MODULARITY
IN NON-PROCEDURAL LANGUAGES
THROUGH ABSTRACT DATA TYPES

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This dissertation presents abstract data types as a means of introducing modularity in non-procedural languages. Non-procedural languages based on equational specifications have been proposed in recent years to improve programmer productivity reliability. Issues of structured programming (i.e. disciplined use of the control structure) have no meaning in the context of...
these languages because these are devoid of any control structure. Statements in a specification can be given in any order; the sequence of execution is determined after an analysis of the specification. Modularity, however, still remains an important issue in the context of these languages, as it allows specifications to be written and processed independently. Abstract data types are proposed as a means of introducing modularity. Notion of module for the specification of abstract data types is introduced and its denotational semantics is given. Nopal, a non-procedural language for the specification of testing of electrical circuits, has been chosen in which abstract data types are introduced for modularity. The abstract data types also allow specification of virtual devices in testing. An implementation of the Nopal processor is given. The Nopal processor analyzes a Nopal specification for completeness, consistency, and non-ambiguity; and generates a sequential program in Equate-Atlas corresponding to the specification. The various phases of the Nopal processor for the analysis of a specification are described. Finally, some example specifications together with their generated Equate-Atlas programs are given.
MODULARITY IN
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To Amma and Papa
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Chapter One

INTRODUCTION

1.1 MOTIVATION

The software crisis of the sixties saw the acceptance of structured programming, modularity, and top down design methodologies in building and maintaining software systems. The underlying philosophy behind these methodologies was that the software systems are complex; that they are hard to understand and difficult to manage; and to keep them within manageable limits, the discipline of structured programming should be imposed on the programmers. It reflected and still reflects the state of software technology. The requirements for systems are specified informally or semi-formally to the programming team, which then implements a system satisfying the requirements. There is a large gap between the specification language (generally, English for informal specifications) and the implementation language (Fortran, Cobol etc.), thus causing the implementation to address a lot of detail. This leads to increased complexity of software which makes the debugging and maintenance difficult. The structured programming and top down approach accepts this complexity as unavoidable, and tries to keep it under control by requiring the programmer to use simple program structures.

Continued growth in the size of the software systems, the demands of reliability and programmer productivity requires new solutions. It has led to activity in the field of, what are called, very high level languages (VHLL). These languages reduce the gap between the informal specifications and programs. Sometimes, these languages are of sufficiently high
1.1 MOTIVATION

level that the program itself is the specification satisfying the (intuitive or mental) requirements. Some of these languages, in which order of statements in programs is immaterial, are called non-procedural languages. In fact, a program in these languages is so unlike a program in procedural languages that we call it a specification.\(^1\) Many of the issues of structured programming (e.g. disciplined use of the control structure) no longer have any meaning in the context of non-procedural languages, since the specifications do not have any control structure. The details relating to the control are no longer the concern of the user, but rather, are handled by the compiler for the language.

Modularity still remains a useful and important issue for large specifications. Modularity may be defined as independence in compiling and composing of different parts of a larger specification. It is desirable because it simplifies the specification. This simplification results not only because of reduced size, but also because, with proper subdivision, the smaller specifications represent logical subunits of the larger specification. Modularity allows incremental development of a large specification. It also lends itself to easier modification. In most cases, only a few of the smaller specifications need to be changed when the needs of the specified system evolve or change.

1.2 BACKGROUND: MODEL AND NOPAL SYSTEMS

Model and Nopal are non-procedural languages developed at the University of Pennsylvania in an attempt towards a simple yet powerful very high level language. These languages have no control structure, and are based on the familiar notions of mathematics.

\(^1\) "Specification" has also been used in the literature to express the "requirements" of a system, or the set of algebraic axioms defining an abstract data type etc. Usage of the term here should not be confused with its other meanings.
The Model system [42] has been designed to automate the generation of software for data processing applications. The first step is to provide a data processing requirements. It consists of three main parts. The first part is the header, which consists of the name of the specification and names of the data bases. The second part, the data description, consists of descriptions of the structure of the source and target data in the specification. The source data corresponds to the input data, generally on sequential and indexed sequential files; the target data refers to the desired output files. The third part, a set of assertions, specifies the relations between the source and target variables. There are no control statements typical of procedural high level languages, e.g. those that deal with input/output, loop control etc.

The Model processor analyzes many aspects of the specification. It checks for ambiguities, incompleteness and inconsistencies and issues appropriate messages to the user. It also generates a number of reports which serve as the documentation for the specification. The processor then produces a sequence of execution for the assertions, with appropriate loop control statements. Finally, it produces a PL/I (or Cobol) program.

The Nopal system [46] has been designed to automate the generation of programs for automatic testing of electronic circuits. A specification in Nopal has three major parts. The first part gives the test specification, the second part the unit under test (UUT) specification, and the third part the automatic test equipment (ATE) specification. These parts can occur in any order in the specification. The test specification consists of a number of tests each of which is used to specify the stimuli to be applied, measurements to be made, computations to be performed, and diagnosis to be selected. The specification of the individual tests is non-procedural, and similarly, there is no sequence specified between the tests. The diagnoses are normally selected based on the outcome of tests. They are used to isolate faulty components and print appropriate message to that effect. The UUT and ATE
specifications are used to specify the characteristics of UUT and ATE.

The Nopal processor, similar to the Model processor, analyzes the specification for ambiguity, incompleteness and inconsistency. It too generates reports which serve as the documentation for the specification. The processor produces a sequence of execution for the tests, in the phase called inter-test sequencing. It then analyzes each of the tests individually and generates a sequence for the assertions, conjunctions, and diagnoses in the test. Finally, when all the problems are resolved it generates a program in Equate Atlas.

The issue of modularity is an important one for both the systems. At present the specification must be submitted as one unit. It leads to many of the problems mentioned in the previous section, and to some very practical problems when the processors for the language run out of address space during execution.

1.3 CONTRIBUTIONS

This dissertation examines and proposes the approach of abstract data types for modularity in these languages, and describes the implementation for the Nopal language. The following are the contributions of this work:

It has led to:

1. the definition of a scheme for modularity in non-procedural languages,

2. a novel way to define the abstract data types, namely, by means of the non-procedural specification, and

3. automatic generation of program modules that correspond to respective specification of the abstract data types.

Abstract data types provide a non-procedural way to introduce modularity. Variables in the
1.3 CONTRIBUTIONS

Specification can be declared to be of abstract type, in which case they may be operated upon by a restricted set of functions. The definition of an abstract data type along with the set of functions is given separately by means of a "module". The specification of a module is given non-procedurally, leading to the dual contributions (1) and (2).

Finally, the above ideas on modularity are used in the Nopal system. The Nopal language has been developed to generate programs for testing of electronic circuits. The abstract data type facility is used to define the devices for testing. My work on the above system has been on the development and completion of the original Nopal system [7], and implementation of the idea of abstract data types.

1.4 ORGANIZATION OF THE DISSERTATION

This dissertation is divided into six chapters. Introduction is given in this chapter, followed in Chapter 2 by a survey of past work in the fields of non-procedural languages and abstract data types.

Chapter 3 contains the use and specification of the abstract data types in a non-procedural languages independent of either Mod or Nopal. The use and specification of "modules" is described. Formal semantics of the modules is given and similarity of the module specification with algebraic axioms is shown.

In Chapter 4 the language Nopal incorporating the above ideas is described. Features of Nopal for specification of automation testing of electronic circuits are presented. Implementation of Nopal is given in Chapter 5, and the various phases of the Nopal processor are described. Examples of Nopal specifications and the reports generated by the Nopal processor are given in the Appendix.
Conclusions and ideas for future work are suggested in Chapter 6.
Chapter Two

SURVEY OF RELATED LITERATURE

2.1 SURVEY OF NON-PROCEDURAL LANGUAGES

Looking back at the development of computers we find a hierarchy of computer programming languages. The assembly level languages form the lowest level and the higher level languages such as Fortran, PL/I, Algol etc. form the next higher level. Both classes of languages are characterized as (a) procedural, and (b) domain independent. They are procedural because the individual statements are prescriptive and a program in the language consists of a sequence of such statements. These languages may be used in widely varied application areas and hence are called domain independent.

The next higher level languages are referred to as very high level languages (VHLL) and they may be sub divided into two groups. The first group consists of languages which are domain dependent e.g. Business Definition Language (BDL) [21]; the second group consists of domain independent languages with facilities to describe higher level concepts which allow the omission of many details. Examples of this group are: SETL [29] which allows manipulation of sets and relations, APL [27] which has many convenient operators for matrices, LISP [57] which works on lists etc. In the second group there are many languages that are descriptive and are devoid of any control facilities. This class of languages is referred to as non-procedural, because a “program” in these languages does not give a prescriptive sequence to be followed, but rather defines variables and their values in a sequence free manner. A “program” in these languages is so unlike that in procedural languages that we
call it by a different name: "specification", as mentioned earlier in Chapter 1.

The goal of the VHLLs is to allow the user to express his or her problem directly in these languages, thus leading to automatic programming systems which accept the specification and generate a program corresponding to it. [42]

"The ultimate expectation for automatic programming may be visualized as a user (no longer a 'programmer') making a few simple statements, to which the automatic programming system responds by spewing out a program of several hundred statements, already correct and satisfying the user's intentions."

Nonprocedural languages have been around for more than a decade ([6], [26], [47], [52], etc.) and they continue to be of current interest ([1], [4], [25], [42] etc.).

One of the early attempts by Tesler [52] defined lists and operations on lists. An important operation was PRECEDING, which was used to express the relationship of the current item in the list to the preceding item in the same list or some other list. The language was restrictive because recurrence relations between items in lists could be specified using only PRECEDING. Some of the other early languages were interpreted and hence slow in time and inefficient in memory space.

More recently, LUCID has been designed as a formal system in which programs can be written and their proofs carried out. "The proofs are easy to follow and straightforward to produce because the statements in a LUCID program are simply axioms from which proof proceeds by conventional reasoning [1]." Variables and their history of values can be defined. The history is defined as a sequence of values using the primitives FIRST and NEXT. They essentially allow the specification of one level loops. To allow nested loops, a function called LATEST is introduced. However, it clutters up the program; consequently, BEGIN-END blocks to nest iterations are included in the language.
The limitations of the LUCID language are the absence of arrays or any compound structures and the use of NEXT to define relationships between sequences of values. The latter implies that the relationships be known in advance at program writing time, and cannot be computed at run time. For example, it is not possible to specify that the current element depends on the kth previous element, where k is computed at execution time.

Non-procedural languages Model [42] [48] [50] [39] and Nopal [7] [11] [56] [46] allow relationships between array variables to be defined explicitly by means of indices. This makes the languages richer than LUCID. At the same time, they are compiled rather than interpreted. A brief introduction to them has been given in Chapter 1.

A recent proposal by Kessels [30] is to mix procedural and non-procedural approaches. In his approach, "block" is the basic structure which indicates the scopes of names, as well as the mode (non-procedural or sequential). A "valued-block" has a set of values. Besides these, there are multi-state blocks which retain information after the exit from the block. Many of these features serve to increase the complexity of the language, and make it difficult to learn and use.

A number of domain dependent systems have been proposed. Some of them are described below.

Business Definition Language [21] is a very high level domain dependent language. It is aimed at the problems of business data processing. It assumes a model of the processes involved in the manual methods used in businesses and tries to mimic those. There are three components: one for defining the business forms, one for describing the business organization, and one for writing calculations. Using a graphics screen the forms may be defined. They serve both as input and output, as well as internal representation of
2.1 SURVEY OF NON PROCEDURAL LANGUAGES

These documents can be routed to different parts of the organization or stored in files. Computations can be defined on the elements in the forms. Essentially, it is a tabular language with special constructs to represent the domain of business.

PSI system developed at Stanford [16] uses a model based approach like DDL. However, it has provision for incorporation of an independent domain expert module. Information about objects and their relationships in the domain is included in the module, thus freeing the user from defining commonly used terminology. The modules may be changed depending on the domain.

PST0YSYSTEM I has been developed by the Automatic Program Generation Group at M.I.T. [45]. It consists of two parts. The top part consists of a man machine interface, a knowledge base on business management etc. The bottom part obtains a data processing specification from the top part, performs system design, and generates PL/I code. The specification language used is SSL, which is non-procedural and resembles Model.

There are other examples of domain dependent systems, most notably, APS developed at University of Southern California at I.S.I [3], SBA [62] etc.

2.2 SURVEY OF ABSTRACT DATA TYPE SPECIFICATION TECHNIQUES

Data abstraction has been identified as a widely useful program unit by recent work in programming methodology. It has also been identified to be a unit for which formal specifications can be written easily. It can serve as a basis for modularity. Consequently, work related to data abstraction or abstract data types is reviewed here.
2.2 SURVEY OF ABSTRACT DATA TYPE SPECIFICATION TECHNIQUES

There are two approaches for giving the formal specification of abstract data types. The specification can be given either by means of an abstract model, or implicitly via descriptions of operations on the data types [35]. In following the first approach, the behaviour is actually defined by giving an abstract implementation in terms of another data abstraction or mathematical discipline. In the second approach, the class of objects is determined inductively from the operations. Usually, it is the smallest set closed under the operations.

Liskov and Zilles [35] have further classified the approaches for specification of abstract data types into five categories. The classification is based on the method used for specification, e.g.

1. use of a fixed domain of formal objects, such as sets, graphs or arrays;
2. use of an appropriate known formal domain;
3. use of a state machine model;
4. use of an implicit definition in terms of axioms; and
5. use of an implicit definition in terms of algebraic relations;

to specify abstract data types. The first two categories use the first, i.e. abstract model approach, while the remaining use the second, i.e. implicit definition approach. Some examples belonging to each of the categories are given below.

In the first category, a fixed domain of formal objects is used to provide a high level implementation of the desired abstract data type. For example, $V$-graphs were used by Earley [11] to represent instances of data structures. Operations on the data structure are specified either by expressions written in terms of primitive $V$-graph operations, or by means of pictures of $V$-graph transformations.

An appropriate known formal domain can be chosen to give the high level representation
for the abstraction. Generally, this is some established mathematical domain. Hoare has used this approach to specify sets and subsets of integers [24]. The advantage of this approach is that a body of knowledge is available about the formal domain; on the other hand, it may not be suitable for representing the abstraction.

Parnas [38] has developed a technique and notation for viewing the abstraction as states of an abstract state machine.

Use of axiomatic descriptions to specify the abstractions falls under the fourth category. The axioms define equivalence classes over the set of all expressions. If the set of axioms are well chosen, the equivalence classes are unique. The axiomatic specifications are minimal and widely applicable; however, they are deficient with respect to comprehensibility.

Recently, an algebraic specification technique based on the algebraic construction, known as "presentation", has emerged as a popular one. The algebraic axioms are easier to understand than the general axiomatic specifications, and they too are representation independent. An algebraic specification has two components: syntactic and semantic. The syntactic component gives the domains and ranges of the operations on the abstract data type. The semantic component consists of a set of algebraic axioms in the form of equations, which relate the operations to each other. An implementation may also be given for the data types. "An implementation of an abstract data type is an assignment of meaning to the values and operations in terms of the values and operations of another data type or set of data types [18]." A correct implementation must satisfy the algebraic axioms. The data types used in the implementation are also specified by means of axioms; and their implementation may again be specified if they are abstract types. The proof of the correctness of the implementation requires showing that each of the algebraic axioms for the data type is
satisfied when the implementations are substituted in the axioms. The definition of equality interpretation for the implementation is needed for the proof. A general principle used in the proof is that of data type induction. It means proving some invariant property of the data type, and involves establishing the base step and the induction step.

Goguen, Thatcher and Wagner have described an initial algebra approach to the specification, correctness, and implementation of the abstract data types. They describe a first order language (or $\Sigma$-algebra) using sorts and signature over sorts. They then define a category $C$ of $\Sigma$-algebras to consist of $\Sigma$-algebras together with all the $\Sigma$ homomorphisms. $\text{Alg}_\Sigma$ is defined as a [53]

"universe of discourse where the process of axiomatizing on the data types is going on. In particular, the free algebra in $\text{Alg}_\Sigma$ provides a language in which to write down the axioms. and their homomorphisms tell us how to interpret the axioms."

Given the above algebra, the concepts of presentation and initial algebra are introduced: it is proved that the initial algebras are isomorphic leading to the main result: "An abstract data type is the isomorphic class of an initial algebra in a category of $\Sigma$-algebras." It provides a rigorous mathematical basis for the specification techniques using axioms.

2.3 LANGUAGES SUPPORTING ABSTRACT DATA TYPES

The use of axiomatic specifications is still far from practicable. It involves fair degree of mathematical expertise to formulate the axioms and to check their consistency and completeness. Consequently, the practical languages which allow the definition of abstract data types are still based on the abstract model approach (which includes categories (1),(2), and (3)) described in the previous section.
Old language was developed at MIT [13] to support the use of abstractions in program construction. It supports three types of abstractions: procedural, control, and data. It has a mechanism called "cluster" to define the data abstraction. A cluster is used to define the representation of a data type and the set of operations which can be performed on it. The representation may be given using variables whose data types are again defined in other clusters. In such cases, references are associated with these variables, and the actual data is stored in the clusters. The only way to access or modify this data is by means of operations defined in the cluster for the appropriate abstract data type.

In the implementation, the variables which are defined to be of abstract data type actually store references to data, while the data and its representational details are given in the cluster. It does away with explicit manipulation of pointers, yet allows an efficient implementation. However, it causes a change in semantics of the traditional assignment statement. In the example:

\[
\begin{align*}
B & \quad \text{NEW}; \\
A & \quad \text{B}; \\
\text{MODIFY}(B); \\
\end{align*}
\]

the variables \(A\) and \(B\) are of some abstract type which has operations \(\text{NEW}\) and \(\text{MODIFY}\) defined in a cluster. The first statement causes \(B\) to be defined, but since the data type is defined in a cluster, \(B\) simply stores a reference to the data. In the second statement the same reference is stored in \(A\). The problem is caused by the third statement. Modification of the structure pointed to by \(B\) causes the modification of \(A\), as a side effect.

The above suggests two alternatives: either the notion that \(A\) and \(B\) are of abstract data type should be abandoned, and they should simply be declared to be of pointer type, or the semantics of the assignment statement be redefined. In CIU, the latter approach is chosen and the assignment statement is defined to mean "renaming". In the example, the second
statement will be taken to mean that A is the name of the same object as denoted by B. In a
language which is side-effect free the above problem, of course, does not arise.

Concurrent Pascal has been developed by Brinch-Hansen [5] for the writing of concurrent
programs. It allows the definition of monitors. A monitor defines a type whose instances may
be created. The data associated with an instance can be accessed using that particular
instance of the monitor. This restriction disallows recursive definition of monitors. Moreover,
operations defined in the monitor can operate on variables only in one particular instance of
the monitor. These restrictions may be justified for concurrent programming, however, the
language is not discussed any further here, due to those severe limitations.
Chapter Three
ABSTRACT DATA TYPES IN A
NONPROCEDURAL LANGUAGE

3.1 INTRODUCTION

This chapter describes modularity in a simple non-procedural programming language based on mathematical equations, through the use of abstract data types. The presentation is independent of the Model or Nopal systems, referred to previously. The objective in this Chapter is to keep the language simple so as to convey the concepts without being encumbered by details.

Section 3.2 introduces the non-procedural language. Alternative approaches to modularity are discussed in section 3.3. Use of abstract data types is described in section 3.4; and their specification using modules is given in sections 3.5, 3.6 and 3.7. Finally, the semantics of modules is given in Section 3.8, followed by a summary in Section 3.9.

In short, this chapter describes the design rationale of abstract data types for non-procedural languages based on mathematical equations.

3.2 A SIMPLE NON-PROCEDURAL LANGUAGE BASED ON EQUATIONS

A specification in a non-procedural language basically consists of two kinds of statements:
A Simple Non-Procedural Language Based on Equations

1. Declaration of variables (including arrays and structures) and their data types, and

2. Mathematical relations (also called assertions) between the variables.

A variable can take a value belonging to the set specified by its data type. The data type of a variable can either be declared explicitly or be determined from its use. It is immaterial to the specification where the variables are stored, i.e. in main memory or secondary memory.

The basic data structure in the language is the array. Variables or structures may be declared to be arrays. A sequential file is considered to be an array of records.

Assertions are essentially equations which define relationships between variables. A variable can have only one value as in mathematics. Each assertion, in fact, defines the value of a variable. The assertions can be composed by the user in any order because they specify relations, which do not have any temporal meaning associated with them.

By the use of free subscripts, a single assertion can define the value of an entire array. Identifiers corresponding to the free subscripts can be declared. The notion and use of free subscripts is similar to that in mathematics. For example, let "F" be an array variable, and "I" a free subscript, then the assertion:

\[
F(I) = \begin{cases} 
1 & \text{IF } I=1 \\
I \times F(I-1) & \text{ELSE}
\end{cases}
\]

defines the value of the entire array F. Each element of the array F is defined in terms of the previous one, except for the first element which is defined to be 1.

In the above example, the size of the array F is not specified, and hence is possibly infinite. The size can be specified in essentially two ways:

1. An upper bound can be declared for the subscript I; or

2. A special array of the same dimensions and sizes as F can be defined, which
identifies the size for the rightmost dimension of $F$. This special array is called the \textit{end array}. $F$ is defined up to the largest index such that the corresponding element in the special array is true, and all elements of lower index are false. Its use is illustrated by means of an example:

\begin{verbatim}
END.F(I) = IF I=4 THEN TRUE ELSE FALSE;
\end{verbatim}

The above causes an array $F$ to be of size 4. In other words, an array variable $F$ is defined for as many elements until and including the first true element of END.F.

Certain rules govern the usage of subscripts. These have been designed so that the specification can be compiled rather than interpreted. A subscript can occur in one of three forms:

1. a subscript term e.g. $I$ in $F(I)$;

2. an expression of the form $(1-k)$ where $k$ is a positive integer, e.g. $(I-1)$ in $F(I-1)$; and

3. another variable or subscripted variable, e.g. $G(I)$ in $F(G(I))$.

For a subscripted variable which occurs on the left hand side of the equation, its subscripts must be in the first form. This makes the consistency analysis simpler.

The above is the essence of a non-procedural language using mathematical equations. There are many additional features in the Model language to handle file organization, and in the Nopal language for fault isolation in testing of physical systems. A processor for such a language analyzes the specifications for consistency, completeness and non-ambiguity; and if successful, generates a program in a high level language. By consistency we mean that the variables are defined only once, and by completeness that the variables are defined at least once. In the generated program, the variables should be defined before they are referenced. This analysis, which is non trivial when free subscripts are used, is described with respect to the Nopal system in Chapter 5.
3.3 APPROACHES TO MODULARITY

Need for modularity has been discussed in Chapter 1. As discussed earlier, it means sub-dividing a problem into smaller specifications, and compiling each of the specifications separately. A number of alternative approaches are possible to achieve modularity in non-procedural languages. Some of them are described below.

The simplest approach is to divide a large specification into smaller specifications which communicate through commonly named variables. The aggregate of sub-parts is exactly equivalent to the total, obtained by simply putting the sub-parts together and forming one large specification.

In a different approach, each sub-part represents a specification of a function, and these functions may be used in other sub-parts. In this approach, the functions may be specified once and used many times resulting in a more compact overall specification. A judicious choice of functions may also correspond to a decomposition of the specification at the logical or "conceptual" level.

Still another approach utilizes the idea of data abstraction. In this approach a sub-part specifies an abstract data type and the functions which are allowed to operate on variables of the data type. The data type can now be used in other sub-parts. In other words, variables in other sub-parts can be declared to be of the defined data type and be operated upon by the specified functions. This approach has the advantage similar to the functional approach, namely, that a data type specified once in a sub-part may be used many times in other sub-parts.

A procedure in a programming language accomplishes an action (or performs a sequence of steps). A procedure is used knowing "what" it accomplishes without knowing "how" it
accomplishes it, and similarly it is defined knowing "what" it is supposed to accomplish without knowing "how" it will be used. Thus the abstraction separates use from definition and introduces modularity. In a similar fashion, a data type is specified independently of its use. It represents a set of objects which satisfy certain properties, and frequently, these objects correspond to the user's problem domain, e.g. stacks, tokens, sets etc. A variable of the said data type represents one of these objects and allows us to express relationships directly among these objects in a non-procedural specification. Thus it also makes the specification closer to the terminology of the problem.

Another advantage of this approach is that the representation for the variables belonging to abstract types need not be known while writing the specification. This allows the representation of a data type to be modified without affecting its use. The representation of a data type is specified by means of a sub-part defining the data type, and can be changed by changing that sub-part alone.

In light of the above advantages, this latter approach to modularity is adopted in this dissertation. (Another motivation for choosing the latter approach is that it provides a convenient way to represent devices for testing in the Nopal system.) It should be recognized that the sub-part specifying the data type allows the functions which can operate on the data type to be clustered together. The use of this abstraction serves as the guiding principle for clustering of the functions. We hope to illustrate below that this is, indeed, a natural way to modularize non-procedural languages.
3.4 USE OF ABSTRACT DATA TYPES

Each variable in a non-procedural specification has a data type, which gives the set of its possible values. The data type of a variable can be elementary (i.e., one defined by the language e.g., real, integer, character etc.) or can be one of the abstract types.

An abstract data type must be specified non-procedurally by means of a specification called the module for that data type. Just as a variable of the elementary data type can be operated upon by the functions for the data type, e.g., functions +, -, *, / for the integers, a variable of the abstract data type can only be operated upon by the set of functions defined in the corresponding module.

Variables can occur in assertions as defined below. Assertions define the relationships between the variables. An assertion is of the form:

\[ A_1(l_1, \ldots, l_{d1}) = r(l_1, \ldots, l_{d1}, A_1, \ldots, A_n) \]

where \( A_1, \ldots, A_n \) are names of array variables, \( l_1, \ldots, l_{d1} \) are subscripts for \( d1 \) dimensional array variable \( A_1 \), and \( r \) denotes the expression formed using function symbols, subscripts and array variables.

Expressions are formed using notation familiar in mathematics. Informally:

1. An array variable followed by a list of subscript expressions is an expression, and the data type of the variable gives the set to which the value of the expression belongs.

2. A function symbol followed by expressions in parenthesis is an expression. The data types of the expressions should match the domains of the function symbol. The data type of the new expression formed is the range (as in mathematics) of the function. The expression defines a mapping from the domains to the range of the function.

3. Symbols +, -, *, / denote the functions for addition, subtraction, multiplication and division, and they may be used as infix operators. Similarly, the function if then else (cond, x, y) with three arguments can be written in its familiar form: if
cond then x else y.

Data types place restrictions on the ways in which expression can be combined to form new expressions. In particular, the data types of the arguments of a function must match the domains of the function.

There is no distinction in the use of elementary and abstract data types. The user of the language once provided with a set of data types and the functions which can be performed on them may use the given set of data types without ever knowing which are elementary and which abstract. The use of the abstract data types, therefore, does not require any new meaning to be given to variables or assertions in the nonprocedural language.

3.5 SPECIFICATION OF ABSTRACT DATA TYPES

This section introduces the concept of a module for the specification of the abstract data types. The specification of an abstract data type is independent of its use. It is specified non-procedurally within the framework of the language introduced in section 3.2. The module specification can be analysed for inconsistency, incompleteness, and ambiguity, independent of other module specifications. In particular, the variables in the module are single valued, subscripts are consistently used, and are independent of the subscripts and dimensions in other module specifications. Finally, as will be shown later, the generated program supports the use of variables of the defined abstract type in other modules.

A module consists of: (1) a header - which gives the name of the abstract data type, (2) data declarations - which give the representation for the abstract data type, and (3) module functions (modfuns for short) - which specify the functions which can operate on the abstract data type being specified by the module. The function specification consists of
assertions, including formal parameters and return value.

A module named say ADT, specifies a representation for an abstract data type ADT. By representation is meant the components of a data type. The word "representation", rather than the word "data structure", is used because the components themselves can be abstract, in which case they are specified by means of other modules. A modfun may return a value of type ADT, in which case the value is defined by defining the value of variables in the representation. This is done by means of assertions in the body of the modfun. If the value is specified using the formal parameters of the modfun, then the modfun specifies the relationship between the formal parameters and the value returned. If one of the parameters is of type ADT, its representation is accessible in the module ADT and can be used in defining the return value.

In general, the return value of a modfun may be of any arbitrary data type. Appropriate function must be used to define the return value.

3.6 AN EXAMPLE - STACK

The ideas presented in the previous section are illustrated by means of an example in this section. The syntax of assertions has already been explained; the syntax of the declarations is somewhat like Pascal and PL/I. The subscripts are declared by means of a statement of the form:

<subs> IS A SUBSCRIPT;

where <subs> is the name of the subscript.

The example chosen is stack of integers. It has four modfuns. Their domains and range are:
3.6 AN EXAMPLE - STACK

Emptystack: \( \rightarrow \text{stack} \)
Push: \( \text{stack} \times \text{integer} \rightarrow \text{stack} \)
Pop: \( \text{stack} \rightarrow \text{stack} \)
Top: \( \text{stack} \rightarrow \text{integer} \)

The \textit{emptystack} maps from null domain to an empty stack; \textit{Push} maps a stack \( S \) and integer \( X \) to a stack whose top element is \( X \) and the remaining part is the same as stack \( S \); \textit{Pop} maps a stack \( S \) to another stack which is the same as \( S \) except with the top element removed; and \textit{Top} maps a stack \( S \) to an integer \( X \) such that \( X \) is the same as the top element of \( S \).

The above is an informal description of stack in English. The module \textsc{STACK} gives the formal specification of stack and its functions. The specification captures the concept expressed informally above and makes it precise. (The formal semantics of the module is discussed in Section 3.8.)

Consider the following example having an array \( A \) of stacks. Each of the elements of the array \( A \) is a stack onto which integers from arrays \( P \) and \( Q \) are pushed.

\begin{verbatim}
MAIN EX1:
  DCL A:STACK ARRAY(10),
  P, Q: INTEGER ARRAY (10);
  R: BOOLEAN ARRAY (10);
  I IS A SUBSCRIPT;
  A(I) = IF I=1 THEN EMPTystack
    ELSE IF R(I) THEN PUSH(A(I-1),P(I-1));
    ELSE PUSH(A(I-1),Q(I-1));
/* ARRAYS P, Q, R ARE ASSUMED TO BE DEFINED ALREADY. */
END EX1;
\end{verbatim}

The \textsc{STACK} module is:
3.6 AN EXAMPLE - STACK

MODULE STACK;
DCL 1 STACK: RECORD,
2 TOPZ: INTEGER,
2 Z: INTEGER ARRAY(100);
J IS A SUBSCRIPT;

MODFUN PUSH(S:STACK, X:INTEGER) RETURNS (S1:STACK);
S1.TOPZ = S.TOPZ + 1;
S1.Z(J) = IF J<=S.TOPZ THEN S.Z(J) ELSE X;
END S1.Z(J) = (J=S1.TOPZ)
END;

MODFUN POP(S:STACK) RETURNS (S1:STACK);
S1.TOPZ = S.TOPZ-1;
S1.Z(J) = S.Z(J);
END S1.Z(J) = (J=S1.TOPZ);
END;

MODFUN TOP(S:STACK) RETURNS (X:INTEGER);
X=S.Z(S.TOPZ);
END;

MODFUN EMPTYSTACK RETURNS (S1:STACK);
S1.TOPZ=0;
END;
END STACK;

In the above example, representation for a stack consists of two components: a 100 element integer array called Z, and an integer TOPZ. The familiar notation of record (as in PL/I, Pascal etc.) is used to show the components of stack. Variables S1 and S which occur in the modfuns are of data type stack. Outside the STACK module the two components of stack are not visible, however, inside the module the variables S and S1 are seen to consist of two components. To refer to their components qualified names are used, e.g. S1.TOPZ refers to a component of stack S1, while S.TOPZ refers to that of stack S.

The STACK module can be analysed for consistency independent of the use of stack data type. The modfuns PUSH and POP define a stack by defining the value of its components which satisfy certain relationship with components of another stack. For example, the modfun PUSH defines the value of a stack S1 in terms of stack S and integer X, which are the
3.6 AN EXAMPLE: STACK

formal parameters of PUSH. The two components, Z and TOPZ, of the stack S1 are defined in terms of the components of the stack S and integer X. EMPTYSTACK defines a stack which satisfies certain properties independent of any other stack; TOP defines an integer with respect to the stack S, which is again a formal parameter.

The definition of the array of stacks, A, in the main module does not require knowledge of the representation of stack. It can be analysed for consistency independent of the module STACK.

3.7 RECURSIVE DEFINITIONS

Modules can be used to define data types whose representation is specified recursively. For an abstract data type, say ADT, its representation can be specified in terms of variables which themselves can be of type ADT. Modfuns can now be applied to these variables recursively to define their values.

The recursive data types are illustrated below by means of an example. Stack of stacks data types (SOS for short) is chosen to show the similarity with the previous stack example. The specification of SOS is same as that for STACK except that the data type of the array Z in the representation of SOS is of type SOS instead of INTEGER.
3.7 RECURSIVE DEFINITIONS

MAIN EX2;
  DCL S,T: SOS ARRAY(100);

S(I) = IF I=1 THEN PUSH(S(EMPTY,SOS, EMPTYSOS))
  ELSE PUSH(S(I-1), EMPTYSOS);
T(I) = IF I=1 THEN PUSH(S(EMPTYSOS, S(I)),
  ELSE PUSH(T(I-1), S(I));

END EX2;

Figure 3-1: EXAMPLE EX2: USING STACK OF STACKS
Stack of stacks (SOS), as defined above, is not very useful because it cannot handle a stack of integers. A SOS can only contain other SOS's. The difficulty arises because the data type of Z, a component of SOS, is restricted to be of data type SOS; hence it does not allow a stack of integers to be part of SOS. There are a number of ways of dealing with the problem, e.g. parameterized modules, disjoint union of data types etc. explained below. A particularly elegant method is by using parameterized modules.

A general or parameterized module defines a class of data types. Different values of the parameter of the module result in different members of the class of data types. The SOS example is rewritten using generic module. A single module defines stack of integers, stack of characters, stack of stacks etc. depending on the value of the parameter.

STK specifies a parameterized stack. Its parameter is a data type which determines the
components which a given STK can have. For example, S is declared to be an array of stacks of integers i.e. each of the element of the array S is a stack and can contain integers. Similarly, T is an array of stack of stacks. At the time of declaration of variables of data type STK, the parameter of STK must be specified.

```
MAIN EX3;
  DCL S: STK[INTEGER] ARRAY(100),
    T: STK[STK] ARRAY(100);

  S(I) = PUSHSTK(EMPTYSTK(INTEGER), I);
  T(I) = IF I=1 THEN PUSHSTK(EMPTYSTK(STK), S(1)),
        ELSE PUSHSTK(T(I-1),S(I));
END EX3;
```

Figure 3-2 illustrates the various stacks in EX3, by means of a picture.
3.7 RECURSIVE DEFINITIONS

MODULE STK[U: TYPE];
  DCL 1 STK: RECORD,
       2 TOPZ: INTEGER,
       2 Z: U ARRAY(100);
  J IS A SUBSCRIPT;
MODFUN  PUSHSTK(S:STK[V], X:V) RETURNS (S1:STK[V]);
  S1.TOPZ = S.TOPZ + 1;
  S1.Z(J) = IF (J <= S.TOPZ) THEN S.Z(J)
             ELSE X;
  END.S1.Z(J) = (J = S1.TOPZ);
END;

MODFUN  POPSTK(S:STK[V]) RETURNS (S1:STK[V]);
  S1.TOPZ = S.TOP - 1;
  S1.Z(J) = S.Z(J);
  END.S1.Z(J) = (J = S1.TOPZ);
END;

MODFUN  TOPSTK(S:STK[V]) RETURNS (X:V),
  X = S.Z(S.TOPZ);
END;

MODFUN  EMPTYSTK(V: TYPE) RETURNS (S1:STK[V]);
  S1.TOPZ = 0;
END;
END STK;

The construct of disjoint union also allows a single module to define a class of data types. A variable is said to be of disjoint union of data types X and Y, if the variable can take a value denoted by either of the data types, and there is a way to distinguish whether its value is of data type X or data type Y. Part of SOS example is rewritten below to illustrate the idea. In the example, a tag field is associated with the SOS record, which indicates one of two possible choices in the variant part of the record. Thus depending on the tag field, it represents a stack of integers or stack of stacks. (It is assumed that TYPE OF STACK is a data type defined to be a set consisting of two keywords INTEGER and SOS. CASE has similar meaning as in Pascal.) Accordingly, the data type of the parameter X in the function PUSHSTK is of type SOS or INTEGER.
MODULE STK;

DCL 1 STK: RECORD,
  CASE TAG: TYPE-OF-STACK OF
  INT: 2 TOPZI: INTEGER,
       2 ZI: INTEGER ARRAY(100),
    SOS: 2 TOPZS: INTEGER,
       2 ZS: STK ARRAY(100);
  J IS A SUBSCRIPT;

MODFUN PUSHSTK(S:STK, X:CASE(STK,INTEGER)) RETURNS(S1:STK); CASE S.TAG OF
  INT: S1.TOPZI = S.TOPZI + 1;
   S1.ZI(J) = IF (J <= S.TOPZI) THEN S.ZI(J)
                 ELSE X;
   END.S1.ZI(J) = (J = S1.TOPZI);
  SOS: S1.TOPZS = S.TOPZS + 1;
   S1.ZS(J) = IF (J <= S.TOPZS) THEN S.ZS(J)
                 ELSE X;
   END.S1.ZS(J) = (J = S1.TOPZS);

END;

END STK;

Unlike the parameterized module, the class of stacks that STK specifies is limited to those explicitly defined in the module, e.g. in the above example it is limited to two INTEGER and STK. In case of the parameterized module, the class of stacks specified by STK is left open in the specification.

Disjoint union and parameterization are not included while defining the semantics of modules to keep the treatment simple. Parameterized modules (or disjoint union) can always be replaced by a number of different modules, each corresponding to a different value of the parameter (or a different data type in the union).
3.8 SEMANTICS OF MODULES

This section defines the denotational semantics or the fix point semantics of the modules. The denotational approach has been chosen because the semantics so defined is independent of the computation rules (or the interpreter) used to evaluate the modules. This may be contrasted with the operational or axiomatic approach, in which the semantics is defined in terms of the interpreter. The denotational approach is particularly suited for non-procedural languages, because these languages are independent of the sequence of control of the statements. The denotational semantics of modules shows two things: (1) the module defines a set of functions, and (2) the functions can be computed.

The equations and arrays in the specification are considered as partially defined recursive functions. This allows us to translate our notation into the standard recursive function equations, and use the results regarding least fix point already known in that domain.

Some of the important definitions used in denotational semantics are described here. Partial ordering "\(\leq\)" on every extended domain \(D^+ = D \cup \{\bot\}\), where \(\bot\) stands for the undefined value, corresponds to the notion of less defined than or equal to. It is defined as:

\[
\bot \leq d, \text{ and } d \leq d \text{ } \forall d \in D^+
\]

A function \(I\) is said to be monotonic if:

\[
x \leq y \Rightarrow I(x) \leq I(y) \forall x, y \in D^+
\]

Starting with these basic definitions semantics for recursive equations is defined (Chap. 5 in [37]).

First, the semantics of equational specification (Section 3.2) is presented. It is based on [40]. Later, it is extended to give semantics to modules. It is also shown that a module specification defines a set of algebraic axioms satisfied by the abstract data type.
An equational specification, introduced informally in Section 3.2, for the array symbols $A_1$, ...
 $A_n$ of dimensionalities $d_1$, ..., $d_n$, and data types $T_1$, ..., $T_n$, respectively, is a system of
equations:

$$A_1(l_1, ..., l_{d_1}) = \tau_1(l_1, ..., l_{d_1}, A_1, ..., A_n)$$

$$\vdots$$

$$A_n(l_1, ..., l_{d_n}) = \tau_n(l_1, ..., l_{d_n}, A_1, ..., A_n)$$

The terms $\tau_i(l_1, ..., l_{d_i}, A_1, ..., A_n)$ for $i = 1$ to $n$ are defined recursively as follows:

Letters $f_1, f_2, \ldots$ are used to denote functions over array values, and $g_1, g_2, \ldots$ are used to
denote integer valued functions used as subscripts. A subscript is defined as follows:

1. $l_k$ is a subscript. Its appearance in $\tau_i$ satisfies $k \leq d_i$.
2. $l_k c$ is a subscript, where $c$ is an interpreted integer constant.
3. If $J_1, \ldots, J_m$ are subscripts, then so is $g_i(J_1, \ldots, J_m)$.

A term is defined as:

1. If $J_1, \ldots, J_n$ are subscripts, then $A(J_1, \ldots, J_n)$ is a term of
data type $T_i$.
2. If $t_1, \ldots, t_m$ (terms of data types $S_1, \ldots, S_m$ respectively, then $f_i(t_1, \ldots, t_m)$ is a term
of data type $S_i$ (where occurrence of the symbol $f_i$ is always followed by terms of
the data types $S_1, \ldots, S_m$).

An interpretation for a specification consists of:

1. domains $D_1, \ldots, D_i$, over which the elements of array vary, and let $D = \{D_1, \ldots, D_i\}$;
2. a one to one onto mapping $M$ such that: $M(x) = D_i$, where $x$ is a data type, and $D_i \in D$;
3. an assignment of concrete functions to the symbols $\{f_i\}$, i.e. $M[f_i] : D_1 \times D_2 \times \ldots \times D_m \rightarrow D_i$, where $m$ is the arity of $f_i$, $S_j$ the data type for the $j^{th}$ argument of the
function satisfies the relation $M(S_j) = D_j$, and similarly the data type for the range
of the function satisfies $M(S_i) = D_i$, where $D_i \in D$ for $1 \leq i \leq m$, $D_i \in D$, and
4. an assignment of concrete natural number functions to the symbols \( \{g_i\}\) i.e. \( l[g_i]_i \)
\((Z^*)^d_i \rightarrow Z^*\), where \(d_i\) is the arity of \(g_i\),

where \(D_i^*\) is the extended domain, \(D_i^* = D_i \cup \{\bot\}\); and \(Z^*\) is the extended domain of natural numbers, \(Z^* = Z \cup \{\bot\}\), where \(\bot\) stands for undefined value. Moreover, \(f_i\) and \(g_i\) are restricted to be monotonic in the sense of partial ordering.

Least fix point semantics is adopted to give a meaning to the specification. Thus, the solution to a given set of equations is taken to be the least fix point solution. Each of the \(A_i\) is specified as a partial function, \(A_i: Z^{d_i} \rightarrow D_i\). Monotonicity of functions \(f_1, f_2, \ldots, g_1, g_2, \ldots\) assures that the \(\tau_i\) are continuous. Therefore, the least fix point solution exists and is unique (Thms. 5-1, 5-2 in [37]).

The semantics of module specification is presented next. A module specification consists of the declaration of the representation for the abstract data type specified by the module, and the operations which may be performed on variables of the type. Let an abstract data type called ADT be specified by a module of the same name. The modfuns specified by the module may be divided into two classes:

1. those which return a variable of data type ADT, and
2. those which return a variable of data type other than ADT.

Semantics of modfuns for each of the classes will be presented.

Representation of the abstract data type ADT, in its most general form, is given by a structure of the form:

\[
\text{dcl 1 ADT: record,} \\
\quad 2 A_1: T_1, \\
\quad \ldots \\
\quad 2 A_n: T_n.
\]
where \( A_i \)'s are the variables and \( T_i \)'s are their data types respectively. Each of the \( A_i \)'s may be arrays or simple variables. A structure declaration is given the semantics of a tuple, and therefore, the structure for ADT denotes the tuple:

\[
\langle A_1, A_2, \ldots, A_n \rangle.
\]

Note that since any of the \( T_i \)'s may in turn be of type ADT, the abstract data type, ADT, may be defined recursively.

A modfun in the module ADT which returns a variable of data type ADT is of the form:

\[
\text{MODFUN } \text{OPC}(C_1: \text{ADT}, \ldots, C_p: \text{ADT}, B_1: u_1, \ldots, B_q: u_q) \text{RETURNS}(C: \text{ADT});
\]

\[
C.A_1(l_1, \ldots, l_{d_1}) = \tau_1(l_1, \ldots, l_{d_1}, A_1, \ldots, A_n, C, B, \text{op})
\]

\[
C.A_n(l_1, \ldots, l_{d_n}) = \tau_n(l_1, \ldots, l_{d_n}, A_1, \ldots, A_n, C, B, \text{op})
\]

\[\text{END}\]

where OPC is the name of the modfun; \( C_i \)'s are the formal parameters of data type ADT; \( B_i \)'s are formal parameters of data types \( u_i \)'s respectively where none of the \( u_i \)'s is ADT; and \( \tau_i \)'s represent expressions. \( C \) is used to denote \( C_1, C_2, \ldots, C_p \); \( B \) to denote \( B_1, B_2, \ldots, B_q \); and \( \text{op} \) to denote the modfun in the module. \( A_i \)'s are array symbols and are components of the tuple of ADT, defined earlier. The \( d_i \)'s give the arities of the corresponding \( A_i \)'s, and \( l_i \)'s are the subscripts of the respective \( A_i \)'s, where \( 1 \leq i \leq d_i \).

The expressions \( \tau_i \)'s can now be defined as below. Letters \( l_1, l_2, \ldots \) are used to denote functions over array values; and \( g_1, g_2, \ldots \) are used to denote integer valued functions used as subscripts. A subscript is defined as follows:

1. \( l_i \) is a subscript. Its appearance in \( \tau_i \) satisfies \( k \leq d_i \).

2. \( l_i - c \) is a subscript, where \( c \) is an interpreted integer constant.

3. If \( J_1, \ldots, J_n \) are subscripts, so is \( g_i(J_1, \ldots, J_n) \).
A term is defined as:

1. If $J_1, \ldots, J_{q_d}$ are subscripts, then $C_{J_1}A_{J_1}(J_1, \ldots, J_{q_d})$ is a term of data type $T_i$ where $j$ satisfies $1 \leq j \leq p$, and $i$ satisfies $1 \leq i \leq n$.

2. $B_i(l_1, \ldots, l_{q_i})$ is a term of data type $u_i$, where $1 \leq i \leq q$.

3. If $t_1, \ldots, t_{m}$ are terms of data types $S_{t_1}, \ldots, S_{t_m}$ respectively, then $f_i(t_1, \ldots, t_m)$ is a term of data type $S_{t_i}$ where occurrence of $f_i$ is always followed by terms of data types $S_{t_1}, \ldots, S_{t_m}$.

4. Same as (3) with the symbol $f$ replaced by $op$, where $op \in op$, and $S_{t_i}$’s replaced appropriately.

The following interpretation is given to the above set of equations.

1. a set of basic domains $D_1, \ldots, D_r$ including domain $Z$ of the set of positive integers, and let $D_{tot} = \{D_1, \ldots, D_r, D\}$, where set $D$ is defined by the module;

2. for each of the data types $T_i$’s, $u_i$’s and ADT define a one-to-one onto mapping $M$ such that:

   \[
   M(ADT) = D \\
   M(x) = d \text{ where } x \in \{T_1, \ldots, T_n, u_1, \ldots, u_q\} \\
   \text{and } d \in \{D_{tot}, D\}
   \]

3. for each symbol $f_i$ of arity $d_i$ assign a concrete function:

   \[
   f_i: D_{i_1} \times \ldots \times D_{i_{d_i}} \rightarrow D_i \\
   \text{where } D_i \in D_{tot} \\
   \text{and } \forall k, D_{ik} \in D_{tot}
   \]

   where $S_{t_i}$, the data type for the $j^{th}$ argument of the function $f_i$ satisfies $M(S_{t_i}) = D_{i_j}$, and $S_{t_i}$, the data type for the range of the function satisfies $M(S_{t_i}) = D_i$;

4. for each symbol $g_i$ of arity $d_i$ assign a concrete number theoretic function:

   \[
   g_i: (Z^*)^{d_i} \rightarrow Z^*;
   \]

5. a set of projection functions $P_i$’s such that

   \[
   \langle A_1, \ldots, A_n \rangle A_i = P_i(\langle A_1, \ldots, A_n \rangle) \\
   \text{and with subscripts and symbol } C_i \text{ for the tuple } \langle l_1, \ldots, l_{d_i} \rangle
   \]

   \[
   C_i A_i(l_1, \ldots, l_{d_i}) = P_i(C_i)(l_1, \ldots, l_{d_i})
   \]
3.8 SEMANTICS OF MODULES

for $1 \leq j \leq p$
and $1 \leq i \leq n$;

6. a set of functions $OPC_1, \ldots, OPC_n$ (instead of the multi-valued function $OPC$)
defined as follows:

\[
OPC_1(C, B, l_1, \ldots, l_{d_1}) = C.A(l_1, \ldots, l_{d_1})
\]

\[
\vdots
\]

\[
OPC_n(C, B, l_1, \ldots, l_{d_n}) = C.A(l_1, \ldots, l_{d_n})
\]

where $C$ and $B$ are the formal parameters of $OPC$.

With the interpretations (5) and (6) the equational specification of a module can be written
in the familiar form of recursive equations:

\[
OPC_1(C, B, l_1, \ldots, l_{d_1}) = \tau_1(l_1, \ldots, l_{d_1}, P, C, B, op)
\]

\[
\vdots
\]

\[
OPC_n(C, B, l_1, \ldots, l_{d_n}) = \tau_n(l_1, \ldots, l_{d_n}, P, C, B, op)
\]

where $op$ is the set of operations with proper substitutions. (For example, $OPC \circ op$ is written
as the tuple $<OPC_1, \ldots, OPC_n>$) $P$ represents $P_1, \ldots, P_n$.

For each of the modfuns of class 1, i.e. those which return a value of data type ADT, a
similar set of recursive equations can be written.

For each of the modfuns of class 2, i.e. those which return a value of data type other than
ADT, a similar but simpler set of recursive equations can be written. A modfun belonging to
the second class is of the form:

\[
MODFUN OPD(C_1:ADT, \ldots, C_p:ADT, B_1:u_1, \ldots, B_q:u_q) \text{RETURNS}(E:u)
\]

\[
E(l_1, \ldots, l_{d_1}) = \tau_1(l_1, \ldots, l_{d_1}, A_1, \ldots, A_n, C, B, op)
\]

which reduces to the recursive equation:
3.8 SEMANTICS OF MODULES

OPD(C,B,I₁,...,Iₙ) = τ(l₁,...,lₙ,P,C,B,OP)

All the recursive equations are now put together, by renaming the variables which occur as formal parameters of modfuns, to avoid clash of names.

The functions f₁,f₂,...,g₁,g₂,... are constrained to be monotonic in the sense of partial ordering. The projection functions are monotonic because:

Let Pᵢ be the iᵗʰ projection function. Now
let \( x = <x₁,...,xᵢ,...,xₙ> \)
and \( y = <y₁,...,yᵢ,...,yₙ> \)
\[
x \preceq y \Rightarrow xᵢ \preceq yᵢ \text{ for all } i, \text{ (where } \preceq \text{ stands for less defined than or equal to)}
\]
Pᵢ(x) = xᵢ
Pᵢ(y) = yᵢ
\[
x \preceq y \Rightarrow Pᵢ(x) \preceq Pᵢ(y)
\]
therefore, Pᵢ is monotonic.

Hence, τᵢ's are continuous and the least fix point solution of the recursive equations exists (Thms. 5.1, 5.2 in [37]).

The set D, which corresponds to the data type ADT, is defined inductively as follows:

1. **Base step.** For a modfun OP which returns a value of data type ADT, and none of whose formal parameters is of type ADT, the tuple defined by OP: \( <OP₁,...,OPₙ>(B) \) is a member of set D. B are the formal parameters of function OP, and OP represents a tuple of functions.

2. **Inductive step:** For a modfun OPC which returns a value of data type ADT, the tuple defined by the modfun: \( <OPC₁,...,OPCₙ>(C,B) \) is a member of set D, where C are the members of set D, and B are members of other domains (D₀ → D).

The existence of the least fix point solution assures the existence of the set D.

With the semantics of the modules defined, algebraic axioms about the abstract data types can now be proved. The proof involves substituting non-procedural equations for the occurrences of the module functions, and reducing the equations until the desired equality is obtained. This is illustrated by means of the STACK example. Note that since it does not
3.8 SEMANTICS OF MODULES

involve recursive definition of the data type the derivation is straight forward.

To prove: \( \text{POP(PUSH(S,X)}) = S \), where \( S \) is a stack, and \( X \) is an integer.

Proof:

LHS
\[
\begin{align*}
= \text{POP}(S') & \text{ where } S' \text{ is a stack and } \\
& S'.\topz = S.\topz + 1 \\
S'.z(j) & = \begin{cases} 
S.z(j) & \text{if } j \leq S.\topz \\
X & \text{if } j = S'.\topz \\
\bot & \text{otherwise} 
\end{cases} \\
S'.z(j) & = X \\
& = S'' \text{ where } S'' \text{ is a stack and } \\
& S''.\topz = S'.\topz \cdot 1 \\
S''.z(j) & = \begin{cases} 
S'.z(j) & \text{if } j \leq S'.\topz \\
\bot & \text{otherwise} 
\end{cases} \\
S''.z(j) & = S.z(j) \forall j \text{ (from Lemma 1.)} \\
S'' & = S \\
\end{align*}
\]
Q.E.D.

Lemma 1: \( \forall S \in \text{STACK}, S.z(j) = \bot \text{ for } J > S.\topz \)

Proof: Since the stacks can only be defined by the modfuns in the module STACK, the
proof follows from induction:

Base step: Follows from the definition of the EMPTystack.
3.8 SEMANTICS OF MODULES

Induction step: Let $S$ be a stack satisfying the proposition of the Lemma.

Claim: The stacks $\text{POP}(S,X)$ and $\text{PUSH}(S,X)$ also satisfy the lemma.

Proof:

1. Let $S' = \text{POP}(S,X)$
   
   $S'.Z(J) = \bot$ for $J > (S.\text{TOPZ} - 1)$
   
   $= \bot$ for $j > S'.\text{TOPZ}$

2. Let $S' = \text{PUSH}(S,X)$
   
   $S'.Z(J) = \bot$ for $J > S'.\text{TOPZ}$

Q.E.D.

3.9 SUMMARY

This chapter introduces a non-procedural language based on equations. Use of abstract data types has been proposed as a means to introduce modularity in the non-procedural language. It has been argued that the use of abstract data types is consistent with the philosophy of non-proceduralness, and leads to modular specifications.

The notion of "module" has been introduced to allow specification of the abstract data types. It allows the definition of the representation of the abstract data types, and the specification of the functions which can operate on it. These functions are specified non-procedurally by means of equations.

Finally, the denotational semantics of the modules is defined. It is shown that an abstract data type defined by a module is a well defined set. It is also illustrated that the axioms satisfied by the abstract data types can be derived from the equational specification.
4.1 OVERVIEW OF THE NOPAL LANGUAGE

Nopal is a descriptive language used to write specifications for the programming of automatic test systems. It can be used for testing of electronic circuits, mechanical systems, chemical processes etc. It also has the capability to perform general purpose computational tasks.

Basic statements in Nopal are assertions and data declarations similar to those described in Chapter 3. However, Nopal has additional constructs which are superimposed on the assertions and data declarations. These additional features facilitate the specification of testing. The most important construct is that of a test. A test section consists of a specification of a physical test. Outcome of the test, i.e. passing or failing the test, determines fault isolation. There are also sections to describe the UUT (Unit Under Test) and the ATE (Automatic Test Equipment). These sections are needed to check consistency of interfaces with the UUT and ATE.

Several features of Nopal are extremly important in providing ease of use. First, the language is non-procedural. The user saves effort because the execution order of events or control logic need not be specified. Second, the specification can be divided into sub-parts, the modules. Each of the modules can be specified and processed by the language processor independently. This is the essence of modularity of a specification. Third, each of the modules may be further divided into data declarations and functions. The functions are
divided into tests, diagnoses and messages. Each test has subparts: stimulus, measurement and logic. All these correspond to notions which occur in testing. Fourth, the language allows incremental development of specification. Tests can be added to a specification without changing the tests already specified.

The Nopal system produces a number of reports which serve as the documentation for the specification. It also enhances the user-system interaction, and helps the user in locating errors in the specification.

In this chapter, the Nopal language is described informally with examples. A more detailed explanation including the formal syntax is given in [46].

A Nopal specification gives a complete description of the desired tests specific to a given UUT and ATE. In general, a Nopal specification consists of a collection of modules. One of the modules is called the main module and it consists of the tests on a given UUT with an ATE. Communication between the modules is by means of abstract data types. A module (except the main module) represents an abstract data type which can be used by other modules.

A module specification includes the data representation for an abstract data type together with the functions (called module functions or modfuns for short) which can operate on the variables of the abstract type (also called abstract variables for short). An abstract data type that has been specified by means of a module can be used in any of the modules. The abstract variables are defined and operated upon by means of the modfuns specified in the module.

The modules are specified non-procedurally. For organizational purposes each module can be divided into four major sections, which can be given in any order. They are:

1. Data declaration specification,
4.1 OVERVIEW OF THE NOPAL LANGUAGE

2. Modfun specification,
3. UUT specification, and
4. ATE specification.

Each of the four sections are explained briefly below, followed by a more detailed description later.

The data declaration specification provides the data types of the variables and the data structure used in the specification.

The modfun specification describes the mapping between the input and the output parameters of the modfun. The main module has only one (implicit) modfun, while the other modules may have more than one. Each modfun consists of tests, diagnoses and messages. The tests may be further sub-divided into stimuli, measurements and logic. A test corresponds to the notion of a physical test on the UUT, i.e. application of stimuli, taking of measurements and selection of diagnoses, based on the results of the test as expressed in the logic part. The diagnoses report of the test consists of messages that typically identify the faults in the UUT.

The UUT specification gives the description of failure modes, connection points etc. of the UUT. This description is cross checked by the language processor for consistency within the module.

The ATE specification provides the description of the functions used in the module. These functions can be used for application of stimuli, taking of measurements, or for computations. These functions must be specified outside the module. They can be either part of a library of functions, or they can be specified as modfun by other modules. The ATE specification gives the function parameters and their data types. In other words, it gives the specification of the interface with the rest of the modules and with ATE.
4.2 DATA DECLARATION SPECIFICATION

The data declaration specification allows the user to declare the data types of variables. The data type of a variable specifies the set to which (the value of) the variable must belong, and the operations which can be performed on it.

Data types can be either elementary, e.g. real, integer, or character or they can be abstract, in which case they must be specified by means of modules.

Data declarations include specification of the structure of the data. The two basic structuring methods are: (1) arrays, and (2) structures. An array is a homogeneous structure of elements, all of which are of the same data type. A structure, on the other hand may consist of components of different types which are grouped together. The components themselves can be arrays or structures, thus permitting structures of arbitrary complexity to be declared.

A structure may be viewed as a tree. The root of a tree represents the entire structure, and its descendants correspond to the components of the structure. Finally, the leaves of the tree correspond to the individual variables in the structure. Below are some examples of declarations of variables:

```
DCL  A, B, X : INTEGER;
DCL  Y, Z : STACK ARRAY (10);
DCL  P : GROUP ARRAY (5),
     2 Q : GROUP ARRAY (*),
     3 R : INTEGER,
     3 S : REAL;
```

In the first statement, variables A, B and X are declared to be of type integer; in the second, Y and Z are declared to be one dimensional arrays of size 10, and data type stack, and in the third, a three level tree structure is declared. In the tree structure the root is the variable P having the descendant Q which has variables R and S. P is an array of five elements and Q an array of size which is to be specified elsewhere.
A declared structure is implied to be on secondary storage if the data type of the root node is FILE. Name of the root node, in that case, gives the name of a file and the structure declaration gives the structure of the file. In other words, the declared structure represents a file, and is called a file structure. For example:

```
DCL 1 F: FILE,
    2 P: GROUP ARRAY (*),
    3 Q: RECORD ARRAY (10),
    4 R: INTEGER,
    4 S: REAL,
    3 Q1: RECORD ARRAY (5),
    4 R1: CHAR;
```

A file F is declared to contain an array P of indefinite size. Each element of P contains 10 Q’s and 5 Q1’s.

A file structure is considered by the system to be input if all the fields (i.e., leaves) of the structure are not defined in the specification, and output otherwise. The non-leaf nodes of a file structure can be of type RECORD or GROUP. A non-leaf node which corresponds to a unit of input/output on the secondary storage is declared as a RECORD, and GROUP otherwise.

Variables in an input file structure are defined in the generated program by means of a special function called ACCESS. Calls on this function are generated at appropriate places in the generated program for the specification. SAVE function is the exact dual of above for an output file structure. Use of ACCESS and SAVE function is implicit and need not be specified by the user.

For ISAM files, a key is represented by a variable name which is the name of the record prefixed by “PTR ”. For example, an instance of a record named “Z” in an ISAM file can be defined by means of its key “PTR.Z”. The value of the key is passed as a parameter to the ACCESS and SAVE function.
The notion of file structure has been generalized to abstract structures in NOPAL. An input or output structure can be declared to be of abstract type by specifying the data type of the root node as abstract (instead of the keywords RECORD, GROUP or FILE). An example of an abstract structure is:

```
DCL P: AT1 ARRAY (*),
   Q: INTEGER,
   R: REAL;
```

in which a structure P is declared to be of abstract type AT1.

An abstract structure is considered input if the value of all its fields is not defined in the specification, and output otherwise. Value of input abstract structures is defined in the generated program by means of function named: "ACCESS," suffixed by the name of the abstract data type. In the previous example, if the structure P is input, its value would be defined by ACCESS(AT1). The ACCESS function for an abstract data type must be specified in its module. Calls to this function are generated at appropriate places in the generated program. An exact dual of the above is the SAVE function for output abstract structures.

Abstract structures allow convenient representation of those files whose physical organization is different from that specified in the main module.

Parameters can be associated with ACCESS and SAVE functions associated with abstract structures. The use of parameters provides a means of communication between the main module and the module which defines the abstract structure. It allows the use of abstract structures to represent testing devices as well. For example, a device which measures ratio of two voltages on two ports can simply be declared as:
The function ACCESS,GAIN,DEVICE in the module GAIN,DEVICE can give the specification for the appropriate measurements. Thus, each value of the variable GAIN defined by means of the ACCESS function represents a different measurement. Information relating to the ports and ranges can be passed as parameters.

The parameters are specified by a syntax similar to that used for specifying key for ISAM files. In the example above, the parameters of the abstract record GD are given by means of variables named PTR1,GD, PTR2,GD, etc.

4.3 MODFUN SPECIFICATION

This section describes the specification of the module functions (modfuns). Each modfun, like a mathematical function, specifies a mapping from its domain to the ranges. A modfun has zero or more parameters. Parameters are called source parameters if their value is defined outside the modfun, and are called target parameters if they are defined in the body of the modfun. A modfun can return a value by means of its target parameters or explicitly as in programming or mathematics. The data types of the source parameters are the domains, the data types of the target parameters and explicitly returned value are the ranges of the mapping specified by a modfun.

The main module has only one implicit modfun; the other modules normally contain more than one modfun. A modfun has four parts:

1. header,
2. test specification,
3. diagnoses, and
4. messages.
4.3 MODFUN SPECIFICATION

The header must be the first statement, after which the tests, diagnoses and messages may occur in any order.

4.3.1 HEADER

Each modfun starts with a header consisting of the keyword MODFUN followed by the name of the modfun, the list of formal parameters and their data types, and the data type of the value explicitly returned by the modfun. It also states which of the parameters are source and which are target. In effect, the header defines the interface with the other modules which use the modfun.

For example, the following header:

```
MODFUN PUSH (S0:S STACK, X:S INTEGER)
RETURNS (S1:STACK);
```

defines a function called PUSH which has two source parameters S0 and X, and it returns a value S1, explicitly. The data type of S0 and S1 are STACK, and the data type of X is INTEGER. Consequently, PUSH specifies a mapping from its domains of STACK and INTEGER to its range STACK.

4.3.2 TEST SPECIFICATION

The test specification consists of a collection of tests. As mentioned earlier, tests correspond to the idea of a physical test on a UUT. A test consists of three parts: 1) stimuli that are to be applied to the UUT at the test time, 2) measurements that need to be taken and conditions that must be met, and 3) logic to select the diagnoses based on the result of passing or failing the test.

Stimuli and measurements both optionally contain two parts: a conjunction and a set of assertions (Generic word, waveform, is used to refer to either a conjunction or an assertion).
4.3.2 TEST SPECIFICATION

A conjunction in stimuli specifies the simultaneous application of stimuli to the UUT, while in the measurement it specifies the simultaneous measurement to be taken of the UUT. All the functions specified in conjunctions must be performed in parallel. For example, the following conjunction:

```
STIM;
CONJ: <J1,J2> = PSUPPLY (30V) &
      <J3,J4> = FSOURCE (1KHZ,10V);
```

specifies applying a power supply of 30 volts across the connecting pins J1 and J2, and applying a frequency source of 1kHz and 10 volts between pins J3 and J4.

A conjunction can also be used with an if-statement, in which case it is called an if-conjunction. An if-conjunction consists of a boolean condition followed by a conjunction after "THEN" and a conjunction after "ELSE". One of the conjunctions following the "THEN" or "ELSE" part is performed depending on the boolean condition. For example,

```
STIM;
CONJ: IF VAR<20 THEN <J1,J2> = PSUPPLY (30V)
      ELSE <J3,J4> = FSOURCE (1KHZ,10V);
```

If a variable VAR is less than 20 then the power supply and otherwise a frequency source is applied.

Conjunctions are used to specify some actions - stimuli or measurements - on the UUT. Assertions, on the other hand, are used to specify relations that must be satisfied by the variables. An assertion specifies relations between variables. It can be used in two roles: as an explicit definition of variables or to specify a condition on the variables. Variables defined in an assertion are said to be target variables of the assertion. All others variables in the assertion are called source variables of the assertion.

If an assertion does not have any target variable then it specifies a relation which is tested for truth value. An assertion evaluates to true if the specified relation is satisfied, otherwise it
evaluates to false. Assertions which have target variable(s) are always taken to evaluate to true.

The syntax of assertions is:

```
ASRT: <EXPRESSION1> <RELATIONAL OPERATOR> <EXPRESSION2>
       SOURCE: <LIST OF VARS>
       TARGET: <LIST OF VARS>
```

<expression1> and <expression2> are arithmetic or boolean expressions. <relational operator> is one of (=,>,<,>=,<=). <list of vars> is a list of variables with their subscript expressions, if any.

Target variables in an assertion must occur as <expression1> or as the target parameters of the function in <expression2>. Moreover, the relational operator must be "=". Examples of assertions are:

```
ASRT: A > B*SIN(30) SOURCE:A,B;
ASRT: A = B*SIN(30) TARGET:A SOURCE:B;
```

The first assertion tests for the inequality and evaluates to true or false; the second assertion, on the other hand, defines variable A and always evaluates to true.

In addition to arithmetic operators, the + - operator is used in an assertion:

```
ASRT: e1 = e2 + - e3;
```

where e1, e2, and e3 are expressions. The assertion is an abbreviation for the following relationship:

```
e2-e3 <= e1 <= e2 + e3
```

and evaluates to true provided the above relations are satisfied.

Assertions may also be used to specify a relation that must be satisfied by a target parameter of a function in a conjunction. For example, an assertion written as:
4.3.2 TEST SPECIFICATION

CONJ: \langle J_1, J_2 \rangle = \text{VOLTMETER (} \langle \text{V1} \rangle \\
\text{SOURCE : V1;}

specifies that the value of the target parameter of the function VOLTMETER must be less than V1.

If-clause can be used with assertions just as in if conjunctions. Syntax of if assertion is:

\text{ASRT: IF } \langle \text{BOOLEAN CONDITION} \rangle \text{ THEN } \langle \text{ASSERTION} \rangle \\
\text{ELSE } \langle \text{ASSERTION} \rangle \\
\text{SOURCE: } \langle \text{LIST OF VARS} \rangle \\
\text{TARGET: } \langle \text{LIST OF VARS} \rangle;

The keywords THEN and ELSE may be followed by another assertion which may again have an if-clause. This allows the if-assertion to be nested to indefinite depth. (In the present implementation, the assertion following THEN cannot have an if clause. Thus only a right recursive tree is permitted.)

The if assertion is taken to evaluate to the same boolean value as the selected assertion following THEN and ELSE. In other words, if the boolean condition in an if assertion evaluates to true then the assertion is said to evaluate to the same value as the assertion following the keyword THEN, and if the boolean condition evaluates to false, then the assertion is said to evaluate to the same value as the assertion following the keyword ELSE. If an if assertion (or if conjunction) defines some variables in its then part, it must also define exactly the same variables in its else part.

The concept of free subscript is introduced next. Its use allows entire arrays to be defined by means of one conjunction or assertion. It also allows relations to be specified between arrays. The notion and use of free subscripts is similar to that in mathematics. For example, the assertion with free subscript I:
define the values of $F(I)$ for all values of free subscript $I$. In other words, it defines the entire array $F$. Similarly, the assertion with free subscript $I$

$$\text{ASRT: } A(I) = B(I)$$

$$\text{SOURCE: } A(I), B(I);$$

specifies relation between two array variables $A$ and $B$. This assertion is taken to evaluate to true if the relation holds for all values of the subscript $I$.

Syntax for declaration of a free subscript is similar to that of an assertion. Statement containing the keyword SUBSCRIPT in the following example:

$$\text{ASRT: } I = \text{SUBSCRIPT ('A,B:2',10) TARGET: } I;$$

is used to declare a free subscript "I" for the first dimension of array variable $A$, and the second dimension of array variable $B$. The size of the respective dimensions of the variables is ten. Even though the declaration looks like an assertion it should not be confused with an assertion. It declares a subscript which takes values from 1 to 10. The list of variables and their dimensions, i.e. "A,B:2", is called parent list.

Subscripts are a powerful way to define arrays. However, certain restrictions have been placed on their use so that the specification may be analysed and an efficient program generated. Let $I$ be a free subscript. A subscript must be in one of the following forms:

1. a subscript term, e.g. $I$ in $A(I)$;

2. an expression of the form $(I*K)$, where $K$ is a positive integer; and

3. another variable or subscripted variable, e.g. $B(I)$ in $A(B(I))$, $X$ in $A(X)$.

For variables which are targets in a conjunction or in an assertion, only the first of the above three forms is permitted.
In the declaration of a subscript the upperbound may be omitted, if it is not known, and replaced by "..". For example, in the assertion:

\[ I = \text{SUBS ('F', *) TARGET:i}; \]

upper bound of a variable \( F \) is unknown. For such variables, the program generator tries to optimize memory. In particular, the program generator allocates memory for 2 elements: current and the previous. Elements corresponding to only the current (i.e. \( I \)) and the previous (i.e. \( I-1 \)) value of subscript may be referenced.

The size of an array variables with subscript \( I \), whose upper bound has been declared to be indefinite, is specified by means of a special array called END-I. Such special arrays are called end arrays. The meaning of end arrays is introduced by means of an example below:

\[ I = \text{SUBS ('F', *) TARGET:i}; \]

IF \( I=1 \) THEN \( F(I) = 1 \)
ELSE \( F(I) = I*(F-1) \)
TARGET:F(I)
SOURCE:F(I-1);

IF \( I=5 \) THEN END-I(I) = TRUE
ELSE END-I(I) = FALSE
TARGET:END-I(I);

First statement, in the example above, is declaration for a subscript \( I \). It is followed by an assertion which defines an array \( F \) in terms of itself. The second assertion defines an end array END-I whose first four elements are false and the fifth element is true. This specifies that the size of array \( F \) is equal to five. In other words, the size of \( F \) is specified to be equal to \( N \) such that for index \( N \) the value of END-I is true and for all indices less than \( N \) the value of END-I is false.

More generally, if "\( I \)" is a free subscript then END-I is a multi-dimensional array, its dimensionality being equal to the maximum dimension in the parent list in the declaration of "\( I \)". END-I defines the size of those dimensions of the array variables which are in the parent
3.2 TEST SPECIFICATION

list. For example,

\[ I = \text{SUBS} ('G:1,F',*) \quad \text{T} \quad I; \]
\[ J = \text{SUBS} ('G:2',*) \quad \text{T} \quad J; \]

the dimensionality of END_I is one and that of END_J is two. END_I defines the size of the one
dimensional array F and the first dimension of two-dimensional array G. Similarly, END_J
defines the size of the second dimension of array G.

Use of free subscripts allows an array to be defined by means of a single assertion or single
conjunction. It is important, however, for the variables (be they arrays or scalars) to be single
valued. Consequently, a conjunction or assertion which defines multiple values for arrays is
invalid. For example, the assertion:

\[ \text{ASRT: A(I) = B(I,J)} \quad \text{T} \quad A(I) \]
\[ \text{SOURCE: B(I,J)}; \]

is invalid because it defines an element of array A to be equal to an entire row (second
dimension) of array B. In general, whenever the set of free subscripts associated with a target
variable is a subset of the number of free subscripts of the source variables, it defines multiple
values for the target variable. There are two exceptions to the above rule:

1. when a source variable containing an extra free subscript occurs as an argument
   of a reduction function, and the extra free subscript is reduced; or

2. when a boolean condition precedes the assertion. A warning is issued in this case
   and it is the responsibility of the user to ensure that the target variable is single
   valued.

Example of an assertion containing a reduction function is:
ASRT : $F(I) = \text{SUM}(G(I,J),J)$
TARGET:$F(I)$
SOURCE:$G(I,J)$;

Reduction function SUM takes two dimensional array $G$ and sums the elements of the same $I$ index value, thus producing a one dimensional array $F$. The array variable $F$ is single valued even though the source variable $G$ has an extra subscript $J$. Example of the second exception is:

ASRT: IF END_I(I) THEN OUT = $F(I)$
TARGET: OUT
SOURCE: $F(I), \text{END}_I(I)$;

OUT is defined by the last element of the array $F$. However, it is the responsibility of the user to make sure that OUT is not defined by more than one element of $F$. Nopal program generator does no further analysis to check that it is indeed so.

The logic component of a test specifies the selection of diagnoses. The diagnoses are selected depending on whether the test evaluates to true or false. The test evaluates to true if all the assertions in the test evaluate to true, and false otherwise. The operators given in Table 4.1 may be specified with each of the diagnoses for their selection.

The logic component is specified by a list, each of whose elements consists of an operator followed by a diagnosis name. For example:

LOGIC : $\text{D1, D2, } \neg D6$;

4.3.3 DIAGNOSES

The diagnoses are used to report the result of the test, to isolate failure modes or to elicit a response from the user. It has five parts which can be specified in any order.

1. List of affected components and their failure modes which are isolated by this diagnosis. They may be in conjunctive or disjunctive form where the former means that all the components in the list have failed, while the latter that at least one has failed.
4.3.3 DIAGNOSES

Table 4.1: LOGIC OPERATORS IN A TEST

<table>
<thead>
<tr>
<th>OPERATOR</th>
<th>MEANING</th>
</tr>
</thead>
<tbody>
<tr>
<td>*</td>
<td>Select the diagnoses unconditionally i.e. irrespective of the outcome of the test.</td>
</tr>
<tr>
<td>/</td>
<td>Select the diagnoses if the test evaluates to true.</td>
</tr>
<tr>
<td>!</td>
<td>Select the diagnoses if the test evaluates to false.</td>
</tr>
<tr>
<td>&amp;</td>
<td>Mark the diagnoses as selected if the test evaluates to true. The diagnoses should be executed only if all other tests which use this diagnoses (with operators: &amp; or &amp;-) also mark it as selected.</td>
</tr>
<tr>
<td>&amp;-</td>
<td>Mark the diagnoses as selected if the test evaluates to false. The diagnoses is executed only if all other tests which use this diagnoses (with operators: &amp; or &amp;-) also mark it as selected.</td>
</tr>
</tbody>
</table>

2. Name of the message to be printed. The message itself is specified separately.

3. Parameters. This specifies the variables whose values must be substituted in the message at the appropriate places.

4. Operator response. It specifies the response from the operator when the generated program is executed. The program waits for a response. Response can be of three types:
   a. press PROCEED key;
   b. press Y(yes) or N(no); or
   c. enter a number.

Pressing the PROCEED key simply causes the program to continue execution. It is typically used to turn knobs and set switches manually, i.e., those which cannot
be controlled by ATE. Y or N response is typically used for asking the operator to make a binary choice. The response \( C' \) is usually used to enter reading of meters etc. manually, i.e. those which cannot be taken by ATE.

5. Time: Specifies the real time which must elapse from the start of a test, before the message is issued.

Except for the name of the message and the parameters it takes, if any, all the other parts of the diagnosis are optional.

A diagnosis specification is illustrated below:

```
DIAG D1:
    AFFECTED COMPONENTS = OPEN(RESISTOR1) | OPEN(RESISTOR2),
    PRINT = MSG1,
    PARAMETERS = V,
    TIME = 0;
```

It specifies that at least one of two resistors \( \text{RESISTOR1} \) or \( \text{RESISTOR2} \) has failed due to open circuit, and that message MSG1 with parameter V must be printed. Time 0 specifies that no time delay is necessary in issuing the message.

### 4.3.4 MESSAGE SPECIFICATION

This specification consists of the text of a message, and parameters and affected components, if any. It implies the printing of the message including the affected components and parameters.

For example, the message MSG1 of Section 4.3.3 can be specified as follows:
MESSAGE MSG1:

'ONE OF THE FOLLOWING FAILURES HAS OCCURED: (C). THE MEASURED VOLTAGE IS (P).' ;

When the above message is printed "(C)" is substituted by "OPEN (RESISTOR1)OPEN(RESISTOR2)" and "(P)" is substituted by the value of variable V.

4.4 UUT SPECIFICATION

Information relating to the UUT is specified in this section. This allows various consistency checks to be performed within the module. It is organized in two parts: (1) interconnecting points, which are used for identification of the connection points of the UUT to the ATE. (2) component failures which identify all possible faulty components with the failure modes (i.e. types of failures).

A UUT connection point defines a symbolic name for a connection point on UUT, the type of connector used, and the maximum and minimum value of the stimuli which may be applied on it. For example:

UUPT 40 : J1. CONNECTOR=(A). LIMIT=(VOLT,70,0,GND);

J1 is the name by which this connection point is referred to, its type of connector is A, and the maximum and minimum value of stimuli that may be applied with respect to the ground (GND) is 70 volts and 0 volts respectively.

In UUT component failure section, all possible faulty components and their failure modes are listed. Each component specification includes the failure mode, likelihood of the failure, and protection. Protection consists of a list of other components whose failure prohibit testing of this component. For example:
4.4 UUT SPECIFICATION

COMPONENT FAILURE 2:
RESISTOR1, FAIL=OPEN, INDEX=1, PROT=(1,11);

specifies that the component RESISTOR1 has a failure mode called OPEN, the frequency of failure is 1 (the lower the number the larger the likelihood), and that should the components 1 or 11 fail, tests for failure of this component must not be conducted.

4.5 ATESPECIFICATION

Information relating to the Automatic Test Equipment and the functions used in a module (computational, stimuli or measurement) is stated here. It has two parts: (1) ATE connection point specification, and (2) functions. ATE connection point specification consists of the names of the ATE connections points. Optionally, the specification includes identifying ATE points of the respective UUT points. In the example below:

ATEPOINT 1: ATEPT#30, UUPTS=(J1,J2);

"ATEPT # 30" may be connected to UUT points J1, J2. The checking for the UUT points has not been implemented. It is used purely as a documentation device.

Functions used for (1) stimuli, (2) measurement or (3) computational purposes, and (4) for denoting failures are declared in the ATE function specification. Functions in the first three categories are assumed to be defined either by means of other modules or by means of a library of functions. The failure functions (category (4)) are for the purpose of denoting kinds of failure. They are not functions in the sense of the earlier three categories.

Function specification has an item called TYPE which specifies which of the above 4 types does the function belong to, and items PARM and VALUE RETURNED to specify the data types of the parameters and the value to be returned. The number of pins used may also be specified if the function is of type stimuli or measurement.
For example a function PUSH

\[
\text{FUNCTION PUSH, TYPE=E, PARM=(INSTACK,S:STACK),}
\]
\[
\text{PARM=(ELEM,S,INTEGER), VALUE RETURNED=(STACK);}\]

is of type evaluation. It has two parameters, both source, with the data types STACK and INTEGER, and it returns a value of type STACK. The names INSTACK and ELEM have no significance for the specification. Their use is only for providing mnemonics.
Chapter Five

THE NOPAL PROGRAM GENERATOR

5.1 OVERVIEW OF THE PROGRAM GENERATOR

The Nopal program generator is designed to automate the program design, coding and debugging phases of program development based on a specification in the Nopal language. The program generator analyzes a Nopal module specification, issues a number of reports for the user and, if the module is error free, generates a program in the Equate-Atlas test programming language.

There are three phases in the program generation process. Phase 1 consists of syntax analysis and construction of internal data structures. Phase 2 consists of analysis of the specification for completeness, consistency and non-ambiguity, and of sequencing. In phase 3 Equate-Atlas code is generated. A number of user reports are issued by each of the phases. The three phases are described individually in Sections 5.2, 5.3 and 5.4. More detailed documentation is provided in [46].

The Nopal processor has evolved through numerous revisions over the past several years. The research reported here includes extending the original system [7] with the following capabilities:

1. Modules to provide modularity and abstract data type definition facility.

2. Recursive assertions to allow the arrays to be defined recursively.

3. Declaration of data types and data structures as well as virtual subscripts.
5.1 OVERVIEW OF THE PROGRAM GENERATOR

Figure 5.1: OVERVIEW OF NOPAL PROCESSOR

- Syntax Analysis
- Sequencing & Optimization
- Code Generation

NOPAL MODULE

NOPAL HANDLERS

EQUATE
ATLAS PROGRAM

Analysis Reports
5.1 OVERVIEW OF THE PROGRAM GENERATOR

NOPAL Specification

PHASE 1:
Syntax & Statement Analysis
Specification reports
Errors/warnings
Cross references

PHASE 2:
Specification Analysis & Sequencing
Errors/warnings
Precedence Matrix
Flowchart report

PHASE 3:
Code Generation
Code generation report
Program listing

Program

Figure 5-2: MAJOR PHASES OF NOPAL PROCESSOR
5.1 OVERVIEW OF THE PROGRAM GENERATOR

4. Input output from secondary storage.

5. Virtual subscripts for efficient utilization of memory.

These extensions entailed modifying some parts of the original system and completely rewriting other parts. In particular, the scheduling algorithm was completely rewritten to handle recursive assertions and input/output from secondary storage. It is described in Section 5.3.2.

The code generator was not implemented in the original system [7] but completed later [55]. The Nopal system was demonstrated on an actual Equate Atlas machine [15].

5.2 SYNTAX ANALYSIS AND THE ASSOCIATIVE MEMORY

5.2.1 OVERVIEW

The first phase of the Nopal processor performs syntax and local semantic analysis of specification statements. At the end of the analysis, each Nopal statement is encoded and stored in a simulated associative memory for ease of further processing. The first phase includes a Syntax Analysis Program (SAP). SAP itself is generated automatically by a meta processor called Syntax Analysis Program Generator (SAPG), by inputting the formal specification of the Nopal language in a meta-language, called Extended Backus Normal Form with Subroutine Calls (EBNF/WSC). SAPG and SAP are described in Section 5.2.2.

SAP incorporates six types of supporting routines, which are composed manually: Lexical Analyzer, Error Stacking, Recognizer, Encoding/Encoding/Storage Semantic Checking and Service Routines. These are described in Section 5.2.2.

At the end of each Nopal statement, a storing routine is invoked to store the statement in
5.2.1 OVERVIEW

the simulated associative memory using the Store/Retrieval package. The Store/Retrieval package and the associative memory is described in 5.2.4.

Finally, the set of reports generated by this phase are described in 5.2.5.

5.2.2 SYNTAX ANALYSIS PROGRAM - SAP

SAP is generated by the Syntax Analysis Program Generator (SAPG). The input to SAPG is the specification of the Nopal language in the meta-language EBNF/WSC. SAPG and EBNF/WSC were originally developed at the University of Pennsylvania Data Definition Language Project [43] [44]. A brief review of EBNF/WSC and SAPG is given below.

EBNF/WSC extends the standard EBNF to provide semantics. The semantics is specified by means of subroutine names which are included in the productions, along with the terminals and non terminals. These subroutine names indicate the need to call the respective subroutine upon successful recognition of the preceding syntactic unit by the parser. For example, the production

\( \langle A \rangle \rightarrow \langle B \rangle /aa/ \langle C \rangle \)

indicates that a subroutine named "aa" needs to be called on successful recognition of the non-terminal \( \langle B \rangle \) in the process of recognizing the non-terminal \( \langle A \rangle \). The subroutines themselves are written manually.

SAPG accepts the specification in EBNF/WSC and generates a recursive descent parser to recognize the syntax defined by the EBNF. Calls are inserted to the subroutines upon recognition of non-terminals as specified by EBNF/WSC specification. SAPG requires that the EBNF grammar must be in LL(1) form. The grammar should be free of left recursion, and the first terminal symbol should distinguish between the optional groups at any point in the grammar.
5.2.3 SUPPORTING SUBROUTINES

The EBNF/WSC specification contains names of subroutines which are called from SAP.

They can be categorized into six types:

1. **Lexical analyzer** scans the Nopal input string and returns tokens of syntactic units to SAP or the recognizer routines.

2. **Error message stacking routines** help compose and stack error messages before every syntactic unit in the specification. In case of incorrect or missing syntactic units, SAP generates the error message from the error stack.

3. **Recognizer routines** recognize a class of input tokens such as names and integers. These occur in productions of the form:
   \[ <A> \rightarrow \text{/RR/} \]
   where RR is the name of a recognizer routine.

4. **Encoding 'saving/storing routines** save the tokens in appropriate data structures and finally in associative memory for purposes of later analysis.

5. **Semantic checking routines** check the local semantics of a Nopal statement.

6. **Service routines** are used by SAP to perform some internal services e.g., popping the error stack.

At the end of each Nopal statement a storing routine is called by SAP, which in turn calls STORE to enter the information relating to the present statement into the associative memory.

5.2.4 ASSOCIATIVE MEMORY AND STORE/RETRIEVE SUB-SYSTEM

The Store/Retrieve Subsystem is a generalized means of storing the Nopal source statements and later retrieving them. It consists of two types of routines:

1. **STORE** for storing the source language strings, including tokens and entities, gathered during the syntax analysis, and

2. **RETRIEVE** for retrieving the source strings, and for accessing the "directory entries", the former is through RETREVS and the latter through RETREVD.

The STORE routine is called to create or add to the associative memory, and RETRIEVE to
Figure 5-3: FLOWCHART OF SAPG AND SAP WITH SUBROUTINES
access or modify it.

There are eighteen classes of statements and names in Nopal. A list of classes, their mnemonics, and the entities they represent is given in Table 5.1. For example, class 15 represents the variables, and class 2 represents the tests. An identifier occurring in two different classes denotes two different entities. In other words, a name together with its class uniquely identifies an entity.

A directory is used to store all the names and their classes. It is organized as a binary tree according to the lexicographic order of entries. Each node of the tree corresponds to a name and its class. There are cross links in this tree which connect all nodes with the same name together, and all nodes of the same class together. Each node has an additional link (called REF LIST in Figure 5.4) to a storage entry containing this name and type.

There is a storage entry for each Nopal source statement. It contains the names (KEY) of all the symbols (rather pointers to the names in the directory) which occur in a the corresponding statement. With each symbol name it has a pointer (called NEXT) which points to another storage entry which uses it. Thus, it provides a very efficient means to find occurrences of symbols in different statements. Associated with each storage entry there is also a pointer (DATA) which points to the entire parsed source string, stored in a separate data area.

The storage entries together with the directory and the data area is called the associative memory.

As mentioned in the previous section, STORE is called at the end of each Nopal statement. Its arguments are (1) a list of names and their classes encountered in the statement, and (2) pointer to the data area containing the parsed source statement. It enters the names and their
### Table 5-1: CLASSES OF NAMES AND THEIR TYPES

<table>
<thead>
<tr>
<th>CLASSES</th>
<th>END-PLIC</th>
<th>CLASS OF ENTITIES REPRESENTED</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>SPEC#</td>
<td>NOFAL specification label/statement</td>
</tr>
<tr>
<td>2</td>
<td>TEST#</td>
<td>Test module label/statement or modfun header</td>
</tr>
<tr>
<td>3</td>
<td>STIM#</td>
<td>Stimulus label/statement</td>
</tr>
<tr>
<td>4</td>
<td>MEAS#</td>
<td>Measurement label/statement</td>
</tr>
<tr>
<td>5</td>
<td>DIAG#</td>
<td>Diagnosis label/statement</td>
</tr>
<tr>
<td>6</td>
<td>MSG#</td>
<td>Message label/statement</td>
</tr>
<tr>
<td>7</td>
<td>LOGIC#</td>
<td>Logic label/statement</td>
</tr>
<tr>
<td>8</td>
<td>CONJ#</td>
<td>Conjunction label/statement</td>
</tr>
<tr>
<td>9</td>
<td>ASRT#</td>
<td>Assertion label/statement</td>
</tr>
<tr>
<td>10</td>
<td>COMP#</td>
<td>UUT component identifier (id)</td>
</tr>
<tr>
<td>11</td>
<td>CMPFL#</td>
<td>Component-failure (i.e. affected component) id/statement</td>
</tr>
<tr>
<td>12</td>
<td>UUITPT#</td>
<td>UUT connection point id/statement</td>
</tr>
<tr>
<td>13</td>
<td>ATEPT#</td>
<td>ATE inter-connection point/id statement</td>
</tr>
<tr>
<td>14</td>
<td>FUNC#</td>
<td>Function id</td>
</tr>
<tr>
<td>15</td>
<td>VAR#</td>
<td>Variable id</td>
</tr>
<tr>
<td>16</td>
<td>END#</td>
<td>End statement</td>
</tr>
<tr>
<td>17</td>
<td>dtyp#</td>
<td>data type name</td>
</tr>
<tr>
<td>18</td>
<td>rec#</td>
<td>data declaration statement</td>
</tr>
</tbody>
</table>
(a) **DIRECTORY ENTRY**

<table>
<thead>
<tr>
<th>Key-entry</th>
<th>Tree-link</th>
<th>Cross-link</th>
</tr>
</thead>
<tbody>
<tr>
<td>Keyname</td>
<td>Reflist</td>
<td>Up</td>
</tr>
<tr>
<td>Key class</td>
<td>Down</td>
<td>Name</td>
</tr>
<tr>
<td></td>
<td>Next</td>
<td>Type</td>
</tr>
</tbody>
</table>

(b) **STORAGE ENTRY**

<table>
<thead>
<tr>
<th>Keyentry(1)</th>
<th>Keyentry(#keys)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Data</td>
<td>#keys</td>
</tr>
<tr>
<td></td>
<td>Key</td>
</tr>
<tr>
<td></td>
<td>Next</td>
</tr>
<tr>
<td></td>
<td>Key</td>
</tr>
<tr>
<td></td>
<td>Next</td>
</tr>
</tbody>
</table>

Other data

**Figure 5-4: STRUCTURE OF THE DIRECTORY AND STORAGE ENTRIES**
classes into the directory, and creates a storage entry corresponding to the statement. The storage entry contains the names (rather pointers to the names in directory) which occur in this statement. STORE then proceeds to create all the association links corresponding to each of the names, and also to store the pointer to the data area in the storage entry.

The two procedures RETREV0 and RETREV5 allow the information to be retrieved from the associative memory. The former retrieves pointers to directory entries, and the latter retrieves storage entries. Entries can be retrieved by logical expressions of their names and classes. For example, all entries belonging to a certain class which do not occur in some statement class can be retrieved by constructing an appropriate logical expression.

5.2.5 REPORTS

Listings of the specification and errors encountered, if any, in the specifications are reported at the end of the Syntax Analysis Phase. The programs XREF1 and XREF2 generate a cross-reference listing, and the program SOURCE2 generates a formatted listing of the user specification. Samples of these reports are shown in examples in the Appendix.

XREF1 also determines the scopes of variables i.e. whether the variables are global or local, and enters it in the data areas of the associative memory.

5.3 SPECIFICATION ANALYSIS AND SEQUENCE DETERMINATION

5.3.1 OVERVIEW

Phase 2 of the Nopal processor analyzes a Nopal specification and determines the sequence of execution of the statements. The analysis is based on a graph representation of
the specification. This section presents the background and terminology used in this phase.

Phase 2 is divided into two sub-phases. In sub-phase 1 each of the tests is analyzed, and in sub-phase 2 the relations between tests within a module are analyzed. The sub-phases are called intra-test analysis and inter-test analysis respectively. In the intra-test analysis a graph is constructed for each of the tests. Nodes of the graph represent variables, assertions, conjunctions and diagnoses, and the edges represent precedence relationships between them. In the inter-test analysis on the other hand, the nodes of the graph represent tests, diagnoses and global variables, and the edges represent precedence relationships between them. Edges in both the sub-phases are labeled to denote the different types of precedence relationships.

The Nepali processor stores the graph in a matrix form. The rows and columns represent the nodes, and the entries in the matrix represent edges. A non-zero entry, say m, in the position (u, v) in the matrix represents an edge of type m from node u to node v, while a zero entry denotes the absence of an edge.

After the graph is constructed, it is checked for consistency and completeness. It is then checked for cycles, and an attempt is made to eliminate them. Finally, if successful, the nodes are ordered in an execution sequence. Construction of the graph, consistency, and completeness analysis, cycle elimination, and sequencing are described for the intra-test sub-phase in Section 5.3.1 and for the inter-test sub-phase in Section 5.3.2. Figure 5.5 shows a flowchart of the processes involved in graph analysis and sequencing.

5.3.2 INTRA-TEST ANALYSIS AND SEQUENCING

Each of the tests in a specification are analyzed in this sub-phase. To perform analysis and sequencing, a graph is constructed for each of the tests. Nodes of a graph are conjunctions.
5.3.2 INTRA-TEST ANALYSIS AND SEQUENCING

![Flowchart Diagram]

**Figure 5-5: Flowchart for Phases 2 and 3 of NOPAL Processor**
assertions, variables and their ancestors, and diagnoses associated with the test. There are six types of precedence relationships between nodes, which are represented by edges in the graph. Table 5.2 shows the edge types and the relationships that they represent. A priority is associated with each edge: 1 denotes the highest priority and 6 denotes the lowest. Edges with priority 1 are considered mandatory and cannot be deleted. Edges with lower priority are not essential and can be deleted during the cycle elimination stage; they represent preferred relationships rather than mandatory ones.

Relationship of data determinacy exists between variables on one hand and conjunctions, assertions and diagnoses on the other. A variable node is the predecessor of conjunctions and assertions if it occurs as a source, and is successor if it occurs as a target in them. Similarly, a variable is predecessor of a diagnosis if it occurs as a parameter, and is successor if it occurs in the operator response. The relationship of data determinacy expresses the idea that a variable must be defined before it is referenced.

Relationship of waveform setup exists between the stimulus conjunction and measurement conjunction. It is not mandatory and is of priority 2. It expresses the notion that stimulus is usually applied before the measurements are made.

Relationship of diagnosis waveform exists between diagnosis on one hand and conjunctions and assertions on the other. This relationship is entered as type 16 or 17. A diagnosis which is selected unconditionally on the outcome of a test precedes each of the conjunctions and assertions in the test by an edge of type 16. A diagnosis which, on the other hand, is selected by the logic $\lor$, $\land$, $\land$ and $\lor$ succeeds each of the conjunctions and assertions by an edge of type 17.

All the unconditionally selected diagnoses precede all other diagnoses by edges of type
### Table 5.2 Intra-Test Precedence Relationships

<table>
<thead>
<tr>
<th>Type</th>
<th>Priority</th>
<th>Relationship</th>
<th>Predecessor</th>
<th>Successor</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>Data-determinacy</td>
<td>Source variable in an assertion</td>
<td>The assertion</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>An assertion having a target variable</td>
<td>The target variable</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>A variable in a parameter of diagnosis</td>
<td>The diagnosis</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>A diagnosis</td>
<td>Variable in operator response of the diagnosis</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>Waveform-setup</td>
<td>Stimulus-conjunction</td>
<td>Measurement-conjunction</td>
</tr>
<tr>
<td>16</td>
<td>5</td>
<td>Waveform-diagnosis</td>
<td>Diagnosis selected by * logic</td>
<td>All waveforms</td>
</tr>
<tr>
<td>17</td>
<td>5</td>
<td></td>
<td>All waveforms</td>
<td>All diagnoses not selected by * logic</td>
</tr>
<tr>
<td>18</td>
<td>5</td>
<td></td>
<td>Diagnoses selected by * logic</td>
<td>All other diagnoses</td>
</tr>
<tr>
<td>19</td>
<td>1</td>
<td>Hierarchical</td>
<td>Node in an input structure declaration</td>
<td>All its direct descendent nodes</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Node in an output structure</td>
<td>Its parent node in the structure</td>
</tr>
</tbody>
</table>
### Table 5.2: INTRA-TEST PRECEDENCE RELATIONSHIPS

<table>
<thead>
<tr>
<th></th>
<th></th>
<th>Pointer</th>
<th>Pointer variable (i.e., variable with prefix PTR_ or PTR_y, where y is a digit 1 to 5)</th>
<th>Structure for which the pointer variable is a key or parameter (given by the suffix of the pointer variable)</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>1</td>
<td>Pointer</td>
<td></td>
<td></td>
</tr>
<tr>
<td>21</td>
<td>6</td>
<td>Recursive*</td>
<td>A source variable in an assertion with subscript of the form 1-k, where k is positive integer</td>
<td>The assertion</td>
</tr>
</tbody>
</table>

*This relationship is originally entered as type 1, but is changed later to type 21 in the subscript analysis phase.*
18.

Relationship between nodes in a data structure is called hierarchical, and is entered as edge of type 19. A node in a structure precedes each of its direct descendants in an input structure, and succeeds each of its direct descendants in an output structure.

Pointer relationship exists between a variable which is a key of an ISAM file and the record node of the ISAM file. It is entered as type 20 edge.

Certain data determinacy relations are identified as recursive and are entered as type 21 edges. They are mentioned here for the sake of completeness and are described later after a discussion of array graph.

An array is represented by a single node in the graph. An array variable is represented as a single node independent of its dimensions, similarly an assertion is represented by a single node irrespective of the free subscripts which occur in the assertion. Edges in the graph represent relations between the nodes. An edge between two nodes, when at least one of the nodes represents an array variable, denotes an array of relations \((\text{array relations})\) between the two nodes. A graph whose nodes represent array variables and whose edges represent array relations is called an array graph.

The intuitive notion of array graph, introduced above, can be made more precise in terms of what is called the underlying graph \((\text{UG})\) of a specification. A variable node of a UG represents a simple variable, conjunction, assertion, or diagnosis. In other words if \(B\) is an array variable of two dimensions of size 5 and 10 each respectively, then a separate node is needed in the UG to represent each of the 50 elements of \(B\) similarly, for conjunctions, assertions and diagnoses which have free subscripts and express array of relations between array variables, a node represents an element of the array of relations, e.g. if \(B\) is an array as
before and it occurs in a conjunction, assertion or diagnosis, then there will be 50 nodes, each representing a conjunction, assertion or diagnosis involving one element of B. Edges in a UG represent relationship between nodes as outlined before, and as the nodes represent simple entities the edges also represent simple relations.

Array graph (AG) can be formed by taking the union of nodes and edges in an underlying graph as follows: represent the nodes, say N, W, in UG representing different elements of an array variable (or conjunction, assertion or diagnosis) by a single node, say N, in the corresponding array graph and for an edge from any of the nodes, N, to any other node, say P, in UG form an edge from N to P in AG. The resulting smaller graph is an AG of the given UG. Thus, AG is a compact way to represent UG. The UG may be an enormous graph which is impractical to analyze.

An array graph is shown in Figure 5-6. It is for the familiar PUSH function of stack data type Nodes S, Z, a2 and S1 Z are array nodes in the example. The rest of the nodes represent simple variables and assertions.

The array graph is constructed by means of the procedure IN1SEQ. It is first analyzed for two types of consistency checks:

1. Single assignment rule: Variable nodes should have exactly one predecessor assertion or diagnosis, i.e. a variable should be defined by exactly one assertion or diagnosis etc. (In case the variable is part of an input structure or is a source parameter of the modfun, then it need not have any predecessor in the graph. In the first case, the input file is taken to be the implicit predecessor. In the second case, the value of the formal parameter is defined when the modfun is called and hence it does not have a predecessor in the present graph.)

2. Target variables in an assertion should occur either on the left hand side of the relational operator, or as target parameters of function. Target variables of a conjunction should occur only as parameters of functions.
5.3.2 INTRA-TEST ANALYSIS AND SEQUENCING

Figure 5-6: SPECIFICATION OF PUSH AND ITS ARRAY GRAPH

Legend:
- assertion node
- variable or diagnosis node
- H: hierarchical edge
- D: data determinacy edge
- WD: waveform-diagnosis edge
5.3.2 INTRA-TEST ANALYSIS AND SEQUENCING

Subscript analysis is performed by the procedure SUBANAL. First all the declarations
free subscripts are checked for correctness i.e. that no subscript is declared twice and the
same variable dimension is not used in two subscript declarations. Finally, a table of
the free subscripts is constructed containing their names and upper bounds.

Further checks of the free subscripts are conducted by the procedure SUBFAC
follows.

1. All occurrences of a target variable in an assertion or conjunction must have the
   same free subscript. For example in the assertion (from FUNC example)
   \[
   \begin{array}{l}
   \text{IF } J = \text{S.TOPZ} \text{ THEN } S1.Z(J) = X \\
   \text{ELSE } S1.Z(J) = \text{S.TOPZ} \\
   \text{TARGET: } S1.Z(J);
   \end{array}
   \]
   variable S1.Z(J) is the target variable occurring in both the IF and ELSE parts.

2. The free subscripts of the source variables must appear as subscripts with the
   target variables. There are, however, two exceptions. First a free subscript
   which is reduced by a reduction function, need not appear as a subscript of the
   target variable. Second, in an if-assertion or if-conjunction the free subscript of
   source variables need not appear with the target variables. In that case, a
   warning is issued to the user that the target variable should be checked that it does
   not have multiple definitions. A warning will be issued if the following case.
   \[
   \begin{array}{l}
   \text{IF END-J(J) = TRUE THEN OUT = A(J)} \\
   \text{TARGET: OUT;}
   \end{array}
   \]

3. Subscripts must be in one of the following forms:
   a. a subscript term e.g. I in A(I);
   b. a subscript expression of the form (I k) where I is a free subscript and k is a
      positive integer;
   c. another variable e.g. B(I) in A(B(I)) or X in A(X).

4. If a positive integer or a subscript term appears as an index of an array variable V,
   and the range for the corresponding dimension of V is declared to be d, then in
   case of the integer its value, and in case of the subscript term its upper bound,
   should be less than d. In other words, a subscript expression is checked to see
   that it lies within the range for the above two cases.
The array graph is analyzed, next, for cycles by the CYCLES procedure. If a cycle is detected in the graph then the procedure attempts to eliminate it. Edges in a cycle having priority value greater than 1 may be removed. These edges correspond to two cases:

1. The edges are considered as preference edges and are not essential e.g. a type 2 edge between stimuli conjunction and measurement conjunction denotes the usual situation that the stimulus is applied before the measurement. However, there may be situations in which a stimuli depends on the measured value, and can only be applied after the measurement is performed.

2. The edges do not imply a cycle in the underlying graph. This occurs with recursive edges. For example, the array graph for an assertion of the form:

   \[ a: \text{IF } I = 1 \text{ THEN } A(I) = 1 \]
   \[ \text{ELSE } A(I) = I \times A(I-1) \]
   \[ \text{TARGET: } A(I); \]

   is given by Figure 5-7. In the underlying graph recursive edges give rise to acyclic spiral like structures.

   In the event that deletion of edges fails to resolve all the cycles, an error is reported to the user that the specification contains a circular definition and that it is not possible to sequence it. A warning is issued for each edge deleted in the cycle elimination process.

Procedure PROPAGT determines the relation between the nodes and the free subscripts in order to find the proper scopes for each possible iteration. This procedure constructs for each node a list of subscripts on which it depends, and hence the list of iterations in which it should participate. In the Nopal language, iterations result from explicit appearance of subscripted variables and subscripts themselves.

The final stage is to sort the nodes into a possible execution sequence. If there were no subscripts, and hence no iterations, then a simple topological sort would be sufficient. The presence of subscripts introduces an additional factor. A brute force approach to handle subscripts is to enclose each node in the iteration scopes of its subscripts, with the exception
that the nodes belonging to a recursive cycle (which was opened during cycle elimination stage) must be enclosed in the scope of a common subscript iteration. The algorithm used in the Nopal processor does better than the brute force approach and tries to maximize scopes of iterations. It is performed by the procedure SCHEDLR. The scheduling process is described below. At the end of this process an order vector is generated along with subscripts and subscripts of iterations.

There are three inputs to the scheduling process:

1. an array graph,

2. a list of free subscripts for each of the nodes and a list of nodes for each free subscript, and

3. a list of recursive cycles, where for each recursive cycle there is a list of nodes which occur in it.

The scheduling process consists of two procedures: SCHEDLR and ORDERER. SCHEDLR calls on ORDERER requesting trial ordering of nodes depending on a subscript. Bas
5.3.2 INTRA-TEST ANALYSIS AND SEQUENCING

the results of the trial ordering, SCHEDLR calls ORDERER a second time to perform actual scheduling of nodes.

SCHEDLR makes use of a stack called NEST, which contains free subscripts. The NEST stack contains free subscripts corresponding to which iterations have begun. Iterations are nested within each other, with the free subscript on top of the NEST stack representing the innermost iteration. Nodes currently being ordered by ORDERER are within all these iterations. In addition to the NEST stack, SCHEDLR also has a stack containing free subscripts called TBNESI. It contains those free subscripts which are candidates nested at the innermost level in the iterations corresponding to the free subscripts in the NEST stack.

SCHEDLR has three phases. In Phase 1 it picks up all those nodes in the graph that have no predecessors, and finds the union of the free subscripts associated with the nodes. These subscripts form the set CANDLIST. If one of the nodes does not depend on any other node then it is treated as belonging to subscript free set, and a special entry (zero) is added to CANDLIST. From the set CANDLIST, another set called BESTCANDLIST is formed. The following cases are performed progressively in succession until a non-empty BESTCANDLIST results:

1. all the subscripts in set CANDLIST which also belong to TBNESI are placed in BESTCANDLIST;

2. a subscript in the CANDLIST set which also belongs to NEST stack is placed in BESTCANDLIST;

3. if entry zero, corresponding to subscript free nodes, belongs to CANDLIST, it is placed in BESTCANDLIST; otherwise

4. all entries belonging to CANDLIST are placed in BESTCANDLIST.

BESTCANDLIST now contains those free subscripts which are possible candidates for inclusion in the NEXT list.

BESTCANDLIST now contains those free subscripts which are possible candidates for inclusion in the NEXT list.
5.3.2 INTRA-TEST ANALYSIS AND SEQUENCING

ordering process.

In Phase 2, SCHEDLR calls ORDERER with each of the entries in BESTC
perform a trial schedule. The results of the trial schedule are evaluated ac
priority table given in Table 5.3.

Let the ORDERER be called to perform a trial ordering with a subscript IC helo
set BESTCANDLIST. It performs a trial schedule and returns the following informa
1. whether all the nodes depending on IC got scheduled; or whether it
completely scheduled;
2. a set of other subscripts, IOC, which got completely scheduled;
3. a set of other subscripts, IOP, some of whose nodes got scheduled;
subscripts which got partially scheduled; and
4. whether there is a recursive cycle some but not all of whose node
scheduled.
A priority value is evaluated based on the above results as per Table 5.3. In the
ture if condition (1) is satisfied, and CY is equal to 0 if condition (4) is satisfied.

If the priority value is 1 then the SCHEDLR proceeds to Phase 3 to call their
second time with IC, this time to do the actual scheduling. If the priority value is gr
then trial schedule for a new subscript in BESTCANDLIST is done. Let all the
subscripts in BESTCANDLIST have been trial scheduled, the subscript, say IH, with
value of priority, say P, is chosen. If P is equal to 5 an error message is issued that
cycle needs to be broken. If P is equal to 4 a warning is issued indicating to the
same files must be entirely located in the main memory. For other values of P at 1
Phase 3 of SCHEDLR to do the actual scheduling with subscript IH.

Phase 3 corresponds to the second call on ORDERER to do the actual sel
5.3.2 INTRA TEST ANALYSIS AND SEQUENCING

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<th>IC has</th>
<th>IOP = NULL</th>
<th>IOP has no I/O</th>
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<td>CY = 0</td>
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I/O stands for input-output. Meaning of IC, IOP, CP, CY etc. is explained in the

Table 5-3: PRIORITIES OF THE TRIAL SCHEDULE
MODULARITY IN NON-PROCEDURAL LANGUAGES THROUGH ABSTRACT DATA TYPES

AUG 80 R SANGAL

UNCLASSIFIED

N00014-76-C-0416

END
nodes. Following this, the nodes which got scheduled are removed from the graph. Finally, if some nodes still remain in the graph, Phase 1 is started all over again.

Procedure ORDERER is described next. It has two modes: (1) to perform trial scheduling, and (2) to perform actual scheduling of nodes. It has a parameter, IC, which gives the name of a free subscript.

In mode (1) it does a topological sort of the nodes which depend on the subscript IC. It then evaluates the result of the trial ordering and returns the result in CP. IOC, IOP and CY as described earlier.

In mode (2) it performs a topological sort of the nodes which depend on the subscript IC, on all of the subscripts in the stack NEST and on no other subscripts. The resulting ordered set of nodes is added to the ORDER vector and removed from the graph.

The scope of iterations is determined from the NEST stack. Each time an entry is pushed on the NEST stack it defines the beginning of a new iteration; and each time the NEST stack is popped it defines the termination of an iteration. The NEST stack is updated as follows:

1. Each time the ORDERER is called to do the actual scheduling with a subscript IC, an entry is made on NEST provided IC was not selected by case (2) in Phase 2 of SCHEDLR.

2. The NEST stack is popped (in case(2) in Phase 2 of SCHEDLR) until the selected subscript IC is on top of the NEST stack.

The final result of scheduling process is an order vector and an iteration table giving the scopes of iterations. They are used by the code generation phase (by procedure CDETEST described in Section 5.4) to generate Equate-Atlas code.
5.3.3 INTER-TEST ANALYSIS AND SEQUENCING

In this sub-phase a graph is constructed for the entire modfun specification. The nodes of the graph are tests, diagnoses and global variables. There are seven types of precedence relationships between nodes. They are described in Table 5.4. The table gives the name, type, and priority associated with a precedence relationship. It is followed by a description of the predecessor and successor nodes which satisfy the relationship. The meaning of the terms: type, priority etc. is the same as discussed in Section 5.3.2. The seven relationships are described below.

Data determinacy relationship exists between tests, diagnoses and global variables. A test or a diagnosis is the predecessor of a variable if the variable is defined by one of them, and successor if the variable is used as a source by them.

Interactiveness relationship exists between a diagnosis and the test which selects the diagnosis by "after" and "after not" logic operator (A and A-). It means that the test is selected based on the operator response to the diagnosis.

Component protection relationship exists between a diagnosis and a test, if the test has an affected component which is protected by the diagnosis. Its purpose is to inhibit testing of a component if another component which protects it has failed.

Fault isolation relationship exists between a diagnosis and a test, if the set of affected components of the diagnosis contains the set of affected components of the test. It expresses the idea that those tests which isolate smaller number of failures should be performed later compared to the tests which isolate larger number of failures.

Stimuli-application relationship exists between two tests if one of the tests has stimulus functions which are applied more frequently than those in the other test. It leads to performing
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5.3.3 INTER-TEST ANALYSIS AND SEQUENCING

of as many tests as possible once an ATE device is connected.

Two tests are related by means of failure likelihood relationship if the predecessor test isolates those failures which are more likely to occur. The likelihood of a failure is supplied by the user in the specification.

Finally, a test is the predecessor of a diagnosis selected by one of the logic operators: $\land$, $\land\sim$, $\&$ and $\&\sim$ in the test. The selection of a diagnosis by means of one of the above logic operators is dependent on the outcome of the test. This is expressed by the logic operator relationship.

Several of the relationships described above are not mandatory. They represent desirable but not necessary relationships; in other words, such relationships are good for efficiency but not necessary for correctness. A priority value greater than 1 is associated with them in Table 5.4.

Procedure EXTSEQ constructs a graph for the modfun specification. The nodes of the graph represent simple entities, unlike the graph for a test. This is so because there are no free subscripts associated with the entities which are represented by the nodes. The graph is analyzed to check:

1. that every variable node has a predecessor, i.e. every variable is defined;

2. that every variable node has only one predecessor, i.e. every variable is defined by only one test or diagnosis;

3. that a diagnosis does not precede two or more tests with type 2 or 3 edges, i.e. a diagnosis does not select more than one test by the logical operators $\land$ and $\land\sim$.

The next step is to detect cycles and, if possible, eliminate them by removing edges with priority value greater than 1. They correspond to preference edges and are not essential e.g.
5.3.3 INTER-TEST ANALYSIS AND SEQUENCING

a failure likelihood edge (type 10 priority 4) between two tests expresses that the likelihood of detecting a failure by the predecessor test is higher. It reflects knowledge which may be useful for quicker fault isolation, but is not mandatory for correct fault isolation.

The final step is to sort the nodes into a possible execution sequence. A simple topological sort is sufficient because there are no free subscripts or iterations. Finally, an order vector is generated. The order vector is used by Phase 3 to generate Equate-Atlas code.

5.4 CODE GENERATION

This is the third and final phase which generates Equate-Atlas code corresponding to the Nopal specification. Code is generated for each of the entities: tests, diagnosis, assertions, conjunctions, variables, structures etc. The order of execution of these entities is determined in Phase 2 in the form of an order vector. This is used in the present phase in generating the sequential program in Equate-Atlas.

Equate-Atlas is a test programming language and is a subset of IEEE standard Atlas. It has a number of features to support the programming of ATE. However, it does not support many of the widely accepted programming constructs. Mostly notably,

1. The procedures in Equate-Atlas do not have parameters. The procedure simply represents a body of sequential code which is executed when called.

2. There is no provision for local variables in procedures. All variables are considered global.

3. The if-then-else construct is absent. It can be simulated using "compare" and "goto" statements, reminiscent of the assembly language instructions.

4. It does not have a do-while construct. It has for-loop similar to the Do-loop in Fortran.
5. It does not have a linking facility. Consequently, all the procedures should be included in one program at compile time. The procedures communicate by means of global variables.

6. The only data structuring method in the language is array. Declarations for records and structures are not allowed.

7. The language has only two data types: decimal and digital. Decimal is used for floating point numbers and digital for bit strings. There are no other data types e.g. character strings, integers etc.

8. It does not allow dynamic memory allocation.

Certain conventions were established, in view of the rather severe limitation given above. For example, to pass parameters to a procedure, named say P, the following convention was adopted: The parameters were passed in the special variable names P.PRMO1, P.PRMO2, ... and so on. At the time of the procedure call these parameter variables are given values. The body of the procedure uses these names to receive source parameters and defines values of the target parameters to return values.

Lack of a linking facility forces that the Equate-Atlas statements generated separately for each of the modules be put together and the resulting total program be compiled at one time. This raises a problem, however. The language has no local variables, and hence, two variables of the same name occurring in the two different modules would be treated as one. The clash of the variable names is avoided by generating unique names for the module. All variables in a module are suffixed by "." followed by the module name.

The absence of if-then-else and do-while is handled using the primitives "compare" and "goto". The absence of structure declaration is handled by simple variables and arrays. Although, these make the generated code messy, they pose no conceptual problem.

The code generation phase consists of three sub-phases. Sub-phase 1 consists of
5.4 CODE GENERATION

generation of program header, declaration for the global variables and system variables, and a procedure definition for each of the diagnosis. Sub-phase 2 consists of generation of a procedure for each test. The third and final sub-phase 3 consists of generation of logic and sequence of calls on procedures for tests within a modfun. The procedures for each of the sub-phases are CDEMAIN, CDETEST and TRMNATE respectively. The highlights of the sub-phases are presented below.

In sub-phase 1 the declarations for global variables are issued. For a simple variable in the Nopal module, a simple variable by the same name (suffixed by the module name as described earlier) is declared in Equate-Atlas. Similarly, for an n-dimensional array variable in Nopal, an array with the same upper bounds for each of the dimensions is declared in Equate-Atlas. There is an exception, however. For array dimensions whose upper bound has been declared as "0" in Nopal, and for which only two elements - current and the previous need to be kept in memory, size of 2 is declared in Equate-Atlas. The two elements in Equate-Atlas are used to store the current and the previous value of the elements of memory and is part of the space optimization done by the Nopal processor.

Equate-Atlas does not have any facility for declaration of structures. Consequently, a translation is made: the fields in the structures are declared as variables. The dimensionality of the variables is the same as the dimensionality of the fields. (The dimensionality of a field is obtained by propagating the dimensionality of its ancestor nodes in the structure, to the field. This is done by the procedure XREF1.)

In case of a module M (not the main module) an additional dimension is added to the fields of the record which gives the representation for the abstract data type M. For example, in the declaration of representation of a stack...
5.4 CODE GENERATION

NOPAL MODULE STACK;
DCL 1 STACK: RECORD,
  2 TOPZ: INTEGER,
  2 Z: INTEGER ARRAY(100);

the fields TOPZ is declared to be a one dimensional array, and Z a two dimensional array.
This extra dimension is added to allow storage of all the variables of type stack. Similarly, in
the usage of the fields of stack, S.TOPZ, the qualifier S becomes an index which provides the
reference into the array TOPZ. All this became necessary because the object language does
not have facilities for dynamic memory allocation. In PL/I for example, the above could have
been implemented by means of based variables and pointers. Record STACK with
components, i.e. variable TOPZ and one dimensional array Z, would have been declared as a
based structure. The qualifiers would simply have been pointers. There would be no need to
add an additional dimension.

It follows from the above discussion that, in the current implementation, the variables of
abstract data types are indices to arrays in the Equate-Atlas program and store decimal
numbers.

Procedure CDETEST which performs sub-phase 2 is called at the end of sequencing of
each test in the intra-test analysis and sequencing. CDETEST generates a procedure for the
test. The body of the procedure contains sequential code corresponding to the conjunctions,
assertions, and logic for selecting diagnoses. Statements for conjunctions and assertions are
generated one at a time in the order determined from the earlier intra test sequencing phase.
Iteration statements are also generated based on information about the name of the iteration
variable, its upper bound and its scope. In cases, where the upper bound is not specified an
arbitrarily large upper bound is used. However, the appropriate termination condition is
generated to exit the loop.
5.4 CODE GENERATION

In the case of input (or output) structure, calls are generated on the ACCESS (or SAVE) functions to read (or write) the structure from (or to) the appropriate file. Similarly, in case of abstract structures of abstract data type, say DT, calls are issued on ACCESS.DT or SAVE.DT as the case may be.

Finally, sub-phase 3 generates calls on the procedures for the test, and the logic which precedes these calls. The order in which these calls are generated depends on the ORDER vector produced by the inter-test analysis and sequencing phase. This sub-phase is not needed for modules (except the main module) because only one test per modfun is permitted in the present implementation.

At the end of the three sub-phases, Equate-Atlas code is generated for a module specification. This can be put together with the code for other modules, thus yielding a complete Equate-Atlas program. One of the modules must be a main module. This program can now be run on an Equate-Atlas machine.
Chapter Six

CONCLUSIONS AND FUTURE WORK

6.1 SUMMARY

This dissertation presents the approach of abstract data types to introduce modularity in non-procedural languages. It introduces the notion of module for the specification of an abstract data type in a non-procedural language based on equational specification. A module specification can be analyzed for consistency, completeness and non-ambiguity independent of other modules. It allows abstract data types to be specified independent of their use. The concept of module is general enough to allow the specification of recursive data types.

A simple equational language is introduced, and the least fix point semantics of modules is presented. It is shown by means of an example how a data type specified by a module satisfies certain algebraic axioms.

Nopal, a non-procedural language designed for automatic testing of physical systems is used as an example to show the feasibility of the use of abstract data types. Nopal language allows abstract data types to be specified by means of modules. The data types once specified can be used in other modules.

A complete implementation of the Nopal program generator is described in brief. A number of examples and their sample runs are given in the Appendix. The program generator analyzes the specification and generates an efficient program in Equate-Atlas satisfying the specification. Optimization for memory and execution time is done in the generated program.
The use of abstract data types allows relations to be specified between variables which are not just of elementary type, but are of arbitrary type. It allows a data type to have an arbitrary degree of complexity hidden away in the module and shielded from its use. This is of particular advantage in decomposition of the problem. It allows operations on larger units of data, ignoring lot of detail, in the process. When these large units of data correspond to some concept naturally occurring in the problem domain (e.g. stacks and tokens while parsing a string in a formal language) the specification is written in terms of these concepts. It also allows devices in automatic testing to be treated as data types.

Procedures or subroutines are procedural abstraction in the conventional programming languages. They represent a form of abstract action which fits well with the prescriptive style of programming. In non-procedural languages, on the other hand, the relationships between variables is the building block. Use of abstract data types allows the variables to be used and their values defined free of the details of the arbitrarily complex data structure that they might represent. It is felt that just as the procedures are a natural way to introduce modularity in procedural language, the abstract data types are a natural way to introduce modularity in non-procedural languages.

A most important feature of the introduction of the abstract data types in the non-procedural language has been that it does not lead to a change in semantics of the non-procedural language. This is in contrast to procedural languages where an abstract data type facility has led to an object oriented semantics e.g. CLU (Section 2.2), which is different from conventional and generally accepted value oriented semantics.
6.2 FUTURE WORK

Work needs to be done in two areas to make the abstract data types easy to use in non-procedural languages:

1. Efficiency of the generated program should be improved upon, and

2. Additional extensions should be made to the language.

Some of the problems are outlined below.

6.2.1 EFFICIENCY CONSIDERATIONS

In the current implementation, Nopal processor does the following memory optimization: If an array variable is declared to be of dimension '*.' and is used such that only the current and the previous element of the array is needed, then the memory allocated for the array is equal to two elements. This is of great value when the array is an input/output structure and represents a big file on secondary storage. The above should be extended to not just 2 but $k$ elements of an array variable (where $k$ is an integer). It should be determined when a constant storage, $k$, may be used in the generated program automatically without having the user to declare it. This is part of ongoing research by Mr. K.S. Lu [36] to generate efficient programs from a non-procedural specification (and is independent of the use of abstract data types).

Modularity makes some of the optimizations impossible at program generation time. For example, in the generated program for the specification of an abstract data type storage is allocated for the representation of each of the variables of abstract data type. Even when some of the variables are not needed at the same time, memory optimization cannot be done at the program generation time, since the use of the abstract data type is independent from its specification, and the corresponding information is not available at the time the program is
6.2.1 EFFICIENCY CONSIDERATIONS

generated from the specification.

A possible way to reuse the memory which is no longer needed is to do garbage collection. Any one of the well known techniques can be used [31] to provide better utilization of memory.

6.2.2 LANGUAGE EXTENSIONS

The data typing facility described here can be extended in many ways to improve compactness, clarity etc. To give an example: The language should permit (and the implementation should support) the specification of "parameterized" data types. By this it is meant that the specification of the abstract data types contains a data type as a parameter. For instance, it should permit the specification of a stack of type T, where T can be integer, character, stack etc.; and is specified with the use of the generic stack. This would allow a single stack specification to represent the various types of stack and lead to compactness as well as economy of names of data types and their modfuns.

Non-procedural specification should be investigated in the light of distributed processing. The applicative nature of the language is ideally suited for detection of parallelism within a module. The array graph can be directly translated into a parallel program. Research needs to be conducted to allow different modules to execute on different processors and communicate with each other.
Appendix A

EXAMPLES OF NOPAL SPECIFICATIONS

Some example specifications are given here. Sample runs for specification of stack together with a complete set of reports generated by the Nopal processor are given in the first section. The sections which follow, contain other example specifications with sequencing report for each of the specifications.
A.1 STACK

A.1 STACK

Nopal specification for stack is given in this section. Nopal module STACK defines a representation consisting of TOPZ and Z. It is followed by a specification of the functions PUSH, POP, TOP, and EMPTYSTACK which can operate on stacks. Each function implicitly has a test and is specified by means of assertions. The assertions specify relationships between the input and output parameters of the function. For example, in statement number 6 (which is an assertion in modfun PUSH) value of TOPZ component of stack S1 is specified in terms of the value of TOPZ component of stack S (where S1 is the output parameter, and S the input parameter of PUSH). The stack has been discussed quite extensively in Chapter 3 and the various assertions are not discussed any further here. Since a logic component must be associated with a test in Nopal, a dummy diagnosis is specified. Similarly, since the assertions must be part of stimuli or measurements, the assertions have been arbitrarily placed under stimuli in each of the modfuns.

A sequencing report is generated for each of the functions by the Nopal processor. It consists of weighted adjacency matrix representing the array graph; followed by an order vector which represents an ordering of the nodes of the graph. The order vector determines the sequence in which Equate-atlas code is generated for the module. Equate-Atlas code is given after the sequencing report. It is followed by a cross reference and attribute report, and warning messages.
/* NOPAL TEST SPECIFICATION SOURCE INPUT, FILE: SAPLIST */

NOPAL PROCESSOR OPTIONS SPECIFIED: SAPLIST, REF, CORE, SER, NONREF2, SOURCE2, TRACE=4, DEBUG=SER, CODE=LINE=5000

# STAT NO. *

1
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30

N O P A L  P O S I T I O N  S T A C K ;
2  D E L T A  S T A C K :  R E C O R D ,
2  T O P Z :  I N T E G E R ,
2  Z :  I N T E G E R  A R R A Y ( 1 0 0 ) ;
N O P A N  P O P S S T A C K ) R E T U R N S ( S T :  S T A C K ) ;
N O P A N  P O P S S T A C K ) R E T U R N S ( Y : I N T E G E R ) ;
N O P A N  E M P T Y  S T A C K  R E T U R N S ( S T :  S T A C K ) ;
D I A G N O M  :  P R I N T  = M S G ,
M E S S A G E  M S G :  " N O T I N G " ;
F U N C T I O N  S U B S T ,  T Y P E = E ,
F U N C T I O N  T R U E ,  T Y P E = E ,  V A L U E = B I T ( 1 ) ;
F U N C T I O N  F A L S E ,  T Y P E = E ,  V A L U E = B I T ( 1 ) ;
E N D  S T A C K ;
### INTRA TEST SEQUENCING PUSH

**ANALYSIS OF THE ADJACENCY MATRIX**

<p>| | | | | | | | | |</p>
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### SEQUENCE OF PROCESSING FOR TEST PUSH

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<td>GLOBAL / SOURCE /</td>
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<td>S</td>
<td>VARIABLE</td>
<td>LOCAL</td>
</tr>
<tr>
<td>6</td>
<td>1</td>
<td>S_SUB</td>
<td>ASSER</td>
<td>J = SUBS(&quot;S1&quot;, S1.(EMB_J).100)</td>
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<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>TARGET: J</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>SOURCE: SUBS</td>
</tr>
</tbody>
</table>

103
7 7 1 S.Topz VARIABLE GLOBAL / SOURCE /
8 2 2 S3.WOOGZ ASSERTION S1.TOPZ = S1.TOPZ+1
    TARGET: S1.TOPZ
    SOURCE: $3.TOPZ
9 6 2 J VARIABLE GLOBAL / TARGET /
10 8 3 S1.TOPZ VARIABLE GLOBAL / TARGET /

LOOP-1 STARTS: SUBSCRIPT J ITERATES FROM 1 TO 100
11 4 4 S3.WOOCCZ ASSERTION IF J=S.TOPZ THEN Enb.J(J) = TRUE
    ELSE Enb.J(J) = FALSE
    TARGET: Enb.J
    SOURCE: J, S.TOPZ, TRUE, FALSE;

12 10 4 S.J SUBSCRIPT_VA GLOBAL / SOURCE /
13 3 3 S3.WOOGC3 ASSERTION IF J=S.TOPZ THEN S.T.Z(J) = T
    ELSE S.T.Z(J) = S.T.Z(J)
    TARGET: S.T.Z
    SOURCE: J, S.TOPZ, T, S.T.Z;

14 14 5 Enb.J SUBSCRIPT_VA GLOBAL / TARGET /
15 11 6 S.T.Z SUBSCRIPT_VA GLOBAL / TARGET /
16 10 7 S7 VARIABLE LOCAL

LOOP-1 ENDS;

LOOP SUMMARY TABLE :
  LOOP-1 FIRST NODE IS 11 LAST NODE IS 10 SUBSCRIPT IS J

INTRA TEST SEQUENCING POP
ANALYSIS OF THE ADJACENCY MATRIX

1 1 1 1 1
1 2 3 4 5 6 7 8 9 0 1 2 3 4 5 6
... ... ... ... ...

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104
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<th>RANK</th>
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<tr>
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<td>$i$</td>
<td>VARIABLE</td>
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<tr>
<td>5</td>
<td>1</td>
<td>1</td>
<td>$ss_w0001$</td>
<td>0</td>
<td>ASSERTION</td>
<td>J = SUBS(&quot;$i$.2, $i$.2, END.2&quot;, 100)</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>TARGET: J</td>
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</tr>
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<td></td>
<td></td>
<td></td>
<td></td>
<td>SOURCE: SUBS;</td>
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<tr>
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<td>8</td>
<td>1</td>
<td>$i$.TOP1</td>
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<td>VARIABLE</td>
<td>GLOBAL / SOURCE /</td>
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<td>$ss_w0002$</td>
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<td>ASSERTION</td>
<td>$i$.TOP2 = $i$.TOP2-1</td>
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<td></td>
<td>TARGET: $i$.TOP2</td>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>SOURCE: $i$.TOP2;</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>7</td>
<td>2</td>
<td>$J$</td>
<td>0</td>
<td>VARIABLE</td>
<td>GLOBAL / TARGET /</td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>9</td>
<td>3</td>
<td>$i$.TOP2</td>
<td>0</td>
<td>VARIABLE</td>
<td>GLOBAL / TARGET /</td>
<td></td>
</tr>
</tbody>
</table>

LOOP-1 STARTS; SUBSCRIPT J ITERATES FROM 1 TO 100

10 4 4  $ss_w0004$ ASSERTION IF J=$i$.TOP2 THEN END.2(J) = TRUE
ELSE END_J(J) = FALSE
TARGET: END_J
SOURCE: J, S.TOP, TRUE, FALSE;

11 10 4 S.J SUBSCRIPT-UA GLOBAL / SOURCE /
12 3 5 S5_WOOD Assertion S1.Z(J) = S.Z(J)
TARGET: S1.J
SOURCE: J, S.Z;
13 14 5 END_J SUBSCRIPT-UA GLOBAL / TARGET /
14 5 6 BM DIAGNOSES PRINT = MSG;
15 11 0 S1.J SUBSCRIPT-UA GLOBAL / TARGET /
16 16 7 S1 VARIABLE LOCAL

LOOP SUMMARY TABLE:
LOOP-1 FIRST NODE IS 10 LAST NODE IS 16 SUBSCRIPT IS J

INTRA TEST SEQUENCING TOP
ANALYSIS OF THE ADJACENCY MATRIX

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SEQUENCE OF PROCESSING FOR TEST TOP

ORDER VECT ORDER RANK NAME TYPE TEXT
INNER VECTOR
1 4 6 SUBS VARIABLE GLOBAL / SOURCE /
# intra test sequencing empty stack

**Analysis of the Adjacency Matrix**

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<th>Vector</th>
<th>Rank</th>
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<td>assertion</td>
<td>$S_{WCC1}$</td>
<td>$j = \text{subset}(S_{2},100)$</td>
</tr>
<tr>
<td>2</td>
<td>run</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
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<td>$S_{TOP2}$</td>
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<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>$S_{I}$</td>
<td></td>
<td>variable</td>
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**Sequence of Processing for Test Empty Stack**

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<th>Description</th>
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<td>0</td>
<td>assertion</td>
<td>$S_{WCC1}$</td>
<td>$S_{TOP2} = 0$</td>
</tr>
<tr>
<td>2</td>
<td>run</td>
<td></td>
<td></td>
<td></td>
<td>print = msg;</td>
</tr>
<tr>
<td>3</td>
<td>$S_{TOP2}$</td>
<td>0</td>
<td>variable</td>
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<td>global / target /</td>
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<tr>
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<td>$S_{I}$</td>
<td></td>
<td>variable</td>
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107
BEGIN EQUATE PROGRAM "STACK" $  

NAMES INDEX  

*** TEST MODULES ***  

"PUSH" $1  

"POP" $2  

"TOP" $3  

"EMPTYSTACK" $4  

*** DIAGNOSES ***  

"RUN" $1  

DECLARE DIGITAL "SYS.VERIFIER.STA" $  

DECLARE DIGITAL "SYS.VERIFIER2.STA" $  

DECLARE DECLARATIONS FOR USER DEFINED GLOBAL VARIABLES $  

DECLARE DECIMAL "J-STA" $  

DECLARE DECIMAL "TOP2-STA" (100) $  

DECLARE DECIMAL "TOP-STA" (100) $  

DECLARE DECIMAL "TOP-STA" (1000) $  

DECLARE DIGITAL "TOP2-STA" "ENS-J-STA" (100) $  

DECLARE DECIMAL "K-STA" $  

DECLARE DECIMAL "S-STA" $  

DECLARE DECIMAL "S-STA" $  

DECLARE DIGITAL "SYS.BIG.01-STA" $  

DECLARE DIGITAL "SYS.BIG.02-STA" $  

DECLARE DECIMAL "S-STA" $  

DECLARE DECIMAL "S-STA" $  

DECLARE DECIMAL "S-STA" $  

DECLARE DECIMAL "S-STA" $  

C $  

C USER DEFINED NFE FUNCTIONS $  

C $  

INCLUDE "UPLIB" $  

C $  

DECLARE PROCES $  

C $  

DEFINE PROCEDURE "DUM-STA" $  

RECORD "NOTHING" $  

END "DUM-STA" $  

C $  

DEFINE PROCES $  

C $  

DEFINE PROCEDURE "PUSH" $  

$T-STA" + "PUSH.PRC2" $  

"S-STA" = "PUSH.PRC2" $  

"STACK.GEN" = "STACK.GEN" + 1 $  

"ST" = "STACK.GEN" $  

"SYS.FLAG-STA" = "SYS.TRUE" $  

"SYS.ARRY-FLAG-STA" = "SYS.TRUE" $  

"TOP2-STA"("S-STA") = ("TOP2-STA"("S-STA") + 1) $  

"END-J-STA" = "SYS.TRUE" $  

FOR "S-STA" = 1 THRU 100 BY 1 THEN $  

"SYS.ARRAY-FLAG-STA" = "SYS.TRUE" $  

COMPARE "J-STA", ("TOP2-STA"("S-STA")) $
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<th>ATTRIBUTES AND REFERENCES</th>
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<td>DIAGNOSIS LABEL</td>
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<tr>
<td>EMPTYSTACK</td>
<td>21</td>
<td>TEST LABEL</td>
</tr>
<tr>
<td>END</td>
<td>8</td>
<td>VARIABLE ID, 1-DIMENSIONAL ARRAY, GLOBAL</td>
</tr>
<tr>
<td>END</td>
<td>16</td>
<td>VARIABLE ID, 1-DIMENSIONAL ARRAY, GLOBAL</td>
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<td>T</td>
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</tr>
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<td>VARIABLE ID, 1-DIMENSIONAL ARRAY, GLOBAL</td>
</tr>
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</table>
ERROR/WARNING MESSAGES GENERATED DURING NOPAL SYNTAX ANALYSIS:

- STATISTICS
  - NO. OF ERRORS = 0
  - NO. OF WARNINGS = 0
  - NO. OF STATEMENTS = 30

ERROR/WARNING MESSAGES GENERATED DURING CROSS-REFERENCE:

- STATISTICS
  - NO. OF ERROR MESSAGES = 0
  - NO. OF WARNINGS = 0

ERROR/WARNING MESSAGES GENERATED DURING SEQUENCING AND CODE GENERATION:

** WARNING ** (POSSIBLE INCOMPATIBILITY): GLOBAL VAR \texttt{J} DEFINED AS TARGET IN TEST PUSHP; BUT NEVER USED.

** WARNING ** (POSSIBLE INCOMPATIBILITY): GLOBAL VAR \texttt{J} DEFINED AS TARGET IN TEST POP; BUT NEVER USED.

** WARNING ** (POSSIBLE INCOMPATIBILITY): GLOBAL VAR \texttt{J} DEFINED AS TARGET IN TEST TOP; BUT NEVER USED.

** WARNING ** (POSSIBLE AMBIGUITY): GLOBAL VAR \texttt{J} DEFINED AS TARGET MORE THAN ONCE IN: TEST PUSHP, TEST TOP TH
EY MUST BE UNDER MUTUALLY EXCLUSIVE CONDITION.

** WARNING ** (POSSIBLE AMBIGUITY): GLOBAL VAR \texttt{END} \texttt{J} DEFINED AS TARGET MORE THAN ONCE IN: TEST PUSHP, TEST POP THEY MUS
T BE UNDER MUTUALLY EXCLUSIVE CONDITION.

WARNING MESSAGES GENERATED DURING CODE GENERATION

** WARNING ** (UPFILD DOES NOT EXIST SHOULD BE INCLUDED AT ATLAS COMPILATION TIME).

** WARNING ** (POSSIBLY INCONSISTENT): IN STATEMENT NUMBER 19:

- 1ST SUBSCRIPT OF VARIABLE \texttt{S} \texttt{J} IS A SUBSCRIPTED VARIABLE OR A NON-FREE SUBSCRIPT; RANGE TEST IS NOT PERFORMED.

** STATISTICS **

- NO. OF CODE GENERATION ERRORS = 0
- NO. OF WARNINGS = 1

** STATISTICS **

- NO. OF SEQUENCING ERRORS = 0
- NO. OF WARNINGS = 6
A.2 ACKERMANN'S FUNCTION

Nopal specification which specifies Ackermann's function is given in this section.

Ackermann's function as expressed by recursive equations is:

\[ A(0,n) = n + 1 \]  \hspace{1cm} (A-1)
\[ A(m,0) = A(m-1,1) \]  \hspace{1cm} (A-2)
\[ A(m,n) = A(m-1,A(m,n-1)) \]  \hspace{1cm} (A-3)

Nopal specification is based on the simulation of function calls by means of a stack. It is convenient to imagine that there is an array V of stacks, which is represented in the specification by arrays TOP, LBO, and S. An element V(I) of the array of stacks is represented by LAST(I) which gives the top of the stack V(I), LBO(I) which gives the second element of the stack, and S(I) which gives the rest of the stack.

COMPUTE specifies the computation of the value of Ackermann's function with arguments M, N. To begin, values of M and N are placed on the stack with N being on the top; this is done by defining the value of LAST(1) to be equal to N, the value of LBO(1) equal to M, and the value of S(1) to be a stack with a special symbol -1 signifying the bottom of the stack V(1). Top two elements of the stack V, always contain the arguments for which Ackermann's function needs to be computed at any point in execution. Finally, a single value is left on the stack, and that gives the value of Ackermann's function for arguments M, N. The assertions given by statements 15, 16, and 17 can now be explained as follows:

If the top element of stack V(I-1), i.e. LAST(I-1), is equal zero then it corresponds to Equation A-2. The top two elements (p,0) of stack V(I-1) should be replaced by (p-1,1). This is accomplished in the specification by defining LAST(I) to be 1, LBO(I) to be (LBO(I-1) + 1), and S(I) to be S(I-1).

Similarly, if the second element (from the top) of the stack V(I-1) is zero, it corresponds to
Equation A-1, and the Ackermann's function for the top two elements of the stack evaluates to one plus the top element of the stack. This means popping the stack twice, and pushing the new value on the stack. Thus in the specification, if LBO(I-1) is zero then LAST(I) is equal to (LAST(I) + 1), LBO(I) is equal to TOP(S(I-1)), and S(I) is equal to POP(S(I-1)).

Finally, if it is none of the above two cases, action corresponding to the RHS of Equation A-3 is carried out.

After the specification, sequencing reports are included; they are: inter-test and intra-test sequencing reports. Inter-test sequencing report shows that the test INIT should be performed before the test COMPUTE. Intra-test reports contain sequencing of tests INIT and COMPUTE.
A.2 ACKERMANN'S FUNCTION.

```c
/* NOPAL TEST SPECIFICATION SOURCE INPUT, FILE: SAPLIST */

NOPAL PROCESSOR OPTIONS SPECIFIED: SAPLIST, XREF1, CORE, SEQ, NOXREF2, SOURCE2, TRACE=3, DEBUG=SEQ, CODE

STAT NO.

1  NOPAL PAIN ACKERMANN;
2    BCL S:STACK ARRAY(+);
3    BCL M:STACK;
4     /* TWO TOP ELEMENTS: LAST AND LBO (I.E. LAST BUT ONE) */
5    BCL LBO: INTEGER ARRAY(+);
6    BCL LAST: INTEGER ARRAY(+);

7  TEST INIT;
8    STM;
9    ASRT: N=3  TARGET: M;
10   ASRT: N=2  TARGET: M;
11   ASRT: NEW = NEWSTACK  TARGET: NEW;
12     LOGIC: *BUN;

13  TEST COMPUTE;
14    STM;
15    ASRT: I = SUBS("LAST,LBO,END.Output",*)  TARGET: I;
16    ASRT: IF I=1 THEN LAST(I) = N
17      ELSE IF LBO(I-1) = 0 THEN LAST(I) = LAST(I-1) + 1
18      ELSE IF LAST(I-1) = 0 THEN LAST(I) = 1
19      ELSE LAST(I) = LAST(I-1) - 1
20      TARGET: LAST(I)
21      SOURCE: LAST(I-1), LBO(I-1);
22      ASRT: IF I=1 THEN LBO(I) = M
23      ELSE IF LBO(I-1) = 0 THEN LBO(I) = TOP(S(I-1))
24      ELSE IF LAST(I-1) = 0 THEN LBO(I) = LBO(I-1) - 1
25      ELSE LBO(I) = LBO(I-1)
26      TARGET: LBO(I)
27      SOURCE: S(I-1), LBO(I-1), LAST(I-1);
28      ASRT: IF I=1 THEN S(I) = PUSH(NEW, -1)
29      ELSE IF LBO(I-1) = 0 THEN S(I) = POP(S(I-1))
30      ELSE IF LAST(I-1) = 0 THEN S(I) = S(I-1)
31      ELSE S(I) = PUSH(S(I-1), LBO(I-1)-1)
32      TARGET: S(I)
```

A2 ACKERMANN'S FUNCTION.
17  SOURCE: \texttt{S(1-1)} \texttt{L(1-1)} \texttt{L(1)}; \\
18  ASRT: IF \texttt{L(1)} = -1 THEN \texttt{END}(1) = \texttt{TRUE} \\
19  ELSE \texttt{END}(1) = \texttt{FALSE} \\
20  \texttt{TARG}: \texttt{END}(1) \\
21  \texttt{SOURCE}: \texttt{L(1)}; \\
22  \texttt{LOGIC}: \texttt{DUM}; \\
23  \\
24  \texttt{DIAG DUM}: \texttt{PRINT} = \texttt{MSG}; \\
25  \texttt{MESSAGE MSG}: "\texttt{NOTHING}"; \\
26  \\
27  \texttt{FUNCTION SUBS}, \texttt{TYPE=1}; \\
28  \texttt{FUNCTION TRUE, TYPE=E, VALUE=BIT}; \\
29  \texttt{FUNCTION FALSE, TYPE=E, VALUE=BIT}; \\
30  \texttt{FUNCTION PUSH, TYPE=E, PARAM="S STACK", PARAM="S INTEGER", \texttt{VALUE=STACK}}; \\
31  \texttt{FUNCTION POP, TYPE=E, PARAM="S STACK", \texttt{VALUE=STACK}}; \\
32  \texttt{FUNCTION NEWSTACK, TYPE=E, \texttt{VALUE=STACK}}; \\
33  \texttt{END ACKER:}
A.2 AGKERMANN'S FUNCTION

SEQUENCE OF PROCESSING FOR NORMAL SPECIFICATION ACKERMANN

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<tr>
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<th>VECTOR ORDER</th>
<th>BANK</th>
<th>TYPE</th>
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SEQUENCE OF PROCESSING FOR NORMAL SPECIFICATION ACKERMANN

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INTRA TEST SEQUENCING INIT

ANALYSIS OF THE ADJACENCY MATRIX

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SEQUENCE OF PROCESSING FOR TEST INIT

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</tbody>
</table>
| 11 | 1 | 1 | #S=0001 | ASSERTION | I = SUBS("LAST, LBO, END-1, S")
| | | | | TARGET: I |
| | | | | SOURCE: SUBS |
| 12 | P | 2 | I | VARIABLE | LOCAL |
| | | | | | LOOP-1 STARTS: SUBSCRIPT I ITERATES FROM 1 TO |
| 13 | 4 | 3 | #S=0004 | ASSERTION | IF I=1 THEN S(I) = PUSH(W, m-1) |
| | | | | ELSE IF LBO(I-1)=O THEN S(I) = POP(S(I-1)) |
| | | | | ELSE IF LBO(I-1)=0 THEN S(I) = S(I-1) |
| | | | | ELSE S(I) = TOP(S(I-1), LBO(I-1)-1) |
| | | | | TARGET: S |
| | | | | SOURCE: I, PUSH, POP, NEW |
| 14 | 14 | 4 | S | SUBSCRIPT_XA | LOCAL |
| 15 | 3 | 5 | #S=0003 | ASSERTION | IF I=1 THEN LBO(I) = M |
| | | | | ELSE IF LBO(I-1)=O THEN LBO(I) = TOP(S(I-1)) |
| | | | | ELSE IF LBO(I-1)=C THEN LBO(I) = LBO(I-1)-1 |
| | | | | ELSE LBO(I) = LBO(I-1) |
| | | | | TARGET: LBO |
| | | | | SOURCE: I, TOP, M, S |
| 16 | 10 | 6 | LBO | SUBSCRIPT_XA | LOCAL |
A.2 ACKERMANN'S FUNCTION

17 2 7 $SS\_W0002$ ASSERTION

18 5 7 $SS\_W0005$ ASSERTION

19 11 8 LAST SUBSCRIPT_VA LOCAL

20 20 8 END_1 SUBSCRIPT_VA GLOBAL / TARGET /

LLOOP SUMMARY TABLE:

LLOOP-1 FIRST NODE IS 13 LAST NODE IS 20 SUBSCRIPT IS 1
A.3 BAND-WIDTH METER

The main module BWM specifies the application of a voltage source with frequencies in a range with a given step size to a UUT. For each application of a frequency, the gain of voltages (ratio of output voltage to input voltage) across the UUT is measured. A table corresponding to the applied frequencies and the measured gains is printed out. The devices are represented by means of abstract structures: gain measurement device is represented by the structure GD, and frequency source by the structure FS. A call is issued to ACCESS_GAIN_DEVICE whenever the value of GAIN, a field in the structure GD, is accessed (before statement 24); and similarly, a call is issued to SAVE_FREQ_SOURCE in the case of structure FS (after statements 16, 17, and 18). The assertions in the specification are self explanatory.
/* Nopal test specification source input, file: saplist */

nopal processor options specifier: saplist, ref1, core, seq, noref2, source2, trace=3, debug=seg

stmt no.

1 nopal main bwp;

/* abstract structures as devices */
2 dcl 1 gb: gain_device array(4);
3 2 gain: real;
4 dcl 1 fs: freq_source array(4);
5 2 freq: real;
6 2 in1: integer;
7 2 in2: integer;

test init;
8 stmt;
9 asrt: min = 100 target: min;
10 asrt: min = 2000 target: min;
11 asrt: in2 = 5 target: in2;
12 asrt: in2 = 5 target: in2;
13 logic: end;

test chartreg;
14 stmt;
15 asrt: i = sum("freq, in1, in2, ptr1, ptr2, ptr3, ptr4", x, y, gains, err"
16 x30) target: i;
17 asrt: freq(i) = freq + (max - min)/10 target: freq(i);
18 asrt: in1(i) = 5 target: in1(i);
19 asrt: in1(i) = 5 target: in1(i);

/* parameters for gain device */
20 asrt: ptr1 = 1 target: ptr1;
21 asrt: ptr2 = 1 target: ptr2;
22 asrt: ptr3 = 1 target: ptr3;
23 asrt: ptr4 = 1 target: ptr4;

/* causes freqency freq(i) to be applied */
24 asrt: x(i) = freq(i) target: x(i)
25 source: freq(i);

/* causes gain measurements to be performed */
26 asrt: y(i) = gains target: y(i)
27 source: gains;

/* chart: function which prints out a table */
28 asrt: err(x) = chart(x(i), y(i)) target: err(x)
29 source: x(i), y(i);

logic: end;
27 diag run: print = msg;
28 message msg: "nothing ";
29 function sub5, type=E;
30 function true, type=E;
31 function chart, type=E;
32 end bwp;
### Weighed Adjacency Matrix for Nodal Specification BW

|     | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 0 |
| 1   | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 2   | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 3   | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 4   | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 5   | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 6   | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 7   | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 8   | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 9   | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 10  | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

### Sequence of Processing for Nodal Specification BW

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<th>Order</th>
<th>Rank</th>
<th>Type</th>
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## A.3 BANDWIDTH METER

**Sequencing for Knap Specification BNR**

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**Intra Test Sequencing Initial Analysis of Adjacency Matrix**

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**Sequencing for Processing Test Initial**

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<td>A.3 BAND WIDTH METER</td>
<td>126</td>
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```
INTRA TEST SEQUENCING CHART

ASSEREOION 13 = 3
TARGET: 13;

ASSEREOION 14 = 4
TARGET: 14;

DIAGNOSIS 8 8 1
VARIABLE 9 9 1
GLOBAL/TARGET:

VARIABLE 10 10 1 11
GLOBAL/TARGET:

VARIABLE 12 12 1 11
GLOBAL/TARGET:

VARIABLE 13 13 1 14
GLOBAL/TARGET:

ANALYSIS OF THE ADJACENCY MATRIX

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<td>SUBS</td>
</tr>
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<td>55_0DDC119</td>
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```
```
ORDER  VELT  ORDER  INDEX  VECTOR  RANK  NAME  TYPE  TEXT
1      15     0      SUBS    VARIABLE   GLOBAL / SOURCE /
2      15     0      FMIN    VARIABLE   GLOBAL / SOURCE /
3      16     0      FMAX    VARIABLE   GLOBAL / SOURCE /
4      18     0      I1      VARIABLE   GLOBAL / SOURCE /
5      20     0      I2      VARIABLE   GLOBAL / SOURCE /
6      24     0      I3      VARIABLE   GLOBAL / SOURCE /
7      26     0      I4      VARIABLE   GLOBAL / SOURCE /
8      31     0      CHART   VARIABLE   GLOBAL / SOURCE /
9      1      1      SS_WDOC1  ASSERTION  I
   * SUBSET "FREQ,IN1,IN2,PTR1,OD,PTR2,OD,PTR3,OD,PTR4,OD,2,Y,GAIN,ERR",S
   TARGET: I
   SOURCE: SSMS;
10     14     2      I      VARIABLE   LOCAL

LOOP-1 STARTS: SUBSCRIPT I ITERATES FROM 1 TO 30
11     2      3      SS_WDOC2  ASSERTION  FREQ(1) = FMIN+(FMAX-FMIN)*I/10
   TARGET: FREQ
   SOURCE: I, FMIN, FMAX;
<table>
<thead>
<tr>
<th>Line</th>
<th>Column</th>
<th>Symbol</th>
<th>Type</th>
<th>Description</th>
</tr>
</thead>
</table>
| 12   | 3      | $SS_WOOC3$ | ASSERTION  | $INT(1) = 11$  
|      |        |          |            | TARGET:  $IN1$  
|      |        |          |            | SOURCE:  $1$, $11$ |
| 13   | 4      | $SS_WOOC4$ | ASSERTION  | $INT(2) = 12$  
|      |        |          |            | TARGET:  $IN2$  
|      |        |          |            | SOURCE:  $1$, $12$ |
| 14   | 5      | $SS_WOOC5$ | ASSERTION  | $PTR1_6B(2) = 11$  
|      |        |          |            | TARGET:  $PTR1_6B$  
|      |        |          |            | SOURCE:  $1$, $11$ |
| 15   | 6      | $SS_WOOC6$ | ASSERTION  | $PTR2_6B(1) = 12$  
|      |        |          |            | TARGET:  $PTR2_6B$  
|      |        |          |            | SOURCE:  $1$, $12$ |
| 16   | 7      | $SS_WOOC7$ | ASSERTION  | $PTR3_6B(1) = 13$  
|      |        |          |            | TARGET:  $PTR3_6B$  
|      |        |          |            | SOURCE:  $1$, $13$ |
| 17   | 8      | $SS_WOOC8$ | ASSERTION  | $PTR4_6B(1) = 14$  
|      |        |          |            | TARGET:  $PTR4_6B$  
|      |        |          |            | SOURCE:  $1$, $14$ |
| 18   | 17     | $FREQ$   | SUBSCRIPT  | $GLOBAL / TARGET$  
| 19   | 19     | $INT1$   | SUBSCRIPT  | $GLOBAL / TARGET$  
| 20   | 21     | $INT2$   | SUBSCRIPT  | $GLOBAL / TARGET$  
| 21   | 22     | $PTR1_6D$ | SUBSCRIPT  | $GLOBAL / TARGET$  
| 22   | 23     | $PTR2_6D$ | SUBSCRIPT  | $GLOBAL / TARGET$  
| 23   | 25     | $PTR3_6D$ | SUBSCRIPT  | $GLOBAL / TARGET$  
| 24   | 27     | $PTR4_6D$ | SUBSCRIPT  | $GLOBAL / TARGET$  
| 25   | 9      | $SS_WOOC9$ | ASSERTION  | $X(1) = FREQ(1)$  
|      |        |          |            | TARGET:  $X$  
|      |        |          |            | SOURCE:  $1$, $FREQ$ |
A.3 BAND-WIDTH METER

SUBSCRIPT_va GLOBAL / SOURCE /

SUBSCRIPT_va GLOBAL / SOURCE /

SUBSCRIPT_va LOCAL

SUBSCRIPT_va GLOBAL / SOURCE /

ASSERTION Y(I) = GAIN(I)
TARGET: Y
SOURCE: I, GAIN;

SUBSCRIPT_va LOCAL

ASSERTION ERR(I) = CHART(X(I), Y(I))
TARGET: ERR
SOURCE: I, X, Y, CHART;

PRINT = MSG;

DIAGNOSES

SUBSCRIPT_va GLOBAL / TARGET /

LOOP-1 ENDS;

LCP SUMMARY TABLE:
LOOP-1 FIRST NODE IS 11 LAST NODE IS 34 SUBSCRIPT IS I
The specification for GAIN.DEVICE, given below, has only one modfun called ACCESS.GAIN.DEVICE. The modfun takes voltage measurements across pins (11,12) and (13,14). The ration of the two measurements defines the value of GAIN. It depends on two functions: VOLTMETER and MICROVOLTMETER to take the actual measurements.
/* NOPAL TEST SPECIFICATION SOURCE INPUT, FILE: SAPLIST */

NOPAL PROCESSOR OPTIONS SPECIFIED: SAPLIST, MSREF, CORE, SEQ, NOREF2, SOURCE2, TRACE=3, DEBUG=ALL, LINE=20000

### STAT NO.

```
1 NOPAL MODULE GAIN_DEVICE;

2 NODFUN ACCESS_GAIN_DEVICE (11:5 CNH, 12:5 CNH, 13:5 CNH, 14:5 CNH, GAIN:7 REAL);

3 MEAS;

4 CONJ: (11, 12) = MICROVOLTMETER(V1) &
(13, 14) = VOLTMETER(V2);

5 TARGET: V1, V2;

6 ASRT: GAIN = V2 / V1 TARGET: GAIN

7 SOURCE: V1, V2;
```

LOGIC: NOTHING;

DIAG NOTHING;

PRINT=SS5;

MESSAGE MSG1;

TEST = "NOTHING";

WUT_PT: 11, ALIAS=11;

W1_PT: 12, ALIAS=12;

WUT_PT: 13, ALIAS=13;

W2_PT: 14, ALIAS=14;

FUNCTION SMS, TYPE=R;

FUNCTION TRUE, TYPE=S;

FUNCTION VOLTMETER, TYPE=M;

FUNCTION MICROVOLTMETER, TYPE=M;

FUNCTION SUM, TYPE=E;

END GAIN_DEVICE;
INTRA TEST SEQUENCING ACCESS_GAIN:
ANALYSIS OF THE ADJACENCY MATRIX

<table>
<thead>
<tr>
<th>ORDER</th>
<th>NAME</th>
<th>TYPE</th>
<th>TEXT</th>
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</thead>
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<tr>
<td>1</td>
<td>SP_WOO1</td>
<td>CONJUNCTION</td>
<td>(&lt;15, 12&gt; = MICROVOLTMETR(V1) ) &amp; (&lt;13, 14&gt; = VOLTMETR(V2))</td>
</tr>
<tr>
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<td>TARGET: V2, V1;</td>
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<tr>
<td>2</td>
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A3 BAND-WIDTH METER
The specification for FREQSOURCE defines a function SAVE_FREQSOURCE which specifies the application of a frequency source by means of the function FREQ_GEN. The voltage and frequency to be applied are specified by the input parameters. An error is issued if the parameters specify a frequency which falls out of range of the instrument.
A.3

BAND WIDTH METER

1
2  NOPAL MODULE FREQ_SOURCE;
3  MOD/FUN SAVE_FREQ_SOURCE(FREQ:REAL,V:REAL,IN1:S,IN2:S,CH:R,CH2:R);
4  ST IN;
5  CONJ: IF RANGE>0 THEN <INT1,IN2> = FREQ_GEN(FREQ,V,RANGE);
6  ASRT: IF FREQ<F1 & FREQ>F2 THEN RANGE = 1
7  ELSE IF FREQ<F2 & FREQ>F3 THEN RANGE = 2
8  ELSE RANGE = 0 TARGET: RANGE;
9  ASRT: RANGE > 0;
10  ASRT: F1 = 10000 TARGET:F1;
11  ASRT: F2 = 1000 TARGET:F2;
12  ASRT: F3 = 10 TARGET:F3;
13  LOGIC: $01;
14  DIA1 PT:
15  PRINT = MSG;
16  PARAMETER = FREQ;
17  MESSAGE MSG: TEXT = "FREQUENCY OUT OF RANGE (P)";
18  FUNCTION FREQ_GEN, TYPE=3;
19  WUT PT: IN1;
20  WUT PT: IN2;
21  END FREQ_SOURCE;
### INTRA TEST SEQUENCING SAVE_FREQ

ANALYSIS OF THE ADJACENCY MATRIX

<table>
<thead>
<tr>
<th>ORDER</th>
<th>ORDER INDEX VECTOR</th>
<th>RANK</th>
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<td>1</td>
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<td>$s_{0000}$</td>
<td>ASSERTION</td>
<td>$F_1 = 10000$</td>
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<td>$s_{0000}$</td>
<td>ASSERTION</td>
<td>$F_2 = 100$</td>
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<td>TARGET: $F_2$</td>
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<td>ASSERTION</td>
<td>$F_3 = 10$</td>
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<td>$V$</td>
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<td>$IN_2$</td>
<td>VARIABLE</td>
<td>LOCAL</td>
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<td>7</td>
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<td>$IN_1$</td>
<td>VARIABLE</td>
<td>LOCAL</td>
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<td>8</td>
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<td>$F_3$</td>
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<td>LOCAL</td>
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<td>9</td>
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<td>1</td>
<td>$F_2$</td>
<td>VARIABLE</td>
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<tr>
<td>10</td>
<td>13</td>
<td>1</td>
<td>$F_1$</td>
<td>VARIABLE</td>
<td>LOCAL</td>
</tr>
<tr>
<td>11</td>
<td>2</td>
<td>0</td>
<td>$s_{0000}$</td>
<td>ASSERTION</td>
<td>IF FREQ &lt; FREQ &lt; $F_2$ THEN RANGE = 1</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>ELSE IF FREQ &lt; $F_2$ THEN RANGE = 2</td>
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<td></td>
<td></td>
<td></td>
<td>ELSE RANGE = 0</td>
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<td></td>
<td></td>
<td>TARGET: RANGE</td>
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<td></td>
<td></td>
<td></td>
<td>SOURCE: FREQ, $F_3$, $F_2$, $F_1$</td>
</tr>
<tr>
<td>12</td>
<td>9</td>
<td>3</td>
<td>RANGE</td>
<td>VARIABLE</td>
<td>LOCAL</td>
</tr>
<tr>
<td>13</td>
<td>1</td>
<td>4</td>
<td>$s_{0000}$</td>
<td>CONJUNCTION</td>
<td>IF RANGE &gt; 0 THEN ($IN_1$, $IN_2$) = FREQ_GEN(FREQ, $V$, RANGE)</td>
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<tr>
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<td></td>
<td></td>
<td>SOURCE: $V$, RANGE, FREQ;</td>
</tr>
<tr>
<td>14</td>
<td>3</td>
<td>4</td>
<td>$s_{0000}$</td>
<td>ASSERTION</td>
<td>RANGE &gt; 0</td>
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<tr>
<td></td>
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<td></td>
<td></td>
<td></td>
<td>SOURCE: RANGE;</td>
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</table>
A.4 FILE INPUT-OUTPUT

This example illustrates the updating of an inventory file, named INV, based on transactions contained in a sequential file, called TRANS. A record in TRANS has two fields: KEY and an array A. A record in INV is found corresponding to the KEY in each of the records in TRANS and is updated based on the sum of the corresponding array A. General functions ACCESS and IACCESS are used to read, and SAVE and ISAVE to store, records from SAM and ISAM files respectively.

Corresponding sequence reports and Equate-atlas code are given after the specification.
/* NOPAL TEST SPECIFICATION SOURCE INPUT, FILE: SAPLIST */

NOPAL PROCESSOR OPTIONS SPECIFIED: SAPLIST, REF1, CORE, SEQ, NORREF2, SOURCEZ, TRACE=3, DEBU=ALL

SMT NO.

1  NOPAL SPEC 10;
2   DCL 1 TRANS: FILE;
3     2 W: RECORD ARRAY(*);
4       3 A: REAL ARRAY(20);
5   DCL 1 OLD_INR: FILE;
6       2 OLD_A: RECORD ARRAY(*);
7       3 OLD_B: REAL;
8       3 OLD_C: REAL;
9   DCL 1 NEW_INR: FILE;
10     2 NEW_A: RECORD ARRAY(*);
11     3 NEW_B: REAL;
12     3 NEW_C: REAL;
13   TEST PROCESS TRANS;
14     REL;  
15     ASRT: I = SUBSTR "NEW_A,NEW_E,NEW_B,PTG,OLD_A,PTG,OLD_B,KEY,A,SUMVAL,  
16     " OLD_A,OLD_E,OLD_B,NEW_A,NEW_B,PTG, "I" ;
17     TARGET: I;
18     ASRT: J = SUBSTR "X", 00; TARGET: J;
19     /* READ RECORD A */  
20     ASRT: SUMVAL(I) = SUM(A(I,J),J) TARGET: SUMVAL(I)
21     SOURCE: A(I,J);  
22     ASRT: X(I) = KEY(I) TARGET: X(I)
23     SOURCE: KEY(I);  
24     /* UPDATE RECORD C */  
25     ASRT: PTR_OLD_IR(I) = KEY(I) TARGET: PTR_OLD_IR(I)
26     SOURCE: KEY(I);  
27     ASRT: NEW_B(I) = OLD_B(I) + SUMVAL(I) TARGET: NEW_B(I)
28     SOURCE: SUMVAL(I);  
29     ASRT: NEW_C(I) = OLD_C(I) TARGET: NEW_C(I)
30     SOURCE: OLD_C(I);  
31     ASRT: PTR_NEW_IR(I) = KEY(I) TARGET: PTR_NEW_IR(I)
32     SOURCE: KEY(I);  
33     LOGIC: IDUM;
34     DIA M: PRINT = MS4;
35     MESSAGE MS4: "NOTHING";
36     FUNC SUBT: TYPE=E;
37     FUNC SUM: TYPE=E;
38  ENB 10;
### Weighted Adjacency Matrix for Nopal Specification 10

<table>
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<tr>
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<th>2</th>
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### Sequence of Processing for Nopal Specification 10

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INTRA TEST SEQUENCING PROCEDURE

ANALYSIS OF THE ADJACENCY MATRIX

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</tr>
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<td>j</td>
<td>VARIABLE</td>
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</tr>
</tbody>
</table>

**LOOP-1**

**Starts:** SUBSCRIPT 1 iterates from 1 to 4

- **R**: SUBSCRIPT VA
- **a**: GLOBAL/SOURCE
- **i**: KEY SUBSCRIPT VA
- **j**: KEY

**SOURCE:**

- **KEY**: $m_nWOOC4
- **KEY**: $m_nWOOC5
- **KEY**: $m_nWOOC6
- **KEY**: $m_nWOOC7

**TARGET:**

- **PTR_OLD_IR(1)**: $m_nWOOC4
- **PTR_OLD_IR(1)**: $m_nWOOC5
- **PTR_OLD_IR(1)**: $m_nWOOC6
- **PTR_OLD_IR(1)**: $m_nWOOC7
A.4 FILE INPUT-OUTPUT

18 20 6 OLD_B SUBSCRIPT_VA GLOBAL / SOURCE /
19 22 8 OLD_C SUBSCRIPT_VA GLOBAL / SOURCE /
20 24 8 OLD_D SUBSCRIPT_VA GLOBAL / SOURCE /
41 7 9 BK_WOODP ASSERTION NEW_C(1) = OLD_C(1)
TARGET: NEW_C
SOURCE: 1, OLD_C;
42 8 9 BK_WOODB ASSERTION NEW_D(1) = OLD_D(1)
TARGET: NEW_D
SOURCE: 1, OLD_D;
43 23 10 NEW_C SUBSCRIPT_VA GLOBAL / TARGET /
44 25 10 NEW_D SUBSCRIPT_VA GLOBAL / TARGET /
45 15 11 A SUBSCRIPT_VA GLOBAL / SOURCE /

LOOP-2 STARTS; SUBSCRIPT J ITERATES FROM 1 TO 10
26 3 2 BK_WOODS ASSERTION SUMVAL(1) = SUMA(1, J, J)
TARGET: SUMVAL
SOURCE: 1, J, SUM, A;
LOOP-2 ENDS;
27 16 3 SUMVAL SUBSCRIPT_VA LOCAL
48 6 4 BK_WOODC ASSERTION NEW_D(1) = OLD_D(1) + SUMVAL(1)
TARGET: NEW_D
SOURCE: 1, SUMVAL, OLD_D;
69 10 5 SUM DIAGNOSES PRINT = MSG;
30 21 5 NEW_B SUBSCRIPT_VA GLOBAL / TARGET /
31 31 6 NEW_IA SUBSCRIPT_VA GLOBAL / SOURCE /
32 32 7 NEW_IA VARIABLE GLOBAL / SOURCE /
LOOP-1 ENDS;

LOOP SUMMARY TABLE:
LOOP-7 FIRST NODE IS 9 LAST NODE IS 32 SUBSCRIPT IS 1
LOOP-2 FIRST NODE IS 26 LAST NODE IS 26 SUBSCRIPT IS 1
BEGIN ENLARGE PROGRAM "10"$ NAMERS INBER

*** TEST MODULES ***
"PROCESTRAN" - 1

*** DIAGNOSIS ***
"DUM" - 1

DECLARATIONS OF SYSTEM VARIABLES
DECLARE DIGITAL LIST "SYS-BFAG-FLAG"(11)
DECLARE DIGITAL LIST "SYS-S-TIME"$ 
DECLARE DIGITAL LIST "SYS-B-NAME"$ 
DECLARE DIGITAL LIST "SYS.B-NAME"$ 
DECLARE DIGITAL LIST "SYS.B-NAME"$ 
DECLARE DIGITAL LIST "SYS.CLOCK"(6)
DECLARE DIGITAL LIST "SYS.CLOCK"(6)
DECLARE DIGITAL LIST "SYS.CLOCK"(6)
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DECLARE DIGITAL LIST "SYS.CLOCK"(6)
DECLARE DECIMAL; LIST; "OLD-C" (2) $
DECLARE DECIMAL; LIST; "NEW-C" (2) $
DECLARE DECIMAL; LIST; "OLD-P" (2) $
DECLARE DECIMAL; LIST; "NEW-P" (2) $
DECLARE DECIMAL; LIST; "PTM-NEW-PR" (2) $

C SYSTEM UTILITY ROUTINES $
DEFINE PROCEDURE; "GET-TIME"$
READTIME; "SYS.CLOCK" (1) ALL), SYS-CLOCK$
"SYS.CLOCK" * 60 + "SYS.CLOCK" (2) +
"SYS.CLOCK" (3) $
END "GET-TIME" $
DECLARE DECIMAL; "J.1" $
DECLARE DECIMAL; "J.1" $
DECLARE DECIMAL; LIST; "SUMVAL.1" (2) $
DECLARE DECIMAL; "SYS.BIND.1" $
DECLARE DECIMAL; "END-1.1"$

C 3 USER DEFINED ATE FUNCTIONS $
C 3 INCLUDE "UPLIB"$

C******************************************************************************
C DIAGNOSES PROCES $
C******************************************************************************

1100 DEFINE PROCEDURE; "SUM"$
RECORD "NOTHENA" $
"SYS.FLAG-FLAG" (4) = "SYS.SELECTED"$
END "SUM"$

C******************************************************************************
C TEST PROCES $
C******************************************************************************

1100 DEFINE PROCEDURE; "PROCESSTRANS"$
"SYS.FLAG" = "SYS.TRUE"$
"SYS.SELECT-FLAG" = "SYS.TRUE"$
PERFORM "GET-TIME"$
"SYS-NAME" = "SYS.TIME"$
RECORD """" After step 1100 """" entered test procedure ",
""PROCESSTRANS" at ","PTI.TIME"$

C WAVEFORM SIM-WG01 follows: ********************************************$
C CODE FOR SUBSCRIPTS & PARENT DECLS.$
C WAVEFORM SIM-WG02 FCG01x: ********************************************$
C CODE FOR SUBSCRIPTS & PARENT DECLS.$
"END-1.1" = "SYS.TRUE"
"SYS.WRITER" = "SYS.FALSE"
FOR "J.1" + 1 THRU 16 DO UT THEN 1
"SYS.WRITER" = NOT("SYS.WRITER")$
COMPARE "SYS.WRITER" EQ "SYS.TRUE"
GO TO STEP 1105 IF NO G0$
"J.1" = 1$
GO TO STEP 1110$
"J.1" = 2$
"ISAVE.PRN" = 04 B
PERFORM "ISAVE" B
COMPARE "END=1.1", "SYS.TRUE" B
GO TO STEP 1135 IF N0GO B
END FOR B
1135 "SYS.TEST-FLAG"(1) = "SYS.TESTER" B
PERFORM "GET.TIME" B
RECORD "** AFTER STEP 1135 RETURNING FROM TEST PROCEDURE "", "**", "PROCESTRANS" AT "**, "PROCESTRANS" B
END "PROCESTRANS" B
****************************************************************************************************************************
C system variable initialization and first entry point
****************************************************************************************************************************
E 1200 PERFORM "GET.TIME" B
RECORD "TIME TESTING USING IO" B
RECORD "SYS.CLOCK"(4), "DATE #/", "SYS.CLOCK"(5), "#/", "SYS.CLOCK"(6), "#/ TIME", "#/, TIME" B
"SYS.T+" = "SYS.TIME" B
FOR "SYS.1" = 1 THRU "SYS.ABSIZE" THEN B
"SYS.CLOCK-FLAG"("SYS.1") = "SYS.NOT SELECTED" B
"SYS.TESTS IN CONJ"("SYS.1") = 0 B
END FOR B
FOR "SYS.1" = 1 THRU "SYS.TESTS" THEN B
"SYS.TEST-FLAG"("SYS.1") = "SYS.NOT TESTED" B
END FOR B
C BEGINNING OF TESTING B
C B
CONTROL PRECEDING THE CALL ON THE TEST MODULE "PROCESTRANS" B
1300 "SYS.FLAG" = "SYS.TRUE" B
PERFORM "PROCESTRANS" B
C B
1400 PERFORM "GET.TIME" B
RECORD "FINISHED TESTING AT", "#/, TIME" B
"SYS.T+" = "SYS.TIME" - "SYS.T." B
"SYS.CLOCK"(1) = INT ("SYS.TIM"/3600) B
"SYS.T." = "SYS.TIM" - 3600*"SYS.CLOCK"(1) B
"SYS.CLOCK"(2) = INT ("SYS.TIM"/60) B
"SYS.CLOCK"(3) = "SYS.TIM" - 60*"SYS.CLOCK"(2) B
RECORD "DURATION", "#/, TIME" B
DELETE ALL B
1405 RECORD "DO YOU WISH TO RUN THIS PROGRAM AGAIN?", "YES-NO" B
WAIT FOR MANUAL-DATA-NO-NOGO B
GO TO STEP 1410 IF NOGO B
RECORD "IP" B
GO TO STEP 1200 B
1410 RECORD "TERMINATE EQUATE PROGRAM "10" !IP" B
1415 FINISH B
TERMINATE EQUATE PROGRAM "10" B

---

A.4 FILE INPUT-OUTPUT
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