COMPUTATION OF SUPERSONIC SPACE ENCIRCLING FLOW OF BLUNT-NOSED ETCA(U)
JUN 79 Z YUAN, W RUAN, Z XICHANG

UNCLASSIFIED

END
<table>
<thead>
<tr>
<th>DISTRIBUTION STATEMENT A</th>
<th>DISTRIBUTION STAMP</th>
</tr>
</thead>
<tbody>
<tr>
<td>FOR PUBLIC RELEASE;</td>
<td></td>
</tr>
<tr>
<td>DISTRIBUTION UNLIMITED</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>ACCESSION FOR</th>
<th>DISTRIBUTION /</th>
</tr>
</thead>
<tbody>
<tr>
<td>NTIS GRAI</td>
<td>AVAILABILITY CODES</td>
</tr>
<tr>
<td>DTIC TAB</td>
<td></td>
</tr>
<tr>
<td>UNANNOUNCED</td>
<td></td>
</tr>
<tr>
<td>JUSTIFICATION</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>DATE RECEIVED IN DTIC</th>
<th>9 11 13 243</th>
</tr>
</thead>
</table>

<table>
<thead>
<tr>
<th>DATE ACCESSIONED</th>
<th>DDC RECEIVED JAN 28 1980</th>
</tr>
</thead>
</table>

<table>
<thead>
<tr>
<th>DISTRIBUTION STAMP</th>
<th>DATE RECEIVED IN DTIC</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>9 11 13 243</td>
</tr>
</tbody>
</table>

PHOTOGRAPH THIS SHEET AND RETURN TO DTIC-DDA-2

DTIC FORM OCT 79 70A DOCUMENT PROCESSING SHEET
FOREIGN TECHNOLOGY DIVISION

COMPUTATION OF SUPERSONIC SPACE ENCIRCLING FLOW OF BLUNT-NOSED BODY

By

Zhu Youlan, Wang Ruquan, Zhong Xichang

Approved for public release; distribution unlimited.
EDITED TRANSLATION

FTD-ID(RS)T-0645-79 21 June 1979

MICROFICHE NR: AID '79 C 000 822

COMPUTATION OF SUPersonic SPACE ENCIRCLING FLOW OF BLUNT-NOSED BODY

By: Zhu Youlan, Wang Ruquan, Zhong Xichang

English pages: 27

Source: Li Hsueh, Nr. 4, 1977, pp. 270-282

Country of Origin: China

Translated by: LINGUISTIC SYSTEMS, INC.
F33657-78-D-0618
H. P. Lee

Requester: FTD/TQTA

Approved for public release; distribution unlimited.

THIS TRANSLATION IS A RENDITION OF THE ORIGINAL FOREIGN TEXT WITHOUT ANY ANALYTICAL OR EDITORIAL COMMENT. STATEMENTS OR THEORIES ADVOCATED OR IMPLIED ARE THOSE OF THE SOURCE AND DO NOT NECESSARILY REFLECT THE POSITION OR OPINION OF THE FOREIGN TECHNOLOGY DIVISION.

PREPARED BY:

TRANSLATION DIVISION
FOREIGN TECHNOLOGY DIVISION
WP-afb, OHIO.

FTD-ID(RS)T-0645-79

Date 21 Jun 1979
Computation of Supersonic Space Encircling Flow of Blunt-Nosed Body

Zhu Youlan, Wang Ruquan, Zhong Xichang

Computer Technology Research Institute
The Chinese Academy of Science

Contents

1. Introduction 1
2. The Way of Relaying Questions 2
3. Numerical Solution 5
4. Computation Results 17
   Bibliography 27
Research Report

Computation of Supersonic Space Encircling Flow of Blunt-Nosed Body

Zhu Youlan, Wang Ruquan, Zhong Xichang

Computer Technology Research Institute
The Chinese Academy of Sciences

I. Introduction

Since the 1950's, for numerical solution of the problems of supersonic encircling inviscid flow of blunt-nosed body, a number of different methods has been developed. Of them one category is stationary method and the other is nonstationary method. In the category of stationary method, there are method of finite difference, method of integral relation and method of lines. Applied to smooth bodies, all these methods can have satisfactory results. Only because the nonstationary method must take steady process for time, it has to consume a great deal of machine time. As for the method of finite difference, in order to have very precise result, it needs quite a number of net points and large machine storage capacity, and it uses more computing time. Compared with these conditions, the method of lines has more points of excellence. For instance, its computing method is simple, the storage capacity it needs is small and, using only a few rays, it can bring about satisfactory result. This article is intended to report our work of using the method of lines to compute supersonic encircling flow of blunt-nosed body.

We use the method of lines to make broad computation of supersonic
encircling flow of blunt-nosed body. The objects we computed include ellipsoid of various axial ratio and disk-analogous bodies. The range of incoming flow M number is 1.5 to infinity. Under the condition of axial symmetry, besides the frozen gas of $\gamma = 1.4$, we have also computed balanced and unbalanced air.

In addition, we also use the method of lines to compute the flow in supersonic zone and the pointed conical encircling flow with attack angle.

To the results of computation, we make multi-way check, and all show that the results of computation by using method of lines are considerably satisfactory.

2. The Way of Relaying Questions

2.1 Fundamental Equation

To consider the inviscid and non-heat conducting air flow. The equation of aerodynamics in spherical coordinate system $(r, \theta, \varphi)$ is:

$$
\frac{1}{r \sin \theta} \left[ \frac{\partial}{\partial r} \left( \rho v r \sin \theta \right) + \frac{\partial}{\partial \theta} \left( \rho v r \sin \theta \right) + \frac{\partial}{\partial \varphi} \left( \rho w r \right) \right] = 0
$$

$$
\frac{d u}{d s} - \frac{v^2 + w^2}{r} + \frac{1}{\rho} \frac{\partial \rho}{\partial r} = 0
$$

$$
\frac{d v}{d s} + \frac{u v}{r} - r \cot \theta \frac{\partial \varphi}{\partial r} + \frac{1}{\rho r} \frac{\partial \rho}{\partial \theta} = 0
$$

$$
\frac{d w}{d s} + \frac{u w}{r} + r \cot \theta \frac{\partial \varphi}{\partial \theta} + \frac{1}{\rho r \sin \theta} \frac{\partial \rho}{\partial \varphi} = 0
$$

$$
\frac{d \rho}{d s} - c \frac{\partial \rho}{d s} = 0
$$

2
Here \( \frac{\partial}{\partial t} = r \frac{\partial}{\partial r} + \frac{1}{r} \frac{\partial}{\partial \theta} + \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi} \), \( u, v, w \) are component when speed is along \( r, \theta, \phi \) direction. \( p \) is pressure, \( \rho \) is density and \( c \) is speed. In the equation, all quantity are dimensionless quantity and their dimension factor are respectively

\[
p \sim \rho_\infty V_\infty^2, \quad \rho \sim \rho_\infty, \quad u, v, w \sim V_\infty, \quad r \sim R_0.
\]

Here \( \rho_\infty \) indicates the quantity of incoming flow and \( R_0 \) is the curvature radius at the top of the subject.

For the convenience of computing, we introduce the following transformation of coordinate,

\[
\xi = \frac{r - G(\theta, \varphi)}{F(\theta, \varphi) - G(\theta, \varphi)}, \quad \theta = \theta, \quad \varphi = \varphi
\]

Here \( r = G(\theta, \varphi) \) \& \( r = F(\theta, \varphi) \) are equations respectively of the object surface and shock wave. Obviously, in \( (\xi, \theta, \varphi) \) coordinate system, the shock wave is in the plane of \( \xi = 1 \) and the surface of the object is in the plane of \( \xi = 0 \). Let

\[
a = -(G_\theta + \xi \xi_\theta), \quad b = -\frac{1}{\sin \theta} (G_\theta + \xi \xi_\theta), \quad \epsilon = F - G
\]

Due to

\[
\frac{\partial}{\partial r} = \frac{1}{\xi} \frac{\partial}{\partial \xi}, \quad \frac{\partial}{\partial \theta} = \frac{\alpha}{\xi} \frac{\partial}{\partial \xi} + \frac{\partial}{\partial \theta}
\]

\[
\frac{1}{\sin \theta} \frac{\partial}{\partial \phi} = \frac{\beta}{\xi} \frac{\partial}{\partial \xi} + \frac{1}{\sin \theta} \frac{\partial}{\partial \phi}
\]

so equation (2.1) can be rewritten into

\[
\begin{align*}
\alpha \frac{\partial \rho}{\partial \xi} + \rho \left( r \frac{\partial u}{\partial \xi} + \frac{\alpha}{\rho} \frac{\partial \epsilon}{\partial \xi} + \rho \frac{\partial w}{\partial \xi} \right) = F_1, \\
\alpha \frac{\partial u}{\partial \xi} + \frac{r}{\rho} \frac{\partial p}{\partial \xi} = F_1
\end{align*}
\]

\[
\begin{align*}
\alpha \frac{\partial v}{\partial \xi} + \frac{\alpha}{\rho} \frac{\partial p}{\partial \xi} = F_1, \\
\alpha \frac{\partial w}{\partial \xi} + \frac{\beta}{\rho} \frac{\partial p}{\partial \xi} = F_1, \\
\alpha \left( \frac{\partial p}{\partial \xi} - \epsilon \frac{\partial \epsilon}{\partial \xi} \right) = F_1
\end{align*}
\]
Or written into solved form of \( \frac{\partial p}{\partial \xi}, \ldots, \frac{\partial w}{\partial \xi} \):

\[
\begin{align*}
\frac{\partial p}{\partial \xi} &= \epsilon^t [F_1 + \rho (r F_1 + \alpha F_0 + \beta F_0)] + F_0 \\
\frac{\partial p}{\partial \xi} &= \frac{1}{\epsilon^t} [F_1 + \frac{\partial p}{\partial \xi}] \\
\frac{\partial u}{\partial \xi} &= \frac{1}{\rho} [F_1 - \frac{\partial p}{\partial \xi}] \\
\frac{\partial v}{\partial \xi} &= \frac{1}{\rho} [F_1 - \frac{\partial p}{\partial \xi}] \\
\frac{\partial w}{\partial \xi} &= \frac{1}{\rho} [F_1 - \frac{\partial p}{\partial \xi}]
\end{align*}
\]

(2.3)

In the equation, \( a = u + v + w \)

\( r^t = r^t + \alpha^t + \beta^t \)

\[
\begin{align*}
F_1 &= -\epsilon \left[ \frac{\partial p}{\partial \theta} + \frac{\omega}{\sin \theta} \left( \frac{\partial u}{\partial \phi} \cos \theta + \frac{\partial v}{\partial \phi} \sin \theta \right) + \frac{1}{\rho} \frac{\partial p}{\partial \theta} \right] \\
F_1 &= -\epsilon \left[ \frac{\partial u}{\partial \theta} + \frac{\omega}{\sin \theta} \left( \frac{\partial u}{\partial \phi} \cos \theta + \frac{\partial v}{\partial \phi} \sin \theta \right) + \frac{1}{\rho} \frac{\partial p}{\partial \theta} \right] \\
F_1 &= -\epsilon \left[ \frac{\partial p}{\partial \theta} - \epsilon^t \frac{\partial p}{\partial \theta} + \frac{\omega}{\sin \theta} \left( \frac{\partial p}{\partial \phi} \cos \theta - \epsilon \frac{\partial p}{\partial \phi} \right) \right]
\end{align*}
\]

2.2 Boundary Condition

(1) Condition of shock wave On the shock wave, the shock wave relation equation

\[
\begin{align*}
\lambda + \frac{V_1^2}{2} &= \lambda_0 + \frac{V_{0s}^2}{2} \\
\rho + \frac{\rho V_1^2}{2} &= \rho_0 + \frac{\rho_0 V_{0s}^2}{2} \\
\rho &= \rho_0 \\
\rho_0 V_{0s} &= \left( 1 - \frac{\rho_0}{\rho} \right) n_s V_{0s} \\
\rho_0 V_{0s} &= \left( 1 - \frac{\rho_0}{\rho} \right) n_s V_{0s} \\
\rho_0 V_{0s} &= \left( 1 - \frac{\rho_0}{\rho} \right) n_s V_{0s}
\end{align*}
\]

(2.4)
Here the quantity indicated by an infinity mark is wave-front quantity and that not indicated by an infinity mark is wave-back quantity, $V$ is the speed projection of $\mathbf{A}$ along the direction of wave normal line, $h$ is han, $(n, n, n)$ are direction cosines respectively along the shock wave normal line, namely

$$
\begin{pmatrix}
\frac{n_1}{n_2} \\
\frac{n_3}{n_4}
\end{pmatrix} = \frac{1}{\sqrt{1 + \left(\frac{F_x}{r}\right)^2 + \left(\frac{F_y}{r \sin \theta}\right)^2}}
$$

$$
\times \begin{pmatrix}
1 \\
-\frac{F_x}{r} \\
-\frac{F_y}{r \sin \theta}
\end{pmatrix}
$$

(2) Condition of the object surface. On the surface of the object, it must satisfy the condition that the normal direction speed is zero, namely

$$
\rho = uG - \nu G_x - \omega \frac{G_x}{\sin \theta} = 0 \quad (2.5)
$$

3. Numerical Solution

In order to make numerical solution, we introduce some rays to the solution zone. For instance, at $\theta$ direction we introduce coordinate surface of $\theta = \theta_1 = \text{const}$ and at $\phi$ direction, we introduce coordinate surface of $\phi = \phi_1 = \text{const}$, then we take the intersecting lines of these coordinate surfaces as rays. For $\rho$, we use the value of "low parameter" on the ray as nodal point value to construct interpolating polynomial equation and then to
determine the partial derivative of $\theta$ & $\psi$ correspondingly. Let equation (2.3) be formulated on the ray, then we have a constant differential equation group and the problem of marginal value will correspondingly become marginal-value problem of constant differential equation group. For this reason, we change marginal-value problem into initial-value problem, and work out solution through iteration, namely we first assume that the form of shock wave has been known, and then from shock wave condition (2.4), we have the flow parameter of wave back. Taking this as initial value of integral constant differential equation group, then we check whether the flow parameter of the object surface can satisfy the condition of object surface (2.5). If not, we adjust the shape of shock wave till the condition of object surface is satisfied. The integration of constant differential equation can use general method, such as quartic-valence Runge-Kutta method. In the following, we shall describe some specific treatment.

3.1 Equation on Axis $\theta = 0$

Assuming that flow field is symmetrical with $\varphi = 0$, $\varphi$-plane and that axis $\theta = 0$ is always in a symmetrical plane. From equation (2.2), it can be seen that due to the fact that $\sin\theta$ appears in the denominator, the equation at $\theta = 0$ must be given a treatment. Let $v^* = v(\xi, 0, 0)$, clearly $v(\xi, 0, \varphi) = v^*(\xi)\cos\varphi$, $w(\xi, 0, \varphi) = -v^*(\xi)\sin\varphi$, $u(\xi, 0, \varphi) = u(\xi, 0, 0)$, $\rho(\xi, 0, \varphi) = \rho(\xi, 0, 0)$. By applying Low-bi-ta (transliteration of Chinese sound and it may be a Chinese transliteration of Robert) method to $\varphi$ which appears in equation (2.2), we can have the equation on $\theta = 0$. In principle, it will do by taking any equation from $\varphi$ surface randomly. But because the
computing error of numerical value, of different \( \varphi \), there will be different results. In order to eliminate such incongruity, we make integration of those equations of \( \varphi \) from \( 0 \) to \( \pi \) to induce the necessary equation. For instance, we use \( \cos \varphi \) to multiply the third equation of equation (2.2), and take off the fourth equation and use \( \sin \varphi \) to multiply it, then we make integration. Due to

\[
\int_0^1 \left( \frac{\partial \varphi}{\partial \xi} \cos \varphi - \frac{\partial \psi}{\partial \xi} \sin \varphi \right) \, d\varphi = \int_0^1 \left( r \xi + a \xi + b \psi \right) \frac{\partial \varphi}{\partial \xi} \, d\varphi - \frac{\partial \psi^*}{\partial \xi} \int_0^1 \left( \frac{\partial \psi}{\partial \varphi} \right) \, d\varphi = \frac{\partial \psi^*}{\partial \xi} \int_0^1 \left( \frac{\partial \psi}{\partial \varphi} \right) \, d\varphi,
\]

\[
\int_0^1 \left( \frac{\partial \varphi}{\partial \psi} \right) \, d\varphi = - \frac{\partial \psi^*}{\partial \xi} \left( \frac{\partial \psi}{\partial \varphi} \right) \int_0^1 \left( \frac{\partial \psi}{\partial \varphi} \right) \, d\varphi + \frac{\partial \psi^*}{\partial \xi} \int_0^1 \left( \frac{\partial \psi}{\partial \varphi} \right) \, d\varphi,
\]

\[
\frac{1}{\rho} \int_0^1 \left( \frac{\partial \psi^*}{\partial \varphi} \right) \, d\varphi = - \frac{\partial \psi^*}{\partial \xi} \left( \frac{\partial \psi}{\partial \varphi} \right) \int_0^1 \left( \frac{\partial \psi}{\partial \varphi} \right) \, d\varphi + \frac{\partial \psi^*}{\partial \xi} \int_0^1 \left( \frac{\partial \psi}{\partial \varphi} \right) \, d\varphi.
\]

So we can have

\[
\frac{\partial \varphi}{\partial \xi} + \frac{\partial \psi}{\partial \xi} = F_i^*.
\]

And analogously we can have

\[
\frac{\partial \psi}{\partial \xi} + \frac{\partial \varphi}{\partial \xi} = F_i^*.
\]

To write into solved form of \( \frac{\partial \psi}{\partial \xi} \), \( \cdots \), \( \frac{\partial \psi^*}{\partial \xi} \), we can have the necessary equation

\[
\begin{align*}
\frac{\partial \psi}{\partial \xi} &= c^2 \left( \frac{\partial \psi^*}{\partial \xi} - c \left( \frac{\partial \psi}{\partial \xi} + \frac{\partial \psi^*}{\partial \xi} \right) \right) + \frac{\partial \psi^*}{\partial \xi} \frac{\partial \psi}{\partial \xi} \\
\frac{\partial \psi^*}{\partial \xi} &= \frac{1}{c^2} \left( - \frac{\partial \psi}{\partial \xi} + \frac{\partial \psi^*}{\partial \xi} \right) \\
\frac{\partial \varphi}{\partial \xi} &= \frac{1}{c} \left( F_i^* - \frac{\partial \psi}{\partial \xi} \right) \\
\frac{\partial \psi}{\partial \xi} &= F_i^* - \frac{\partial \psi^*}{\partial \xi} \frac{\partial \psi}{\partial \xi} \\
\frac{\partial \psi^*}{\partial \xi} &= \frac{1}{c} \left( F_i^* - \frac{\partial \psi}{\partial \xi} \right) \\
\frac{\partial \psi}{\partial \xi} &= \frac{1}{c} \left( F_i^* - \frac{\partial \psi^*}{\partial \xi} \right)
\end{align*}
\]

(2.6)
In it,

\[ a^* = \frac{2}{\pi} \int u \cos \varphi d\varphi \]

\[ e^* = ru + a^* \rho \]

\[ r^* = r' + a^* \rho \]

\[ F_i^* = -\frac{2 \varphi}{\pi} \left( \int \varphi \left( \frac{\partial \rho}{\partial \theta} \cos \varphi d\varphi + \rho \left( \frac{\partial \rho}{\partial \varphi} d\varphi + \rho \sin \varphi \cos \varphi \right) + \frac{1}{\rho} \left( \frac{\partial \rho}{\partial \theta} \cos \varphi \right) d\varphi + \frac{\pi}{2} \nu \right) \]

3.2 Interpolating Multinomial Equation

Because the flow field is assumed to be symmetrical with \( \varphi = 0 \), \( \pi \) plane, it is only necessary to have solution between \( 0 \leq \varphi \leq \pi \). Between \( 0 - \pi \), we introduce \( k + 1 \) planes. And at the same time, we make \( n + 1 \) conical surfaces, \( \theta = \theta_i = \cos (\theta, = 0), k = 0, 1, \ldots, n \). They intersect with half plane \( \varphi = \varphi \), and \( \varphi = \varphi + \pi \) to form \( (2n + 1) \) rays. Noticing that the flow parameter on the flow symmetry, \( \varphi = -\varphi \), and the flow parameter on \( \varphi = \varphi + \pi \) are equal or different by one symbol, for the fixed \( \varphi \), we can utilize the value of \( 2n + 1 \) rays on \( \varphi = \varphi \) & \( \varphi = -\varphi \), to construct 2nth order interpolating multinomial equation of \( \theta \).

\[ \xi = \sum_{i=0}^{2n} a_i \theta^i \]  

(2.7)

\( g \) indicates flow parameter. For the purpose of saving time in the process of computing, we do not first compute coefficient \( a_i \), but use the following computing methods instead. Because interpolating function and its derivative
can be expressed as a linear combination of function values on interpolating nodal point, and the linear combination coefficient is only related with the position of interpolating nodal point and the position of interpolating point, so when the nodal point and interpolating point are given, these coefficients can be determined. When the function of each point and the derivative value are computed, it will do to use these coefficients and the function value on nodal point to make point product. Taking equation (2.7) as example. If nodal point is $\theta_m (m = 0, 1, \ldots, 2n)$, $g(\theta)$ at $\theta$ of some interpolating point will be computed. Because there is condition at nodal point,

$$\sum_{i=0}^{n} a_i \theta_i = g_i \quad (m = 0, 1, \ldots, 2n)$$

$g_i = g(\theta_m)$. or written into matrix form:

$$Ma = g$$

Here

$$M = \begin{pmatrix}
1 & \theta_0 & \theta_1 & \cdots & \theta_{2n} \\
1 & \theta_0 & \theta_1 & \cdots & \theta_{2n} \\
1 & \theta_0 & \theta_1 & \cdots & \theta_{2n} \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
1 & \theta_0 & \theta_1 & \cdots & \theta_{2n}
\end{pmatrix}$$

$$a = \begin{pmatrix} a_0 \\ a_1 \\ \vdots \\ a_{2n} \end{pmatrix} \quad g = \begin{pmatrix} g_0 \\ g_1 \\ \vdots \\ g_{2n} \end{pmatrix}$$

Therefore we have

$$a = M^{-1}g$$

Then we can rewrite the equation of $g(\theta)$,

$$g(\theta) = d^T \cdot a$$
Into

\[ g(\theta) = d^* \cdot (M^{-1} g) \]
\[ = (M^{-1} d)^* \cdot g \]
\[ = b^* \cdot g \quad (2.8) \]

Here \( b = M^{-1} d, \) \( d^* = (1, \theta, \cdots, \theta^m). \) Evidently, when nodal point and interpolating point are given, \( M^* \) and \( d \) can be determined, and then we can have \( b. \) Similarly because,

\[ g'(\theta) = \sum_{i=0}^{n-1} a_i(\eta)^{-i} \]
\[ = d^* \cdot a \]
\[ = (M^* - d_i)^* \cdot g \]

Here \( d^*_i = (0, 1, \theta, \cdots, 2\theta^{m-1}) \) represents derivative of \( \theta, \) so to compute derivative can be of analogous treatment.

So far as \( \varphi \) is concerned, when \( \theta \) is fixed, we can utilize the value at its intersecting line with \( k + 1 \) planes to construct trigonometric interpolating multinomial equation of \( \varphi. \) In computing, the method mentioned above can also be used. For even function, we take,

\[ g = \sum_{i=0}^{n} a_i \cos \varphi \]

Then

\[ g' = (M^* - d_i)^* \cdot g \]

Now there is

\[ M^* = \begin{pmatrix} 1 & 1 & \cdots & 1 \\ \cos \varphi_0 & \cos \varphi_1 & \cdots & \cos \varphi_k \\ \vdots & \vdots & \cdots & \vdots \\ \cos^k \varphi_0 & \cos^k \varphi_1 & \cdots & \cos^k \varphi_k \end{pmatrix} \]
\[ d^*_i = (0, -\sin \varphi, \cdots, -k \sin \varphi \cos^{k-1} \varphi) \]
\[ g^* = (s_0, s_1, \cdots, s_k) \]

10
For \( \frac{1}{\pi} \int_{-\pi}^{\pi} \frac{1}{2} g \cos \varphi \, d\varphi \), similar expression can also be written. It is not necessary to exemplify them here. For odd function, we take,
\[
g = \sum_{n=0}^{L-1} s_n \cos \varphi \sin \varphi
\]
Then
\[
g' = (M^{-1}d')^*g
\]
Now
\[
M^* = \begin{pmatrix}
\sin \varphi_1 & \sin \varphi_2 & \cdots & \sin \varphi_{L-1} \\
\sin \varphi_1 \cos \varphi_1 & \cdots & \cdots & \\
\vdots & \ddots & \ddots & \\
\sin \varphi_{L-1} \cos \varphi_{L-1} & \sin \varphi_{L-1} \cos \varphi_{L-1} & \cdots & \sin \varphi_{L-1} \cos \varphi_{L-1}
\end{pmatrix}
\]
\[
d^* = (\cos \varphi, \sin \varphi + \cos \varphi, \ldots, (k-2)\cos^{k-1} \varphi \sin \varphi + \cos^k \varphi)
\]

In addition to the methods mentioned above, we also use the following methods to construct interpolating multinomial equations. For even function of \( \varphi \), we take
\[
g(\xi) = \sum_{i=0}^{L} \sum_{r=0}^{i} g_{i,r}(\xi) \cos^r \varphi
\]
For odd function, we take
\[
w(\xi) = \left( \sum_{i=0}^{L} \sum_{r=0}^{i} w_{i,r}(\xi) \cos^r \varphi \right) \sin \varphi
\]
In order to make the function and the derivative of \( \varphi \) at \( \theta = 0 \) in some sense be single value, some proper condition must be added to the multinomial equation. Now we try to describe such conditions.

For instance, for shock wave form, \( r = F(\theta, \varphi) \), we naturally require, when \( \theta = 0 \), it has no relationship with \( \varphi \). This means that we require when \( j = 0 \), \( F_\theta = 0 \). And at the same time, in order to warrant that the normal...
line has definite direction and when \( \theta = 0 \), the normal line direction spherical coordinate should have such a form: \((a, b \cos \varphi, -b \sin \varphi)\) and in it \(a\) and \(b\) are constants. This means to require \(F_i = 0 (i \neq 1)\). So for \(F\), the multinomial equation should be:

\[
F(\theta, \varphi) = F_0 + F_1 \theta \cos \varphi + \sum_{i=1}^{\infty} \sum_{j=0}^{i} F_{ij} \theta^i \cos \varphi
\]

(2.9)

Obviously, \(u, v,\) and \(p\) should also have the same form as \(F\). The above conclusion and the form of \(v\) and \(w\) can be obtained as well in the following way. Let

\[
\begin{align*}
g &= g_0(\xi) + \sum_{i=1}^{\infty} \sum_{j=0}^{i} g_{ij}(\xi) \theta^j \cos \varphi \\
v &= v_0(\xi) \cos \varphi + \sum_{i=1}^{\infty} \sum_{j=0}^{i} v_{ij}(\xi) \theta^j \cos \varphi \\
w &= -v_0(\xi) \sin \varphi + \left(\sum_{i=1}^{\infty} \sum_{j=0}^{i} v_{ij}(\xi) \theta^j \cos \varphi\right) \sin \varphi
\end{align*}
\]

Here \(g\) can be used to express \(p, \rho, u, F,\) and utilizes the property \(v(\xi, 0, \varphi) = \lambda \cos \varphi,\) \(w(\xi, 0, \varphi) = -\lambda \sin \varphi,\) then there is \(v_0 = 0 (i \neq 1), w_0 = 0 (i \neq 0),\) \(v_0 = -w_0.\)

To combine the above equation with equation (2.2), we notice that,

\[
\begin{align*}
\frac{\partial}{\partial \theta} G(0, \varphi) &= G_0(0, 0) \cos \varphi, \\
\frac{G_0}{\sin \theta} \Big|_{\theta=0} &= -G_0(0, 0) \sin \varphi
\end{align*}
\]

(Here the object body is symmetrical with \(\varphi = 0, =\) surface), so when \(\theta \to 0,\) we have

\[
\begin{align*}
s \frac{dp_0}{d\xi} + r_0 \rho_0 \frac{du_0}{d\xi} - \rho_0 \left( G_0 + \xi (F_1 - G_1) \right) \frac{du}{d\xi} &= \lim_{\theta \to 0} F_i \\
s \frac{du_0}{d\xi} + \frac{F_1}{\rho_0} \frac{d\rho_0}{d\xi} &= \lim_{\theta \to 0} F_i
\end{align*}
\]

12
\[
\begin{align*}
\left( a_0 \frac{d\rho}{d\xi} - \frac{G_m + \xi(F_{11} - G_0)}{\rho_0} \frac{d\rho}{d\xi} \right) \cos \varphi &= \lim_{\delta \to 0} F_3 \\
- \left( a_0 \frac{d\rho}{d\xi} - \frac{G_m + \xi(F_{11} - G_0)}{\rho_0} \frac{d\rho}{d\xi} \right) \sin \varphi &= \lim_{\delta \to 0} F_4 \\
a_0 \left( \frac{d\rho}{d\xi} - c_1 \frac{d\rho}{d\xi} \right) &= \lim_{\delta \to 0} F_5,
\end{align*}
\]

In it
\[
\begin{align*}
a_0 &= u_m r_o - r_u [G_m + \xi(F_{11} - G_0)] \\
r_o &= G(0, 0) + \xi[F_m - G(0, 0)] \\
G_m &= \frac{\partial}{\partial \theta} G(0, 0) \\
c_1 &= \frac{TP_m}{\rho_0}
\end{align*}
\]

To write the right end of the above equation into multinomial equation of \( \cos \varphi \) (or, in addition, to multiply it by \( \sin \varphi \)), and to use the linear independence of \( 1, \cos \varphi, \ldots, \cos^n \varphi \), we can reason out that \( g \) should have the form of equation (2.9) and \( v \) and \( w \) should take

\[
v = v_u \cos \varphi + v_\theta \theta + \sum_{i=1}^n \sum_{j=0}^n v_{i,j} \cos^i \varphi \\
w = -v_{\theta} \sin \varphi - v_\theta \theta \cos \varphi \sin \varphi + \left( \sum_{i=1}^n \sum_{j=0}^n w_{i,j} \cos^i \varphi \right) \sin \varphi
\]

At the same time, we have equation on \( \theta = 0 \):

\[
\begin{align*}
a_0 \frac{d\rho}{d\xi} + r_0 \rho_0 \frac{d\rho_0}{d\xi} - \rho_0 [G_m + \xi(F_{11} - G_0)] &\frac{d\rho}{d\xi} \\
- (F_m - G(0, 0)) &\left[ \nu_o (v_{11} + \nu_m) + \rho_0 (v_{11} + 2v_{10} + 2u_m) \right] \\
&\left( \frac{d\rho}{d\xi} - \frac{G_m + \xi(F_{11} - G_0)}{\rho_0} \frac{d\rho}{d\xi} \right) \\
&\left( F_m - G(0, 0) \right) \left[ \nu_m (v_{10} + v_{11} + u_m) + \rho_0 \right] \\
a_0 \left( \frac{d\rho}{d\xi} - c_1 \frac{d\rho}{d\xi} \right) &= \left( F_m - G(0, 0) \right) \nu_m \left( \rho_0 - \frac{TP_m}{\rho_0} \nu_m \right)
\end{align*}
\]
3.3 Iteration Method

As what has been stated at the beginning of this section, we shall try to solve the problem of marginal value through iteration. In fact, it can be interpreted as a problem of solving a transcendental equation group. That is to select one group of \( F \) (to indicate the shock wave form on \( i \)th ray).

To make,

\[
q_i(F_1, \ldots, F_m) = 0 \quad (i = 1, 2, \ldots, m)
\]

Here \( q = 0 \) is the boundary condition (2.5). We use Newton method, namely to use alteration quantity \( \delta F \) of \( F_i \) to satisfy the following equation:

\[
\sum_{i=0}^{m} \frac{\partial q_i}{\partial F_j} \delta F_j = -q_i \quad (i = 1, \ldots, m)
\]

Usually there is no way to express derivative \( \frac{\partial q_i}{\partial F_j} \) by using analytic equation, so we use numerical value method, namely

\[
\frac{\partial q_i}{\partial F_j} = \frac{q_i(F_1, \ldots, F_m, F_j + \Delta F_j, F_{j+1}, \ldots, F_m) - q_i(F_1, \ldots, F_m)}{\Delta F_j}
\]

By using this method, it needs \( m + 1 \) times of integration for each iteration, so it consumes a great deal of machine time. For the purpose of saving time, we can use the simplified Newton method, but because of the lack of accuracy in most of \( \frac{\partial q_i}{\partial F_j} \), the speed of convergence, therefore, can possibly become slow. In order to make \( \frac{\partial q_i}{\partial F_j} \) more accurate without increasing much of the volume of computation, we suggest a method as follows. Let \( Q \) indicate the vector constructed from \( q_1, \ldots, q_m \) and \( R \) the vector constructed from \( F_1, \ldots, F_m \). \( q' \) of \( Q \) with respect to \( R \). If \( Q(R_0) = Q_0 \) and at other \( m \)-point of \( R_1, \ldots, R_m \) close to \( R_0 \), \( Q(R_i) = Q_i (i = 1, \ldots, m) \) has been known, and if \( R_0 - R_i (i = 1, 2, \ldots, m) \) is linear independent, then \( Q' \) can be decided.
approximately by $R_i$ and $Q_i$. In fact, because

$$Q_i \approx Q_i + Q_i'(R_i - R_i) \quad (i = 1, 2, \ldots, m)$$

So there is

$$(Q_1 - Q_1, \ldots, Q_m - Q_m) \approx Q_i'(R_i - R_i, \ldots, R_m - R_m)$$

and then there is

$$Q_i = (Q_1 - Q_1, \ldots, Q_m - Q_m)(R_1 - R_i, \ldots, R_m - R_i)^{-1}$$

thus we can have an iteration formula

$$R_{n+1} = R_n - \left( R_{n-1} - R_n, \ldots, R_n - R_n \times Q_{n-1} - Q_n, \ldots, Q_{n+1} - Q_n \right) Q_n$$

$$n = m + 1, \ldots$$

(2.11)

Evidently, using the above equation to make iteration and begin with $R_1, \ldots, R_{m+1}$ to solve $Q_1, \ldots, Q_{m+1}$ needs $m + 1$ times of integration. But thereafter, one iteration needs only one time of integration.

Now we try to make a simple estimation of the speed of convergence.

Obviously, when

$$\bar{R}_{m+1} = (R_1 - R_{m+1}, \ldots, R_m - R_{m+1}) = \Delta F \cdot E$$

equation (2.11) becomes difference half Newton formula. Here $E$ is unit matrix and $\Delta F$ is pure quantity. Because now there is,

$$\bar{Q}_{m+1} = (Q_1 - Q_{m+1}, \ldots, Q_m - Q_{m+1}) = Q_{m+1} \bar{R}_{m+1} + o(\Delta F')$$

Then there is

$$\bar{Q}_{m+1} = \bar{R}_{m+1} \bar{Q}_{m+1} + o(\Delta F') \bar{Q}_{m+1} = \bar{R}_{m+1} \bar{Q}_{m+1} + o(\Delta F)$$

And thereupon we can have an estimation equation for difference half Newton formula.

$$R^* - R_{m+1} = R^* - R_{m+1} + \bar{R}_{m+1} \bar{Q}_{m+1}$$

$$- R^* - R_{m+1} + Q_{m+1} \bar{Q}_{m+1} + (\bar{R}_{m+1} \bar{Q}_{m+1} - Q_{m+1}) \bar{Q}_{m+1}$$

$$= o(||R^* - R_{m+1}||^2) + o(\Delta F ||Q_{m+1}||)$$

or written into

$$||R^* - R_n|| \leq A ||R^* - R_{m+1}|| + B \Delta F ||Q_{m+1}|| (n = 1, 2, \ldots)$$

15
Here $R^*$ is true solution, $\| \|$ indicates mode, and $A$ and $B$ are suitable constants. Similarly, for difference simplified Newton method, there is an estimation equation,

$$
\|R^* - R_n\| \leq A\|R^* - R_{n-1}\| + B\Delta F\|Q_{n-1}\| + C\|R_{n+1} - R_{n-1}\|\|Q_{n-1}\|
$$

($n = m + 2, \ldots$)

For the method suggested by us there is an estimation equation,

$$
\|R^* - R_n\| \leq A\|R^* - R_{n-1}\| + D\|Q^*_{n-1}\| \sup_{1 \leq i \leq n} \|R_{n-1} - R_{n-1-i}\|\|Q_{n-1}\|
$$

Here $A$, $B$, $C$, and $D$ are constants.

It is easy to see that when $\Delta F$ & $\|R^* - R_{n-1}\|$ are of same quantity level or smaller, difference Newton method basically maintains the speed of convergence of Newton method. But $\|R_{n+1} - R_{n-1}\|$ is generally increased as $n$ is increased, so of simplified Newton method the speed of convergence is slow. Because $\|Q^*_{n-1}\| \sup_{1 \leq i \leq n} \|R_{n-1} - R_{n-1-i}\| = o(1)$, and $\sup_{1 \leq i \leq n} \|R_{n-1} - R_{n-1-i}\|$ is reduced as $n$ is increased, so the method suggested by us can possibly converge faster than simplified Newton method. This has been proved in practical computation.

3.4 Selection of Initial Shock Wave and Interpolation of Object Surface Quantity

When the methods mentioned above are used to make iteration, the success in computing will depend on how well the selection of initial shock wave is made. For this reason, we use the ready results according to the way of some parameter gradual transition. For instance, when we want to compute
the flow result under certain attack angle \( \eta \), we select attack angle \( \eta \) as parameter. After the result of \( \eta \) has been obtained (for example \( \eta_0 = 0^\circ \)), the result can be used as initial value to compute \( \eta + \Delta \eta \). After we have had the result of \( \eta + \Delta \eta \), we use the results of \( \eta, \eta + \Delta \eta \) to obtain initial value of \( \eta_0 + 2\Delta \eta \) by way of linear interpolation. In the same fashion, till we have the result of \( \eta^* \). As for the initial shock wave form which is needed in the beginning of computing, it can be secured by utilizing the result available currently.

From equation (2.3), it can be understood that on the object surface \( a = 0 \), so integration cannot reach the object surface. In order to have the quantity of object surface, we use extrapolation method. When integration reaches a certain \( \xi^* \) (for example \( \xi^* = 0.1 \)), then we use the \( \xi \) values of a few neighbouring points to extrapolate the object surface quantity for example using the values of \( \xi = 0.3, 0.2, 0.1 \) makes a quadratic interpolation. Here we would like to make a random suggestion that if the other computing form, such as implicit form integration, extrapolation can be completely avoided. For a situation of axial symmetry, we designed another form to compute, and the result proves that it is a success. Here we have no plan to give its details.

4. Computation Results

We have made broad computation on blunt-nosed body, axial symmetry and three-dimension space encircling flows by using the methods mentioned above. The object forms we computed include ellipsoid of various axial ratio and objects analogous to disk (object expressed by equation \( z^* + (x^* + y^*)^2 = 1 \),
The range of incoming flow $M$ is $1.5 \leq M < \infty$. For the situation of axial symmetry, besides the frozen gas of $\gamma = 1.4$, we compute the balanced air as well as the unbalanced. The method we used is borrowed from article 12 in the bibliography appended to this article. The patterns of unbalanced air are presented in another article of ours. The precision of our computation results have been checked by several different ways. One of the checks is made in computing as it is in process. For instance, we use different number of rays and different integral step length to check the relations which should be satisfied by flow field, such as maintaining constancy. Another way is to compare with other results acquired from experiments and other methods, such as integral relation method. All the checks we made indicate that the precision of our computation results is satisfactory. In the following, we shall present a part of our computation results.

Figure 1 illustrates the forms of shock wave and sonic line of frozen gas spherical flow under different $M_0$ number. From the Figure, it can be understood that the forms of sonic line are of two different types. When $M > 3$, the limit characteristic line is the second family characteristic line that can reach sonic flow.
point of the object surface. But when $M = 3$, the limit characteristic line is composed of the first family characteristic line (which comes from object surface) in contact with sonic line and the second family characteristic line (which comes from shock wave).

![Figure 2](image-url)

**Figure 2** Distribution of pressure along object surface

Figure 2 shows the distribution of object surface pressure of frozen gas spherical flow.

![Figure 3](image-url)

**Figure 3** Shock wave position and sonic line form ($M = 3$)

Figure 3 illustrates $M = 3, \gamma = 1.4$, the shock wave form and sonic line position of different objects. For very blunt body, if $n > 20$, shock wave position will basically maintain unchanged. After the contraction of the curvature radius of object surface adjacent to sonic point, for solid $M$ number, beginning with a certain curvature, there will be torsional point on the sonic line.

Figure 4 shows shock wave position and sonic line form of balanced air
spherical flow. The conditions of incoming flow are $M = 4$, $\rho = 0.87 \times 10^5$ dyne/cm$^2$, $\rho = 0.95 \times 10^{-4}$ g/cm$^3$, for $M = 20$, $\rho = 0.122 \times 10^5$ dyne/cm$^2$, $\rho = 0.192 \times 10^{-3}$ g/cm$^3$. From the Figure, it can be seen that ionization makes the situation of shock wave position and sonic line with frozen gas of $\gamma = 1.4$ change remarkably. Shock wave moves much closer to the object.
Figure 5 shows shock wave position and sonic line formation of unbalanced air spherical flow. The conditions of incoming flow are \( \rho = 0.947 \times 10^1 \) dyne/cm², \( \rho = 0.123 \times 10^{-1} \) cm³, \( R = 5 \) cm. What is worth of attention is the special form of \( M = 20 \) sonic line at the place of shock wave.

Figure 6 shows the relationship between the detachment distance of stationary point and \( M \)-number. For frozen flow, when \( M > 10 \), it remains unchanged. For balanced air, following the increase of \( M \), the change of detachment distance appears to be not unique.

Using 5 rays to compute encircling flow of axial symmetry.

Figure 7 shows that of the ellipsoidal flow of \( \theta = 1.5 \) when \( M = 3 \) & 4, shock wave and sonic line in symmetrical plane will follow the change of attack angle \( \phi \). Figure 9 shows that the object surface pressure in symmetrical plane will follow the change of attack angle. Also Figure 7 shows position of stationary point and, in accuracy, stationary angles of \( M = 3 \) & \( M = 4 \) are overlapping. When attack angle is changing, it moves along object surface by almost the same speed. Figure 8 shows that shock wave and sonic line in \( \phi = \pi /2 \) plane follow the change of attack angle. In the Figure, it can be seen that the change of shock wave form is slow and the change of sonic line is faster.

Figure 10 shows the encircling flow of disk-analogue object of
Figure 7 Shock wave form and sonic line in symmetrical plane following the change of attack angle ($\delta = 1.5$)

1. sonic line, 2. shock wave, 3. direction of incoming flow, 4. stationary point, 5. result from article 12)

When we compute space encircling flow, we take four $\psi$ surfaces and from each $\psi$ surface we take 4 rays. Because the axis line is common, we take 13 rays altogether. The z axis of coordinate system is placed in the symmetrical plane of flow field, and, for the convenience of computing, we

$M = 5.8$, $\alpha = 20$ and shock wave form and sonic line position on symmetric plane under different attack angle.

Figure 11 shows the distribution of object surface pressure in symmetric plane.
let it make an attack angle with angle $\beta = (0.5 - 0.6) \eta, \eta$ of the object symmetrical axis.

Figure 9 Object surface pressure in symmetrical plane following the change of attack angle ($\beta = 1.5\degree$) result from article 12

Figure 10 Shock wave form and sonic line position on symmetrical surface ($M_0 = 5.8, \eta = 20\degree$)

Figure 11 The distribution of object surface pressure in symmetrical surface ($M_0 = 5.8, \eta = 20\degree$)

About the problem of whether the greatest entropy value on object
surface can be reached, from our experience of computing, we think that for a certain object in a certain error range, the greatest entropy can be reached.

In order to check our computation results, we use several different kinds of ways. For instance, for axial symmetrical enswirling flow, we use 5 rays and 3 rays respectively to compute and the result shows that error is no more than 1%. We also use different integral step length, for example, for spherical flow of $M_e = 6, \gamma = 1.4$, from shock wave to object surface we integrate 10-step, 20-step and 50-step. The relative error of 10-step and 20-step is no more than 0.3%, and between the results of 20-step and 80-step there are at least three same effective digits. This means that we do not have to worry about the increase of roundoff error.

We compare the results of $M_e = 3, \delta = 1.5, \eta = 15^\circ$ with those of Telenin[16] they are completely identical as showed in Figure 1. For ellipsoidal and spherical frozen flow of $\delta = 1.5$, our computation results have three coincide effective digits with the results Belotserkovskiy obtained by using integral relation method.

We also made integration check and examine the accuracy of integral equations

$$
\int \int \rho u \cdot da = 0
$$

$$
\int \int \mu u \cdot da + \int \int \rho x \cdot da = 0
$$

24
Here \( x_i \) indicates three axial unit vectors under rectangular coordinate, \( u \) is the projection of velocity vector \( u \) at three directions, \( \sigma \) is a curved surface containing no shock wave. Under the condition of \( M = 4, \beta = 1.5, \) and \( \gamma = 10^\circ, 20^\circ \), the integration result can be found in Table 1. Besides the total integration, Table 1 also shows the integration on shock wave, object surface and conical surface. From Table 1, it can be seen that the computation results are accurate, and there is error only at the third digit of the integration on shock wave and conical surface. The object surface condition is well satisfied and it is at \( 10^{-4} \) numerical level.

In addition, we also compute the total energy on all nodal points and

\[
(i = 1, 2, 3)
\]

\[
\int \rho \phi^i \rho u_i \, d\sigma = 0
\]
and entropy of each nodal point on object surface. From Table 2, it can be seen that for \( M_\infty = 4, \delta = 1.5, \eta \leq 15^\circ \), the relative error of total energy is less than 1%. From Table 3, it can be seen that for \( M_\infty = 4, \delta = 1.5, \eta \leq 15^\circ \), the entropy of object surface is different only by 1 at the third effective digit, and for \( \eta = 20^\circ \), there is only a difference by 3 at the third digit.

In summary, using method of lines to compute encircling flow of smooth bodies can produce very satisfactory results.

Comrades Rui Wei-ming participated in part of this work, He Jiao-min gave us significant help, and Feng Kang once enthusiastically led us to work on this project. Here we thank them all.
Bibliography


DISTRIBUTION LIST
DISTRIBUTION DIRECT TO RECIPIENT

<table>
<thead>
<tr>
<th>ORGANIZATION</th>
<th>MICROFICHE</th>
<th>ORGANIZATION</th>
<th>MICROFICHE</th>
</tr>
</thead>
<tbody>
<tr>
<td>A205 DMA TC</td>
<td>1</td>
<td>E053 AF/INAKA</td>
<td>1</td>
</tr>
<tr>
<td>A210 DMA AC</td>
<td>2</td>
<td>E017 AF/RDXTR-W</td>
<td>1</td>
</tr>
<tr>
<td>B344 DIA/RDS-3C</td>
<td>9</td>
<td>E403 AFSC/INA</td>
<td>1</td>
</tr>
<tr>
<td>C043 USAMIAA</td>
<td>1</td>
<td>E404 AEDC</td>
<td>1</td>
</tr>
<tr>
<td>C509 BALLISTIC RES LABS</td>
<td>1</td>
<td>E408 AFWL</td>
<td>1</td>
</tr>
<tr>
<td>C510 AIR MOBILITY R&amp;D LAB/FIO</td>
<td>1</td>
<td>E410 ADTC</td>
<td>1</td>
</tr>
<tr>
<td>C513 PICATINNY ARSENAL</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>C535 AVIATION SYS COMD</td>
<td>1</td>
<td>CCN</td>
<td>1</td>
</tr>
<tr>
<td>C591 FSTC</td>
<td>5</td>
<td>ASD/FTD/NIIS</td>
<td>3</td>
</tr>
<tr>
<td>C619 MIA REDSTONE</td>
<td>1</td>
<td>NIA/PHS</td>
<td>1</td>
</tr>
<tr>
<td>D008 NISC</td>
<td>1</td>
<td>NIIS</td>
<td>2</td>
</tr>
<tr>
<td>H300 USAICE (USAREUR)</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>P005 DOP</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>P050 CIA/CRB/ADG/SD</td>
<td>2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>NAVORDSTA (50L)</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>NASA/NST-44</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>AFIT/LD</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>LLL/Code 1-389</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>NSA/1213/TDL</td>
<td>2</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

FTD-TD(RS)T-0645-79