FINITE ELEMENT SIMULATION OF FAST FRACTURE IN STEEL DCB SPECIMEN

JUL 81 T NISHIOKA, S N ATLURI

UNCLASSIFIED GIT-CACM-SNA-12
Finite Element Simulation of Fast Fracture in Steel DCB Specimen.
FINITE ELEMENT SIMULATION OF FAST FRACTURE
IN STEEL DCB SPECIMEN

T. Nishioka* and S.N. Atluri**

Center for the Advancement of Computational Mechanics
School of Civil Engineering
Georgia Institute of Technology, Atlanta, GA 30332

* Research Scientist II
** Regents' Professor of Mechanics
Abstract:

Results of a numerical simulation, based on an energy consistent moving singularity dynamic finite element procedure, of fast crack propagation and arrest in a high strength steel DCB specimen are presented. The influence of material properties of high strength steel on dynamic crack propagation and arrest is investigated. The influence of the loss of contact of specimen with the loading wedge is also critically examined. The present numerical results are compared with available experimental data. It is found that the present results agree well with available experimental data, and the crack arrest toughness values obtained in the present analysis correlate well with the ratio of the maximum kinetic energy of the specimen to the input energy.

Introduction:

The technique of the measurement of dynamic stress intensity factors for fast running and arresting cracks in specimen made from a transparent photoelastic material, Aralidite B, has been developed by Kalthoff et al [1,2,3]. In the experiments, stress intensity factors for fast running cracks were measured by means of the shadow optical method of caustics. This method was later applied for a nontransparent specimen [4]. The stress intensity factors were measured by the caustics reflected from the mirrored surface of a high strength steel specimen. In the case of high strength steel, the overall variation of stress intensity factors during the crack propagation was found to be similar to that in Araldite B. For some portion of the crack propagation phase, however, the stress intensity factors in the high strength steel specimen show large oscillations, whereas the data for Araldite B specimen can be represented by a rather smooth curve. The authors in Ref. [4] attribute this oscillation to high frequency stress waves interacting with the crack. However, it is the present authors' opinion that these oscillations may be limited to the surface of the
specimen, due to the presence of vibration of the specimen surface. Therefore, stress intensity factors along the crack front within the specimen thickness may be expected to show a rather smooth variation.

The primary objective of the present paper is an attempt to simulate the crack propagation and arrest by using the data for steel specimens presented in Ref. [4]. The authors have presented a "moving singularity" finite element procedure for simulation of fast crack propagation in finite bodies [5,6,7]. This special finite element method has been previously applied, for the "generation" and "prediction" phase calculations of dynamic fracture in DCB specimen made from the model-material Araldite B [8], and for analysis of dynamic fracture in dynamic tear test specimen [9].

In Ref. [4], insufficient data for crack propagation history which are required in the present generation phase study [calculation of dynamic K-factors for a given crack-propagation history] have been measured in the experiment. In the present paper three curves for crack propagation history are hypothesized to perform the calculation. The influence of material constants on crack propagation and arrest in DCB specimen is also investigated by changing Young's modulus $E$, Poisson's ratio $\nu$ and the mass density $\rho$. In addition, in the present paper, careful attention is paid to the wedge-loading condition. Both fixed and contact/no-contact loading conditions are analyzed. The obtained numerical results are critically examined and some conclusions that may be germane to the process of crack propagation in structural steels are made.

Outline of Moving Singularity Finite Element Method:

In the procedure adopted in the paper, the basis functions used for displacement, velocity, and acceleration in the singular element near the crack-tip are:

$$ u_a(\xi,x_2,t) = u_{aj}(\xi,x_2,b)\delta_j(t) \ [a=1,2; \ j=1,\ldots,N] \quad (1) $$
\[
\dot{u}_a = u_{aj} \dot{\beta}_j - v u_{aj} \xi \dot{\beta}_j \\
\ddot{u}_a = u_{aj} \ddot{\beta}_j - 2v u_{aj} \xi \dot{\beta}_j + v^2 u_{aj} \xi^2 \beta_j
\]

where \( u_{aj} \) correspond to the "steady-state" (i.e., which are invariant to an observer moving with the crack-tip) eigen-function solutions for the elasto-dynamic wave equations (with independent variables \( \xi \), and \( x_2 \)) for crack propagation at constant velocity \( v \) in a plane domain. Note that \( x_\alpha (\alpha = 1, 2) \) are fixed coordinates, with \( x_2 = 0 \) defining the crack plane and \( \xi = x_1 - vt \). It is noted that the first term, viz., \( u_{a1} \), leads to the appropriate \( (r^{-1}) \) type singularity in strains and stresses. The singular element in the present procedure is surrounded by the usual isoparametric [8-noded, in the present case] elements. The displacement compatibility between the singular element and the surrounding isoparametric elements is satisfied in the present analysis through a least-square technique [5,6].

Consider two instants of time, \( t_1 \) and \( t_2 = t_1 + \Delta t \). Assuming that in a Mode I crack propagation problem, the crack-lengths at \( t_1 \) and \( t_2 \) are, respectively, \( E_1 \) and \( E_1 + \Delta E \). Let the displacements, strains, and stresses at \( t_1 \) be denoted by \( u_1^1, \varepsilon_{ij}^1, \) and \( \sigma_{ij}^1 \), respectively, while those at \( t_2 \) are denoted by a superscript 2 for each variable. The variables at time \( t_1 \) are presumed to be known. It has been shown in [5,6] that the variational principles governing the dynamic crack propagation between times \( t_1 \) and \( t_2 \) can be written as:

\[
\int_{V_2} \left( \sigma_{ij}^1 + \sigma_{ij}^2 \right) \delta \varepsilon_{ij}^1 + \rho \left( \dot{u}_{ij}^1 + u_{ij}^2 \right) \delta u_{ij}^2 \, dV = \int_{S_2} (\tilde{T}_{ij}^1 + \tilde{T}_{ij}^2) \delta \varepsilon_{ij}^1 \, ds + \int_{\varepsilon_1^+} (\tilde{T}_{ij}^2 + \tilde{T}_{ij}^1) \left( \delta \varepsilon_{ij}^2 \right) \, ds \\
+ \int_{\Delta L^+} (\tilde{T}_{ij}^2 + \tilde{T}_{ij}^1) \left( \delta \varepsilon_{ij}^2 \right) \, ds
\]

(4)
where $V_2$ is the domain of the body, and $S_{0_2}$ is the boundary of $V_2$ where trac-
sions are prescribed, at time $t_2$. $\overline{T}_{1}$ are the prescribed tractions at time $t_1$
at $S_{0_1}$ ($=S_{0_2}$) and $\overline{T}_{1}$ are the prescribed tractions at $S_{0_2}$ as well as at the newly
created crack surface $\Delta E$ at time $t_2$. It is seen that $\sigma_{i j}^{1}$ and $v_{j}^{1}$ at $\Delta E$ are the co-
hesive forces holding the crack-face together at time $t_1$. In the above, mode I
conditions are assumed; hence, only the upper half of the domain with the crack
face $\mathbb{E}^+$ is considered.

In the variational principle in Eq. (4), the variables $\bar{u}_{i}^{1}$ and $\sigma_{i j}^{1}$ are
presumed to be known; while $\sigma_{i j}^{2}$, $\epsilon_{i j}^{2}$ and $u_{j}^{2}$ are the variables. The variables
$u_{j}^{2}$ are assumed according to Eq. (1), with the velocity $v_{2}$ appearing in them.
Further, the variational principle in Eq. (4) is used to develop a discrete
(finite element) approximation for a (finite element) mesh at time $t_2$. Note
that at time $t_2$, in the present problem, the crack-tip is located at $x=E_1+\Delta E$.
In developing the equations for the finite element mesh at $t_2$, it is seen
from Eq. (4), that the variation of $\sigma_{i j}^{1}$ and $u_{j}^{1}$ must be known in the finite
element mesh at time $t_2$. However, $\sigma_{i j}^{1}$ and $u_{j}^{1}$, and $\bar{u}_{i}^{1}$ were solved for, in the
finite element mesh at $t_1$. In the mesh at $t_1$ the crack-tip is located at
$x_1=E_1$ and hence the crack-element is centered at $\Sigma_1$. Thus, between $t_1$ and $t_2$
($=t_1+\Delta t$) the crack-element is translated by an amount $\Delta E$. While the crack-
element is translated, only the elements immediately surrounding the moving
 crack-tip are distorted. Thus the finite meshes at times $t_1$ and $t_2$
only in the location of crack-tip (and hence the crack-element) and the shapes
of the immediately surrounding isoparametric elements. Thus, the known data
for $\sigma_{i j}^{1}$ and $u_{j}^{1}$ in the mesh at $t_1$ is interpolated easily into corresponding
data in the mesh at $t_2$. Based on these concepts, the development of the finite-
element equations form the principle in Eq. (4), and the numerical integration
of these equations follows the well-established procedures. Further details
can be found in [5,6] where it is shown that the dynamic k-factors can be computed directly in the present analysis procedure.

Analysis Procedure for Double-Cantilever-Beam Specimen:

The test specimen geometry is indicated in Fig. 1 along with the initial configuration of the finite element mesh. Because of symmetry, only the upper half of the DCB specimen is modeled in the present analysis. Point L in Fig. 1 represents the loading point. Forty six 8-noded isoparametric elements and one moving singularity element shown by the shaded area are used. The specimen geometry indicated in Fig. 1 corresponds to that reported in Ref. [4], and a plane-stress condition is invoked in the present two-dimensional analysis.

In the present series of computations, the crack growth history is used as input data to the "generation phase" fracture simulation. As output of these generation phase computations, dynamic stress intensity factors for the propagating crack is directly obtained as a function of time. Fig. 2 shows three types of data for the crack extension history $E = E(t)$ as well as the crack velocity history $V = V(t)$, i.e., Data 1, Data 2, and Data 3. The data obtained by experiment in Ref. [4] are shown by the solid lines. To complete the input data, the broken lines are assumed, as plausible extensions of the experimentally measured dates. The crack extension histories are obtained by integrating the crack velocity histories for each case.

In Ref. [4], the crack initiation stress intensity factor for a blunt notch, $K_{IQ}$, was quoted as 224 MNm$^{-1.5}$. Prior to the dynamic analysis, a static analysis of the specimen is performed to obtain the critical load-point deflection which produces the initiation stress intensity factor $K_{IQ} = 224$ MNm$^{-1.5}$ at the crack tip. Then the crack starts propagating dynamically from this initial static state of the specimen. The static stress intensity factor as well as dynamic stress intensity factors during the crack propagation are obtained
directly by the present singularity element procedure as described earlier.

In the experiment [4], the specimen was loading in a testing machine by forcing a 20-degree wedge between the pins as shown in Fig. 3a. After crack initiation the wedge was fixed at the same position. Obviously the wedge can "push" the pins attached to the specimen but not "pull" them. Thus there is the possibility of a lack of contact of the specimen (pins) with the wedge (see Fig. 3b). In one case, the wedge loading condition taking account of the above effect of no-contact is considered, while, in other cases, the fixed loading condition, i.e., one in which the wedge is always in contact with the pins, is used.

Using the standard notation, the reaction forces at the points where displacements are prescribed are calculated by:

\[ P = Kq + m\ddot{q} \]

The displacement \( u \) and reaction force \( P \) in the time step \((n+1)\) are predicted by:

\[ u_{n+1} = u_n + \Delta t\frac{\Delta u_n}{\Delta t} \]

\[ P_{n+1} = P_n + \frac{(P_n - P_{n-1})}{\Delta t_n} \Delta t_{n+1} \]

(6) \hspace{1cm} (7)

It is noted that we may use \( \Delta t_{n+1} = \Delta t_n = \Delta t \).

We designate the reaction forces with which the wedge pushes the pins as being positive. Thus in Fig. 3a, both the reaction forces acting on the upper and lower pins are positive. The no-contact condition during the time increment \( n \) to \((n+1)\) is predicted to occur after the sub-increment of time:

\[ \Delta t_c = \frac{P_n}{(P_{n-1} - P_n)} \Delta t \]

(8)

If \( 0 < \Delta t_c < \Delta t \), during the \((n+1)\) step we change \( \Delta t \) to \( \Delta t_c \) and perform the analysis.
with the condition of contact, and during (n+2) step, we change $\Delta t$ to $\Delta t_F$ ($=\Delta t-\Delta t_c$) and perform the analysis with the condition of no-contact (free).

An analogous scheme is used to predict the transition from no-contact to contact conditions. By monitoring the displacement, the sub-increment of time to reestablish contact is predicted by:

$$\Delta t_F = \frac{-\delta_L}{\delta_L}$$

where $\delta_L = u_L - u_{L\cdot}$. If $0 < \Delta t < \Delta t_F$, during the (n+1) step we change $\Delta t$ to $\Delta t_F$ and perform the analysis with the no-contact condition, and during the (n+2) step we change $\Delta t$ to $\Delta t_c$ ($=\Delta t-\Delta t_F$) and perform the analysis with the contact condition. These schemes are repeated for the entire computation.

The high strength maraging steel HFX760 was chosen in the experiment [4]. Reference [4] has indicated that the steel has a yield strength of $\sigma_{ys} = 2.1$ GN/m$^2$, a crack initiation toughness $K_{IC}$ in the range of 70 to 100 MNm$^{-1.5}$, and a bar wave speed of $C = 5190$ m/sec. However reference [4] has not indicated any other material properties such as Young's modulus $E$, Poisson's ratio $\nu$ and the mass density $\rho$ which are required in an elastodynamic analysis. To investigate the effect of material properties on crack propagation and arrest in the DCB specimen, four different hypothesized material- properties, as listed in Table 1, are used in the present analysis.

Results and Discussions

(1) **Fixed Loading (Prescribed Displacement; wedge always in contact with specimen)**

First we consider the Material I case. The variation of dynamic stress intensity factor computed in the present generation phase simulation is shown in Fig. 4. The time increment $\Delta t$ used in the present analysis is 1.5 $\mu$sec. After 183 $\mu$sec. the simulation was continued with three different crack extension histories, i.e., Data 1, Data 2, and Data 3. As seen from the figure, in the
Data 1 case, the dynamic stress intensity factors continuously decrease before the crack arrest. On the other hand in the Data 2, and Data 3 cases, the stress intensity factors increase just before the crack arrest. Obviously, the Data 1 case is the most realistic. The crack arrest toughness $K_{\text{ia}}$ in this case for Material I is obtained as 55.3 MPa m$^{1.5}$. The range for the crack initiation toughness $K_{\text{ic}}$ is also shown in Fig. 4. $K_{\text{ia}}$ value appears to be lower than the crack initiation toughness $K_{\text{ic}}$. Notations $D_A$, $S_C$, $D_B$ and $R_A$ will be explained later.

The presently obtained $K$-values for Material I are shown in Fig. 5 along with those measured in the experiment [4]. The experimental results show large oscillations for the period of the crack length of 100 mm to 190 mm. After this period the experimental results become smoother. The present result is very close to the experimental results during the period of $L > 190$ mm, and close to the lower bound of the experimental oscillations during $100 \text{ mm} < L \leq 190$ mm.

As mentioned earlier, in the authors' opinion, these oscillations in the experiment may be due to the high frequency vibration of the surface of the steel specimen. Although a three-dimensional analysis is required to investigate the effects of the surface vibrations, inside the thickness of this thin specimen, a "generalized plane stress" two-dimensional analysis may be seen to be valid. In comparing both the results it seems plausible that this vibration occurs only on the surface of the specimen.

The computed variations of input energy $W$, strain energy $U$, kinetic energy $T$, and fracture energy $F$ are shown in Fig. 6. It is noted that in the present procedure the dynamic $K_I$-value is calculated directly as a variable in the finite element equations [5,6]. The fracture energy is thus calculated directly by integrating the energy release rate based on the present $K_I$-value. Alternatively,
fracture energy is also calculated directly from a crack-tip integral of work
done in separation of crack-faces. These two procedures gave almost identical
results in the present analyses.

Since the input energy to the specimen W is a constant in the present
case, the above computed F, U, and T should add up to a constant. It is seen
that the error in (F+U+T) as compared to W increases almost linearly from
0.0% to 3.3% towards the end of crack propagation. Since this analysis was
carried out in 140 time steps, it is reasonable to presume that the error in
each time step is thus roughly 0.02%. This appears to give enough credence
to the presently computed stress intensity factors for this type of specimen.
In other types of specimen such as dynamic tear test specimen [9], however,
it was found that the total output energy (F+U+T) is almost identical to the
input energy W during the analysis carried out in 360 time steps. It is seen
from Fig. 6 that about 88% of input energy is consumed as fracture energy in
the present steel DCB specimen. The strain energy U continuously decreases up
to the time of crack arrest. Contrary to this, the kinetic energy T, takes its
maximum value as 28.9% of the total input energy at the earlier stage of the
-crack propagation, and becomes negligible at crack arrest.

Next we consider the Material II case. Fig. 7 shows the variation of dynamic
stress intensity factors. In the Data 1 and Data 2 cases the stress intensity
factors take the minimum values before crack arrest. The minimum $K_I$-value in
the Data 1 case is 40.5 Mnm$^{-1.5}$ which is considerably lower than $K_{Ia}$ in the
Material I case. Fig. 8 shows the $K_I$-value as a function of crack length. For
the crack length values of 100 to 190 mm, the present results agree well with
the lower bound of the experimental data. The variations of the total work,
strain energy, kinetic energy, and fracture energy are shown in Fig. 9. The
maximum kinetic energy in this case is 25.6% of the total input energy, which
is lower than that in the Material I case.

Now we consider the Material III case. In this case, only Poisson's ratio is different from that in the Material I case. The variation of dynamic stress intensity factors is shown in Fig. 10. The results are very close to those in the Material I case. The $K_I$-value as a function of crack length and the energy variation in this specimen are respectively shown in Figs. 11 and 12. Again the results are very close to those in the Material I case.

Finally, we consider the Material IV case. In this case only the mass density is different and 14% higher than that in the Material II. The variation of dynamic stress intensity factors is shown in Fig. 13. The crack arrest toughness $K_{IA}$ obtained for this specimen using Data 1 is 51.0 MNm$^{-1.5}$, which is about 8% lower than that in the Material I case. Fig. 14 shows dynamic $K_I$-value as a function of crack length. For the crack length of 100 to 190 mm, the present $K_I$-value variation is lower than the lower bound of oscillation of the experimental data, while for $\Sigma > 190$ mm the present results agree excellently with the experimental results. Fig. 15 shows the energy variations. The maximum kinetic energy obtained in this specimen is 28.1% of the total input energy.

The maximum kinetic energies and the crack arrest toughness obtained for the four cases are summarized in Table 2. A good correlation between the inertia effect (the ratio of the maximum kinetic energy to input energy) and crack arrest toughness, i.e., the increasing $K_{IA}$ with the increasing ratio of the maximum kinetic energy to input energy $[(\text{max } T)/W]$ can be observed in Table 2.

The influence of Poisson's ratio on dynamic stress intensity factors is shown in Fig. 16, comparing directly the Material I and II cases. Almost identical variations of stress intensity factor can be seen in Fig. 16 for the two cases of $\nu$. On the contrary, a large effect of Poisson's ratio on crack propagation
and arrest in DCB specimen has been reported in Ref. [12]. The author of Ref. [12] has claimed that for any given geometry, different materials are distinguished in the finite difference scheme by their correspondingly different Poisson's ratio only. This is quite different from the situation in any other numerical schemes such as the finite element method and so on. This is also different from the situation in elastostatic analysis. To explain the claim, the author in Ref. [12] described that all physical quantities in the problem were given relative to the specimen height $H$, the dilatational wave velocity $C_1$, and the material density $\rho$. The distortional wave velocity $C_2$ was defined in terms of $C_1$ according to the relation $C_2 = C_1 \sqrt{(1-2v)/(2-2v)}$. From this, the claims mentioned above was derived. However this explanation does not appear correct, since the dilatational wave velocity $C_1$ cannot be a basic unit. The velocity $C_1$ depends not only on the Poisson's ratio and mass density but also on the Young's modulus, since $C_1$ is expressed as

$$C_1 = \sqrt{\frac{E(1-v)}{\rho(1+v)(1-2v)}}$$

under the plane strain condition assumed in Ref. [12]. If Poisson's ratio is changed with keeping $C_1=1$ and $\rho=1$, Young's modulus is also changed according as:

$$E = \frac{(1+v)(1-2v)}{(1-v)}$$

Therefore the dynamic effect shown in Ref. [12] includes the effects of Young's modulus as well as Poisson's ratio.

The influence of the Young's modulus on dynamic stress intensity factors is shown in Fig. 17. The result shown by the solid line for $v=0.3$ was obtained by taking the average of $K_1$-values for $v=0.318$ (Material I) and $v=0.280$ (Material II). The figure indicates that the dynamic effect in the specimen of $E=183$ GPa (Material I) is larger than that in the case of $E=190$ GPa (Material IV). This
means that the dynamic effect increases with the decreasing Young's modulus. This tendency can also be found in Table 2, i.e., the ratio of maximum kinetic energy to input energy in Material I (E=183 GPa) is larger than that in Material IV (E=190 GPa).

The influence of mass density on the dynamic stress intensity factors is shown in Fig. 18. The figure indicates that the dynamic effect increases with the increasing mass density. Again this tendency can be observed on Table I.e., the ratio of maximum kinetic energy to input energy in Material IV (ρ=8042 kg/m$^3$) is larger than that in Material II (ρ=7053 kg/m$^3$).

For all cases considered here, at the beginning of the crack propagation, the dynamic stress intensity factors decrease drastically, and then become constant for a while. At about a half of the crack propagation histories, the present stress intensity factor variations exhibit their peaks. To investigate these phenomena, the times for various waves, generated from the fast crack initiation and reflected from boundaries, to interact with the propagating crack-tip are computed and shown in Figs. 4, 7, 10, and 13. With A, B, and C denoting the three boundaries as marked in Fig. 1, $D_B$ and $D_C$ are the times when the dilatational waves reflected from the boundaries B and C, respectively, interact with the propagating crack-tip. Similar notations are used for $R_A$ and $S_C$ denoting respectively the Rayleigh wave reflected from the boundary A and the shear wave reflected from the boundary C. It is interesting to note that the $K_I$-value begins to be constant at the time $D_C$, and begins to peak at the time $D_B$. It is also seen that the peak in the variation of $K_I$-value occurs shortly after the time $R_A$. Effects of Rayleigh waves in dynamic crack propagation have also been studied in Ref. [7,13,14].

Furthermore, to investigate the effect of Rayleigh wave on dynamic fracture, the Rayleigh wave velocities $C_R$ are also listed in Table 2. It is seen that the Rayleigh wave velocity has good correlations with both the ratio of maximum
kinetic energy to input energy, and the crack arrest toughness.

(ii) **Wedge Loading (Contact/No-contact)**

For the Material I, the variation of reaction force at the loading point where the displacement is prescribed during the crack propagation is shown in Fig. 19. The reaction force becomes zero at \( t = 60 \mu \text{sec} \), and then oscillates with decreasing amplitude. A negative reaction force is observed during time periods 60 \( \mu \text{sec} \) to 100.5 \( \mu \text{sec} \), 129 \( \mu \text{sec} \) to 171 \( \mu \text{sec} \), 187.5 \( \mu \text{sec} \) to 202.5 \( \mu \text{sec} \), and so on. This phenomenon can also be observed in the reaction force variation in the dynamic tear test specimen [9]. During the periods of negative reaction force, the wedge is not pushing but pulling the specimen (pines). This situation is not realistic in the mechanism of the wedge loading.

The variation of crack opening displacements during the crack propagation is shown in Fig. 20. Since the displacement at the loading point of \( x = 16 \text{ mm} \) and \( y = 20 \text{ mm} \) is always fixed, the beam parts of the specimen rotate around this point due to the crack extension. The variation of crack-face profiles indicates this rotation.

To simulate a more realistic mechanism of the wedge loading, the conditions of contact/no-contact are invoked in the present analysis. The variations of reaction force, and the distance between the wedge and the point \( L \) are shown in Fig. 21. \( L_1 \) as shown in Fig. 21 is the time when the reaction force becomes zero. As seen from the figure, the specimen is not in contact with the wedge after \( L_1 \) (=60 \( \mu \text{sec} \)). The distance between the wedge and the point \( L \), \( u_L - u_L' \), becomes larger and larger with time.

The variation of crack opening displacements with the condition of contact/no-contact is shown in Fig. 22. In contrast to the crack-face profiles for the fixed loading case as shown in Fig. 20, it can be seen from Fig. 22 that the variation of the crack-face profiles shows the parallel movement of the beam parts of the specimen after the no-contact condition occurs at \( t = 60 \mu \text{sec} \).
Fig. 23 shows the comparison of the dynamic stress intensity factors obtained with the different loading conditions. In comparing the both results, it is seen that the $K_I$-values calculated with the wedge (contact/no-contact) loading, are exactly same before 60 μsec, almost identical during the time of 60 μsec to about 120 μsec, and lower during the time of 120 μsec to 210 μsec. The effect of the no-contact condition on dynamic stress intensity factor starts manifesting roughly 60 μsecs after the condition of no-contact occurs. This is due to the time-lag in which the "no-contact" effect propagates from the point L to the running crack-tip. To further investigate the propagation speed of this effect, the arrival times of the elastic waves emanating from the loading point are examined. $D_L$ and $S_L$ as shown in Fig. 23 are, respectively, the arrival times of the dilatational and shear waves, emanated from point L, at the crack-tip. It is seen that the no-contact effect at the crack-tip begins to manifest itself at the instant $S_L$ while no effect can be seen at the time $D_L$. In the wedge loading (contact/no-contact) case, a slightly lower crack arrest toughness was obtained as 54.2 Mnm$^{-1.5}$.

Fig. 24 shows the variation of the energies obtained from the present analysis with the condition of contact/no-contact. The kinetic energy variation after 120 μsec appears to be higher than that in the fixed loading case as shown in Fig. 6. This higher kinetic energy is due to the movement of the beam parts of the specimen away from the wedge.

Summary and Conclusion:

Utilizing the moving-singularity element procedure, finite element simulations of fast fracture in high strength steel DCB specimen have been performed for different material properties, different crack propagation histories, and different loading conditions.

The major conclusions and observations obtained from this study are summarized below:
(1) The dynamic crack propagation and arrest are influenced, largely by the mass density, moderately by the Young's modulus, and almost negligibly by the Poisson's ratio.

(2) The variation of dynamic stress intensity factors is influenced by the various waves originally generated from the fast crack initiations and then reflected from the boundary of the specimen.

(3) The ratio of the maximum kinetic energy to the input energy increases with the decreasing Rayleigh wave velocity.

(4) The crack arrest toughness, for a given crack propagation history, increases with the increasing ratio of the maximum kinetic energy to the input energy, or with the decreasing Rayleigh wave velocity.

(5) Analysis with a realistic wedge loading condition (contact/no-contact) gives a slightly lower variation of stress intensity factors than that with the fixed loading condition (specimen always in contact with the wedge). Effects of the different loading conditions depend on the initial crack length and crack velocity. This contact/no-contact effect propagates with a speed of the order of shear wave velocity. Thus, if a larger initial crack length is used, this effect appears at the crack-tip much later.

Acknowledgements:

This work was supported by ONR under Contract No. N00014-78-C-0636. The authors thank N. Perrone for his encouragement. Sincere appreciation to Ms. Margarete Eiteman for her care in typing this manuscript. The authors also thank M. Perl for providing useful information.

Reference:


(11) Kalthoff, J.F., Private Communication to M. Perl, Institut fur Frestkorpermechanik der Fraunhofer-Gesellschaft, Freiburg, Germany.


Captions for Figures and Tables:

Table 1: Material Property Data for Different Cases

Table 2: Dynamic Effects on crack arrest toughness

Fig. 1: Finite element model for a double-cantilever-beam specimen.

Fig. 2: Crack propagation history and crack velocity history as input data to generation phase fracture simulation.

Fig. 3: Contact/no-contact conditions between wedge and pins.

Fig. 4: Variation of dynamic stress intensity factors (Material I).

Fig. 5: Dynamic stress intensity factors versus crack length (Material I).

Fig. 6: Energy variations (Material I).

Fig. 7: Variation of dynamic stress intensity factors (Material II).

Fig. 8: Dynamic stress intensity factors versus crack length (Material II).

Fig. 9: Energy variations (Material II).

Fig. 10: Variation of dynamic stress intensity factors (Material III).

Fig. 11: Dynamic stress intensity factors versus crack length (Material III).

Fig. 12: Energy variations (Material III).

Fig. 13: Variation of dynamic stress intensity factors (Material IV).

Fig. 14: Dynamic stress intensity factors versus crack length (Material IV).

Fig. 15: Energy variations (Material IV).

Fig. 16: Influence of Poisson's ratio on dynamic crack propagation and arrest.

Fig. 17: Influence of Young's modulus on dynamic crack propagation and arrest.

Fig. 18: Influence of mass density on dynamic crack propagation and arrest.

Fig. 19: Variation of reaction force between wedge and pins during the crack propagation (fixed loading condition).

Fig. 20: Variation of crack-face profiles (fixed loading condition).

Fig. 21: Variations of reaction force and distance between wedge and pin L (wedge loading condition: contact/no-contact).

Fig. 22: Variation of crack-face profiles (wedge loading condition).

Fig. 23: Influence of the loading conditions on dynamic crack propagation and arrest.

Fig. 24: Energy variations with the wedge loading condition.
Table 1
(Data 1)

<table>
<thead>
<tr>
<th>Material Number</th>
<th>Young's Modulus E[GN/M²]</th>
<th>Poisson's Ratio ν</th>
<th>Mass Density ρ[kg/m³]</th>
<th>Bar Wave Speed √E/ρ [m/sec]</th>
</tr>
</thead>
<tbody>
<tr>
<td>I</td>
<td>183&lt;sup&gt;(a)&lt;/sup&gt;</td>
<td>0.318&lt;sup&gt;(a)&lt;/sup&gt;</td>
<td>8042&lt;sup&gt;(a)&lt;/sup&gt;</td>
<td>4770</td>
</tr>
<tr>
<td>II</td>
<td>190&lt;sup&gt;(b)&lt;/sup&gt;</td>
<td>0.3&lt;sup&gt;(c)&lt;/sup&gt;</td>
<td>7053&lt;sup&gt;(d)&lt;/sup&gt;</td>
<td>5190</td>
</tr>
<tr>
<td>III</td>
<td>183</td>
<td>0.280</td>
<td>8042</td>
<td>4770</td>
</tr>
<tr>
<td>IV</td>
<td>190</td>
<td>0.3</td>
<td>8042</td>
<td>4860</td>
</tr>
</tbody>
</table>

(a) Obtained from J.F. Kalthoff [11].
(b) Taken from Ref. [10].
(c) Assumed.
(d) Calculated by ρ=E/C₀²; C₀=5190 m/sec.
<table>
<thead>
<tr>
<th>C (m/sec)</th>
<th>K^I (Kaw = 1.0)</th>
<th>(max.) W (%)</th>
<th>Number</th>
</tr>
</thead>
<tbody>
<tr>
<td>2790</td>
<td>61.0</td>
<td>28.1</td>
<td>IV</td>
</tr>
<tr>
<td>2750</td>
<td>54.8</td>
<td>28.8</td>
<td>III</td>
</tr>
<tr>
<td>2790</td>
<td>45.7 (40.5)**</td>
<td>25.6</td>
<td>II</td>
</tr>
<tr>
<td>2730</td>
<td>55.3</td>
<td>28.9</td>
<td>I</td>
</tr>
</tbody>
</table>

** Minimum K-value in this case. * Obtained for data I case.

Table 2
NO-CONTACT (if $u_1 > u_2$)

CONTACT (if $P > 0$)

PIN

WEDGE

PIN

PIN

WEDGE

PIN

PIN

Fig. 3
HIGH STRENGTH STEEL
HFX 760
$K_{IQ} = 224 \text{ MNm}^{-1.5}$

Generation Phase
Plane Stress
Material 1

- Present $K_I$ Value

--- Input Data

$(\Sigma = \Sigma(t); \mathcal{U} = \mathcal{U}(t))$

Fig. 4
HFX - 760
MATERIAL I
DATA I

- PRESENT

○ EXPERIMENT (Kalthoff et al)

\[ \frac{K_1}{K_{10}} \]

\[ \Sigma (\text{mm}) \]

Fig. 5
HFX 760
MATERIAL I, DATA I

E (Input Energy)
W
U + T + F

U (Strain Energy)

F (Fracture Energy)

T (Kinetic Energy)

Energy/Thickness (joule/mm)

0 30 60 90 120 150 180 210

0 1.0 2.0 3.0 4.0 5.0 6.0

t (μsec)

Fig. 6
HIGH STRENGTH STEEL
HFX 760

MATERIAL II

- PRESENT $K_I$ - VALUE

- INPUT DATA

Fig. 7
HFX 760
MATERIAL II
DATA I

--- PRESENT

□ EXPERIMENT (Kalthoff et al)

Fig. 8
HIGH STRENGTH STEEL
HFX 760

MATERIAL III

- PRESENT $K_1$ VALUE
- INPUT DATA

Fig. 10
HFX 760
MATERIAL III
DATA I

- PRESENT
- EXPERIMENT (Kalthoff et al.)

![Graph showing material property data for HFX 760](image)
HFX 760
MATERIAL III, DATA I

Fig. 12
HIGH STRENGTH STEEL
HFX 760
MATERIAL IV

- PRESENT $K_I$ - VALUE
- INPUT DATA

![Graph showing data points for $K_I$ and $\Sigma(t)$ over time.](image)

Fig. 13
HFX 760
MATERIAL IV
DATA I

- PRESENT

○ EXPERIMENT (Kalthoff et al)

Fig. 14
HFX 760
MATERIAL IV, DATA I

Fig. 15

Energy/Thickness (joule/mm)

W
U + T + F

U
F
T

t (µsec)

0 30 60 90 120 150 180 210

0 1.0 2.0 3.0 4.0 5.0 6.0
$E = 183 \text{ GPa}$

$\rho = 8042 \text{ Kg/m}^3$

$K_\Sigma$ (MNm$^{-1.5}$)

$t$(μsec)

$v = 0.280$

$v = 0.318$

Fig. 16
\[ \nu = 0.3 \]
\[ \rho = 8042 \text{ Kg/m}^3 \]
$E = 190 \ \text{GPa}$

$\nu = 0.3$

$\rho = 7053 \ \text{kg/m}^3$

$\rho = 8042 \ \text{kg/m}^3$

$K_x (\text{MNm}^{1.5})$

$t (\mu\text{sec})$

Fig. 13
FIXED LOADING, MATERIAL I, DATA I

\[ U_L = \bar{U}_L \]

\[ P_L \text{ (Reaction Force)} \]

\[ P_L/B \text{ (MN/m)} \]

\[ U_L, \bar{U}_L \text{ (mm)} \]

\[ t \text{ (\mu sec)} \]

Fig. 19
WEDGE LOADING, MATERIAL I, DATA 1

Fig. 21
Wedge Loading, Material I, Data 1

Crack Opening Displacement

Fig. 22
Fig. 23
WEDGE LOADING
HFX 760
MATERIAL I, DATA

Fig. 24
Results of a numerical simulation, based on an energy consistent moving singularity dynamic finite element procedure, of fast crack propagation and arrest in a high strength steel DCB specimen are presented. The influence of material properties of high strength steel on dynamic crack propagation and arrest is investigated. The influence of the loss of contact of specimen with the loading wedge is also critically examined. The present numerical results are compared with available experimental data. It is found that the present results agree well with available experimental data, and the crack arrest toughness
values obtained in the present analysis correlate well with the ratio of the maximum kinetic energy of the specimen to the input energy.