ . Here  $\underline{E}$  and  $\underline{B}$  denote the electric and magnetic fields. We note that the expression for  $E_z$  in TM mode is similar to eq. (1), with one notable exception. For TE mode the first term in region II is with  $m = 1$ , while it is with  $m = 0$  for TM mode. The usual periodicity of the dispersion relation in the axial wavenumber  $k$  with the period of  $2\pi/L$ , and the symmetry with respect to  $k$  are evident from eq. (1), even without the field matching considerations. Thus it is sufficient to obtain the dispersion relation for  $0 \leq k < \pi/L$ .

Since an analytical dispersion relation is sought in this paper, we need an approximation scheme for matching fields at the mouth ( $r = a$ ). Instead of matching fields for all  $z$ , we only match the average fields over the one axial

period  $L$ . That is, we demand that  $\langle \psi^I \rangle = \langle \psi^{II} \rangle$ , where  $\psi$  stands for the fields and  $\langle \psi \rangle = \int_0^L dz \psi(r = a, z)$ . Furthermore, we assume that the axial wavenumber is small, that is,

$$kL \ll \pi. \quad (3)$$

Then it can be shown (Choe and Uhm 1982) that the dominant term is for  $n = 0$  in region I and for  $m = 1$  for region II, and that the average fields are matched provided eq. (3) is valid. This can be compared with TM mode where, with the same approximation scheme (eq. (3)), the  $n = 0$  term in region I couples with the  $m = 0$  term in region II. Within this truncation method, the dispersion relation for the TE mode is given by

$$D^{TE} = \psi_J(p_0 a) - \phi_1(q_1 b, q_1 a) = 0, \quad (4)$$

where

$$\psi_J(x) \equiv J_1(x) / [xJ_0(x)],$$

$$\phi_i(y_b, y_a) \equiv \frac{N_i(y_b)J_1(y_a) - J_i(y_b)N_1(y_a)}{y_a [N_i(y_b)J_0(y_a) - J_i(y_b)N_0(y_a)]}. \quad (5)$$

We recall that the corresponding TM dispersion relation is given by

$D^{TM} = \psi_J(p_0 a) - \phi_0(q_0 b, q_0 a) = 0$ . Here  $p_n^2$  and  $q_m^2$  are previously defined in eq. (2). The difference in the dominant term in region II ( $m = 1$  for TE,  $m = 0$  for TM) is reflected in the dispersion relation ( $\phi_1$  for TE,  $\phi_0$  for TM).

Careful examination of the dispersion relation reveals several characteristics of the disk loaded waveguide mode. For given  $k$ , the frequency  $\omega$  is higher than that for the smooth wall (i.e.  $a = b$ ). The reverse is true for the TM mode.

Also the frequency increases for given  $k$  as the period  $L$  decreases, and as the ratio  $a/b$  decreases. This can be compared with the TM mode, where  $\omega$  is independent of  $L$  and increases as  $a$  approaches  $b$  (smooth wall). The lower cutoff frequency  $\omega_{c0}$  increases as  $L$  increases and as  $a/b$  decreases. For TM mode,  $\omega_{c0}$  is independent of both  $L$  and  $a/b$ . These dependence of the frequency on the period  $L$  and the ratio  $a/b$  are further illustrated in Fig. 2. In Fig. 2(a), the TE mode dispersion curves for several disk dimensions  $a/b$  are plotted at given period ( $\pi b/L = 10.0$ ). It is evident from the graph the cutoff frequency  $\omega_{c0}$  at  $k = 0$  is decreasing function of  $a/b$ . At the same time, if we extrapolate our analysis to the limit at  $k = \pi/L$ , the frequencies for all  $a/b$  converge to that for the smooth wall. This pivot-like phenomenon occurs at  $k = 0$  for the TM modes. Obviously the group velocity of the wave decreases as the ratio  $a/b$  decreases. The dependence on the period  $L$  is shown in Fig. 2(b). Here the dispersion curves are drawn for several  $L$  at given disk dimension ( $a/b = 0.5$ ). Also shown is the dispersion curve for the smooth wall (broken curve) for reference. Evidently for given  $k$ ,  $\omega$  is an increasing function of  $L$ . The graph also reveals that the group velocity of the wave decreases as  $L$  increases. We conclude that the group velocity can be easily adjusted by variation of the disk parameters,  $a/b$  and  $L$ .

### B. Gyrotron Dispersion Relation

In this subsection we will derive the dispersion relation for the disk loaded gyrotron in the presence of the electron beam. It is assumed that the thin hollow electron beam is located at  $r = R_0$  ( $0 < R_0 < a$ ), under the influence of the strong axial magnetic field  $B_0$ , and the configuration otherwise is the same as in Fig. 1. Again we limit our attention to the azimuthally symmetric ( $\ell = 0$ ) TE mode.

The analysis is carried out within the framework of the linearized Maxwell-Vlasov system for the fields  $\underline{E}$  and  $\underline{B}$ , and for the beam electron distribution function  $f$ . Following the scheme in previous subsection, the perturbed fields are for those with the fundamental space harmonic ( $n = 0$ ) and with the first nodal number ( $m = 1$ ). Namely, in the vacuum region,

$$B_z = \begin{cases} A_1 J_0(p_0 r), & 0 \leq r \leq R_0, \\ A_2 J_0(p_0 r) + A_3 N_0(p_0 r), & R_0 \leq r \leq a, \\ A_4 J_0(q_1 r) + A_5 N_0(q_1 r), & a \leq r \leq b. \end{cases} \quad (6)$$

The coefficients A's are to be determined from the boundary conditions, the field matching condition at  $r = a$  (Subsection A), and the jump condition on  $B_z$  at the beam location  $R_0$ . The jump condition on  $B_z$  at  $R_0$ , in turn, is obtained from the moment equation with the perturbed distribution function. In the present analysis we assume that the equilibrium distribution function  $f_0$  is Lorentzian in the axial momentum  $p_z$ . Namely,

$$f_0 \propto \hat{p}_z \Delta / \left[ (p_z - \hat{p}_z)^2 + \hat{p}_z^2 \Delta^2 \right], \quad (7)$$

where  $\Delta$  refers to the axial momentum spread ratio. We further designate the total electron energy and the average axial (transverse) velocity by  $\gamma mc^2$  and  $c\beta_z$  ( $c\beta_\perp$ ), respectively. The jump condition at  $R_0$ , or equivalently impedance matching across the beam (Choe et al 1981), provides the dispersion relation for the gyrotron.

$$B = \frac{B_N}{B_D} = - \frac{\nu \beta_\perp^2 c^2}{2\gamma R_0^2 \left[ \omega - \omega_B + ic|k|\beta_z \gamma \Delta / \gamma_z^3 \right]^2} \quad (8)$$

where

$$B_N = 2B_1 \quad B_D = -\pi x_0^2 J_1(x_0) \left[ J_1(x_0) B_2 - N_1(x_0) B_1 \right],$$

$$B_1 = J_0(x_a) \left[ \psi_J(x_a) - \phi_1(y_b, y_a) \right],$$

$$B_2 = N_0(x_a) \left[ \psi_N(x_a) - \phi_1(y_b, y_a) \right],$$

$$\begin{pmatrix} x_a^2 \\ x_0^2 \end{pmatrix} = p_0^2 \begin{pmatrix} a^2 \\ R_0^2 \end{pmatrix}, \quad \begin{pmatrix} y_b^2 \\ y_a^2 \end{pmatrix} = q_1^2 \begin{pmatrix} b^2 \\ a^2 \end{pmatrix}, \quad (9)$$

$$\psi_N(x) \equiv N_1(x) / [x N_0(x)],$$

$$\omega_B = kc\beta_z + \omega_c/\gamma, \quad \gamma_z = (1 - \beta_z^2)^{-1/2},$$

and  $\omega_c = eB_0/mc$  is the non-relativistic cyclotron frequency and  $\nu \equiv Ne^2/mc^2$  is the Budker parameter. Here  $N$  is the total number of electrons per unit axial length,  $c$  is the velocity of light, and  $(-e)$  and  $m$  are the electronic charge and mass. The quantities,  $p_0$ ,  $q_1$ ,  $\psi_J$ ,  $\phi_1$ , and  $\Delta$  are previously defined in eqs. (2), (5) and (7). Note that  $B_1 \propto D^{\text{TE}}$  so that the equation (8) recovers the vacuum waveguide dispersion relation (4) when the beam is absent ( $\nu = 0$ ). The dispersion relation (8) can be used to investigate gain and bandwidth of the disk loaded gyrotron amplifier for a broad range of physical parameters. Here we will give only one example in Fig. 3. At the given system parameters ( $\nu = 0.002$ ,  $\beta_1 = 0.4$ ,  $\beta_z = 0.2$ ,  $a/b = 0.3$ ,  $a\omega_c/c = 2.8$ ,  $L\omega_c/c = 3.2$ ,  $R_0\omega_c/c = 2.0$ ), the normalized gain ( $-100 k_i c/\omega_c$ ) versus the normalized frequency ( $\omega/\omega_c$ ) is plotted for several values of the axial velocity spread ( $\Delta$ ). Even without the benefit of the parametric optimization, both the gain and the bandwidth for this disk loaded gyrotron are at least comparable to those for the smooth wall gyrotron. We will leave the parametric optimization as future works.

## III. HELIX LOADED GYROTRON

As illustrated in Fig. 4, the system configuration consists of a sheath helix with radius  $R_h$  located inside a cylindrical conductor at  $R_c$ . We assume that conducting wires in the helix are very fine in texture, thereby replacing the actual helix by a helically conducting sheet. This sheet is perfectly conducting in a helical direction making a pitch angle  $\phi$  with a plane normal to the axis of the system, as shown in Fig. 4. The effect of the helix is then restricting the current over the sheet in  $\phi$  direction, while allowing the fields penetration to  $R_h > r > R_c$ . Again the cylindrical coordinates are used.

Although this helix structure has been investigated before (Pierce 1950, Sensiper 1955, Berezin et al 1960), these studies either neglect the role of the outer conductor, thereby restricting to slow wave propagation only, or concentrate only on the azimuthally symmetric ( $\ell=0$ ) mode. We, therefore, investigate the dispersion characteristics for arbitrary azimuthal mode number ( $\ell \neq 0$ ) including the outer conductor. As before, the vacuum waveguide dispersion relation is obtained and analyzed in subsection A. Two interesting limits, namely as  $R_c \rightarrow \infty$  and as  $R_c \rightarrow R_h$ , are examined. The former recovers previous results and the latter yields clear pictures of the mode identifications. The gyrotron dispersion relation with the electron beam will be derived and some numerical examples will be given in subsection B.

## A. Vacuum Waveguide Dispersion Relation

Since the detailed procedure of the vacuum dispersion relation is given elsewhere (Uhm and Choe 1982a), only the brief outline will be given

here. In anticipation of the presence of the hybrid modes, we express both  $E_z$  and  $B_z$  as a general solution of the wave equation for the Fourier component  $\ell$  (azimuthal mode number),  $k$  (axial wavenumber) and  $\omega$  (frequency). Then the boundary conditions on the wall and on the helix yield the desired dispersion relation.

The primary fields  $E_z$  and  $B_z$  are given by

$$E_z = \begin{cases} A_1^E J_\ell(pr) & 0 \leq r \leq R_h \\ A_2^E [N_\ell(pR_c) J_\ell(pr) - J_\ell(pR_c) N_\ell(pr)] & R_h \leq r \leq R_c \end{cases} \quad (10)$$

$$B_z = \begin{cases} A_1^B J_\ell(pr), & 0 \leq r < R_h \\ A_2^B [N_\ell'(pR_c) J_\ell(pr) - J_\ell'(pR_c) N_\ell(pr)] & R_h < r \leq R_c \end{cases}$$

where

$$p^2 \equiv \omega^2/c^2 - k^2, \quad (11)$$

and the prime ( $'$ ) denotes the derivative of Bessel functions. Other components of the fields are given in terms of  $E_z$  and  $B_z$ . The boundary conditions on the sheath helix ( $r=R_h$ ) are

$$\begin{aligned} \vec{E} \cdot \hat{e}_\phi \Big|_{R_h^\pm} &= 0, \\ \vec{E} \times \hat{e}_\phi \Big|_{R_h^-} &= \vec{E} \times \hat{e}_\phi \Big|_{R_h^+} \\ \vec{B} \cdot \hat{e}_\phi \Big|_{R_h^-} &= \vec{B} \cdot \hat{e}_\phi \Big|_{R_h^+} \end{aligned} \quad (12)$$

where  $\hat{e}_\phi$  is the unit vector in the helix direction  $\phi$ , and  $R_h^\pm$  refers to the evaluation at just inside (-) or just outside (+) the helix surface. The dispersion relation for the vacuum waveguide mode is obtained by combining eqs. (10) and (12). The resultant dispersion relation is given by

$$D = \frac{\omega^2}{c^2} R_h^2 J_\ell'(X_c) J_\ell'(X_h) + X_h^2 t_\ell^2 J_\ell'(X_c) J_\ell(X_h) f = 0 \quad (13)$$

where

$$f = f_N/f_D, \quad t_\ell = \tan\phi - \ell k R_h / X_h^2,$$

$$f_N = J_\ell(X_c) N_\ell(X_h) - N_\ell(X_c) J_\ell(X_h),$$

$$f_D = J_\ell'(X_c) N_\ell'(X_h) - N_\ell'(X_c) J_\ell'(X_h), \quad (14)$$

$$\begin{pmatrix} X_h^2 \\ X_c^2 \end{pmatrix} = p^2 \begin{pmatrix} R_h^2 \\ R_c^2 \end{pmatrix},$$

and  $p^2$  is defined in eq. (11). Note that the sign of  $p^2$  determines whether the wave is fast ( $\omega > ck$ ,  $p^2 > 0$ ) or slow ( $\omega < ck$ ,  $p^2 < 0$ ).

In the limit  $R_c \rightarrow \infty$ , the dispersion relation (13) is further simplified as

$$\frac{\omega^2}{c^2} = -p^2 t_\ell^2 \frac{J_\ell(X_h) N_\ell(X_h)}{J_\ell'(X_h) N_\ell'(X_h)}, \quad (15)$$

which has solutions only when  $p^2 < 0$ . This means that when the outer conductor is removed, only the slow wave ( $\omega < ck$ ) can propagate. The dispersion relation (15) with Bessel functions  $J$  and  $N$  explicitly given by modified functions  $I$  and  $K$

can be found in previous literatures (Pierce 1950, Hutter 1950, Sensiper 1955). More interesting features can be found in the other limit. Namely, on the limiting case when the outer conductor approaches to the helix (i.e.  $R_c \rightarrow R_h$ ), eq. (13) is reduced to

$$J'_\ell(X_c) J_\ell(X_c) \left\{ \frac{\omega^2}{c^2} - [k \sin\phi + (\ell/R_c) \cos\phi]^2 \right\} = 0. \quad (16)$$

From eq. (16), we identify three distinctive solutions; the transverse electric (TE) mode

$$\frac{\omega^2}{c^2} - k^2 = \frac{\alpha_{\ell s}^2}{R_c^2}, \quad (17)$$

the transverse magnetic (TM) mode

$$\frac{\omega^2}{c^2} - k^2 = \frac{\beta_{\ell s}^2}{R_c^2}, \quad (18)$$

and the helix mode

$$\omega = \pm [ck \sin\phi + \ell(c/R_c) \cos\phi], \quad (19)$$

where  $\alpha_{\ell s}$  and  $\beta_{\ell s}$  are the  $s$ th roots of  $J'_\ell(\alpha_{\ell s}) = 0$  and  $J_\ell(\beta_{\ell s}) = 0$ , respectively.

It is remarkable to note from eq. (19) that the helix mode for  $R_c \rightarrow R_h$  is a straight line in the  $(\omega, k)$  space. Thus, when the helix mode with  $R_h/R_c \rightarrow 1$  is coupled with the electron beam mode ( $\omega_B = kc\beta_z + \omega_c/\gamma$ , eq. (9)) for the gyrotron, a super wide band amplifier can be constructed by a choice of appropriate beam parameters satisfying

$$\beta_z = \sin\phi, \quad R_c = \gamma c \ell \cos\phi / \omega_c. \quad (20)$$

In general case where  $R_c/R_h \neq 1$ , there exist two distinguishing kinds of modes; (a) the hybrid waves mainly consisting of a combination of the TE and TM modes and (b) the helix mode. The dispersion relation (14) is numerically solved for  $\omega$  at given  $k$ . Shown in Fig. (5) are plots of the normalized frequency  $\omega R_c/c$  versus the normalized wavenumber  $kR_c$  obtained from eq. (14) for the helix mode,  $\phi = \pi/6$ , (a)  $R_c/R_h = 1.43$  and several values of  $\ell$  and (b)  $\ell = 2$  and several values of  $R_c/R_h$ . We note from Fig. 5(a) that for the  $\ell \neq 0$  helix mode, the dispersion curve for the slow wave region ( $\omega < ck$ ) is continuously connected to that for a portion of fast wave region ( $\omega > ck$ ). On the other hand, the dispersion curve for the  $\ell = 0$  helix mode consists entirely of the slow wave region. As mentioned above, the dispersion curves of the helix mode in Fig. 5(b) approach to the straight lines described by eq. (19) as the parameter  $R_c/R_h$  decreases to unity.

As expected, there are infinite number of the hybrid waves which are identified by the radial node number  $n$ . All of these hybrid modes are fast waves ( $\omega > ck$ ). Figure 6 is the plot of the frequency versus the wavenumber obtained from eq. (14) for the  $n = 1$  hybrid waves,  $\phi = \pi/6$ ,  $R_c/R_h = 1.43$ , and several values of  $\ell$ . Note that the dispersion curves for the  $\ell \neq 0$  hybrid waves is not symmetric about  $k = 0$  line. Additional information on the vacuum dispersion properties are given in our previous paper (Uhm and Choe 1982a).

## B. Gyrotron Dispersion Relation

The dispersion relation for the helix loaded gyrotron in the presence of the electron beam will be derived in this subsection. The thin hollow electron beam, located at  $r = R_0$  ( $0 < R_0 < R_h$ ), is assumed to be embedded in the strong axial magnetic field  $B_0$ . The system configuration is otherwise same as given in Fig. 4.

The detailed derivation of the dispersion is given elsewhere (Uhm and Choe 1982b). The general procedure is similar to that given in Sec. II B. Within the framework of the linearized Maxwell-Vlasov system, the perturbed fields in the vacuum region are given as general solutions of the wave equation similar to eq. (10), and the boundary condition on the helix (eq. (12)) and the jump condition on  $B_z$  across the beam location yields the dispersion relation. The jump condition is given by the moment equation of the perturbed distribution function, which is computed from the equilibrium distribution function given by eq. (7).

Then we finally obtain the dispersion relation for the Fourier component  $\ell$  (azimuthal),  $k$  (axial wavenumber), and  $\omega$  (frequency) in the helix loaded waveguide.

$$B = \frac{B_N}{B_D} = - \frac{v\beta_I^2 c^2}{2\gamma R_0^2 \left[ \omega - \omega_B + ic|k|B_z \gamma \Delta / \gamma_z^3 \right]^2}, \quad (21)$$

where

$$B_N = 2B_1, \quad B_D = -\pi X_0^2 J_{\ell-1}(X_0) \left[ J_{\ell-1}(X_0) B_2 - N_{\ell-1}(X_0) B_1 \right].$$

$$B_1 = \frac{\omega^2}{c^2} R_h^2 J_\ell(X_c) J'_\ell(X_h) f_D + X_h^2 t_\ell^2 J'_\ell(X_c) J_\ell(X_h) f_N,$$

$$B_2 = \frac{\omega^2}{c^2} R_h^2 J_\ell(X_c) N'_\ell(X_h) f_D + X_h^2 t_\ell^2 N'_\ell(X_c) J_\ell(X_h) f_N \quad (22)$$

$$- k R_h X_h t_\ell f_D f_N,$$

$$X_0^2 = p^2 R_0^2.$$

Here the quantities,  $X_h$ ,  $X_c$ ,  $f_D$ ,  $f_N$ ,  $t_\ell$  and  $p^2$  are defined in eqs. (14) and (11). The beam mode  $\omega_B$  is defined in eq. (9) and the axial velocity spread ratio  $\Delta$  appears in eq. (7). We note that in the limit of  $v \rightarrow 0$ , the dispersion relation (21) recovers the vacuum waveguide dispersion equation (13) (i.e.  $B_1 \propto D$ ). The dispersion relation in eq. (21) can be used to investigate gain and the bandwidth of the helix loaded gyrotron amplifier for a broad range of physical parameters.

In the remainder of this subsection we show several numerical examples of the gyrotron gain ( $k_i$ ) versus the frequency with assumed beam parameters,  $v=0.002$ ,  $\beta_1 = 0.4$ ,  $\beta_z = 0.2$ . In order to illustrate the broad band amplification in a helix loaded waveguide, Fig. 7 shows a plot of the normalized gain ( $-100k_i c/\omega_c$ ) versus the normalized frequency  $\omega/\omega_c$  obtained from eq. (21) for the helix mode,  $\Delta = 2\%$ ,  $R_c/R_h = 1.1$ ,  $R_0 = R_h - r_L$ , and optimum values of the parameters  $(R_h \omega_c/c, \phi)$  for each azimuthal harmonic number  $\ell$ . The optimum values of the parameters  $(R_h \omega_c/c, \phi)$  are given by  $(1.04, 10.6^\circ)$  for  $\ell = 1$ ,  $(2.09, 11.0^\circ)$  for  $\ell = 2$ ,  $(3.15, 11.0^\circ)$  for  $\ell = 3$  and  $(4.21, 11.0^\circ)$  for  $\ell = 4$ . The normalized electron Larmor radius is  $r_L \omega_c/\bar{c} = 0.447$ . As expected in previous subsection, utilizing the helix mode for  $R_h/R_c \approx 1$ , it is shown that a super wide band gyrotron amplifier is attainable for  $\beta_z \approx \sin\phi$  and  $R_c \approx \gamma \ell \cos\phi / \omega_c$  (eq. (20)). For example, for  $\ell = 2$  and  $\Delta = 2\%$  in Fig. 7, the amplifier bandwidth is more than 60%. Here, the bandwidth is defined by the full width of the real frequency, at which the linear gain drops to  $\exp(-1/2)$  of its maximum value, normalized by the mean frequency. When the axial velocity spread  $\Delta$  is increased, the gain and bandwidth are considerably reduced. However, for  $\ell = 2$ , the bandwidth of the gyrotron amplifier is found to be still more than 40% for  $\Delta = 4\%$ . We can conclude, therefore, the helix mode amplifier is a very effective means to amplify a broad band microwave signal.

In addition to the helix mode, the fast hybrid mode can be used for the gyrotron amplifier. As a typical example of the hybrid wave utilization, Fig. 8 presents plots of the gain versus the frequency for  $\ell = 0$ ,  $n = 1$ ,  $R_0 = R_h - r_L$ , and the geometric parameters  $R_c/R_h = 1.5$ ,  $R_h \omega_c/c = 2.25$  and  $\phi = -60^\circ$ , which satisfy the grazing condition. Also shown in the horizontal line is  $k_b c/\omega_c = \omega/\omega_c - 1/\gamma$ . Although the vacuum waveguide mode for  $(\ell, n) = (0, 1)$  is originated from the TM mode, the maximum gain in Fig. 8 is very similar to that for the ordinary gyrotron where the beam mode couples with the TE mode. This strongly indicates that the hybrid wave for  $(\ell, s) = (0, 1)$  TE and TM modes in eqs. (17) and (18). The fast wave wide band amplification (Lau and Chu 1981) in a helix loaded waveguide is currently under investigation by authors, utilizing these hybrid waves as an amplification mechanism and the helix mode as a signal carrier. The general behavior of the gyrotron gain remains the same for the hybrid modes with  $\ell \neq 0$ .

## IV. CONCLUSION

In this paper we have investigated the gyrotron amplifiers in a disk and a helix loaded waveguides. For each slow wave structure, the vacuum waveguide mode is derived and analyzed, and the gyrotron dispersion relation is obtained.

The disk loaded waveguide is discussed in Sec. II. The dispersion characteristics of the azimuthally symmetric TE mode are examined and compared with those of the TM mode in Sec. IIA. It has been found that the low cutoff frequency of the disk loaded TE mode is higher than that for the smooth wall, and that the group velocity of the wave can be easily adjusted by disk parameters. In Sec. IIB, the gyrotron dispersion relation in the disk configuration is obtained and a numerical example of the gain is given. The gain and the bandwidth of the disk loaded gyrotron is at least comparable to those for the smooth wall gyrotron.

In Sec. III, the helix loaded gyrotron is examined. The analysis of the vacuum waveguide mode reveals that the helix configuration supports two distinctive modes; the fast wave hybrid modes and the helix mode. In particular, when the outer conductor is very close to the helix, the helix mode becomes a straight line in the dispersion  $(\omega, k)$  space. From Sec. IIB, it is shown that, by proper choice of the helix parameters, the bandwidth of the gyrotron utilizing the helix mode can be very wide, in excess of 40% even for 4% of the velocity spread. Also, by coupling with the hybrid mode and using the helix wave as a signal carrier, the hybrid mode gyrotron can be used as one of fast wave wide band schemes.

V. ACKNOWLEDGEMENT

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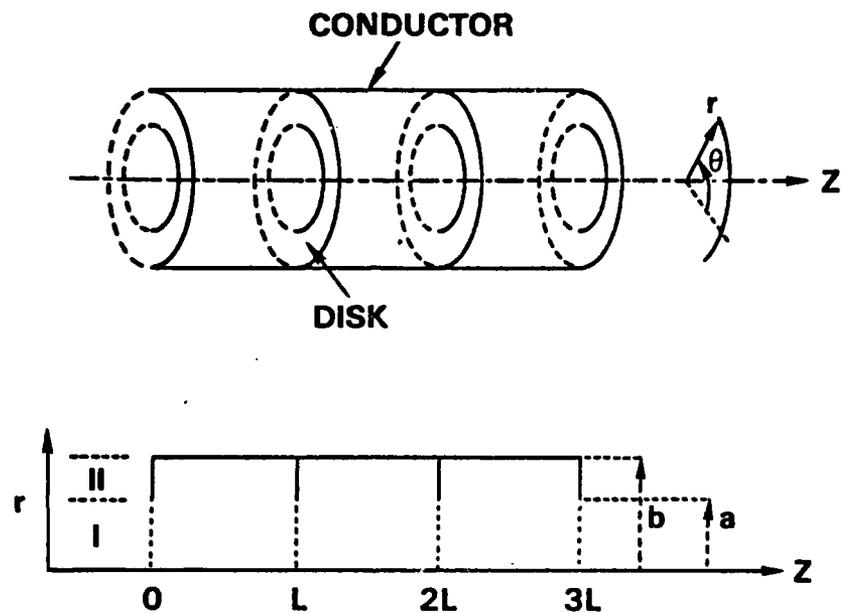


FIGURE 1. SYSTEM CONFIGURATION OF A DISK LOADED WAVEGUIDE

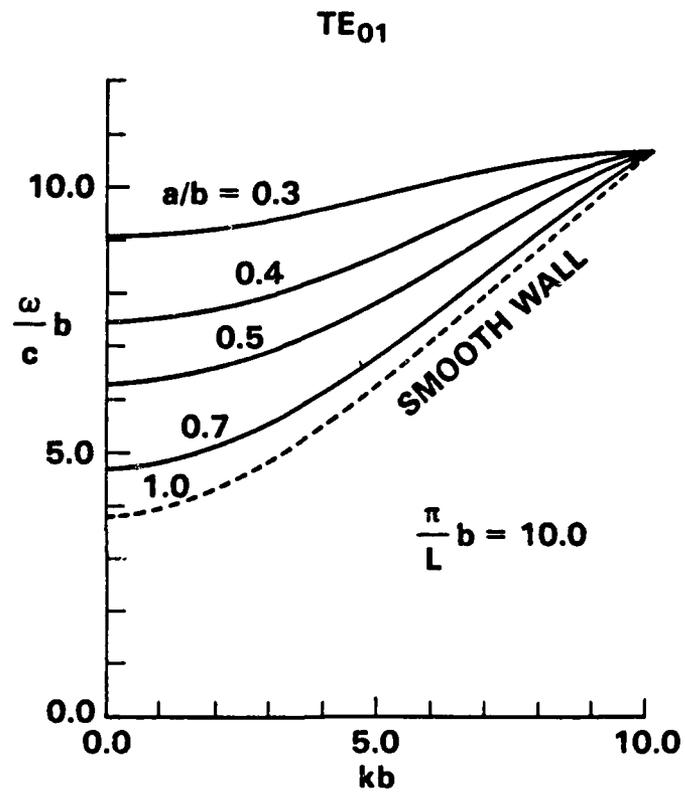


FIGURE 2A. DEPENDENCE OF THE DISPERSION ON THE DISK GEOMETRY (A/B)

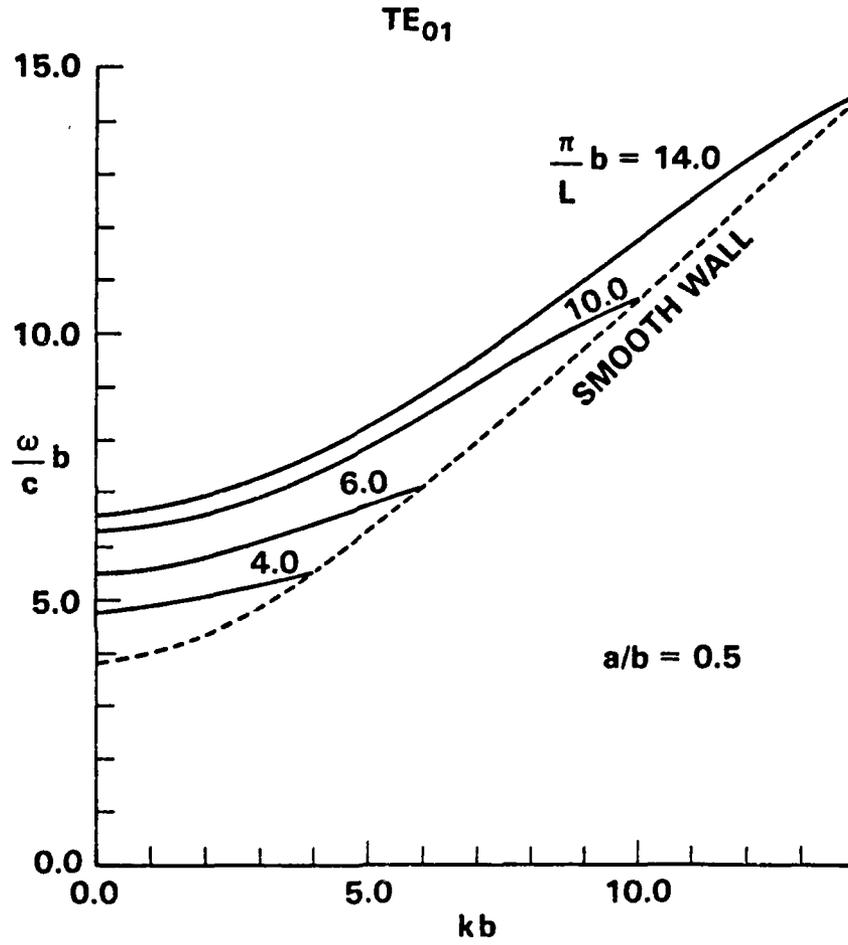


FIGURE 2B. DEPENDENCE OF THE DISPERSION ON THE PERIOD (L)

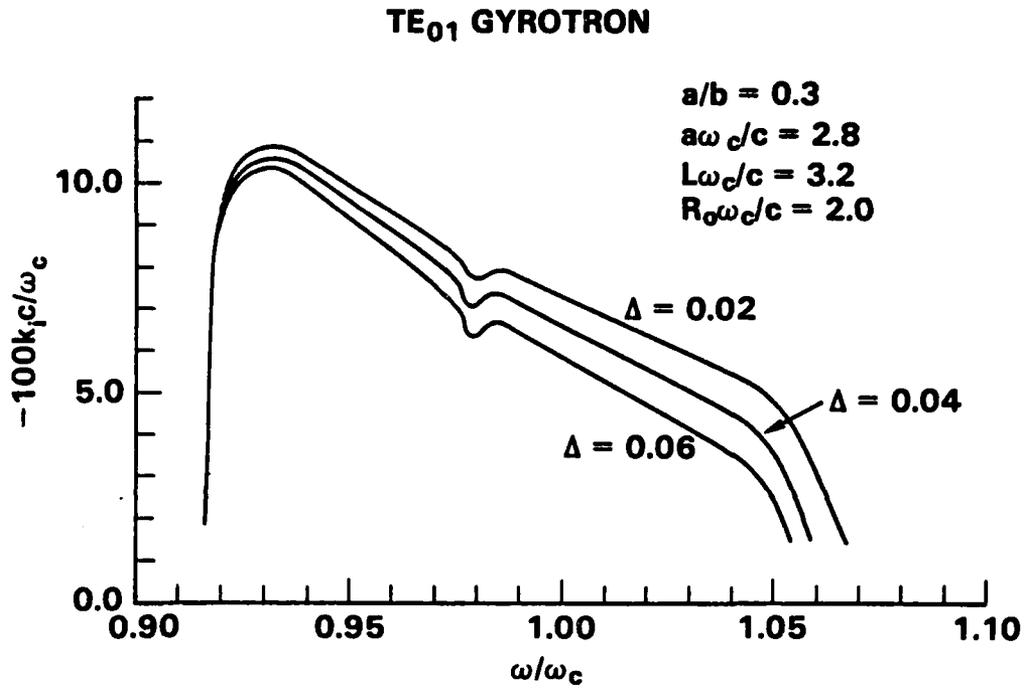


FIGURE 3. AN EXAMPLE OF THE DISK LOADED GYROTRON AMPLIFIER. THE NORMALIZED GAIN ( $-100 k_p c / \omega_c$ ) FOR SEVERAL VALUES OF THE AXIAL VELOCITY SPREAD ( $\Delta$ ) IS PLOTTED AGAINST THE NORMALIZED FREQUENCY ( $\omega/\omega_c$ )

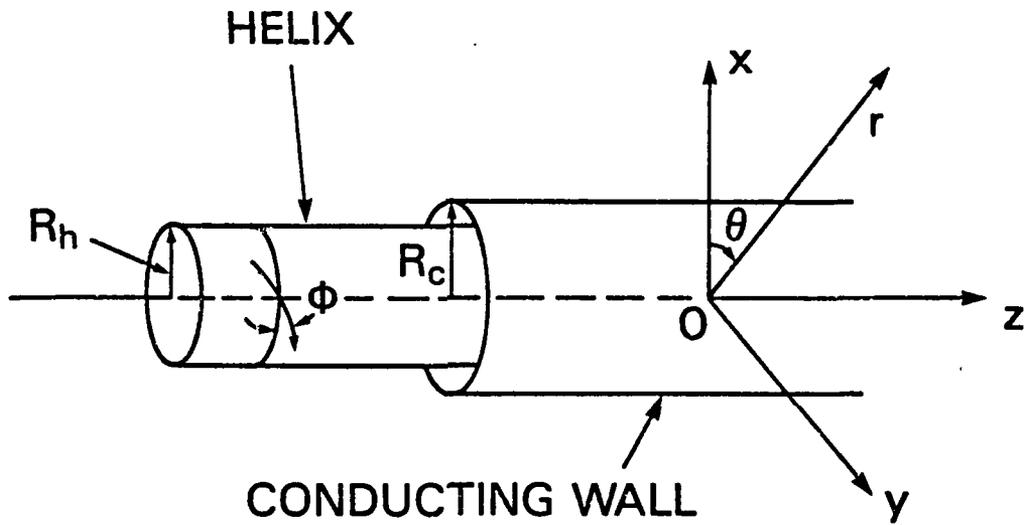


FIGURE 4. SYSTEM CONFIGURATION OF A SHEATH HELIX LOADED WAVEGUIDE

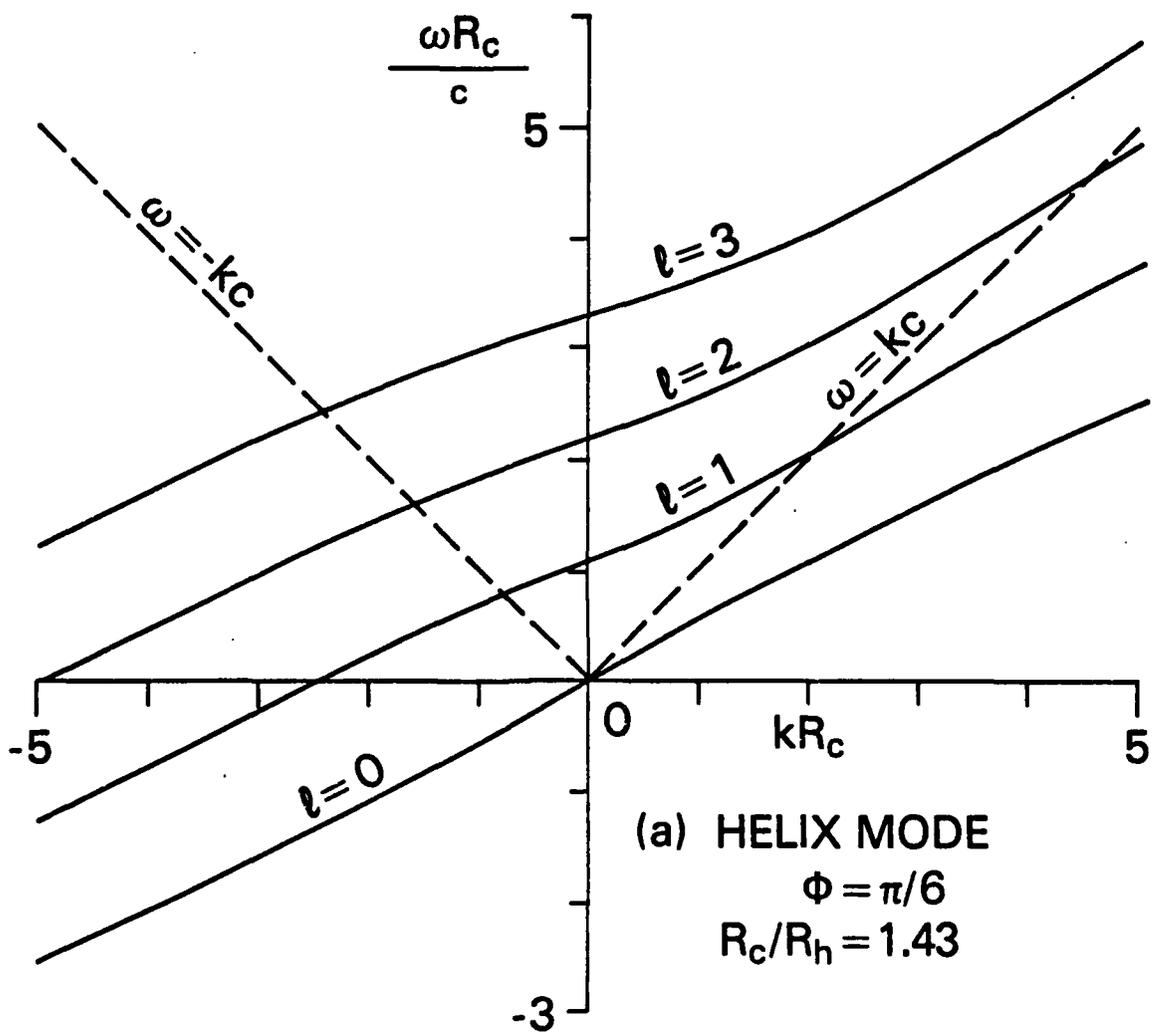


FIGURE 5A. PLOTS OF DISPERSION CURVES FOR THE HELIX MODES WITH  $\phi = \pi/6$ ,  $R_0/R_h = 1.43$  FOR SEVERAL VALUES OF  $l$

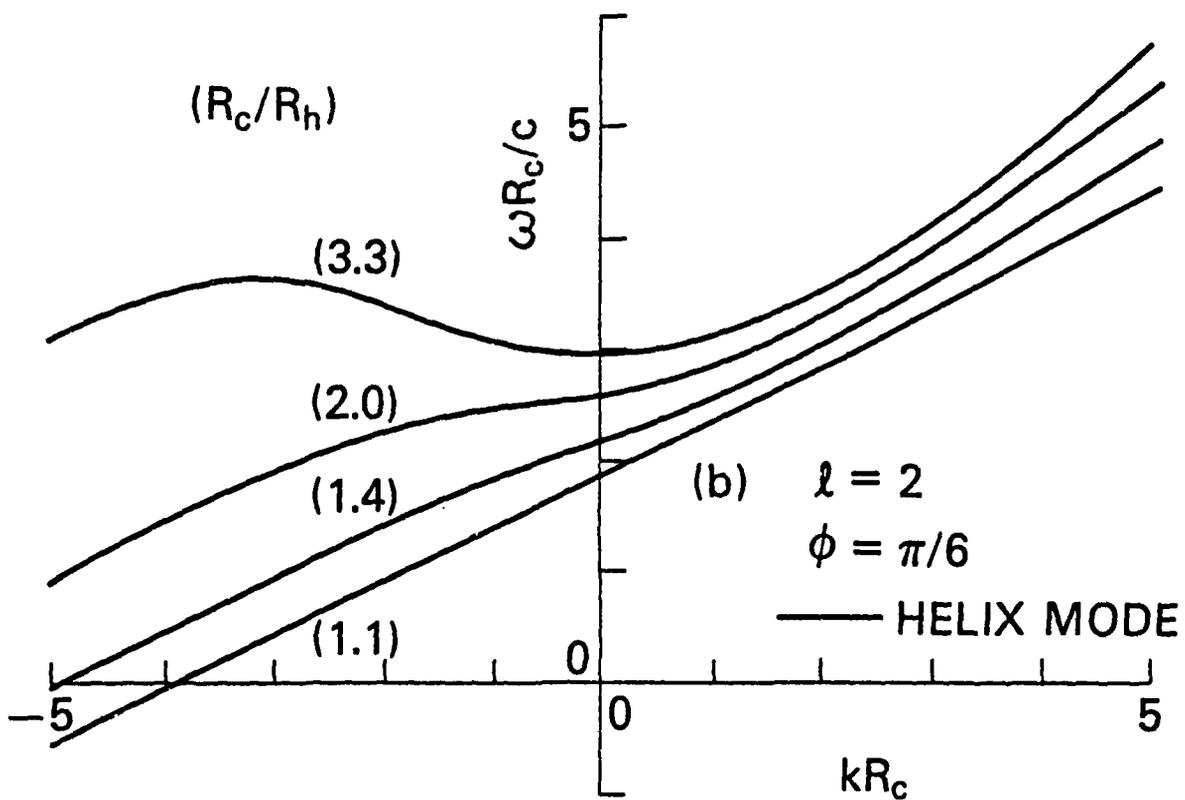


FIGURE 5B. PLOTS OF DISPERSION CURVES FOR THE HELIX MODES WITH  $\phi = \pi/6, l = 2$  FOR SEVERAL VALUES OF  $R_c/R_h$

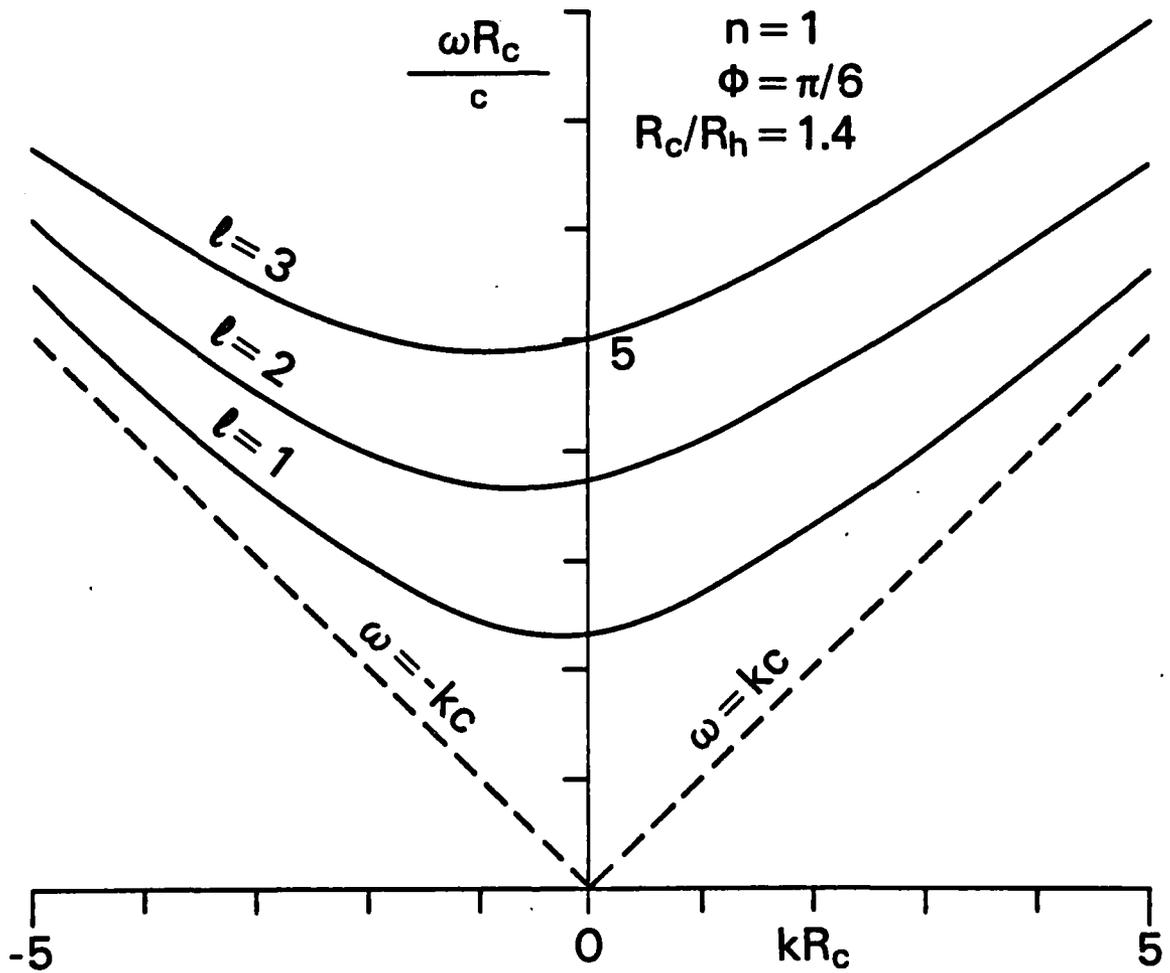


FIGURE 6. PLOTS OF DISPERSION CURVES FOR THE  $n = 1$  HYBRID MODES WITH  $\phi = \pi/6$ ,  $R_c/R_h = 1.4$  FOR SEVERAL VALUES OF  $l$

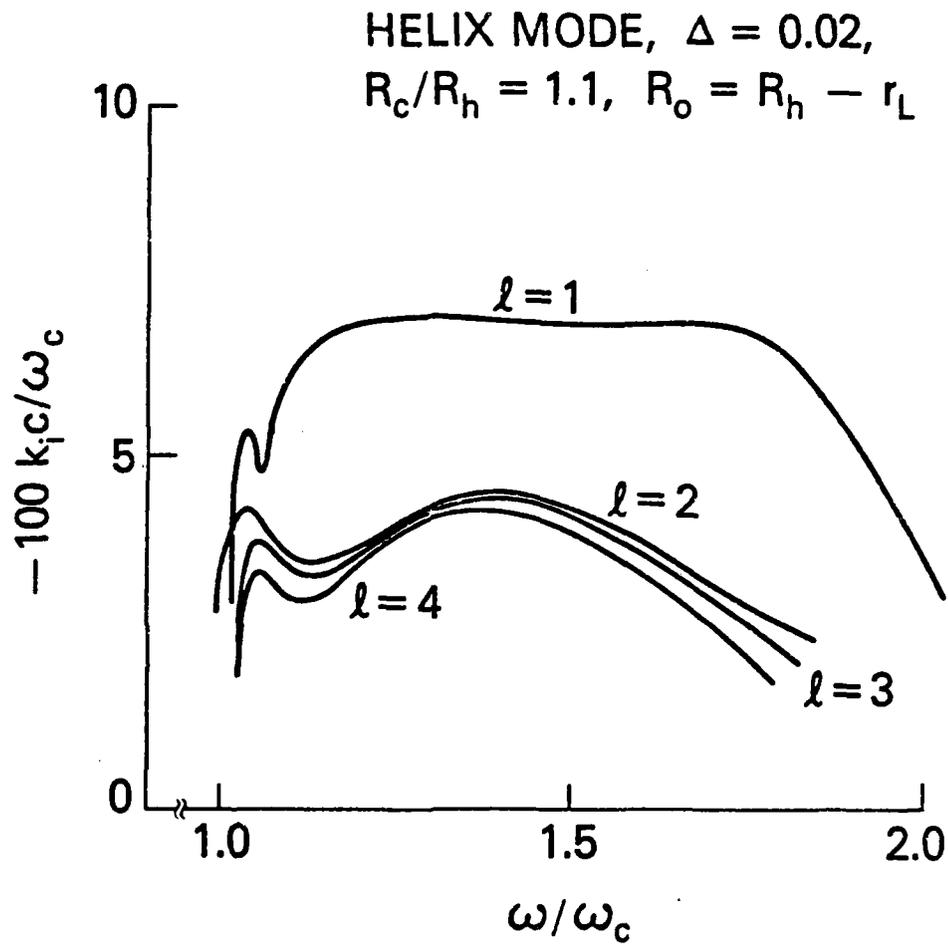


FIGURE 7. PLOTS OF THE GAIN VERSUS THE FREQUENCY FOR THE HELIX MODE WITH  $\Delta = 2\%$ ,  
 $R_c/R_h = 1.1$ ,  $R_o = R_h - r_L$  FOR SEVERAL VALUES OF  $\ell$

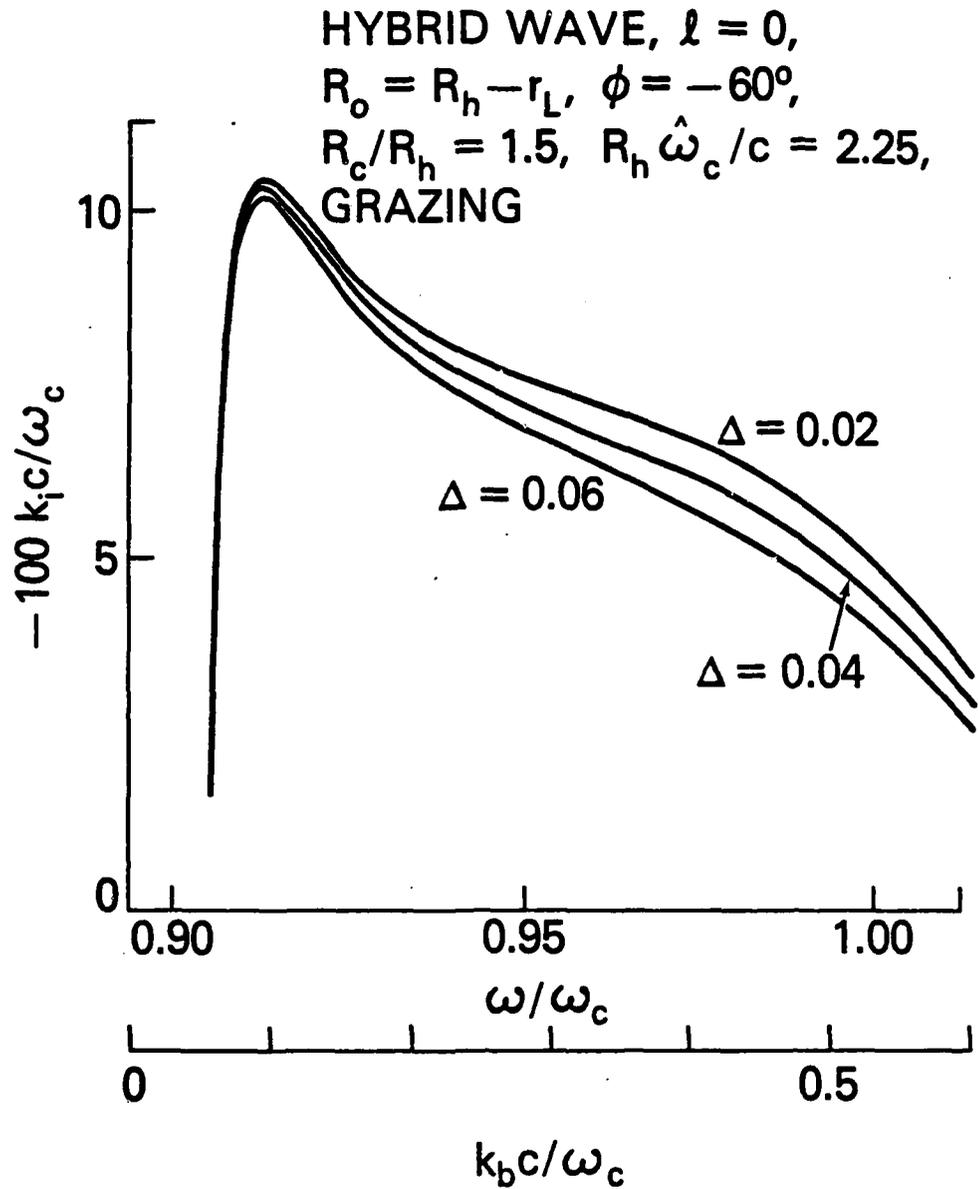


FIGURE 8. PLOTS OF THE GAIN VERSUS THE FREQUENCY FOR THE  $n = 1$  HYBRID WAVE WITH  $\ell = 0$ ,  $R_o = R_h - r_L$ ,  $\phi = -60^\circ$ ,  $R_c/R_h = 1.5$ ,  $R_h \omega_c/c = 2.25$  FOR SEVERAL VALUES OF  $\Delta$

## BIBLIOGRAPHY

- Berezin, A. K., Zeidlits, P. M., Nekhrshevich, A. M., and Silenok, G. A., 1960, Soviet Phys. Tech. Phys., 4, 730.
- Choe, J. Y., and Uhm, H. S., 1982, IEEE Int'l. Conf. on Plasma Science, Conf. Rec., 62.
- Choe, J. Y., Uhm, H. S., and Ahn, S., 1981, J. Appl. Phys., 52, 4508; and references therein.
- Chu, E. L., and Harsen, W. W., 1947, J. Appl. Phys., 18, 996.
- Flyagin, V. A., Gaponov, A. V., Petelin, M. I., and Yulpatov, V. K., 1977, IEEE Microwave Theory Tech., MTT-25, 514; and references therein.
- Hirschfield, J. L., and Granatstein, V. L., 1977, IEEE Microwave Theory Tech., MTT-25, 528; and references therein.
- Hutter, R. E. G., 1960, Beam and Wave Electronics in Microwave Tubes, Van Nostrand, New York.
- Lau, Y. Y., and Chu, K. R., 1981, Int'l. J. Infrared and Millimeter Wave, 2, 415.
- Pierce, J. R., 1950, Traveling-Wave Tubes, Van Nostrand, New York.
- Sensiper, S., 1955, Proc. IRE, 43, 149.
- Slater, J. C., 1950, Microwave Electronics, Van Nostrand, New York.
- Uhm, H. S., and Choe, J. Y., 1982a, Properties of the electromagnetic wave propagation in a helix loaded waveguide (submitted for publication); 1982b, Gyrotron amplifier in a helix loaded waveguide (submitted for publication).

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