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NUMERICAL SOLUTION OF NATURAL CONVECTION IN AN INCLINED RECTANGULAR CAVITY WITH PARTITIONS

THESIS

AFIT/GAE/AA/80D-23 Thomas K. Toltzien
Captain USAF

Approved for public release; distribution unlimited.
NUMERICAL SOLUTION OF NATURAL CONVECTION IN AN INCLINED RECTANGULAR CAVITY WITH PARTITIONS

Masters THESIS

Presented to the Faculty of the School of Engineering of the Air Force Institute of Technology Air Training Command in Partial Fulfillment of the Requirements for the Degree of Master of Science

by

Thomas K. Toltzien, B.S.M.E.
Captain USAF Graduate Aeronautical Engineering

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Acknowledgement

When faced with the task of conducting an independent study, I could not have hoped to bring it to a successful conclusion without the aid and guidance of my thesis advisor and numerous others involved during the duration of the study. It is with this thought in mind that I would like to express my sincere appreciation to Dr. James Hitchcock, my thesis advisor, for his time and effort spent throughout this study. I would also like to thank Dr. Harold Wright and Capt. Robert Roach for their meaningful suggestions, and Mrs. Maripat Meer, who typed this manuscript.

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Thomas K. Toltzien
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Notation

Symbol

A Aspect ratio, \( = \frac{L}{D} \)

\( C_p \) Constant pressure specific heat

\( D \) Width of enclosure

\( g \) Acceleration due to gravity

\( g_C \) Dimensional constant in Newton's second law

\( G_R \) Grashof number, \( = \frac{g\beta(\theta_H-\theta_C)D^3}{\nu^2} \)

\( h \) Local heat transfer coefficient, \( = \frac{q}{\theta_C-\theta_H} \)

\( k \) Thermal conductivity

\( L \) Height of enclosure

\( Nu \) Local Nusselt number, \( = \frac{hD}{k} \)

\( \overline{Nu} \) Mean value of Nusselt number

\( p \) Local dynamic pressure

\( P \) Dimensionless pressure, \( = \frac{P_0D^2gC}{\nu^2\rho} \)

\( Pr \) Prandtl number, \( = \frac{gC\mu C_p}{k} \)

\( q \) Heat flux at hot wall

\( S \) Inclination angle

\( t \) Time

\( u \) Velocity in x-direction

\( U \) Dimensionless velocity in X-direction, \( = \frac{uD}{\nu} \)

\( v \) Velocity in y-direction

\( V \) Dimensionless velocity in Y-direction, \( = \frac{vD}{\nu} \)

\( x \) Distance along hot wall

\( X \) Dimensionless distance along hot wall, \( = \frac{x}{D} \)
Symbol

- **y**: Distance from hot wall
- **Y**: Dimensionless distance from hot wall, $= y/D$

Greek Letters

- **$\alpha$**: Molecular thermal diffusivity, $= \frac{k}{\rho C_p}$
- **$\beta$**: Volume coefficient of thermal expansion
- **$\Delta X$**: Grid spacing in X direction
- **$\Delta Y$**: Grid spacing in Y direction
- **$\Delta t$**: Time increment
- **$\zeta$**: Dimensionless vorticity, $= -\left(\frac{\partial \psi}{\partial X} + \frac{3\psi}{3Y}\right)$
- **$\Theta$**: Temperature ($\theta_H$ and $\theta_C$ refer to the temperatures at the hot and cold walls respectively).
- **$\Theta$**: Dimensionless temperature, $= (\Theta - \Theta_H)/(\Theta_C - \Theta_H)$
- **$\nu$**: Kinematic viscosity
- **$\mu$**: Viscosity
- **$\rho$**: Density
- **$\tau$**: Dimensionless time, $= t\nu/D^2$
- **$\Psi$**: Dimensionless stream function, such that $U = \partial \Psi / \partial Y$ and $V = -\partial \Psi / \partial X$
- **$\omega$**: Relaxation parameter
- **$\phi$**: Slat angle

Subscripts

- **i,j**: Space grid point indices in X and Y directions
- **opt**: Value of relaxation parameter giving fastest convergence
- **w**: Wall grid point

Superscripts

- **n**: Time index
- **m**: Iteration number
Abstract

A numerical investigation was conducted on two-dimensional natural convection within inclined rectangular enclosures partitioned into 45 degree triangular cells. The time dependent governing equations, vorticity, energy, and stream function, were solved by an ADI method and a Gauss-Seidel SOR technique. The numerical procedure was validated for rectangular enclosures, then modified for triangular cells. Heat transfer coefficients were determined for an inclined square enclosure with a diagonal partition for Grashof numbers less than $2 \times 10^5$ and inclination angles between 10 degrees and 90 degrees. These results show a diagonal partition reduces the heat transferred by natural convection across an inclined square enclosure by more than 50%.
NUMERICAL SOLUTION OF NATURAL CONVECTION
IN AN INCLINED RECTANGULAR CAVITY
WITH PARTITIONS

I. Introduction

Background

A major factor in the design of solar collectors is the reduction of natural convection heat losses within the collector enclosure. Traditional designs have suppressed natural convection by developing large aspect ratio enclosures or designing a small aspect ratio honeycomb structure to separate the collector plates (Ref.1). However, recent experimental studies by Meyer, et.al. (Ref.2), and Holland (Ref.3) have demonstrated the effectiveness of inclined slats (partitions) in reducing natural convection heat losses. The slats in these studies were positioned to form a series of moderate aspect ratio parallelogram enclosures. Meyer, et.al., also concluded that slats oriented downward from the hot plate resulted in a reduction of convective heat transfer with the minimum heat loss occurring at a slat angle of 45 degrees.

Objective

In the present study, the influence of slats in
reducing natural convection will be determined for non-
parallel slat arrangements. Specifically, the slats will
be oriented so as to partition a moderate aspect ratio rec-
tangular enclosure into a series of triangular regions (see
Figure 1). The temperature distribution and the cell heat
transfer coefficients will then be determined theoretical-
ly by a numerical procedure which will also be developed
for this investigation. The heat transfer coefficient for
the triangular cells will then be compared to results ob-
tained for similar rectangular enclosures with and without
slats. From these results the effectiveness of triangular
slat arrangements will be determined.

The first step in this investigation, however, will be
to adapt a numerical procedure which is capable of solving
the nonlinear partial differential equations which describe
natural convection in an inclined enclosure. The implicit
finite difference computational scheme developed by Wilkes
and Churchill (Ref.4) is just such a procedure. Since the
Wilkes and Churchill numerical procedure was developed for
a rectangular cavity with one vertical wall hot and the
other cold, the method will be first modified to describe
an inclined rectangular cavity, then modified again to ac-
count for the addition of partitions in the rectangular en-
closure.
Figure 1. Triangular Partitioned Enclosure.
Scope

In this study, natural convection heat transfer coefficients were evaluated for moderate aspect ratio (A=1.0 to 3.0) rectangular enclosures with thin partitions. The partitions were oriented at ±45 degrees to the hot wall. Thermal conduction was assumed to be infinite across the partitions and zero along the partitions. Additionally, the steady state temperature distribution along a partition was considered linear. Finally, since only heat transferred due to natural convection was to be evaluated, thermal radiation heat transfer within the enclosure was neglected.

To follow the development of the present investigation, this report is organized into five additional chapters. The time dependent governing equations which describe natural convection in inclined rectangular cavities are developed in Chapter II. In Chapter III, a numerical procedure is developed to evaluate the governing equations. A discussion of the numerical results is presented in Chapter IV. Finally, the significant conclusions are restated, and recommendations are made for further studies in Chapter V and VI, respectively.
II. Mathematical Model

In this section the governing equations describing natural convection in a 2-D inclined rectangular cavity will be developed. The equations and boundary conditions will then be simplified and rewritten in nondimensionalized form. Finally, an expression for local and average heat transfer coefficient will be derived.

Rectangular Cavity

Consider the inclined, rectangular cavity in Figure 2. The left and right walls are at constant temperatures \( \theta_H \) and \( \theta_C \), respectively, and the other side walls are either insulated or have a linear temperature distribution. Initially, the fluid in the cavity is motionless, and at a constant temperature equal to the average temperature of the hot and cold walls. The fluid thermodynamic and transport properties except density are considered constant and independent of temperature. Under the Boussinesq Approximation, density changes are expressed only as a function of temperature differences, and density is assumed constant except in the buoyant force terms.

Under these conditions, the fluid in an inclined rectangular cavity is described by the following equations:
Figure 2. Inclined Rectangular Enclosure Nomenclature.
Conservation of Mass

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0$$ (1)

Conservation of Momentum

$$\frac{\rho}{g_c} \frac{\partial u}{\partial t} + \frac{\rho}{g_c} \frac{\partial u}{\partial x} + \frac{\rho}{g_c} \frac{\partial v}{\partial y} = -\frac{\partial p}{\partial x} - \frac{\partial \rho \phi}{\partial y} \sin(S) + \mu \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2}\right)$$ (2)

$$\frac{\rho}{g_c} \frac{\partial v}{\partial t} + \frac{\rho}{g_c} \frac{\partial u}{\partial x} + \frac{\rho}{g_c} \frac{\partial v}{\partial y} = -\frac{\partial p}{\partial y} - \frac{\partial \rho \phi}{\partial x} \cos(S) + \mu \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2}\right)$$ (3)

Conservation of Energy

$$\frac{\partial \theta}{\partial t} + u \frac{\partial \theta}{\partial x} + v \frac{\partial \theta}{\partial y} = \alpha \left(\frac{\partial^2 \theta}{\partial x^2} + \frac{\partial^2 \theta}{\partial y^2}\right)$$ (4)

Coefficient of Volumetric Expansion

$$\beta = -\frac{1}{\rho} \frac{\partial \rho}{\partial \theta} \bigg|_p = \frac{\rho_0 - \rho}{\rho (\theta - \theta_0)}$$ (5)

The associated boundary and initial conditions are as follows:

$$\theta(x, 0, t) = \theta_H$$ (6)

$$\theta(x, D, t) = \theta_C$$ (7)
Linear Temperature Side Walls

\[ \theta(0,y,t) = \theta_H + (\theta_H - \theta_C)y/D \]  \hspace{1cm} (8)

\[ \theta(L,y,t) = \theta_H + (\theta_H - \theta_C)y/D \]

Adiabatic Side Walls

\[ \frac{\partial \theta}{\partial x}(0,y,t) = 0 \]  \hspace{1cm} (9)

\[ \frac{\partial \theta}{\partial x}(L,y,t) = 0 \]

Cavity Wall No-Slip Condition

\[ u(x,0,t) = u(x,D,t) = 0 \]
\[ v(0,y,t) = v(L,y,t) = 0 \]  \hspace{1cm} (10)

Initial Conditions

\[ u(x,y,0) = 0 \]
\[ v(x,y,0) = 0 \]
\[ \theta(x,y,0) = \frac{\theta_H + \theta_C}{2} \]  \hspace{1cm} (11)

Since the pressure gradient in the cavity results in part from the change in elevation of the fluid, it is convenient to derive an expression for the total pressure gradient in terms of the dynamic pressure gradient and the change in pressure due to the weight of the fluid.
\[ p = p_0 - \frac{g_0}{g_c} [\sin(S)x + (\cos(S)y)] \quad (12) \]

Differentiating this expression yields

\[ \frac{\partial p}{\partial x} = \frac{\partial p_0}{\partial x} - \frac{g}{g_c} \rho_0 \sin(S) \quad (13) \]

\[ \frac{\partial p}{\partial y} = \frac{\partial p_0}{\partial y} - \frac{g}{g_c} \rho_0 \cos(S) \quad (14) \]

Substituting from Equations (13), (14) and (5) into equations (2) and (3) and simplifying

\[ \frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = - \frac{g_c}{\rho} \frac{\partial p_0}{\partial x} - \beta(\theta - \theta_0) \sin(S) + \nu (\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2}) \quad (15) \]

\[ \frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = - \frac{g_c}{\rho} \frac{\partial p_0}{\partial y} - \beta(\theta - \theta_0) \cos(S) + \nu (\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2}) \quad (16) \]

Equations (1), (15), (16) and (4), and the associated boundary and initial conditions can be restated in nondimensional form. The nondimensional parameters are defined in the List of Symbols.

\[ \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \quad (17) \]
\[
\frac{\partial U}{\partial \tau} + U \frac{\partial^2 U}{\partial X^2} + V \frac{\partial^2 U}{\partial Y^2} = - \frac{\partial P}{\partial X} - G_R \Theta \sin(S) \frac{\partial^2 U}{\partial X^2} + \frac{\partial^2 U}{\partial Y^2} \tag{18}
\]

\[
\frac{\partial V}{\partial \tau} + U \frac{\partial^2 V}{\partial X^2} + V \frac{\partial^2 V}{\partial Y^2} = - \frac{\partial P}{\partial Y} - G_R \Theta \sin(S) \frac{\partial^2 V}{\partial X^2} + \frac{\partial^2 V}{\partial Y^2} \tag{19}
\]

\[
\frac{\partial \Theta}{\partial \tau} + U \frac{\partial \Theta}{\partial X} + V \frac{\partial \Theta}{\partial Y} = \frac{1}{F} \left[ \frac{\partial^2 \Theta}{\partial X^2} + \frac{\partial^2 \Theta}{\partial Y^2} \right] \tag{20}
\]

\[\Theta(X,0,\tau) = 0\]
\[\Theta(X,1,\tau) = 1.0\]
\[\Theta(0,Y,\tau) = \Theta(A,Y,\tau) = Y\]
\[\frac{\partial \Theta}{\partial X}(0,Y,\tau) = \frac{\partial \Theta}{\partial X}(A,Y,\tau) = 0\]

\[U(X,0,\tau) = U(X,1,\tau) = V(A,Y,\tau) = V(0,Y,\tau) = 0\]
\[U(X,Y,0) = V(X,Y,0) = 0\]
\[\Theta(X,Y,0) = 0.5\]

The pressure terms in Equations (18) and (19) can now be eliminated by differentiating Equation (18) and (19) with respect to \(Y\) and \(X\), respectively, subtracting and simplifying the resulting expression with Equation (17). This process yields Equation (22).
\[
\frac{\partial}{\partial t}\left[ \frac{\partial U}{\partial Y} - \frac{\partial V}{\partial X} \right] + U \left( \frac{\partial U}{\partial Y} - \frac{\partial V}{\partial X} \right) + V \left( \frac{\partial U}{\partial Y} - \frac{\partial V}{\partial X} \right) \\
= G_R \left[ \cos(S) \frac{\partial \Theta}{\partial X} - \sin(S) \frac{\partial \Theta}{\partial Y} \right] + \frac{\partial^2}{\partial X^2} \left[ \frac{\partial U}{\partial Y} - \frac{\partial V}{\partial X} \right] \\
+ \frac{\partial^2}{\partial Y^2} \left[ \frac{\partial U}{\partial Y} - \frac{\partial V}{\partial X} \right] 
\] (22)

If a vorticity function (\( \zeta \)) is now defined as

\[
-\zeta = \frac{\partial U}{\partial Y} - \frac{\partial V}{\partial X} 
\] (23)

and the stream function (\( \Psi \)) is introduced, where

\[
U = \frac{\partial \Psi}{\partial Y} 
\] (24)
\[
V = -\frac{\partial \Psi}{\partial X} 
\] (25)

Equation (22) can be rewritten in terms of vorticity, and Equation (23) in terms of the stream function.

\[
\frac{\partial \zeta}{\partial t} + U \frac{\partial \zeta}{\partial X} + V \frac{\partial \zeta}{\partial Y} = G_R \left[ \sin(S) \frac{\partial \Theta}{\partial Y} - \cos(S) \frac{\partial \Theta}{\partial X} \right] \\
+ \frac{\partial^2 \zeta}{\partial X^2} + \frac{\partial^2 \zeta}{\partial Y^2} 
\] (26)

\[
-\zeta = \frac{\partial \Psi}{\partial X} + \frac{\partial \Psi}{\partial Y} 
\] (27)
The governing equations and boundary conditions which describe natural convection in an inclined rectangular cavity can now be written in their final form.

Vorticity Equation

\[
\frac{\partial \zeta}{\partial t} + U \frac{\partial \zeta}{\partial X} + V \frac{\partial \zeta}{\partial Y} = G_R \left[ \sin(S) \frac{\partial \Theta}{\partial Y} - \cos(S) \frac{\partial \Theta}{\partial X} \right] \\
+ \frac{\partial^2 \zeta}{\partial X^2} + \frac{\partial^2 \zeta}{\partial Y^2}
\]  

(28)

Energy Equation

\[
\frac{\partial \Theta}{\partial t} + U \frac{\partial \Theta}{\partial X} + V \frac{\partial \Theta}{\partial Y} = \frac{1}{Pr} \left[ \frac{\partial^2 \Theta}{\partial X^2} + \frac{\partial^2 \Theta}{\partial Y^2} \right]
\]  

(29)

Stream Function Equation

\[-\zeta = \frac{\partial^2 \psi}{\partial X^2} + \frac{\partial^2 \psi}{\partial Y^2}\]  

(30)

Velocity Component Equations

\[U = \frac{\partial \psi}{\partial Y}\]  

(31)

\[V = \frac{\partial \psi}{\partial X}\]  

(32)
Boundary Conditions

\[ U(0,Y,\tau) = U(A,Y,\tau) = 0 \]
\[ V(X,0,\tau) = V(X,1,\tau) = 0 \]
\[ \psi(0,Y,\tau) = \psi(A,Y,\tau) = \psi(X,0,\tau) = \psi(X,1,\tau) = 0 \tag{33} \]
\[ \theta(X,0,\tau) = 0 \]
\[ \theta(X,1,\tau) = 1.0 \]

Adiabatic Side Walls

\[ \frac{\partial \theta}{\partial Y}(0,Y,\tau) = \frac{\partial \theta}{\partial Y}(A,Y,\tau) = 0 \tag{34} \]

Linear Temperature Side Walls

\[ \theta(0,Y,\tau) = \theta(A,Y,\tau) = \gamma \tag{35} \]

Initial Conditions:

\[ U(X,Y,0) = V(X,Y,0) = 0 \]
\[ \psi(X,Y,0) = \zeta(X,Y,0) = 0 \tag{36} \]
\[ \theta(X,Y,0) = 0.5 \]

Heat Transfer Coefficients

Local and average heat transfer coefficients are expressed as non-dimensional Nusselt numbers.

\[ Nu = hD/k \tag{37} \]
Local Nusselt Number

The convection heat transfer coefficient (h) at the hot wall is defined as follows:

\[ h = \frac{-k(\partial \theta / \partial y)_{\text{wall}}}{\partial H - \partial C} \]  

Equation (38)

Introducing the definition of \( \text{Nu} \), Equation (37), \( \theta \), and \( Y \), Equation (38) becomes

\[ \text{Nu} = (\frac{\partial \theta}{\partial Y})_{\text{wall}} \]  

Equation (39)

Average Nusselt Number

To obtain an average Nusselt Number, \( \overline{\text{Nu}} \), along the hot wall, the local Nusselt Numbers, \( \text{Nu} \), are integrated over the length of the hot wall.

\[ \overline{\text{Nu}} = \frac{\int_0^L \text{Nu} \, dx}{L} \]  

Equation (40)

Partitioned Cavity

A review of the mathematical model of natural convection in an inclined rectangular enclosure shows the governing Equations (28), (29), (30), (31) and (32) are independent of the enclosure geometry. Therefore, these equations can be applied to triangular enclosures, and only the boundary conditions need to be changed.
The partitions will be placed in the enclosure at \( \phi = \pm45^\circ \) degrees with respect to the hot wall, and also all partition steady state temperature distributions will be linear. Therefore, applying these assumptions, the boundary conditions for the partitions can now be written.

\[
\phi = 45^\circ
\]

\[
\Theta(1.0-Y,Y,\tau) = Y
\]

\[
\Psi(1.0-Y,Y,\tau) = 0
\]

\[
U(1.0-Y,Y,\tau)\sin\phi + V(1.0-Y,Y,\tau)\sin\phi = 0
\]

\[
\phi = -45
\]

\[
\Theta(Y,Y,\tau) = Y
\]

\[
\Psi(Y,Y,\tau) = 0
\]

\[
U(Y,Y,\tau)\sin\phi + V(Y,Y,\tau)\sin\phi = 0
\]

Now the partition boundary conditions can be used in combination with those for the rectangular cavity to completely describe the boundaries of an inclined rectangular enclosure with partitions.
III. Numerical Procedure

Rectangular Enclosure

This section contains a description of the procedure that was used to solve the system of equations developed in the previous section. This procedure was adapted from a finite difference computational procedure developed by Wilkes and Churchill (Ref. 4) to study natural convection in a rectangular enclosure with one vertical wall heated and the other cooled. This procedure is illustrated by a flow chart in Figure 3. Because the procedures are so similar, tests of stability and convergence were not rigorously carried out in this study.

The geometry of the rectangular enclosure and the finite difference nomenclature are shown in Figure 4. The mesh spacing in the X-direction is \( \Delta x \) and the Y-direction is \( \Delta y \). Subscripts \((i,j)\) are associated with each mesh point, so that the space variables may be expressed as \( x_i = (i-1)\Delta x \), for \( i = 1,2,\ldots,I \) and \( y_j = (j-1)\Delta y \), for \( j = 1,2,3,\ldots,J \). Time is segmented into equal intervals \( \Delta t \) so that the nondimensional time \( \tau \) is \( \tau = n\Delta t \) for \( n = 0,1,2 \).

The notation \( \phi_{i,j}^n \) denotes the values of the variable at mesh point \((i,j)\) at time level \( n \).

The first equation to be solved from \( n\Delta t \) to \((n+1)\Delta t\) is the energy equation (29), which is parabolic in time,
Figure 3. Numerical Procedure Sequence of Solutions of the Governing Equations.
nonlinear and of second order. The solution to this equation is advanced one time level by using an implicit alternating direction (ADI) technique developed by Peaceman-Rachford (Ref.7).

To apply the ADI method to the energy equation (29) requires the coefficient velocities $U$ and $V$ to be held constant at any grid point over a time step. Now the partial derivatives in Equation (29) can be approximated by finite-differences. (Note: All space derivatives are central differences.)
Figure 4. Inclined Rectangular Enclosure Finite-Difference Grid Representation
\[ T = (n+\frac{1}{2}) \Delta t \]

\[
\frac{\Theta_{i,j}^{n+\frac{1}{2}} - \Theta_{i,j}^n}{\frac{\Delta t}{2}} + \nu_{i,j}^n \left[ \frac{\Theta_{i+1,j}^{n+\frac{1}{2}} - \Theta_{i-1,j}^{n+\frac{1}{2}}}{2\Delta X} \right] + \nu_{i,j}^n \left[ \frac{\Theta_{i,j+1}^n - \Theta_{i,j-1}^n}{2\Delta Y} \right]
\]

\[ = \frac{1}{Pr} \left[ \frac{\Theta_{i+1,j}^{n+\frac{1}{2}} - 2\Theta_{i,j}^{n+\frac{1}{2}} + \Theta_{i-1,j}^{n+\frac{1}{2}}}{\Delta X^2} \right] + \frac{1}{Pr} \left[ \frac{\Theta_{i,j+1}^n - 2\Theta_{i,j}^n + \Theta_{i,j-1}^n}{\Delta Y^2} \right] \quad (43)\]

\[ T = (n+1) \Delta t \]

\[
\frac{\Theta_{i,j}^{n+1} - \Theta_{i,j}^{n+\frac{1}{2}}}{\frac{\Delta t}{2}} + \nu_{i,j}^n \left[ \frac{\Theta_{i+1,j}^{n+\frac{1}{2}} - \Theta_{i-1,j}^{n+\frac{1}{2}}}{2\Delta X} \right] + \nu_{i,j}^n \left[ \frac{\Theta_{i,j+1}^{n+1} - \Theta_{i,j-1}^{n+1}}{2\Delta Y} \right]
\]

\[ = \frac{1}{Pr} \left[ \frac{\Theta_{i+1,j}^{n+\frac{1}{2}} - 2\Theta_{i,j}^{n+\frac{1}{2}} + \Theta_{i-1,j}^{n+\frac{1}{2}}}{\Delta X^2} \right] + \frac{1}{Pr} \left[ \frac{\Theta_{i,j+1}^{n+1} - 2\Theta_{i,j}^{n+1} + \Theta_{i,j-1}^{n+1}}{\Delta Y^2} \right] \quad (44)\]

Equations (43) and (44) are implicit in X and Y directions, respectively, and when applied to every point in a row or column, as the case may be, yield a tridiagonal matrix in the unknown temperatures \( \Theta_{i,j}^{n+\frac{1}{2}} \) or \( \Theta_{i,j}^{n+1} \). In this study, a tridiagonal algorithm adapted by Roache (Ref.7) was used to
solve the tridiagonal matrices.

The vorticity equation (28), which has characteristics similar to the energy equation, can now be solved by the ADI method for new values of vorticity at the \( n \) inner grid points. The vorticity at the boundary points will remain at their old \( n \Delta t \) values during this calculation, and will be advanced later. Because there is a temperature gradient in the vorticity equation (28), the new \((n+1)\Delta t\) temperature field will be used to evaluate the temperature gradient at each grid point. The temperature gradient will then be held constant throughout the calculation. The finite difference representations of the vorticity are

\[
\tau = (n + \frac{1}{2}) \Delta t
\]

\[
\frac{\zeta_{i,j}^{n+\frac{1}{2}} - \zeta_{i,j}^{n}}{\Delta t/2} + u_{i,j}^{n} \left[ \frac{\zeta_{i+1,j}^{n+\frac{1}{2}} - \zeta_{i-1,j}^{n+\frac{1}{2}}}{2\Delta x} \right] + v_{i,j}^{n} \left[ \frac{\zeta_{i,j+1}^{n+\frac{1}{2}} - \zeta_{i,j-1}^{n+\frac{1}{2}}}{2\Delta y} \right]
\]

\[
= G_{R} \left[ \sin(S) \left( \frac{\Theta_{i,j+1}^{n+1} - \Theta_{i,j-1}^{n+1}}{2\Delta y} \right) - \cos(S) \left( \frac{\Theta_{i+1,j}^{n+1} - \Theta_{i-1,j}^{n+1}}{2\Delta x} \right) \right]
\]

\[
\left[ \frac{\zeta_{i+1,j}^{n+\frac{1}{2}} - 2\zeta_{i,j}^{n+\frac{1}{2}} + \zeta_{i-1,j}^{n+\frac{1}{2}}}{\Delta x^2} \right] + \left[ \frac{\zeta_{i,j+1}^{n+\frac{1}{2}} - 2\zeta_{i,j}^{n+\frac{1}{2}} + \zeta_{i,j-1}^{n+\frac{1}{2}}}{\Delta y^2} \right]
\]

\[(45)\]
\[\tau = (n+1)\Delta \tau\]

\[
\frac{\zeta_{i,j}^{n+1} - \zeta_{i,j}^{n}}{\Delta \tau / 2} + U_{i,j}^{n} \left[ \frac{\zeta_{i+1,j}^{n} - \zeta_{i-1,j}^{n+1}}{2\Delta X} \right] + V_{i,j}^{n} \left[ \frac{\zeta_{i,j+1}^{n} - \zeta_{i,j-1}^{n+1}}{2\Delta Y} \right]
\]

\[= G \sin(S) \left( \frac{\theta_{i,j+1}^{n+1} - \theta_{i,j-1}^{n+1}}{2\Delta Y} \right) - \cos(S) \left( \frac{\theta_{i+1,j}^{n+1} - \theta_{i-1,j}^{n+1}}{2\Delta X} \right)
\]

\[
+ \left[ \frac{\zeta_{i+1,j}^{n} - 2\zeta_{i,j}^{n} + \zeta_{i-1,j}^{n}}{\Delta X^2} \right] + \left[ \frac{\zeta_{i,j+1}^{n} - 2\zeta_{i,j}^{n} + \zeta_{i,j-1}^{n}}{\Delta Y^2} \right]
\]

(46)

Equations (45) and (46) are also implicit in X and Y directions, respectively, and when applied to every point in a row or column, as the case may be, also yield a tridiagonal matrix. These matrices are solved by the same algorithm that was used for solving the energy equation.

With the new interior vorticity field calculated, the method of successive over-relaxation is used to solve the stream function equation for the new stream function field. The expression for the \(m+1\) iteration of the stream function at a point is as follows:

\[
\psi_{i,j}^{(m+1)} = \psi_{i,j}^{(m)} + \frac{\omega}{4} \left[ (\Delta X)^2 \zeta_{i,j}^{n+1} + \psi_{i,j+1}^{(m)} + \psi_{i,j-1}^{(m)} + \psi_{i+1,j}^{(m)} + \psi_{i-1,j}^{(m)} - 4\psi_{i,j}^{(m)} \right]
\]

(47)

22
TABLE I

<table>
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<th>No. of grid spacings:</th>
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<th>Y Direction</th>
<th>ΔX(=ΔY)</th>
<th>ωOPT</th>
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<td>10</td>
<td>0.1</td>
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</tr>
</tbody>
</table>

Wilkes and Churchill (Ref.4) determined optimum values of relaxation parameters for some representative grid sizes as seen in Table I. Using these values, Wilkes and Churchill experienced good convergence at each grid point with about twenty five iterations. In this study twenty five iterations were performed for each grid point using the optimum value of the relaxation parameters in Table I.

The new wall vorticities can now be determined from the new stream function field. In this study, two wall vorticity expressions were used depending upon the Grashof Number of the fluid. Wilkes and Churchill results indicated the first expression will cause instabilities above $G_R = 200,000$.

$$\frac{n+1}{2} = \frac{8\psi_{n+1}^{i,2} - \psi_{n+1}^{i,1}}{2(\Delta Y)^2} \text{ when } G_R \leq 200,000$$

(48)
Both expressions were derived by Wilkes and Churchill (Ref.4).

The new velocity fields $U$ and $V$ can now be calculated from the new stream function field. In this study second order space central finite difference approximations were used for the new velocities.

\[
U_{i,j}^{n+1} = \frac{\psi_{i,j+1}^{n+1} - 2\psi_{i,j}^{n+1} + \psi_{i,j-1}^{n+1}}{2\Delta Y} \quad \text{(50)}
\]

\[
V_{i,j}^{n+1} = \frac{\psi_{i+1,j}^{n+1} - 2\psi_{i,j}^{n+1} + \psi_{i-1,j}^{n+1}}{2\Delta X} \quad \text{(51)}
\]

These expressions differ from those of Wilkes and Churchill who used a fourth order finite difference approximation.

Now using the newest temperature field, the local and average Nusselt Numbers can also be calculated. The derivative in Equation (39) is expressed by a second order forward finite difference relation.

\[
Nu = \frac{\Theta_{i,3} - 4\Theta_{i,1}}{2\Delta Y} \quad \text{(52)}
\]

The average Nusselt Number is obtained by integration using the Trapezoidal rule.
In the previous chapter, the mathematical model of natural convection in an inclined rectangular enclosure with partitions was developed. The governing equations were determined to be unchanged. However, new boundary conditions were necessary to describe the partitioned enclosure. In this section, the numerical procedure previously developed will be modified to account for 45 degree partitions. And finally, a method of solution of a partitioned rectangular enclosure will be discussed.

**Numerical Procedure Modification.** The two significant modifications made to the inclined rectangular enclosure numerical procedure were; 1) a new wall vorticity model for the 45 degree partition, and 2) local heat transfer coefficients for the partition. While the wall vorticity models used in the rectangular enclosure are accurate for grid points along the mesh, the following expression (see Ref.7 page 144) provides a more accurate evaluation of the wall vorticity of a sloping wall ($\phi=45$ degrees) with $\Delta X=\Delta Y$.

\[
\zeta_{iw,jw} = \frac{2(\psi_{iw-1,jw} + \psi_{iw,jw+1} - 2\psi_{iw,jw})}{\Delta X}
\]  

(53)

This expression was used to evaluate the wall vorticity of all partitions.

Finally, the local heat transfer equation was modified to determine the heat transfer coefficient across a
partition. First and second order finite difference schemes were sufficient for all grid points along the partition except the end points. At the end points, the heat transfer coefficient across the partition was determined to be equal to the heat transferred along the partition. Details of the heat transfer coefficients expressions can be found in Appendix B.

**Solution Method.** Since the natural convection governing equations did not change with the addition of partitions, each triangular cell can be independently solved by assuming common boundary conditions for the neighboring triangles. However, it is then necessary to compute an energy balance at each partition grid point. If the partition boundary conditions do not balance, it is necessary to iterate the triangular cell partition boundary conditions until the heat transfer coefficients and temperatures match. This iterative procedure, however, was simplified in this study by the thermal characteristic of the partition model.

In this study, the partition model steady state temperature distribution was linear, and the partition was a pure conductor across the partition. Because of these thermal characteristics, the temperature and heat transfer coefficients at each partition grid point always match. Therefore, it was decided to build a composite model of the rectangular enclosure with partitions.
The composite model was composed of individual triangular cells which were each solved independently. Then the solutions were added together to obtain the final natural convection heat transfer results. A complete computer program listing is in Appendix B.
IV. Discussion of Results

The discussion of results centers on two areas: determining the validity and accuracy of the numerical procedure and computer code; and determining the effect of partitioning an inclined rectangular enclosure into triangular regions on natural convection heat transfer.

The computations were conducted (using a CDC 6600 computer) for air cavities ($Pr = 0.7333$) with aspect ratios from 1.0 to 3.0 at heat fluxes yielding $Gr$ values up to $2 \times 10^5$.

Rectangular Enclosure Numerical Results

To determine the validity and accuracy of the numerical procedure, transient and steady state heat transfer results were obtained for rectangular enclosures at various inclination angles, aspect ratios, side wall boundary conditions and Grashof numbers. These results were then compared with previous numerical results obtained by Wilkes and Churchill (Ref.4), Koutsoheras (Ref.5), and Ozoe, et.al. (Ref.6). A complete summary of the computer runs is presented in Appendix A.

Vertical Rectangular Enclosure. The accuracy of the heat transfer solution was determined by comparing the steady state numerical solution of the rectangular enclosure in the vertical position ($S = 90^\circ$)
with heat transfer results attained by Wilkes and Churchill (Ref. 4). A comparison of the two results is shown in Table II.

The results in Table II show that in each comparison, the numerical procedure developed in this study overestimates by five to 12 percent the mean Nusselt numbers achieved by Wilkes and Churchill. This difference in results could be caused by one or both of two differences in the numerical procedures.

In this investigation, the velocity field was calculated from the new stream functions with a second order finite difference representation. On the other hand, Wilkes and Churchill used a fourth order finite difference model to
calculate the velocity field. The higher order model yields more accurate velocities per time step. But, since this investigation was primarily interested in the steady state solution, the improved accuracy of the transient solution velocity field was not necessary. So it was decided to use the less complicated second order finite difference representation.

A second difference between the numerical methods could be the finite difference representation used to determine the local Nusselt numbers at the hot wall. The wall heat flux approximation used by Wilkes and Churchill (Ref.4) was not specified in their report. So, it was decided to calculate the local heat flux with a second order, forward difference approximation in this study. The second order approximation will provide sufficient accuracy for comparison and trend information, but may represent the difference observed in the heat transfer results.

One further comparison of the two numerical procedures was to compare the transient heat transfer results. Figure 5 is a plot of this study's mean Nusselt numbers vs. non-dimensional time, starting from the initial condition to steady state. The shape and indicated trends of the transient solution curve is identical to the plot achieved by Wilkes and Churchill (Ref.4). A conclusion that can be deduced from this result is that even though the two numerical
Figure 5. Transient Solution for the Vertical Square Enclosure
procedures produce slightly different values for mean Nusselt numbers, the difference is constant throughout the solution. Therefore, the numerical procedure developed in this study is an adequate numerical model of transient, as well as steady-state, natural convection in a vertical rectangular enclosure.

**Inclined Rectangular Enclosure.** The previous discussion was limited to determining the adequacy of this study's numerical procedure for the vertical rectangular enclosure. Now it is necessary to analyze the results of the numerical procedure and computer code over the total planned operating range of each of the variables. Figures (6), (7), and (8) illustrate the effects of inclination angle, aspect ratio, Grashof number, and side wall boundary conditions on heat transfer. The following are conclusions which can be drawn from the figures.

I. **Effect of Side Wall Boundary Conditions.** Figures (6) and (7) show that the heat transfer at the hot wall is a strong function of the side wall boundary conditions. The heat transferred at the hot wall decreases approximately 35% when the side walls are changed from an insulated boundary to a pure conductor across the boundary (linear temperature distribution along the side wall). The effect of the side wall boundary condition also appears to be independent of Grashof number and inclination angle. The results of this
effect are in excellent agreement with those reported by Koutsoheras (Ref.5).

II. Effect of Inclination Angle. The effect of inclination angle is best illustrated by Figure 7. The highest heat transfer takes place when the enclosure is inclined at 60° from the horizontal. However, the total change in heat transfer due to a change in inclination angle is insignificant when compared to side wall boundary conditions and aspect ratio changes. This result was previously observed by Koutsoheras (Ref.5) and Ozoe (Ref.6).

III. Effect of Aspect Ratio. The effect of aspect ratio on heat transfer for the case of moderate aspect ratio enclosures with insulated side walls is illustrated in Figure 8.
Figure 7. Effect of Inclination Angle on Heat Transfer for Two Side Wall Boundary Conditions
Figure 8. Effect of Aspect Ratio on Heat Transfer at Various Inclination Angles
This figure shows that changes in Grashof number and inclination angle have a stronger influence on heat transfer in a rectangular enclosure where \(A=1.0\) than in enclosures with \(A=2.0\) or 3.0. This is due to the side wall disturbances in a square enclosure occupying a larger proportion of the enclosure than in higher aspect ratio cavities.

In summary, the numerical results for the inclined moderate aspect ratio rectangular enclosure indicate the validity of the numerical procedure and computer code.

**Effect of Partitions**

In this section, the validity of natural convection heat transfer results for composite rectangular enclosures will be determined. Then, the heat transfer results for the partitioned enclosure will be compared to heat transfer results of rectangular enclosures without partitions. From these comparisons the effectiveness of partitions in reducing natural convection heat transfer across and enclosure will be resolved.

**Composite Enclosures.** To determine the validity of composite heat transfer solutions, two partitioned rectangular enclosures were investigated. These enclosures are shown in Figure (9). The square enclosure is composed of two triangular cells while the rectangular enclosure \((A=2)\) is composed of three triangular cells. Natural convection heat transfer coefficients were evaluated for each of
Figure 9. Partitioned Rectangular Enclosures
these triangular cavities. The heat transfer coefficients of adjoining triangular cells were then compared at the common partition boundary.

In the square enclosures, the total heat transfer across the partition was balanced, however, heat conduction along the partition was required to maintain the partition boundary linear temperature distribution. On the other hand, the total heat transfer across the partitions in the rectangular enclosure (A=2.0) did not balance, eventhough the total heat transfer at the hot and cold walls were balanced. These results indicate valid composite heat transfer solutions exist only for square enclosures with a diagonal partition. An iterative numerical procedure is required for other than square enclosure.

Partitioned Square Enclosures. To determine the effectiveness of diagonal partitions in suppressing natural convection, heat transfer coefficients were evaluated for three square enclosures with adiabatic side walls at various inclination angles, and Grashof numbers. The results are shown in Figure 10.

From this figure, it was concluded that a diagonal partition in a square enclosure reduces natural convection heat transfer by more than 50%. An explanation for the substantial decrease in natural convection heat transfer across the square enclosure is that the diagonal partition increases
Figure 10. The Effect of a 45° Diagonal Partition in an Inclined Square Enclosure on the Rate of Heat Transfer
the wetted surface area by 70%. And, when air flows over this surface, additional friction forces are generated which suppress the natural convection in the enclosure.

Figure 10 also illustrates the effect of partition angle on natural convection heat transfer. The partition oriented at $\phi=-45$ degrees to the hot wall provided an additional 15% decrease in natural convection heat transfer when compared to the partition at $\phi=45$ degrees. To provide an explanation for this further decrease in heat transfer, the steady state temperature distributions for the three square enclosures were examined in Figures 11, 12 and 13.

From these figures, it was concluded that the partition angle affects the thickness of the thermal boundary layer at the hot wall. The partition oriented at $\phi=-45$ degrees resulted in the greater reduction in heat transfer because it produced the thicker thermal boundary layer on the lower half of the hot wall (the region of highest heat transfer), as evidenced by the increased spacing between isotherms.

In summary, the composite heat transfer solution was validated for square enclosures with partitions. Then, a diagonal partition in an inclined enclosure was determined to reduce natural convection heat transfer by more than 50%. 

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Figure 11. Steady State Isotherms in a Vertical Square Enclosure.
Figure 12. Steady State Isotherms in a Vertical Square Enclosure with a Diagonal Partition $\phi=45$ degrees.
Figure 13. Steady State Isotherms in a Vertical Square Enclosure with a Diagonal Partition \( \alpha = -45 \) degrees.
V. Conclusions

Conclusions

The results of this study provide the following conclusions:

1. The finite difference numerical procedure yields valid transient and steady state, natural convection heat transfer coefficients for air filled, inclined, moderate aspect ratio, rectangular enclosures. The procedure is limited to $G_R < 2.0 \times 10^5$, and $10 \leq S \leq 90$.

2. A thin diagonal partition in an inclined square enclosure with insulated side walls reduces natural convection across the enclosure by more than 50%.
VI. Recommendations

Recommendations

The following recommendations are suggested for follow on investigations:

1. Numerical techniques should be developed which would extend the present procedure's Grashof number limitation of $2.0 \times 10^5$.

2. A numerical procedure should be developed to evaluate natural convection heat transfer in an inclined rectangular enclosure with more than one partition. One approach to this procedure would be to assume an initial partition temperature distribution, compute the flow field in each partition cell, then compare the resulting heat transfer coefficients at each partition grid point. If the heat transfer coefficients do not balance, select a new partition temperature distribution, and repeat the process until the heat transfer coefficients balance at each partition grid point. This procedure preserves the computational efficiency obtained with tridiagonal matrices.

3. The effects of radiation heat transfer within the enclosure on partition, and side wall thermal boundary conditions should be investigated.
Bibliography


Appendix A

Numerical Data

Triangular Cell with $\phi = 45^\circ$

$DX = DY = 0.1 \quad Dr = 0.002$

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<th>$G_R$</th>
<th>$AR$</th>
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Triangular Cell with $\phi = 45^\circ$

\[ DX = DY = 0.1 \quad DZ = 0.002 \]

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Rectangular Cavity

$DX = DY = 0.1 \quad DT = .002$

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Appendix B

Computer Code Listing

I. Inclined Rectangular Enclosure with Insulated Side-walls.

II. Inclined Triangular Enclosure $\phi=45$ degrees, Insulated Side Wall.

III. Inclined Triangular Enclosure $\phi=45$ degrees, Insulated Side Wall.

IV. Inclined Triangular Enclosure Two Partition Walls.

V. Tridiagonal Algorithm Subroutine.

Computer Code Notation

AR  Aspect Ratio
DT  Time Increment
DX  Grid Spacing X-direction
DY  Grid Spacing Y-direction
GR  Grashof Number
IX  Number Grid Points in X-direction
IY  Number Grid Points in Y-direction
PR  Prandil Number
S   Inclination Angle (Degrees)
S1  Inclination Angle (Radians)
ST  Stream Function
T   Dimensionless Temperature
U   Dimensionless Velocity in X-direction
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PROGRAM BASIC 74/74 OPT=1

1. PROC A: BASIC (INPU, OUTPUT, INPU=1, OUTPUT=1, TFP=0, Output)

DIMENSION S(31, 31), V(X, 31), T(6, 31), U(31, 31), W(31, 31),

I(31, 31), J(31), K(31), L(31), T(71), W(31, 31),

=, F(31), N(31), 

2. PRINT T(1X, 3, (F11, 5))

3. F0100 (2X, F11, 5, D, F11, 5)

5. INPUT INITIAL BOUNDARY CONDITIONS

1. TIME=1,

PRINT 1, 3, 1, 3, P, G, 8, X, Y, T, A, S1, 17

F0 (INPUT), NE . GO TO 999

S = 31

P0 = A / 3X

IX = A31 + 1.

IY = 1. / Y

TV = A32 + 1.

0. PRINT

PRINT 1, 3, 2, 1, 3, "POINT NUMBER = " , P

PRINT 1, 3, 2, 1, 3, "CMODE NUMBER = " , G, R

PRINT 1, 3, 2, 1, 3, "ASPECT RATIO = " , 17, P

PRINT 1, 3, 2, 1, 3, "DELTA X = " , D, " Y " , "DELTA Y = " , R

PRINT 1, 3, 2, 1, 3, "NUMBER OF INCREMENTS = " , IX

PRINT 1, 3, 2, 1, 3, "Y-INCREMENT = " , IY

PRINT 1, 3, 2, 1, 3, "TIME INCREMENT = " , IT

PRINT 1, 3, 2, 1, 3, "INCLINATION ANGLE = " , S1

PRINT 3, 1, 3, "INCLINATION ANGLE = " , S1

PRINT 3, 1, 3, ""

PRINT 3, 1, 3, ""

0. CONTINUE

O 0 1 I = 1, IX

O 0 1 J = 1, IY

W (I, J) = 0.

U(I, J) = 0.

V(I, J) = 0.

T(I, J) = 0.

I(V(I, J)) = 1.

CONTINUE

F0 (7, 10, 1) TO 110

PRINT 3, 1, 3, "TIME = " , TIME

PRINT 3, 1, 3, "SHEAR FUNCTION"

W2 (I, J) = ((U(I, J), J=1, IY), I=1, IX)

PRINT 3, 1, 3, "VELOCITY "

W2 (I, J) = ((W(I, J), J=1, IY), I=1, IW)

PRINT 3, 1, 3, "V-VELOCITY "

W2 (I, J) = ((U(I, J), J=1, IY), I=1, IW)

PRINT 3, 1, 3, "VALUE ANGLE "

W2 (I, J) = ((V(I, J), J=1, IY), I=1, IW)

PRINT 3, 1, 3, "TEMPERATURE "

W2 (I, J) = ((T(I, J), J=1, IY), I=1, IW)

0. SOLVE ENERGY EQUATION FOR TIME=N+1/2
TEMPERATURE SOLUTION IN X-DICTION (INTERIOR NODES)

10 TT=TT = THE + DT
   TY=3, X=1
   IV=2, Y=1
   $T = 2(\alpha - (Y^2, 2, J))$
   $L = 2(\alpha - (Y^2, 2, J))$
   $A = 2$,
   $A = 2(\alpha - (Y^2, 2, J))$
   DO 2 J = 2, 1, Y
   DO 2 J = 2, 1, Y
   (Y) = $(T - (U(1, J) - A))$
   R(J) = $(T - (U(1, J) - A))$
   R'(J) = $(T - (U(1, J) - A))$
   T(J) = $(T - (U(1, J) - A))$
   T(J) = $(T - (U(1, J) - A))$
   DO 1 T = 1, 1, Y
   CONTINUE

20 CONTINUE
   DO 14 X = 1, 1, Y
      $L = 2$
      $L = 2$
      $X = 1$
      $X = 1$
   CONTINUE

30 SOLVE TRI-DIAGONAL MATRIX
   CALL GTXI (X, Y, P, E, F, N, M, A, L, M, N, M, F)
   DO 12 X = 2, 2, Y
      WK(I, J) = W(I, J)
      WK(I, J) = T(I, J)
      WK(I, J) = T(I, J)
   CONTINUE

20 CONTINUE
   DO 11 X = 2, 2, Y
      $T = 1$
      $K = IX + 1$
      $T = 1$
      $T = 1$
   CONTINUE

27 NOW SOLVE TEMPERATURE DISTRIBUTION, $TIME = N + 1$

11 $TIME = TIME + DT$
   DO 3 X = 2, 2, Y
      DO 3 J = 2, 2, Y
         A(J) = $(T - (U(1, J) - A))$
         R(J) = $(T - (U(1, J) - A))$
         R'(J) = $(T - (U(1, J) - A))$
         T(J) = $(T - (U(1, J) - A))$
         T(J) = $(T - (U(1, J) - A))$
         DO 1 T = 1, 1, Y
         CONTINUE

30 CONTINUE
   DO 19 X = 1, 1, Y
      $L = 1$
      $L = 1$
      $X = 1$
      $X = 1$
   CALL GTXI (X, Y, $P, E, F, M, N, M, F)

54
\[
\begin{align*}
((c^4(0^4))) &= (c^4(0^4)) \\
\lambda_{2} &= 1 + \lambda_{2} = 1 \\
\lambda_{4} &= 1 + \lambda_{4} = 1
\end{align*}
\]
\[ C(J) = (r^J + J_1 + T - (I_J - .)) - (\tau(T + 1 - \tau_1)) + 2 - I(J) + J_4^K (\tau + W_1 IJ + L) \]

\[ V_{-n} = - (10 + (J + K) J) - \left( T_1 - \frac{T_2}{I} \right) \]
CALCULATE WALL VISCOITY FROM DENSITY FUNCTION AT TIME=N+1
FIRST OTHER WALL

\[ \text{IF} \left( \frac{X + \frac{1}{2}}{\Delta X} \right) \text{ IS TO 120} \]
\[ \text{PRINT}, \ "\text{VISCOITY AT TIME=", TIME} \]
\[ \text{IF} \left( \frac{X + \frac{1}{2}}{\Delta X} \right) \text{ IS TO 120} \]
\[ \text{PRINT}, \ "\text{VISCOITY AT TIME=", TIME} \]
\[ \text{IF} \left( \frac{X + \frac{1}{2}}{\Delta X} \right) \text{ IS TO 120} \]
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\[ \text{IF} \left( \frac{X + \frac{1}{2}}{\Delta X} \right) \text{ IS TO 120} \]
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\[ \text{IF} \left( \frac{X + \frac{1}{2}}{\Delta X} \right) \text{ IS TO 120} \]
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\[ \text{PRINT}, \ "\text{VISCOITY AT TIME=", TIME} \]
\[ \text{IF} \left( \frac{X + \frac{1}{2}}{\Delta X} \right) \text{ IS TO 120} \]
\[ \text{PRINT}, \ "\text{VISCOITY AT TIME=", TIME} \]
\[
(1) = (T(1,2,3) - X)^2 + T(1,2,3) + 3
\]

\[
\text{CONTINUE}
\]

\[
\text{PRINT} \quad \text{"TIME = "}, \text{TIME}
\]

\[
\text{PRINT} \quad \text{""}
\]

\[
\text{CONTINUE}
\]

\[
\text{PRINT} \quad \text{""}
\]

\[
\text{PRINT} \quad \text{""}
\]

\[
\text{CONTINUE}
\]

\[
\text{PRINT} \quad \text{""}
\]

\[
\text{PRINT} \quad \text{""}
\]

\[
\text{IF((TIME < 0.15) \&\& \text{?}) \text{GO TO 11; \text{GO TO 1).}
\]

\[
\text{STOP}
\]

\[
\text{END}
\]

GENERAL TRIANGULAR MATRIX SOLVER

DECLARE A(1),B(1), C(1), D(1), E(1), F(1), G(1), H(1), I(1), J(1)

IF(L+EO.1) E(1)=...
IF(L+EO.1) E(1)=A1

IF (L+EO.1) E(1)=1.
IF (L+EO.1) E(1)=0.
IF (L+EO.1) E(1)=A1

F(1)=F(1)-l/(A1-1.)
F(1)=F(1)/(1.-A1)

Y=1
X=2

"END"
(1) \( T(I,J) = (V(I,J) \cdot V(X,J)) \)
(2) \( T(I,J) = (W(I,J) - T(I,J)) \)
(3) \( T(I,J) = T(I,J) - T(I,J) \)
(4) \( T(I,J) = \frac{T(I,J)}{T(I,J)} \)
(5) \( T(I,J) = T(I,J) - T(I,J) \)
(6) \( T(I,J) = T(I,J) - T(I,J) \)
(7) \( T(I,J) = T(I,J) - T(I,J) \)
(8) \( T(I,J) = T(I,J) - T(I,J) \)
(9) \( T(I,J) = T(I,J) - T(I,J) \)
(10) \( T(I,J) = T(I,J) - T(I,J) \)
(11) \( T(I,J) = T(I,J) - T(I,J) \)
(12) \( T(I,J) = T(I,J) - T(I,J) \)
(13) \( T(I,J) = T(I,J) - T(I,J) \)
(14) \( T(I,J) = T(I,J) - T(I,J) \)
(15) \( T(I,J) = T(I,J) - T(I,J) \)
(16) \( T(I,J) = T(I,J) - T(I,J) \)
(17) \( T(I,J) = T(I,J) - T(I,J) \)
(18) \( T(I,J) = T(I,J) - T(I,J) \)
(19) \( T(I,J) = T(I,J) - T(I,J) \)
(20) \( T(I,J) = T(I,J) - T(I,J) \)
(21) \( T(I,J) = T(I,J) - T(I,J) \)
(22) \( T(I,J) = T(I,J) - T(I,J) \)
(23) \( T(I,J) = T(I,J) - T(I,J) \)
(24) \( T(I,J) = T(I,J) - T(I,J) \)
(25) \( T(I,J) = T(I,J) - T(I,J) \)
(26) \( T(I,J) = T(I,J) - T(I,J) \)
(27) \( T(I,J) = T(I,J) - T(I,J) \)
(28) \( T(I,J) = T(I,J) - T(I,J) \)
(29) \( T(I,J) = T(I,J) - T(I,J) \)
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(32) \( T(I,J) = T(I,J) - T(I,J) \)
(33) \( T(I,J) = T(I,J) - T(I,J) \)
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(120) \( T(I,J) = T(I,J) - T(I,J) \)
(1, 1) = v^*(K)
W_1(1, Y) = V_0((1, Y))
W_1(1, Y) = W_0(1, Y)

3. CONTINUE

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CALCULATE VELOCITY AT THE WALL FROM THE STREAM FUNCTION AT Tn:

\[ \text{Wall velocity at time } T_n = \frac{1}{2 \pi} \theta'(x) \]

CALCULATE VELOCITIES AT TIME Tn+1:

\[ u(x, y, T_{n+1}) = \frac{1}{2 \pi} \theta'(x) \]

CALCULATE LOCAL AND AVERAGE NuSELF NUmBER:

\[ Nu_{local} = \frac{1}{2 \pi} \theta'(x) \]
\[ Nu_{average} = \frac{1}{2 \pi} \theta'(x) \]
INITIAL SUMMARY CONDITIONS

PRINT " 
PRINT "POLAR COORDINATE = ", P
PRINT "S. ASK FOR KINSEY = ", K
PRINT " ASK FOR TSO = ", T
PRINT "内部 X = ", X, " ASK FOR Y = ", Y
PRINT "NUMBER OF INCREMENTS = ", I
PRINT "Y=16.667 = ", Y
PRINT "TANGENT ANGLE = ", T
PRINT "OCCUPATION ANGLE = ", O
PRINT " 
D Y = Y + 1
D X = X + 1
IF (J, = R) GO TO 1
IF (J, = R) GO TO 25
IF (I, = R) GO TO 10
T(J, J) = 
G 10 TO 25
T(J, J) = 
G 10 TO 18
10 "(I, J) = 
G 10 TO 18
15 "(I, J) = 
G 10 TO 18
18 "(I, J) = 
G 10 TO 18
20 CONTINUE
G 10 TO 18
SOLVER FOR TIME = N+1/2
TEMPERATURE SOLUTION IN X-DIRECTION (INTERIORS & BOUNDARIES)

1
TIME = TIME + DELT

VX = VX - 1
VY = VY - 1
VXX = VX - 2
VYY = VY - 2
VXY = VX - 1
VYY = VX - 2

UP = DT / (1.0 + (FX'2'2))
PP = DT / (1.0 + (FY))

VX = VX + UP
VY = VY + PP
VXY = VX + 1

K = -VX + J

VXX = VX + 1

KXX = VXX - 2

K = 2.0

T = 100

4

CONTINUE
10 DEF initialize(I, K, J)  
20 FOR I = 1 TO N-1  
30 FOR J = 1 TO N-1  
40 GOTO 20  
50 END


```
CALCULATE LOCAL AND AVERAGE WINDS FOR EACH GRADATION

END
VIII. INITIAL, BOUNDARY CONDITIONS

IF(\^X, F1) THEN...

IF(I1) THEN...

CONTINUE

\text{CONTINUE}
10 \* 1 = 2

11 \* 2 = \* \[XY \times 1\]

12 \* 3 = \* \[\text{J} Y + 1\]

13 \* 4 = \* \[\text{J} \times \text{Y} \times 1\]

14 \* 5 = \* \[\text{J} \times \text{T} \times \text{Y} \times 1\]

15 \* 6 = \* \[\text{J} \times \text{T} \times \text{Y} \times 1\]

16 \* 7 = \* \[\text{J} \times \text{T} \times \text{Y} \times 1\]

17 \* 8 = \* \[\text{J} \times \text{T} \times \text{Y} \times 1\]

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20 \* 11 = \* \[\text{J} \times \text{T} \times \text{Y} \times 1\]

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25 \* 16 = \* \[\text{J} \times \text{T} \times \text{Y} \times 1\]

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67 \* 58 = \* \[\text{J} \times \text{T} \times \text{Y} \times 1\]

68 \* 59 = \* \[\text{J} \times \text{T} \times \text{Y} \times 1\]

69 \* 60 = \* \[\text{J} \times \text{T} \times \text{Y} \times 1\]
PROGRAM D WL '/ ' CPRT=1

\[ T(1) = T(1) + \alpha \cdot \left( \frac{1}{2} \right) / \alpha \]
\[ W = W + \frac{V_2}{X} \cdot \left( \frac{1}{2} \right) / \alpha \]
\[ W = \frac{W + V_2}{V_2} \cdot \left( \frac{1}{2} \right) / \alpha \]

CONTINUE
PRINT " "
PRINT " "
PRINT " NAME = " "
PRINT " "
DO 10 I = 1, N
XX = XX + 1
I = TR, (X, I), P(I)
CONTINUE
PRINT " "
PRINT " NAME = " "
PRINT " "
PRINT " NAME = " "
PRINT " "
IF (Y = G, ..., G) GO TO 1
GO TO 10
END
VITA

Thomas K. Toltzien was born on May 15, 1949 in Madison, Wisconsin to Paul R. and Jo K. Toltzien. In June 1967, he graduated from Madison West High School. He then attended the University of Wisconsin-Madison, and received a Bachelor of Science degree in Mechanical Engineering in January 1972. He entered the United States Air Force in June 1972, and received a commission through OTS in September 1972. He was then assigned to Mather AFB, Ca. for navigator training. Following graduation in July 1973, he was assigned to the 16th Tactical Reconnaissance Squadron (TRS), Shaw AFB, SC for RF-4C Weapon Systems Officer (WSO) training. Upon completion of training, he was assigned to the 14th TRS, Udorn RTAFB, Thailand as a Mission Ready RF-4C WSO. In April 1975, he was reassigned to the 1st TRS, RAF Alconbury, England. While stationed at RAF Alconbury, he was a RF-4C Instructor Weapon Systems Officer, and a Flight Examiner. Capt. Toltzien was assigned to the United States Air Force Institute of Technology in June 1979 in the Graduate Aeronautical Engineering Program.

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Madison, Wisconsin 53711
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<td>Numerical Solution of Natural Convection in an Inclined Rectangular Cavity with Partitions.</td>
<td>MS Thesis</td>
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### ABSTRACT
A numerical investigation was conducted on two-dimensional natural convection within inclined rectangular enclosures partitioned into 45 degree triangular cells. The time dependent governing equations, vorticity, energy, and stream function, were solved by an ADI method and a Gauss-Seidel SOR technique. The numerical procedure was validated for rectangular enclosure, then modified for triangular cells. Heat transfer coefficients were determined for an inclined.
Numerical Solution of Natural Convection in an Inclined Rectangular Channel
square enclosure with a diagonal partition for Grashof numbers less than $2 \times 10^5$, and inclination angles between 10 degrees and 90 degrees. These results show a diagonal partition reduces the heat transferred by natural convection across an inclined square enclosure by more than 50%.