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SEISMOLOGICAL DISCRIMINATION AND
YIELD DETERMINATION RESEARCH

FINAL REPORT

SYSTEMS, SCIENCE AND SOFTWARE
P.O. Box 1620
La Jolla, California 92038

June 1981

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   This report summarizes work conducted by Systems, Science and Software concerning the generation, propagation, detection and analysis of seismic waves by both nuclear explosions and earthquake sources. Specific topics covered included numerical simulation of the near field ground motion from earthquakes and explosions, automatic signal processing relating to the detection of seismic events and magnitude determination, a compilation of near
7. Authors (continued)

J. R. Murphy, T. J. Bennett, M. G. Brown, K. D. Pyatt and H. J. Swanger

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source data and the synthesis of this data in terms of the seismic source function, and the determination of the spectral characteristics of acoustic waves from an explosion near the ocean surface.
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Project Scientist and Phone No.
Mr. Brian W. Barker, (202) 325-7581

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I. INTRODUCTION AND SUMMARY

1.1 INTRODUCTION

The objective of the Systems, Science and Software (S3) research program is to extend our present understanding of the generation, propagation, detection and analysis of seismic waves by both underground explosions and earthquake sources. The goal is to improve the United States' ability to monitor compliance with treaties limiting underground nuclear explosions. This report covers work performed at S3 during the twelve month contract period between 1 October 1979 and 1 October 1980, under Contract Number F08606-79-C-0008 (VSC Project VT/0712).

The report includes six distinct technical sections, which are briefly summarized below, together with the references to the appropriate task in the Work Statement of the contract. Much of this work has been described previously in several S3 topical and technical reports. In such cases, we have provided an executive summary of the work performed during the contract period, including a digest of the principal conclusions and the relevant figures.

1.2 SUMMARY OF SECTION II: SEISMIC SOURCE CALCULATIONS

This section contains three subsections.

- Development of a constitutive model for salt based on an analysis of free-field ground motion data for nuclear and high explosive events in salt. The events included GNOME, SALMON, STERLING and COWBOY. Because of the large body of digitized data available for SALMON, this event was chosen for normalization purposes. The purpose was to explain
simultaneously all observations with a single constitutive model for salt so as to permit development of realistic decoupling scenarios. Good agreement with data from STERLING and GNME was produced. For COWBOY, predicted and observed peak velocities were in agreement, but predicted peak displacements were larger than those observed by a factor of two. This work was done by Dr. J. Theodore Cherry and Dr. Norton Rimer.

Analysis of the dynamical aspects of seismic sources which yield different signatures for earthquakes and explosions was conducted through numerical simulations of earthquake sources. The simulations were performed on the ILLIAC IV computer, using a three-dimensional finite difference code. Inelastic response along the fault zone was modeled through nonlinear boundary conditions on the fault plane. As a result of this work, it appears necessary to include more complex rupture physics in the modeling procedure, and, in particular, a better description of the cessation of rupture is required to explain the discrepancies between modeled and observed stopping phases. Stress irregularities have been shown to have a significant influence on the spectral- and time-domain characteristics of the teleseismic signals from earthquakes; they tend to increase the separation of earthquake and explosion populations for the mb-Ms discriminant. This work was performed by Dr. Steven M. Day.
A simulation study for a (hypothetical) fully decoupled 5.3 KT explosion at the SALMON site was conducted by scaling regional phases recorded in the eastern United States for SALMON. Such an event could probably be detected at epicentral distances up to ~650 km, but not at distances greater than ~1000 km. For low-noise conditions, the Lg phase would probably be detected at distances up to ~1500 km, but not the initial P phase. This study was performed by Mr. John R. Murphy and Dr. T. Joseph Bennett.

1.3 SUMMARY OF SECTION III: REGIONAL SEISMOLOGY

This section pertains to a study of far-field seismic waves associated with a series of two-dimensional calculations of buried explosions. The purpose was to determine the importance of nonlinear free surface interactions, including spallation, and the depth dependence of overburden pressure and rheology. These effects result in higher order source properties, which constitute a departure from the classical spherically symmetric point source approximation. This work has been the subject of a detailed report by Drs. Thomas C. Bache, Terrance G. Barker, Norton Rimer and J. Theodore Cherry (1980) and we only include the executive summary for completeness.

1.4 SUMMARY OF SECTION IV: AUTOMATIC SIGNAL PROCESSING

This section includes two subsections.

- A review of the MARS (Multiple Arrival Recognition System) detector. The MARS-based detection algorithm was optimized
and an efficient code was tested on an off-line basis on data supplied by VELA Seismological Center (VSC). This subsection was written by Dr. William E. Farrell, Mr. Robert C. Goff and Mr. James Wang.

A review of state-of-the-art detection algorithms, by Dr. Jonathon Berger. This section identifies and evaluates all pertinent automatic detection algorithms, and provides a classification by equation, mathematical derivation, and usage history. It includes algorithms currently under development and scheduled to be validated by October 1981. In addition, recommendations for further research efforts are made.

1.5 SUMMARY OF SECTION V: EVALUATION OF SUITES OF EVENTS

This section summarizes work by Dr. Thomas C. Bache and Mr. Boris Shkoller which is described more fully in a semiannual technical report by Bache, et al. (1980). It pertains to the automatic determination of body wave magnitudes using the MARS processor, and the testing of a similar automatic surface wave magnitude estimator. Particular attention is paid to the effect of seismic noise, which are evaluated by superposition of a signal with known magnitude and seismic noises of varying levels. The results appear to be robust with respect to noise even in the case of high noise level.

Applications to actual records from Eurasian events at RKON have also been performed and have been described in the aforementioned report.
1.6 SUMMARY OF SECTION VI: GROUND MOTION ANALYSIS

This work, by Mr. John R. Murphy and Dr. T. Joseph Bennett pertains to the compilation and evaluation of near-source data from underground explosions. In particular, an assessment of the data set in terms of the seismic source function for different emplacement media has been conducted. The expanded data set includes previously unpublished data from the Sandia Corporation archives. A detailed report has been provided by Murphy and Bennett (1980).

1.7 SUMMARY OF SECTION VII: ACOUSTIC WAVES FROM EXPLOSIONS IN THE OCEAN

The results for this section have been reported by Bache, et al. (1980). They specifically include estimates of the gross spectral characteristics and signal duration of acoustic waves generated by a nuclear explosion near the ocean surface. A nominal yield of 1 KT and nominal range of 6600 km are assumed.
II. SEISMIC SOURCE CALCULATIONS

2.1 INTRODUCTION

Investigations of seismic sources by theoretical and numerical calculations were covered by three tasks:

One- and two-dimensional explosion calculations (Task 4.1.1). (See also Section II, Task 4.2.)

Earthquake simulation studies using the ILLIAC IV (Task 4.1.2).

Decoupling-evasion research (Task 4.1.3).

Progress accomplished under these tasks during the contract period is described in the following subsections, where specific references are made to reports in which greater detail can be found.

2.2 A CONSTITUTIVE MODEL FOR SALT BY J. T. CHERRY AND N. RIMER

Several numerical calculations of underground explosions performed at S3 have been used principally in Task 4.2, and the results are summarized in Section II of this report.

In this subsection, we focus on calculations designed to permit development of realistic decoupling scenarios in salt. For this purpose, it is necessary to understand free field motion data for actual explosions in this material. We have used ground motion data from nuclear and high explosive events including GNOME, SALMON, STERLING and COWBOY.

Because the SALMON event provided a large subset of the data, and because many of the associated records are available in digital form, we chose this event for the purpose of normalizing the constitutive model. This model was then applied to the other events, in order to determine how much
of the salt ground motion observations could be explained using a single constitutive model.

This procedure produced good agreement with the ground motion data from STERLING and GNOME. The predicted peak displacements for the tamped COWBOY shots were approximately a factor of two greater than those observed. However, predicted and observed peak velocities for COWBOY were in close agreement.

2.2.1 Normalization to SALMON

Figure 1 shows the laboratory strength data for SALMON, GNOME and polycrystalline salt. The curve shown in the figure fits the data for SALMON and GNOME and was used in the model for the ultimate strength of salt \( Y_{\text{lim}} \).

The best agreement with the SALMON ground motion data was obtained by assuming that salt work hardened to its ultimate strength. The expression used to calculate the strength \( Y \) as a function of the inelastic energy \( E \) deposited in the material during yielding was

\[
y = Y_0 (1 + e_1 E - e_2 E^2) \leq Y_{\text{lim}}
\]  

(1)

where \( Y_0 \) is the initial (saturated) strength and \( e_1 \) and \( e_2 \) are respectively work hardening and work softening material constants.

If \( S_{ij} \) is the deviatoric component of the stress tensor and \( J_2' \) is the unadjusted second deviatoric invariant, then the increment in inelastic energy becomes

\[
\Delta E = S_{ij} \Delta \pi_{ij} = \frac{S_{ij} S_{ji}}{2\mu} \sqrt{3J_2'} - Y
\]  

(2)
where

\[ 3 J_2^2 > \gamma^2 \]

\( \pi_{ij} \) = the deviatoric component of the inelastic strain tensor

\( \mu \) = the shear modulus.

This model is simple and easily implemented in a finite difference stress wave code. The physical basis for the work hardening aspect of the model may be an increase in effective stress, and conversely a decrease in pore fluid pressure, caused by dilatancy. If this is the case, then \( Y_0 \) is the saturated material strength. During shock loading microcracks open, the pore fluid pressure decreases and the strength increases. During release, the cracks close, pore fluid pressure increases and strength decreases. These modes of material behavior are quantitatively contained in the model with the rate of hardening and softening determined by the constants \( e_1 \) and \( e_2 \).

Figure 2 compares the calculated and observed ground motion from SALMON at a range of 620 m where the calculations were performed with the work hardening model. The emergence of a precursor with a peak velocity of approximately 0.5 m/s is adequately modeled by assuming a saturated strength \( (Y_0) \) of 25 bars. Work hardening is required in order to match the observed pulse shape. At a radius of 967 m, the peak velocity in the calculation is determined by the precursor. Elastic material behavior occurs beyond this radius in the calculation.

Figure 3 compares calculated and observed peak velocities and peak displacements. The results of two calculations are shown in this figure; one (dashed curve) in which \( Y_{lim} \) equaled the maximum strength (0.68 kb) given in Figure 1, and
Figure 2. Comparison between calculated (dashed curve) and observed (solid curve) ground motion from SALMON at a range of 620 m.
Figure 3. Comparison between calculated and observed peak velocities and displacements for SALMON.
the second (solid curve) in which $Y_{\text{lim}}$ varied with stress state ($\overline{P}$) as shown in Figure 1.

Figure 4 shows the RVP spectra ($|\tilde{\Phi}|$) for these two calculations. Also shown are the spectra of Springer, et al. (1968), which represents an average of the free field SALMON data, and Murphy, which was obtained by scaling the spectrum of the GNOME event to the yield and depth of SALMON.

These results, involving comparisons between calculated and observed ground motions and RVP spectra indicate that the constitutive model adequately explains the SALMON data. We now apply this model to other salt events.

2.2.2 STERLING

Simulation of the STERLING event was accomplished by detonating 0.38 KT in the SALMON cavity. The RVP spectrum for STERLING was calculated and divided into the calculated SALMON spectra shown in Figure 4 ($Y_{\text{lim}} = Y_{\text{max}}$). The resulting spectral ratios are shown in Figure 5. In this figure we also show the averaged spectral ratios obtained by Springer, et al. (1968) from seismic stations common to the two shots. Agreement is excellent over the frequency range analyzed by these investigators.

2.2.3 GNOME

The GNOME event was simulated using the work hardening model. Figures 6 and 7 compare calculated and observed peak velocities and displacements for this event. The calculated elastic radius was 790 m.

Figure 8 compares the Mueller-Murphy estimate of the GNOME RVP spectrum with the calculated spectrum. Agreement is surprisingly good considering that the Mueller-Murphy spectrum was based on ground motion data at a range of 300 m, a distance well within the region of nonlinear material behavior.
Figure 4. Comparison of calculated and observed RVP spectra for SALMON.
Figure 5. Calculated and observed spectral ratios for SALMON/STERLING.
Figure 6. Comparison of calculated and observed peak velocities for the GNOME event.
Figure 7. Comparison of calculated and observed peak displacements for the GNOME event.
Figure 8. Comparison of calculated and observed RWP spectra for GNOME.
2.2.4 COWBOY

Figures 9 and 10 compare calculated and observed peak velocities and peak displacements for the tamped shots in the COWBOY series. Agreement is good for peak velocities. However, the calculated peak displacements are a factor of two larger than those observed.

There are a number of possible explanations for this result, e.g., the COWBOY salt was not saturated, the HE was not adequately simulated, the peak displacements were not free field, the charge emplacement was not consistent with a spherically symmetric geometry, the material properties (strength and wave velocities) of the COWBOY salt are different from GNOME and SALMON.

These issues are worth pursuing, but not here. Our objective was to develop a constitutive model for salt based on SALMON ground motion data and then to determine its range of applicability for other salt events. The results of the model are consistent with data from STERLING and GNOME. They are not consistent with the data from the tamped COWBOY series.

2.3 EARTHQUAKE SIMULATION STUDIES USING THE ILLIAC IV
BY S. M. DAY

Differentiation of earthquakes from underground nuclear explosions on the basis of their seismic signatures ultimately depends on features related to the details of source dynamics. We have conducted a series of numerical calculations on the ILLIAC IV computer designed to provide a realistic three-dimensional model of the earthquake rupture phenomenon. These are dynamical simulations, which can be compared in turn with simple elastostatic or kinematical solutions in order to help identify the effect of rupture complexities on the observable seismograms. This research has been previously reported by Bache, et al. (1980a).
Figure 9. Comparison of observed and calculated peak velocities for the tamped COWBOY events.
Figure 10. Comparison of observed and calculated peak displacements for the tamped COWBOY events.
We are using a three-dimensional finite difference method to model the features of earthquake dynamics believed to be important for predicting the teleseismic signal. The calculations have simulated inelastic response of the fault zone through nonlinear boundary conditions on the fault plane. The numerical method admits more general nonlinear material behavior, which is being incorporated as required.

Our initial numerical simulations were for a simple, constant rupture velocity, constant stress-drop earthquake model. These results show a significant influence of fault width on the slip function. For points on the fault which are more than a fault width away from the focus, the slip function is spatially quite uniform. The static slip is given by $\Delta \sigma w/\rho \beta^2$, in agreement with estimates based on elastostatic solutions. The numerical simulations predict a rise time of $w/2\beta$ and peak slip velocity of $\sqrt{2f_w} \Delta \sigma/\rho \beta$. In these expressions, $w$ is the fault width, $\Delta \sigma$ the stress-drop, $f$ the maximum frequency, $\beta$ the shear speed, and $\rho$ the density.

Careful studies of the broadband character of earthquake teleseismic signatures indicate that the relative excitation of long- and short-period waves is inconsistent with predictions from the simple model. In addition, a few isolated, severe stopping phases dominate near-field accelerograms synthesized from the simple model, in conflict with strong motion data. More complex rupture physics is required to explain the discrepancies between the model predictions and teleseismic and strong motion observations. In particular, a better physical description of the cessation of rupture growth appears necessary.

A displacement-weakening constitutive model, described by Figure 11, has been applied to simulate spontaneous rupture in the presence of both uniform and heterogeneous prestress.
Figure 11. Displacement-weakening constitutive model for the fault zone.
In this model of failure, the shear strength of the fault zone is assumed to be a decreasing function of its deformation; energy is dissipated during rupture extension and shear stress is bounded on the fault edges. When rupture initiates in a limited region of high stress (Figure 12a), the model leads to spontaneous propagation, deceleration and stopping of faulting. Figure 13 shows the evolution of the rupture front in this case, as well as the far-field P and S wave displacement spectra and the corresponding displacement, velocity, and acceleration pulses. In the presence of multiple high-stress regions (Figure 12b), each isolated stress concentration behaves roughly as an independent event. As shown in Figure 14, rupture velocity becomes quite irregular, and is strongly coupled to peak velocity of slip on the fault surface. Figure 15 shows the irregular rupture growth, as well as the far-field spectra and time-domain pulses which result. Predicted accelerograms are in better qualitative accord with strong motion data.

The model predicts significant consequences for the spectral and time-domain characteristics of the earthquake teleseismic signal due to the presence of stress irregularities. For example, Figure 16 compares the short-period teleseismic P-wave for the stress-concentration model with that for a uniform stress model (scaled to a source dimension equal to the dimension of the stress concentration). Both the period and amplitude of the $b$ phase (first peak-to-trough) agree for the two models, while the stress-concentration model has twice the moment of the uniform stress model. The two events have been superimposed on an $m_b$ versus $M_s$ plot (from Filson and Bungum, 1972) to illustrate that the stress-concentration phenomenon enhances separation of earthquake and explosion populations.
(a) STRESS-CONCENTRATION MODEL  (b) MULTIPLE STRESS-CONCENTRATION MODEL

Figure 12. Stress-concentration fault models considered in this study.
Figure 13. Rupture mechanism and far-field spectra and pulse shapes for stress concentration earthquake model at spherical coordinates $\theta = 45^\circ$, $\phi = 45^\circ$, relative to fault normal.
Figure 14. Peak slip velocity (low-passed, 5 Hz cutoff) and rupture velocity along the x axis, for multiple stress-concentration model. Dashed curves for rupture velocity indicate regions which ruptured out of sequence. For example, rupture occurred at x = 5.6 km while the region between 5.0 and 5.6 km was still intact.
Figure 15. Rupture mechanism and far-field spectra and pulse shapes for multiple stress-concentration earthquake model (at spherical coordinates $\theta = 45^\circ$, $\phi = 45^\circ$ relative to fault normal).
Figure 16. Short-period P-waves from uniform stress model and stress concentration model. The two events are plotted as triangles on an $m_b$-versus-$M_b$ diagram (from Filson and Bungum), in which open circles and closed circles represent presumed explosions and earthquakes, respectively.
2.4 A SIMULATION STUDY OF THE DETECTABILITY OF A 5.3 KT DECOUPLED EXPLOSION AT REGIONAL DISTANCES IN THE EASTERN UNITED STATES BY J. R. MURPHY AND T. J. BENNETT

A detailed description of this research has been previously provided in the Semiannual Technical Report by Bache, et al. (1980a). For completeness, we include below an executive summary of objectives and accomplishments.

2.4.1 Objective

The objective of this task has been to conduct a preliminary theoretical evaluation of CTBT evasion capabilities associated with the cavity decoupling evasion scenario. In particular, the investigation has focused on extending the existing regional seismic data base for explosions in the eastern United States by theoretically scaling observed SALMON data to simulate the seismograms to be expected from a hypothetical, fully decoupled 5.3 KT explosion at the SALMON shotpoint.

2.4.2 Accomplishments

Four eastern United States stations were selected for analysis: Eutaw, Alabama (EUAL, \( \Delta = 246 \) km), Cumberland Plateau Observatory, Tennessee (CPO, \( \Delta = 623 \) km), Beckley, West Virginia (BLWV, \( \Delta = 1065 \) km) and Wykoff, Minnesota (WFMN, \( \Delta = 1437 \) km). The locations of these four stations are indicated by squares on Figure 17 which provides a map view of the North American Stations which recorded the SALMON event (Jordan, et al., 1966). The observed vertical component SALMON data recorded at these four stations have been theoretically scaled (Murphy, 1977) to the ground motion to be expected from a fully decoupled 5.3 KT explosion at the SALMON shotpoint. The selected theoretical decoupling factor (with respect to SALMON), corresponding to a simple step in pressure in a 39 m radius...
Figure 17. Map locations of regional SALMON stations used in the decoupling simulation.
cavity, is shown in Figure 18. Observed SALMON vertical component seismograms recorded at stations EUAL and WFMN are shown at the top of Figures 19 and 20 respectively, where they are compared with the corresponding simulated decoupled seismograms (bottom). The simulated decoupled seismograms were obtained by convolving the observed SALMON seismograms with an operator defined by the ratio of the decoupled to SALMON theoretical source functions. The traces shown to the left of the simulated decoupled seismograms correspond to samples of the noise recorded prior to SALMON at each station, amplified so that they can be compared with the estimated decoupled signal levels. This provides a basis for assessing the detectability of the hypothesized decoupled explosion at these stations under the local noise conditions prevailing at the time of the SALMON experiment. A review of this simulated data, as well as that from the other two selected stations, indicates that, relative to the noise background prevailing during SALMON, a 5.3 decoupled explosion would probably have been detectable on the short-period recordings from the two nearer stations (EUAL and CPO) but not from those expected at the more distant stations (BLWV and WFMN). With respect to the lower noise background expected at a modern, quiet site, the Lg phase from such a decoupled explosion would probably be detectable at all four stations, but initial P wave detection would still be questionable at the two distant stations. Furthermore, as might be expected on the basis of previous noise studies, increasing the effective bandwidth of the short-period data to encompass lower frequencies does not improve this detectability due to the fact that the noise level increases with decreasing frequency while the decoupling factor remains essentially constant. By the same argument, consideration of higher frequency data should improve detectability, at least for high Q paths. However, it has not been possible to quantitatively evaluate
Figure 18. Theoretical decoupling factor for 5.3 KT in a 39 m radius cavity in SALMON salt.
Figure 19. Comparison of observed SALMON and simulated decoupled vertical component seismograms, Station EUAL.
Figure 20. Comparison of observed SALMON and simulated decoupled vertical component seismograms, Station WFMN.
this potential improvement using the available data set due to the relatively low sampling rate employed in the digitization.
III. REGIONAL SEISMOLOGY

3.1 INTRODUCTION

The work reported in this section pertains to Task 4.2. It must be noted that several of the numerical calculations performed under Task 4.1.1 for buried explosions have been used extensively for the purposes of the present task and have, therefore, not been described in Section 2.2 of this report.

The results pertinent to the present section have been the object of a detailed report by Bache, et al. (1980b). They have also been summarized in the Semiannual Technical Report by Bache, et al. (1980a). For this reason, we only include for completeness an executive summary in the following subsection.

3.2 CONTRIBUTION OF TWO-DIMENSIONAL SOURCE EFFECTS TO THE FAR-FIELD SEISMIC SIGNATURES OF UNDERGROUND NUCLEAR EXPLOSIONS BY T. C. BACHE, T. G. BARKER, N. RIMER AND J. T. CHERRY

3.2.1 Objective

As the contract evolved, the objective of Task 4.2 became to study the far-field seismic waves from a series of two-dimensional explosion calculations done under Task 4.1.1. The purpose was to determine the importance of nonlinear interaction with the free surface (including spallation) and the depth-dependence of overburden pressure and material properties. While the potential importance of these two-dimensional effects has long been acknowledged, previous attempts to model the seismic signatures of underground explosions have almost all employed spherically symmetric point source representations. A quantitative understanding
of the potential influence of higher order source effects is important for delineating the validity of this convenient approximation.

3.2.2 Accomplishments

The results summarized here are extracted from a 1980 S3 report by Bache, Barker, Rimer and Cherry. The report presents a detailed analysis of the seismic waves from eleven two-dimensional finite difference calculations of underground nuclear explosions in granite. Seven were 150 KT explosions at depths from 159 to 1000 meters done by J. Trulio and N. Perl of Applied Theory, Inc. (ATI).

The other four calculations were done at S3 with one intended to model the PILEDRIVER event. The constitutive model and source geology (three layers) were chosen for this particular event. As described by Rimer, et al. (1979), the computed and observed ground motions were compared at some twenty-five near-field gauge locations, where the agreement was quite good, except that the calculation overpredicted the amount of cracking (spallatic. This turns out to be important when comparing synthetic and observed far-field seismograms. The other three S3 calculations were the same, except that the depth and yield were varied. The four calculations were as follows:

<table>
<thead>
<tr>
<th>DEPTH (Meters)</th>
<th>YIELD (KT)</th>
</tr>
</thead>
<tbody>
<tr>
<td>463</td>
<td>60 (PILEDRIVER)</td>
</tr>
<tr>
<td>1000</td>
<td>150</td>
</tr>
<tr>
<td>1000</td>
<td>20</td>
</tr>
<tr>
<td>400</td>
<td>20</td>
</tr>
</tbody>
</table>
The main results of the study may be summarized by plots of $M_s$ and $m_b$ versus source depth and yield. The observed values for the United States granite explosions PILEDRIVER, SHOAL and HARDHAT provide a standard for comparison.

In Figure 21, the $M_s$ for all eleven calculations are plotted versus source depth. For this plot all $M_s$, including the observed value for PILEDRIVER, have been scaled to 150 KT by adding $\log(150/W)$.

In Figure 22, the $M_s$ values are plotted versus yield. Also shown are the $M_s$ from seismograms computed with reduced displacement potential (RDP) sources. The RDP calculations were done at $S^3$ for two depths (460 and 1000 meters) with the same constitutive models used for the two-dimensional calculations. Thus, comparing seismograms from the RDP and the two-dimensional calculations directly displays the influence of two-dimensional effects.

The $m_b$ data from the ATI and $S^3$ source calculations are plotted versus source depth in Figure 23 and versus yield in Figures 24 and 25. Again, the values for comparable RDP sources are shown to directly display the two-dimensional effects predicted by the $S^3$ calculations.

The most important result of this study is that the $S^3$ calculations show $M_s$ to be a strong function of depth. The shallow $S^3$ calculations have surface wave amplitudes that are a factor of two or three larger than those from a comparable one-dimensional source calculation. This effect is probably exaggerated because the free-surface interaction effects are too large in the $S^3$ calculations, but would remain important even with increased strength in the near-surface material. On the other hand, the ATI calculations show no strong dependence of $M_s$ on depth, even though the shallow ATI sources cratered. We do not know why the two sets of calculations give such different results.
Figure 21. The $M_s$ values for all the two-dimensional calculations are plotted versus source depth. The observed value for PILEDRIVER is also shown. All magnitudes have been scaled to 150 KT.
Figure 22. The $M_s$ values for the $S^3$ RDP and two-dimensional source calculations are plotted versus explosion yield. The PILEDRIVER observed value and the range of $M_s$ for the seven 150 KT ATI sources are also shown. The source depth of the $S^3$ two-dimensional calculations is noted with the $M_s$. 
Figure 23. The $m_b$ values for all the two-dimensional calculations are plotted versus source depth. The $S^3$ calculations at the same yield are connected with a dashed line. The observed values for HARDHAT, SHOAL, and PILEDIVER are also plotted with $m_B = m_D - 0.25$. All magnitudes have been scaled to 150 KT.
Figure 24. The b phase magnitude, $m_b$, is plotted versus yield. The values for the ATI calculations fall within the indicated range. The observed values are the published $m_b$ minus 0.25 for HARDHAT, SHOAL and PILEDIVER.
Figure 25. The c phase magnitude, \( m_c^C \) is plotted versus yield. Published (network average) magnitude values for HARDHAT, SHOAL and PILEDRIVER are also plotted.
Comparison of waveforms, as well as the magnitude data in the plots, leads to the following conclusions:

**Applied Theory, Inc. Calculations**

- Neither \( m_h \) nor \( M_s \) are strongly dependent on depth. The most effect was on \( M_s \) at shallow depths.

- Compared to the semiempirical RDP source of Mueller and Murphy (1971), depth dependence in both amplitude and corner frequency is less for the ATI sources.

- The \( pP \) phase appears to be smaller than expected from elastic theory.

**Systems, Science and Software Calculations**

- Two-dimensional effects are not very important for the two deep explosions (20 KT and 150 KT at 1000 meters). Both \( m_b \) and \( M_s \) are little different from the values estimated from an RDP source computed with the same constitutive model at the same depth.* It is gratifying that these two very different and complex procedures arrive at the same results. This is true even though considerable cracking and spallation occur in the two-dimensional calculations.

- For body waves the first arriving P wave is essentially the same for one- and two-dimensional sources.*

- The two-dimensional effects enhance the surface wave amplitudes for the shallow events (60 KT at 463 meters and 20 KT at 400 meters) by a factor of two or three. We must qualify this by pointing out that these shallow calculations have very strong surface interaction effects. Comparison with PILEDRIVER data indicates that the free surface interaction is

* These results are essentially tests of the entire computational procedure.
overpredicted, at least for that event. Less free surface interaction would presumably give less enhancement of the surface wave amplitudes.

- For the shallow events, the $m_b^C$ is different than predicted with an RDP source, though by less than 1.2 units.

- Analysis of the spectra show that in no case is $pP$ a spectral shadow of $P$, as it is for an RDP source and elastic propagation.

- Phases that seem to be associated with spall closure can be seen on the shallow source body wave records. However, they are not easily associated with identifiable crack closure patterns in the source calculation.

- Comparison of observed and calculated body and surface waves for PILEDRIVER leads to the conclusion that the two are in rather good agreement. This conclusion is subject to the qualifications one often faces in this kind of comparison. For the surface waves, it is the need to account for the nonaxisymmetric component, usually attributed to tectonic stress release. Adding a recent estimate for this component by Rivers and von Seggern (1979) to our solution, we get good agreement with the data. However, if the strike-slip solution of Toksoz and Kehrer (1972) is correct, the synthetic surface waves are about a factor of six too small.

- For body waves the comparison is complicated by the apparent presence of strong azimuthal effects in the radiated short period energy (Hadley and Hart, 1979). Our conclusion is that the computed PILEDRIVER source (in one- or two-dimensions) has about the right direct $P$ amplitude. However, the two-dimensional source calculation appears to include too much nonlinear interaction with the free surface. The later portion of the $P$ waveform does not match the data, apparently because $pP$ is too greatly suppressed and because the seismic energy from spall closure is too large or is timed incorrectly. This "overprediction" of surface interaction effects is expected since comparison of theoretical and observed near-field motions and plots of the cracking near the source indicate that there was too much spallation in the calculation.
The constitutive models used by S3 (in spherically symmetric source calculations) lead to RDP source functions that are strongly peaked, with the value near 1 Hz a factor of five or more larger than the value at long periods. The peaking is due to the incorporation of an effective stress law and the choice of unconfined compressive strength (0.75 kb), based on laboratory data for fractured granite and results of comparison with near-field ground motion observations.

While we do not have RDP source functions for the ATI granite, comparison of $M_s$ and $m_b$ for the ATI two-dimensional calculations indicates that the RDP peaking is probably less than a factor of two. Due primarily to this difference, the $m_b$ for the S3 calculations is about 0.5 units higher than that for ATI calculations of the same yield. The ATI $M_s$ values fall between those for the shallow and deep S3 calculations.
IV. AUTOMATIC SIGNAL PROCESSING

4.1 INTRODUCTION

This section reviews accomplishments during the contract period on:

Task 4.3.1 - Development of the MARS Detector,
Task 4.3.3 - Review of Seismic Event Detectors.

Although we had hoped initially to run the MARS (Multiple Arrival Recognition System) detector at VELA Seismological Center (VSC) in an on-line experiment (Task 4.3.2), it was not possible to perform this task. The principal reason for this was the decision to commit the resources allocated to Task 4.3.2 to the MARS detector task (4.3.1). The results which were obtained from this added effort were:

1. Increase in efficiency obtained by development of heterodyne technique.
2. Extensive analysis of signal-to-noise ratios using the modern theory of statistical signal analysis.

Results on Task 4.3.1 are described in the next subsection, where the MARS detection algorithm is described, together with an evaluation of its performance in an off-line mode on a suite of test tapes supplied by VSC, containing both noise and signal recordings. A more complete description may be found in Farrell, et al., 1980. Results on Task 4.3.3 have been detailed in a separate report to VSC (Berger, 1980) and we give below an executive summary of the most salient points and recommendations.
4.2 MARS SEISMIC DETECTION, BY W. E. FARRELL, R. C. GOFF AND J. WANG

4.2.1 Objective

The objective of this task was to optimize the MARS-based signal detection algorithm and evaluate it in an off-line mode on data supplied by VSC.

4.2.2 Accomplishments

The principal accomplishment has been the development of an efficient code which has been tested on four hour noise samples from NORSAR and Pinedale, and on the 24-hour NORSAR and Pinedale test tapes supplied by VSC. Results from both test tapes, which contained over 30 signals at each of four different amplitude levels, were comparable to the VSC benchmark run; that is, at similar false alarm rates, about the same pattern of events was detected. On the UNIVAC 1100/81 the algorithm runs at 40 times real time on the 10 sample/second NORSAR data. As with the VSC detector, most of the time (80 percent) is consumed by Fourier transforms.

As an example of the current state of the MARS detector, Figure 26 shows the first ten NORSAR signals extracted from the 24-hour test tape. Each signal was buried in noise at four distinct amplitude levels, which Blandford refers to as "raw signal-to-noise ratio 1/2, 1/4, 1/8, 1/16." We refer to these four scaled copies as signal classes A, B, C and D. Thus, the plot shows ten A class events, those with raw SNR of 1/2. Furthermore, the seismograms shown in this figure are not the actual data present on the tape, but they have been high-pass filtered through a filter with a 1 Hz corner frequency. This is to attenuate the long period energy which contains mostly noise power and very little signal power. The events are much less obvious in the broadband data (see Figure 29).
Figure 26. Events 1 to 10 from VSC 24-hour NORSAR test tape, high pass filtered. Letters A, B, C and D denote times of detection on signals with "raw signal-to-noise ratio 1/2, 1/4, 1/8, 1/16" respectively. There were 165 false alarms for this run over the 24-hour tape.
each seismogram we have shown the times at which "events" were detected by the MARS processor. Events labeled A were detections found in the A class seismograms, just the records shown here. Events labeled B were found on the B class seismograms, and so on.

The most important point to be made about these results is that the principal objective in the work to date has been to optimize the speed of the code and to calibrate the false alarm behavior. Thus, we have not "educated" it to look for specific signal types, nor to pick "first motion." Thus, the narrow band, long period motion in Event 2, is ignored in favor of later, broadband energy. Seismogram 3 is easily found at all four signal levels, but the peak in the broadband power falls well back in the Lg wave train.

It should be emphasized that no preprocessing or signal conditioning (e.g., optimum band-pass filtering) precedes the MARS analysis. Instead, the raw data is at the very first stage decomposed into a multiplicity of band pass channels. The signal amplitude in each channel changes dynamically as the background noise power rises and falls, as the shape of the noise spectrum changes with time, and as true seismic events come and go. By keeping a running history of noise amplitude in each channel, the MARS process then flags significant short term excursions, and finally searches for a pattern across the many frequency bands.

Among the subsidiary accomplishments in this automatic signal processing task, the most important are the following:

- A tenfold or more acceleration in processing speed was obtained by incorporating a heterodyne and decimate operation in the construction of the narrow band envelope function. Implementation of this feature was based on the observation that the spectrum of a narrow band
signal is band limited, and practically vanishes outside a narrow region about the center frequency. The heterodyne operation is a signal processing device which shifts the center frequency down to zero frequency. But now the signal spectrum drops to a negligible value at frequencies much less than the Nyquist frequency. Then the inverse transform back to the time domain can be accurately found with a new and much smaller Nyquist frequency.

An extensive study was made of the statistical properties of narrow band seismic noise. This study was performed on the continuous envelope functions, rather than the envelope maxima catalog actually used by MARS, in order to be able to relate the experimental results with classical statistical theory. It was found, for example, that the envelope probability density function closely follows the Rayleigh law, which is expected if narrow band envelopes are extracted from Gaussian noise whose spectrum is not too ragged. Further, the joint statistics of multiple envelope functions were studied to estimate the cross-correlation between two envelope functions generated by different filters. This work was necessary to quantify the possibility of cross-correlation in envelope maxima, and to give objective guidance both to the construction of the comb of filters, and to the significances of envelope alignments. Preliminary work was undertaken in multiple envelope correlation, using the Bernoulli trial model, but we have not yet obtained definitive results.
Working still with noise records, we know how to tune the MARS false alarm rate by adjusting the three key parameters: amplitude (normalized with respect to the noise in each band), bandwidth and dispersion. Figure 27 shows a cube in this parameter space, each cell of which contains a number related to the False Alarm Rate. The bigger this number, the poorer the detector. In our terminology, the bandwidth parameter is called $k$; it gives the number of envelope maxima (out of twenty possible) required before an event is called. The amplitude parameter, also referred to as normalized amplitude cutoff in the third figure, expresses how large extrema must be before an envelope peak is to be included in the search for events. We refer to this as a normalized amplitude because each envelope function in the time window currently being processed is scaled by the mean envelope amplitude of the previous $N$ windows. There is, then, a floor on the minimum instantaneous signal spectrum required before an event is called. The floor is just some multiple of the preceding noise spectrum. Finally, the dispersion parameter specifies how broad a time swath one permits the $k$ peaks to fall within.

Figure 28 shows a specific result selected from our noise study. It is a slice along the $k = 6$ plane for a two-hour section of NORSAR data. The figure shows that the lower left hand corner is good, but that the upper right hand corner is bad. But we do not want to be too far down in the lower left hand corner. That gives great noise rejection, but concomitantly requires an
Figure 27. Schematic representation of the three-dimensional parameter space spanned by the key MARS detection parameters. Each cell within this cube contains a number giving the false alarm rate when the algorithm operates on pure noise.
HOW MARS DETECTION PARAMETERS AFFECT FALSE ALARM RATES

Figure 28. Contour plot giving number of false alarms in two hours of NORSAR data when k = 6 peaks are required to flag an event. Best region of operation is the hatched zone.
extremely large and impulsive arrival to trigger. Thus, this part of the parameter space would show a low probability of detection for easily seen signals. To capture weak, moderately dispersed signals, one wants to site the detector parameters somewhere in the hatched region.

- New graphical display procedures have been implemented for showing the time-frequency structure of seismograms. These have been found to be extremely powerful tools in our research studies, and should be equally useful at seismic analyst stations for operational detection and discrimination. Figure 29 displays the prebandpass filtered version of Seismogram 5 from Figure 26, along with its associated time-frequency decomposition. This is a true amplitude plot at each frequency, which clearly indicates the dominance of the long period noise, as does the comparison between this version of the seismogram and the bandpassed version in Figure 26. It can be seen, for example, that the best signal amplitude occurs over the 2.0 to 3.5 Hz frequency band. There is also significant signal power out to 5.0 Hz, but the noise there is so low, it is not possible to get an accurate estimate of the signal-to-noise ratio.

- Another type of display is shown in Figure 30. This display is similar to the sonogram display, long used in acoustic signal processing, but these figures were generated by digital rather than analog signal analysis methods. In this display, high power points in the time-frequency plane are shown as black zones, small amplitude...
Figure 29. Seismic Event 5 (see Figure 26) and its associated time-frequency decomposition. The fin at 16 sec (this time is arbitrary) and 2.5 Hz is the same event which appears at 56 seconds, 2.5 Hz in the middle panel of Figure 30. In this figure the true amplitude in each frequency band is preserved. This makes the predominance of the long period noise obvious. In Figure 30, the data has been "whitened" by scaling according to the largest amplitude in each band. This emphasizes frequency bands with good signal-to-noise ratio.
Figure 30. "Sonograms" for seismic Events 3, 5 and 9 which are also displayed in Figure 26.
regions shade down through various gray levels towards pure white. Unlike the previous display, these data have been scaled according to the "peak" power in each frequency band. This tends to "whiten" any signals present, and make more visible these frequency bands with good signal-to-noise ratio.

- The extra frequency dimension in Figures 29 and 30 tells much more about the nature of the seismic events than does the seismogram itself. Event 9, for example, is barely visible in Figure 26, but on Figure 30, it shows up as the dark band between 2.0 and 3.0 Hz, slightly later than nine minutes. One does see, of course, bands of similar length elsewhere in the figure, but they are not surrounded by the long gray zone, indicating they are most likely noise signals.

4.3 DETECTION STATE-OF-THE-ART BY J. BERGER

4.3.1 Objective

The objective of this review study was to identify all pertinent automatic signal detection algorithms by equation, mathematical derivation and usage history, including algorithms currently under development and scheduled to be validated by October 1981.

4.3.2 Accomplishments

A draft report entitled "Seismic Detectors" The State-of-the-Art" has been prepared and submitted to VSC. In this report, the following detection algorithms were reviewed:

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General conclusions reached were:

1. All detectors reviewed in this report are based on a comparison between some form of variance estimate of the signal calculated over a time period approximately equal to the duration of an expected seismic event, and the normal (or long term) variance.

   Possible exceptions to this general form are the phase detector described by Unger (1978) and the similar part of MARS. The former did not work because the short period phase fluctuations were so rapid that they could not reliably be predicted; the latter has not been implemented.

2. Ad hoc detection algorithms such as Allen's and Stewart's (1977) offer a hope of some improvement in the detection process. These methods, after having made the basic detection statistic test and having made a tentative identification, are followed by a further process that is designed to:

   a. reduce the false alarm rate,
   b. improve the timing capability, and
   c. speed the recovery of the detection algorithm after an event is encountered.
How much these algorithms can be expected to offer significant improvements depends upon the noise environment in which they are operating. If the SNR is such that a high probability of detection is achieved with a tolerable FAR, then little improvement can be expected. If, however, the SNR is poor, so that the probability of detection is low for a given FAR, then significant improvement may be achieved by such two-stage algorithms.

3. Testing of the detectors described in this report was not carried out in a uniform manner on the same or even similar data sets. Thus, no definitive statement about their relative performance may be made. However, it appears that no one detector is obviously superior to all others. Some have been optimized for teleseismic detection using a moderately large computing facility. Some have been designed for operation in microprocessor controlled field recording units, typically used in the near field or at least at regional distances. These applications stress ease of implementation in microprocessors. Some algorithms stress timing ability as this may be another object of the algorithm.

4. Little theoretical advance has been achieved since Frieberger's 1963 work in which he "solved" the problem for detection of a Gaussian signal in Gaussian noise. The influence of this work has rightly guided the design and implementation of many of the detectors used today. However, it must not be thought that the "real problem" has been solved. The "real problem" is the detection of certain non-Gaussian signals in the presence of non-Gaussian noise. Frieberger discovered the optimum detector for an approximate model of the actual situation, but, other algorithms may work significantly better on "real" data. Further, considerations such as timing ability, recovery of the algorithm after an event, and immunity to highly non-Gaussian noise such as line spikes and data dropouts may dictate very different approaches.
As a result of the review, the following recommendations were made:

- Uniform testing of all viable detectors should be conducted with
  a. a realistic synthetic data set;
  b. all detectors coded for and running on the same or similar machines;
  c. ROC curves produced for each detector comparing them with the theoretical performance of the detector for a completely known signal.

- Theoretical and experimental research in phase sensitive detectors should be supported as this is an area where it may be possible to exploit signal information not used in energy or power detectors.

- Research should be encouraged to test if matched filters for specific types of signals (station/source pairs) improves detector performance.

- Further development of hybrid detection algorithms, that combine high probability of detection with a high FAR and then are followed by a post processing to reduce the FAR should be undertaken.

- New algorithms, designed specifically for use with the new generation of three component broadband seismographs, should be developed and tested.

- In view of data rates from these new data sources, dedicated microprocessors to run the detection algorithms on a one processor per channel (or seismic station) basis should be considered.
V. EVALUATION OF SUITES OF EVENTS

5.1 INTRODUCTION

The objective of this task (Task 4.4 of our Contract F08606-79-C-0008) was to study and evaluate the feasibility of automatic determination of body wave magnitude using the MARS processor described in Section 4.2. In addition, the work included developing and testing of an analogous automatic surface wave magnitude algorithm.

This work is summarized in an S^3 Semiannual Technical Report (Bache, et al., 1980a). The next subsection summarizes the most salient results.

5.2 AUTOMATED MAGNITUDE \( \hat{m}_b \) AND \( \hat{m}_s \), BY T. C. BACHE AND B. SHKOLLER

In FY '79, we proposed an automated magnitude measure called \( \hat{m}_b \) and tested it by processing high signal/noise recordings of eleven Pahute Mesa explosions at six teleseismic stations (Bache, 1979; Bache, Day and Savino, 1979). We concluded that the \( \hat{m}_b \) was at least as good a magnitude measure and yield indicator as the most carefully determined time domain \( m_b \). The \( \hat{m}_b \) algorithm used in that earlier work did not account for the presence of seismic noise, and so was viewed as primarily a demonstration of the concept.

As part of the VSC conducted discrimination experiment, algorithms were constructed to compute variable frequency magnitudes, \( \hat{m}_b(\ell) \), at selected frequencies (Masso, et al., 1979; Savino, et al., 1980). These algorithms do incorporate corrections for the presence of interfering phases and seismic noise. Otherwise the \( \hat{m}_b \) used by Bache (1979) is not much different from \( \hat{m}_b \) (1 Hz).
In the current contract, we have implemented a new algorithm for $m_b$ (which is essentially $m_b$ (1 Hz)) and tested it by application to a series of synthetic seismograms which are constructed by embedding a signal of known $m_b$ in seismic noise. The $m_b$ has also been computed for a set of RKON recordings of Eurasian events taken from the AI data set. A similar algorithm has been implemented for computing an analogous $m_b$, and some testing has been done.

5.2.1 Description of the $m_b$ Algorithm

The calculation of $m_b$ includes the following steps:

1. The seismogram is processed by MARS, which applies a suite of narrow band filters and constructs a table of envelope function peak amplitudes ($A_c$) and group arrival times ($t_g$).

2. The MARS detection algorithm is applied to identify an undispersed P wave arrival. This algorithm works with a "surface" like that is shown in Figure 31, where the $A_c$ are plotted versus $t_g$ and filter center frequency, $f_c$. For each $f_c$ the largest $A_c$ is denoted by an asterisk. The relative amplitudes of the other peaks are denoted by integers, with the asterisk given the value 10. The detection algorithm searches for a "ridge" of amplitudes with nearly the same $t_g$ to find the group arrival time, $t_g$, of a detected P wave. The "+" and "-" symbols in the plot denote a statistically determined uncertainty window within which any $A_c$ could be associated with the detected signal.

3. For each $f_c$, one $A_c$ is chosen to define the "MARS signal spectrum." This is done by a scoring algorithm which, in its current form, works fairly well, but could probably be improved for low S/N events.
Figure 31. Bottom portion is a seismogram recorded at a station in Bluff, Alaska, from an event in the Kurils. The top half is a plot of filter center frequency versus group arrival time (sec). The t\(_g\) with arrow attached shows where the automated detection and first arrival algorithms picked the signal arrival time.
4. The $A_C$ values about a specific $f_c$ (e.g., 1 Hz) are fit to give a "smoothed" estimate for the spectral amplitude at that frequency. This amplitude is corrected for the presence of nearby envelope peaks and a statistical estimate of the uncertainty is made, based on the "MARS spectrum" of the ambient noise. The $m_b$ is computed from $\log \left( A_q^{**}; f_c \right) + B$, where $A_q^{**}$ is the noise corrected $A_C$ and $B$ is the usual distance correction.

5.2.2 $m_b$ Algorithm Testing

In Figure 32, we show the $m_b$ for a synthetic seismogram which has been added to a noise sample from RKON, with the ratio of peak time domain amplitudes ("Peak S/N") being scaled to 100. The $\hat{m}_b$ is 3.589, which may be compared to the time domain $m_b$ of 3.78, computed from $\log(A/T) + B$, with $T = 0.7$ seconds. Systematic differences between $m_b$ and $\hat{m}_b$ are expected.

The same synthetic was added to various segments of noise recorded at RKON. Some examples are shown in Figure 33. Bache, et al. (1980) show fifteen such examples. The error in arrival time and $\hat{m}_b$ for these examples are tabulated in Table 1. Only when the ratio of MARS signal spectrum to MARS noise spectrum gets to be 1.5 or smaller are the errors very large. That is, even when the signals can barely be detected by eye, the $m_b$ algorithm is able to give a good estimate for the magnitude.

5.2.3 $\hat{m}_b$ for Actual Data

Bache, et al. (1980) present the $\hat{m}_b$ results for Eurasian explosions and earthquakes recorded at RKON and LASA. The epicentral distances are from 53 to 94 degrees and the events have PDE magnitudes from 4.8 to 6.0. The $\hat{m}_b$ algorithm appears to
Figure 32. Calculation of $m_b$ for a seismogram with peak synthetic/peak noise = 100. The seismogram is shown at the top with an asterisk denoting the signal arrival time $t_s$. The $m_b$ calculation is shown graphically, with the heaviest line being $\log (A_s^2 f_c) + B$. The line of medium shade is analogous magnitude for the noise. The light line is the $t_q$ for each $A_s^2 f_c$, with zero on the $t_q$ scale (at right) being $t_q$. The $m_b$ is computed at 1 Hz and is marked with an X. Printed above the graph are $m_b$ (MB), the uncertainty in $m_b$ imposed by the noise (+ DMB), the noise magnitude at 1 Hz (MBNF), the mean signal/noise power over the frequency band from FLEPT to FRIGHT, and the B correction for the magnitude (BDEL).
Figure 33. Test of the \( m_0 \) algorithm with noise Section 62110. The ratio of the peak amplitude of the synthetic to the peak noise amplitude is denoted by Peak S/N. The actual arrival time of the signal is the time of the asterisk plus \( t_A \).
TABLE 1
SUMMARY OF $\hat{m}_D$ TEST CALCULATIONS

<table>
<thead>
<tr>
<th>Identifier</th>
<th>Peak Signal</th>
<th>S/N (1 Hz)</th>
<th>$\hat{m}_D$</th>
<th>$\hat{m}_D$ Uncertainty</th>
<th>$\hat{m}_D$ Error</th>
<th>Arrival Time Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>Identifier</td>
<td>Peak Noise</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Noise Section 62110 (Figure 32)</td>
<td>100</td>
<td>217</td>
<td>3.589</td>
<td>0.001</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>A</td>
<td>3</td>
<td>6.5</td>
<td>3.583</td>
<td>0.018</td>
<td>-0.006</td>
<td>+0.02</td>
</tr>
<tr>
<td>B</td>
<td>1</td>
<td>2.2</td>
<td>3.593</td>
<td>0.055</td>
<td>0.004</td>
<td>0.03</td>
</tr>
<tr>
<td>C</td>
<td>1</td>
<td>2.6</td>
<td>3.667</td>
<td>0.046</td>
<td>0.078</td>
<td>-0.09</td>
</tr>
<tr>
<td>D</td>
<td>1</td>
<td>2.2</td>
<td>3.586</td>
<td>0.056</td>
<td>-0.003</td>
<td>0.48</td>
</tr>
<tr>
<td>E</td>
<td>1</td>
<td>2.2</td>
<td>3.581</td>
<td>0.057</td>
<td>-0.008</td>
<td>-0.01</td>
</tr>
<tr>
<td>F</td>
<td>0.5</td>
<td>1.5</td>
<td>3.734</td>
<td>0.082</td>
<td>0.145</td>
<td>0.09</td>
</tr>
<tr>
<td>G</td>
<td>0.5</td>
<td>1.2</td>
<td>3.622</td>
<td>0.110</td>
<td>0.033</td>
<td>-0.76</td>
</tr>
<tr>
<td>H</td>
<td>0.5</td>
<td>1.5</td>
<td>3.708</td>
<td>0.088</td>
<td>0.119</td>
<td>0.14</td>
</tr>
<tr>
<td>I</td>
<td>0.5</td>
<td>1.4</td>
<td>3.689</td>
<td>Missed Signal</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Noise Section 274110</td>
<td>100</td>
<td>219</td>
<td>3.586</td>
<td>0.001</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>J</td>
<td>1</td>
<td>2.0</td>
<td>3.546</td>
<td>0.111</td>
<td>-0.05</td>
<td>-0.05</td>
</tr>
<tr>
<td>K</td>
<td>1</td>
<td>2.2</td>
<td>3.595</td>
<td>0.095</td>
<td>0.09</td>
<td>-0.15</td>
</tr>
<tr>
<td>L</td>
<td>0.5</td>
<td>1.1</td>
<td>3.583</td>
<td>0.226</td>
<td>-0.03</td>
<td>-0.05</td>
</tr>
<tr>
<td>M</td>
<td>0.5</td>
<td>1.0</td>
<td>3.548</td>
<td>Missed Signal</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
give excellent results, even when the signal is difficult to detect by eye so that time domain $m_b$ measurements would probably not be attempted.

5.2.4 Description of the $M_S$ Algorithm

The $M_S$ algorithm is nearly the same as the $m_b$ algorithm, except that the dispersion character of the surface wave signal of interest must be specified explicitly. The $t_g-f_c$ plane (Figure 31) is first mapped into a $t_g'-f_c$ plane where a signal with the expected dispersion appears to be nearly undispersed. The algorithm then follows the same steps as for $m_b$.

5.2.5 $M_S$ Algorithm Testing

In Figure 34, we show an example of the $M_S$ calculation. A synthetic seismogram was added to a long period noise segment (from LASA), with the peak signal and noise amplitudes being equal. Comparing to the $M_S$ calculation for the synthetic itself, the 20 second arrival time error is 4 seconds and the $M_S$ error is 0.06. This and similar calculations done with a "perfect" estimate for the dispersion of the expected signal, show that the $M_S$ algorithm works very well. Testing with real data where the prespecified dispersion is only approximately correct has not yet been done. However, we point out that the $M_S$ calculation only requires an accurate identification of the MARS spectrum in a narrow period band, in this case near 20 seconds.

5.2.6 Conclusions

The automated magnitude algorithms appear to give consistent and convenient results, though much more extensive testing with real data is required. The $m_b$ and $M_S$ values may be viewed as a by-product of signal processing with the MARS
Figure 34. Calculation of $M_a$ for a seismogram with peak synthetic/peak noise = 1. The reference dispersion was that of the synthetic seismogram.
program, which is also configured for signal detection and earthquake/explosion discrimination. Thus, these values can easily be catalogued when processing data with MARS for other purposes.
VI. GROUND MOTION ANALYSIS

6.1 INTRODUCTION

Task 4.5 involved a compilation and assessment of near-source data recorded from underground explosions with the purpose of determining their significance for the definition of nuclear source functions for different emplacement media. More specifically, previously unpublished data from the Sandia Corporation archives are being reviewed and integrated into the previously compiled database.

Work on this task was the topic of a report by Murphy and Bennett (1980) and was described by Bache, et al. (1980a). A summary is provided in the following subsection.

6.2 ANALYSIS OF FREE-FIELD DATA FROM EXPLOSIONS IN WET TUFF AND ALLUVIUM EMPLACEMENT MEDIA BY J. R. MURPHY AND T. J. BENNETT

Table 2 lists the events for which previously unpublished free-field data have been collected. It can be seen that data from eleven different explosions covering a yield range from about 1 to 1200 KT are being investigated. These events were detonated in wet tuff/rhyolite and alluvium emplacement media and the associated depths of burial vary by more than a factor of six. These data, together with those previously collected, are being used to assess the dependence of seismic coupling on source medium. For example, Figure 35 shows a comparison of the reduced displacement potentials (RDP's) predicted using an analytical model based on Pahute Mesa explosions in wet tuff/rhyolite with several observed RDP's from Yucca Flat events in wet tuff. It can be seen that the predicted and observed agree fairly well, which suggests that the seismic coupling properties of Yucca Flat tuff are similar to those of the Pahute Mesa volcanics. However, a very different
TABLE 2
NUCLEAR EXPLOSIONS FOR WHICH PREVIOUSLY UNPUBLISHED
FREE-FIELD DATA HAVE BEEN COLLECTED

<table>
<thead>
<tr>
<th>EVENT</th>
<th>MEDIUM</th>
<th>YIELD</th>
<th>DEPTH</th>
</tr>
</thead>
<tbody>
<tr>
<td>AGILE</td>
<td>Wet Tuff</td>
<td>L-I</td>
<td>732 m</td>
</tr>
<tr>
<td>BOXCAR</td>
<td>Wet Rhyolite</td>
<td>1200 KT</td>
<td>1165 m</td>
</tr>
<tr>
<td>CALABASH</td>
<td>Wet Tuff</td>
<td>110 KT</td>
<td>626 m</td>
</tr>
<tr>
<td>CARPETBAG</td>
<td>Wet Tuff</td>
<td>220 KT</td>
<td>663 m</td>
</tr>
<tr>
<td>COMMODORE</td>
<td>Wet Tuff</td>
<td>250 KT</td>
<td>749 m</td>
</tr>
<tr>
<td>CYPRESS</td>
<td>Wet Tuff</td>
<td>L</td>
<td>411 m</td>
</tr>
<tr>
<td>DIESEL TRAIN</td>
<td>Wet Tuff</td>
<td>L</td>
<td>419 m</td>
</tr>
<tr>
<td>FAULTLESS</td>
<td>Wet Tuff</td>
<td>I</td>
<td>975 m</td>
</tr>
<tr>
<td>HUTCH</td>
<td>Wet Tuff</td>
<td>I</td>
<td>549 m</td>
</tr>
<tr>
<td>LANPHER</td>
<td>Wet Tuff</td>
<td>L-I</td>
<td>714 m</td>
</tr>
<tr>
<td>PLATTE</td>
<td>Tuff</td>
<td>1.85 KT</td>
<td>191 m</td>
</tr>
</tbody>
</table>
Figure 35. Comparison of observed tuff RDP's with RDP's predicted for the same yield and depth of burial in a wet tuff/rhyolite emplacement medium.
picture emerges when this same procedure is applied to explo-
sions in dry Yucca Flat alluvium. Figure 36 shows a compari-
son of the observed RDP's from four events in dry alluvium
with the corresponding RDP's predicted for the same yields
and depths of burial in wet tuff/rhyolite emplacement media.
It can be seen that these data clearly indicate that dry
alluvium is a weak coupling medium with respect to wet tuff/
ryolite, in agreement with the observed differences in the
teleseismic $m_d$ data from explosions in these two media. Thus,
the available free-field data are essentially consistent with
the teleseismic $m_d$ data and, consequently, should be of use
in their interpretation.
Comparison of observed alluvium RDP's with RDP's predicted for the same yield and depth of burial in a wet tuff/rhyolite emplacement medium.

Figure 36.
VII. ACOUSTIC WAVES FROM EXPLOSIONS IN THE OCEAN

7.1 INTRODUCTION

The study of the acoustic signature of a near surface oceanic explosion gave rise to a report by Bache, et al. (1980c). An executive summary of the results is included below.

7.2 THE UNDERWATER ACOUSTIC SIGNATURE OF A NUCLEAR EXPLOSION AT THE OCEAN SURFACE BY T. C. BACHE, T. G. BARKER, M. G. BROWN, K. D. PYATT AND H. J. SWANGER

7.2.1 Objective

The objective of this task is to estimate the gross spectral character and duration of the acoustic wave signature of a nuclear explosion near the ocean surface. The explosion is assumed to have a yield of 1 KT and the nominal range is 6600 km.

7.2.2 Accomplishments

The main results of this work are summarized in a report by Bache, et al. (1980). The technique was to construct theoretical pressure-time histories by convolving an elastic representation for the source with a Green's function representing the propagation. The source may include two parts. The first is the airblast loading applied to the surface and the second is the direct coupling of energy into the water. When the explosion is above a certain height, estimated to be 2.3 meters for 1 KT, the direct coupling contribution may be ignored. Thus, the calculations include the cases when the explosion is on or above the surface, though no attempt is made to account for height-of-burst effects that
may become important when the (1 KT) explosion is more than 10 meters above the surface.

Both components of the source are expressed in terms of pressure-time histories, \( P(r,t) \) applied to the ocean surface. The total force applied is

\[
\hat{F}(\omega) = \int_0^\infty P(r,\omega) J_0(\omega r) r dr .
\] (3)

The spectral amplitudes of the total force for both components of the source are plotted in Figure 37 for the ray parameter \( p = 0.667 \text{ sec/km} \) appropriate for large distances.

The pressure at the receiver is obtained by convolving \( \hat{F}(\omega) \) with the appropriate Green's function, which is the pressure at the receiver due to a vertical point load applied at the center of the source region. The Green's functions were computed with the WKBJ seismogram method (Chapman, 1978; Brown, et al., 1980). The results turned out to be very little different from those from geometric ray theory. Then for any particular ray arrival, the spectral pressure at the receiver is approximately

\[
\hat{P}_r(\omega) \approx i \omega \hat{F}(\omega) \cdot Q(\omega) ,
\] (4)

where \( Q(\omega) \) represents the frequency-dependent filter imposed by the travel path. However, at the frequencies of interest (< 50 Hz), absorption in the ocean is very small. Therefore, we assume that \( Q(\omega) = 1 \). The total record is a summation of many rays, leading to a total spectrum which is merely a modulated version of Equation (4).

In Figure 38, we plot our estimates for the spectra of the pressure pulse at a hydrophone in the deep ocean at a large distance from the explosion. The direct coupling
Figure 37. The explosion source spectra.
Figure 38. The spectrum of the pressure time history of a single ray arrival at a SOFAR axis receiver station. The complete signal spectrum, which is a sum of many single ray spectra, would have the same basic shape. The amplitude units are arbitrary, depending on the amplitude of the Green's function for the travel path.
contribution is small and the spectrum is band-limited, having a peak near 22 Hz and being down by a factor of 3 from the peak at about 4 and 50 Hz. The spectra cube-root scale with yield. That is, if the yield were 2 KT, the spectrum in Figure 38 shifts to frequencies smaller by a factor of 1.26.

To estimate the signal duration, the Green's functions were computed with WKBJ seismogram theory for a variety of assumptions about the ocean sound velocity profile. At the large ranges (> 3500 km) of interest, the main contribution is from rays that turn above the ocean bottom. For a reflection coefficient of as large as 0.98, the bottom bounces make almost no contribution because they reflect so many times.

The calculated signal duration varies widely, depending upon the assumptions about the sound velocity profile. Values from 20 to 60 seconds seem most reasonable for a range of about 6600 km. The duration scales directly with range.
REFERENCES


Filson, J. and H. Bungum (1972), "Initial Discrimination Results from the Norwegian Seismic Array," Geophys. J., 31, pp. 315-328


