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ABSTRACT

This thesis develops a straightforward and accurate method to determine mechanical heating system changeover timing. Transitional season weather causes buildings to stay within acceptable thermal comfort ranges without requiring supplemental heating. Significant energy savings can be realized if heating plants can be shut down during periods they are not required. The term "trigger temperature" is used to describe the minimum acceptable comfort conditions which must be maintained before changeover can be made. Computer simulation of ninety-four hypothetical office buildings is used to record data for hourly building temperatures. Statistical regression analysis techniques are employed to analyze the data and develop temperature prediction models for a range of building envelopes and occupancy schedules. Hand calculation and micro-computer applications are offered to provide changeover decision criteria for facility managers using this method.

Key words for this thesis are: transitional seasons, changeover timing, regression analysis, thermal comfort, and Trigger Temperature Method.
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A Methodology for Determining Building Heating System Changeover Timing

'A Thesis in
Architectural Engineering
by
William A. Formwalt

Submitted in Partial Fulfillment
of the Requirements
for the Degree of

Master of Science
August 1982

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Professor of Architectural Engineering,
Thesis Advisor

26 July 1982

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26 July 1982

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Louis F. Geschwindner, Jr.
Assistant Professor of Architectural Engineering
This thesis develops a straightforward and accurate method to determine mechanical heating system changeover timing. Transitional season weather causes buildings to stay within acceptable thermal comfort ranges without requiring supplemental heating. Significant energy savings can be realized if heating plants can be shut down during periods they are not required. The term "trigger temperature" is used to describe the minimum acceptable comfort conditions which must be maintained before changeover can be made. Computer simulation of ninety-four hypothetical office buildings is used to record data for hourly building temperatures. Statistical regression analysis techniques are employed to analyze the data and develop temperature prediction models for a range of building envelopes and occupancy schedules. Hand calculation and micro-computer applications are offered to provide changeover decision criteria for facility managers using this method.

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Sincere appreciation is extended to Professors Gifford H. Albright, Luis H. Summers, and Louis F. Geschwindner Jr. for their expert advice and assistance throughout the course of my studies and research. Special appreciation is extended to my thesis advisor, Professor Stanley F. Gilman, for the invaluable advice, technical expertise, and enthusiastic support he has given me. I am indebted to Stephen A. Hathaway, Captain Frank J. Tustin, and Freddie L. Beason of The United States Air Force Engineering and Services Center for their timely support which made this research possible, and to Captain Steven D. Heinz of The United States Air Force MX/AFRCE for his numerous insights in building energy analysis techniques. Appreciation is also extended to The Department of Statistics, Statistical Consulting Service, for their advice in statistical analysis, to Edward J. Hull of the Computer-Aided Design Laboratory for his advice in computer programming applications, and to J. Carrol Dean of the Department of Physical Plant for his assistance and advice on building energy use.
CHAPTER ONE

INTRODUCTION

Since the Oil Embargo of 1973, social, economic, and political pressures have underscored the need for energy conservation throughout the world. The recent reduction in crude oil prices has been directly linked with the conservation efforts at work during the past year. The resultant reduction in energy demand has created an oil surplus: a gap between the demand and available supplies. One major contribution in reducing energy consumption has come from the energy conservation accomplishments in building design and operation. From the Federal Energy Administration indoor temperature guidelines established in 1974, there has been a conscientious effort to make buildings more "energy efficient" without sacrificing the comfort of the occupants. Increasing attention is being given to annual energy costs of existing and proposed facilities.

Many different efforts have been directed toward reducing building energy consumption. Improvements have been made in the operating efficiency of heating, ventilation, and air-conditioning (HVAC) equipment, and
facility managers and owners have concentrated on tightening the building thermal envelope. Engineering analysis methods have been developed to maximize energy efficiency. These techniques range from simple energy audits which track fuel consumption to sophisticated computer controlled energy monitoring systems. One area which has not received much attention is that related to facility energy use during transitional seasons.

**Background**

A critical weather transition period occurs each Spring and Fall for facilities in temperate climates. At this time, the startup or shutdown of the facility heating plant must be considered. The timing of this "changeover" is critical because it directly affects the annual energy consumption of the building. In addition, it is often an irreversible decision which may adversely limit the comfort for the facility occupants. It is important that the timing of the changeover reflects a careful balance between maintaining an acceptable thermal comfort within the building and the economic pressures to save on energy bills when fuel costs are high. The potential for savings lies in a changeover timing which avoids costs associated with running and maintaining a heating plant during a period without any heating requirements. When the facility is
heated by a central plant, the savings potential is the greatest.

Where a central heating plant serves several facilities, the changeover timing has additional impact on energy use and potential savings. Central plants must be prepared for heating load requirements which may not occur. In addition, losses occur in the distribution network serving all facilities. Central heating plants are often constructed where one organization owns and operates all of the facilities in the distribution network. This situation is common on university campuses and military installations as well as in industrial complexes, yet no simple method has been created for changeover estimation. For instance, the United States Air Force has no existing method to use for its numerous (over 100) locations around the world. Nor does ASHRAE, which provides many of the engineering design standards for HVAC equipment, describe a changeover estimation method in any of its publications. The purpose of this thesis is to propose a procedure from which a changeover decision process may be developed.

Objectives

The objective of this thesis is to develop a simple and accurate method to determine changeover dates for office type buildings, by predicting how the buildings will perform
during transitional seasons. It is intended that this method would be used by facility manager and engineer alike when making building energy analyses.

Research will be comprised of the following steps:

1. Evaluate facility manager needs for a changeover methodology from input information to end use.
2. Review existing changeover estimation techniques and their present applications.
3. Use heat balance engineering analysis methods to determine how a range of office type buildings perform during the transitional seasons.
4. Determine the most critical weather, building envelope, and occupant use characteristics affecting the building changeover conditions.
5. Employ statistical regression techniques to predict internal building temperatures.
6. Integrate weather and user input data into the model developed and establish its accuracy and range of application.

Limitations

The methodology developed in this thesis is limited to determining the changeover date for mechanical heating systems only. The changeover decision is based upon building temperatures during the hours of 6am to 10am.
Occupancy schedules used in this research have been developed by studying the weekdays of Tuesday through Friday in a five-day work week. Data generated for the statistical portion of the research are limited to slab on grade single story medium density masonry structures with office type occupancies. Outdoor temperatures used have daily ranges of from 10 F to 30 F, and solar data is typical of from 35 to 45 degrees North or South latitude locations. Applications for weather or building types outside these limits have not been validated by the statistical model developed as part of this thesis.

**Contribution**

The contribution of this thesis is the development of a method to quickly and accurately determine building heating system changeover dates. This methodology also provides the user with a technique to assess the impact of differing changeover dates on each facility by predicting how each will perform without a heating plant. Although established and accepted methods are available to calculate building performance under these conditions, there is no simple yet accurate approach which accounts for heat gains due to solar radiation and the time lag effects of building thermal mass. These thermal gains and losses are critical if an accurate building temperature is to be calculated for use in making
changeover decisions. The development of a simple and precise model to determine building changeover dates offers the area of energy management a valuable tool to conserve energy without sacrificing building occupant comfort.

**Overview**

The development of this thesis is presented in the following chapters: Chapter Two reviews facility manager needs when estimating building changeover and describes possible engineering applications. Chapter Three reviews several existing methods which could be used to make changeover date estimations. Chapter Four details the statistical analysis procedures which are used to establish building temperature prediction models. Chapter Five integrates the statistical models into the Trigger Temperature Method for determining changeover timing and provides examples to demonstrate the method's capabilities and applications. Chapter Six offers conclusions and recommendations for future research.
CHAPTER TWO

FACILITY MANAGER NEEDS

The responsibility for an organization's building operation and maintenance program is typically under the central control of the facility manager. The facility manager may direct the needs for a single building or an entire industrial complex. In order to maximize potential energy savings, a changeover method should provide him with a means to ensure buildings are heated adequately, as well as efficiently. Energy savings can be realized if heating plants can be shut down during periods they are not required. An ideal analysis method would offer flexibility in approach, be straightforward and simple in application, yet have a high degree of accuracy when estimating changeover timing.

Method Flexibility

Changeover concepts are addressed by large and small organizations alike. Although the scope of application may differ, any changeover method would need to include buildings of varying size, construction, occupant use, and site conditions. It should apply to older, less efficient
buildings, as well as newer, energy efficient ones. As older buildings are upgraded to be thermally more efficient, their performance during the changeover seasons is altered. A system of changeover analysis should be able to adjust to these energy upgrades.

**Application Simplicity**

A changeover method should be straightforward and easily applied for a multitude of facilities. Facility management organizations are not always staffed to do detailed energy analyses and must concentrate primarily on the maintenance and running of the "physical plant". This puts a limit on the time and engineering expertise which may be available for changeover estimation. Each hour added to this estimation process by extensive and time consuming engineering calculations is an hour which can be spent in other areas of energy conservation.

Typically, facility management for smaller organizations is not staffed with engineers to perform changeover analysis. This responsibility may rest with central heating plant managers or individual building custodians. They need a method which does not rely upon the expertise of architects or engineers trained in energy analysis techniques. Simplicity and ease of use is their primary concern. Regardless of the end user within a
facility management organization, a changeover method should offer an accuracy level sufficient to ensure thermal comfort for the building occupants.

**Accuracy and Accountablility**

When estimating changeover timing, the accuracy of any method is a function of several parameters. The most accurate method of analysis would be one derived from observations of actual facilities in operation. This is an impracticable approach, however, because it would not be cost effective to gather data from test facilities operated without any heating supply. A more reasonable approach which sacrifices little accuracy is one which employs scientific analysis methods based upon engineering research studies. For exacting engineering analysis techniques, accuracy becomes primarily a function of the input data used. For example, weather data is one uncontrollable factor which can limit the accuracy of an otherwise sound analysis method. Another accuracy constraint is the time interval for which a method predicts changeover.

A method which determines changeover dates on a monthly basis does not offer the sensitivity needed to be of much value to the user. On the other hand, one which can pinpoint this date to a single day of the month may not be considering daily weather fluctuations. The ideal method
would consider at least weekly weather trends, yet retain sufficient precision to determine occupant comfort conditions.

Occupant comfort is the most important accountable item in a changeover analysis. The concept of a changeover date negates all of the reasons buildings are heated in the first place if it cannot in some way estimate whether or not people will be comfortable. Occupant comfort should be recorded in some way so that changeover conditions can be determined as a function of a specified comfort condition. There are several methods which can be used to assess thermal comfort for occupants. The relative merits for these methods are covered in Chapter Three.
CHAPTER THREE

CHANGEOVER ESTIMATION TECHNIQUES

Building changeover dates can be estimated in several ways. The historical data approach uses records of changeovers from previous years as a data base from which future predictions may be made. Engineering calculations may be made for either steady state or transient thermal conditions to determine the optimal changeover date. The end goal in all cases is to assess when weather conditions have established a situation where there is no longer a facility heating requirement.

Historical Data

The simplest approach uses historical data as the basis for estimating changeover timing. This general procedure employs past records of weather and building performance to predict future trends. The number of years observations have been taken is an important facet of this approach. Records for each facility are kept of past years' changeover dates. When the heating plant is turned off (or on), a record is made of how this timing affected the facility occupants. The facility manager assumes that if no
complaints are received, the changeover date chosen was acceptable. Weather data for this period is recorded and compared with weather from previous observations. The goal for the coming seasonal changeover is then selected as a compromise between energy conservation goals and the number of "too cold" complaints from the occupants.

In application, this management by exception approach has several limitations. Building temperatures cannot be determined, and occupant thermal discomfort can be predicted only indirectly. In addition, accuracy in this approach is primarily a function of the quantity of previously recorded observations. Unfortunately, this method rarely accumulates enough sample years to be of much value.

As a facility's use changes or architectural modifications are made, the thermal performance of the facility also changes. Added insulation or new occupancy hours will change how a building will react to the environment. As a result of any changes, the previous years' records become invalid predictors for future performance. With recent efforts to insulate and improve thermal performance of his buildings, a facility manager may find that it is never possible to accumulate enough data years using the historical data method. A more useful and scientific approach involves using engineering heating load calculations to estimate changeover timing.
Steady State Analysis

Steady state analysis is the most widely used and accepted method to determine heating transfer rates (ASHRAE, 1981). Steady state building load calculations are made by assuming that the rate of heat flow through a building component is constant over a period of time and that the rate of flow can be approximated by comparing the potential energy differences at the beginning and end of the period (usually one hour). The thermal transmittance, or U-value, is the coefficient of heat transmission for the material through which the heat is passing (ASHRAE, 1981). Table 3-1 lists ASHRAE steady state equations used for estimating building heat gains and losses.

Balance Point Temperature

The weather condition which causes a building's heat gains to be equal to its heat losses is referred to as the facility's balance point. The outside dry bulb temperature under these conditions is called the balance point temperature (BPT). For residential construction, this has typically been 65°F, but the greater internal loads due to lighting and occupants cause office type facilities to have much lower values (ASHRAE, 1981). By calculating the balance point temperature, conditions can be determined when no net heat will be required.
Table 3-1

<table>
<thead>
<tr>
<th>Component</th>
<th>Steady state equation</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Envelope</td>
<td>$UA \times (IDBT - ODBT)$</td>
<td>Btuh ( - )</td>
</tr>
<tr>
<td>Infiltration</td>
<td>$1.1 \times CFM \times (IDBT - ODBT)$</td>
<td>Btuh ( - )</td>
</tr>
<tr>
<td>Ventilation</td>
<td>$1.1 \times CFM \times (IDBT - ODBT)$</td>
<td>Btuh ( - )</td>
</tr>
<tr>
<td>Occupancy</td>
<td>$255 \times \text{PEOPLE}$</td>
<td>Btuh ( + )</td>
</tr>
<tr>
<td>Lights and equipment</td>
<td>$3.413 \times \text{WATTS}$</td>
<td>Btuh ( + )</td>
</tr>
</tbody>
</table>

where $*$ denotes multiplication

- $\text{Btuh} = \text{Btu/hour heat gains ( + ) or losses ( - )}$
- $UA = \text{U-value*area of the envelope component}$
- $IDBT = \text{indoor dry bulb temperature}$
- $ODBT = \text{outdoor dry bulb temperature}$
- $\text{PEOPLE} = \text{number of facility occupants}$
- $\text{WATTS} = \text{the total internal electric load in watts}$

Note: 255 Btuh per person is sensible heat only.
An application of the BPT concept can be demonstrated in an example problem:

At the balance point temperature, building heat losses are matched by gains, where:

\[
\text{Heat losses} = \text{Transmission} + \text{Infiltration} \\
\text{Heat gains} = \text{Lights} + \text{People} + \text{Solar}
\]

Table 3-2 lists the building data for a 2000 sf modern construction office building.

Table 3-2
Balance Point example building

<table>
<thead>
<tr>
<th>Component</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Transmission</strong></td>
<td></td>
</tr>
<tr>
<td>Walls</td>
<td>Area, sf</td>
</tr>
<tr>
<td>Glass</td>
<td>1600</td>
</tr>
<tr>
<td>Roof</td>
<td>2000</td>
</tr>
<tr>
<td><strong>Infiltration</strong></td>
<td></td>
</tr>
<tr>
<td></td>
<td>130 cu ft/min</td>
</tr>
<tr>
<td><strong>Occupants</strong></td>
<td></td>
</tr>
<tr>
<td></td>
<td>16 people</td>
</tr>
<tr>
<td><strong>Lights</strong></td>
<td></td>
</tr>
<tr>
<td></td>
<td>2.2 watts/sf</td>
</tr>
</tbody>
</table>

Using this data to calculate the building's balance point temperature, the building indoor temperature must first be set. If an indoor setting of 72°F is used,

\[
\text{Heat losses in MBtuh} = 503*(72-\text{DBT}) \\
\text{Heat gains in MBtuh} = 19,097.0
\]
By setting the gains and losses equal,

\[ \text{ODB} = \text{balance point temperature} = 34.0 \, \text{F} - \text{Solar} \]

The balance point method has some limitations when used for estimating changeover timing. The thermal gains from solar and the time delayed gains from the building mass cannot be determined by steady state analysis techniques.

Solar Gains

Thermal gains due to the sun can be a significant portion of the total heat gain for a facility. Solar gain alone may reduce the annual heating load by 10 - 15 \% for an office building having an eight-to-one ratio of building floor area to south-facing glass area (Balcomb, 1980). However, due to the transient nature of solar conditions, these gains cannot be calculated using steady state equations. Figure 3-1 shows how the load profiles for the previous example problem would be affected if solar gains were considered. Steady state analysis methods are also unable to account for the thermal capacitance effects caused by a building's mass.

Thermal Capacitance Effects

The capacitive effect of a building is another significant contribution to the building thermal balance.
Figure 3-1. Building load profiles
Each hour of the day, thermal energy is being stored and released by the building roof, slab, walls and partitions. During the occupied hours, this building mass absorbs heat from the lights and sun as well as the ambient air. After the lights are turned off the stored heat is released to the space as the processes reverses during the unoccupied hours.

The amount of heat which can be stored in and released by the building thermal mass will depend upon many factors, including the building construction and interior layout.

Though widely used for load calculations, steady state heat transfer analysis is limited because it cannot account
for solar gains and thermal mass capacitance effects inherent in a structure. It lacks accuracy in predicting indoor temperatures when other than steady state conditions are present. In order to achieve precise results under varying thermal conditions, transient heat flow methods must be applied.

**Transient Thermal Conditions**

Transient thermal analysis offers the greatest precision possible for modeling heat transfer in buildings. The actual radiation, conduction, and convection thermal processes are accounted for with hour by hour load calculations. Because of the complexity and magnitude of the calculation process, computerization of this method is a necessity.

**Computer Simulation**

Computer analysis is a very flexible method which offers the user numerous options. Energy analysis programs can simulate heat transfer through an entire building structure, and thus can specifically calculate the thermal capacitance effect due to the building mass. Internal zone temperatures can be determined accurately, and hourly heating, ventilating, and air-conditioning loads developed. Solar gains may be recorded from actual or simulated weather
One of the most prominent hourly simulation computer programs is called the Building Loads Analysis and System Thermodynamics Program (BLAST).

**BLAST Computer Program**

Developed by the U. S. Army Construction Engineering Research Laboratory for use by the Department of Defense, BLAST is one of the most widely used programs performing transient thermal calculations. It allows the user to describe the building geometry and construction in detail, control the input weather, and model a number of HVAC systems. It can simulate widely differing facility types, from passive solar architecture to more typical office occupancy facilities. Heat gain through walls, roof, and slab is performed using the ASHRAE transfer function method.

Although extremely capable for performing energy analyses, programs such as BLAST are costly and time consuming. Computer simulation to design the HVAC equipment for a multi-zone office building can be quite costly. This expense is added to the training costs an engineering firm must face before their personnel are familiar with the program input requirements. Although program execution is a time saving process, the time required for training and data input prior to the run can be lengthy. Several hours of time would be necessary to prepare the input deck for a
multi-zone building. The detail required of the input information could also be a problem. Programs of this type require hourly weather data which may not be available to the user. The disadvantages are primarily those of cost and time— the benefits are the high degree of accuracy and reliability.

**Method Comparison**

The changeover alternatives discussed each have valuable benefits for the facility manager or energy engineer. Although the historical approach cannot determine building thermal performance, it offers a system by which changeover timing can be evaluated. When weather conditions create thermal discomfort for the occupants, the following season's changeover date can be adjusted. Steady state analysis offers simplicity for the user and a method to determine building temperatures. Transient analysis offers precision and flexibility. Solar and thermal mass gains are calculated on an hourly basis, and the user can input the actual building operation schedule as part of the computer simulation.

The ideal changeover method would borrow benefits from each of these approaches. User input information should be kept simple and to a minimum. Accuracy should be a high priority, but it should not depend upon expensive computer
analysis for calculations. The facility manager must be able to assess the thermal comfort for building occupants, yet be able to maximize his savings by conserving energy. One method to ensure thermal comfort is maintained is to set changeover timing as a function of the indoor building temperature.

**Trigger Temperature Method**

When weather conditions cause a building's temperature to stay within an acceptable comfort range, there is no need for supplemental heating. The acceptable temperature under these comfort conditions can be referred to as the "trigger temperature", a critical condition which is a function of the building responding to the weather. When the weather causes the building trigger temperature to be achieved, heating is no longer required. In the Autumn, this would indicate that the heating season has begun, whereas in the Spring, it would be time to shut the heating system down.

The Trigger Temperature Method uses the building temperature as an index to make changeover decisions. The building temperature can be predicted through statistical analysis of a range of BLAST computer simulations. This can be accomplished for the first few hours of occupancy, when the building is the coldest. The resulting method combines the accuracy of computer simulation with the simplicity of
hand calculation procedures. A high precision level, however, can only be achieved with a carefully developed statistical analysis plan.
CHAPTER FOUR

STATISTICAL MODEL DEVELOPMENT

No simple methods are available to accurately determine interior building temperatures. The thermal capacitance of a structure will cause a time delaying effect so that gains from solar, lighting, and people are not felt in the building immediately. Calculations of instantaneous thermal gains and losses can inaccurately represent the hourly building temperatures. Computer simulation is a necessary tool to accurately describe the hourly temperatures and thermal conditions. Through simulation of hypothetical test facilities, data may be gathered to represent a broad spectrum of building types and weather conditions. It is then possible to employ statistical analysis techniques to develop temperature predictive models which are accurate within the range for which they are developed. These models can be formulated to retain precision without the time and expenses inherent in computer simulations.

Statistical Models

Three mathematical models may be used to determine building temperatures: functional, control, and predictive.
(Draper and Smith, 1981). If the basic deterministic relationships among the variables can be defined, the functional model is best suited to the problem. However, in many cases where the underlying mathematical relationships are complex and involved, the functional model becomes difficult to develop.

The control model is used in carefully designed experiments. As the variable relationships become more complex, it is difficult to "control" the variables. This leads to the application of the predictive model.

Predictive models are used when functional relationships are complicated and difficult to control. For example, they are often used to determine the strength and reliability of construction materials. The compressive strength of a concrete mixture can be calculated using a functional model which considers the chemical bonding processes. However, for the purposes required in construction practice, the complexity involved in this procedure can be greatly simplified by using a predictive model. An easier approach involves testing of sample mixtures and recording the forces required to produce measurable failures. From these observations, a model is developed to predict compressive strength based upon the types and quantities of the concrete mixture components. The predictive model need not represent the actual chemical
processes which cause concrete hardening in order to produce an accurate and useful predictive model.

A predictive model can similarly be developed to calculate building temperatures as a function of the envelope, occupancy, and weather conditions. The actual thermal processes, including the solar gains and capacitance effects, can be predicted as part of the indoor temperature. In order to develop the predictive model, it is important to outline the analysis plan and describe the statistical procedures which apply.

**Model Building Analysis Plan**

An organized analysis plan is a necessary starting point in any problem-solving procedure. Methods to establish goals and evaluate the final solution should be clearly defined. The model building process in statistical studies can be developed in three phases: planning, development, and verification/validation. Figure 4-1 presents the model building flow diagram to be used for this statistical analysis. The planning phase includes defining the problem, selecting variables, outlining regression techniques, and establishing goals.

**Planning Phase**

The most important part in the planning phase is the
Figure 4-1 Model building flow diagram
development of a specific statement of the problem (Draper and Smith, 1981). For the work presented in this thesis, the predictive model should accurately determine transitional season building temperatures prior to, and during the initial hours of occupancy. Changeover timing will be based upon building and weather conditions which cause the building temperature to fall below a user defined threshold. The term "trigger temperature" will be used in this thesis to describe the acceptable building temperature which must be maintained for occupant comfort. Above this temperature, the building changeover can be made. (The changeover condition has been "triggered".) Prediction models will be developed on an hourly basis during the critical building hours from 6-10am. The first step in the planning phase involves the selection of possible model variables.

**Variable Selection**

The dependent variables for this study are the hourly building temperatures. For a facility functioning without heat, the coldest and therefore most critical period is prior to, and during the first few occupancy hours. Four dependent variables have been selected to determine the hourly average temperatures from 6-10am (Table 4.1). This enables the user to assess building temperatures during the critical occupancy hours.
Table 4-1

Model dependent variables

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>TEMP6</td>
<td>Building DBT from 6am-7am</td>
<td>(F)</td>
</tr>
<tr>
<td>TEMP7</td>
<td>Building DBT from 7am-8am</td>
<td>(F)</td>
</tr>
<tr>
<td>TEMP8</td>
<td>Building DBT from 8am-9am</td>
<td>(F)</td>
</tr>
<tr>
<td>TEMP9</td>
<td>Building DBT from 9am-10am</td>
<td>(F)</td>
</tr>
</tbody>
</table>

Note: DBT indicates Dry Bulb Temperature

Independent variables describe all heat gains and losses from occupancy and weather conditions. These variables must be fundamental to the problem and available to the user (Draper and Smith, 1981). Building envelope variables should be specific and in a usable format. For example, infiltration can be described in either cubic feet per minute (CFM) or as air changes each hour. Both are widely used in load calculations, but the widely varying range for CFM makes it a poor choice for statistical prediction use. A large facility with tight envelope construction could have the same CFM infiltration rate as a smaller, but older facility. The effect 1,000 CFM would have on each of these buildings would vary considerably. The initial variable list, shown in Table 4-2, is developed from ASHRAE standards widely used in heating and cooling load calculations.
Table 4-2
Initial variables - building and occupancy

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>APART</td>
<td>Area of partitions</td>
<td>(sf)</td>
</tr>
<tr>
<td>ASLAB</td>
<td>Area of building slab</td>
<td>(sf)</td>
</tr>
<tr>
<td>AWALL</td>
<td>Opaque wall area</td>
<td>(sf)</td>
</tr>
<tr>
<td>BVOL</td>
<td>Building volume</td>
<td>(cf)</td>
</tr>
<tr>
<td>DPART</td>
<td>Density of partitions</td>
<td>(lbs/cf)</td>
</tr>
<tr>
<td>EGLAS</td>
<td>Projected area of east glass</td>
<td>(sf)</td>
</tr>
<tr>
<td>ELEC</td>
<td>Lights, equip gains</td>
<td>(watts/sf)</td>
</tr>
<tr>
<td>HVAC</td>
<td>Heat recovery system (70% eff.)</td>
<td>(yes or no)</td>
</tr>
<tr>
<td>INFIL</td>
<td>Infiltration</td>
<td>(air changes/hour)</td>
</tr>
<tr>
<td>PSLAB</td>
<td>Perimeter of slab</td>
<td>(lf)</td>
</tr>
<tr>
<td>SCHED1</td>
<td>Scheduled occupancy begins</td>
<td>(7am or 8am)</td>
</tr>
<tr>
<td>SCHED2</td>
<td>Early occupancy</td>
<td>(up to one hour early)</td>
</tr>
<tr>
<td>SGLAS</td>
<td>Projected area of south glass</td>
<td>(sf)</td>
</tr>
<tr>
<td>SHADE</td>
<td>Glass shading coefficient</td>
<td>(fraction)</td>
</tr>
<tr>
<td>TGLAS</td>
<td>Area of total glass</td>
<td>(sf)</td>
</tr>
<tr>
<td>UGLAS</td>
<td>Glass U-value</td>
<td>(Btu/hr°F*sf)</td>
</tr>
<tr>
<td>UROOF</td>
<td>Roof U-value</td>
<td>(Btu/hr°F*sf)</td>
</tr>
<tr>
<td>UWALL</td>
<td>Wall U-value</td>
<td>(Btu/hr°F*sf)</td>
</tr>
</tbody>
</table>
Building schedule options are best described by a special type of independent variable, called an indicator or dummy variable. Indicator variables are used where measurements are not recorded on a continuous and well-defined scale, or when simplicity in model application is desired. The emphasis is on qualitative, rather than quantitative effects. Examples include sex (male or female), and political preference (Republican, Democrat, or Independent). Several variables (Table 4-2) have been described using two level indicator variables (0 = no effect, 1 = some effect).

Weather conditions involve perhaps the most difficult variables to select. A balance is needed between selecting sufficient variables to develop an accurate predictive model and limiting the list to variables generally available to the user. Hourly weather data can provide very accurate building energy calculations, but many potential users do not have access to this information. For this reason, weather variables were selected on the basis of daily records (high and low temperatures). Table 4-3 lists the preliminary selection of weather variables. After identifying the variables, statistical analysis methods can be used to formulate the predictive models.
Table 4-3

Initial variables - site and weather

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>ODBMAX</td>
<td>Outdoor dry bulb temp max</td>
<td>(F)</td>
</tr>
<tr>
<td>ODBMIN</td>
<td>Outdoor dry bulb temp min</td>
<td>(F)</td>
</tr>
<tr>
<td>SEASON</td>
<td>Weather season</td>
<td>Spring or Autumn</td>
</tr>
<tr>
<td>SOLAR</td>
<td>Clearness number</td>
<td>(fraction)</td>
</tr>
<tr>
<td>TGRND</td>
<td>Ground temperature</td>
<td>(F)</td>
</tr>
<tr>
<td>TSDEV</td>
<td>Temperature standard deviation</td>
<td>(F)</td>
</tr>
</tbody>
</table>

Regression Techniques

Regression analysis is the most common statistical method to predict responses from quantifiable independent variables (Draper and Smith, 1981). It is a widely used method where underlying, but unknown, deterministic relationships exist between dependent and independent variables.

The regression equation, or model, may contain one or more independent variables. The highest power of any independent variable is referred to as the order of the model. The general form of a simple, first-order model is:

\[ Y_1 = B_0 + B_1 X_1 + E_1 \] (4.1)
In this equation, $Y_i$ is the value at the $i^{th}$ trial, $B_0$ and $B_1$ are parameters, $X_i$ is the value of the dependent variable at the $i^{th}$ trial, and $E_i$ describes the random error. The error term is the amount by which any observation of $Y$ will differ from the regression line. Linear regression models are linear in parameters only and may contain higher order polynomial terms. Because $E$ changes for each observation and the $B$ terms can only be determined after seeing all of the data, these terms are replaced with estimates in regression analysis. The equation would then be written as:

$$Y_h = b_0 + b_1 X_i + e_i$$  \hspace{1cm} (4.2)

In this equation, $Y_h$ is called Y-hat, the predicted value of $Y$, $b_0$ and $b_1$ are parameter estimates, and $X$ is the value of the dependent variable. The difference between $Y$ and $Y_h$, $e_i$, is the error in the equation. This $e_i$ term is referred to as the residual.

To obtain the best estimate of the model parameters, regression analysis uses the method of least squares. The regression model which fits the data best is one in which the sum of squared error terms (SSE) is the lowest. A sample regression line shown in Figure 4-2 shows how tree diameter may be used to estimate the volume of usable lumber which may be produced.
Figure 4-2 Method of least squares
In many research problems, more than one independent variable is required to accurately describe the response. Multiple linear regression techniques are used for these cases. The general form of a first-order model with two independent variables would be written:

\[
Y_i = B_0 + B_1X_{i1} + B_2X_{i2} + B_3X_{i1}X_{i2} + E_i \quad (4.3)
\]

Often the response of one independent variable depends upon its relationship with another related variable. Interaction terms are used to account for this information in multiple regression analysis. In the previous example, the diameter alone was used to predict lumber volume. If the interaction term, diameter*height is used, the observations fall in a pattern closer to the regression line (See Figures 4-3a and 4-3b). However, both of these patterns indicate nonlinear trends. This can be corrected by using a variable transformation. Transformations commonly used in regression analyses include: \(1/X^2\), \(1/X\), \(1/\log(X)\), \(\log(X)\), and \(X^2\). The transformation is clear in this simple example. Figure 4-3c shows the best fit of the data - a result of using the transformation closest to the mathematical equation for a cylindrical volume. The preliminary selection of interaction terms used in this regression analysis is shown in Table 4-4.
Figure 4-3a
Simple regression example

Figure 4-3b
Multiple regression with interaction term

Figure 4-3c Transformed interaction example
### Table 4-4

**Initial interaction variable terms**

<table>
<thead>
<tr>
<th>Predictor</th>
<th>Interaction terms = f(variables)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Heat stored by partitions</td>
<td>ADPART = APART*DPART</td>
</tr>
<tr>
<td>Infiltration effect from outside air (see TDIFF)</td>
<td>AIRCH = INFIL*TDIFF</td>
</tr>
<tr>
<td>Heat recovered from early occupancy hours</td>
<td>AIRCH1 = INFIL<em>SCHED1</em>HVAC*TDIFF</td>
</tr>
<tr>
<td>Heat recovered from warm-up lights</td>
<td>AIRCH2 = INFIL<em>SCHED2</em>HVAC*TDIFF</td>
</tr>
<tr>
<td>Ventilation effect from heat recovery system</td>
<td>AIRCH3 = INFIL<em>HVAC</em>TDIFF</td>
</tr>
<tr>
<td>East solar gain reduced by glass shading</td>
<td>EGLAS1 = EGLAS*SHADE</td>
</tr>
<tr>
<td>East solar effect</td>
<td>EGLAS2 = EGLAS*SOLAR</td>
</tr>
<tr>
<td>Combined east solar effect</td>
<td>EGLAS3 = EGLAS<em>SHADE</em>SOLAR</td>
</tr>
<tr>
<td>7am occupancy light gains</td>
<td>ELEC1 = ELEC*SCHED1</td>
</tr>
<tr>
<td>Warm-up light gains</td>
<td>ELEC2 = LEC*SCHED2</td>
</tr>
<tr>
<td>Daily temperature range</td>
<td>RANGE = ODBMAX-ODBMIN</td>
</tr>
<tr>
<td>South solar gain reduced by glass shading</td>
<td>SGLAS1 = SGLAS*SHADE</td>
</tr>
<tr>
<td>South solar effect</td>
<td>SGLAS2 = SGLAS*SOLAR</td>
</tr>
<tr>
<td>Combined south solar effect</td>
<td>SGLAS3 = SGLAS<em>SHADE</em>SOLAR</td>
</tr>
<tr>
<td>Losses through building envelope</td>
<td>TAVE = (ODBMIN+ODBMAX)/2</td>
</tr>
<tr>
<td>Balance point difference</td>
<td>TDIFF = 65-ODBMIN</td>
</tr>
</tbody>
</table>
Multiple linear regression becomes a complex and involved calculation procedure as the number of variables increases. There are \( n \times 2^k \) possible regression equations in any analysis, where \( n \) is the number of independent variables and \( k \) is the number of dependent variables (Neter and Wasserman, 1974). In this study, the more than thirty variable terms (variables, interactions and transformations), would result in more than a billion possible regression equations. Computer analysis is necessary to perform regressions of this scope. One of the most powerful statistical packages available is the Statistical Analysis System (SAS). Developed by the SAS Institute in North Carolina, this program includes a variety of statistical procedures ranging from graphics to complex multivariate techniques (SAS Institute, 1979). The extensive descriptive statistics of SAS make it an ideal tool for developing and checking regression equations against specified goals.

Analysis Goals

In order to select the best regression equation from the many possible, it is necessary to define several goals. Preliminary regression goals include establishing the model type and maximum number of variable terms. A predictive regression model will be used in this research. The model
will be limited to having twenty or fewer variable terms (parameters) so that hand calculation methods may be used in follow-on applications. Additional goals will include setting acceptable values for the Coefficient of Determination ($R^2$), Coefficient of Variation, (C.V.), and parameter significance ($F$ test). Finally, models with different dependent variables will be compared for accuracy and consistency.

Coefficient of Determination

The Coefficient of Determination, or $R^2$ term, is the square of the correlation coefficient. It indicates what proportion of the total variation in the dependent variable Y is explained by the regression model (Walpole and Meyers, 1978). The $R^2$ is often given as a fractional value, ranging from zero to one. An $R^2$ value of zero means that the regression model is of no help in reducing the variation in Y, and a value of one indicates a perfect fit with all observations lying on the regression line.

An $R^2$ goal of .95 is set to ensure that the final regression equations will be accurate predictors of the building temperature. Any equation failing to meet this minimum value can be rejected as lacking sufficient precision. One limitation of the $R^2$ statistic is that as the number of parameters increases, the $R^2$ value cannot decrease.
Coefficient of Variation

The Coefficient of Variation is very useful in statistical analyses because it is a measure of model precision which takes into account the number of parameters in the model. It is a unitless term used to describe the variation unaccounted for by a fitted regression equation. In least squares regression analysis, the goal is to minimize the sum of the squared residuals. One method to measure the variability of the residuals is by calculating the variance of the residuals, called the mean square error (MSE). The Coefficient of Variation, expressed as a percentage of the mean response, is the square root of the MSE divided by the predicted value mean. A value of 1.0% is set as the goal for this research. This will ensure that a very small amount of error will occur in the regression models. The next step is to ensure that all parameters are statistically significant.

Parameter Significance

Before a regression equation can be selected as the best model, the parameters should be tested for significance. The possibility that a parameter is not very valuable in explaining model error is expressed in the form of a test statistic. First, a null hypothesis, $H_0$, is proposed that a parameter is equal to zero. Then an
alternative hypothesis, $H_A$, counters that the parameter is not equal to zero and is indeed significant to the regression equation. Finally, an F test statistic is developed to see if the parameter is equal to zero within specified probability limits. This test is performed at standard significance levels. The significance of a parameter can be evaluated by identifying the amount of error which would be added if that parameter were dropped from the model. In order to ensure that the selected regression models do not contain any questionable parameters, the probability level for the F test is set at 0.01%.

Model Agreement

The final goal to be met is one of model agreement. After regression equations for each of the four hours are developed, they will be used together to estimate the building temperatures from 6-10am. It is necessary that these equations are consistent in accuracy. If one equation differs from the others substantially in its ability to predict temperatures, errors in interpretation could result.

The $R^2$ term is used to measure accuracy of the final predictive models. The variation in $R^2$ can be used to ensure that all models are consistent with each other. The difference in the $R^2$ values for any two predictive models is
set at 1.0% to ensure that all models will be consistent as well as accurate. With all of the goals set, the analysis plan is ready for the next phase – development of the models.

Development Phase

The development phase is central to the statistical model building process. During this phase, data are gathered, and regression equations are developed, tested, and evaluated.

Data Collection

Computer-simulated data were generated for 94 hypothetical single story masonry office buildings, using the Building Loads Analysis and System Thermodynamics (BLAST) program. This program, developed by the U. S. Army Construction Engineering Research Laboratory, uses the ASHRAE transfer functions to perform hourly heat transfer calculations (U.S. Army CERL, 1979). A base condition hypothetical office facility of 5000 sf was developed and then modified through a series of envelope, occupancy, and siting variations. These variations included changes to the building size, area and U-values of envelope components, and infiltration rates, as well as occupancy hours and site orientation. A survey of existing U. S. Air Force
administrative facilities was used as a basis for selecting the ranges for building construction and occupancy criteria.

During 1977 through 1979 the U. S. Air Force conducted an intensive survey and analysis program to reduce energy consumption in existing and proposed buildings. Through this energy audit program, a data base for Air Force facilities was developed. From this data base and informal discussions with Air Force Civil Engineering officials, representative building areas and constructions, envelope component U-Values, infiltration rates, and occupancy schedules have been identified for use in this thesis. Tables 4-5a and 4-5b present a listing of the selected variable levels. A weather data base was then developed for BLAST input.

Design days for three daily temperature ranges (Figure 4-4) representative of Spring and Fall weather were generated by examining the 29-year data base recorded by The Pennsylvania State University Department of Meteorology. The extreme high and low recorded temperatures were set as limits for the design days. Steps of 2 °F were used to develop 58 different design days, having lows ranging from 18 °F to 54 °F and highs ranging from 28 °F to 84 °F. Simulation of the hypothetical test facilities was then performed.

A minimum of ten observations for each proposed model
Table 4-5a
Variable levels tested in BLAST simulations

<table>
<thead>
<tr>
<th>Run #s</th>
<th>Description</th>
<th>Levels - See Note #1</th>
<th>(* Denotes base condition)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1 to 8</td>
<td>Area of building (sf)</td>
<td>1800</td>
<td>5000</td>
</tr>
<tr>
<td></td>
<td></td>
<td>2450</td>
<td>7200</td>
</tr>
<tr>
<td></td>
<td></td>
<td>3200</td>
<td>9800</td>
</tr>
<tr>
<td>9 to 16</td>
<td>Area of partitions (sf)</td>
<td>0</td>
<td>1875</td>
</tr>
<tr>
<td></td>
<td></td>
<td>625</td>
<td>2500</td>
</tr>
<tr>
<td></td>
<td></td>
<td>1250</td>
<td>3125</td>
</tr>
<tr>
<td>17 to 22</td>
<td>Density of partitions (lbs/sf)</td>
<td>6.16</td>
<td>12.5</td>
</tr>
<tr>
<td></td>
<td></td>
<td>* 12.36</td>
<td>25.2</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>40.7</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>59.1</td>
</tr>
<tr>
<td>23 to 28</td>
<td>Area per occupant (sf/person)</td>
<td>63</td>
<td>100</td>
</tr>
<tr>
<td></td>
<td></td>
<td>75</td>
<td>* 125</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>200</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>inf</td>
</tr>
<tr>
<td>29 to 35</td>
<td>Lighting and elec load (watts/sf)</td>
<td>1.5</td>
<td>2.25</td>
</tr>
<tr>
<td></td>
<td></td>
<td>2.0</td>
<td>* 2.50</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>3.25</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>3.91</td>
</tr>
<tr>
<td>36 to 46</td>
<td>Site orientation angle (axis angle - Note #2)</td>
<td>0</td>
<td>60</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>* 90</td>
</tr>
<tr>
<td>47 to 49</td>
<td>Occupancy schedule (% lights and people)</td>
<td>0% 6-7am, 100% 7am-5pm</td>
<td>*</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>50 to 53</td>
<td>Available sunshine (clearness number)</td>
<td>.00</td>
<td>.25</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>.50</td>
</tr>
<tr>
<td>54</td>
<td>Seasonal difference</td>
<td>Autumn</td>
<td>* Spring</td>
</tr>
</tbody>
</table>

Note #1: The base condition is counted as a single simulation and therefore is not represented as a separate run with each description group.

Note #2: Orientation levels were run at 20% and 60% glass levels.
Table 4-5b

Variable levels tested in BLAST simulations

<table>
<thead>
<tr>
<th>Run #s</th>
<th>Description</th>
<th>Levels</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>(* Denotes base condition)</td>
</tr>
<tr>
<td>55 to 61</td>
<td>Infiltration/ventilation (air changes/hour)</td>
<td>.25</td>
</tr>
<tr>
<td></td>
<td></td>
<td>.50</td>
</tr>
<tr>
<td></td>
<td></td>
<td>1.00</td>
</tr>
<tr>
<td>62 to 69</td>
<td>Heat recovery option</td>
<td>yes</td>
</tr>
<tr>
<td>70 to 74</td>
<td>Total glass (% glass in ext. walls)</td>
<td>10</td>
</tr>
<tr>
<td></td>
<td></td>
<td>* 20</td>
</tr>
<tr>
<td>75 to 80</td>
<td>South-facing glass (% of south glass)</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td></td>
<td>10</td>
</tr>
<tr>
<td></td>
<td></td>
<td>60</td>
</tr>
<tr>
<td>81 to 86</td>
<td>Shading coefficient (Note #2)</td>
<td>.24</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>87</td>
<td>Glass U-value</td>
<td>.55</td>
</tr>
<tr>
<td>88 to 90</td>
<td>Wall U-value</td>
<td>.0440</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>91 to 93</td>
<td>Roof U-value</td>
<td>.0409</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>94</td>
<td>Base condition</td>
<td></td>
</tr>
</tbody>
</table>

Note #1: Infiltration levels were run at 30% during occupied hours to simulate heat recovery systems.

Note #2: Shading coefficients were run for 20% and 60% glass levels, and for single and double glazing levels.
A variable is recommended for statistical regression analyses (Draper and Smith, 1981). For the 26 independent and 4 dependent variables, this would require 300 observations. Over 1300 observations were actually recorded so that the variables could be tested at several levels. Validation was also considered prior to data collection.

Model validation requires new observations to prove the stability of a developed regression equation. One of the strongest and statistically useful validation procedures is to use half of the data to generate the equation, and the other half for validation purposes. For this reason, over 2600 observations were collected and divided in half prior to the statistical regression analysis.
Regression Analysis

The regression model building process is a series of development and testing steps. After the variable selection is made, regression equations are formulated and tested against defined goals. The ideal regression equation is not always clear, however. Often a compromise must be made between the accuracy desired and the utility of the final equation. The maximum number of variable terms was limited to 20 or fewer so that the selected regression equations would be relatively simple and easy to use.

Goals were then set for the statistical tests. Any models failing to meet a minimum $R^2$ value of 0.95 were rejected. Remaining models were tested to meet a Coefficient of Variation of 1.0% or lower. Parameters were then tested for significance with an $F$ test probability level of 0.01%. This regression analysis procedure was followed for each hour from 6-10am. The resultant four regression equations were finally compared for consistency by making certain that the $R^2$ values did not vary by more than 1.0% for any two models.

Appendix A includes the individual model statistical data for all of the generated predictive models. The detailed results of the analysis approach are described in the following sections for the first hour dependent variable, TEMP6 (6-7am).
Coefficient of Determination

The first step in testing the regression equation was to select only those models with a Coefficient of Determination, or $R^2$, of 0.95 as a minimum. One of the most effective statistical methods for this purpose is the STEPWISE procedure available in SAS. Stepwise regression is a selective process which chooses variables for model inclusion based upon their ability to produce a high model $R^2$ value.

The SAS routine MAXR was selected to perform the stepwise regression analysis. This form of stepwise regression begins with a one variable model having the highest $R^2$ value and then selectively adds a second variable to give the greatest $R^2$ increase. As new variables are added, MAXR drops variables in favor of more significant ones so that the "best" $R^2$ will be achieved for the number of variables present. Table 4-6 shows the results of running MAXR for the dependent variable TEMP6. The $R^2$ values are listed by the number of variable terms in the model. Although the stated goal of 0.95 was achieved with only 5 variable terms, improvement is seen until 15 terms have been included. All equations meeting the $R^2$ goal were next tested for error analysis.
Table 4-6  R Squared values for TEhro

<table>
<thead>
<tr>
<th>Number of Independent Variable Terms</th>
<th>Dropped Variable Terms</th>
<th>Added Variable Terms</th>
<th>R Squared Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>---</td>
<td>TAVE</td>
<td>* 0.728</td>
</tr>
<tr>
<td>2</td>
<td>---</td>
<td>AIRCH</td>
<td>* 0.883</td>
</tr>
<tr>
<td>3</td>
<td>---</td>
<td>SOLAR</td>
<td>* 0.910</td>
</tr>
<tr>
<td>4</td>
<td>---</td>
<td>UGLAS</td>
<td>* 0.939</td>
</tr>
<tr>
<td>5</td>
<td>---</td>
<td>EGLAS3</td>
<td>0.952</td>
</tr>
<tr>
<td>6</td>
<td>---</td>
<td>UWALL</td>
<td>0.961</td>
</tr>
<tr>
<td>7</td>
<td>---</td>
<td>TDIFF</td>
<td>0.970</td>
</tr>
<tr>
<td>8</td>
<td>---</td>
<td>TGLAS</td>
<td>0.978</td>
</tr>
<tr>
<td>9</td>
<td>---</td>
<td>ELEC1</td>
<td>0.983</td>
</tr>
<tr>
<td>10</td>
<td>---</td>
<td>UROOF</td>
<td>0.985</td>
</tr>
<tr>
<td>11</td>
<td>---</td>
<td>ELEC</td>
<td>0.987</td>
</tr>
<tr>
<td>12</td>
<td>---</td>
<td>AIRCH2</td>
<td>0.987</td>
</tr>
<tr>
<td>13</td>
<td>---</td>
<td>SGLAS2</td>
<td>0.988</td>
</tr>
<tr>
<td>14</td>
<td>SGLAS2</td>
<td>ADPART, ASLAB1/2</td>
<td>0.990</td>
</tr>
<tr>
<td>15</td>
<td>---</td>
<td>SGLAS2</td>
<td>0.991</td>
</tr>
<tr>
<td>16</td>
<td>---</td>
<td>INFIL</td>
<td>0.991</td>
</tr>
<tr>
<td>17</td>
<td>AIRCH2</td>
<td>ELEC2, AIRCH1</td>
<td>0.991</td>
</tr>
<tr>
<td>18</td>
<td>ASLAB1</td>
<td>PEOPLE, ASLAB</td>
<td>0.991</td>
</tr>
<tr>
<td>19</td>
<td>---</td>
<td>ASLAB1/2</td>
<td>0.991</td>
</tr>
<tr>
<td>20</td>
<td>---</td>
<td>SHADE</td>
<td>0.991</td>
</tr>
</tbody>
</table>

Note:  * Values failed to meet goal of $R^2 > 0.95$. 
Coefficient of Variation

The maximum value for the Coefficient of Variation was set so that the standard error of the estimate would be no more than 1.0% of the mean response. Two more models were eliminated because they failed to meet this criterion. Table 4-7 lists the results. The remaining equations were tested for parameter significance.

Parameter Significance

The parameter significance F test was set not to exceed a probability of 0.01%. Equations with 18 and 19 variable terms failed this significance test. The remaining equations with from 7 to 17 variable terms met all preliminary goals and were retained for comparison with other dependent variable models. Summary statistics for all models are shown in Table 4-8.
Table 4-7
Coefficient of Variation for TEMP6

<table>
<thead>
<tr>
<th>Number of Independent Variable Terms</th>
<th>Mean Square Error (MSE)</th>
<th>Standard Error of Estimate (s)</th>
<th>Coeff of Var (C.V.)</th>
<th>Note</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>(TEMP6 Mean = 60.6 F)&lt;br&gt;C.V. = 100*s / Mean</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>0.546</td>
<td>0.739</td>
<td>* 1.219</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>0.447</td>
<td>0.669</td>
<td>* 1.103</td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>0.349</td>
<td>0.591</td>
<td>0.975</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>0.256</td>
<td>0.506</td>
<td>0.835</td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>0.200</td>
<td>0.447</td>
<td>0.738</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>0.168</td>
<td>0.410</td>
<td>0.676</td>
<td></td>
</tr>
<tr>
<td>11</td>
<td>0.155</td>
<td>0.394</td>
<td>0.650</td>
<td></td>
</tr>
<tr>
<td>12</td>
<td>0.144</td>
<td>0.379</td>
<td>0.626</td>
<td></td>
</tr>
<tr>
<td>13</td>
<td>0.136</td>
<td>0.369</td>
<td>0.609</td>
<td></td>
</tr>
<tr>
<td>14</td>
<td>0.117</td>
<td>0.342</td>
<td>0.564</td>
<td></td>
</tr>
<tr>
<td>15</td>
<td>0.109</td>
<td>0.330</td>
<td>0.545</td>
<td></td>
</tr>
<tr>
<td>16</td>
<td>0.105</td>
<td>0.324</td>
<td>0.535</td>
<td></td>
</tr>
<tr>
<td>17</td>
<td>0.102</td>
<td>0.317</td>
<td>0.527</td>
<td></td>
</tr>
<tr>
<td>18</td>
<td>0.100</td>
<td>0.316</td>
<td>0.522</td>
<td></td>
</tr>
<tr>
<td>19</td>
<td>0.100</td>
<td>0.316</td>
<td>0.522</td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>0.099</td>
<td>0.315</td>
<td>0.519</td>
<td></td>
</tr>
</tbody>
</table>

Note: * Values failed to meet goal of C.V. < 1.0%
Model Agreement

The last development phase goal was one of model consistency. The goal was set to have all model $R^2$ values within 1.0% of each other. Figure 4-5 shows a graph of the $R^2$ values as a function of the number of variable terms in the model. Plateaus in the TEMP6 regression equation can be seen for models with 11 and 15 variable terms. In order to keep the TEMP6 $R^2$ value within 1.0% of the other equations, the eleven variable term model was selected as the final regression equation.

Table 4-8
Summary statistics for prediction equations

<table>
<thead>
<tr>
<th>Dependent Variable Term</th>
<th>Number of Independent Variable Terms</th>
<th>$R$ Squared Value</th>
<th>Coeff of Var (C.V.)</th>
<th>Parameters Failing Significance Test</th>
</tr>
</thead>
<tbody>
<tr>
<td>TEMP6</td>
<td>11</td>
<td>0.987</td>
<td>0.650</td>
<td>NONE</td>
</tr>
<tr>
<td>TEMP7</td>
<td>15</td>
<td>0.979</td>
<td>0.805</td>
<td>NONE</td>
</tr>
<tr>
<td>TEMP8</td>
<td>15</td>
<td>0.982</td>
<td>0.694</td>
<td>NONE</td>
</tr>
<tr>
<td>TEMP9</td>
<td>16</td>
<td>0.981</td>
<td>0.732</td>
<td>NONE</td>
</tr>
</tbody>
</table>
Figure 4-5 Model consistency comparison
The final regression equations for all four hours are then written as:

**TEMP6** =

\[55.25 - 0.1841*AIRCH + 0.2594*TAVE - 0.08513*TDIFF + 0.001418*TGLAS + 3.634*SOLAR - 15.029*UWALL - 20.587*UROOF - 4.5821*UGLAS + 0.7916*ELEC + 0.4407*ELECI + 0.008542*EGLAS3,\]  

**TEMP7** =

\[56.64 - 0.1734*AIRCH + 0.1388*AIRCH1 - 1.214*INFIL + 0.2720*TAVE - 1.007*TDIFF + 0.01367*EGLAS2 + 4.190*SOLAR - 16.424*UWALL - 22.431*UROOF - 5.043*UGLAS + 0.454*PEOPLE - 0.0001926*ADPART + 0.5775*ELEC + 2.383*ELECI - 0.0003305*ASLAB,\]  

**TEMP8** =

\[51.07 - 0.1982*AIRCH + 0.06307*AIRCH1 + 0.0717*AIRCH3 + 0.3337*TAVE - 0.02643*RANGE + 0.002237*TGLAS + 0.01103*EGLAS2 + 4.229*SOLAR - 16.263*UWALL - 25.358*UROOF - 3.9537*UGLAS + 0.04519*PEOPLE - 0.0002585*ADPART + 3.102*ELEC - 0.0003496*ASLAB\]  

and

**TEMP9** =

\[50.51 - 0.1926*AIRCH + 0.1353*AIRCH3 + 0.3353*TAVE - 0.01826*RANGE + 0.004268*TGLAS + 0.01348*EGLAS2 - 0.007367*EGLAS3 + 5.12*SOLAR - 16.769*UWALL - 25.502*UROOF - 3.8904*UGLAS + 0.04750*PEOPLE - 0.0003031*ADPART + 2.821*ELEC + 0.5003*ELECI - 0.0004114*ASLAB.\]
Verification and Validation

Once an equation has met all of the goals set in the planning phase and is considered useful, it should be examined for stability, analyzed for its practicality, and be validated by an accepted method. The stability of a model depends upon the accuracy over its entire range of application. A model appearing to be accurate may still lack precision in a specific range. Verification that this condition does not exist is made by examining plots of the residuals.

Residual Plots

Examination of residuals can offer many insights into a selected model's stability. Residual trends can indicate if important variables have been omitted, if variable transformations are called for, or if the model variance is not constant.

The residuals, or the differences between the observations and the predicted values, are plotted against the dependent variable. Figures 4-6a through 4-6c show residual patterns typically found in regression analyses. If the residuals do not fall within a horizontal band, as in Figure 4-6a, the regression equation may require modification.

The TEMP6 residual plot for the selected regression
Figure 4-6a Acceptable residual plot

Figure 4-6b Non-linear residual plot

Figure 4-6c Non-constant variance residual plot
equation is shown in Figure 4-7. The pattern shows a central tendency with most points clustered between \(-1.0\) °F and \(+1.0\) °F. No systematic lack of fit is shown in the residual pattern. Residuals for the remaining dependent variables were plotted, with similar results (See Appendix A). Once the prediction equations have satisfied the statistical requirements, they are analyzed from an engineering perspective to see if underlying functional relationships have been properly reflected.

Model Plausibility

Engineering analysis of a prediction equation should be made by considering the model as a whole. The least squares regression coefficients are determined by adjusting for all model variables. Often in multiple regression models, variables are correlated with each other or with variables not included in the model. It is therefore important to interpret variable coefficients from a perspective of the model as a whole. The parameters which are included in the model should, however, be studied to see if they are plausible and reasonable predictors.

Equation 4.4 (page 54) shows how the building temperature is a function of envelope, occupancy, and site criteria. The 6-7am temperature receives positive temperature gains from solar radiation (SOLAR), average
Figure 4-7 TEMP6 residual plot
outdoor temperature (TAVE), east-facing glass (EGLAS3) and internal electric loads (ELEC and ELEC1). Losses are seen in infiltration (AIRCH), the indoor to outdoor temperature difference (TDIFF), the total glass (TGLAS), and the building U-Values (UROOF, UWALL, UGLAS). The variables which are not included in the selected model are also important to consider.

Although $R^2$ improvement is seen in the TEMP6 equation until 15 variable terms have been included (Table 4-6), the added terms do not improve the model significantly. The infiltration due to a 20% early occupancy option (AIRCH2) and the amount of south-facing glass (SGLAS2) do not substantially affect the calculation of a building temperature. This is possibly due to the fact that the early occupancy does not create a significant infiltration load, and south glass does not receive direct sun until later morning hours. The partitions (ADPART) are not important because by 6-7am most of the stored heat from the previous day has been released to the space. The building area ($ASLAB^{1/2}$) is also unimportant in improving the model predictive ability. Other variable correlations may be causing this. Variable terms which indirectly describe building area are included in the model before the slab area is considered (EGLAS3, TGLAS, SGLAS2, ADPART). They are proportional to the slab area, making $ASLAB^{1/2}$ redundant.
All variables remaining in the selected model are ones developed from steady state heat calculation equations, indicating that the model is both plausible and reasonable from an engineering standpoint. Similar analysis results were concluded after judging the engineering practicality of the remaining models. Before the models can be used confidently, however, they must be validated using new data.

**Validation**

Validation of a statistical model is a necessary step in the regression process (Draper and Smith, 1981). Even when the selected equation is acceptable in statistical terms, its ability to accurately predict future observations should be tested. At the outset of the model building process, half of the data was reserved for validation purposes. These observations are now used to test the predictive abilities of the model.

Two methods have been used to present the validation summary for the variable TEMP6. Both are intended to describe model accuracy in terms meaningful to the engineer or end user of the equation. The first method defines the model error as a temperature deviation (F) from the BLAST results, and the second method shows the error as a percent of variation. Figure 4-8 shows the frequency distribution for the TEMP6 temperature difference. All observations for
<table>
<thead>
<tr>
<th>TEMP6 TEMPERATURE DIFFERENCE</th>
</tr>
</thead>
<tbody>
<tr>
<td>(COMPUTER - PREDICTED)</td>
</tr>
<tr>
<td></td>
</tr>
<tr>
<td>(F)</td>
</tr>
<tr>
<td>-----------------</td>
</tr>
<tr>
<td>-2.0</td>
</tr>
<tr>
<td>-1.9</td>
</tr>
<tr>
<td>-1.8</td>
</tr>
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<td>-1.7</td>
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<td>-1.6</td>
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<td>-1.5</td>
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<tr>
<td>-1.4</td>
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<td>-1.3</td>
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<tr>
<td>-1.2</td>
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<tr>
<td>-1.1</td>
</tr>
<tr>
<td>-1.0</td>
</tr>
<tr>
<td>-0.9</td>
</tr>
<tr>
<td>-0.8</td>
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<tr>
<td>-0.7</td>
</tr>
<tr>
<td>-0.6</td>
</tr>
<tr>
<td>-0.5</td>
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<tr>
<td>-0.3</td>
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<td>-0.1</td>
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<tr>
<td>0.0</td>
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<td>0.1</td>
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<tr>
<td>0.3</td>
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<tr>
<td>0.4</td>
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<td>0.5</td>
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<tr>
<td>0.6</td>
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<td>0.7</td>
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<td>0.8</td>
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<tr>
<td>0.9</td>
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<tr>
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<tr>
<td>1.1</td>
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<td>1.4</td>
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<td>1.7</td>
</tr>
<tr>
<td>1.8</td>
</tr>
<tr>
<td>1.9</td>
</tr>
<tr>
<td>2.0</td>
</tr>
</tbody>
</table>

**Figure 4-8** TEMP6 temperature difference distribution
this hour are within 2 F of the simulated value, indicating a high degree of agreement between the predictive model and the BLAST data. Table 4-9 presents the validation results for all four models, showing the distribution percentages.

Table 4-9
Summary of model validations

<table>
<thead>
<tr>
<th>Description</th>
<th>TEMP6</th>
<th>TEMP7</th>
<th>TEMP8</th>
<th>TEMP9</th>
</tr>
</thead>
<tbody>
<tr>
<td>Predictions within 1 F of BLAST</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>97.8%</td>
<td>91.9%</td>
<td>94.1%</td>
<td>93.3%</td>
</tr>
<tr>
<td>Predictions within 2 F of BLAST</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>100.0%</td>
<td>99.4%</td>
<td>99.5%</td>
<td>98.8%</td>
</tr>
<tr>
<td>Maximum difference (BLAST - model)</td>
<td>-1.9 F</td>
<td>+2.6 F</td>
<td>-2.4 F</td>
<td>-2.6 F</td>
</tr>
<tr>
<td>Average Error (BLAST - model)/BLAST</td>
<td>0.50%</td>
<td>0.57%</td>
<td>0.48%</td>
<td>0.50%</td>
</tr>
<tr>
<td>Maximum Error (BLAST - model)/BLAST</td>
<td>3.1%</td>
<td>3.7%</td>
<td>3.4%</td>
<td>3.6%</td>
</tr>
</tbody>
</table>

Note: Validation data contained 1,313 new observations.

within 1.0 F and 2.0 F. This table also presents the second method, showing the model error as a percentage. The average error is less than 0.60% in all cases, and the maximum error for any observation is only 3.7%.

The prediction equations for all models have proven to be precise and reliable predictors of building temperatures from 6-10am. They now can be integrated into the Trigger Temperature Method and used in changeover analyses.
CHAPTER FIVE

TRIGGER TEMPERATURE METHOD

The Trigger Temperature Method integrates the building temperature prediction equations developed in Chapter Four into a system to determine seasonal changeover timing. This method establishes the weather conditions which cause buildings to fall below a minimum comfort level, or "trigger temperature". Average year weather recorded by The National Oceanic and Atmospheric Administration (NOAA) is used to predict the optimal changeover date. Both hand calculation and computerized methods are available to the user. In this chapter, two example problems are discussed to demonstrate the Trigger Temperature Method capabilities and flexibility.

Weather Input Data

One of the primary concerns in developing a changeover analysis method is the nature of the weather information required. In any energy analysis, weather data should be available and appropriate for the use intended. Daily normal temperature data, developed by NOAA from 30 years of observations, are ideal for changeover purposes. Daily high and low temperatures have been recorded for numerous
locations and compiled into representative "average" weather years. Table 5-1 shows the NOAA daily normal weather data for Harrisburg, Pennsylvania, during February through May. (This table will be used in the example problems discussed later.) NOAA weather information shows the seasonal progression on a daily basis, and thus can be used in changeover estimation methods.

**User Requirements**

The Trigger Temperature Method provides two procedures for determining changeover timing. If hand calculation methods are required, linear programming techniques can be used to select the changeover date. If micro-computer capability exists, printout options are available to provide changeover decision information. The user flow chart, shown in Figure 5-1, describes the Trigger Temperature Method use. The first step is for the user to set temperature comfort goals. The Trigger Temperature Method determines a changeover date for a facility based upon minimum building temperatures specified by the user. Trigger temperatures are set for each hour to be studied. This is a minimum of two hours — the threshold hour when occupancy begins, and the upper limit when the normal desired building temperature has been reached. The threshold Trigger Temperature would normally be set at the thermostat night setback temperature.
Table 5-1

Daily normals of temperature for Harrisburg, Pa

(NOAA Environmental Data Service, 1973)

<table>
<thead>
<tr>
<th>Day</th>
<th>February</th>
<th>March</th>
<th>April</th>
<th>May</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Julian date</td>
<td>Max</td>
<td>Min</td>
<td>Julian date</td>
</tr>
<tr>
<td>1</td>
<td>32</td>
<td>38</td>
<td>23</td>
<td>60</td>
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<tr>
<td>31</td>
<td>90</td>
<td>57</td>
<td>36</td>
<td></td>
</tr>
</tbody>
</table>
Figure 5-1 Trigger Temperature Method flow chart
The upper limit temperature can be set at any value and for any hour after occupancy begins. The user also has the option of studying any intermediate occupancy hour to see how the building warmup is progressing. After determining the hours to be studied, the user selects the appropriate predictor equations and reviews the building and site characteristics which need to be recorded. The next step is the collection of data required for input into the predictor equations. Weather data for the selected location are gathered (NOAA Environmental Data Service, 1973), and the specific building characteristics are recorded.

Example Problems

Two example problems are developed to demonstrate the different methods available to the user. The building input data for both example problems are presented in Table 5-2.

Problem #1

The first example uses linear programming techniques and hand calculations to determine the Spring changeover date for a hypothetical 5000 sf office building in Harrisburg, Pennsylvania. Although this analysis is made to determine when heating could be turned off in the Spring, a similar procedure would apply for turning the heat on in the Fall. Occupancy hours of 7am-5pm in this example permit
### Table 5-2
Building data for example problems

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description/Unit</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>APART</td>
<td>Area of partitions (sf)</td>
<td>1875</td>
</tr>
<tr>
<td>ASLAB</td>
<td>Area of building slab (sf)</td>
<td>5000</td>
</tr>
<tr>
<td>DPART</td>
<td>Density of partitions (lbs/sf)</td>
<td>12.5</td>
</tr>
<tr>
<td>EGLAS</td>
<td>Projected area of east glass (sf)</td>
<td>90</td>
</tr>
<tr>
<td>ELEC</td>
<td>Lights, equip gains (watts/sf)</td>
<td>2.0</td>
</tr>
<tr>
<td>HVAC</td>
<td>Heat recovery system (no)</td>
<td>0</td>
</tr>
<tr>
<td>INFIL</td>
<td>Infiltration air changes/hour</td>
<td>.750</td>
</tr>
<tr>
<td>PEOPLE</td>
<td>Number of occupants</td>
<td>45</td>
</tr>
<tr>
<td>SCHED1</td>
<td>Occupancy hours (7am-5pm)</td>
<td>1</td>
</tr>
<tr>
<td>SGLAS</td>
<td>Projected area of south glass (sf)</td>
<td>180</td>
</tr>
<tr>
<td>SHADE</td>
<td>Glass shading coefficient</td>
<td>0.88</td>
</tr>
<tr>
<td>SOLAR</td>
<td>Clearness number (fraction)</td>
<td>.50</td>
</tr>
<tr>
<td>TGLAS</td>
<td>Area of total glass (sf)</td>
<td>540</td>
</tr>
<tr>
<td>UGLAS</td>
<td>Glass U-value (Btu/hr°F*sf)</td>
<td>0.55</td>
</tr>
<tr>
<td>UROOF</td>
<td>Roof U-value (Btu/hr°F*sf)</td>
<td>.0897</td>
</tr>
<tr>
<td>UWALL</td>
<td>Wall U-value (Btu/hr°F*sf)</td>
<td>.1063</td>
</tr>
</tbody>
</table>
analysis of four hours, 6-10am. For this problem, trigger temperatures have been set as follows:

<table>
<thead>
<tr>
<th>Trigger Temperature</th>
<th>Variable</th>
</tr>
</thead>
<tbody>
<tr>
<td>55 °F for 6-7am</td>
<td>TEMP6</td>
</tr>
<tr>
<td>68 °F for 7-8am</td>
<td>TEMP7</td>
</tr>
<tr>
<td>70 °F for 8-9am</td>
<td>TEMP8</td>
</tr>
<tr>
<td>72 °F for 9-10am</td>
<td>TEMP9</td>
</tr>
</tbody>
</table>

By substituting into the prediction equations from page 54 and solving in terms of $\text{ODBMAX} = f(\text{ODBMIN})$, where $\text{ODBMAX}$ and $\text{ODBMIN}$ are the outdoor dry bulb high and low daily temperatures, the prediction equations are reduced to ones having with only two variables:

\[
\begin{align*}
\text{ODBMAX} &= -2.721\times\text{ODBMIN} + 145.6 \quad (6-7am) \quad (5.1) \\
\text{ODBMAX} &= -2.696\times\text{ODBMIN} + 204.2 \quad (7-8am) \quad (5.2) \\
\text{ODBMAX} &= -2.424\times\text{ODBMIN} + 192.4 \quad (8-9am) \quad (5.3) \\
\text{ODBMAX} &= -2.211\times\text{ODBMIN} + 186.1 \quad (9-10am) \quad (5.4)
\end{align*}
\]

These equations can then be graphed, as shown in Figure 5-2. Dashed lines show 10°F and 30°F daily temperature ranges, the limits for which the prediction models were validated. The Trigger Temperature lines are plotted next to determine the critical area during which heat will not be required. (The critical area is shown in Figure 5-2 as a gray band.) The user then selects possible changeover dates from Spring weather days which fall in the critical region.
Figure 5-2  Spring changeover graph
Problem #2

Although hand calculation procedures provide a quick and simple method to determine changeover timing, the user may want to consider hourly building temperature profiles when making changeover decisions. This would involve calculating the hourly building temperatures throughout the entire transitional season. Although this can be done with hand calculation or programmable calculator methods, it is a tedious and time consuming process which could be conveniently handled by a micro-computer.

In this example problem, the same hypothetical office building has been used, but the trigger temperatures now have been set at 55 F and 68 F for all hours. For the computer application of the Trigger Temperature Method, the user inputs the weather as well as the building data, indicating the trigger temperatures and applicable hours to be studied. The summary output (Figure 5-3) selects the weather days for which the most stringent trigger temperature condition is met and marks (*) the satisfactory building temperatures. The temperature profile output (Figure 5-4) graphically plots the hourly building temperatures during the transitional season being studied. With micro-computer applications, the user is able to select a changeover date from the hourly temperature profiles.
### Trigger Temperature Changeover Method

**Building Location:** Harrisburg, PA  
**Clearness Number:** 0.50

**Building Components**

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<thead>
<tr>
<th>Component</th>
<th>U-Value</th>
<th>(SF)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roof</td>
<td>0.0697</td>
<td></td>
</tr>
<tr>
<td>Wall</td>
<td>0.1064</td>
<td></td>
</tr>
<tr>
<td>Glass</td>
<td>0.3500</td>
<td></td>
</tr>
<tr>
<td>Shading Corp</td>
<td>0.8900</td>
<td></td>
</tr>
<tr>
<td>Partitions</td>
<td>0.50</td>
<td></td>
</tr>
</tbody>
</table>

**Building Areas**

<table>
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<th>Area</th>
<th>(SF)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Slab</td>
<td>5000</td>
</tr>
<tr>
<td>East Glass</td>
<td>90</td>
</tr>
<tr>
<td>South Glass</td>
<td>180</td>
</tr>
<tr>
<td>Total Glass</td>
<td>720</td>
</tr>
<tr>
<td>Partitions</td>
<td>1075</td>
</tr>
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</table>

**Gains/Losses**

<table>
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<th>Value</th>
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</thead>
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**Schedule**

- Spring: 7AM-5PM
- Autumn: 7AM-5PM

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**Outdoors Temperatures**

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**Figure 5-3 Trigger Temperature Method Summary Output**
Range of Application

As demonstrated by the two previous example problems, the Trigger Temperature Method provides a valuable tool for facility managers or engineers to evaluate heating needs during Fall and Spring seasons. This methodology is based upon maintaining a user defined comfort level when the building does not benefit from an available heating system. It can provide accurate and useful results when applied within the conditions for which the prediction models have been validated. The user must be careful to limit applications of the Trigger Temperature Method to those within the range of applications listed in Table 5-3.
Table 5-3

Trigger Temperature Method range of application

### INDEPENDENT VARIABLES

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<td>East glass (% of east wall)</td>
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<tr>
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<td>Masonry construction (density lbs/sf)</td>
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| **Internal Gains**                 |         |         |
| Lights, equip gains (watts/sf)     | 1.5     | 3.9     |
| Infiltration (air changes/hr)      | 0.25    | 3.0     |
| Occupancy schedule                 | 7am-5pm | 8am-5pm |
| Occupants (people/1000 sf)         | 0       | 14      |
| Area of partitions (sf)            | 0       | 15700   |
| Density of partitions (lbs/sf)     | 6.16    | 59.1    |
| Heat recovery system (70% eff)     | no      | yes     |

| **Weather Factors**                |         |         |
| Clearness number (fraction)        | 0.00    | 0.98    |
| Ground temperature (F)             | 44      | 59      |
| Outdoor dry bulb temp max (F)      | 28      | 84      |
| Outdoor dry bulb temp min (F)      | 18      | 54      |
| Daily temp range (F)               | 10      | 30      |

### DEPENDENT VARIABLES

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<td>Indoor temp from 8-9am (F)</td>
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<td>TEMP9</td>
<td>Indoor temp from 9-10am (F)</td>
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CHAPTER SIX

CONCLUSIONS AND RECOMMENDATIONS

Summary

Existing methods which could be used for changeover estimation have serious deficiencies in accuracy and application. Steady state heating load calculation procedures lack precision in calculating hourly building temperatures because solar gains and building capacitance effects are not considered. Computer simulations perform accurate heat transfer analyses, but are time consuming and expensive to use.

Changeover decisions are usually the responsibility of a facility manager. A methodology to determine changeover timing should provide the facility manager a procedure to maximize energy savings without sacrificing building occupant comfort. It should be flexible and precise, yet simply applied by engineers and non-engineers alike.

Conclusions

The key concern in a changeover method is the level of occupant thermal comfort. Changeover timing can be
developed in terms of an occupant comfort threshold, or "trigger temperature". When comfort conditions can be maintained without mechanical heating, changeover can be made.

Statistical analysis methods can be used to determine the weather, building envelope, and occupant use characteristics critical to facilities during transitional seasons. Through multiple regression techniques, prediction equations can be generated to calculate building temperatures.

The Trigger Temperature Method provides an accurate, yet straightforward method for changeover determination. User input information is tailored to use widely available weather data and engineering standardized building envelope descriptions. Both hand calculation and micro-computer applications are offered.

**Recommendations for Future Study**

The Trigger Temperature Method should be extended to include different building types and occupancies. The BLAST simulated data base should be enlarged to encompass varying envelope constructions, floor plan layouts, and occupancy schedules. Multiple regression analysis methods should be used to evaluate new variables and develop broader, more general prediction equations.
Changeover criteria for air-conditioning should be developed. Trigger temperature concepts can be extended to describe cooling equipment changeover timing in terms of occupant comfort.

Comfort conditions for facility occupants should be expanded to consider the mean radiant temperature effects in a building. Trigger temperatures can be described in terms of the operative temperatures to more effectively assess occupant comfort.

Sensitivity analyses should be made to study how thermal storage may be designed to boost morning building temperatures. Thermal flywheel effects could significantly alter changeover conditions, offering an extended application for the Trigger Temperature Method.

Probability studies should be performed on multi-year weather data. Trigger Temperature prediction models should be used to assign probability risk factors associated with each calendar date.
REFERENCES


APPENDIX A

MODEL DEVELOPMENT STATISTICS

The Trigger Temperature Method uses statistical prediction models to determine building temperatures from 6-10am. The prediction models were developed from multiple regression analysis of Building Loads Analysis and System Thermodynamics (BLAST) computer simulations.

Regression Statistics

Regression models were developed and tested against goals defined for three statistics:

1. Coefficient of Determination (\( R^2 \))
2. Coefficient of Variation (C.V.)
3. F test for parameter significance

This appendix presents the statistical analysis results used to select the final prediction models. Individual model statistics and residual plots are included. The individual model statistics are presented in Tables A-1 through A-4. Residual plots are shown in Figures A-1 through A-4. User information and variable descriptions are included in Appendix B.
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<tr>
<td>14</td>
<td>---</td>
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<td>0.980</td>
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<tr>
<td>17</td>
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<td>---</td>
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<tr>
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<td>SHADE</td>
<td>---</td>
<td>0.984</td>
</tr>
<tr>
<td>19</td>
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<td>ELEC2</td>
<td>---</td>
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<td>SGLAS1</td>
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Table A-4 TEMP9 regression statistics

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<th>Dropped Variable Terms</th>
<th>Added Variable Terms</th>
<th>R Squared Value</th>
<th>C. V. Value</th>
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<td>TAVE</td>
<td>0.468</td>
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<td>ADPART</td>
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<td>0.956</td>
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<td>---</td>
<td>UWALL</td>
<td>0.965</td>
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<td>EGLAS2</td>
<td>0.970</td>
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<td>UROOF</td>
<td>0.974</td>
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<td>0.978</td>
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<td>0.779</td>
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<td>ASLAB</td>
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</table>
TEMP6 residual plot
Temperature residuals plot for 7AM-8AM predicted temperature. The residuals are plotted against the predicted temperature in degrees Fahrenheit.
8AM-9AM PREDICTED TEMPERATURE (F)

TEMP8 residual plot
9AM-10AM PREDICTED TEMPERATURE (°F)

TEMP9 residual plot
APPENDIX B

USER INPUT INFORMATION

This appendix provides user input information for the Trigger Temperature Method. Descriptions of the variables and the prediction equations for the hours of 6-10am are included.

Variable Information

Two types of variables are used in the Trigger Temperature Method prediction equations. Continuous variables are expressed in the engineering units shown in Table B-1. Indicator variables are used to describe several building operation schedule options. Tables B-2 and B-3 present user information for the two indicator variables included in the prediction equations.

Prediction Equations

The statistical regression analysis described in Chapter Four, developed the final prediction equations as a function of variables and transformations (variable terms). In order to simplify the procedures which would be required for hand calculation methods, all prediction equations have...
been expressed in terms of single variables only. Final model prediction equations are listed in Table B-4.

Table B-1

Continuous Variables

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>APART</td>
<td>Area of partitions</td>
<td>sf</td>
</tr>
<tr>
<td>ASLAB</td>
<td>Area of building slab</td>
<td>sf</td>
</tr>
<tr>
<td>DPART</td>
<td>Density of partitions</td>
<td>lbs/cf</td>
</tr>
<tr>
<td>EGLAS</td>
<td>Projected area of east glass</td>
<td>sf</td>
</tr>
<tr>
<td>ELEC</td>
<td>Lights and equip gains</td>
<td>watts/sf</td>
</tr>
<tr>
<td>INFIL</td>
<td>Infiltration</td>
<td>air changes/hour</td>
</tr>
<tr>
<td>SGLAS</td>
<td>Projected area of south glass</td>
<td>sf</td>
</tr>
<tr>
<td>SHADE</td>
<td>Glass shading coefficient</td>
<td>fraction</td>
</tr>
<tr>
<td>SOLAR</td>
<td>Clearness number</td>
<td>fraction</td>
</tr>
<tr>
<td>TGLAS</td>
<td>Area of total glass</td>
<td>sf</td>
</tr>
<tr>
<td>ODBMAX</td>
<td>Outdoor dry bulb temp max</td>
<td>°F</td>
</tr>
<tr>
<td>ODBMIN</td>
<td>Outdoor dry bulb temp min</td>
<td>°F</td>
</tr>
<tr>
<td>UGLAS</td>
<td>Glass U-value</td>
<td>Btu/hr<em>F</em>sf</td>
</tr>
<tr>
<td>UROOF</td>
<td>Roof U-value</td>
<td>Btu/hr<em>F</em>sf</td>
</tr>
<tr>
<td>UWALL</td>
<td>Wall U-value</td>
<td>Btu/hr<em>F</em>sf</td>
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</table>
Table B-2
Final model indicator variables

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description (use)</th>
<th>Value</th>
<th>HVAC</th>
<th>(Heat recovery system option)</th>
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<tr>
<td></td>
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</table>

SCHED1 (Hours of full occupancy and lighting)

|          |          |       |      | 0 | 8am to 5pm - 100% occupancy and lighting loads |
|          |          |       |      | 1 | 7am to 5pm - 100% occupancy and lighting loads |

Table B-3
Building schedule options

<table>
<thead>
<tr>
<th>Variable</th>
<th>Schedule</th>
<th>Solar time</th>
<th>Values</th>
<th>Option</th>
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<th>07-08</th>
<th>08-17</th>
<th>17-06</th>
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</tr>
<tr>
<td>HVAC</td>
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<td>100</td>
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</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Recov.</td>
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<td></td>
<td></td>
<td>Recov.</td>
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<td>0</td>
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</tr>
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<td>HVAC</td>
<td>0</td>
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<td>Lights</td>
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<td>5</td>
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<td></td>
<td></td>
<td>Recov.</td>
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<td>0</td>
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<td>100</td>
<td>100</td>
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Table B-4

Trigger Temperature prediction equations

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<th>Temperature</th>
<th>Equation</th>
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<td>$49.72 + ODBMIN*(.2148 + 1.1841<em>INFIL) + .1297</em>ODBMAX -11.97<em>INFIL + SOLAR</em>(3.634 + .008542<em>EGLAS</em>SHADE) - .001418<em>TGLAS - 20.587</em>UROOF - 15.029<em>UWALL - 4.5821</em>UGLAS + ELEC*(.7916 + .4407*SCHED1)</td>
</tr>
<tr>
<td>TEMP7</td>
<td>$50.10 + INFIL*(-12.48 + 9.019<em>HVAC</em>SCHED1) + ODBMIN*(.2367 + INFIL*(-1.12.48 + 9.019<em>HVAC</em>SCHED1)) + .1360<em>ODBMAX + SOLAR</em>(4.19 + .01367<em>EGLAS) - 22.431</em>UROOF - 16.424<em>UWALL - 5.0432</em>UGLAS - 1.926<em>APART</em>DPART<em>10**-5 + ELEC</em>(.5775 + 2.383<em>SCHED1) - 33.05</em>ASLAB<em>10**-5 + .0454</em>PEOPLE</td>
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</table>